

## SMITHSONIAN MATHEMATICAL TABLES

## HYPERBOLIC FUNCTIONS

PREPARED BY

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## ADVERTISEMENT.

Among the early publications of the Smithsonian Institution was a very important volume of meteorological tables by Dr. Arnold Guyot. They were so widely used by geographers and physicists as well as by meteorologists that when the fourth edition was exhausted it was decided to recast the entire work and publish three separate volumes, Meteorological Tables, Geographical Tables, and Physical Tables, each of which has now passed through several editions.

In the application of the data of these volumes to the study of natural phenomena certain mathematical tables beside those included in ordinary tables of logarithms are urgently needed in order to save recurrent computation on the part of observers and investigators. It was therefore decided to publish the present volume of Mathematical Tables, on Hyperbolic Functions.

Hyperbolic Functions are extremely useful in every branch of pure physics and in the applications of physics whether to observational and experimental sciences or to technology. Thus whenever an entity (such as light, velocity, electricity, or radioactivity) is subject to gradual extinction or absorption, the decay is represented by some form of Hyperbolic Functions. Mercator's projection is likewise computed by Hyperbolic Functions. Whenever mechanical strains are regarded as great enough to be measured they are most simply expressed in terms of Hyperbolic Functions. Hence geological deformations invariably lead to such expression, and it is for that reason that Messrs. Becker and Van Orstrand, who are in charge of the physical work of the United States Geological Survey, have been led to prepare this volume.

## Charles D.- Walcott, Secretary.

Washington, D. C., April, 1909.

In this first reprint of the Hyperbolic Functions a few misprints of trifling importance have been corrected and four values of the exponential have been changed by a unit in the eighth significant place.
April, igir.
C. D. W.

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## DEFINITIONS AND FORMULAS.

The hyperbolic functions are named the hyperbolic sine, cosine, tangent, cotangent, secant, and cosecant from their close analogy to the circular functions, the tangent being the ratio of the hyperbolic sine to the cosine and the other three functions being reciprocals of these, as in circular trigonometry. They are usually denoted by adding $h$ to the symbols of the circular functions, as $\cosh u$ for the hyperbolic cosine of $u$, $\sinh u$ for the hyperbolic sine of $u$, etc. ${ }^{1}$

Historically speaking, the hyperbolic functions were evolved from studies of the hyperbola. They might have been developed from the geometry of the ellipse or the catenary or that of other curves. These functions, however, may be considered independently of any geometrical interpretation and can be derived from very fundamental functional theorems.

At least two methods have been devised of defining circular and hyperbolic functions analytically. One of these is due to Mr. Yvon Villarceau, ${ }^{2}$ and is so extremely brief that it can be given here in a somewhat modified form.

It has long been known that

$$
e^{2 m i \pi}=\mathrm{I} ; e^{u+2 m i \pi}=e^{u} ; e^{(u+2 m \pi) i}=e^{i u} .
$$

The second of these equations has a single imaginary period, $2 i \pi$, and the third a single real period, $2 \pi$. Hence every exponential $e^{u}$ in which $u$ is real has a single imaginary period, $2 i \pi$, and every exponential with the same base, but with an imaginary exponent, has a real period, $2 \pi$. Now, all real purely circular functions may be expressed in terms of constants and exponentials with purely imaginary exponents, and all real hyperbolic functions may be expressed in terms of constants and exponentials with exclusively real exponents.

Hence hyperbolic functions may be defined as the singly periodic exponential functions with real exponents. The circular functions are then the singly periodic exponential functions with imaginary exponents.

It remains to be considered how, from this point of view, the hyperbolic functions of complex variables are to be regarded. The question almost answers itself ; for

$$
e^{x+i y}=e^{x} \cdot e^{i y}
$$

[^0]which is evidently the product of two functions-one circular, the other hyperbolic. Such functions have a real period and an imaginary one, but since they are single-valued they are not elliptic functions.

The circular and hyperbolic functions being defined as above, it is merely as a matter of convenience that a few of the simpler combinations of exponentials receive special names, as sine, cosine, etc.

The other analytical method of generalizing the two classes of functions is due to Edward Lucas, ${ }^{1}$ and is too long to be given here in full, but the method may be indicated. If $a$ and $b$ are the two roots of the equation

$$
x^{2}-P x+Q=0,
$$

where $P$ and $Q$ are positive or negative whole numbers, then two functions may be defined as follows:

$$
U_{n} \equiv \frac{a^{n}-b^{n}}{a-b} ; V_{n} \equiv a^{n}+b^{n},
$$

and these functions are related by the equation

$$
U_{2 n}=U_{n} V_{n} .
$$

Lucas develops and studies these functions, limiting $n$ at first to whole positive numbers. He finds that all the theorems resulting from this study are converted into those of ordinary trigonometry when $U$ is replaced by $2 \sin n$ and $V$ by $2 \cos n$. He infers that between the limits I and minus $\mathrm{I}, n$ may be replaced by any real value, and shows that the theorems dealing with $U$ and $V$ when translated into trigonometric formulas on this assumption can be verified. By substituting for $n$ an imaginary argument, the hyperbolic functions also are found to be comprehended in the general functions $U$ and $V$.

Both the circular and hyperbolic functions may further be regarded as integrals of the equation

$$
\frac{d}{d x} \log \frac{d^{2} y}{d x^{2}}=\frac{d}{d x} \log y, \text { or } \frac{d^{2} y}{d x^{2}}=c y .
$$

If $c=a^{2}$, this gives

$$
\frac{y}{a}=A e^{x}+B e^{-x},
$$

where $A$ and $B$ are arbitrary constants ; so that the integral expression includes $\sinh x, \cosh x$, and the sum or difference of these functions.

If $c=-b^{2}$.

$$
\frac{y}{b}=A_{1} \cos x+B_{1} \sin x
$$

${ }^{1}$ Am. Jour. of Math., vol. I, 1878, p. 184.
and $P C^{\prime}$, may be drawn from a point $P$ to a line $A B$; the sum of the angles of a triangle is less than two right angles, and the angle of parallelism II ( $p$ ) is dependent upon the perpendicular distance $p$ of the point $P$ from the line $A B$. If now any line passing through $A$, such as $A E$, is extended until the perpendicular erected at its middle point is parallel to $A B$, the locus of the points $E$ is a boundary curve, and the revolution of this curve about $A B$ or one of its parallels develops a boundary surface. It is upon this surface of constant negative curvature that Lobachevsky imagines a triangle of sides $a, b, c$ and angles $A, B, C$ to be drawn. He establishes as fundamental relations between the sides and angles of this triangle ${ }^{1}$

$$
\begin{aligned}
& \sin A \tan \Pi(a)=\sin B \tan \Pi(b)=\sin C \tan \Pi(c), \\
& \sin \Pi(b) \sin \Pi(c)=\sin \Pi(a)-\cos \Pi(b) \cos \Pi(c) \sin \Pi(a) \cos A, \\
& \sin \Pi(a) \cos A=-\cos B \cos C \sin \Pi(a)+\sin B \sin C
\end{aligned}
$$

and also proves that

$$
\begin{aligned}
& \sin I(u)=(\cos i u)^{-1}=(\cosh u)^{-1} \\
& \tan I(u)=i(\sin i u)^{-1}=(\sinh u)^{-1}, \\
& \cos I I(u)=-i \tan i u=\tanh u .
\end{aligned}
$$

Hence the preceding equations may be written

$$
\begin{aligned}
& \frac{\sin A}{\sinh a}=\frac{\sin B}{\sinh b}=\frac{\sin C}{\sinh c}, \\
& \cosh a=\cosh b \cosh c-\sinh b \sinh c \cos A, \\
& \cos A=-\cos B \cos C+\sin B \sin C \cosh a .
\end{aligned}
$$

These formulas are, in fact, precisely those of spherical trigonometry, in which the real sides $a, b, c$ have been replaced by the imaginaries $i a, i b, i c$. If the triangle on the boundary surface is infinitesimal, the above equations reduce to the well-known relations between the sides and angles of a triangle on the Euclidean plane. The theorems of non-Euclidean geometry may not therefore be inconsistent with experience, for the largest triangle which we can measure is infinitesimal in comparison with a triangle on the boundary surface. Lobachevsky pointed out that a triangle on a boundary surface would correspond to a triangle connecting three stars in distant parts of the universe, and that the postulates of his geometry, involving as they do the question of the curvature of space, would be capable of experimental proof if the parallaxes of distant stars could be measured with sufficient accuracy.

Lastly, there is an important relation between the numerical values of the circular and hyperbolic functions. If the argument $u$ assumes successive values between $o$ and $+\infty$, $\sinh u$ assumes successive values between $o$ and $+\infty$ just as $\tan a$ does when $a$ varies from o to $90^{\circ}$; cosh $u$ assumes values between I and $+\infty$ like sec $\beta$, and $\tanh u$ assumes values between o and I

[^1]in the same way as $\sin \gamma$. The variation of the hyperbolic functions throughout the entire plane and their similarity to the circular functions between the limits $0^{\circ}$ and $180^{\circ}$ is shown



Fig. 3. in the diagram. Since each of the functions is singly periodic, there must be a single value of $\alpha, \beta, \gamma$ corresponding to a particular value of $u$, such that

$$
\begin{aligned}
& \sinh u=\tan \alpha, \\
& \cosh u=\sec \beta \\
& \tanh u=\sin \gamma .
\end{aligned}
$$

It will be found by substituting in the trigonometric formulæ that $\alpha=\beta=\gamma$ $=\phi$, and the required relations are therefore

$$
\begin{aligned}
\cosh u & =\sec \phi, \\
\sinh u & =\tan \phi, \\
\tanh u & =\sin \phi .
\end{aligned}
$$

The angle $\phi$ which renders it possible to evaluate the hyperbolic functions by means of the circular functions is of great importance in pure and applied mathematics. Some of its properties and applications will be considered in the section on geometrical illustrations. It is called gudermannian $u$ and is written

$$
\phi=g d u .
$$

The following list of formulæ involving the hyperbolic functions might be greatly extended, but it includes the most useful relations. ${ }^{1}$

[^2]A.-Relations between Hyperbolic and Circular Functions.

1. $\sinh u=-i \sin i u=\tan g d u$.
2. $\cosh u=\cos i u=\sec g d u$.
3. $\tanh u=-i \tan i u=\sin g d u$.
4. $\tanh \frac{1}{2} u=\tan \frac{1}{2} g d u$.
5. $e^{u}=(\mathrm{I}+\sin g d u) \div \cos g d u$, $=\left[1-\cos \left(\frac{1}{2} \pi+g d u\right)\right] \div \sin \left(\frac{1}{2} \pi+g d u\right)$, $=\tan \left(\frac{1}{4} \pi+\frac{1}{2} g d u\right)$.
6. $\sinh i u=i \sin u$.
7. $\cosh i u=\cos u$.
8. $\tanh i u=i \tan u$.
9. $\sinh (u \pm i v)= \pm i \sin (v \mp i u)$, $=\sinh u \cos v \pm i \cosh u \sin v$.
เo. $\cosh (u \pm i v)=\cos (v \mp i u)$, $=\cosh u \cos v \pm i \sinh u \sin v$.
II. $\cosh (m i \pi)=\cos m \pi$. ( $m$ is an integer.)
10. $\sinh (2 m+1) \frac{1}{2} i \pi=i \sin (2 m+1) \frac{1}{2} \pi$. ( $m$ is an integer.)

## B.-Relations among the Hyperbolic Functions.

13. $\sinh u=\frac{1}{2}\left(e^{u}-e^{-u}\right)=-\sinh (-u)=(\operatorname{csch} u),^{-1}$

$$
=2 \tanh \frac{1}{2} u \div\left(\mathrm{I}-\tanh ^{2} \frac{1}{2} u\right)=\tanh u \div\left(\mathrm{I}-\tanh ^{2} u\right)^{1 / 2}
$$

14. $\cosh u=\frac{1}{2}\left(e^{u}+e^{-u}\right)=\cosh (-u)=(\operatorname{sech} u)^{-1}$,

$$
=\left(1+\tanh ^{2} \frac{1}{2} u\right) \div\left(\mathrm{I}-\tanh ^{2} \frac{1}{2} u\right)=\mathrm{I} \div\left(\mathrm{I}-\tanh ^{2} u\right)^{1 / 2}
$$

15. $\tanh u=\left(e^{u}-e^{-u}\right) \div\left(e^{u}+e^{-u}\right)=-\tanh (-u)$,

$$
=(\operatorname{coth} u)^{-1}=\sinh u \div \cosh u=\left(\mathrm{r}-\operatorname{sech}^{2} u\right)^{1 / 2}
$$

16. sech $u=\operatorname{sech}(-u)=\left(1-\tanh ^{2} u\right)^{1 / 2}$.
17. $\operatorname{csch} u=-\operatorname{csch}(-u)=\left(\operatorname{coth}^{2} u-1\right)^{1 / 2}$.
18. coth $u=-\operatorname{coth}(-u)=\left(\operatorname{csch}^{2} u+1\right)^{1 / 2}$.
19. $\cosh ^{2} u-\sinh ^{2} u=\mathrm{I}$.
20. $\sinh \frac{1}{2} u=\sqrt{\frac{1}{2}(\cosh u-1)}$.

2I. $\cosh \frac{1}{2} u=\sqrt{\frac{1}{2}(\cosh u+1)}$.
22. $\tanh \frac{1}{2} u=(\cosh u-1) \div \sinh u$,

$$
=\sinh u \div(1+\cosh u) \doteq \sqrt{(\cosh u-1) \div(\cosh u+1)}
$$

$23 \sinh 2 u=2 \sinh u \cosh u=2 \tanh u \div\left(1-\tanh ^{2} u\right)$.
24. $\cosh 2 u=\cosh ^{2} u+\sinh ^{2} u=2 \cosh ^{2} u-\mathrm{I}$,

$$
=\mathrm{I}+2 \sinh ^{2} u=\left(\mathrm{I}+\tanh ^{2} u\right) \div\left(\mathrm{I}-\tanh ^{2} u\right)
$$

25. $\tanh 2 u=2 \tanh u \div\left(1+\tanh ^{2} u\right)$.
26. $\sinh 3 u=3 \sinh u+4 \sinh ^{3} u$.
27. $\cosh 3 u=4 \cosh ^{3} u-3 \cosh u$.
28. $\tanh 3 u=\left(3 \tanh u+\tanh ^{3} u\right) \div\left(1+3 \tanh ^{2} u\right)$.
29. $\sinh n u=$

$$
u \cosh ^{n-1} u \sinh u+\frac{(n)(n-1)(n-2)}{6} \cosh ^{n-3} u \sinh ^{3} u+\ldots
$$

30. $\cosh n u=\cosh ^{n} u+\frac{n(n-1)}{2} \cosh ^{n-2} u \sinh ^{2} u+\ldots$
31. $\sinh u+\sinh v=2 \sinh \frac{1}{2}(u+v) \cosh \frac{1}{2}(u-v)$.
32. $\sinh u-\sinh v=2 \cosh \frac{1}{2}(u+v) \sinh \frac{1}{2}(u-v)$.
33. $\cosh u+\cosh v=2 \cosh \frac{1}{2}(u+v) \cosh \frac{1}{2}(u-v)$.
34. $\cosh u-\cosh v=2 \sinh \frac{1}{2}(u+v) \sinh \frac{1}{2}(u-v)$.
35. $\sinh u+\cosh u=\left(1+\tanh \frac{1}{2} u\right) \div\left(1-\tanh \frac{1}{2} u\right)$.
36. $(\sinh u+\cosh u)^{n}=\cosh n u+\sinh n u$.
37. $\tanh u+\tanh v=\sinh (u+v) \div \cosh u \cosh v$.
38. $\tanh u-\tanh v=\sinh (u-v) \div \cosh u \cosh v$.
39. $\operatorname{coth} u+\operatorname{coth} v=\sinh (u+v) \div \sinh u \sinh v$.
40. coth $u-\operatorname{coth} v=-\sinh (u-v) \div \sinh u \sinh v$.
41. $\sinh (u \pm v)=\sinh u \cosh v \pm \cosh u \sinh v$.
42. $\cosh (u \pm v)=\cosh u \cosh v \pm \sinh u \sinh v$.
43. $\tanh (u \pm v)=(\tanh u \pm \tanh v) \div(1 \pm \tanh u \tanh v)$.
44. $\operatorname{coth}(u \pm v)=(\operatorname{coth} u \operatorname{coth} v \pm 1) \div(\operatorname{coth} v \pm \operatorname{coth} u)$.
45. $\sinh (u+v)+\sinh (u-v)=2 \sinh u \cosh v$.
46. $\sinh (u+v)-\sinh (u-v)=2 \cosh u \sinh v$.
47. $\cosh (u+v)+\cosh (u-v)=2 \cosh u \cosh v$.
48. $\cosh (u+v)-\cosh (u-v)=2 \sinh u \sinh v$.
49. $\tanh \frac{1}{2}(u+v)=(\sinh u+\sinh v) \div(\cosh u+\cosh v)$.
50. $\tanh \frac{1}{2}(u-v)=(\sinh u-\sinh v) \div(\cosh u+\cosh v)$.

5I. $\operatorname{coth} \frac{1}{2}(u+v)=(\sinh u-\sinh v) \div(\cosh u-\cosh v)$.
52. $\operatorname{coth} \frac{1}{2}(u-v)=(\sinh u+\sinh v) \div(\cosh u-\cosh v)$.
53. $\frac{\tanh u+\tanh v}{\tanh u-\tanh v}=\frac{\sinh (u+v)}{\sinh (u-v)}$.
54. $\frac{\operatorname{coth} u+\operatorname{coth} v}{\operatorname{coth} u-\operatorname{coth} v}=-\frac{\sinh (u+v)}{\sinh (u-v)}$.
55. $\sinh (u+v)+\cosh (u+v)=(\cosh u+\sinh u)(\cosh v+\sinh v)$.
56. $\sinh (u+v) \sinh (u-v)=\sinh ^{2} u-\sinh ^{2} v$,

$$
=\cosh ^{2} u-\cosh ^{2} v
$$

57. $\cosh (u+v) \cosh (u-v)=\cosh ^{2} u+\sinh ^{2} v$, $=\sinh ^{2} u+\cosh ^{2} v$.
58. $\sinh (m i \pi)=0 . \quad(m$ is an integer $)$.
59. $\cosh (m i \pi)=(-1)^{m}$.
60. $\tanh (m i \pi)=0$.

6I. $\sinh (u+m i \pi)=(-\mathrm{I})^{m} \sinh u$.
62. $\cosh (u+m i \pi)=(-\mathrm{I})^{m} \cosh u$.
63. $\sinh (2 m+1) \frac{1}{2} i \pi= \pm i$.
64. $\cosh (2 m+1) \frac{1}{2} i \pi=0$.
65. $\sinh \left(\frac{i \pi}{2} \pm u\right)=i \cosh u$.
66. $\cosh \left(\frac{i \pi}{2} \pm u\right)= \pm i \sinh u$.
67. $\tanh (u+i \pi)=\tanh u$.

## C. -Inverse Hyperbolic Functions.

68. $\sinh ^{-1} u=\log \left(u+\sqrt{u^{2}+1}\right)=\cosh ^{-1} \sqrt{u^{2}+\mathrm{I}}=\int \frac{d u}{\left(u^{2}+\mathrm{I}\right)^{1 / 2}}$.
69. $\cosh ^{-1} u=\log \left(u+\sqrt{\left.u^{2}-\mathrm{I}\right)}=\sinh { }^{-1} \sqrt{u^{2}-\mathrm{I}}=\int \frac{d u}{\left(u^{2}-\mathrm{I}\right)^{1 / 2}}\right.$.
70. $\left.\tanh ^{-1} u=\frac{1}{2} \log (\mathrm{I}+u)-\frac{1}{2} \log (\mathrm{I}-u)\right)=\int \frac{d u}{\mathrm{I}-u^{2}}$.

7I. $\operatorname{coth}^{-1} u=\frac{1}{2} \log (\mathrm{I}+u)-\frac{1}{2} \log (u-\mathrm{I})=\int \frac{d u}{\mathrm{I}-u^{2}}=\tanh ^{-1} \frac{\mathrm{I}}{u}$.
72. $\operatorname{sech}^{-1} u=\log \left(\frac{\mathrm{I}}{u}+\sqrt{\frac{\mathrm{I}}{u^{2}}-\mathrm{I}}\right)=-\int \frac{d u}{u\left(\mathrm{I}-u^{2}\right)^{3 / 2}}=\cosh ^{-1} \frac{\mathrm{I}}{u}$.
73. $\operatorname{csch}^{-1} u=\log \left(\frac{\mathrm{I}}{u}+\sqrt{\frac{\mathrm{I}}{u^{2}}+\mathrm{I}}\right)=-\int \frac{d u}{u\left(u^{2}+\mathrm{I}\right)^{1 / 2}}=\sinh ^{-1} \frac{\mathrm{I}}{u}$.
74. $\sin ^{-1} u=-i \sinh ^{-1} i u=-i \log \left(i u+1 \overline{\left.1-u^{2}\right)}\right.$.
75. $\cos ^{-1} u=-i \cosh ^{-1} u=-i \log \left(u+i v \overline{\left.\mathrm{I}-u^{2}\right)}\right.$.
76. $\tan ^{-1} u=-i \tanh ^{-1} i u=\frac{\mathrm{I}}{2 i} \log (\mathrm{I}+i u)-\frac{\mathrm{I}}{2 i} \log (\mathrm{I}-i u)$.
77. $\cot ^{-1} u=i \operatorname{coth}^{-1} i u=\frac{\mathrm{I}}{2 i} \log (i u-\mathrm{I})-\frac{\mathrm{I}}{2 i} \log (i u+\mathrm{I})$.
78. $\sin ^{-1} i u=i \sinh ^{-1} u=i \log \left(u+\sqrt{\left.\mathrm{I}+u^{2}\right)}\right.$.
79. $\cos ^{-1} i u=-i \cosh ^{-1} i u=\frac{\pi}{2}-i \log \left(u+1 \overline{\left.1+u^{2}\right)}\right.$.

8o. $\tan ^{-1} i u=i \tanh ^{-1} u=\frac{i}{2} \log (\mathrm{I}+u)-\frac{i}{2} \log (\mathrm{I}-u)$.
$8 \mathrm{I} . \cot ^{-1} i u=-i \operatorname{coth}^{-1} u=-\frac{i}{2} \log (u+\mathrm{I})+\frac{i}{2} \log (u-\mathrm{I})$.
82. $\cosh ^{-1} \frac{1}{2}\left(u+\frac{1}{u}\right)=\sinh ^{-1} \frac{1}{2}\left(u-\frac{1}{u}\right)=\tanh ^{-1} \frac{u^{2}-1}{u^{2}+1}$,

$$
=2 \tanh _{-1}^{-1} \frac{u-1}{u+1}=\log u
$$

83. $\tanh ^{-1} \tan u=\frac{1}{2} g d^{-1} u$.
84. $\tan ^{-1} \tanh u=\frac{1}{2} g d=1^{-1} u$. $=\frac{1}{2}$
85. $\cosh ^{-1} \csc 2 u=-\sinh ^{-1} \cot 2 u=-\tanh ^{-1} \cos 2 u=\log \tan u$.
86. $\tanh ^{-1} \tan ^{2}\left(\frac{1}{4} \pi+\frac{1}{2} u\right)=\frac{1}{2} \log \csc u$.
87. $\tanh ^{-1} \tan ^{2} \frac{1}{2} u=\frac{1}{2} \log \sec u$.
88. $\cosh ^{-1} u \pm \cosh ^{-1} v=\cosh ^{-1}\left[u v \pm V \overline{\left.\left(u^{2}-1\right)\left(v^{2}-1\right)\right]}\right.$.
89. $\sinh ^{-1} u \pm \sinh ^{-1} v=\sinh ^{-1}\left[u V^{\prime} \overline{I+v^{2}} \pm v V^{\prime}+u^{2}\right]$.

> D.-SERIES.
90. $e^{u}=\mathrm{I}+u+\frac{u^{2}}{2!}+\frac{u^{3}}{3!}+\frac{u^{4}}{4!}+\ldots$.
91. $\log u=(u-1)-\frac{1}{2}(u-1)^{2}+\frac{1}{3}(u-1)^{3}-\ldots \quad(2>u>0$. $)$
92. $\log u=\frac{u-\mathrm{I}}{u}+\frac{\mathrm{I}}{2}\left(\frac{u-\mathrm{I}}{u}\right)^{2}+\frac{\mathrm{I}}{3}\left(\frac{u-\mathrm{I}}{u}\right)^{3}+\ldots \quad\left(u>-\frac{1}{2}.\right)$
93. $\log u=2\left[\frac{u-\mathrm{I}}{u+\mathrm{I}}+\frac{\mathrm{I}}{3}\left(\frac{u-\mathrm{I}}{u+\mathrm{I}}\right)^{3}+\frac{\mathrm{I}}{5}\left(\frac{u--\mathrm{I}}{u+\mathrm{I}}\right)^{5}+\ldots\right](u>0$.
94. $\log (\mathrm{I}+u)=u-\frac{\mathrm{I}}{2} u^{2}+\frac{\mathrm{I}}{3} u^{3}-\frac{\mathrm{I}}{4} u^{4}+\ldots \quad\left(u^{2}<\mathrm{I}.\right)$
95. $\log \left(\frac{\mathrm{I}+u}{\mathrm{I}-u}\right)=2\left[u+\frac{\mathrm{I}}{3} u^{3}+\frac{\mathrm{I}}{5} u^{5}+\frac{\mathrm{I}}{7} u^{7}+\ldots\right] \quad\left(u^{2}<\mathrm{I}.\right)$
96. $\log \left(\frac{u+1}{u-1}\right)=2\left[\frac{1}{u}+\frac{\mathrm{I}}{3}\left(\frac{\mathrm{I}}{u}\right)^{3}+\frac{\mathrm{I}}{5}\left(\frac{\mathrm{I}}{u}\right)^{5}+\ldots\right] \quad\left(u^{2}>\mathrm{I}\right.$. $)$
97. $\sinh u=u+\frac{u^{8}}{3!}+\frac{u^{5}}{5!}+\frac{u^{7}}{7!}+\ldots \quad \quad\left(u^{2}<\infty\right.$.)

$$
=u\left(\mathrm{I}+\frac{u^{2}}{\pi^{2}}\right)\left(\mathrm{I}+\frac{u^{2}}{2^{2} \pi^{2}}\right)\left(\mathrm{I}+\frac{u^{2}}{3^{2} \pi^{2}}\right) \ldots \quad\left(u^{2}<\infty .\right)
$$

98. $\cosh u=\mathrm{I}+\frac{u^{2}}{2!}+\frac{u^{4}}{4!}+\frac{u^{6}}{6!}+\ldots \quad\left(u u^{2}<\infty.\right)$

$$
=\left(\mathrm{I}+\frac{4 u^{2}}{\pi^{2}}\right)\left(\mathrm{I}+\frac{4 u^{2}}{3^{2} \pi^{2}}\right)\left(\mathrm{I}+\frac{4 u^{2}}{5^{2} \pi^{2}}\right) \cdots \quad\left(u^{2}<\infty .\right)
$$

99. $\tanh u=u-\frac{1}{3} u^{3}+\frac{2}{15} u^{5}-\frac{17}{3 \mathrm{I} 5} u^{7}+\ldots \quad\left(u^{2}<\frac{1}{4} \pi^{2}\right.$.) 100. $u \operatorname{coth} u=\mathrm{I}+\frac{\mathrm{I}}{3} u^{2}-\frac{\mathrm{I}}{45} u^{4}+\frac{2}{945} u^{6}-\ldots \quad\left(u^{2}<\pi^{2}\right.$.) IOI. $\operatorname{sech} u=\mathrm{I}-\frac{\mathrm{I}}{2} u^{2}+\frac{5}{24} u^{4}-\frac{6 \mathrm{I}}{720} u^{6}+\ldots \quad\left(u^{2}<\frac{1}{4} \pi^{2}\right.$.) 102. $u \operatorname{csch} u=\mathrm{I}-\frac{1}{6} u^{2}+\frac{7}{360} u^{4}-\frac{3 \mathrm{I}}{\mathrm{I}_{5120}} u^{6}+\ldots \quad\left(u^{2}<\pi^{2}\right.$. $)$ 103. $g d u=\phi=u-\frac{1}{6} u^{3}+\frac{1}{24} u^{5}-\frac{61}{5040} u^{7}+\ldots \quad$ (u small.)

$$
=\frac{\pi}{2}-\operatorname{sech} u-\frac{1}{2} \frac{\operatorname{sech}^{3} u}{3}-\frac{1}{2} \frac{3}{4} \frac{\operatorname{sech}^{5} u}{5}-\ldots \quad(u \text { large. })
$$

104. $u=g d^{-1} \phi=\phi+\frac{\mathrm{I}}{6} \phi^{3}+\frac{\mathrm{I}}{24} \phi^{5}+\frac{6 \mathrm{I}}{5040} \phi^{7}+\ldots \quad\left(\phi<\frac{\pi}{2}.\right)$
105. $\sinh ^{-1} u=u-\frac{\mathrm{I}}{2} \frac{u^{3}}{3}+\frac{\mathrm{I}}{2} \frac{3}{4} \frac{u^{5}}{5}-\frac{\mathrm{I}}{2} \frac{3}{4} \frac{5}{6} \frac{u^{7}}{7}+\ldots \quad\left(u^{2}<\right.$ I. $)$

$$
=\log 2 u+\frac{\mathrm{I}}{2} \frac{\mathrm{I}}{2 u^{2}}-\frac{\mathrm{I}}{2} \frac{3}{4} \frac{\mathrm{I}}{4 u^{4}}+\frac{\mathrm{I}}{2} \frac{3}{4} \frac{5}{6} \frac{\mathrm{I}}{6 u^{6}}-\ldots\left(u^{2}>\mathrm{I} .\right)
$$

106. $\cosh ^{-1} u=\log 2 u-\frac{\mathrm{I}}{2} \frac{\mathrm{I}}{2 u^{2}}-\frac{\mathrm{I}}{2} \frac{3}{4} \frac{\mathrm{I}}{4 u^{4}}-\frac{\mathrm{I}}{2} \frac{3}{4} \frac{5}{6} \frac{\mathrm{I}}{6 u^{6}}-\ldots\left(u^{2}>\mathrm{I}\right)$
107. $\tanh ^{-1} u=u+\frac{\mathrm{I}}{3} u^{3}+\frac{\mathrm{I}}{5} u^{5}+\frac{\mathrm{I}}{7} u^{7}+\ldots \quad\left(u^{2}<\mathrm{I}\right.$. $)$
108. $\operatorname{coth}^{-1} u=\tanh ^{-1} \frac{\mathrm{I}}{u}=\frac{\mathrm{I}}{u}+\frac{\mathrm{I}}{3 u^{3}}+\frac{\mathrm{I}}{5 u^{5}}+\frac{\mathrm{I}}{7 u^{7}}+\ldots\left(u^{2}>\mathrm{I}.\right)$

Iog. $\operatorname{sech}^{-1} u=\cosh ^{-1} \frac{\mathrm{I}}{u}=\log \frac{2}{u}-\frac{1}{2} \frac{u^{2}}{2}-\frac{1}{2} \frac{3}{4} \frac{u^{4}}{4}-\frac{1}{2} \frac{3}{4} \frac{5}{6} \frac{u^{6}}{6}-\underset{\left(u^{2}<\text { I. }^{\circ}\right)}{ }$
I 10. $\operatorname{csch}^{-1} u=\sinh ^{-1} \frac{\mathrm{I}}{u}=\frac{\mathrm{I}}{u}-\frac{\mathrm{I}}{2} \frac{\mathrm{I}}{3 u^{3}}+\frac{\mathrm{I}}{2} \frac{3}{4} \frac{\mathrm{I}}{5 u^{5}}-\frac{1}{2} \frac{3}{4} \frac{5}{6} \frac{\mathrm{I}}{7 u^{7}}$

$$
+\ldots\left(u^{2}>\mathrm{I} .\right)
$$

$=\log \frac{2}{u}+\frac{1}{2} \frac{u^{2}}{2}-\frac{1}{2} \frac{3}{4} \frac{u^{4}}{4}+\frac{\mathrm{I}}{2} \frac{3}{4} \frac{5}{6} \frac{u^{6}}{6}-\ldots\left(u^{2}<\right.$ I. $)$

## E.-DERIVATIVES.

III. $\frac{d e^{u}}{d u}=e^{u}$.

II2. $d \frac{\log _{e} u}{d u}=\frac{\mathrm{I}}{u}$.
I I3. $\frac{d a^{v}}{d u}=a^{v} \cdot \frac{d v}{d u} \cdot \log _{e} a$.
II4. $\frac{d u^{u}}{d u}=u^{u}\left(\mathrm{I}+\log _{e} u\right)$.
II5. $\frac{d \sinh u}{d u}=\cosh u$.
I 6 . $\frac{d \cosh u}{d u}=\sinh u$.
II7. $\frac{d \tanh u}{d u}=\operatorname{sech}^{2} u$.
II8. $\frac{d \operatorname{coth} u}{d u}=-\operatorname{csch}^{2} u$.
ing. $\frac{d \operatorname{sech} u}{d u}=-\operatorname{sech} u . \tanh u$.
120. $\frac{d \operatorname{csch} u}{d u}=-\operatorname{csch} u$. $\operatorname{coth} u$.

I2 1. $\frac{d \sinh ^{-1} u}{d u}=\frac{\mathrm{I}}{\sqrt{u^{2}+\mathrm{I}}}$.
122. $\frac{d \cosh ^{-1} u}{d u}=\frac{\mathrm{I}}{\sqrt{/ \sqrt{u^{2}-\mathrm{I}}}}$.
123. $\frac{d \tanh ^{-1} u}{d u}=\frac{\mathrm{I}}{\mathrm{I}-u^{2}}$.
124. $\frac{d \operatorname{coth}^{-1} u}{d u}=\frac{\mathrm{I}}{\mathrm{I}-u^{2}}$.
125. $\frac{d \operatorname{sech}^{-1} u}{d u}=\frac{-\mathrm{I}}{u v^{\prime}}$.
126. $\frac{d \operatorname{csch}^{-1} u}{d u}=\frac{-\mathrm{I}}{u \sqrt{u^{2}+\mathrm{I}}}$.
127. $\frac{d \operatorname{gd} u}{d u}=\operatorname{sech} u$.
128. $\frac{d g^{-1} u}{d u}=\sec u$. $=\frac{d}{d \phi} \log \tan \left(\frac{\pi}{4}+\frac{\phi}{2}\right)=\frac{1}{\cos \phi}$

## F.-Integrals. (Integration constants are omitted.)

129. $\int \sinh u d u=\cosh u$.
130. $\int \cosh u d u=\sinh u$.

I3I. $\int \tanh u d u=\log \cosh u$.
132. $\int \operatorname{coth} u d u=\log \sinh u$.
133. $\int \operatorname{sech} u d u=2 \tan ^{-1} e^{u}=\operatorname{gd} u$.
134. $\int \operatorname{csch} u d u=\log \tanh \frac{u}{2}$.
135. $\int \sinh ^{n} u d u=\frac{\mathrm{I}}{n} \sinh ^{n-1} u$. $\cosh u-\frac{n--\mathrm{I}}{n} \iint \sinh ^{n}-2 u d u$,

$$
=\frac{\mathrm{I}}{n+\mathrm{I}} \sinh ^{n+1} u \cosh u-\frac{n+2}{n+\mathrm{I}} \int \sinh ^{n+2} u d u .
$$

I36. $\int \cosh ^{n} u d u=\frac{\mathrm{I}}{n} \sinh u \cdot \cosh ^{n-1} u+\frac{n-\mathrm{I}}{n} \int \cosh ^{n-2} u d u$, V

$$
=-\frac{1}{n+1} \sinh u \cosh ^{n+1} u+\frac{n+2}{n+1} \int \cosh ^{n+2} u d u .
$$

137. $\int u \sinh u d u=u \cosh u-\sinh u$.
138. $\int u \cosh u d u=u \sinh u-\cosh u$.
139. $\int u^{2} \sinh u d u=\left(u^{2}+2\right) \cosh u-2 u \sinh u$.
140. $\int u^{n} \sinh u d u=u^{n} \cosh u-m u^{n-1} \sinh u$

$$
+n\left(n-\text { I } \int u^{n-2} \sinh u d u\right.
$$

141. $\int \sinh ^{2} u d u=\frac{1}{2}(\sinh u \cosh u-u)$.
142. $\int \sinh u$. $\cosh u d u=\frac{1}{4} \cosh (2 u)$.
143. $\int \cosh ^{2} u d u=\frac{1}{2}(\sinh u \cosh u+u)$.
144. $\int \tanh ^{2} u d u=u-\tanh u$.
145. $\int \operatorname{coth}^{2} u d u=u-\operatorname{coth} u$.
146. $\int \operatorname{sech}^{2} u d u=\tanh u$.
147. $\int \operatorname{sech}^{3} u d u=\frac{1}{2} \operatorname{sech} u \tanh u+\frac{1}{2} \operatorname{gd} u$.
148. $\int \operatorname{csch}^{2} u d u=-\operatorname{coth} u$.
149. $\int \sinh ^{-1} u d u=u \sinh ^{-1} u-\left(\mathrm{I}+\mathrm{u}^{2}\right)^{1 / 2}$.

I 50. $\int \cosh ^{-1} u d u=u \cosh ^{-1} u-\left(u^{2}-1\right)^{1 / 2}$.
151. $\int \tanh ^{-1} u d u=u \tanh ^{-1} u+\frac{1}{2} \log \left(\mathrm{I}-u^{2}\right)$.
152. $\int u \sinh ^{-1} u d u=\frac{1}{4}\left[\left(2 u^{2}+\mathrm{I}\right) \sinh ^{-1} u-u\left(\mathrm{I}+u^{2}\right)^{1 / 2}\right]$.
153. $\int u \cosh ^{-1} u d u=\frac{1}{4}\left[\left(2 u^{2}-\mathrm{I}\right) \cosh ^{-1} u-u\left(u^{2}-\mathrm{I}\right)^{1 / 2}\right]$.
154. $\int(\cosh a+\cosh u)^{-1} d u=2 \operatorname{csch} a \cdot \tanh ^{-1}\left(\tanh \frac{1}{2} u \cdot \tanh \frac{1}{2} \alpha\right)$,
$=\operatorname{csch} a\left[\log \cosh \frac{1}{2}(u+a)-\log \cosh \frac{1}{2}(u-a)\right]$.
155. $\int(\cos a+\cosh u)^{-1} d u=2 \csc a \cdot \tan ^{-1}\left(\tanh \frac{1}{2} u \cdot \tan \frac{1}{2} a\right)$.
156. $\int(1+\cos a \cdot \cosh u)^{-1} d u=2 \csc a \cdot \tanh ^{-1}\left(\tanh \frac{1}{2} u \cdot \tan \frac{1}{2} a\right)$.

I57. $\int \sinh u \cos u d u=\frac{1}{2}(\cosh u \cdot \cos u+\sinh u \cdot \sin u)$.
158. $\int \cosh u \cdot \cos u d u=\frac{1}{2}(\sinh u \cdot \cos u+\cosh u \cdot \sin u)$.
159. $\int \sinh u \cdot \sin u d u=\frac{1}{2}(\cosh u \cdot \sin u-\sinh u \cdot \cos u)$.
160. $\int \cosh u \cdot \sin u d u=\frac{1}{2}(\sinh u \cdot \sin u-\cosh u \cdot \cos u)$.

16I. $\int \sinh (m u) \sinh (n u) d u \int \operatorname{shm} \operatorname{Vm}$

$$
=\frac{1}{m^{2}-n^{2}}[m \sinh (n u) \cosh (m u)-n \cosh (n u) \sinh (m u)]
$$

162. $\int \cosh (m u) \sinh (n u) d u$

$$
=\frac{\mathbf{I}}{m^{2}-n^{2}}[m \sinh (n u) \sinh (m u)-n \cosh (n u) \cosh (m u)] .
$$

163. $\int \cosh (m u) \cosh (n u) d u$

$$
=\frac{1}{m^{2}-n^{2}}[m \sinh (m u) \cosh (n u)-n \sinh (n u) \cosh (m u)]
$$

164. $\int \sinh u \tanh u d u=\sinh u-g d u$.
165. $\int \cosh u \operatorname{coth} u d u=\cosh u+\log \tanh \frac{u}{2}$.
166. $\int \sec u d u=\operatorname{gd}^{-1} u$.
167. $\int \sec ^{3} \phi d \phi=\int\left(\mathrm{I}+\tan ^{2} \phi\right)^{1 / 2} d \tan \phi=\frac{1}{2} \sec \phi \tan \phi+\frac{1}{2} \mathrm{gd}^{-1} \phi$, $=\frac{1}{2} \tan \phi\left(\mathrm{I} \perp \tan ^{2} \phi\right)^{1 / 2}+\frac{1}{2} \sinh ^{-1}(\tan \phi)$. Here $\phi=g d u$.
$168 \int \frac{d u}{\left(u^{2}+a^{2}\right)^{1 / 2}}=\sinh ^{-1} \frac{u}{a} . \quad \int \frac{d u}{\left(a^{2}-u^{2}\right)^{1 / 2}}=\sin ^{-1} \frac{u}{a}$.
168. $\int \frac{d u}{\left(u^{2}-a^{2}\right)^{1 / 2}}=\cosh ^{-1} \frac{u}{a}$.
$\int \frac{-d u}{\left(a^{2}-u^{2}\right)^{1 / 2}}=\cos ^{-1} \frac{u}{a}$.
169. $\int \frac{d u}{\left(a^{2}-u^{2}\right)_{u<a}}=\frac{\mathrm{I}}{a} \tanh ^{-1} \frac{u}{a}$. $\int \frac{d u}{a^{2}+u^{2}}=\frac{\mathrm{I}}{a} \tan ^{-1} \frac{u}{a}$.
170. $\int \frac{-d u}{\left(u^{2}-a^{2}\right)_{u>a}}=\frac{\mathrm{I}}{a} \operatorname{coth}^{-1} \frac{u}{a} . \quad \int \frac{-d u}{a^{2}+u^{2}}=\frac{\mathrm{I}}{a} \cot ^{-1} \frac{u}{a}$.
171. $\int \frac{-d u}{u\left(a^{2}-u^{2}\right)^{1 / 2}}=\frac{\mathrm{I}}{a} \operatorname{sech}^{-1} \frac{u}{a}$. $\quad \int \frac{d u}{u\left(u^{2}-a^{2}\right)^{1 / 2}}=\frac{\mathrm{I}}{a} \sec ^{-1} \frac{u}{a}$.
172. $\int \frac{-d u}{u\left(a^{2}+u^{2}\right)^{1 / 2}}=\frac{\mathrm{I}}{a} \operatorname{csch}^{-1} \frac{u}{a} . \quad \int \frac{-d u}{u\left(u^{2}-a^{2}\right)}=\frac{\mathrm{I}}{a} \csc ^{-1} \frac{u}{a}$.
173. $\int \frac{d u}{\left(a u^{2}+2 b u+c\right)^{3 / 2}}=\frac{1}{V^{\prime}} \frac{1}{a} \sinh { }^{-1} \frac{a u+b}{\left(a c-b^{2}\right)^{1 / 2}} \quad a$ positive, $a c>b^{2}$; $\begin{array}{lr}=\frac{\mathrm{I}}{\sqrt{a}} \cosh ^{-1} \frac{a u+b}{\left(b^{2}-a c\right)^{1 / 2}}, & a \text { positive, } a c<b^{2} ; \\ =\frac{1}{\sqrt{-a}} \cos ^{-1} \frac{a u+b}{\left(b^{2}-a c\right)^{3 / 2}}, & a \text { negative. }\end{array}$
174. $\int \frac{d u}{\left(a u^{2}+2 b u+c\right)}=\frac{1}{\left(a c-b^{2}\right)^{1 / 2}} \tan ^{-1} \frac{a u+b}{\left(a c-b^{2}\right)^{1 / 2}}, \quad a c>b^{2}$;

$$
\begin{array}{ll}
=\frac{-\mathrm{I}}{\left(b^{2}-a c\right)^{1 / 2}} \tanh -1 \frac{a u+b}{\left(b^{2}-a c\right)^{1 / 2}}, & a c<b^{2}, \\
& a u+b<\left(b^{2}-a c\right)^{1 / 2} . \\
=\frac{-1}{\left(b^{2}-a c\right)^{3 / 2}} \operatorname{coth}-1 \frac{a u+b}{\left(b^{2}-a c\right)^{1 / 2}}, & a c<b^{2}, \\
& a u+b>\left(b^{2}-a c\right)^{1 / 2} .
\end{array}
$$

176. $\int \frac{d u}{(a-u)(u-b)^{1 / 2}}=\frac{2}{(a-b)^{3 / 2}} \tanh ^{-1} \sqrt{\frac{u-b}{a-b}}$,

$$
\text { or } \frac{-2}{(b-a)^{1 / 2}} \tan ^{-1} \sqrt{\frac{u-b}{b-a}} \text {, }
$$

or $\frac{2}{(a-b)^{1 / 2}} \operatorname{coth}^{-1} \sqrt{\frac{u-b}{a-b}}$. (The real form is to be taken.)
177. $\int \frac{d u}{(a-u)(b-u)^{1 / 2}}=\frac{2}{(b-a)^{1 / 2}} \tanh ^{-1} \sqrt{\frac{b-u}{b-a}}$,

$$
\text { or } \frac{2}{(b-a)^{3 / 2}} \operatorname{coth}^{-1} \sqrt{\frac{b-u}{b-a}},
$$

$$
\text { or } \frac{-2}{(a-b)^{1 / 2}} \tan ^{-1} \sqrt{\frac{\overline{b-u}}{a-b}} \text {. (The real form is to be taken.) }
$$

178. $\int\left(u^{2}-a^{2}\right)^{\frac{1}{2}} d u=\frac{1}{2} u\left(u^{2}-a^{2}\right)^{\frac{1}{2}}-\frac{1}{2} a^{2} \cosh ^{-1} \frac{u}{a}$.
179. $\int\left(a^{2}-u^{2}, x_{2} d u=\frac{1}{2} u\left(a^{2}-u^{2}\right)^{\frac{1}{2}}+\frac{1}{2} a^{2} \sin ^{-1} \frac{u}{a}\right.$.
180. $\int\left(u^{2}+a^{2}\right)^{\frac{1}{2}} d u=\frac{1}{2} u\left(u^{2}+a^{2}\right)^{\frac{1}{2}}+\frac{1}{2} a^{2} \sinh ^{-1} \frac{u}{a}$.
181. $\int e^{a u} d u=\frac{e^{a u}}{a}$.
182. $\int u e^{a u} d u=\frac{e^{a u}}{a^{2}}(a u-1)$.
183. $\int u^{m} e^{a u} d u=\frac{u u^{m} e^{a u}}{a}-\frac{m}{a} \int u u^{m-1} e^{a u} d u$.
184. $\int \frac{e^{a u} d u}{u^{m}}=\frac{1}{m-1}\left[-\frac{e^{a u}}{u^{m-1}}+a \int \frac{e^{a u} d u}{u^{m-1}}\right]$.
185. $\int a^{b u} d u=\frac{a^{b u}}{b \log a}$.
186. $\int u^{n} a^{u} d u=\frac{a^{u} u^{n}}{\log a}-\frac{n a^{u} u^{n-1}}{(\log a)^{2}}+\frac{n(n-1) a^{u} u^{n}-2}{(\log a)^{3}} \cdots$

$$
\pm \frac{n(n-1)(n-2) \ldots 2 \mathrm{I} a^{u}}{(\log a)^{n+1}}
$$

187. $\int \frac{a^{u} d u}{u^{n}}=\frac{a^{u}}{n-1}\left[-\frac{1}{u^{n-1}}-\frac{\log a}{(n-2) u^{n-2}}-\frac{(\log a)^{2}}{(n-2)(n-3) u^{n-3}}\right.$

$$
\left.-\ldots+\frac{(\log a)^{n-1}}{(n-2)(n-3) \cdots 2.1} \int \frac{a^{u} d u}{u}\right]
$$

188. $\int \frac{a^{u} d u}{u}=\log u+u \log a+\frac{(u \log a)^{2}}{2 \cdot 2!}+\frac{\left(u \log a^{3}\right.}{3 \cdot 3!}+\ldots$.
189. $\int \frac{d u}{\mathrm{I}+e^{u}}=\log \frac{e^{u}}{\mathrm{I}+e^{u}}$.
190. $\int \frac{d u}{a+b e^{m u}}=\frac{\mathrm{I}}{a m}\left[m u-\log \left(a+b e^{m u}\right)\right]$.
191. $\int \frac{d u}{a e^{m u}+b e^{-m u}}=\frac{1}{m(a b)^{1 / 2}} \tan ^{-1}\left(e^{m u} \sqrt{\frac{a}{b}}\right)$.
192. $\int \frac{d u}{\left(a+b e^{m u}\right)^{1 / 2}}=\frac{1}{m V^{\prime} \frac{a}{a}}\left[\log \left(\sqrt{a+b e^{m u}}-\sqrt{\bar{a}}\right)\right.$ $\left.-\log \left(\sqrt{a+b e^{m u}}+\sqrt{ } \bar{a}\right)\right]$.
193. $\int \frac{u e^{u} d u}{(\mathrm{I}+u)^{2}}=\frac{e^{u}}{\mathrm{I}+u}$.
194. $\int e^{u u} \log u d u=\frac{e^{a u} \log u}{a}-\frac{1}{a} \int \frac{e^{a u} d u}{u}$.
195. $\int \log u d u=u \log u-u$.
196. $\int u^{m} \log u d u=u^{m+1}\left[\frac{\log u}{m+\mathrm{I}}-\frac{\mathrm{I}}{(m+\mathrm{I})^{2}}\right]$.
197. $\int(\log u)^{n} d u=u(\log u)^{n}-n \int(\log u)^{n-1} d u$.
198. $\int u^{m}(\log u)^{n} d u=\frac{u^{m+1}(\log u)^{n}}{m+\mathrm{I}}-\frac{n}{m+\mathrm{I}} \int u^{m}(\log u)^{n-1} d u$.
199. $\int \frac{(\log u)^{n} d u}{u}=\frac{(\log u)^{n+1}}{n+\mathrm{I}}$.
200. $\int \frac{d u}{\log u}=\log (\log u)+\log u+\frac{(\log u)^{2}}{2.2!}+\frac{(\log u)^{3}}{3 \cdot 3!}+\ldots$
201. $\int \frac{d u}{(\log u)^{n}}=-\frac{u}{(n-\mathrm{I})(\log u)^{n-1}}+\frac{\mathrm{I}}{n-\mathrm{I}} \int \frac{d u}{(\log u)^{n-1}}$.
202. $\int \frac{u^{m} d u}{(\log u)^{n}}=-\frac{u^{m}+1}{(n-\mathrm{I})(\log u)^{n-1}}+\frac{m+\mathrm{I}}{n-\mathrm{I}} \int \frac{u^{m} d u}{(\log u)^{n-1}}$.
203. $\int \frac{u^{m} d u}{\log u}=\int \frac{e^{-y}}{y} d y$, where $y=-(m+1) \log u$.
204. $\int \frac{d u}{u \log u}=\log (\log u)$.
205. $\int \frac{d u}{u(\log u)^{n}}=-\frac{\mathrm{I}}{(n-\mathrm{I})(\log u)^{n-1}}$.
206. $\int(a+b u)^{m} \log u d u=$

$$
\frac{\mathrm{I}}{b(m+\mathrm{I})}\left[(a+b u)^{m+1} \log u-\int \frac{(a+b u)^{m+1} d u}{u}\right]
$$

207. $\int u^{m} \log (a+b u) d u=$

$$
\frac{\mathrm{I}}{m+\mathrm{I}}\left[u^{m+1} \log (a+b u)-b \int \frac{u^{m+1} d u}{a+b u}\right] .
$$

208. $\int \frac{\log (a+b u) d u}{u}=$

$$
\begin{aligned}
& \log a \cdot \log u+\frac{b u}{a}-\frac{\mathrm{I}}{2^{2}}\left(\frac{b u}{a}\right)^{2}+\frac{\mathrm{I}}{3^{2}}\left(\frac{b u}{a}\right)^{3}-\cdots \\
= & \frac{\mathrm{I}}{2}(\log b u)^{2}-\frac{a}{b u}+\frac{\mathrm{I}}{2^{2}}\left(\frac{a}{b u}\right)^{2}-\frac{\mathrm{I}}{3^{2}}\left(\frac{a}{b u}\right)^{3}+\cdots
\end{aligned}
$$

209. $\int \frac{\log u d u}{(a+b u)^{m}}=\frac{\mathrm{I}}{b(m-\mathrm{I})}\left[-\frac{\log u}{(a+b u)^{m-1}}+\int \frac{d u}{u(a+b u)^{m-1}}\right]$.
210. $\int \frac{\log u d u}{a+b u}=\frac{\mathrm{I}}{b} \log u \cdot \log (a+b u)-\frac{1}{b} \int \frac{\log (a+b u)}{u} d u$.

2II. $\int(a+b u) \log u d u=\frac{(a+b u)^{2}}{2 b} \log u-\frac{a^{2} \log u}{2 b}-a u-\frac{1}{4} b u^{2}$.
21 2. $\int \frac{\log u d u}{(a+b u)^{1 / 2}}=$

$$
\begin{gathered}
\frac{2}{b}\left[(\log u-2) \sqrt{(a+b u)}+\sqrt{a} \log \left(\sqrt{a+b u}+v^{\prime} \bar{a}\right)\right. \\
-\sqrt{a} \log (\sqrt{a+b u}-\sqrt{a})], \text { if } a>0, \\
=\frac{2}{b}\left[(\log u-2) \sqrt{(a+b u)}+2 \sqrt{-a} \tan ^{-1} \sqrt{\frac{a+b u}{-a}}\right], \text { if } a<0 .
\end{gathered}
$$

213. $\int_{0}^{\infty} e^{-a^{2} u^{2}} d u=\frac{1 \bar{\pi}}{2 a}=\frac{1}{2 a} \Gamma\left(\frac{1}{2}\right)$.
214. $\int_{0}^{\infty} u^{n} e^{-a u} d u=\Gamma \frac{(n+1)}{a^{n+1}}=\frac{n!}{a^{n+1}}$.
215. $\int_{0}^{\infty} u^{2 n} e^{-a u^{2}} d u=\frac{1 \cdot 3 \cdot 5 \cdots(2 n-1)}{2^{n+1} a^{n}} \sqrt{\frac{\pi}{a}}$.
216. $\int_{0}^{\infty} e^{-u^{2}-\frac{a^{2}}{u^{2}}} d u=\frac{e^{-2 a}}{2} \sqrt{\pi}$.
$a>0$.
217. $\int_{0}^{\infty} e^{-n u} \sqrt{u} d u=\frac{\mathrm{I}}{2 n} \sqrt{\frac{\pi}{n}}$.
218. $\int_{11}^{\infty} \frac{e^{-n u}}{\sqrt{u}} d u=\sqrt{\frac{\pi}{u}}$.
219. $\int_{0}^{\infty} \frac{d u}{\sinh (n u)}=\frac{\pi}{2 n}$.
220. $\int_{0}^{\infty} \frac{u d u}{\sinh (n u)}=\frac{\pi^{2}}{4 n^{2}}$.

22I. $\int_{0}^{i \pi} \sinh (m u) \cdot \sinh (n u) d u=\int_{0}^{i \pi} \cosh (m u) \cdot \cosh (n u) d u$ $=0$, if $m$ is different from $n$.
222. $\int_{0}^{i \pi} \cosh ^{2}(m u) d u=-\int_{0}^{i \pi} \sinh ^{2}(m u) d u=\frac{i \pi}{2}$.
223. $\int_{-i \pi}^{+i \pi} \sinh (m u) d u=0$.
224. $\int_{0}^{i \pi} \cosh (m u) d u=0$.
225. $\int_{-i \pi}^{i \pi} \sinh (m u) \cosh (n u) d u=0$.
226. $\int_{0}^{i \pi} \sinh (m u) \cosh (m u) d u=0$.
227. $\int_{0}^{1} \frac{\log u}{\mathrm{I}-u} d u=-\frac{\pi^{2}}{6}$.
228. $\int_{0}^{1} \frac{\log u}{1+u} d u=-\frac{\pi^{2}}{12}$.
229. $\int_{0}^{1} \frac{\log u}{\mathrm{I}-u^{2}} d u=-\frac{\pi^{2}}{8}$.
230. $\int_{0}^{1} \log \left(\frac{\mathrm{I}+u}{\mathrm{I}-u}\right) \cdot \frac{d u}{u}=\frac{\pi^{2}}{4}$.

23I. $\int_{0}^{1} \frac{\log u d u}{\left(\mathrm{I}-u^{2}\right)^{1 / 2}}=-\frac{\pi}{2} \log 2$.
232. $\int_{0}^{1} \frac{\left(u^{p}-u^{q}\right) d u}{\log u}=\log \frac{p+\mathrm{I}}{q+\mathrm{I}}$, if $p+\mathrm{I}>0, q+\mathrm{I}>0$.
233. $\int_{0}^{1}(\log u)^{n} d u=(-1)^{n} \cdot u$ !.
234. $\int_{0}^{1}\left(\log \frac{1}{u}\right)^{1 / 2} d u=\frac{\sqrt{\pi}}{2}$.
$235 \int_{0}^{1}\left(\log \frac{\mathrm{I}}{u}\right)^{n} d u=n!$.
236. $\int_{0}^{1} \frac{d u}{\left(\log \frac{1}{u}\right)^{1 / 2}}=\sqrt{\pi}$.
237. $\int_{0}^{1} u^{m} \log \left(\frac{\mathrm{I}}{u}\right)^{n} d u=\frac{\Gamma(n+\mathrm{I})}{(m+\mathrm{I})^{n+1}}$, if $m+\mathrm{I}>\mathrm{O}, u+\mathrm{I}>0$.
238. $\int_{0}^{\infty} \log \left(\frac{e^{u}+\mathrm{I}}{e^{u}-\mathrm{I}}\right) d u=\frac{\pi^{2}}{4}$.
G.-Formulas for the Solution of Pseudo-spherical Triangles.

$$
\begin{aligned}
& \text { a.--Right Triangles. } \\
& \sin A=\frac{\cot I(a)}{\cot I(c)}=\frac{\sinh a}{\sinh c} . \\
& \cos A=\frac{\cos I I(b)}{\cos I(c)}=\frac{\tanh b}{\tanh c} . \\
& \cos A=\frac{\sin B}{\sin I(a)}=\sin B \cosh a . \\
& \cot A=\frac{\cot I(b)}{\cos I I(a)}=\frac{\sinh b}{\tanh a} . \\
& \cos B=\frac{\cos I(a)}{\cos I(c)}=\frac{\tanh a}{\tanh c} . \\
& \cos B=\frac{\sin A}{\sin I(b)}=\sin A \cosh b . \\
& \sin B=\frac{\cot I(b)}{\cot I(c)}=\frac{\sinh b}{\sinh c} . \\
& \cot B=\frac{\cot I(a)}{\cos I I(b)}=\frac{\sinh a}{\tanh b .} \\
& \tan A \tan B=\sin \Pi(c)=\sin I(a) \sin I(b) . \\
&=\operatorname{sech} c=\operatorname{sech} a \operatorname{sech} b . \\
& b .- \text { Oblique Triangles. }
\end{aligned}
$$

The general relations are:
$\cosh a=\cosh b \cosh c-\sinh b \sinh c \cos A$.
$\sin A \sinh b=\sin B \sinh a$.
coth $a \sinh b=\cosh b \cos C+\sin C \cot A$.
$\cos A=-\cos B \cos C+\sin B \sin C \cosh a$.
Forti solves the six typical cases in the following manner:
CASE I.-Given $a, b, c$. Put $2 p=a+b+c$. Then,

$$
\tan \frac{1}{2} A=\sqrt{\frac{\sinh (p-b) \cdot \sinh (p-c)}{\sinh p \sinh (p-a)}} .
$$

The conditions are $a<b+c ; b<a+c$; and $c<a+b$.
Case 2.-Given $a, b, A$. Draw the geodetic line $C D$ perpendicular to $A B$.
Then $a>C D ; \frac{\sinh b \sin A}{\sinh a}<\mathrm{I} ; \cot \frac{1}{2} C>0 ;$ and $\tanh \frac{1}{2} c>0$.

$$
\begin{aligned}
& \sin B=\frac{\sinh b \sin A}{\sinh a} . \\
& \cos \frac{1}{2} C=\frac{\tan \frac{1}{2}(A-B) \sinh \frac{1}{2}(a+b)}{\sinh \frac{1}{2}(a-b)} . \\
& \tanh \frac{1}{2} c=\frac{\tanh \frac{1}{2}(a-b) \sin \frac{1}{2}(A+B)}{\sin \frac{1}{2}(A-B)} .
\end{aligned}
$$

Case 3.-Given $a, b, C . \quad 2 \Delta=\pi-(A+B+C)$.

$$
\begin{aligned}
& \tan \frac{1}{2}(A+B)=\cot \frac{1}{2} C \frac{\cosh \frac{1}{2}(a-b)}{\cosh \frac{1}{2}(a+b)} \\
& \tan \frac{1}{2}(A-B)=\cot \frac{1}{2} C \frac{\sinh \frac{1}{2}(a-b)}{\sinh \frac{1}{2}(a+b)} \\
& \tanh \frac{1}{2} c=\sqrt{\frac{\sin \Delta \sin (\Delta+C)}{\sin (\Delta+A) \sin (\Delta+B)}} .
\end{aligned}
$$

Case 4.-Given $A, B, c . \quad A+B<\pi$ and $D B C<D B G$. The angle $D B G$ is the angle between the geodetic $D B$ drawn perpendicular to $A C$ and the geodetic $B G$ drawn parallel to $A C$.

$$
\begin{aligned}
& \tanh \frac{1}{2}(a+b)=\tanh \frac{1}{2} c \frac{\cos \frac{1}{2}(A-B)}{\cos \frac{1}{2}(A+B)} . \\
& \tanh \frac{1}{2}(a-b)=\tanh \frac{1}{2} c \frac{\sin \frac{1}{2}(A-B)}{\sin \frac{1}{2}(A+B)} . \\
& \tan \frac{1}{2} C=\sqrt{\frac{\sinh (p-a) \sinh (p-b)}{\sinh p \sinh (p-c)}}
\end{aligned}
$$

Case 5.-Given $A, B, a, \quad a>C D$ and $A+B<\pi$.
Solve the two right triangles formed by the geodetic line $C D$ drawn perpendicular to $A B$.

Case 6.-Given $A, B, C . \quad A+B+C<\pi$.

$$
\tanh \frac{1}{2} a=\sqrt{\frac{\sin \Delta \sin (\Delta+A)}{\sin (\Delta+B) \sin (\Delta+C)}}
$$

H.-Formulas for the Solution of the Cubic ${ }^{1}$.

If a cubic equation is given in the form

$$
z^{3}+a z^{2}+b z+c=0,
$$

it can be reduced by the substitution $z=x-\frac{a}{3}$ to the simpler form

$$
x^{3}+p x+q=0 .
$$

CASE I.-When $x^{3}+p x \pm q=0 ; p$ and $q$ positive. Compute the auxiliary variable $u$ from $\sinh u=\frac{\frac{1}{2} q}{\frac{1}{3} p\left(\frac{1}{3} p\right)^{\frac{1}{2}}}$; then the roots are

$$
\begin{aligned}
& x_{1}=\mp 2 \sqrt{\frac{1}{3} p} \sinh \frac{1}{3} u . \\
& x_{2}= \pm \sqrt{\frac{1}{3} p} \sinh \frac{1}{3} u+i \sqrt{p} \cosh \frac{1}{3} u . \\
& x_{3}= \pm \sqrt{\frac{1}{3} p} \sinh \frac{1}{3} u-i \sqrt{p} \cosh \frac{1}{3} u .
\end{aligned}
$$

CASE 2.-When $x^{3}-p x \pm \dot{q}=\mathrm{o} ; p$ and $q$ positive. $\left(\frac{1}{3} p\right)^{3}<\left(\frac{1}{2} q\right)^{2}$. Compute $u$ from $\cosh u=\frac{\frac{1}{2} q}{\frac{1}{3} p\left(\frac{1}{3} p\right)^{\frac{1}{2}}}$; then the roots are

$$
\begin{aligned}
& x_{1}=\mp 2 \sqrt{\frac{1}{3} p} \cosh \frac{1}{3} u . \\
& x_{2}= \pm \sqrt{\frac{1}{3} p} \cosh \frac{1}{3} u+i \sqrt{p} \sinh \frac{1}{3} u . \\
& x_{3}= \pm \sqrt{\frac{1}{3} p} \cosh \frac{1}{3} u-i \sqrt{p} \sinh \frac{1}{3} u .
\end{aligned}
$$

CASE 3.-When $x^{3}-p x \pm q=0 ; p$ and $q$ positive. $\left(\frac{1}{3} p\right)^{3}>\left(\frac{1}{2} q\right)^{2}$. Compute the angle $u$ from $\cos u=\frac{\frac{1}{2} q}{\frac{1}{3} p\left(\frac{1}{3} p\right)^{1 / 2}}$; then the roots are

$$
\begin{aligned}
& x_{1}=\mp 2 \sqrt{\frac{1}{3} p} \cos \frac{1}{3} u . \\
& x_{2}=\mp 2 \sqrt{\frac{1}{3} p} \cos \left(\frac{1}{3} u+120^{\circ}\right) . \\
& x_{3}=\mp 2 \sqrt{\frac{1}{3} p} \cos \left(\frac{1}{3} u+240^{\circ}\right) .
\end{aligned}
$$

Case 4.-When $x^{3}-p x \pm q=0 ; p$ and $q$ positive. $\left(\frac{1}{3} p\right)^{3}=\left(\frac{1}{2} q\right)^{2}$.

$$
\begin{aligned}
& x_{1}=\mp{ }_{2} \sqrt{\frac{1}{3} p} . \\
& x_{2}=x_{3}= \pm \sqrt{\frac{1}{3} p} .
\end{aligned}
$$

For applications of hyperbolic and circular functions to the solution of the cubic whose coefficients are general (i.e., real or complex), see a brief paper by Mr. W. D. Lambert in American Mathematical Monthly for April, 1906.

## GEOMETRICAL ILLUSTRATIONS OF HYPERBOLIC FUNCTIONS..

The algebraic relationship of the hyperbolic functions to the circular functions has been discussed in the section on definitions and formulas. A close relationship also exists between the elliptic functions and the hyperbolic functions. Thus it may be shown that the elliptic integral of the first kind,

$$
u=\int \frac{d \phi}{\sqrt{1-k^{2} \sin ^{2} \phi}},
$$

in which $k$ is the modulus and $\phi$ the amplitude, reduces to $u=g d^{-1} \phi$ when $k=\mathrm{r}$. The elliptic functions thus degenerate into the hyperbolic functions when the modulus is equal to unity. A case in point is the elastica, the equation of which takes the form of an elliptic integral, excepting when the modulus is unity. It then reduces to the two equations

$$
\frac{x}{a}=u-2 \tanh u ; \frac{y}{a}=\frac{2}{\cosh u}
$$

which is a syntractrix described by the free end of a rod whose middle point traces out the tractory. ${ }^{1}$

Ligowski gives the following easy geometrical method of demonstrating the relations between the hyperbolic and circular functions. Let the equation of the circle of unit radius be

$$
x_{c}^{2}+y_{c}^{2}=\mathrm{I},
$$

and call $u_{c}$ the arc of this circle from the positive $x$ axis to the point $x_{c} y_{c}$ Then, of course, the circle may be repre-
 sented by the two equations

$$
x_{c}=\cos u_{c} ; y_{c}=\sin u_{c} .
$$

Now, the area of the circular sector, whose chord is $2 y_{c}$, is $\frac{2 . u_{c} \text {. } 1}{2}=u_{c}$, so that $x_{c}$ and $y_{c}$ may be regarded as the cosine and sine of a sector $u_{c}$. The ellipse may be derived from the unit circle by multiplying the ordinates $y_{c}$ by $b$. Hence, in the ellipse, the area of the sector subtended by the chord $2 y_{e}$ is, say, $u_{e}$ and $u_{e}=b u_{c}$.
${ }^{1}$ If in these equations $m$ is substituted for 2 they represent any syntractrix. The two equations, with this substitution, can be combined to the following :

$$
\frac{(a u-x)^{2}}{a^{2} m^{2}}+\frac{y^{2}}{a^{2} m^{2}}=\mathrm{I},
$$

showing that the curve is traced by a point on a circle of radius $a m$ whose center is in motion. It is noteworthy that if in this equation the hyperbolic sector $u$ is replaced by a circular sector $\phi$, the new equation represents a prolate or a curtate cycloid, or better the syncycloid. Thus the syntractrix may be considered as a syncycloid with an infinite period.

Thus

$$
\begin{gathered}
x_{c}=\cos u_{c}=\cos \frac{u_{e}}{b} \\
y_{c}=\sin u_{c}=\frac{y_{e}}{b}=\sin \frac{u_{e}}{b},
\end{gathered}
$$

so that for the ellipse,

$$
\begin{gathered}
x_{e}^{2}+\frac{y_{e}^{2}}{b^{2}}=\mathrm{I} \\
x_{c}=x_{e}=\cos \frac{u_{e}}{b} ; y_{e}=b \sin \frac{u_{e}}{b}
\end{gathered}
$$

The equation

$$
x^{2}-y^{2}=\mathrm{I}
$$

represents an equilateral hyperbola, and if $u$ is the area of the hyperbolic sector whose chord is $2 y$, then there can be no objection to writing

$$
x=\cosh u ; y=\sinh u
$$

where cosh and sinh are functions whose nature is still to be determined. The most evident relation is

$$
\cosh ^{2} u-\sinh ^{2} u=\mathrm{I}
$$

Now if $i=1-\mathrm{I}$, the hyperbola may be written

$$
x^{2}+\frac{y^{2}}{i^{2}}=\mathrm{I}
$$

which is an ellipse whose major axis is unity and whose minor axis is $i$. Comparing this with the ellipse discussed above, it appears at once that

$$
\begin{aligned}
& x=\cosh u=\cos \frac{u}{i} \\
& y=\sinh u=i \sin \frac{u}{i}
\end{aligned}
$$

or, in an equivalent form,

$$
\begin{aligned}
& \cosh u=\cos i u ; \sinh u=-i \sin i u \\
& \cosh i u=\cos u: \sinh i u=i \sin u
\end{aligned}
$$

The investigation of $\cosh u$ and $\sinh u$ can be completed in various ways; for example, by writing out the series for $\cos i u$ and $-i \sin i u$ and showing that their sum or difference is $e^{ \pm u}$.

The geometrical properties of the hyperbolic functions themselves are commonly discussed in reference to the equilateral hyperbola. They could also be derived from the geometry of the ellipse without reference to the hyperbola; but a more perspicuous method seems to be to study the relations of these functions to both curves at the same time. ${ }^{1}$

In any ellipse,

$$
\frac{x^{2}}{\beta^{2}}+\frac{y^{2}}{a^{2}}=\mathrm{I}
$$

[^3]the area $a \beta$ may be chosen as the unit area, so that the equation of the curve becomes
$$
\alpha^{2} x^{2}+\frac{y^{2}}{a^{2}}=\mathrm{I}
$$


By varying the value of $a$ in this equation a family of ellipses is obtained each of area $\pi$, all with the same center and all with axes lying in the axes of coördinates. The envelope of this system of curves is the hyperbola $x y=\frac{1}{2}$, and this may be conceived as generated by the motion of a single point. The coördinates of the point $P_{1}$, at which the hyperbola is tangent to the ellipse, are

$$
x_{1}=\frac{1}{\sqrt{\prime 2} \alpha} \quad y_{1}=\frac{\alpha}{V^{\prime}-}
$$

and the coördinates of the point $c$ at which the hyperbola is tangent to the unit circle, are

$$
x=y=\frac{\mathrm{I}}{\mathrm{I}^{\prime}}
$$



Fig. 5.
If the hyperbola is conceived as generated by the point $c$ in moving from its original position to $P_{1}$ (or as a "line of flow"), its radius vector sweeps over an hyperbolic sector $o c P_{1}$. If this area is called $\frac{u}{2}$, then by a wellknown formula,

$$
d u=x d y-y d x
$$

and because $x y=\frac{1}{2}$,

$$
d u=\frac{1}{2}\left(\frac{d y}{y}-\frac{d x}{x}\right) .
$$

Since no integration constant is required,

$$
u=\frac{1}{2} \log \frac{y_{1}}{x_{1}}=\frac{1}{2} \log a^{2} \text { or } a=e^{u} .
$$

The area $u$ is the sector $o P_{1} c P_{2}$, where the coördinates of $P_{2}$ are $x_{2}=y_{1}$, and $y_{2}=x_{1}$. It is noteworthy that two other areas, $A P_{1} c P_{2} B$ and $C D P_{1}$ $c P_{2}$, have this same value, for evidently

$$
\int_{x_{1}}^{x_{2}} y d x=\int_{y_{1}}^{y_{2}} x d y=\log \alpha=u .
$$

The length of the chord $P_{1} P_{2}$ is

$$
\sqrt{\left(x_{2}-x_{1}\right)^{2}+\left(y_{1}-y_{2}\right)^{2}}=a-a^{-1},
$$

and half of this, or $P_{1} a$, is the hyperbolic sine which may evidently be put in the form

$$
\sinh u=\frac{e^{u}-e^{-u}}{2}
$$

Since the curve $P_{1} c P_{2}$ is an hyperbola,

$$
\overline{o a^{2}}-\overline{a P_{1}^{2}}=\mathrm{r}
$$

and therefore

$$
o a=\sqrt{1-\sinh ^{2} u}=\frac{e^{u}+e^{-u}}{2}=\cosh u .
$$

The diameters connecting the points of intersection of the unit circle and the ellipse whose axes are $a$ and $a^{-1}$, may be called the isocyclic diameters of the ellipse, because the circle and the ellipse have the same area. These diameters are not conjugate. If the ellipse is conceived as the section on the greatest and least axes of an ellipsoid of unit volume, the isocyclic diameters are the traces of the circular sections of the ellipsoid. The coördinates of one of the points of intersection, say $E$, are

$$
x=\frac{\mathrm{I}}{\sqrt{a^{2}+\mathrm{I}}} ; y=\frac{a}{\sqrt{a^{2}+\mathrm{I}}},
$$

and therefore the angle $\nu$, which the vector $o E$ makes with the major axis of the ellipse, is given by the relation
and it follows that

$$
\tan \nu=a^{-1}=e^{-u},
$$

$$
\tan \left(\frac{\pi}{2}-2 v\right)=\frac{1}{2}(\cot v-\tan v)=\sinh u .
$$

This angle $\left(\frac{\pi}{2}-2 v\right)$ is $g d u$, or the gudermannian of $u$, so that in any
ellipse whatever the angle made by any line parallel to one isocyclic diameter with a perpendicular on the other isocyclis diameter is the gudermannian of the natural logarithm of the semi-major axis, this being expressed in terms of the isocyclic radius, which in the general case is the square root of the product of the semiaxes. ${ }^{1}$ In the diagram the gudermannian $b o b_{1}$ is shown as bisected by the axis of the hyperbola, and it is worth remarking that if the ellipse were to be distorted into a circle by compressing the major axis and elongating the minor axis, the line $o b$ would be brought into coincidence with $o b_{1}$, so that $g d u$ can be defined as the angle through which an isocyclic diameter has swept when the ellipse has been derived from a circle by irrotational plane strain.

The angle $45^{\circ}+\frac{g d u}{2}$ which occurs in the formula for meridional parts is the angle made by either isocyclic diameter of the ellipse with the minor axis, and the tangent of this angle is the semi-major axis $\alpha$.

The twofold relations of the hyperbolic functions to the hyperbola and the ellipse are illustrated in a somewhat different manner in figure 6.

Here the curve $p_{1} c p_{2}$ is an arc of an hyperbola $y^{2}-x^{2}=\mathrm{I}$. If the area of the sector $o p_{1} c p_{2}$ is called $u, a p_{1}=\sinh u$ and $o a=\cosh u$. Make $b c=p_{1} a$ and draw the associated ellipse shown in the diagram. Then the angle $b o c=g d u ; b o=\cosh u$ and

$$
\begin{aligned}
\tan g d u & =\sinh u \\
\sec g d u & =\cosh u \\
\sin g d u & =\tanh u .
\end{aligned}
$$

The ellipse has corresponding properties. Since the gudermannian is the angle between either isocyclic diameter and a line perpendicular to the other, the line $o b$ may be regarded as coinciding with one isocyclic diameter and the axis of abscissas with the other. The major axis of the ellipse then bisects

[^4]the angle $90^{\circ}-g d u$, its magnitude is $2 e^{u}$, and the equation of the ellipse is
$$
x^{2}+4 x y \tan g d u+y^{2}\left(4 \tan ^{2} g d u+1\right)=\mathrm{I} .
$$

By varying the value of $\tan g d u$ (or $\sinh u$ ) a system of ellipses is obtained whose envelopes are $y= \pm \mathrm{I}$, so that if any one of the ellipses is supposed to be derived from the circle by distortion, the process is that generally known as "shearing motion or scission."

If the points in the circle are sought which correspond to the points on the


Fig. 6.
major axis of the ellipsoid, it will be found that the angle between the two positions (the angle of rotation) is equal to the gudermannian. ${ }^{1}$

If instead of the horizontal, the vertical line in figure 6 had been taken as coinciding with the isocyclic diameter of the ellipse, the result would have been the discovery of a system of ellipses whose envelopes are $x= \pm \mathrm{I}$, similar in all respects excepting orientation to that discussed.
${ }^{1}$ Love's Treatise on the Theory of Elasticity, vol. I, p. 43.

## METHODS OF INTERPOLATION.

It is not easy to describe the use of the tables which follow without some notes on the methods of interpolation with reference to which they are arranged. In all of them the argument advances by equal increments, each equal, say, to $\omega$. It is required to find a value of the function $F$ intermediate between two tabulated values, $F_{0}$ and $F_{1}$, corresponding to a fractional value of the argument or to $n \omega$, where $n$ is always less than unity, and preferably less than one-half.

Let $F_{n}$ be the value of the function to be determined ; let $F_{-1}$ and $F_{-2}$ be tabulated values of $F$ immediately preceding $F_{0}$, and let $F_{1}, F_{2}$ be values immediately following $F_{0}$. Denote $F_{1}-F_{0}$ by $a_{1}$, other first differences ( $\Delta^{\prime}$ ) being similarly represented. If also $a_{2}-a_{1}=b_{1}, b_{1}-b_{0}=c_{1}$, etc., the whole system of functions and differences is shown in the following schedule : ${ }^{1}$

| $F$ | $d^{\prime}$ | $d^{\prime \prime}$ | $d^{\prime \prime \prime}$ | $d^{i v}$ | $\Delta^{v}$ | $d^{v i}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $F_{-2}$ |  | $b^{\prime \prime}$ |  | $d^{\prime \prime}$ |  | $f^{\prime \prime}$ |
| $F_{-1}$ | $a^{\prime \prime}$ | $b^{\prime}$ | $c^{\prime \prime}$ | $d^{\prime}$ | $e^{\prime \prime}$ | $f^{\prime}$ |
| $F_{0}$ | $a^{\prime}$ | $b_{0}$ | $c^{\prime}$ | $d_{0}$ | $e^{\prime}$ | $f_{0}$ |
| $F_{1}$ | $a_{1}$ | $b_{1}$ | $c_{1}$ | $d_{1}$ | $e_{1}$ | $f_{1}$ |
| $F_{2}$ | $a_{2}$ | $b_{2}$ | $c_{2}$ | $d_{2}$ | $e_{2}$ | $f_{2}$ |

The most familiar formula of interpolation is due to Newton, and in the above notation it may be written thus:

$$
\begin{gathered}
F_{n}-F_{0}=n a_{1}+\frac{n(n-1)}{2!} b_{1}+\frac{n(n-1)(n-2)}{3!} c_{2} \\
\quad+\frac{n(n-1)(n-2)(n-3)}{4!} d_{2}+\ldots
\end{gathered}
$$

[^5]The coefficients are those of the binomial theorem. This formula is applicable to the first intervals of a series, which is not the case with any other mode of interpolation. It may also be adapted to the last intervals by substituting - $n$ for $n$ and $a^{\prime}, b^{\prime}, c^{\prime \prime}, d^{\prime \prime}, \ldots$ for $a_{1}, b_{1}, c_{2}, d_{2}, \ldots$ In systematic interpolation, such as is involved in the construction of tables, it is usual to employ the more rapidly converging formulas of Stirling or Bessel; but when a computing machine and a table of products are available it is sometimes less laborious to compute an extra term of Newton's formula than to calculate and apply the mean differences called for by the other methods. Both Stirling's and Bessel's formulas can be derived from Newton's by known relations between the several differences.

In Stirling's formula the mean of the first differences next preceding and following $F_{0}$ is made use of instead of only the latter, as in Newton's formula. The third differences are similarly treated, so that $a_{0}, c_{0}$, etc., being new quantities, are defined by

$$
\frac{a^{\prime}+a_{1}}{2}=a_{0} ; \frac{c^{\prime}+c_{1}}{2}=c_{0}, \text { etc. }
$$

These mean values are used in conjunction with the even differences on the same horizontal line with $F_{0}$ in the schedule, and Stirling's formula is

$$
\begin{aligned}
F_{n}-F_{0}= & n a_{0}+\frac{n^{2}}{2!} b_{0}+\frac{n\left(n^{2}-1\right)}{3!} c_{0}+\frac{n^{2}\left(n^{2}-1\right)}{4!} d_{0} \\
& +\frac{n\left(n^{2}-1\right)\left(n^{2}-4\right)}{5!} e_{0}+\ldots
\end{aligned}
$$

To interpolate backward it is only needful to substitute $-n$ for $n$.
In Bessel's formula use is made of mean differences of the even orders, and if $b ; d$, etc., are these means they are defined in terms of the scheduled differences, thus:

$$
\frac{b_{0}+b_{1}}{2}=b ; \frac{d_{0}+d_{1}}{2}=d, \text { etc. }
$$

They are used in conjunction with the simple odd differences $a_{1}, c_{1}$, etc., and the formula is

$$
\begin{gathered}
F_{n}-F_{0}=n a_{1}+\frac{n(n-1)}{2!} b+\frac{n(n-1)\left(n-\frac{1}{2}\right)}{3!} c_{1}+\frac{(n+1) n(n-1(n-2)}{4!} d \\
\\
+\frac{(n+1) n(n-1)(n-2)\left(n-\frac{1}{2}\right)}{5!} e_{1}+\ldots
\end{gathered}
$$

When $n=\frac{1}{2}$, or for interpolation to the middle of an interval, the coefficient of $c_{1}$ vanishes and $F_{n}-F_{0}$ is independent of third differences, which is clearly a great advantage. In general this method is very advantageous when $n$ approaches one-half, while Stirling's formula is preferred for small values of $n$.

When Bessel's formula is used for backward interpolation, it may be written
$F_{-n}-F_{0}=-n a^{\prime}+\frac{n(n-1)}{2!}\left(\frac{b_{0}+b^{\prime}}{2}\right)-\frac{n(n-1)\left(n-\frac{1}{2}\right)}{3!} c^{\prime}+\ldots$, $n$ being taken as positive.

A distinct method of interpolation is founded directly upon Taylor's theorem. If $F_{0}^{\prime} F_{0}^{\prime \prime}$, etc., are the successive derivatives of $F_{0}$, and $\omega$ is the constant increment of the argument, this fundamental theorem may be written
$F_{n}-F_{0}=n \omega F_{0}^{\prime}+\frac{n^{2} \omega^{2} F_{0}^{\prime \prime}}{2!}+\frac{n^{3} \omega^{3} F_{0}^{\prime \prime \prime}}{3!}+\frac{n^{4} \omega^{4} F_{0}^{i v}}{4!}+\ldots \ldots(a)$, and this becomes an interpolation formula when the derivatives are expressed in terms of the differences. This is readily accomplished to any degree of exactness whenever the differences become rigorously or sensibly constant at some particular order and the tabular interval is small relatively to the period of the function. To find the numerical values of the derivatives it is not necessary that the analytical expression of the function should be known ; for, rearranging the terms of the formula of Bessel and Stirling according to ascending powers of $n$ and comparing coefficients,

$$
\begin{array}{rlrl}
\quad \text { (Bessel.) } & & \quad \begin{aligned}
\quad \text { (Stirling.) }
\end{aligned} \\
F_{0}^{\prime} & =\frac{1}{\omega}\left(a_{1}-\frac{1}{2} b+\frac{1}{12} c_{1}+\frac{1}{12} d-\frac{1}{120} e_{1}-\ldots\right) & =\frac{1}{\omega}\left(a_{0}-\frac{1}{6} c_{0}+\frac{1}{30} e_{0}-\ldots\right) \\
F_{0}^{\prime \prime} & =\frac{1}{\omega^{2}}\left(b-\frac{1}{2} c_{1}-\frac{1}{12} d+\frac{1}{24} e_{1}+\ldots\right) & & =\frac{1}{\omega^{2}}\left(b_{0}-\frac{1}{12} d_{0}+\ldots\right) \\
F_{0}^{\prime \prime \prime} & =\frac{1}{\omega^{3}}\left(c_{1}-\frac{1}{2} d+0 \ldots\right) & & =\frac{1}{\omega^{3}}\left(c_{0}-\frac{1}{4} e_{0}+\ldots\right) \\
F_{0}^{i v} & =\frac{1}{\omega^{4}}\left(d-\frac{1}{2} e_{1}-\ldots\right) & & =\frac{1}{\omega^{4}}\left(d_{0}-\ldots\right) \\
F_{0}^{v} & =\frac{1}{\omega^{5}}\left(e_{1}-\ldots\right) & & =\frac{1}{\omega^{5}}\left(e_{0}-\ldots\right) .
\end{array}
$$

Hence, to compute the first derivative, say from Stirling's formula, when the 6 th differences and $\frac{1}{30}$ of the mean of the corresponding third differences are negligible, it is only needful to take the mean of the first differences preceding and following the tabular value of the function, subtract from it onesixth ( $\frac{1}{6}$ ) of the mean of the corresponding third differences, and divide the result by $\omega$.

Newton's formula gives for arguments near the beginning of the series of tabular values :

$$
\begin{aligned}
& F_{0}^{\prime}=\frac{1}{\omega}\left(a_{1}-\frac{1}{2} b_{1}+\frac{1}{3} c_{2}-\frac{1}{4} d_{2}+\frac{1}{5} e_{3}-\ldots\right) \\
& F_{0}^{\prime \prime}=\frac{1}{\omega^{2}}\left(b_{1}-c_{2}+\frac{11}{12} d_{2}-\frac{5}{6} c_{3}+\ldots .\right) \\
& F_{0}^{\prime \prime \prime}=\frac{1}{\omega^{3}}\left(c_{2}-\frac{3}{2} d_{2}+\frac{7}{4} e_{3}-\ldots\right)
\end{aligned}
$$

$$
\begin{aligned}
& F_{0}^{i v}=\frac{1}{\omega^{4}}\left(d_{2}-2 e_{3}+\ldots\right) \\
& F_{0}^{v}=\frac{1}{\omega^{5}}\left(c_{3}-\ldots .\right)
\end{aligned}
$$

and for arguments near the end of the series of tabular values,

$$
\begin{aligned}
& F_{0}^{\prime}=\frac{1}{\omega}\left(a^{\prime}+\frac{1}{2} b^{\prime}+\frac{1}{3} c^{\prime \prime}+\frac{1}{4} d^{\prime \prime}+\frac{1}{5} e^{\prime \prime \prime}+\ldots\right) \\
& F_{0}^{\prime \prime}=\frac{1}{\omega^{2}}\left(b^{\prime}+c^{\prime \prime}+\frac{11}{1} d^{\prime \prime}+\frac{5}{6} e^{\prime \prime \prime}+\ldots\right) \\
& F_{0}^{\prime \prime \prime}=\frac{1}{\omega^{3}}\left(c^{\prime \prime}+\frac{3}{2} d^{\prime \prime}+\frac{7}{4} e^{\prime \prime \prime}+\ldots\right) \\
& F_{0}^{i v}=\frac{1}{\omega^{4}}\left(d^{\prime \prime}+2 e^{\prime \prime \prime}+\ldots .\right) \\
& F_{0}^{v}=\frac{1}{\omega^{5}}\left(e^{\prime \prime \prime}+\ldots . .\right) .
\end{aligned}
$$

The differences of the derivatives may of course be found and discussed in the same manner as those of any other function, and the higher derivatives, $F_{n}{ }^{\prime \prime}, F_{n}{ }^{\prime \prime}$, . . . . . can be expressed in terms of the differences of $F_{n}{ }^{\prime}$. To distinguish the differences of $F^{\prime}$ from those of $F$, they may be denoted by Greek letters, and the notation is exhibited in the following scheme :


Using Stirling's formulæ, page xxxvi, the successive derivatives inclusive of fifth differences are now
$F_{0}^{\prime \prime}=\frac{\mathrm{I}}{\omega}\left(\alpha_{0}-\frac{1}{6} \gamma_{0}\right) ; F_{0}^{\prime \prime \prime}=\frac{\mathrm{I}}{\omega^{2}}\left(\beta_{0}-\frac{1}{12} \delta_{0}\right) ; F_{0}^{i v}=\frac{\mathrm{I}}{\omega^{3}}\left(\gamma_{0}\right) ; F_{0}^{v}=\frac{\mathrm{I}}{\omega^{4}}\left(\delta_{0} ;\right.$
and the interpolation formula may be written
$\left.F_{n}=F_{0}+n \omega F_{0}^{\prime}+\frac{n^{2} \omega}{2!}{ }^{\prime} \alpha_{0}-\frac{1}{6} \gamma_{0}\right)+\frac{n^{3} \omega}{3!}\left(\beta_{0}-{ }_{1} \frac{1}{2} \delta_{0}\right)+\frac{n^{4} \omega}{4!} \gamma_{0}+\frac{n^{5} \omega}{5!} \delta_{0} ;$
or, neglecting fifth differences,

$$
F_{n}=F_{0}+n \omega\left[F_{0}^{\prime}+\frac{n}{2} \alpha_{0}+\frac{n^{2}}{6} \beta_{0}+\frac{n}{12}\left(\frac{n^{2}}{2}-\mathrm{I}\right) \gamma_{0}\right]
$$

and for backward interpolation

$$
F_{-n}=F_{0}-n \omega\left[F_{0}^{\prime}-\frac{n}{2} \alpha_{0}+\frac{n^{2}}{6} \beta_{0}-\frac{n}{12}\left(\frac{n^{2}}{2}-\mathrm{I}\right) \gamma_{0}\right] .
$$

In the tables which follow, the first derivatives multiplied by $\omega$ are tabulated in units of the last decimal place of the tabulated function (except Table VII), and the remaining quantities required in the computation can be found by mere inspection. The higher order of differences will be needed only for a very few arguments at the beginning or end of those tabular values whose numerical magnitudes approach o or $\infty$. For the remaining arguments it will be found that the $\frac{1}{48}$ part of the second difference of $\omega F_{n}^{\prime}$ is not great enough to influence the result, and it is therefore sufficient to use

$$
\left.\begin{array}{l}
F_{n}=F_{0}+n \omega\left(F_{o}^{\prime}+\frac{n}{2} a_{o}\right)  \tag{b}\\
F_{-n}=F_{0}-n \omega\left(F_{\mathrm{o}}^{\prime}-\frac{n}{2} \alpha_{o}\right)
\end{array}\right\}
$$

$\omega \alpha_{0}$ being the mean first difference of $\omega F^{\prime}$ corresponding to $F_{0}$. This formula is rigorous when third differences are zero. In most cases $\frac{n \omega a_{0}}{2}$ can be found mentally, and since $\omega\left(F_{0}^{\prime}+\frac{n}{2} a_{0}\right)$ is here to be regarded as an interpolated value of $\omega F_{o}^{\prime}$, no confusion can arise as to the sign of the correction. It thus becomes almost as easy to include $\omega a_{o}$ in the computation as to omit it. A convenient rule is: Find by linear interpolation the value $\omega F^{\prime}$ for one-half the interval $\left(\frac{n}{2}\right)$; multiply this interpolated value by the entire interval ( $n$ ) and apply the product to the tabular value of the function, either positively or negatively, according as the function is increasing or decreasing. To illustrate the application of this rule, find $\log _{10} \sinh 0.00304$. In this case $n=0.4$ and the table gives

$$
F_{\mathrm{o}}=7.477 \mathrm{I} 2 ; \omega F_{0}^{\prime}=1447,7 ; \omega a_{0}=-48,3
$$

the last two quantities being expressed in units of the fifth decimal place. Interpolating $\omega F^{\prime}$ linearly for one-half the interval,

$$
\omega F_{\frac{n}{2}}^{\prime}=\omega\left(F_{0}^{\prime}+\frac{n}{2} a_{0}\right)=1447,7-0.2 \times 48,3=1438,0
$$

multiplying this value by $n$ and adding the result to the tabular value of the function, there results

$$
F_{n}=1438,0 \times 0.4+7.47712=7.48287
$$

The corresponding difference formula (Bessel's) is

$$
F_{n}=F_{0}+n\left[a_{1}-\frac{(\mathrm{I}-n)}{2} b\right]
$$

The derivative formula ( $b$ ) with two terms has the advantage of being much more convenient than the difference formula, while the accuracy of the two is the same (five-eighths of a unit) when the derivatives are tabulated to the
same order of decimal as the function. In the case of linear interpolation, however, it is in general more accurate to use the differences, the maximum error of the difference formula being one-half of a unit and that of the derivative formula three-fourths of a unit in the next succeeding decimal place. The accuracy of the two formulas is the same when the next succeeding decimal of the derivative is tabulated. The error of the derivative formula is then simply the error of the tabular value, while the error of the difference formula may be $=,>$ or $<$ than that of the tabular value, but is never greater than one-half of a unit.

Interpolation formulas which are applicable only to a single function are rarely advantageous, because as much time is often consumed in looking them up as is saved by employing them ; but some formulas applicable to hyperbolic functions are so simple that when once suggested they can hardly be forgotten. Thus, Taylor's theorem gives at once
$\cosh (u+n \omega)-\cosh u=n \omega \sinh u+\frac{n^{2} \omega^{2}}{2!} \cosh u+\frac{n^{3} \omega^{3}}{3!} \sinh u+\ldots$,
and the form for the sine is of course similar. Again, when, as here, the cosine is tabulated with an argument in terms of radians,

$$
\cos (u+n \omega)-\cos u=-n \omega \sin u-\frac{n^{2} \omega^{2}}{2!} \cos u+\frac{n^{3} \omega^{3}}{3!} \sin u+\ldots
$$

the series for the sine being similar.
So, too,

$$
\begin{aligned}
& \log _{e}(u+n \omega)-\log _{e} u=\log _{e}\left(\mathrm{I}+\frac{n \omega}{u}\right) \\
& \quad=\frac{n \omega}{u}-\frac{1}{2} \frac{n^{2} \omega^{2}}{u^{2}}+\frac{1}{3} \frac{n^{3} \omega^{3}}{u^{3}}-\frac{1}{4} \frac{n^{4} \omega^{4}}{u^{4}}+\ldots \quad\left(\frac{n^{2}}{u^{2}}<\mathrm{I} .\right)
\end{aligned}
$$

Simplest of all is the exponential,

$$
\begin{array}{r}
e^{u+n \omega}-e^{u}=e^{u}\left(e^{n \omega}-\mathrm{I}\right)=e^{u}\left(n \omega+\frac{n^{2} \omega^{2}}{2!}+\frac{n^{3} \omega^{3}}{3!}+\ldots\right) \ldots(c), \\
=e^{u}\left(+0.01 n+0.000,05 n^{2}+0.000,000,167 n^{3}+\ldots\right),(\omega=0.0 \mathrm{I}) \\
=e^{u}\left(+0.001 n+0.000,000,5 n^{2}+\ldots\right) .
\end{array}
$$

The series in $n \omega$ may be replaced by $h$, and this may have any finite value. Especially when a computing machine is available, this formula is easily applied and is, of course, rigorous.

From time to time inverse interpolation by a method more accurate than first differences is called for ; indeed, whenever interpolation of a function by higher differences is needful, it is equally needful that the argument corresponding to a given function should be ascertained by a like process. The method ordinarily pursued in such cases is to estimate two values of the argument, one a little greater and the other a little less than that of the required argument, interpolate corresponding values of the function, and finally interpolate linearly over the reduced interval for a final value of the argument.

Another method consists in interpolating values of the function and its derivatives for an approximate value of the required interval and then computing a correction to this approximate value by means of a reversed Taylor's series. ${ }^{1}$

If second differences only are to be taken into account, the usual method of procedure is to estimate an approximate value of $n$, say $n^{\prime}$, and with this estimated value we interpolate linearly as before and find the value of $\omega F_{\frac{n^{\prime}}{2}}^{\prime}$ corresponding to one-half of the estimated interval $\left(\frac{n^{\prime}}{2}\right)$. Then the required interval $(n)$ is equal to the difference between the given value and the nearest tabular of the function divided by $\omega F_{\frac{n^{\prime}}{2}}^{\prime}$. This method is in fact simply the reverse of the one for direct interpolation. A recomputation is of course necessary if the values of $n$ and $n^{\prime}$ are not practically the same. As an illustration, find $u$ when $\log _{10} \sinh u=7.48287$. We first compute

$$
n^{\prime}=\frac{7.48287-7.47712}{1448,0}=0.4
$$

then the value of $\omega \frac{F_{\frac{n^{\prime}}{2}}^{\prime}}{}$ in terms of the last tabular unit is found as before by linear interpolation to be $1438, \mathrm{o}$. Hence

$$
n=\frac{7.48287-7.47712}{1438,0}=0.40 \text { and } u=0.00304
$$

Since the estimated and computed values of the interval agree, there is no need of a recomputation.

The methods which are based upon an estimated value of the argument are unsystematic and clumsy. It is much better to use a formula which gires the required result by a direct and rigorous method. To find such a formula, divide Taylor's series (eq. a) by $\omega F_{0}^{\prime}$, and put

$$
n_{1}=\frac{F_{n}-F_{0}}{\omega F_{0}^{\prime}} ; f_{2}=\frac{\omega^{2} F_{0}^{\prime \prime}}{2 \omega F_{0}^{\prime \prime}} ; f_{3}=\frac{\omega^{3} F_{0}^{\prime \prime \prime}}{6 \omega F_{0}^{\prime}} ; f_{4}=\frac{\omega^{4} F_{0}^{i \nu}}{24 \omega F_{0}^{i}} ; f_{5}=\frac{\omega^{5} F_{0}^{v}}{120 \omega F_{0}^{\prime}} ;
$$

then the interpolation formula may be written

$$
n_{1}=n+f_{2} n^{2}+f_{3} n^{3}+f_{4} n^{4}+f_{5} n^{5}
$$

Reversing this series in accordance with the relation, ${ }^{2}$

$$
\begin{gathered}
x=\frac{y}{a_{0}}+\frac{y^{2}}{a_{0}^{3}}\left(-a_{1}\right)+\frac{y^{3}}{a_{0}^{5}}\left(-a_{0} a_{2}+2 a_{1}^{2}\right) \\
\quad+\frac{y^{4}}{a_{0}^{7}}\left(-a_{0}^{2} a_{3}+5 a_{0} a_{1} a_{2}-5 a_{1}^{3}\right) \\
+\frac{y^{5}}{a_{0}^{9}}\left(-a_{0}^{3} a_{4}+3 a_{0}^{2}\left(a_{2}^{2}+2 a_{1} a_{3}\right)-2 \mathrm{I} a_{0} a_{1}^{2} a_{2}+14 a_{1}^{4}\right),
\end{gathered}
$$

[^6]which is the reversed series of
$$
y=a_{0} x+a_{1} x^{2}+a_{2} x^{3}+a_{3} x^{4}+a_{4} x^{5}
$$
and rearranging the terms, ${ }^{1}$
\[

$$
\begin{align*}
n=n_{1} & +n_{1}\left[-n_{1} f_{2}+2\left(n_{1} f_{2}\right)^{2}-5\left(n_{1} f_{2}\right)^{3}+14\left(n_{1} f_{2}\right)^{4}+\ldots\right] \\
& +n_{1}^{2}\left[n_{1} f_{3}\left(-1+5\left(n_{1} f_{2}\right)-2 \mathrm{I}\left(n_{1} f_{2}\right)^{2}+. .\right)\right] \\
& +n_{1}^{3}\left[n_{1} f_{4}\left(-\mathrm{I}+6 n_{1} f_{2}\right)+3\left(n_{1} f_{3}\right)^{2}+. . .\right] \\
& +n_{1}^{4}\left[-n_{1} f_{5}+\ldots\right] . . . \tag{d}
\end{align*}
$$
\]

In the actual computation it is convenient to put

$$
r=\frac{n_{1}}{2 \omega F_{0}^{\prime}}
$$

then, when successive values of $\omega F_{n}^{\prime}$ are tabulated in units of the last decimal place, and Stirling's coefficients are used,

$$
\begin{array}{ll}
n_{1} f_{2}=r \omega\left(\alpha_{0}-\frac{1}{6} \gamma_{0}\right) & n_{1} f_{3}=\frac{1}{3} r \omega\left(\beta_{0}-\frac{1}{12} \delta_{0}\right) \\
n_{1} f_{4}=\frac{1}{12} r \omega \gamma_{0} & n_{1} f_{5}=\frac{1}{60} r \omega \delta_{0}
\end{array}
$$

The formula is rigorous inclusive of fifth differences, and does not require the computation of an approximate value of $n$. It is applicable to any function or series of tabulated values whose successive derivatives become evanescent. It is particularly convenient when differences higher than the second are neglected. The formula then becomes

$$
n=n_{1}+n_{1}\left[-r \omega a_{0}+2\left(r \omega a_{0}\right)^{2}-5\left(r \omega a_{0}\right)^{3}+14\left(r \omega a_{0}\right)^{4}\right] .
$$

Since $r \omega \alpha_{0}$ is a very small quantity, the higher powers are seldom needed, and, should they be required, are easily taken into account. As an example, let it be required to find $u$ when $\log _{10} \sinh u=7.48287$. We compute

$$
\begin{aligned}
n_{1} & =\frac{7.48287-7.47712}{1447,7}=0.40 \\
r & =\frac{n_{1}}{2 \omega F_{0}^{\prime}}=\frac{0.40}{2 \times 1447,7}=0.0001
\end{aligned}
$$

and

$$
n_{1} r \omega \alpha_{0}=0.40 \times 0.0001 \times(-48,3)=0.00
$$

Hence $n=n_{1}=0.40$ and $u=0.00304$, the same as obtained by the other method.

When $F_{n}=e^{u}$, it is easily shown, either by means of series $(d)$ or by independent methods, that

$$
\begin{aligned}
& n \omega=\log \left(\mathrm{I}+n_{1} \omega\right) \quad . \quad . \quad . \quad . \quad . \quad . \quad(e) \\
& n=+n_{1}-0.005 n_{1}^{2}+0.000,033 n_{1}^{3}+\ldots \quad(\omega=\mathrm{o.01}) \\
& n=+n_{1}-0.0005 n_{1}^{2}+\ldots \quad(\omega=\mathrm{o.001})
\end{aligned}
$$

These formulæ afford an easy means of finding the natural logarithm of a

[^7]number from the tabular values of $e^{ \pm u}$. Thus, to find the natural logarithm of 0.9642 IO , we compute
$$
n_{1}=\frac{0.9646403-0.9642102}{0.0009646403}=0.44587
$$

Substituting in the last of the above equations

$$
n=0.44587-0.0005 \times(0.45)^{2}=0.44577
$$

hence nat $\log$ of $0.9642102=-0.0364458$.
One of the most important applications of differences is the detection of errors in values tabulated at equal intervals of the argument. It may be shown by substitution in the schedule of differences (page xxxiv) that an error, $+\epsilon$, in $F_{0}$ produces errors in the successive differences of any order which are multiples of $\epsilon$, the law of distribution of the multiples being that of the corresponding coefficients of the binomial theorem, and the signs of the errors being alternately positive and negative. Since some order of differences of every continuous function must vanish, the presence of an error in a tabular value must ultimately result in producing successive differences of a certain order which alternate in sign. A comparison of these differences with the corresponding binomial coefficients enables one to estimate the magnitude of the error. Thus in the series which follows:

| $X$ | $X^{3}$ | $\Delta^{\prime}$ | $4^{\prime \prime}$ | $4^{\prime \prime \prime}$ | $\Delta i v$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I 3 | 2197 |  |  |  |  |
|  |  | 547 |  |  |  |
| 14 | 2744 | $63 \mathrm{I}$ | 84 | 6 |  |
| I 5 | 3375 |  | 90 |  | + 2 |
|  |  | 721 |  | 8 |  |
| 16 | 4096 |  | 98 |  | - 8 |
| 17 | 4915 | 819 | 98 | - | + 12 |
|  |  | 917 |  | 12 |  |
| 18 | 5832 |  | 110 |  | -8 |
|  |  | 1027 |  | 4 | + 2 |
| 19 | 6859 | I I 41 | 114 | 6 | + 2 |
| 20 | 8000 |  | 120 |  |  |
| 2 I | 926I | I 261 |  |  |  |
|  |  |  |  |  |  |

the alternation in sign occurs in the fourth-order differences, and the numerical values are twice the coefficients of $(a+b)^{4}$. Hence there is an error of +2 units in the value 4915. The corrections $-2,+8,-12,+8,-2$ ap. plied to the fourth differences causes them to vanish, and the corrections - 2 , $+6,-6,+2$ applied to the third differences reduces them to a constant.

This method is particularly useful in detecting large accidental errors in a series of observed values and in estimating their magnitudes.

## DESCRIPTION OF TABLES.

Table I is devoted to 5 -place values of the logarithmic hyperbolic sine, cosine, tangent, and cotangent of $u$ expressed in radians. The argument $u$ advances by ten-thousandths from o to O.I, by thousandths from o. I to 3.0 , and by hundredths from 3.0 to 6.0 In this as in all the tables (except Table VII), instead of the first differences, the first derivatives of the functions multiplied by the tabular interval ( $\omega$ ) are tabulated in units of the last decimal place, under the heading $\omega F_{0}{ }^{\prime}$. As noted above, this agrees with much of the most authoritative modern practice and facilitates interpolation. It did not appear worth while to extend the tabulation of the table beyond six radians, because higher values are seldom needed ; but in Table IV a few very high values of $e^{ \pm u}$ are given, from which in case of need the hyperbolic functions can be found.

In Table II the natural values of the hyperbolic functions are tabulated for the same arguments as in Table I. In some instances the values are given to one or to two places of decimals more than would be obtained by taking the inverse logarithms of the preceding table.

Table III gives $\sin u=-i \sinh i u$ and $\cos u=\cosh i u$ with their logarithms to 5 decimal places, the argument $u$ being expressed in radians. The tabulation extends from $u=0.0000$ to 0.1000 , and from $u=0.100$ to r. 600 , because $90^{\circ}=1.5707963$ radians; so that, this value of $\frac{\pi}{2}$ being borne in mind, the table affords the means of finding the sine or cosine of any arc expressed in radians.

Independently of hyperbolic functions, this table is often convenient. It also facilitates the computation of the principal hyperbolic functions of complex variables. Thus

$$
\begin{aligned}
& \sinh (u \pm i v)=\sinh u \cos v \pm i \cosh u \sin v \\
& \cosh (u \pm i v)=\cosh u \cos v \pm i \sinh u \sin v
\end{aligned}
$$

and to compute either of these functions it is only needful to take out two tabulated logarithms from Table III, two from Table I, make two additions, and look out two antilogarithms. It is of course conceivable that all the four quantities involved shnuld be tabulated once for all; but even if $u$ and $v$ advanced only by hundredths, such a table would occupy 200 pages. To find from it functions corresponding to $u$ and $v$ expressed in thousandths would require three interpolations-a process quite as laborious as the use of the tables here given.

Space which would otherwise be vacant is utilized to give the angular values of the radian arguments, or a table of conversion of radians from xliii
0.0000 to 0.1000 and from 0.100 to I .600 into degrees, minutes, seconds, and hundredths of a second.

Table IV gives the values of $\log _{10} e^{u}, e^{u}$ and $e^{-u}$ to 7 decimal places from $u=0.000$ to 3.000 and from 3.00 to 6.00 . The values of $e^{u}$ and $e^{-u}$ enter into a vast number of equations representing natural phenomena, especially those (as Cournot remarked) which can be classed under the generic denomination of phenomena of absorption or gradual extinction. The ascending and descending exponentials may be regarded at will either as hyperbolic functions or as independent components of hyperbolic functions, since

$$
e^{ \pm u}=\cosh u \pm \sinh u
$$

while, on the other hand,

$$
\begin{aligned}
& \sinh u=\frac{e^{u}-e^{-u}}{2} ; \cosh u=\frac{e^{u}+e^{-u}}{2} ; \\
& \tanh u=\frac{e^{u}-e^{-u}}{e^{u}+e^{-u}} ; \operatorname{gd} u=2 \tan ^{-1} e^{u}-\frac{\pi}{2} .
\end{aligned}
$$

It is further evident that a table of $e^{ \pm u}$ is a table of natural antilogarithms. Formula $e$ on page xli affords an easy means of obtaining the natural logarithm of a number from the tabular values of $e^{ \pm u}$. It is of course unnecessary to give the derivative of $e^{u}$, since this is $e^{u}$, while the derivative $e^{-u}$ is $-e^{-u}$. In general the interpolation or extrapolation of the function is very easy. (See formula $c$, page xxxix). The logarithm of $e^{-u}$ is not given because, being merely the arithmetical complement of the $\log _{10} e^{u}$, it can be read off as fast as it can be written down.

In any table of $\log _{10} e^{u}$ where the interval of $u$ is $\omega$, the difference of successive logarithms is constant and equal to $\omega \log _{10} e$ or $0.43429448 \omega$. If the logarithm of $e^{u+n \omega}$ is required, this will be

$$
(u+n \omega) \log _{10} e=\log _{10} e^{u}+n \omega \log _{10} e .
$$

Hence it is practicable to prepare an extended table of proportional parts or a table of $n \log _{10} e$ which is applicable to any table of $\log _{10} e^{n}$ when the tabulated values are multiplied by $\omega$. Such an auxiliary table is given at the close of Table IV, in which the argument $\frac{n}{\omega}$ varies from 0.000 to 0.500 . If $\omega$ is unity, this is merely a 5 -place table of $\log _{10} e^{u}$. If, on the other hand, $\omega$ is o.oor, as in the earlier part of Table IV, the auxiliary table gives the increments corresponding to $n$ to 8 places of decimals. Thus, if $\log _{10} e^{0.088245}$ is required, Table IV gives $\log _{10} e^{0.088}=0.0382179$, the auxiliary table gives for $\frac{n}{\omega}=0.245, n \log _{10} e=0.10640$; and since $\omega=0.00 \mathrm{I}, \omega n \log _{10} e=$ 0.00010640, which added to $\log _{10} e^{0.088}$, gives $\log _{10} e^{0.088445}=0.0383243$. In the latter portion of Table IV $\omega$ is only o.or; so that, if the $\log _{10} e^{3.00245}$ is wanted, the main table gives $\log e^{3.00}=\mathrm{I} .3028834$, and $\omega$ times $n \log e$ is o oorio640; so that the required number is I 3039474 .

When $\log _{10} e^{u}$ is required for $u>6.00$ the auxiliary table is insufficient to give 7 -place values. Then the main table, IV, may be used as an auxiliary table. Thus

$$
\begin{aligned}
\log e^{11.088245} & =\log e^{11}+\log e^{0.088245} \\
& =4.7772393+0.0383243=4.8155636 .
\end{aligned}
$$

In the second part of Table IV values of $e^{ \pm u}$ and the logarithms of $e^{u}$ are given, $u$ varying from I to roo. The logarithms are given to io decimals; the other functions to 9 significant figures. Such high values are seldom needed, but are included here lest these tables might some times fail the computer.

Table V gives the natural logarithms of numbers from I to rooo, with their derivatives to 5 places of decimals. These derivatives are merely the reciprocals of the arguments, and since $\log _{e}\left(\frac{I}{y}\right)=-\log _{e} y$, the logarithms of the derivatives are the tabulated logarithms taken negatively. The table thus gives, in addition to the logarithms of 1000 whole numbers, the logarithms of rooo proper fractions lying between o.oor and unity.

The interpolation of natural logarithms is much less simple than is that of common logarithms, and this is the main reason why the latter are preferred for computation. A few simple rules, however, facilitate the needful calculations. When the natural logarithm of a vulgar fraction is required it is best to look out the logarithm of both numerator and denominator and subtract. If the natural logarithm is required of a fractional number stated decimally and less than 21.000 , no attempt should be made to interpolate it directly, because the third differences of the table cannot be neglected for numbers so near the beginning of the table. If the number lies between 10.000 and 21.000 , as, for example, 12.345 , it should be written $123.45 /$ Io, and the required logarithm will be nat $\log 123.45$ - nat $\log$ io. It is safe to interpolate the first of these between nat $\log 123$ and nat $\log 124$, using the formula for second differences. If the number whose logarithm is to be found lies between I and io, as, for example, 8.2468 , it should be written 824.68 / Ioo, so that the required quantity is nat $\log 824.68$ - nat $\log 100$. The first of these logarithms can be found by using only the mean first differences or the tabulated derivatives between the logarithms of 824 and 825. For values of the argument between 21 and 158 interpolation requires the use of second differences, while above i58 average first differences or the first derivative is sufficiently accurate, inasmuch as the error involved is less than half a unit in the fifth decimal place.

It would be possible to interpolate the negative logarithms of the smaller fractions given by the derivatives-that is, from the reciprocal of 159 on to the end of the table, or for numbers between 0.00628 and $0.00100-b u t$ this would not be expedient, because these reciprocals are themselves rounded values. If the natural logarithm of 0.0068352 is wanted as accurately as
the tables will give it, it is best to find the logarithm of 683.52 and to subtract from it the logarithm of roo,000. (See also formula $e$, page xli.)

The use of second differences may be avoided altogether if the computer chooses, for any number not lying between 158 and i,000 may be multiplied and divided by another number which will bring the numerator within these limits. Thus, if, as before, nat $\log 12.345$ is required, this number may be written $246.90 / 20$, and the natural logarithm of the numerator found by help of the derivative, less nat $\log 20$, is the required value.

The awkwardness of a table of natural logarithms is inherent and cannot be overcome by any device. It depends on the fact that $e$ and the base of numeration, the number io, are incommensurable quantities. If our numeration were duodecimal, as it might have been had six fingers to a hand been the rule instead of the exception, i2 would also have been the most convenient base for a table of logarithms. A great table of natural logarithms, such as Barlow's 8 -place table of all numbers from i to io,000, is only a little more convenient than that here offered, and with it, too, it is expedient to multiply any small number by a factor such that the product approaches io,000.

Table VI gives the values of the gudermannian of $u$ to 7 places from $u=0.000$ to $u=3.000$ and from $u=3.00$ to $u=6.00$. In this table $u$ is expressed in radians, and $g d u$ both in radians and in angular measure. For theoretical work the gudermannian in radians is usually the more convenient, but for use in finding hyperbolic functions it must be reduced to an angle.

The gudermannian, $g d u$, is connected with the hyperbolic functions by the following well-known relations:

$$
\begin{aligned}
& \sinh u=\tan g d u ; \cosh u=\sec g d u ; \tanh u=\sin g d u \\
& \tanh \frac{u}{2}=\tan \frac{1}{2} g d u ; u=\log _{e} \tan \left(\frac{\pi}{4}+\frac{1}{2} g d u\right) .
\end{aligned}
$$

Thus Table VI, with the help of a 7 -place table of logarithms of the circular functions, gives 7 -place values of the hyperbolic functions.

The derivative of $g d u$ is sech $u$, and can be used independently of the gudermannian.

Table VII is substantially a reversion of Table VI, and gives the antigudermannian in terms of the gudermannian, both, however, being expressed in minutes and decimals of a minute. If $m$ is the antigudermannian expressed in minutes and $u$ the same function expressed in radians,

$$
m=3437.7468 u=3437.7468 \log _{e} \tan \left(\frac{\pi}{4}+\frac{1}{2} g d u\right)
$$

Table VII is a table of $m$, and if $m$ is multiplied by 0.0002908882 I the product is $u$ in radians. This table is known to navigators as a table of Meridional Parts for a Spherical Globe. It is frequently of use in the discussion of physical questions and is the very foundation of navigation with Mercator charts. In the more modern works on navigation, however, the
ellipticity of the meridian is allowed for in computing tables of meridional parts, and consequently this table will probably never be reproduced in a navigator. For this reason it is here preserved for computers who are not engaged in navigation.

To test this table, which is borrowed from Inman, 200 of the values, or one in every 27 entries, were compared with Gudermann's 7-decimal place table of the antigudermanaian in radian measure. In nearly all cases Inman's last figure was confirmed, but in a few instances the last figure is incorrect by a unit. Inquiry into these cases showed that the maximum error detected was less than o oo6 of a minute. Thus the last figure is not absolutely trustworthy, but is near enough to enable the computer to interpolate accurately to 5 places. If 7 places of the antigudermannian are required, they can be found by inverse interpolation in Table VI.

The earlier part of Table VII may be interpolated by first differences without considerable error. At about $84^{\circ} 30^{\prime}$ one-eighth of the second difference becomes approximately half a unit in the last tabulated place, and beyond this point second differences should be taken into account.

Table VIII is a table for converting radians into angular measure and vice versa. A few numerical constants are appended.

## HISTORICAL NOTE.

The first and most important application of the functions now known as hyperbolic was made by Gerhard Mercator (Kremer) when he issued his map on " Mercator's projection," in $\mathbf{1 5 6 9}^{5}$, or, as some say, in 1550 , while Bowditch gives the date as 1566 . To this day substantially all of the deepsea navigation of the world is carried on by the help of this projection, which has been modified only to the extent of correcting the " meridional parts" for the ellipticity of the meridian. Mercator's problem was to find a projection on which the loxodrome should be a straight line. The solution is unique, and for a spherical globe is $\lambda=g d \frac{m}{a}$ where $\lambda$ is the latitude, $m$ the "meridional part," or the ordinate on the projection of a point in latitude $\lambda$, and $a$ is the radius of the sphere. Of course, this relation gives

$$
\frac{m}{a}=\log _{e} \tan \left(\frac{\pi}{4}+\frac{\lambda}{2}\right)
$$

and this Mercator must have tabulated. He published his map without explanation, however, and it was left to Edward Wright in 1599 to state the formula for $m$.
"The actual inventor of the hyperbolic trigonometry," says Professor McMahon, "was Vincenzo Riccati, S. J. (Opuscula ad res Phys. et Math. pertinens, Bononiae, 1757). He adopted the notation Sh. $\phi$, Ch. $\phi$, for the hyperbolic functions and $S c . \phi, C c . \phi$ for the circular ones. He proved the addition theorem geometically, and derived a construction for the solution of a cubic equation. Soon after Daviet de Foncenex showed how to interchange circular and hyperbolic functions by the use of $\sqrt{-1}$, and gave the analogue of de Moivre's theorem, the work resting more on analogy, however, than on clear definition (Reflex. sur les quant. imag., Miscel. Turin Soc., Tom. I). Johann Heinrich Lambert systematized the subject and gave the serial developments and the exponential expressions. He adopted the notation $\sinh u$, etc., and introduced the transcendent angle, now called the gudermannian, using it in computation and in the construction of tables ${ }^{1}$."
C. Gudermann published an important memoir on Potential or Cyclichyperbolic functions in $1830^{2}$, followed by extended tables. In recogni-

[^8]tion of his contributions to the subject, Cayley, in $1862,{ }^{1}$ proposed the name gudermannian ${ }^{2}$ for the angle which Lambert called transcendent, and which had been variously designated by others. Among other more recent works on hyperbolic functions are Siegmund Günther's Lehre von den Hyperbelfunctionen, 188ı, and Mr. James McMahon's Hyperbolic Functions, 4th edition, 1906.

The first large table of hyperbolic functions we have met with is Legendre's table of $\log \tan \left(\frac{\pi}{4}+\frac{\lambda}{2}\right)$ to 12 decimals. The argument advances by increments of 30 minutes, but five differences are tabulated to facilitate interpolation. ${ }^{3}$ Gudermann in 183 I published a table of the same function, using centesimal degrees and advancing by hundredths of a degree $\left(0^{\circ} o^{\prime} 32^{\prime \prime} .4\right)$ from o to an entire quadrant, the function being given to seven decimal places. This was later supplemented by a table advancing by hundredths of a degree from $88^{\circ}$ to $100^{\circ}$, the function being given to eleven decimal places. Gudermann also gave a 9-place table of $\log \cosh u, \log$ $\sinh u$, and log $\tanh u$, from $u=2.000$ to $u=5.000$, and a ro-place table of the same functions from $u=5.00$ to $u=12.00$.

In 1862 Z. F. W. Gronau ${ }^{4}$ published a 5-place table of hyperbolic functions, the argument being the gudermannian $g d u$ in sexagesimal degrees and minutes. He tabulated to this argument $\log \cosh u, \log \sinh u$, and the Briggs logarithm of $\left(\frac{\pi}{4}+\frac{g d u}{2}\right)$ instead of the natural logarithms of this function, following therein a suggestion of Lambert.

In 1890 W. Ligowski issued his Tafeln der Hyperbelfunctionen und der Kreisfunctionen, which is admirably accurate and much the most useful collection of tables of the hyperbolic functions hitherto printed. He filled the gap left by Gudermann by computing $\log \sinh u, \log \cosh u$, and $\log$ $\tanh u$ from $u=0.000$ to 2.000 . These he gives to only 5 places, but in addition he tabulates $g d u$ in degrees, minutes, seconds, and decimals of a second. These values are in all cases sufficiently accurate to enable the computer to take out from an ordinary table of logarithms 7 -place values of the logarithms of $\cosh u$, $\sinh u$, and tanh $u$. The argument ranges from 0.000 to 2.000 and from 2.00 to 6.00 for $g d u$, while $\log \cosh u$ and $\log \sinh u$ are carried up to $u=9.00$. Ligowski also gives the natural functions $\cosh u$, $\sinh u, \cos u$, and $\sin u$ to 6 decimals for values of $u$ in radians from 0.00 to 2.00 , the $\cosh u$ and $\sinh u$ being continued to $u=8.00$. The only fault we can find with Ligowski's tables is that the increments of the argument are sometimes inconveniently large.

[^9]In 1883 F . W. Newman published a 12 place table ${ }^{1}$ of the descending exponential from $u=0.000$ to $u=15.349$, and a 14 -place table of the same function advancing by two-thousandths from 15.350 to 17.298 and by five-thousandths from 17.298 to 27.635 . In the same volume appeared Mr. J. W. L. Glaisher's tables of the ascending and descending exponential to nine significant figures, with ro-place logarithms. The argument advances by onethousandth to o.r; by one-hundredth to 2.00 ; by one-tenth to 10 , and by a single unit to 500 .

Mr. A. Forti's Nuove Tavole delle Funzioni Iperboliche were published in 1892. The hyperbolic sines, cosines, and tangents, together with their logarithms, are given to six decimals from 0.0000 to 0.2000 , from 0.200 to 2.000 , and from 2.00 to 8.00 . Frequent errors, however, of one, two, and three units in the last decimal place practically limit these tables to five places. The gudermannian is tabulated in degrees, minutes, seconds, and tenths of a second, and the logarithms of the arguments are given to seven places.

In the volume here presented the first thousand values of $\log \sinh u, \log$ $\cosh u$, and $\log \tanh u$ have been computed; the remaining values have been taken from the tables of Gudermann or Ligowski. The values of the natural hyperbolic sines and cosines for values of the argument $<0.1$ and of the tangents for arguments $>2.0$ have been computed; the remaining values have been taken from the tables of Forti and Ligowski. A recomputation of a great number of the borrowed values was made in order to obtain the required accuracy. The values of coth $u$ and $\log \operatorname{coth} u$ have been computed.

In Table III the sines and cosines were obtained by interpolation from the 7 -place values of natural sines and cosines given in Hülsse's Vega, where the argument is expressed in angle. The logarithms of the sines and cosines and the angular equivalents of the arguments have been computed.

In Table IV the values of $e^{-u}$ are all taken from Newman's great table. Those of $e^{+u}$ from 0.000 to 0.100 and from I to 100 are from Glaisher's table. The remainder we computed, checking the results by Glaisher's table or by reciprocating. It should be noted that the 7 place table of $e^{u}$ given in Hülsse's edition of Vega is inaccurate and really amounts to no more than a 5 -place table. The logarithms of $e^{u}$ were computed independently of the values of $e^{u}$.

Tables V and VIII are borrowed.
The values of $g d u$ in Table VI in terms of angle are taken from Ligowski, excepting the thousand values between $u=2.000$ and 3.000 . These were interpolated from Ligowski's values ( 2.00 to 3.00 ) with due checks on his accuracy. In preparing the table of $g d u$ in radians it was necessary for us to make an independent computation of this function from $u=0.300$ to $u=3.000$ in order to secure accuracy in the seventh significant figure. The remaining values were derived from Ligowski by converting angles

[^10]into radians. A considerable number of his values, however, were tested by independent computation.

Table VII is borrowed from the Nautical tables of James Inman, revised by James W. Inman, London, I867, with a few small corrections.

Finally, it may be remarked that the derivatives as given in these tables have been computed for them. They are not derived from the differences of the values as printed, but from more extended values, or are computed independently, and the error of the derivatives as well as of the functions is less than one-half of a unit in the next succeeding decimal place.

These tables were prepared in connection with the geophysical work of the United States Geological Survey, and are published with the permission of the Director.

George F. Becker.<br>C. E. Van Orstrand.

[^11]TABLE I

## LOGARITHMS OF HYPERBOLIC FUNCTIONS

Logarithms of Hyperbolic Functions.

| U | lonsinh \% | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega F_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0000 | - $\infty$ | - $\infty$ | 0.00000 | 0,0 | - $\infty$ | $\mp \infty$ | $\infty$ |
| . 0001 | 6.00000 | 43429,4 | . 00000 |  | 6.00000 | 43429,4 | 4.00000 |
| . 0002 | . 30103 | 21714,7 | . 00000 |  | . 30103 | 21714,7 | 3.69897 |
| . 0003 | . 47712 | 14476,5 | . 00000 |  | . 47712 | 14476,5 | . 52288 |
| . 0004 | . 60206 | 10857,4 | . 00000 |  | . 60206 | 10857,4 | . 39794 |
| 0.0005 | 6.69897 | 8685,9 | 0.00000 | 0,0 | 6.69897 | 8685,9 | $3 \cdot 30103$ |
| . 0006 | .778I5 | 7238,2 | . 00000 |  | .77815 | 7238,2 | . 22185 |
| . 0007 | . 84510 | 6204,2 | . 00000 |  | . 84510 | 6204,2 | . 15490 |
| . 0008 | . 90309 | 5428,7 | . 00000 |  | . 90309 | 5428,7 | . 09691 |
| . 0009 | . 95424 | 4825,5 | . 00000 |  | . 95424 | 4825,5 | . 04576 |
| 0.0010 | 7.00000 | 4342,9 | 0.00000 | 0,0 | 7.00000 | 4342,9 | 3.00000 |
| . 0011 | .04I39 | 3948, I | . 00000 |  | .04139 | 3948, 1 | 2.95861 |
| . 0012 | . 07918 | 3619,1 | . 00000 |  | . 07918 | 3619, 1 | . 92082 |
| .0013 | . II394 | 3340,7 | . 00000 |  | . II 394 | 3340,7 | . 88606 |
| .0014 | . 14613 | 3102,1 | . 00000 |  | . 14613 | 3102,1 | .85387 |
| 0.0015 | 7.17609 | 2895,3 | 0.00000 | 0,0 | 7.17609 | 2895,3 | 2.82391 |
| . 0016 | . 20412 | 2714,3 | . 00000 |  | . 20412 | 2714,3 | . 79588 |
| .0017 | . 23045 | 2554,7 | . 00000 |  | . 23045 | 2554,7 | . 76955 |
| .0018 | . 25527 | 2412,7 | . 00000 |  | . 25527 | 2412,7 | . 74473 |
| .0019 | . 27875 | 2285,8 | . 00000 |  | . 27875 | 2285,8 | . 72125 |
| 0.0020 | 7.30103 | 2171,5 | 0.00000 | 0,0 | 7.30103 | 2171,5 | 2.69897 |
| .002I | . 32222 | 2068, 1 | . 00000 |  | . 32222 | 2068, I | . 67778 |
| . 0022 | . 34242 | 1974, 1 | . 00000 |  | - 34242 | 1974, I | . 65758 |
| . 0023 | -36I73 | 1888,2 | . 00000 |  | . 36173 | 1888,2 | . 63827 |
| . 0024 | .3802 I | I809,6 | . 00000 |  | .3802I | 1809,6 | . 61979 |
| 0.0025 | $7 \cdot 39794$ | 1737,2 | 0.00000 | 0,0 | 7.39794 | 1737,2 | 2.60206 |
| . 0026 | . 41497 | 1670,4 | . 00000 |  | . 41497 | 1670,4 | . 58503 |
| . 0027 | . 43136 | 1608,5 | . 00000 |  | . 43136 | 1608,5 | . 56864 |
| . 0028 | . 44716 | I551, I | . 00000 |  | . 44716 | 1551,0 | . 55284 |
| . 0029 | . 46240 | 1497,6 | . 00000 |  | . 46240 | 1497,6 | - 53760 |
| 0.0030 | 7.47712 | I447,7 | 0.00000 | 0,0 | 7.47712 | 1447,6 | 2.52288 |
| .003I | . 49136 | I40I, 0 | . 00000 |  | . 49136 | I400,9 | . 50864 |
| . 0032 | . 50515 | 1357,2 | . 00000 |  | . 50515 | 1357,2 | . 49485 |
| . 0033 | . 5185 I | I 316,0 | . 00000 |  | . 51851 | 1316,0 | . 48149 |
| . 0034 | . 53148 | 1277,3 | . 00000 |  | . 53148 | 1277,3 | . 46852 |
| 0.0035 | 7.54407 | I240,8 | 0.00000 | 0,0 | 7.54407 | I240,8 | 2.45593 |
| . 0036 | . 55630 | 1206,4 | . 00000 |  | . 55630 | I206,4 | . 44370 |
| . 0037 | . 56820 | II73,8 | . 00000 |  | . 56820 | 1173,8 | . 43180 |
| . 0038 | . 57978 | I I 42,9 | . 000000 |  | . 57978 | I I 42,9 | . 42022 |
| . 0039 | . 59107 | III3,6 | . 00000 |  | . 59106 | I I I 3,6 | . 40894 |
| 0.0040 | 7.60206 | 1085,7 | 0.00000 | 0,0 | 7.60206 | 1085,7 | 2.39794 |
| . 0041 | . 61279 | 1059,3 | . 00000 |  | . 61278 | 1059,2 | - 38722 |
| . 0042 | . 62325 | 1034,0 | . 00000 |  | . 62325 | 1034,0 | - 37675 |
| . 0043 | . 63347 | 1010,0 | . 00000 |  | . 63347 | IOIO,O | - 36653 |
| . 0044 | . 64345 | 987,0 | . 00000 |  | . 64345 | 987,0 | - 35655 |
| 0.0045 | 7.65321 | 965, I | 0.00000 | 0,0 | 7.65321 | 965, I | 2.34679 |
| . 0046 | . 66276 | 944, I | . 00000 |  | . 66275 | 944, I | - 33725 |
| . 0047 | . 67210 | 924,0 | . 00000 |  | . 67209 | 924,0 | - 32791 |
| . 0048 | .68124 | 904,8 | . 00001 |  | . 68124 | 904,8 | - 31876 |
| . 0049 | . 69020 | 886,3 | . 0000 I |  | . 69019 | 886,3 | -3098I |
| 0.0050 | 7.69897 | 868,6 | 0.00001 | 0,0 | 7.69897 | 868,6 | $2 \cdot 30103$ |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \mathbf{c s c} \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0050 | 7.69897 | 868,6 | 0.00001 | 0,0 | 7.69897 | 868,6 | 2.30103 |
| .005I | . 70757 | 851,6 | .0000I |  | . 70757 | $85 \mathrm{I}, 5$ | . 29243 |
| . 0052 | . 71601 | 835,2 | .0000I |  | . 71600 | 835,2 | . 28400 |
| . 0053 | . 72428 | 819,4 | . 00001 |  | . 72427 | 819,4 | . 27573 |
| . 0054 | .73240 | 804,3 | . 00001 |  | . 73239 | 804,2 | . 26761 |
| 0.0055 | 7.74036 | 789,6 | 0.00001 | 0,0 | 7.74036 | 789,6 | 2.25964 |
| . 0056 | .74819 | 775,5 | .0000I |  | .74818 | 775,5 | . 25182 |
| . 0057 | . 75588 | 761,9 | .00001 |  | . 75587 | 761,9 | . 24413 |
| . 0058 | . 76343 | 748,8 | . 00001 |  | . 76342 | 748,8 | . 23658 |
| . 0059 | . 77085 | 736,1 | .0000I |  | .77085 | 736,1 | . 22915 |
| 0.0060 | 7.77815 | 723,8 | 0.00001 | 0,0 | 7.77815 | 723,8 | 2.22185 |
| . 0061 | . 78533 | 712,0 | .0000I |  | . 78532 | 711,9 | . 21468 |
| . 0062 | . 79239 | 700,5 | .0000I |  | . 79239 | 700,5 | . 20761 |
| . 0063 | . 79934 | 689,4 | .0000I |  | . 79933 | 689,3 | . 20067 |
| . 0064 | . 80618 | 678,6 | . 0000 I |  | . 80617 | 678,6 | . 19383 |
| 0.0065 | 7.81292 | 668, I | 0.00001 | 0,0 | 7.81291 | 668, 1 | 2. 18709 |
| . 0066 | .81955 | 658,0 | . 00001 |  | .81954 | 658,0 | . 18046 |
| . 0067 | . 82608 | 648,2 | . 00001 |  | . 82607 | 648,2 | . 17393 |
| . 0068 | . 83251 | 638,7 | .0000I |  | . 83250 | 638,6 | . 16750 |
| . 0069 | . 83885 | 629,4 | . 0000 I |  | . 83884 | 629,4 | . I6II6 |
| 0.0070 | 7.84510 | 620,4 | 0.00001 | 0,0 | 7.84509 | 620,4 | 2.15491 |
| . 0071 | . 85126 | 6II,7 | .0000I |  | . 85125 | 611,7 | . 14875 |
| . 0072 | . 85734 | 603,2 | .00001 |  | . 85732 | 603,2 | . I 4268 |
| . 0073 | . 86333 | 594,9 | .0000I |  | . 86332 | 594,9 | . I3668 |
| . 0074 | . 86924 | 586,9 | .0000I |  | . 86922 | 586,9 | . 13078 |
| 0.0075 | 7.87507 | 579, I | 0.00001 | 0,0 | 7.87505 | 579,0 | 2.12495 |
| .0076 | . 88082 | 571,4 | . 00001 |  | .88081 | 571,4 | . II919 |
| . 0077 | . 88649 | 564,0 | . 00001 |  | . 88648 | 564,0 | . II352 |
| . 0078 | . 89210 | 556,8 | . 00001 |  | . 89209 | 556,8 | . 10791 |
| . 0079 | . 89763 | 549,7 | .0000I |  | . 89762 | 549,7 | . 10238 |
| 0.0080 | 7.90309 | 542,9 | 0.00001 | 0,0 | 7.90308 | 542,8 | 2.09692 |
| .008I | . 90849 | 536,2 | .0000I |  | . 90848 | 536, I | . 09152 |
| . 0082 | .91382 | 529,6 | .0000I |  | .91380 | 529,6 | . 08620 |
| . 0083 | .91908 | 523,2 | . 00001 |  | . 91907 | 523,2 | . 08093 |
| . 0084 | . 92428 | 517,0 | . 00002 |  | . 92427 | 517,0 | . 07573 |
| 0.0085 | 7.92942 | 510,9 | 0.00002 | 0,0 | 7.92941 | 510,9 | 2.07059 |
| . 0086 | . 93450 | 505,0 | . 00002 |  | . 93449 | 505,0 | .0655I |
| . 0087 | . 93952 | 499,2 | . 00002 |  | .9395I | 499,2 | . 06049 |
| . 0088 | . 94449 | 493,5 | . 00002 |  | . 94447 | 493,5 | . 05553 |
| . 0089 | . 94940 | 488,0 | . 00002 |  | . 94938 | 487,9 | . 05062 |
| 0.0090 | 7 7.95425 | 482,6 | 0.00002 | 0,0 | 7.95423 | 482,5 | 2.04577 |
| .0091 | . 95905 | 477,3 | . 00002 |  | . 95903 | 477,2 | . 04097 |
| . 0092 | . 96379 | 472, I | . 00002 |  | . 96378 | 472,0 | . 03622 |
| . 0093 | . 96849 | 467,0 | . 00002 |  | . 96847 | 467,0 | .03153 |
| . 0094 | .97313 | 462,0 | . 00002 |  | . 97312 | 462,0 | . 02688 |
| 0.0095 | 7.97773 | 457,2 | 0.00002 | 0,0 | 7.97771 | 457,I | 2.02229 |
| . 0096 | . 98228 | 452,4 | . 00002 |  | . 98226 | 452,4 | . 01774 |
| . 0097 | . 98678 | 447,7 | . 00002 |  | . 98676 | 447,7 | . OI324 |
| . 0098 | . 99123 | 443,2 | . 00002 |  | . 99121 | 443, I | . 00879 |
| . 0099 | . 99564 | 438,7 | . 00002 |  | . 99562 | 438,7 | . 00438 |
| 0.0100 | 8.00001 | 434,3 | 0.00002 | 0,0 | 7.99999 | 434,3 | 2.00001 |
| u | $\log \tan g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0100 | 8.00001 | 434,3 | 0.00002 | 0,0 | 7.99999 | 434,3 | 2.00001 |
| . OIOI | . 00433 | 430,0 | . 00002 |  | 8.0043 I | 430,0 | 1.99569 |
| . 0102 | .0086I | 425,8 | . 00002 |  | . 00859 | 425,7 | .99141 |
| . 0103 | . 01284 | 421,7 | . 00002 |  | . 01282 | 42I,6 | .98718 |
| . 0104 | . 01704 | 417,6 | . 00002 |  | . 01702 | 417,6 | . 98298 |
| 0.0105 | 8.02120 | 413,6 | 0.00002 | 0,0 | 8.02117 | 413,6 | 1.97883 |
| . 0106 | .02531 | 409,7 | . 00002 |  | . 02529 | 409,7 | . 97471 |
| . 0107 | . 02939 | 405,9 | . 00002 |  | . 02937 | 405,9 | . 97063 |
| . 0108 | . 03343 | 402, I | . 00003 |  | .0334I | 402,1 | . 96659 |
| . 0109 | . 03744 | 398,5 | . 00003 |  | .0374I | 398,4 | . 96259 |
| 0.0110 | 8.04140 | 394,8 | 0.00003 | 0,0 | 8.04138 | 394,8 | 1. 95862 |
| .OIII | . 04533 | 391,3 | . 00003 |  | .04531 | 391,2 | . 95469 |
| . OII2 | . 04923 | 387,8 | . 00003 |  | . 04920 | 387,7 | . 95080 |
| . OII3 | . 05309 | 384,4 | . 00003 |  | . 05306 | 384,3 | . 94694 |
| . OII4 | .05691 | 38I,0 | . 00003 |  | . 05689 | 380,9 | .943II |
| 0.0115 | 8.06071 | 377,7 | 0.00003 | 0,0 | 8.06068 | 377,6 | I. 93932 |
| . OI 16 | . 06447 | 374,4 | . 00003 | 0,I | . 06444 | 374,4 | . 93556 |
| . 0117 | . 06820 | 371,2 | . 00003 |  | .06817 | 371,2 | .93183 |
| . 0118 | . 07189 | 368, 1 | . 00003 |  | .07186 | 368,0 | .928I4 |
| . 0119 | . 07556 | 365,0 | . 00003 |  | . 07553 | 364,9 | . 92447 |
| 0.0120 | 8.07919 | 361,9 | 0.00003 | O,I | 8.07916 | 361,9 | 1.92084 |
| . 0121 | . 08280 | 358,9 | . 00003 |  | . 08276 | 358,9 | . 91724 |
| . 0122 | . 08637 | 356,0 | . 00003 |  | . 08634 | 355,9 | .91366 |
| . 0123 | . 08992 | 353, I | . 00003 |  | . 08988 | 353,0 | .91012 |
| . 0124 | . 09343 | 350,3 | . 00003 |  | . 09340 | 350,2 | . 90660 |
| 0.0125 | 8.09692 | 347,5 | 0.00003 | O,I | 8.09689 | 347,4 | 1.903II |
| . 0126 | . 10038 | 344,7 | . 00003 |  | . 10035 | 344,6 | . 89965 |
| . 0127 | . 10382 | 342,0 | . 00004 |  | . 10378 | 341,9 | . 89622 |
| . 0128 | . 10722 | 339,3 | . 00004 |  | . 10719 | 339,3 | . 8928 I |
| . 0129 | . 11060 | 336,7 | . 00004 |  | . 11057 | 336,6 | . 88943 |
| 0.0130 | 8.11396 | 334, I | 0.00004 | O,I | 8.11392 | 334,0 | I. 88608 |
| .OI3I | . II728 | 33I,5 | . 00004 |  | . II725 | 331,5 | . 88275 |
| .OI32 | . 12059 | 329,0 | . 00004 |  | . 12055 | 329,0 | . 87945 |
| . OI33 | . 12386 | 326,6 | . 00004 |  | . 12383 | 326,5 | . 87617 |
| . 0134 | . 12712 | 324, I | . 00004 |  | . 12708 | 324, I | . 87292 |
| 0.0135 | 8. I3035 | 321,7 | 0.00004 | 0,I | 8.1303I | 331,7 | 1. 86969 |
| . 0136 | . I3355 | 319,4 | . 00004 |  | . I335I | 319,3 | . 86649 |
| . 0137 | . I3673 | 317,0 | . 00004 |  | . I3669 | 317,0 | .8633I |
| . 0138 | . I3989 | 314,7 | . 000004 |  | . I3985 | 314,7 $3 \mathrm{I} 2,4$ | . 86015 |
| . 0139 | . 14303 | 312,5 | . 00004 |  | . 14299 | 312,4 | .8570I |
| 0.0140 | 8.14614 | 310,2 | 0.00004 | O,I | 8.14610 | 310,2 | 1. 85390 |
| . 0174 | . 14923 | 308,0 | . 00004 |  | . 14919 | 308,0 | . 85081 |
| . 0142 | . 15230 | 305,9 | .00004 |  | . 15226 | 305,8 | . 84774 |
| . 0143 | . 15535 | 303,7 | . 00004 |  | . I553I | 303,7 | . 84469 |
| . 0144 | . 15838 | 301,6 | . 00005 |  | . 15833 | 301,6 | . 84167 |
| 0.0145 | 8.16138 | 299,5 | 0.00005 | O,I | 8. 16134 | 299,5 | 1.83866 |
| . 0146 | . 16437 | 297,5 | . 00005 |  | . 16432 | 297,4 | . 83568 |
| . 0147 | . 16733 | 295,5 | . 00005 |  | . 16729 | 295,4 | . 83271 |
| . 0148 | .17028 .17320 | 293,5 | . 000005 |  | .17023 .17315 | 293,4 | . 82977 |
| . 0149 | . 17320 | 291,5 | . 00005 |  | . 17315 | 291,4 | . 8268 |
| 0.0150 | 8.176II | 289,6 | 0.00005 | 0,I | 8.17606 | 289,5 | I. 82394 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathbf{u}$ |

Smithsonian Tables

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0150 | 8.176II | 280,6 | 0.00005 | O, I | 8. 17606 | 289,5 | I. 82394 |
| . 0151 | . 17899 | 287,6 | . 00005 |  | . 17894 | 287,6 | .82106 |
| .OI52 | . 18186 | 285,7 | . 00005 |  | . 18181 | 285,7 | .8I8I9 |
| . 0153 | . 18471 | 283,9 | . 00005 |  | . 18466 | 283,8 | .81534 |
| . 0154 | . 18754 | 282,0 | . 00005 |  | . 18749 | 282,0 | .8I25I |
| 0.0155 | 8.19035 | 280,2 | 0.00005 | O,I | 8. 19030 | 280, 1 | 1. 80970 |
| . 0156 | . 193I4 | 278,4 | . 00005 |  | . 19309 | 278,3 | . 80691 |
| . 0157 | . 19592 | 276,6 | .00005 |  | . 19586 | 276,6 | . 80414 |
| .or58 | . 19868 | 274,9 | .00005 |  | . 19862 | 274,8 | . 80138 |
| . 0159 | . 20142 | 273,2 | . 00005 |  | . 20136 | 273, I | . 79864 |
| 0.0160 | 8.20414 | 271,5 | 0.00006 | O,I | 8.20408 | 271,4 | I. 79592 |
| . 0161 | . 20684 | 269,8 | . 00006 |  | . 20679 | 269,7 | . 79321 |
| .0162 | . 20953 | 268, I | . 00006 |  | . 20948 | 268,0 | . 79052 |
| . 0163 | . 21221 | 266,5 | . 00006 |  | . 21215 | 266,4 | . 78785 |
| . 0164 | . 21486 | 264,8 | . 00005 |  | . 21480 | 264,8 | . 78520 |
| 0.0165 | 8.21750 | 263,2 | 0.00005 | 0,1 | 8.21744 | 263,2 | 1. 78256 |
| . .0166 | . 22013 | 261,6 | . 00006 |  | . 22007 | 261,6 | . 77993 |
| . 0167 | . 22274 | 260, 1 | . 00006 |  | . 22268 | 260,0 | . 77732 |
| . 0168 | . 22533 | 258,5 | . 00006 |  | . 22527 | 258,5 | . 77473 |
| . 0169 | . 2279I | 257,0 | . 00006 |  | . 22785 | 256,9 | . 77215 |
| 0.0170 | 8.23047 | 255,5 | 0.00006 | O,I | 8.23041 | 255,4 | 1.76959 |
| . O171 | . 23302 | 254,0 | . 00006 |  | . 23295 | 253,9 | . 76705 |
| . O172 | . 23555 | 252,5 | . 00006 |  | . 23549 | 252,4 | . 76451 |
| . 0173 | . 23807 | 251, I | .00006 |  | . 23800 | 251,0 | . 76200 |
| . 0174 | . 24057 | 249,6 | . 00007 |  | . 2405 I | 249,5 | . 75949 |
| 0.0175 | 8.24306 | 248,2 | 0.00007 | O,I | 8.24299 | 248, I | 1.75701 |
| . $0176{ }^{\text {a }}$ | . 24554 | 246,8 | . 00007 |  | . 24547 | 246,7 | . 75453 |
| . 0177 | . 24800 | 245,4 | . 00007 |  | . 24793 | 245,3 | . 75207 |
| . 0178 | . 25044 | 244,0 | . 00007 |  | .25037 | 243,9 | - 74963 |
| . 0179 | . 25288 | 242,6 | . 00007 |  | .2528I | 242,6 | . 74719 |
| 0.0180 | 8.25530 | 241,3 | 0.00007 | O,I | 8.25523 | 241,2 | I. 74477 |
| . 0181 | . 25770 | 240,0 | . 00007 |  | . 25763 | 239,9 | . 74237 |
| . 0182 | . 26010 | 238,6 | . 00007 |  | . 26002 | 238,6 | . 73998 |
| . 0183 | . 26248 | 237,3 | . 00007 |  | . 26240 | 237,3 | . 73760 |
| . 0184 | . 26484 | 236, I | . 00007 |  | . 26477 | 236,0 | . 73523 |
| 0.0185 | 8.26720 | 234,8 | 0.00007 | O,I | 8.26712 | 234,7 | 1. 73288 |
| . 0186 | . 26954 | 233,5 | . 00008 |  | . 26946 | 233,4 | . 73054 |
| . 0187 | . 27187 | 232,3 | . 00008 |  | .27179 | 232,2 | . 72821 |
| . 0188 | . 27418 | 231,0 | . 00008 |  | .274II | 231,0 | . 72589 |
| . 0189 | . 27649 | 229,8 | . 00008 |  | .2764I | 229,7 | . 72359 |
| 0.0190 | 8.27878 | 228,6 | 0.00008 | O, I | 8.27870 | 228,5 | 1.72130 |
| . O19I | .28106 | 227,4 | . 00008 |  | . 28098 | 227,3 | . 71902 |
| . 0192 | . 28333 | 226,2 | . 00008 |  | . 28325 | 226, I | . 71675 |
| . 0193 | . 28558 | 225, I | . 00008 |  | . 28550 | 225,0 | . 71450 |
| . 0194 | . 28783 | 223,9 | . 00008 |  | . 28775 | 223,8 | .71225 |
| 0.0195 | 8.29006 | 222,7 | 0.00008 | O, I | 8.28998 | 222,7 | 1.71002 |
| . 0196 | . 29228 | 221,6 | . 00008 |  | . 29220 | 22I,5 | . 70780 |
| . 0197 | . 29449 | 220,5 | . 00008 |  | . 29441 | 220,4 | . 70559 |
| . 0198 | . 29669 | 219,4 | . 00009 |  | .2966I | 219,3 | . 70339 |
| . 0199 | . 29888 | 218,3 | . 00009 |  | . 29880 | 218,2 | . 70120 |
| 0.0200 | 8.30106 | 217,2 | 0.00009 | O, I | 8.30097 | 217, 1 | 1.69903 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }}$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0200 | 8.30106 | 217,2 | 0.00009 | O,I | 8.30097 | 217,1 | 1.69903 |
| .0201 | . 30323 | 216,1 | . 00009 |  | -30314 | 216,0 | . 69686 |
| . 0202 | . 30538 | 215,0 | . 00009 |  | . 30529 | 214,9 | . 6947 I |
| . 0203 | . 30753 | 214,0 | . 00009 |  | . 30744 | 213,9 | . 69256 |
| . 0204 | . 30966 | 212,9 | . 00009 |  | - 30957 | 212,8 | . 69043 |
| 0.0205 | 8.31178 | 2II,9 | 0.00009 | O,I | 8.31169 | 2II,8 | 1.68831 |
| . 0206 | . 31390 | 210,9 | . 00009 |  | . 3138 I | 210,8 | . 686I9 |
| . 0207 | . 31600 | 209,8 | . 00009 |  | .3159I | 209,7 | . 68409 |
| . 0208 | .31809 | 208,8 | . 00009 |  | . 31800 | 208,7 | . 68200 |
| . 0209 | -32018 | 207,8 | . 00009 |  | . 32008 | 207,7 | . 67992 |
| 0.0210 | 8.32225 | 206,8 | 0.00010 | O,I | 8.32216 | 206,7 | 1. 67784 |
| .0211 | . 3243 I | 205,9 | .00010 |  | . 32422 | 205,8 | . 67578 |
| . 0212 | . 32637 | 204,9 | .00010 |  | . 32627 | 204,8 | . 67373 |
| . 0213 | . 3284 I | 203,9 | . 00010 |  | . 32831 | 203,8 | . 67169 |
| . 0214 | . 33045 | 203,0 | . 00010 |  | . 33035 | 202,9 | . 66965 |
| 0.0215 | 8.33247 | 202,0 | 0.00010 | O,I | 8.33237 | 201,9 | r. 66763 |
| . 0216 | . 33449 | 201, I | . 00010 |  | . 33439 | 201,0 | . 66561 |
| . 0217 | . 33649 | 200,2 | .00010 |  | . 33639 | 200, I | . 66361 |
| . 0218 | . 33849 | 199,2 | .00010 |  | . 33839 | 199,2 | . 66161 |
| . 0219 | - 34048 | 198,3 | .00010 |  | - 34037 | 198,2 | . 65963 |
| 0.0220 | 8.34246 | 197,4 | 0.00011 | O, I | 8.34235 | 197,3 | 1. 65765 |
| .022I | . 34443 | 196,5 | .0001 I |  | . 34432 | 196,4 | . 65568 |
| . 0222 | . 34639 | 195,7 | .000I I |  | . 34628 | 195,6 | . 65372 |
| . 0223 | - 34834 | 194,8 | .0001 I |  | . 34823 | 194,7 | . 65177 |
| . 0224 | - 35028 | 193,9 | .000II |  | . 35018 | 193,8 | . 64982 |
| 0.0225 | 8.35222 | 193, 1 | 0.00011 | O,I | 8.352II | 193,0 | 1. 64789 |
| . 0226 | . 35415 | 192,2 | .000I I |  | . 35403 | 192, I | . 64597 |
| . 0227 | . 35606 | 191,4 | .0001 I |  | . 35595 | 191,3 | . 64405 |
| . 0228 | - 35797 | 190,5 | . 0001 I |  | . 35786 | 190,4 | . 64214 |
| . 0229 | -35987 | 189,7 | .000I I |  | - 35976 | 189,6 | .64024 |
| 0.0230 | 8.36177 | 188,9 | 0.00011 | O,I | 8.36165 | 188,8 | 1.63835 |
| . 0231 | . 36365 | 188,0 | .00012 |  | . 36353 | 187,9 | . 63647 |
| . 0232 | . 36553 | 187,2 | .00012 |  | . 36541 | 187, 1 | . 63459 |
| . 0233 | - 36740 | 186,4 | .00012 |  | . 36728 | 186,3 | . 63272 |
| . 0234 | . 36926 | 185,6 | .00012 |  | . 36914 | 185,5 | . 63086 |
| 0.0235 | 8.37 III | 184,8 | 0.00012 | O,I | 8.37099 | 184,7 | 1.62901 |
| . 0236 | . 37295 | 184, 1 | .00012 |  | . 37283 | 184,0 | . 62717 |
| . 0237 | - 37479 | 183,3 | .00012 |  | . 37467 | 183,2 | . 62533 |
| . 0238 | . 37662 | 182,5 | .00012 |  | . 37649 | 182,4 | . 62351 |
| . 0239 | - 37844 | 181,7 | .00012 |  | . 37832 | 181,6 | . 62168 |
| 0.0240 | 8.38025 | 181,0 | 0.00013 | O, I | 8.38013 | 180,9 | I. 61987 |
| .024I | . 38206 | 180,2 | . 00013 |  | .38193 | 180, 1 | .61807 |
| . 0242 | . 38386 | 179,5 | .00013 |  | . 38373 | 179,4 | . 61627 |
| . 0243 | . 38565 | 178,8 | .00013 |  | . 38552 | 178,7 | . 61448 |
| . 0244 | . 38743 | 178,0 | .00013 |  | . 38730 | 177,9 | .61270 |
| 0.0245 | 8.3892 I | 177,3 | 0.00013 | O,I | 8.38908 | 177,2 | 1.61092 |
| . 0246 | . 39098 | 176,6 | .00013 |  | . 39085 | 176,5 | . 60915 |
| . 0247 | . 39274 | 175,9 | .00013 |  | -3926I | 175,8 | . 60739 |
| . 0248 | . 39450 | 175,2 | . 00013 |  | - 39436 | 175,0 | . 60564 |
| . 0249 | -39624 | 174,5 | .00013 |  | . 3961 I | 174,3 | .60389 |
| 0.0250 | 8.39799 | 173,8 | 0.00014 | O.I | 8,39785 | 173,6 | 1.60215 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{gd}$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0250 | 8.39799 | 173,8 | 0.00014 | O,I | 8.39785 | 173,6 | 1.60215 |
| .025I | -39972 | 173, I | . 00014 |  | - 39958 | 173,0 | . 60042 |
| . 0252 | . 40145 | 172,4 | . 00014 |  | .4013 1 | 172,3 | . 59869 |
| . 0253 | . 40317 | 171,7 | .00014 |  | . 40303 | 171,6 | . 59697 |
| . 0254 | . 40488 | 171,0 | .000I4 |  | . 40474 | 170,9 | . 59526 |
| 0.0255 | 8.40659 | 170,3 | 0.00014 | O,I | 8.40645 | 170,2 | I. 59355 |
| . 0256 | . 40829 | 169,7 | .00014 |  | .408I5 | 169,6 | . 59185 |
| . 0257 | . 40998 | 169,0 | .00014 |  | . 40984 | 168,9 | . 59016 |
| . 0258 | .41167 | 168,4 | .00014 |  | . 41152 | 168,3 | . 58848 |
| . 0259 | . 41335 | 167,7 | . 00015 |  | .41320 | 167,6 | . 58680 |
| 0.0260 | 8.41502 | 167, I | 0.00015 | O,I | 8.41488 | 167,0 | 1. 58512 |
| .0261 | . 41669 | 166,4 | . 00015 |  | . 41654 | 166,3 | . 58346 |
| . 0262 | . 41835 | 165,8 | . 00015 |  | . 41820 | 165,7 | . 58180 |
| . 0263 | . 4200 I | 165,2 | . 00015 |  | . 41986 | 165, I | . 58014 |
| . 0264 | . 42165 | 164,5 | . 00015 |  | . 42150 | 164,4 | . 57850 |
| 0.0265 | 8.42330 | 163,9 | 0.00015 | O, I | 8.42314 | 163,8 | 1. 57686 |
| . 0256 | . 42493 | 163,3 | . 00015 |  | . 42478 | 163,2 | . 57522 |
| . 0267 | . 42656 | 162,7 | . 00015 |  | . 4264 I | 162,6 | . 57359 |
| . 0268 | . 42819 | 162, 1 | . 00016 |  | . 42803 | 162,0 | . 57197 |
| . 0269 | . 42980 | 16I,5 | . 00016 |  | . 42965 | 161,4 | . 57035 |
| 0.0270 | 8.43142 | 160,9 | 0.00016 | O,I | 8.43126 | 160,8 | 1.56874 |
| . 0271 | . 43302 | 160,3 | . 00016 |  | . 43286 | 160,2 | . 56714 |
| . 0272 | . 43462 | I 59,7 | .00016 ${ }^{\circ}$ |  | . 43446 | I 59,6 | . 56554 |
| . 0273 | . 43622 | 159, I | .00016 |  | . 43605 | I 59,0 | . 56395 |
| . 0274 | . 43780 | 158,5 | .00016 |  | . 43764 | 158,4 | . 56236 |
| 0.0275 | 8.43939 | 158,o | 0.00016 | O, I | 8.43922 | 157,8 | I. 56078 |
| . 0276 | . 44096 | 157,4 | . 00017 |  | . 44080 | 157,3 | . 55920 |
| . 0277 | . 44254 | 156,8 | .00017 |  | . 44237 | 156,7 | . 55763 |
| . 0278 | . 44410 | 156,3 | .00017 |  | . 44393 | 156, I | . 55607 |
| . 0279 | . 44566 | 155,7 | . 00017 |  | . 44549 | I 55,6 | . 5545 I |
| 0.0280 | 8.44721 | 155, I | 0.00017 | O,I | 8.44704 | 155,0 | 1. 55296 |
| .028I | . 44876 | 154,6 | . 00017 |  | . 44859 | 154,5 | . 5514 I |
| . 0282 | . 45031 | 154,0 | .00017 |  | .45013 | 153,9 | . 54987 |
| . 0283 | . 45 I84 | I 53,5 | .00017 |  | . 45167 | I 53,4 | . 54833 |
| . 0284 | . 45338 | I 53,0 | .00018 |  | . 45320 | I 52,8 | . 54680 |
| 0.0285 | 8.45490 | 152,4 | 0.00018 | O,I | 8.45473 | 152,3 | I. 54527 |
| . 0286 | . 45643 | 151,9 | .00018 |  | . 45625 | I 51,8 | . 54375 |
| .0287 | . 45794 | I5I, 4 | . 00018 |  | . 45776 | 151,2 | . 54224 |
| . 0288 | . 45945 | 150,8 | .00018 |  | . 45927 | 150,7 | . 54073 |
| . 0289 | . 46096 | 1 50,3 | .00018 |  | . 46078 | 150,2 | . 53922 |
| 0.0290 | 8.46246 | 149,8 | 0.00018 | O, I | 8.46228 | 149,7 | I. 53772 |
| .0291 | . 46395 | 149,3 | .00018 |  | . 46377 | 149,2 | . 53623 |
| . 0292 | . 46544 | 148,8 | . 00019 |  | . 46526 | I48,6 | . 53474 |
| . 0293 | . 46693 | 148,3 | . 00019 |  | . 46674 | I48, 1 | . 53326 |
| . 0294 | .4684I | 147,8 | . 00019 |  | . 46822 | 147,6 | . 53178 |
| 0.0295 | 8.46989 | 147,3 | 0.00019 | O,I | 8.46970 | 147, I | I. 53030 |
| . 0296 | . 47136 | 146,8 | . 00019 |  | . 47116 | 146,6 | . 52884 |
| . 0297 | . 47282 | 146,3 | . 00019 |  | . 47263 | 146, I | . 52737 |
| . 0298 | . 47428 | 145,8 | .00019 |  | . 47409 | 145,7 | . 52591 |
| . 0299 | . 47574 | 145,3 | . 00019 |  | . 47554 | 145,2 | . 52446 |
| 0.0300 | 8.47719 | 144,8 | 0.00020 | O,I | 8.47699 | 144,7 | 1.52301 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc g d u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0300 | 8.47719 | 144,8 | 0.00020 | O,I | 8.47699 | 144,7 | I. 52301 |
| .0301 | . 47863 | 144,3 | . 00020 |  | . 47844 | 141,2 | . 52156 |
| . 0302 | . 48007 | -143,8 | . 00020 |  | . 47987 | 143,7 | . 52013 |
| . 0303 | .48I5I | 143,4 | . 00020 |  | .4813I | I43,2 | . 51869 |
| . 0304 | . 48294 | 142,9 | . 00020 |  | . 48274 | 142,8 | . 51726 |
| 0.0305 | 8.48437 | I42,4 | 0.00020 | O,I | 8.48417 | 142,3 | I. 51583 |
| . 0306 | . 48579 | 142,0 | . 00020 |  | . 48559 | 141,8 | . 51441 |
| . 0307 | . 48721 | I4I,5 | . 00020 |  | . 48700 | 141,4 | - 51300 |
| . 0308 | . 48862 | 141,0 | .0002I |  | .48841 | 140,9 | . 51159 |
| . 0309 | . 49003 | 140,6 | .0002I |  | . 48982 | 140,5 | . 51018 |
| 0.0310 | 8.49143 | I40, I | 0.0002 I | O,I | 8.49122 | I40,0 | I. 50878 |
| .03II | . 49283 | 139,7 | .0002I |  | . 49262 | I 39,6 | . 50738 |
| .03I2 | . 49423 | 139,2 | . 0002 I |  | .4940I | I39, I | . 50599 |
| .0313 | . 49562 | 138,8 | . 0002 I |  | . 49540 | 138,7 | - 50460 |
| .0314 | . 49700 | I38,4 | . 0002 I |  | . 49679 | I38,2 | . 5032 I |
| 0.0315 | 8.49838 | 137,9 | 0.00022 | O,I | 8.49817 | I 37,8 | I. 50183 |
| . 0316 | . 49976 | 137,5 | . 00022 |  | . 49954 | 137,3 | . 50046 |
| .03I7 | . 50113 | 137,0 | . 00022 |  | . 50091 | 136,9 | . 49909 |
| .0318 | . 50250 | 136,6 | . 00022 |  | . 50228 | 136,5 | . 49772 |
| .0319 | . 50386 | 136,2 | . 00022 |  | . 50364 | I36, 1 | . 49636 |
| 0.0320 | 8.50522 | 135,8 | 0.00022 | O,I | 8.50500 | I 35,6 | I. 49500 |
| .032I | . 50658 | 135,3 | . 00022 |  | . 50636 | I 35,2 | . 49364 |
| . 0322 | . 50793 | I 34,9 | . 00023 |  | . 50771 | 134,8 | . 49229 |
| . 0323 | . 50928 | I 34,5 | . 00023 |  | . 50905 | 134,4 | - 49095 |
| . 0324 | . 51062 | I34, I | . 00023 |  | . 51039 | I33,9 | -48961 |
| 0.0325 | 8.51196 | 133,7 | 0.00023 | O,I | 8.51173 | I 33,5 | 1. 48827 |
| . 0326 | . 51329 | 133,3 | . 00023 |  | . 51306 | I $33, \mathrm{I}$ | . 48694 |
| . 0327 | . 51463 | 132,9 | . 00023 |  | . 51439 | 132,7 | . 48561 |
| . 0328 | .5I595 | 132,5 | . 00023 |  | . 51572 | 132,3 | . 48.428 |
| . 0329 | . 51727 | I32,I | . 00023 |  | . 51704 | 131,9 | . 48296 |
| 0.0330 | 8.51859 | I3I,7 | 0.00024 | O,I | 8.51836 | I3I,5 | I. 48164 |
| . 0331 | . 51991 | 131,3 | . 00024 |  | . 51967 | I3I, I | . 48033 |
| . 0332 | . 52122 | 130,9 | . 00024 |  | . 52098 | 130,7 | . 47902 |
| . 0333 | - 52252 | 130,5 | . 00024 |  | . 52228 | 130,3 | . 47772 |
| . 0334 | . 52383 | I30, I | . 00024 |  | . 52358 | 129,9 | . 47642 |
| 0.0335 | 8.52513 | 129,7 | 000024 | O,I | 8.52488 | 129,5 | 1.47512 |
| . 0336 | . 52642 | 129,3 | . 00025 |  | . 52618 | I29,2 | . 47382 |
| . 0337 | . 52771 | 128,9 | . 00025 |  | . 52747 | 128,8 | . 47253 |
| . 0338 | . 52900 | 128,5 | . 00025 |  | . 52875 | 128,4 | . 47125 |
| . 0339 | . 53028 | 128,2 | . 00025 |  | . 53003 | 128,0 | . 46997 |
| 0.0340 | 8.53I56 | 127,8 | 0.00025 | O,I | 8.53131 | 127,6 | 1. 46869 |
| . 034 I | . 53284 | 127,4 | . 00025 |  | . 53259 | 127,3 | . 46741 |
| . 0342 | -534II | 127,0 | . 00025 |  | . 53386 | 126,9 | . 46614 |
| . 0343 | . 53538 | 126,7 | . 00026 |  | . 53512 | 126,5 | - 46488 |
| . 0344 | . 53664 | 126,3 | . 00026 |  | . 53639 | 126, I | . 46361 |
| 0.0345 | 8.53791 | 125,9 | 0.00026 | 0,I | 8. 53765 | 125,8 | I. 46235 |
| . 0346 | . 53916 | 125,6 | . 00026 | 0,2 | . 53890 | 125,4 | . 46110 |
| . 0347 | . 54042 | 125,2 | . 00026 |  | . 54016 | 125, I | . 45984 |
| . 0348 | . 54167 | 124,8 | . 00026 |  | - 54140 | 124,7 | . 45860 |
| . 0349 | . 5429 I | 124,5 | . 00026 |  | . 54265 | 124,3 | . 45735 |
| 0.0350 | 8.54416 | 124, I | 0.00027 | 0,2 | 8.54389 | 124,0 | I.456II |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

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Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0350 | 8.54416 | 124, I | 0.00027 | 0,2 | 8.54389 | 124,0 | 1.456II |
| .035I | . 54540 | 123,8 | . 00027 |  | . 54513 | 123,6 | . 45487 |
| . 0352 | . 54663 | 123,4 | . 00027 |  | . 54636 | 123,3 | . 45364 |
| . 0353 | . 54786 | 123, I | . 00027 |  | . 54759 | 122,9 | . 4524 I |
| . 0354 | . 54909 | 122,7 | . 00027 |  | . 54882 | 122,6 | .45118 |
| 0.0355 | 8.55032 | 122,4 | 0.00027 | 0,2 | 8.55005 | 122,2 | 1. 44995 |
| . 0356 | . 55154 | 122,0 | . 00028 |  | . 55127 | 121,9 | . 44873 |
| . 0357 | . 55276 | 121,7 | . 00028 |  | . 55248 | 121,5 | . 44752 |
| . 0358 | . 55398 | I2I,4 | . 00028 |  | . 55370 | 121,2 | . 44630 |
| . 0359 | . 55519 | 121,0 | . 00028 |  | . 5549 I | 120,9 | . 44509 |
| 0.0360 | 8.55640 | 120,7 | 0.00028 | 0,2 | 8.55611 | 120,5 | 1. 44389 |
| . 0361 | . 55760 | 120,4 | . 00028 |  | . 55732 | 120,2 | . 44268 |
| . 0362 | . 55880 | 120,0 | . 00028 |  | . 55852 | I 19,9 | . 44148 |
| . 0363 | . 56000 | II9,7 | . 00029 |  | . 55972 | I 19,5 | . 44028 |
| . 0364 | . 56120 | I 19,4 | . 00029 |  | . 5609 I | II9,2 | . 43909 |
| 0.0365 | 8.56239 | 119,0 | 0.00029 | 0,2 | 8.56210 | 118,9 | I. 43790 |
| . 0366 | . 56358 | 118,7 | . 00029 |  | . 56329 | 118,6 | . 43671 |
| . 0367 | . 56476 | I 18,4 | . 00029 |  | . 56447 | II8,2 | . 43553 |
| . 0368 | . 56595 | 118,1 | . 00029 |  | . 56565 | II7,9 | . 43435 |
| . 0369 | . 56712 | 117,7. | . 00030 |  | . 56683 | II7,6 | . 43317 |
| 0.0370 | 8.56830 | 117,4 | 0.00030 | 0,2 | 8.56800 | II7,3 | 1. 43200 |
| .0371 | . 56947 | II7, I | . 00030 |  | . 56917 | II7,0 | . 43083 |
| . 0372 | . 57064 | 116,8 | . 00030 |  | . 57034 | 116,6 | . 42966 |
| . 0373 | -5718I | 116,5 | .00030 |  | . 57151 | I 16,3 | . 42849 |
| . 0374 | . 57297 | II6,2 | . 00030 |  | . 57267 | I 16,0 | . 42733 |
| 0.0375 | 8.57413 | II5,9 | 0.00031 | 0,2 | 8.57383 | I 15,7 | 1.42617 |
| . 0376 | . 57529 | 115,6 | . 0003 I |  | - 57498 | II 5,4 | . 42502 |
| . 0377 | . 57644 | I 15,3 | .0003I |  | . 57614 | II 5, I | . 42386 |
| . 0378 | . 57760 | I 14,9 | .0003I |  | . 57729 | II 4,8 | . 42271 |
| . 0379 | . 57874 | 114,6 | .0003I |  | . 57843 | II4,5. | . 42157 |
| 0.0380 | 8.57989 | II4,3 | 0.0003 I | 0,2 | 8.57957 | I 14,2 | 1.42043 |
| .0381 | . 58103 | II4,0 | . 00032 |  | . 58071 | I I 3,9 | . 41929 |
| . 0382 | . 58217 | 113,7 | . 00032 |  | . 58185 | I 13,6. | .418I5 |
| . 0383 | . 58330 | I 1 3,4 | . 00032 |  | . 58299 | II 3,3 | .41701 |
| . 0384 | . 58444 | II3,2 | . 00032 |  | . 58412 | II 3,0 | . 41588 |
| 0.0385 | 8.58557 | I 12,9 | 0.00032 | 0,2 | 8.58525 | I 12,7 | I. 41475 |
| . 0386 | . 58670 | I 12,6 | . 00032 |  | . 58637 | I 12,4 | . 41363 |
| . 0387 | . 58782 | I 12,3 | . 00033 |  | . 58749 | II2, 1 | .4125I |
| . 0388 | . 58894 | I 12,0 | . 00033 |  | . 58861 | III, 8 | . 41139 |
| . 0389 | . 59006 | I I I,7 | . 00033 |  | . 58973 | III,5. | .41027 |
| 0.0390 : | 8.59117 | III,4 | 0.00033 | 0,2 | 8.59084 | III,2 | I. 40916 |
| . 0391 | . 59229 | III, I | . 00033 |  | . 59196 | I II, 0 | . 40804 |
| . 0392 | . 59340 | I IIO,8 | . 00033 |  | . 59306 | 110,7 | . 40694 |
| . 0393 | . 59450 | IIO,6. | . 00034 |  | . 59417 | I 10,4 | . 40583 |
| . 0394 | . 59561 | I 10,3. | . 00034 |  | . 59527 | IIO, I | . 40473 |
| 0.0395 | 8.59671 | 110,0 | 0.00034 | 0,2 | 8.59637 | 109,8 | I. 40363 |
| . 0396 | . 5978 I | 109,7 | . 00034 |  | . 59747 | 109,6 | . 40253 |
| . 0397 | . 59890 | 109,5 | . 00034 |  | . 59856 | 109,3 | . 40144 |
| . 0398 | . 60000 | 109,2 | . 00034 |  | . 59965 | 109,0 | . 40035 |
| . 0399 | . 60109 | 108,9 | . 00035 |  | . 60074 | 108,7 | - 39926 |
| 0.0400 | 8.60218 | 108,6 | 0.00035 | 0,2 | 8.60183 | 108,5 | I. 39817 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{gd}$ |

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Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0400 | 8.60218 | 108,6 | 0.00035 | 0,2 | 8.60183 | 108,5 | 1.39817 |
| .0401 | . 60326 | 108,4 | . 00035 |  | . 6029I | 108,2 | . 39709 |
| . 0402 | . 60434 | 108, 1 | . 00035 |  | . 60399 | 107,9 | . 39601 |
| . 0403 | . 60542 | 107,8 | . 00035 |  | . 60507 | 107,6 | . 39493 |
| . 0404 | . 60650 | 107,6 | . 00035 |  | . 60615 | 107,4 | - 39385 |
| 0.0405 | 8.60757 | 107,3 | 0.00036 | 0,2 | 8.60722 | 107, I | 1. 39278 |
| . 0406 | . 60865 | 107,0 | . 00036 |  | . 60829 | 106,9 | . 39171 |
| . 0407 | . 60971 | 106,8 | . 00036 |  | . 60935 | 106,6 | . 39065 |
| . 0408 | .61078 | 106,5 | . 00036 |  | .61042 | 106,3 | . 38958 |
| . 0409 | . 61184 | 106,2 | . 00036 |  | .61148 | 106, 1 | . 38852 |
| 0.0410 | 8.61291 | 106,0 | 0.00036 | 0,2 | 8.61254 | 105,8 | 1. 38746 |
| .04II | . 61396 | 105,7 | . 00037 |  | . 61360 | 105,5 | . 38640 |
| .0412 | .6I502 | 105,5 | . 00037 |  | .61465 | 105,3 | . 38535 |
| .0413 | . 61607 | 105,2 | . 00037 |  | . 61570 | 105,0 | . 38430 |
| . 0414 | .61712 | 105,0 | . 00037 |  | . 61675 | 104,8 | . 38325 |
| 0.0415 | 8.61817 | 104,7 | 0.00037 | 0,2 | 8.61780 | 104,5 | 1. 38220 |
| .0416 | . 61922 | 104,5 | . 00038 |  | . 61884 | 104,3 | .38116 |
| .0417 | . 62026 | 104,2 | . 00038 |  | . 61988 | 104,0 | . 38012 |
| .0418 | . 62130 | 104,0 | . 00038 |  | . 62092 | 103,8 | . 37908 |
| .0419 | . 62234 | 103,7 | . 00038 |  | .62196 | 103,5 | . 37804 |
| 0.0420 | 8.62338 | 103,5 | 0.00038 | 0,2 | 8.62299 | 103,3 | 1.37701 |
| . 0421 | . 6244 I | 103,2 | . 00038 |  | . 62403 | 103,0 | . 37597 |
| . 0422 | . 62544 | 103,0 | . 00039 |  | . 62505 | 102,8 | . 37495 |
| . 0423 | . 62647 | 102,7 | . 00039 |  | . 62608 | 102,5 | . 37392 |
| . 0424 | . 62750 | 102,5 | . 00039 |  | . 627 II | 102,3 | . 37289 |
| 0.0425 | 8.62852 | 102,2 | 0.00039 | 0,2 | 8.62813 | 102, I | 1.37187 |
| . 0426 | . 62954 | 102,0 | . 00039 |  | . 62915 | 101,8 | . 37085 |
| . 0427 | . 63056 | 101,8 | . 00040 |  | .63016 | 101,6 | . 36984 |
| . 0428 | . 63158 | 101,5 | . 00040 |  | . 63118 | 101,3 | . 36882 |
| . 0429 | . 63259 | 101,3 | . 00040 |  | . 63219 | IOI, I | . 36781 |
| 0.0430 | 8.63360 | IOI, I | 0.00040 | 2,2 | 8.63320 | 100,9 | 1. 36680 |
| .043I | . 63461 | 100,8 | . 00040 |  | . 6342 I | 100,6 | . 36579 |
| . 0432 | . 63562 | 100,6 | . 00041 |  | . 6352 I | 100,4 | . 36479 |
| . 0433 | . 63662 | 100,4 | . 00041 |  | . 63622 | 100,2 | - 36378 |
| . 0434 | . 63763 | 100, 1 | . 0004 I |  | . 63722 | 99,9 | . 36278 |
| 0.0435 | 8.63863 | 99,9 | 0.0004 I | 0,2 | 8.63822 | 99,7 | 1.36178 |
| . 0436 | . 63962 | 99,7 | . 00041 |  | . 63921 | 99,5 | . 36079 |
| . 0437 | .64062 | 99,4 | . 0004 I |  | . 64020 | 99,3 | . 35980 |
| . 0438 | .64161 | 99,2 | . 00042 |  | .64120 | 99,0 | . 35880 |
| . 0439 | . 64260 | 99,0 | . 00042 |  | .64219 | 98,8 | . 3578 I |
| 0.0440 | 8.64359 | 98,8 | 0.00042 | 0,2 | 8.64317 | 98,6 | 1. 35683 |
| .044I | . 64458 | 98,5 | . 00042 |  | . 64416 | 98,4 | . 35584 |
| . 0442 | . 64556 | 98,3 | . 00042 |  | . 64514 | 98, 1 | . 35486 |
| . 0443 | . 64655 | 98,1 | . 00043 |  | .646I2 | 97,9 | . 35388 |
| . 0444 | . 64753 | 97,9 | . 00043 |  | . 64710 | 97,7 | . 35290 |
| 0.0445 | 8.64850 | 97,7 | 0.00043 | 0,2 | 8.64807 | 97,5 | 1.35193 |
| . 0446 | . 64948 | 97,4 | . 00043 |  | . 64905 | 97,2 | . 35095 |
| . 0447 | . 65045 | 97,2 | . 00043 |  | . 65002 | 97,0 | - 34998 |
| . 0448 | . 65142 | 97,0 | . 00044 |  | . 65099 | 96,8 | . 34901 |
| . 0449 | . 65239 | 96,8 | . 00044 |  | . 65195 | 96,6 | . 34805 |
| 0.0450 | 8.65336 | 96,6 | 0.00044 | 0,2 | 8.65292 | 96,4 | 1. 34708 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0450 | 8.65336 | 96,6 | 0.00044 | 0,2 | 8.65292 | 96,4 | 1.34708 |
| .0451 | . 65432 | 96,4 | . 00044 |  | . 65388 | 96,2 | . 34612 |
| . 0452 | . 65529 | 96, | . 00044 |  | . 65484 | 96,0 | -34516 |
| . 0453 | . 65625 | 95,9 | . 00045 |  | . 65580 | 95,7 | - 34420 |
| . 0454 | . 6572 I | 95,7 | . 00045 |  | . 65676 | 95,5 | -34324 |
| 0.0455 | 8.65816 | 95,5 | 0.00045 | 0,2 | 8.65771 | 95,3 | 1. 34229 |
| . 0456 | . 65912 | 95,3 | . 00045 |  | . 65866 | 95, I | . 34134 |
| . 0457 | . 66007 | 95, 1 | . 00045 |  | . 65961 | 94,9 | . 34039 |
| . 0458 | . 66102 | 94,9 | . 00046 |  | . 66056 | 94,7 | -33944 |
| . 0459 | .66I97 | 94,7 | . 00046 |  | . 6615 I | 94,5 | . 33849 |
| 0.0460 | 8.66291 | 94,5 | 0.00046 | 0,2 | 8.66245 | 943 | I. 33755 |
| .046I | . 66385 | 94,3 | . 00046 |  | . 66339 | 94, I | . 33661 |
| . 0462 | . 66480 | 94, I | . 00046 |  | . 66433 | 93,9 | . 33567 |
| . 0463 | . 66574 | 93,9 | . 00047 |  | . 66527 | 93,7 | . 33473 |
| . 0464 | . 66667 | 93,7 | . 00047 |  | . 6662 I | 93,5 | - 33379 |
| 0.0465 | 8.66761 | 93,5 | 0.00047 | 0,2 | 8.66714 | 93,3 | 1. 33286 |
| . 0466 | . 66854 | 93,3 | .00047 |  | . 66807 | 93, I | . 33193 |
| . 0467 | . 66947 | 93,I | . 00047 |  | . 66900 | 92,9 | . 33100 |
| . 0468 | . 67040 | 92,9 | . 00048 |  | . 66993 | 92,7 | -33007 |
| . 0469 | . 67133 | 92,7 | . 00048 |  | . 67085 | 92,5 | . 32915 |
| 0.0470 | 8.67226 | 92,5 | 0.00048 | 0,2 | 8.67178 | 92,3 | I. 32822 |
| . 0471 | . 67318 | 92,3 | . 00048 |  | . 67270 | 92, 1 | . 32730 |
| . 0472 | . 67410 | 92,I | . 00048 |  | . 67362 | 91,9 | . 32638 |
| . 0473 | . 67502 | 91,9 | . 00049 |  | . 67454 | 91,7 | . 32546 |
| . 0474 | . 67594 | 91,7 | . 00049 |  | . 67545 | 91,5 | - 32455 |
| 0.0475 | 8.67686 | 9I,5 | 0.00049 | 0,2 | 8.67637 | 91,3 | 1.32363 |
| . 0476 | . 67777 | 91,3 | . 00049 |  | . 67728 | 91, I | . 32272 |
| . 0477 | . 67868 | 91,I | . 00049 |  | .67819 | 90,9 | . 32 I 8 I |
| . 0478 | . 67959 | 90,9 | . 00050 |  | . 67910 | 90,7 | - 32090 |
| . 0479 | . 68050 | 90,7 | . 00050 |  | . 68000 | 90,5 | . 32000 |
| 0.0480 | 8.6814 I | 90,5 | 0.00050 | 0,2 | 8.6809 I | 90,3 | 1.31999 |
| .048I | .6823I | 90,4 | . 00050 |  | .68181 | 90,2 | . 31819 |
| . 0482 | . 68322 | 90,2 | . 00050 |  | .6827I | 90,0 | . 31729 |
| . 0483 | . 68412 | 90,0 | .0005I |  | .6836I | 80,8 | . 31639 |
| . 0484 | .68501 | 89,8 | .0005I |  | .6845I | 89,6 | -31549 |
| 0.0485 | 8.68591 | 89,6 | 0.00051 | 0,2 | 8.68540 | 89,4 | 1.31460 |
| . 0486 | .6868I | 89,4 | .0005I |  | . 68629 | 89,2 | . 31371 |
| . 0487 | . 68770 | 80,2 | .0005I |  | . 68719 | 89,0 | . 3128I |
| . 0488 | . 68859 | 89, 1 | . 00052 |  | . 68808 | 88,9 | . 31192 |
| . 0489 | . 68948 | 88,9 | . 00052 |  | . 68896 | 88,7 | .31104 |
| 0.0490 | 8.69037 | 88,7 | 0.00052 | 0,2 | 8.68985 | 88,5 | 1.31015 |
| .049I | . 69126 | 88,5 | . 00052 |  | . 69073 | 88,3 | . 30927 |
| . 0492 | . 69214 | 88,3 | . 00053 |  | . 69161 | 88, 1 | . 30839 |
| . 0493 | . 69302 | 88,2 | . 00053 |  | . 69250 | 87,9 | . 30750 |
| . 0494 | . 69390 | 88,0 | . 00053 |  | . 69337 | 87,8 | . 30663 |
| 0.0495 | 8.69478 | 87,8 | 0.00053 | 0,2 | 8.69425 | 87,6 | I. 30575 |
| . 0496 | . 69566 | 87,6 | . 00053 |  | . 69513 | 87,4 | . 30487 |
| . 0497 | . 69654 | 87,5 | . 00054 |  | . 69600 | 87,2 | - 30400 |
| . 0498 | . 69741 | 87,3 | . 00054 |  | . 69687 | 87, 1 | . 30313 |
| . 0499 | . 69828 | 87, 1 | . 00054 |  | . 69774 | 86,9 | . 30226 |
| 0.0500 | 8.69915 | 86,9 | 0.00054 | 0,2 | 8.6986 I | 86,7 | 1.30139 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0500 | 8.69915 | 86,9 | 0.00054 | 0,2 | 8.6986 I | 86,7 | I. 30139 |
| .0501 | . 70002 | 86,8 | . 00054 |  | . 69947 | 86,5 | . 30053 |
| . 0502 | . 70089 | 86,6 | . 00055 |  | . 70034 | 86,4 | . 29966 |
| . 0503 | . 70175 | 86,4 | . 00055 |  | . 70120 | 86,2 | . 29880 |
| . 0504 | . 70261 | 86,2 | . 00055 |  | . 70206 | 86,0 | . 29794 |
| 0.0505 | 8.70348 | 86, r | 0.00055 | 0,2 | 8.70292 | 85,9 | 1.29708 |
| . 0506 | . 70434 | 85,9 | . 00056 |  | . 70378 | 85,7 | . 29622 |
| . 0507 | . 70519 | 85,7 | . 00056 |  | . 70464 | 85,5 | . 29536 |
| . 0508 | . 70605 | 85,6 | . 00056 |  | . 70549 | 85,3 | . 29451 |
| . 0509 | . 7069 I | 85,4 | . 00056 |  | . 70634 | 85,2 | . 29366 |
| 0.0510 | 8.70776 | 85,2 | 0.00056 | 0,2 | 8.70719 | 85,0 | I.2928I |
| .05II | . 70861 | 85, I | . 00057 |  | . 70804 | 84,8 | . 29196 |
| . 0512 | . 70946 | 84,9 | . 00057 |  | . 70889 | 84,7 | . 29 III |
| .0513 | . 7103 I | 84,7 | . 00057 |  | . 70974 | 84,5 | . 29026 |
| .0514 | . 71115 | 84,6 | . 00057 |  | . 71058 | 84,3 | . 28942 |
| 0.0515 | 8.71200 | 84,4 | 0.00058 | 0,2 | 8.71142 | 84,2 | I. 28858 |
| . 0516 | . 71284 | 84,2 | . 00058 |  | . 71226 | 84,0 | . 28774 |
| .0517 | . 71368 | 84,1 | . 00058 |  | . 71310 | 83,9 | . 28690 |
| .0518 | . 71452 | 83,9 | . 00058 |  | . 71394 | 83,7 | . 28606 |
| .0519 | . 71536 | 83,8 | . 00058 |  | . 71478 | 83,5 | . 28522 |
| 0.0520 | 8.71620 | 83,6 | 0.00059 | 0,2 | 8.71561 | 83,4 | I. 28439 |
| .052I | . 71703 | 83,4 | . 00059 |  | . 71644 | 83,2 | . 28356 |
| . 0522 | . 71787 | 83,3 | . 00059 |  | . 71728 | 83,0 | . 28272 |
| . 0523 | . 71870 | 83,1 | . 00059 |  | .718II | 82,9 | .28I89 |
| . 0524 | . 71953 | 83,0 | . 00060 |  | . 71893 | 82,7 | .28107 |
| 0.0525 | 8.72036 | 82,8 | 0.00060 | 0,2 | 8.71976 | 82,6 | 1. 28024 |
| . 0526 | .72119 | 82,6 | . 00060 |  | . 72059 | 82,4 | . 27941 |
| . 0527 | . 72201 | 82,5 | . 00060 |  | . 72141 | 82,3 | . 27859 |
| . 0528 | . 72284 | 82,3 | . 0006 I |  | . 72223 | 82, 1 | . 27777 |
| . 0529 | . 72366 | 82,2 | .0006I |  | . 72305 | 81,9 | . 27695 |
| 0.0530 | 8.72448 | 82,0 | 0.00061 | 0,2 | 8.72387 | 81,8 | 1.27613 |
| .0531 | . 72530 | 81,9 | .0006I |  | . 72469 | 8I,6 | . 2753 I |
| . 0532 | . 72612 | 8I,7 | . 00061 |  | . 72550 | 8I,5 | . 27450 |
| . 0533 | . 72693 | 8i,6 | . 00062 |  | . 72632 | 8I,3 | . 27368 |
| . 0534 | . 72775 | 8r,4 | . 00062 |  | .72713 | 8I,2 | .27287 |
| 0.0535 | 8.72856 | 81,3 | 0.00062 | 0,2 | 8.72794 | 81,0 | 1.27206 |
| . 0536 | . 72937 | $8 \mathrm{I}, \mathrm{I}$ | . 00062 |  | . 72875 | 80,9 | . 27125 |
| . 0537 | . 73018 | 81,0 | .00063 |  | . 72956 | 80,7 | . 27044 |
| . 0538 | . 73099 | 80,8 | .00063 |  | . 73036 | 80,6 | . 26964 |
| . 0539 | .73180 | 80,7 | . 00063 |  | .73117 | 80,4 | . 26883 |
| 0.0540 | 8.73260 | 80,5 | 0.00063 | 0,2 | 8.73197 | 80,3 | 1. 26803 |
| .054I | .7334I | 80,4 | . 00064 |  | . 73277 | 80, | . 26723 |
| . 0542 | . 7342 I | 80,2 | . 00064 |  | . 73357 | 80,0 | . 26643 |
| . 0543 | .73501 | 80,I | . 00064 |  | . 73436 | 79,8 | . 26564 |
| . 0544 | .73581 | 79,9 | . 00064 |  | .73517 | 79,7 | . 26483 |
| 0.0545 | 8.73661 | 79,8 | 0.00064 | 0,2 | 8.73597 | 79,5 | 1. 26403 |
| . 0546 | . 73741 | 79,6 | . 00065 |  | . 73676 | 79,4 | . 26324 |
| . 0547 | . 73820 | 79,5 | . 00065 |  | . 73755 | 79,2 | . 26245 |
| . 0548 | . 73900 | 79,3 | . 00065 |  | . 73835 | 79, 1 | . 26165 |
| . 0549 | . 73979 | 79,2 | . 00065 |  | . 73914 | 78,9 | . 26086 |
| 0.0550 | 8.74058 | 79,0 | 0.00066 | 0,2 | 8.73993 | 78,8 | I. 26007 |
| u | $\log \tan \operatorname{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log csc gd u |

Logarithms of Hyperbolic Functions.

| U | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0550 | 8.74058 | 79,0 | 0.00066 | 0,2 | 8.73993 | 78,8 | 1. 26007 |
| .055I | .74137 | 78,9 | . 00066 |  | .74071 | 78,7 | . 25929 |
| . 0552 | . 74216 | 78,8 | . 00066 |  | .74150 | 78,5 | . 25850 |
| . 0553 | . 74295 | 78,6 | . 00066 |  | . 74228 | 78,4 | . 25772 |
| . 0554 | . 74373 | 78,5 | . 00067 | - | . 74307 | 78,2 | . 25693 |
| 0.0555 | 8.74452 | 78,3 | 0.00067 | 0,2 | 8.74385 | 78, 1 | 1.25615 |
| . 0556 | . 74530 | 78,2 | . 00067 |  | . 74463 | 77,9 | . 25537 |
| . 0557 | . 74608 | 78,0 | . 00067 |  | .74541 | 77,8 | . 25459 |
| . 0558 | . 74686 | 77,9 | . 00068 |  | .746I8 | 77,7 | . 25382 |
| . 0559 | . 74764 | 77,8 | . 00068 |  | .74696 | 77,5 | . 25304 |
| 0.0560 | 8.74841 | 77,6 | 0.00068 | 0,2 | 8.74773 | 77,4 | I. 25227 |
| .0561 | . 74919 | 77,5 | . 00068 |  | . 74851 | 77,3 | . 25149 |
| . 0562 | . 74996 | 77,4 | . 00069 | , | . 74928 | 77, 1 | . 25072 |
| . 0563 | . 75074 | 77,2 | . 00069 |  | . 75005 | 77,0 | . 24995 |
| . 0564 | .7515I | 77,I | . 00069 |  | . 75082 | 76,8 | . 24918 |
| 0.0565 | 8.75228 | 76,9 | 0.00069 | 0,2 | 8.75159 | 76,7 | I. 2484 I |
| . 0565 | . 75305 | 76,8 | . 00070 |  | . 75235 | 76,6 | . 24765 |
| . 0567 | . 75382 | 76,7 | . 00070 |  | . 75312 | 76,4 | . 24688 |
| . 0568 | . 75458 | 76,5 | .00070 |  | . 75388 | 76,3 | . 24612 |
| . 0569 | . 75535 | 76,4 | . 00070 |  | . 75464 | 76,2 | . 24536 |
| 0.0570 | 8.756 II | 76,3 | 0.00071 | 0,2 | 8.75540 | 76,0 | I. 24460 |
| .0571 | . 75687 | 76,1 | .0007I |  | .75616 | 75,9 | . 24384 |
| . 0572 | . 75763 | 76,0 | .0007I |  | . 75692 | 75,8 | . 24308 |
| . 0573 | . 75839 | 75,9 | .00071 | $\square$ | . 75768 | 75,6 | . 24232 |
| . 0574 | . 75915 | 75,7 | . 00072 |  | . 75844 | 75,5 | . 24156 |
| 0.0575 | 8.75991 | 75,6 | 0.00072 | 0,2 | 8.75919 | 75,4 | 1.24081 |
| . 0576 | . 76066 | 75,5 | . 00072 | 0,2 | . 75994 | 75,2 | . 24006 |
| . 0577 | . 76142 | 75,4 | .00072 | 0,3 | . 76069 | 75, I | . 23931 |
| . 0578 | . 76217 | 75,2 | . 00073 |  | . 76144 | 75,0 | . 23856 |
| . 0579 | . 76292 | 75, I | . 00073 |  | . 76219 | 74,8 | . 2378 I |
| 0.0580 | 8.76367 | 75,0 | 0.00073 | 0,3 | 8.76294 | 74,7 | I. 23706 |
| .0581 | . 76442 | 74,8 | . 00073 |  | . 76369 | 74,6 | . 23631 |
| . 0582 | . 76517 | 74,7 | .00074 |  | . 76443 | 74,5 | . 23557 |
| . 0583 | .76591 | 74,6 | . 00074 |  | . 76518 | 74,3 | . 23482 |
| . 0584 | . 76666 | 74,5 | .00074 |  | . 76592 | 74,2 | . 23408 |
| 0.0585 | 8.76740 | 74,3 | 0.00074 | 0,3 | 8.76666 | 74, I | 1.23334 |
| . 0585 | .76815 | 74,2 | . 00075 |  | . 76740 | 73,9 | . 23260 |
| . 0587 | . 76889 | 74, 1 | . 00075 |  | . 76814 | 73,8 | . 23186 |
| . 0588 | . 76963 | 73,9 | . 00075 |  | . 76888 | 73,7 | . 23112 |
| . 0589 | . 77037 | 73,8 | . 00075 |  | .76961 | 73,6 | . 23039 |
| 0.0590 | 8.77110 | 73,7 | 0.00076 | 0,3 | 8.77035 | 73,4 | 1. 22965 |
| . 0591 | . 77184 | 73,6 | . 00076 |  | . 77108 | 73,3 | . 22892 |
| . 0592 | . 77258 | 73,4 | .00076 |  | . 77181 | 73,2 | . 228I9 |
| . 0593 | .77331 | 73,3 | . 00076 |  | . 77255 | 73, 1 | . 22745 |
| . 0594 | . 77404 | 73,2 | . 00077 |  | . 77328 | 72,9 | . 22672 |
| 0.0595 | 8.77477 | 73, 1 | 0.00077 | 0,3 | 8.77400 | 72,8 | 1.22600 |
| . 0596 | . 77550 | 73,0 | . 00077 |  | . 77473 | 72,7 | . 22527 |
| . 0597 | . 77623 | 72,8 | . 00077 |  | . 77546 | 72,6 | . 22454 |
| . 0598 | . 77696 | 72,7 | .00078 |  | .77618 | 72,5 | . 22382 |
| . 0599 | . 77769 | 72,6 | .00078 |  | .77691 | 72,3 | . 22309 |
| 0.0600 | 8.77841 | 72,5 | 0.00078 | 0,3 | 8.77763 | 72,2 | 1.22237 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| U | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathbf{F o}^{\prime}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0600 | 8.77841 | 72,5 | 0.00078 | 0,3 | 8.77763 | 72,2 | 1.22237 |
| .0601 | .77914 | 72,3 | . 00078 |  | . 77835 | 72,I | . 22165 |
| . 0602 | . 77986 | 72,2 | . 00079 |  | . 77907 | 72,0 | . 22093 |
| . 0603 | . 78058 | 72, 1 | . 00079 |  | . 77979 | 71,8 | . 22021 |
| . 0604 | .78130 | 72,0 | . 00079 |  | . 7805 I | 71,7 | . 21949 |
| 0.0605 | 8.78202 | 71,9 | 0.00079 | 0,3 | 8.78123 | 71,6 | I. 21877 |
| . 0606 | . 78274 | 71,8 | . 000080 |  | .78194 | 71,5 | . 21806 |
| . 0607 | . 78346 | 71,6 | . 00080 |  | . 78266 | 71,4 | . 21734 |
| . 0608 | . 78417 | 71,5 | . 00080 |  | . 78337 | 71,3 | . 21663 |
| . 0609 | . 78489 | 71,4 | .00080 |  | . 78408 | 71,1 | . 21592 |
| 0.0610 | 8.78560 | 71,3 | 0.0008 I | 0,3 | 8.78479 | 71,0 | I.2I52I |
| .06I I | . 78631 | 71,2 | .0008I |  | . 78550 | 70,9 | .21450 |
| .06I2 | . 78702 | 71,1 | .0008I |  | . 78621 | 70,8 | . 21379 |
| .0613 | .78773 | 70,9 | . 00082 |  | . 78692 | 70,7 | . 21308 |
| .06I4 | . 78844 | 70,8 | . 00082 |  | . 78762 | 70,6 | . 21238 |
| 0.0615 | 8.78915 | 70,7 | 0.00082 | 0,3 | 8.78833 | 70,4 | 1.21167 |
| .06I6 | . 78986 | 70,6 | . 00082 |  | . 78903 | 70,3 | . 21097 |
| .06I7 | . 79056 | 70,5 | . 00083 |  | . 78973 | 70,2 | . 21027 |
| .0618 | . 79127 | 70,4 | . 00083 |  | . 79044 | 70, I | . 20956 |
| .06I9 | . 79197 | 70,3 | . 00083 |  | .791 14 | 70,0 | . 20886 |
| 0.0620 | 8.79267 | 70, 1 | 0.00083 | 0,3 | 8.79184 | 69,9 | 1. 208 I 6 |
| . 0621 | . 79337 | 70,0 | . 00084 |  | . 79253 | 69,8 | . 20747 |
| . 0622 | . 79407 | 69,9 | . 00084 |  | . 79323 | 69,6 | . 20677 |
| . 0623 | . 79477 | 69,8 | . 00084 |  | . 79393 | 69,5 | . 20607 |
| . 0624 | . 79547 | 69,7 | . 00084 |  | . 79462 | 69,4 | . 20538 |
| 0.0625 | 8.79616 | 69,6 | 0.00085 | 0,3 | 8.79532 | 69,3 | 1. 20468 |
| . 0626 | . 79686 | 69,5 | . 00085 |  | .79601 | 69,2 | . 20399 |
| . 0627 | . 79755 | 69,4 | . 00085 |  | . 79670 | 69,1 | . 20330 |
| . 0628 | . 79825 | 69,2 | . 00086 |  | . 79739 | 69,0 | . 2026I |
| . 0629 | . 79894 | 69,1 | . 00086 |  | . 79808 | 68,9 | . 20192 |
| 0.0630 | 8.79963 | 69,0 | 0.00085 | 0,3 | 8.79877 | 68,8 | 1.20123 |
| .063I | . 80032 | 68,9 | . 000086 |  | . 79945 | 68,6 | . 20055 |
| . 0632 | . 80101 | 68,8 | . 00087 |  | . 80014 | 68,5 | . 19986 |
| . 0633 | . 80169 | 68,7 | .00087 |  | . 80082 | 68,4 | . 19918 |
| . 0634 | . 80238 | 68,6 | . 00087 |  | .80151 | 68,3 | . 19849 |
| 0.0635 | 8.80307 | 68,5 | 0.00088 | 0,3 | 8.80219 | 68,2 | I . 1978I |
| . 0636 | . 80375 | 68,4 | . 00088 |  | . 80287 | 68,1 | . 19713 |
| . 0637 | . 80443 | 68,3 | . 00088 |  | . 80355 | 68,0 | . 19645 |
| . 0638 | . 80512 | 68,2 | . 00088 |  | . 80423 | 67,9 | . 19577 |
| . 0639 | .80580 | 68, 1 | .00089 |  | . 80491 | 67,8 | . 19509 |
| 0.0640 | 8.80648 | 68,0 | 0.00089 | 0,3 | 8.80559 | 67,7 | I. 19441 |
| .0641 | . 80716 | 67,8 | .00089 |  | . 80626 | 67,6 | . 19374 |
| . 0642 | . 80783 | 67,7 | . 00008 |  | . 80694 | 67,5 | . 19306 |
| . 0643 | . 80851 | 67,6 | . 00090 |  | . 80761 | 67,4 | . 19239 |
| . 0644 | . 80919 | 67,5 | . 00090 |  | . 80829 | 67,3 | . 1917 1 |
| 0.0645 | 8.80986 | 67,4 | 0.00090 | 0,3 | 8.80896 | 67, 1 | 1. 19104 |
| . 0646 | .81053 | 67,3 | .0009I |  | . 80963 | 67,0 | . 19037 |
| . 0647 | .81121 | 67,2 | . 00091 |  | . 81030 | 66,9 | . 18970 |
| . 0648 | .81188 | 67,1 | . 00091 |  | . 81097 | 66,8 | . 18903 |
| . 0649 | .81255 | 67,0 | . 00091 |  | .81164 | 66,7 | . 18836 |
| 0.0650 | 8.81322 | 66,9 | 0.00092 | 0,3 | 8.81230 | 66,6 | 1.18770 |
| u | $\log \tan \mathrm{gd} \mathrm{u}^{\text {a }}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\underline{\log \sinh } \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log eoth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0650 | 8.81322 | 66,9 | 0.00092 | 0,3 | 8.81230 | 66,6 | 1. 18770 |
| . 0651 | .81389 | 66,8 | . 00092 |  | .81297 | 66,5 | . 18703 |
| . 0652 | .81456 | 66,7 | . 00092 |  | . 81363 | 66,4 | . 18637 |
| . 0653 | .81522 | 66,6 | . 00093 |  | .81430 | 66,3 | . 18570 |
| . 0654 | .8I589 | 66,5 | . 00093 |  | .81496 | 66,2 | . 18504 |
| 0.0655 | 8.81655 | 66,4 | 0.00093 | 0,3 | 8.81562 | 66, 1 | I. 18438 |
| . 0656 | .81722 | 66,3 | . 00093 |  | .81628 | 66,0 | . 18372 |
| . 0657 | .81788 | 66,2 | . 00094 |  | .81694 | 65,9 | . 18306 |
| . 0658 | .81854 | 66,1 | . 00094 |  | . 81760 | 65,8 | . 18240 |
| . 0659 | .81920 | 66,0 | . 00094 |  | . 81826 | 65,7 | . 18174 |
| 0.0660 | 8.81986 | 65,9 | 0.00095 | 0,3 | 8.8189I | 65,6 | 1.18109 |
| .066I | . 82052 | 65,8 | . 00095 |  | .81957 | 65,5 | . I8043 |
| . 0662 | .82118 | 65,7 | . 00095 |  | . 82022 | 65.4 | . 17978 |
| . 0663 | . 82183 | 65,6 | .00095 |  | . 82088 | 65,3 | . 17912 |
| . 0664 | . 82249 | 65,5 | . 00096 |  | . 82 I53 | 65,2 | . 17847 |
| 0.0665 | 8.82314 | 65,4 | 0.00096 | 0,3 | 8.82218 | 65,1 | 1. 17782 |
| . 0666 | . 82380 | 65,3 | .00096 |  | . 82283 | 65,0 | . 17717 |
| . 0667 | . 82445 | 65,2 | . 00097 |  | . 82348 | 64,9 | . 17652 |
| . 0668 | . 82510 | 65,1 | . 00097 |  | . 82413 | 64,8 | . 17587 |
| . 0669 | . 82575 | 65,0 | . 00097 |  | . 82478 | 64,7 | . 17522 |
| 0.0670 | 8.82640 | 64,9 | 0.00097 | 0,3 | 8.82543 | 64,6 | 1. 17457 |
| . 0671 | . 82705 | 64,8 | . 00098 |  | . 82607 | 64,5 | . 17393 |
| . 0672 | . 82770 | 64,7 | . 00098 |  | . 82672 | 64,4 | . 17328 |
| . 0673 | . 82834 | 64,6 | . 00098 |  | . 82736 | 64,3 | . 17264 |
| . 0674 | . 82899 | 64,5 | . 00099 |  | . 82800 | 64,2 | . 17200 |
| 0.0675 | 8.82963 | 64,4 | 0.00099 | 0,3 | 8.82864 | 64, 1 | 1.17136 |
| . 0676 | . 83028 | 64,3 | . 00099 |  | . 82929 | 64, 1 | . 17071 |
| . 0677 | .83092 | 64,2 | . 00099 |  | . 82994 | 64,0 | . 17006 |
| . 0678 | . 83156 | 64,2 | . 00100 |  | . 83056 | 63,9 | . 16944 |
| . 0679 | . 83220 | 64,1 | .00100 |  | . 83120 | 63,8 | . 16880 |
| 0.0680 | 8.83284 | 64,0 | 0.00100 | 0,3 | 8.83184 | 63,7 | 1. 16816 |
| .0681 | . 83348 | 63,9 | .00101 |  | . 83248 | 63,6 | . 16752 |
| . 0682 | . 83412 | 63,8 | .00101 |  | .833II | 63,5 | . 16689 |
| . 0683 | . 83476 | 63,7 | .00101 |  | . 83375 | 63,4 | . 16625 |
| . 0684 | . 83539 | 63,6 | . 00102 |  | . 83438 | 63,3 | . 16562 |
| 0.0685 | 8.83603 | 63,5 | 0.00102 | 0,3 | 8.83501 | 63,2 | 1. 16499 |
| . 0686 | . 83666 | 63,4 | .00102 |  | . 83564 | 63,1 | . 16436 |
| . 0687 | . 83730 | 63,3 | . 00102 |  | . 83627 | 63,0 | . 16373 |
| . 0688 | . 83793 | 63,2 | .00103 |  | . 83690 | 62,9 | . 16310 |
| . 0689 | . 83856 | 63,1 | . 00103 |  | . 83753 | 62,8 | . 16247 |
| 0.0690 | 8.83919 | 63,0 | 0.00103 | 0,3 | 8.83816 | 62,7 | 1. 16184 |
| .0691 | . 83982 | 63,0 | .00104 |  | . 83879 | 62,7 | . 16121 |
| . 0692 | . 84045 | 62,9 | .00104 |  | . 83941 | 62,6 | . 16059 |
| . 0693 | . 84108 | 62,8 | .00104 |  | . 84004 | 62,5 | . 15996 |
| . 0694 | .84171 | 62,7 | . 00105 |  | . 84066 | 62,4 | . I'5934 |
| 0.0695 | 8.84233 | 62,6 | 0.00105 | 0,3 | 8.84129 | 62,3 | 1. 15871 |
| . 0696 | . 84296 | 62,5 | . 00105 |  | . 84191 | 62,2 | . 15809 |
| . 0697 | . 84358 | 62,4 | .00105 |  | . 84253 | 62,I | . 15747 |
| . 0698 | . 84421 | 62,3 | .00106 |  | . 84315 | 62,0 | . 15685 |
| . 0699 | .84483 | 62,2 | .00106 |  | . 84377 | 61,9 | . 15623 |
| 0.0700 | 8.84545 | 62,1 | 0.00106 | 0,3 | 8.84439 | 6I,8 | I. 15561 |
| U | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\text {g }}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{~g} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0700 | 8.84545 | 62, I | 0.00106 | 0,3 | 8.84439 | 61,8 | I. I5561 |
| .0701 | . 84607 | 62,1 | . 00107 |  | .84501 | 61,8 | . I5499 |
| . 0702 | . 84669 | 62,0 | .00107 | - | . 84562 | 61,7 | . I5438 |
| . 0703 | .84731 | 6I,9 | .00107 |  | . 84624 | 6I,6 | . 15376 |
| . 0704 | . 84793 | 6I,8 | . 00108 |  | . 84686 | 6I,5 | . 15314 |
| 0.0705 | 8.84855 | 61,7 | 0.00108 | 0,3 | 8.84747 | 61,4 | I. 15253 |
| . 0706 | . 84917 | 61,6 | . 00108 |  | . 84808 | 6I,3 | . 15192 |
| . 0707 | . 84978 | 6I,5 | . 00108 |  | . 84870 | 61,2 | . 15130 |
| . 0708 | . 85040 | 6I,4 | . 00109 |  | . 84931 | 6I, | . 15069 |
| . 0709 | .85101 | 6I,4 | . 00109 |  | . 84992 | 6I,0 | . 15008 |
| 0.0710 | 8.85162 | 61,3 | 0.00109 | 0,3 | 8.85053 | 61,0 | I. 14947 |
| . 0711 | . 85224 | 61,2 | . 00110 |  | . 85114 | 60,9 | . I4886 |
| . 0712 | . 85285 | 6I, 1 | . 00110 |  | . 85175 | 60,8 | . 14825 |
| . 0713 | . 85346 | 61,0 | . 00110 |  | . 85235 | 60,7 | . 14765 |
| .07I4 | . 85407 | 60,9 | . 0011 I |  | . 85296 | 60,6 | . 14704 |
| 0.0715 | 8.85468 | 60,8 | 0.00111 | 0,3 | 8.85357 | 60,5 | 1. 14643 |
| . 0716 | . 85528 | 60,8 | . 001 I I |  | . 85417 | 60,4 | . 14583 |
| . 0717 | . 85589 | 60,7 | .00112 |  | . 85478 | 60,4 | . 14522 |
| .0718 | . 85650 | 60,6 | . 00112 |  | . 85538 | 60,3 | . 14462 |
| .0719 | . 85710 | 60,5 | . 00112 |  | . 85598 | 60,2 | . I4402 |
| 0.0720 | 8.85771 | 60,4 | 0.00112 | 0,3 | 8.85658 | 60,1 | I. 14342 |
| . 0721 | .8583I | 60,3 | . 00113 |  | . 85718 | 60,0 | . 14282 |
| . 0722 | .85891 | 60,3 | . 00113 |  | . 85778 | 59,9 | . 14222 |
| . 0723 | . 85952 . | 60,2 | . 00113 |  | . 85838 | 59,9 | . 14162 |
| . 0724 | . 86012 | 60,1 | . OOII4 |  | . 85898 | 59,8 | . 14102 |
| 0.0725 | 8.86072 | 60,0 | 0.00114. | 0,3 | 8.85958 | 59,7 | 1.14042 |
| . 0726 | . 86132 | 59,9 | .00114 |  | . 86017 | 59,6 | . I3983 |
| . 0727 | . 86192 | 59,8 | . 00115 |  | . 86077 | 59,5 | . I 3923 |
| . 0728 | . 86251 | 59,8 | . 00115 |  | .86I37 | 59,5 | . 13863 |
| . 0729 | .863II | 59,7 | . 00115 |  | .86196 | 59,4 | . 13804 |
| 0.0730 | 8.86371 | 59,6 | 0.00116 | 0,3 | 8.86255 | 59,3 | I. 13745 |
| . 0731 | . 86430 | 59,5 | . 00116 |  | . 86314 | 59,2 | . I3686 |
| . 0732 | . 85490 | 59,4 | . 00116 |  | . 86374 | 59, 1 | . 13626 |
| . 0733 | . 86549 | 59,4 | . 00117 |  | . 86433 | 59,0 | . I3567 |
| . 0734 | . 86609 | 59,3 | .00117 |  | . 86492 | 59,0 | . I 3508 |
| 0.0735 | 8.86668 | 59,2 | 0.00117 | 0,3 | 8.86551 | 58,9 | I. 13449 |
| . 0736 | . 86727 | 59, I | . 00118 |  | . 86609 | 58,8 | . I3391 |
| . 0737 | . 85786 | 59,0 | . 00118 |  | . 86668 | 58,7 | . 13332 |
| . 0738 | . 86845 | 59,0. | . 00118 |  | . 86727 | 58,6 | . 13273 |
| . 0739 | . 86904 | 58,9 | .00118 |  | . 86785 | 58,6 | . 13215 |
| 0.0740 | 8.85963 | 58,8 | 0.00119 | 0,3 | 8.86844 | 58,5 | I. I3I56 |
| . 0741 | . 87022 | 58,7. | .00119 |  | . 86002 | 58,4 | . 13098 |
| . 0742 | . 87080 | 58,6 | . 00119 |  | .8696I | 58,3 | . I3039 |
| . 0743 | . 87139 | 58,6 | . 00120 | - | . 87019 | 58,2 | . I2981 |
| . 0744 | . 87197 | 58,5 | . 00120 |  | . 87077 | 58,2 | . 12923 |
| 0.0745 | 8.87256 | 58,4 | 0.00120 | 0,3 | 8.87135 | 58,1 | I. 12865 |
| . 0746 | .87314 | 58,3 | . 00121 |  | . 87193 | 58,0 | . 12807 |
| . 0747 | . 87372 | 58,2 | . 00121 |  | . 87251 | 57,9 | . 12749 |
| . 0748 | . 87431 | 58,2. | . 00121 |  | . 87309 | 57,8 | . 12691 |
| . 0749 | . 87489 | 58, I | . 00122 |  | . 87367 | 57,8 | . 12633 |
| 0.0750 | 8.87547 | 58,0 | 0.00122 | 0,3 | 8.87425 | 57,7 | I. 12575 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\boldsymbol{l o g} \sinh \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }}$ coth $\mathbf{u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0750 | 8.87547 | 58,0 | 0.00122 | 0,3 | 8.87425 | 57,7 | I. 12575 |
| . 0751 | . 87605 | 57,9 | .00122 |  | . 87482 | 57,6 | . 12518 |
| . 0752 | . 87663 | 57,9 | . 00123 |  | . 87540 | 57,5 | . 12460 |
| . 0753 | . 87721 | 57,8 | .00123 |  | . 87598 | 57,5 | . 12402 |
| . 0754 | . 87778 | 57,7 | . 00123 |  | . 87555 | 57,4 | . 12345 |
| 0.0755 | 8.87836 | 57,6 | 0.00124 | 0,3 | 8.87712 | 57,3 | I. 12288 |
| . 0756 | . 87894 | 57,6 | . 00124 |  | . 87770 | 57,2 | . 12230 |
| . 0757 | . 87951 | 57,5 | .00124 |  | . 87827 | 57,2 | . 12173 |
| . 0758 | . 88009 | 57,4 | . 00125 |  | . 87884 | 57, I | . 12116 |
| . 0759 | . 88066 | 57,3 | . 00125 |  | . 87941 | 57,0 | . 12059 |
| 0.0760 | 8.88123 | 57,3 | 0.00125 | 0,3 | 8.87998 | 56,9 | I. I2002 |
| .0761 | .88180 | 57,2 | .00126 |  | . 88055 | 56,8 | . 11945 |
| . 0762 | . 88238 | 57, I | .00126 |  | .88II2 | 56,8 | . II888 |
| . 0763 | . 88295 | 57,0 | .00126 |  | .88168 | 56,7 | . 11832 |
| . 0764 | . 88352 | 57,0 | . 00127 | , | . 88225 | 56,6 | . 11775 |
| 0.0765 | 8.88408 | 56,9 | 0.00127 | 0,3 | 8.88282 | 56,5 | I. 11718 |
| . 0766 | . 88465 | 56,8 | .00127 |  | . 88338 | 56,5 | . 11662 |
| . 0767 | . 88522 | 56,7 | .00128 |  | . 88394 | 56,4 | . 11606 |
| . 0768 | . 88579 | 56,7 | .00128 |  | . 88451 | 56,3 | . II 549 |
| . 0769 | . 88635 | 56,6 | .00128 |  | . 88507 | 56,3 | . II493 |
| 0.0770 | 8.88692 | 56,5 | 0.00129 | 0,3 | 8.88563 | 56,2 | I. II437 |
| .0771 | . 88748 | 56,4 | . 00129 |  | . 88620 | 56,1 | . 11380 |
| . 0772 | . 88805 | 56,4 | . 00129 |  | . 88676 | 56,0 | . II324 |
| . 0773 | . 88861 | 56,3 | .00130 |  | . 88732 | 56,0 | . I I268 |
| . 0774 | . 88917 | 56,2 | .00130 |  | . 88787 | 55,9 | . I'12I3 |
| 0.0775 | 8.88974 | 56,2 | 0.00130 | 0,3 | 8.88843 | 55,8 | I. III57 |
| . 0776 | . 89030 | 56, I | .0013I |  | . 88899 | 55,7 | . IIIOI |
| . 0777 | . 89086 | 56,0 | .00131 |  | . 88955 | 55,7 | . 11045 |
| . 0778 | . 89142 | 55,9 | .00131 |  | . 89010 | 55,6 | . 10990 |
| . 0779 | . 89198 | 55,9 | . 00132 |  | . 89056 | 55,5 | . 10934 |
| 0.0780 | 8.89253 | 55,8 | 0.00132 | 0,3 | 8.89122 | 55,5 | I. 10878 |
| .0781 | . 89309 | 55,7 | .00132 |  | . 89177 | 55,4 | . 10823 |
| . 0782 | . 89365 | 55,6 | .00133 |  | . 89232 | 55,3 | . 10768 |
| . 0783 | . 8942 I | 55,6 | .00133 |  | . 89288 | 55,2 | . 10712 |
| . 0784 | . 89476 | 55,5 | .00133 |  | . 89343 | 55,2 | . 10657 |
| 0.0785 | 8.89532 | 55,4 | 0.00134 | 0,3 | 8.89398 | 55, I | 1. 10602 |
| . 0786 | . 89587 | 55,4 | .00134 | . | . 89453 | 55,0 | . 10547 |
| . 0787 | . 89542 | 55,3 | .00134 |  | . 89508 | 55,0 | . 10492 |
| . 0788 | . 89698 | 55,2 | .00135 |  | . 89563 | 54,9 | . 10437 |
| . 0789 | . 89753 | 55,2 | .00135 |  | .89618 | 54,8 | . 10382 |
| 0.0790 | 8.89808 | 55, I | 0.00135 | 0,3 | 8.89672 | 54,7 | I. 10328 |
| .0791 | . 89863 | 55,0 | .00136 |  | . 89727 | 54,7 | . 10273 |
| . 0792 | . 89918 | 54,9 | .00136 |  | . 89782 | 54,6 | . 10218 |
| . 0793 | . 89973 | 54,9 | .00136 |  | . 89836 | 54,5 | . 10164 |
| . 0794 | . 90028 | 54,8 | . 00137 |  | . 89891 | 54,5 | . IOIO9 |
| 0.0795 | 8.90082 | 54,7 | 0.00137 | 0,3 | 8.89945 | 54,4 | I. 10055 |
| . 0796 | . 90137 | 54,7 | .00137 |  | . 90000 | 54,3 | . 10000 |
| . 0797 | .90192 | 54,6 | .00138 |  | . 90054 | 54,3 | . 09946 |
| . 0798 | . 90246 | 54,5 | . 00138 |  | .90108 | 54,2 | . 09892 |
| . 0799 | .90301 | 54,5 | .00138 |  | .90162 | 54, I | . 09838 |
| 0.0800 | 8.90355 | 54,4 | 0.00139 | 0,3 | 8.90216 | 54, I | 1.09784 |
| u | $\log \tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Smithsonian Tables

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0800 | 8.90355 | 54,4 | 0.00139 | 0,3 | 8.90216 | 54, I | 1.09784 |
| .0801 | . 90410 | 54,3 | . OOI39 |  | . 90271 | 54,0 | . 09729 |
| . 0802 | . 90464 | 54,3 | . 00140 |  | . 90324 | 53,9 | . 09676 |
| . 0803 | . 90518 | 54,2 | . 00140 |  | . 90380 | 53,9 | . 09620 |
| . 0804 | . 90572 | 54, I | . 00140 |  | . 90432 | 53,8 | . 09568 |
| 0.0805 | 8.90626 | 54, I | 0.00141 | 0,3 | 8.90486 | 53,7 | I. 09514 |
| . 0806 | .9068I | 54,0 | . 00141 | 0,3 | . 90540 | 53,6 | . 09460 |
| . 0807 | . 90734 | 53,9 | . 00141 | 0,3 | . 90593 | - 53,6 | . 09407 |
| . 0808 | . 90788 | 53,9 | . 00142 | 0,4 | . 90647 | 53,5 | . 09353 |
| . 0809 | . 90842 | 53,8 | .00142 | 0,4 | . 90700 | 53,4 | . 09300 |
| 0.0810 | 8.90896 | 53,7 | 0.00142 | 0,4 | 8.90754 | 53,4 | 1.09246 |
| .08II | . 90950 | 53,7 | . 00143 |  | . 90807 | 53,3 | . 09193 |
| . 0812 | .91003 | 53,6 | . 00143 |  | . 90860 | 53,3 | .09140 |
| .0813 | . 91057 | 53,5 | . 00143 |  | . 90914 | 53,2 | . 09086 |
| .08I4 | .91110 | 53,5 | . 00144 |  | . 90967 | 53, I | . 09033 |
| 0.08I5 | 8.91164 | 53,4 | 0.00144 | 0,4 | 8.91020 | 53, I | 1.08980 |
| .0816 | .91217 | 53,3 | . 00144 |  | . 91073 | 53,0 | . 08927 |
| .08I7 | .9127I | 53,3 | . 00145 |  | .91126 | 52,9 | . 08874 |
| .0818 | .91324 | 53,2 | . 00145 |  | .91179 | 52,9 | . 0882 I |
| .0819 | .91377 | 53,1 | . 00145 |  | .91231 | 52,8 | . 08769 |
| 0.0820 | 8.91430 | 53, I | 0.00146 | 0,4 | 8.91284 | 52,7 | 1.08716 |
| . 0821 | . 91483 | 53,0 | .00146 |  | .91337 | 52,7 | . 08663 |
| . 0822 | . 91536 | 53,0 | . 00147 |  | . 91390 | 52,6 | .08610 |
| . 0823 | .91589 | 52,9 | . 00147 |  | .91442 | 52,5 | . 08558 |
| . 0824 | . 91642 | 52,8 | .00147 |  | .91495 | 52,5 | . 08505 |
| 0.0825 | 8.91695 | 52,8 | 0.00148 | 0,4 | 8.91547 | 52,4 | I. 08453 |
| . 0826 | .91747 | 52,7 | . 00148 |  | .91599 | 52,3 | .08401 |
| . 0827 | .91800 | 52,6 | . 00148 |  | . 91652 | 52,3 | . 08348 |
| . 0828 | .91853 | 52,6 | . 00149 |  | .91704 | 52,2 | . 08296 |
| . 0829 | . 91905 | 52,5 | . 00149 |  | . 91756 | 52, I | . 08244 |
| 0.0830 | 8.91958 | 52,4 | 0.00149 | 0,4 | 8.91808 | 52,I | 1.08192 |
| . 0831 | .92010 | 52,4 | .00150 |  | . 91860 | 52,0 | .08140 |
| . 0832 | . 92062 | 52,3 | . 00150 |  | . 91912 | 52,0 | . 08088 |
| . 0833 | .92II5 | 52,3 | . 0015 I |  | . 91964 | 51,9 | .08036 |
| . 0834 | .92167 | 52,2 | . 00151 |  | . 92016 | 51;8 | . 07984 |
| 0.0835 | 8.92219 | 52, I | 0.00151 | 0,4 | 8.92068 | 51,8 | 1.07932 |
| . 0836 | . 92271 | 52, I | . 00152 |  | .92120 | 51,7 | . 07880 |
| . 0837 | . 92323 | 52,0 | . 00152 |  | .92171 | 51,6 | . 07829 |
| . 0838 | . 92375 | 51,9 | . 00152 |  | . 92223 | 51,6 | . 07777 |
| . 0839 | . 92427 | 51,9 | .00153 |  | . 92274 | 5I,5 | . 07726 |
| 0.0840 | 8.92479 | 51,8 | 0.00153 | 0,4 | 8.92326 | 5I,5 | 1.07674 |
| . 0841 | .9253I | 5I,8 | . 00153 |  | . 92377 | 5I,4 | . 07623 |
| . 0842 | . 92583 | 51,7 | . 00154 |  | . 92429 | 5I,3 | . 0757 I |
| . 0843 | . 92634 | 51,6 | . 00154 |  | . 92480 | 5I,3 | . 07520 |
| . 0844 | . 92686 | 51,6 | . 00154 |  | .9253I | 51,2 | . 07469 |
| 0.0845 | 8.92737 | 51,5 | 0.00155 | 0,4 | 8.92582 | 51,2 | 1.07418 |
| . 0846 | . 92789 | 51,5 | . 00155 |  | . 92634 | $5 \mathrm{I}, \mathrm{I}$ | . 07366 |
| . 0847 | . 92840 | 5I,4 | . 00156 |  | . 92685 | 51,0 | . 07315 |
| . 0848 | . 92892 | 5I,3 | . 00156 |  | . 92736 | 51,0 | . 07264 |
| . 0849 | . 92943 | 51,3 | . 00156 |  | . 92787 | 50,9 | . 07213 |
| 0.0850 | 8.92994 | 51,2 | 0.00157 | 0,4 | 8.92837 | 50,8 | 1.07163 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log csc gd u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0850 | 8.92994 | 51,2 | 0.00157 | 0,4 | 8.92837 | 50,8 | 1.07163 |
| . 0851 | . 93045 | 51,2 | .00157 |  | . 92888 | 50,8 | . 07112 |
| . 0852 | . 93096 | 51,1 | .00157 |  | . 92939 | 50,7 | .0706I |
| . 0853 | .93148 | 51,0 | .00158 |  | . 92990 | 50,7 | . 07010 |
| . 0854 | .93199 | 51,0 | . 00158 |  | . 93040 | 50,6 | . 06960 |
| 0.0855 | 8.93250 | 50,9 | 0.00159 | 0,4 | 8.93091 | 50,5 | 1.06909 |
| . 0856 | . 93300 | 50,9 | .00159 |  | .9314I | 50,5 | . 06859 |
| . 0857 | .9335I | 50,8 | . OOI 59 |  | .93192 | 50,4 | . 06808 |
| . 0858 | . 93402 | 50,7 | .00160 |  | . 93242 | 50,4 | . 06758 |
| . 0859 | . 93453 | 50,7 | .00160 |  | . 93293 | 50,3 | . 06707 |
| 0.0860 | 8.93503 | 50,6 | 0.00160 | 0,4 | 8.93343 | 50,3 | 1.06657 |
| . 0861 | . 93554 | 50,6 | .0016I |  | . 93393 | 50,2 | . 06607 |
| . 0862 | . 93604 | 50,5 | .0016I |  | . 93443 | 50, I | . 06557 |
| . 0863 | . 93655 | 50,4 | .00162 |  | . 93493 | 50, I | . 06507 |
| . 0864 | . 93705 | 50,4 | .00162 |  | . 93543 | 50,0 | . 06457 |
| 0.0865 | 8.93756 | 50,3 | 0.00162 | 0,4 | 8.93593 | 50,0 | 1.06407 |
| . 0866 | .93806 | 50,3 | . 00163 |  | . 93643 | 49,9 | . 06357 |
| . 0867 | . 93856 | 50,2 | .00163 |  | . 93693 | 49,8 | . 06307 |
| . 0868 | . 93907 | 50,2 | .00163 |  | . 93743 | 49,8 | . 06257 |
| . 0869 | . 93957 | 50,1 | .00164 |  | . 93793 | 49,7 | . 06207 |
| 0.0870 | 8.94007 | 50,0 | 0.00164 | 0,4 | 8.93843 | 49,7 | 1.06157 |
| . 0871 | . 94057 | 50,0 | .00165 |  | . 93892 | 49,6 | . 06108 |
| . 0872 | .94107 | 49,9 | . 00165 |  | . 93942 | 49,6 | . 06058 |
| . 0873 | .94157 | 49,9 | .00165 |  | .9399I | 49,5 | . 06009 |
| . 0874 | . 94206 | 49,8 | . 00166 |  | . 9404 I | 49,4 | . 051959 |
| 0.0875 | 8.94256 | 49,8 | 0.00166 | 0,4 | 8.94090 | 49,4 | 1.05910 |
| . 0876 | . 94306 | 49,7 | .00166 |  | . 94140 | 49,3 | . 05860 |
| . 0877 | . 94356 | 49,6 | . 00167 |  | .94189 | 49,3 | .058II |
| . 0878 | . 94405 | 49,6 | .00167 |  | . 94238 | 49,2 | . 05762 |
| . 0879 | . 94455 | 49,5 | .00168 |  | .94287 | 49,2 | . 05713 |
| 0.0880 | 8.94504 | 49,5 | 0.00168 | 0,4 | 8.94336 | 49, I | 1.05664 |
| .0881 | . 94554 | 49,4 | . 00168 |  | . 94385 | 49,0 | .05615 |
| . 0882 | . 94603 | 49,4 | . 00169 |  | . 94434 | 49,0 | . 05566 |
| . 0883 | . 94652 | 49,3 | . 00169 |  | . 94483 | 48,9 | . 05517 |
| . 0884 | . 94702 | 493 | .00169 |  | . 94532 | 48,9 | . 05468 |
| 0.0885 | 8.94751 | 49,2 | 0.00170 | 0,4 | 8.9458I | 48,8 | I. 05419 |
| . 0886 | . 94800 | 49, I | .00170 |  | . 94630 | 48,8 | . 05370 |
| . 0887 | . 94849 | 49, I | .00171 |  | . 94679 | 48,7 | .05321 |
| . 0888 | . 94898 | 49,0 | .00171 |  | . 94727 | 48,7 | . 05273 |
| . 0889 | . 94947 | 49,0 | .00171 |  | . 94776 | 48,6 | . 05224 |
| 0.0890 | 8.94996 | 48,9 | 0.00172 | 0,4 | 8.94825 | 48,5 | 1.05175 |
| . 0891 | . 95045 | 48,9 | . 00172 |  | . 94873 | 48,5 | . 05127 |
| . 0892 | . 95094 | 48,8 | .00173 |  | . 94922 | 48,4 | . 05078 |
| . 0893 | . 95143 | 48,8 | .00173 |  | . 94970 | 48,4 | . 05030 |
| . 0894 | . 95192 | 48,7 | .00173 |  | . 95018 | 48,3 | . 04982 |
| 0.0895 | 8.95240 | 48,7 | 0.00174 | 0,4 | 8.95067 | 48,3 | 1.04933 |
| . 0896 | . 95289 | 48,6 | .00174 |  | .95115 | 48,2 | . 04885 |
| . 0897 | . 95337 | 48,5 | .00174 |  | .95163 | 48,2 | . 04837 |
| . 0898 | . 95386 | 48,5 | .00175 |  | .95211 | 48, I | . 04789 |
| . 0899 | . 95434 | 48,4 | .00175 |  | . 95259 | 48,0 | . 0474 I |
| 0.0900 | 8.95483 | 48,4 | 0.00176 | 0,4 | 8.95307 | 48,0 | 1.04693 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log sec od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0900 | 8.95483 | 48,4 | 0.00176 | 0,4 | 8.95307 | 48,0 | 1.04693 |
| .0901 | .9553I | 48,3 | .00176 |  | . 95355 | 47,9 | . 04645 |
| . 0902 | .95580 | 48,3 | .00176 |  | . 95403 | 47,9 | . 04597 |
| . 0903 | . 95628 | 48,2 | .00177 |  | .9545I | 47,8 | . 04549 |
| . 0904 | . 95676 | 48,2 | .00177 |  | . 95499 | 47,8 | . 04501 |
| 0.0905 | 8.95724 | 48,1 | 0.00178 | 0,4 | 8.95547 | 47,7 | 1.04453 |
| . 0906 | . 95772 | 48, I | .00178 |  | . 95594 | 47,7 | . 04406 |
| . 0907 | . 95820 | 48,0 | .00178 |  | . 95642 | 47,6 | . 04358 |
| . 0908 | . 95868 | 48,0 | .00179 |  | . 95689 | 47,6 | .043II |
| . 0909 | .95916 | 47,9 | .00179 |  | . 95737 | 47,5 | . 04263 |
| 0.0910 | 8.95964 | 47,9 | 0.00180 | 0,4 | 8.95784 | 47,5 | 1.04216 |
| . 091 I | . 96012 | 47,8 | .00180 |  | . 95832 | 47,4 | .04168 |
| . 0912 | . 96060 | 47,8 | .00180 |  | . 95879 | 47,4 | .04121 |
| .0913 | .96107 | 47,7 | .00181 |  | . 95927 | 47,3 | . 04073 |
| .0914 | .96155 | 47,6 | .0018I |  | . 95974 | 47,3 | . 04026 |
| 0.0915 | 8.96203 | 47,6 | 0.00182 | 0,4 | 8.96021 | 47,2 | 1.03979 |
| .0916 | . 96250 | 47,5 | . 00182 |  | . 96068 | 47, 1 | . 03932 |
| .0917 | . 96298 | 47,5 | .00182 |  | .95115 | 47, 1 | . 03885 |
| .0918 | . 96345 | 47,4 | .00183 |  | . 96163 | 47,0 | . 03837 |
| . 0919 | . 96393 | 47,4 | .00183 |  | .96210 | 47,0 | . 03790 |
| 0.0920 | 8.96440 | 47,3 | 0.00184 | 0,4 | 8.96256 | 46,9 | 1.03744 |
| .0921 | . 96487 | 47,3 | .00184 |  | . 96303 | 46,9 | . 03697 |
| . 0922 | . 96535 | 47,2 | .00184 |  | . 96350 | 46,8 | . 03650 |
| . 0923 | . 96582 | 47,2 | .00185 |  | .96397 | 46,8 | . 03603 |
| . 0924 | . 96629 | 47, I | .00185 |  | . 96444 | 46,7 | . 03556 |
| 0.0925 | 8.96676 | 47, 1 | 0.00186 | 0,4 | 8.96491 | 46,7 | 1.03509 |
| . 0926 | . 96723 | 47,0 | . 00186 |  | . 96537 | 46,6 | . 03463 |
| . 0927 | . 96770 | 47,0 | .00186 |  | . 96584 | 46,6 | .03416 |
| . 0928 | .96817 | 46,9 | .00187 |  | . 96630 | 46,5 | . 03370 |
| . 0929 | .96864 | 46,9 | .00187 |  | . 96677 | 46,5 | . 03323 |
| 0.0930 | 8.96911 | 46,8 | 0.00188 | 0,4 | 8.96723 | 46,4 | 1.03277 |
| . 093 I | . 96958 | 46,8 | .00188 |  | . 96770 | 46,4 | . 03230 |
| . 0932 | . 97004 | 46,7 | .00188 |  | . 96816 | 46,3 | . 03184 |
| . 0933 | .97051 | 46,7 | .00189 |  | . 96862 | 46,3 | .03I38 |
| . 0934 | . 97098 | 46,6 | .00189 |  | . 96909 | 46,2 | . 03091 |
| 0.0935 | 8.97144 | 46,6 | 0.00190 | 0,4 | 8.96955 | 46,2 | 1.03045 |
| . 0936 | . 97191 | 46,5 | . 00190 | , | . 97001 | 46, I | . 02999 |
| . 0937 | . 97237 | 46,5 | . 00190 |  | . 97047 | 46, I | . 02953 |
| . 0938 | . 97284 | 46,4 | .0019I | - | . 97093 | 46,0 | . 02907 |
| . 0939 | . 97330 | 46,4 | .00191 |  | . 97139 | 46,0 | . 0286 I |
| 0.0940 | 8.97377 | 46,3 | 0.00192 | 0,4 | 8.97185 | 45,9 | I.028I5 |
| .094I | . 97423 | 46,3 | . 00192 |  | .9723I | 45,9 | . 02769 |
| . 0942 | . 97469 | 46,2 | . 00192 |  | . 97277 | 45,8 | . 02723 |
| . 0943 | . 97516 | 46,2 | .00193 |  | . 97323 | 45,8 | . 02677 |
| . 0944 | . 97562 | 46, 1 | .00193 |  | . 97368 | 45,7 | . 02632 |
| 0.0945 | 8.97608 | 46, I | 0.00194 | 0,4 | 8.97414 | 45,7 | 1.02586 |
| . 0946 | . 97654 | 46,0 | . 00194 |  | . 97460 | 45,6 | . 02540 |
| . 0947 | . 97700 | 46,0 | . 00194 |  | . 97505 | 45,6 | . 02495 |
| . 0948 | . 97746 | 45,9 | .00195 |  | .9755I | 45,5 | . 02449 |
| . 0949 | . 97792 | 45,9 | .00195 |  | . 97597 | 45,5 | . 02403 |
| 0.0950 | 8.97838 | 45,9 | 0.00196 | 0,4 | 8.97642 | 45,4 | 1.02358 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0950 | 8.97838 | 45,9 | 0.00196 | 0,4 | 8.97642 | 45,4 | 1.02358 |
| .0951 | . 97883 | 45,8 | . 00196 |  | . 97687 | 45,4 | .02313 |
| . 0952 | . 97929 | 45,8 | .00197 |  | . 97733 | 45,3 | . 02267 |
| . 0953 | . 97975 | 45,7 | . 00197 |  | . 97778 | 45,3 | . 02222 |
| . 0954 | .9802 I | 45,7 | .00197 |  | . 97823 | 45,2 | . 02177 |
| 0.0955 | 8.98066 | 45,6 | 0.00198 | 0,4 | 8.97869 | 45,2 | I. 02131 |
| . 0956 | .98II2 | 45,6 | . 00198 |  | .97914 | 45,2 | . 02086 |
| . 0957 | .98I57 | 45,5 | .00199 |  | . 97959 | 45, I | .0204I |
| . 0958 | . 98203 | 45,5 | . 00199 |  | . 98004 | 45, 1 | . 01996 |
| . 0959 | . 98248 | 45,4 | .00199 |  | . 98049 | 45,0 | . 01951 |
| 0.0960 | 8.98294 | 45,4 | 0.00200 | 0,4 | 8.98094 | 45,0 | 1. 01906 |
| .0961 | . 98339 | 45,3 | . 00200 |  | .98139 | 44,9 | .01861 |
| . 0962 | . 98384 | 45,3 | .00201 |  | .98I84 | 44,9 | .018i6 |
| . 0963 | . 98430 | 45,2 | .0020I |  | . 98229 | 44,8 | .01771 |
| . 0964 | . 98475 | 45,2 | .0020I |  | . 98273 | 44,8. | . 01727 |
| 0.0965 | 8.98520 | 45, I | 0.00202 | 0,4 | 8.98318 | 44,7 | 1.01682 |
| . 0966 | . 98565 | 45, I | . 00202 |  | . 98363 | 44,7 | . 01637 |
| . 0967 | .98610 | 45, I- | .00203 |  | . 98408 | 44,6 | . OI 592 |
| . 0968 | . 98655 | 45,0 | .00203 |  | . 98452 | 44,6 | . 01548 |
| . 0969 | .98700 | 45,0 | . 00204 |  | . 98497 | 44,5 | . 01503 |
| 0.0970 | 8.98745 | 44,9 | 0.00204 | 0,4 | 8.98541 | 44,5 | I.OI459 |
| . 0971 | . 98790 | 44,9 | . 00204 |  | . 98586 | 44,5 | .01414 |
| . 0972 | . 98835 | 44,8 | . 00205 |  | . 98630 | 44,4 | . 01370 |
| . 0973 | . 98880 | 44,8 | . 00205 |  | . 98675 | 44,4 | .OI325 |
| . 0974 | . 98925 | 44,7 | . 00206 |  | . 98719 | 44,3 | .0128I |
| 0.0975 | 8.98969 | 44,7 | 0.00206 | 0,4 | 8.98763 | 44,3 | I. 01237 |
| . 0976 | .99014 | 44,6 | . 00207 |  | . 98807 | 44,2 | . OI 193 |
| . 0977 | . 99059 | 44,6 | . 00207 | - | . 98852 | 44,2 | . OII48 |
| . 0978 | .99103 | 44,5 | .00207 |  | . 98896 | 44, I. | . OI IO4 |
| . 0979 | . 99148 | 44,5 | . 00208 |  | . 98940 | 44, I- | . 01060 |
| 0.0980 | 8.99192 | 44,5 | 0.00208 | 0,4 | 8.98984 | 44,0 | 1.01016 |
| .098I | -.99237 | 44,4 | . 00209 |  | . 99028 | 44,0 | . 00972 |
| . 0982 | .99281 | 44,4 | . 00209 |  | . 99072 | 43,9 | . 00928 |
| . 0983 | . 99325 | 44,3 | . 00209 |  | .99116 | 43,9 | . 00884 |
| . 0984 | . 99370 | 44,3 | . 00210 |  | . 99160 | 43,9 | . 00810 |
| 0.0985 | 8.99414 | 44,2 | 0.00210 | 0,4 | 8.99203 | 43,8 | 1.00797 |
| . 0986 | . 99458 | 44,2 | .002̇II |  | . 99247 | 43,8 | . 00753 |
| . 0987 | . 99502 | 44,2 | .002II |  | . 99291 | 43,7 | . 00709 |
| . 0988 | . 99546 | 44, I | . 00212 |  | . 99335 | 43,7 | . 00665 |
| . 0989 | . 99590 | 44,1- | . 00212 |  | . 99378 | 43,6 | . 00622 |
| 0.0990 | 8.99634 | 44,0 | 0.00212 | 0,4 | 8.99422 | 43,6 | I. 00578 |
| . 0991 | . 99678 | 44,0 | . 00213 |  | . 99466 | 43,5 | . 00534 |
| . 0992 | . 99722 | 43,9 | . 00213 |  | . 99509 | 43,5 | . 00491 |
| . 0993 | . 99766 | 43,9 | .002I4 |  | . 99553 | 43,4 | . 00447 |
| . 0994 | .99810 | 43,8 | .00214 |  | . 99596 | 43,4 | . 00404 |
| 0.0995 | 8.99854 | 43,8 | 0.00215 | 0,4 | 8.99639 | 43,4 | 1.00361 |
| . 0996 | . 99898 | 43,7 | . 00215 |  | . 99683 | 43,3 | . 00317 |
| . 0997 | . 99941 | 43,7 | .00215 |  | . 99726 | 43,3 | . 00274 |
| . 0998 | . 99985 | 43,7 | . 00216 |  | . 99769 | 43,2. | .0023I |
| . 0999 | 9.00029 | 43,6 | .00216 |  | .99812 | 43,2. | . 00188 |
| 0.1000 | 9.00072 | 43,6 | 0.00217 | 0,4 | 8.99856 | 43, I | I. 00144 |
| u | $\log \tan g d \mu$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.100 | 9.00072 | 435,7 | 0.00217 | 4,3 | 8.99856 | 431,4 | I. 00144 |
| . IOI | . 00506 | 43I,5 | .0022I | 4,4 | 9.00285 | 427, I | 0.99715 |
| . 102 | . 00935 | 427,3 | . 00226 | 4,4 | . 00710 | 422,8 | . 99290 |
| . 103 | . O1360 | 423, I | . 00230 | 4,5 | . OII3I | 418,7 | . 98869 |
| . 104 | . 01782 | 419, I | . 00234 | 4,5 | . O1547 | 414,6 | . 98453 |
| 0.105 | 9.02199 | 415,I | 0.00239 | 4,5 | 9.01960 | 410,6 | 0.98040 |
| . 106 | . 02612 | 4II,2 | . 00244 | 4,6 | . 02368 | 406,7 | . 97632 |
| . 107 | .03021 | 407,4 | . 00248 | 4,6 | . 02773 | 402,8 | . 97227 |
| . 108 | . 03427 | 403,7 | . 00253 | 4,7 | .03174 | 399,0 | . 96826 |
| . 109 | . 03829 | 400,0 | . 00257 | 4,7 | . 03571 | 395,3 | . 96429 |
| O.IIO | 9.04227 | 396,4 | 0.00262 | 4,8 | 9.03965 | 391,6 | 0.96035 |
| . III | . 04621 | 392,9 | . 00267 | 4,8 | . 04354 | 388, I | . 95646 |
| . II2 | .05013 | 389,4 | . 00272 | 4,8 | . 0474 I | 384,5 | . 95259 |
| . II3 | . 05400 | 386,0 | .00277 | 4,9 | .05124 | 381, I | . 94876 |
| . II4 | . 05785 | 382,6 | . 00282 | 4,9 | . 05503 | 377,7 | . 94497 |
| 0.115 | 9.06165 | 379,3 | 0.00287 | 5,0 | 9.05879 | 374,3 | 0.94121 |
| . 116 | . 06543 | 376, I | . 00292 | 5,0 | . 06252 | 371 I | . 93748 |
| . II7 | .06918 | 372,9 | . 00297 | 5, I | . 06621 | 367,8 | . 93379 |
| . 118 | . 07289 | 369,8 | . 00302 | 5, I | . 06987 | 364,7 | . 93013 |
| . 119 | . 07657 | 366,7 | . 00307 | 5, I | . 07350 | 36I,5 | . 92650 |
| 0.120 | 9.08022 | 363,6 | 0.00312 | 5,2 | 9.07710 | 358,5 | 0.92290 |
| . 12 I | . 08384 | 360,7 | . 00317 | 5,2 | . 08067 | 355,4 | . 91933 |
| . 122 | . 08744 | 357,7 | . 00322 | 5,3 | .0842I | 352,5 | .91579 |
| . 123 | . 09100 | 354,9 | . 00328 | 5,3 | . 08772 | 349,5 | . 91228 |
| . 124 | . 09453 | 352,0 | . 00333 | 5,4 | .09120 | 346,7 | . 90880 |
| 0.125 | 9.09804 | 349,2 | 0.00338 | 5,4 | 9.09466 | 343,8 | 0.90534 |
| . 126 | . 10152 | 346,5 | . 00344 | 5,4 | . 09808 | 341, I | . 90192 |
| . 127 | . 10497 | 343,8 | . 00349 | 5,5 | . 10148 | 338,3 | . 89852 |
| . 128 | . 10840 | 341, I | . 00355 | 5,5 | . 10485 | 335,6 | . 89515 |
| . 129 | . I I I79 | 338,5 | .00360 | 5,6 | . 108I9 | 333,0 | .89181 |
| O. I30 | 9.11517 | 336,0 | 0.00366 | 5,6 | 9.III5I | 330,3 | 0.88849 |
| . I3 I | . II85I | 333,4 | . 00372 | 5,7 | . II480 | 327,8 | . 88520 |
| . I32 | . 12183 | 330,9 | . 00377 | 5,7 | . 11806 | 325,2 | .88I94 |
| . I33 | . I2513 | 328,5 | .00383 | 5,7 | . 12130 | 322,7 | . 87870 |
| . 134 | . 12840 | 326,0 | . 00389 | 5,8 | . 12452 | 320,3 | . 87548 |
| 0. 135 | 9.13165 | 323,7 | 0.00395 | 5,8 | 9. 12771 | 317,8 | 0.87229 |
| . 136 | . I3488 | 321,3 | . 00400 | 5,9 | . I3087 | 315,4 | . 86913 |
| . 137 | . I3808 | 319,0 | . 00406 | 5,9 | - 13402 | 313,1 | . 86598 |
| . 138 | . 14126 | 316,7 | .00412 | 6,0 | . 13713 | 310,7 | . 86287 |
| . 139 | . 14441 | 314,5 | .00418 | 6,0 | . 14023 | 308,5 | . 85977 |
| 0.140 | 9. 14755 | 312,2 | 0.00424 | 6,0 | 9.14330 | 306,2 | 0.85670 |
| . I4I | . 15066 | 310,0 | . 00430 | 6, I | . 14635 | 304,0 | . 85365 |
| . 142 | . 15375 | 307,9. | . 00436 | 6,1 | . 14938 | 301,8 | . 85062 |
| . I43 | . 15682 | 305,8 | . 00443 | 6,2 | . 15239 | 299,6 | . 84761 |
| . I44 | . 15986 | 303,7 | . 00449 | 6,2 | . 15538 | 297,5 | . 84462 |
| 0.145 | 9.16289 | 301,6 | 0.00455 | 6,3 | 9. 15834 | 295,4 | 0.84166 |
| . 146 | . 16589 | 299,6 | .0046I | 6,3 | . 16128 | 293,3 | . 83872 |
| . 147 | . 16888 | 297,6 | . 00468 | 6,3 | . 16420 | 291,2 | . 83580 |
| . 148 | . 17185 | 295,6 | . 00474 | 6,4 | . 1671 I | 289,2 | . 83289 |
| . 149 | . 17479 | 293,6 | . 00480 | 6,4 | . 16999 | 287,2 | . 83001 |
| 0.150 | 9.17772 | 291,7 | 0.00487 | 6,5 | 9.17285 | 285,2 | 0.82715 |
| $u$ | $l o g t a n g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{singdu}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.150 | 9.17772 | 291,7 | 0.00487 | 6,5 | 9. 17285 | 285,2 | 0.82715 |
| .15I | . 18063 | 289,8 | . 00493 | 6,5 | . 17569 | 283,3 | .8243I |
| . 152 | . 18351 | 287,9 | . 00500 | 6,6 | . 17852 | 28I, 4 | .82I48 |
| . 153 | . 18638 | 286, I | . 00506 | 6,6 | .18I32 | 279,5 | .81868 |
| . 154 | . 18924 | 284,2 | .005I3 | 6,6 | .184II | 277,6 | .81589 |
| 0.155 | 9.19207 | 282,4 | 0.00520 | 6,7 | 9. 18687 | 275,8 | 0.81313 |
| . 156 | . 19488 | 280,6 | . 00526 | 6,7 | . 18962 | 273,9 | .81038 |
| . 157 | . 19768 | 278,9 | . 00533 | 6,8 | . 19235 | 272,1 | . 80765 |
| . 158 | . 20046 | 277, I | . 00540 | 6,8 | . 19506 | 270,3 | . 80494 |
| . 159 | . 20323 | 275,4 | . 00547 | 6,8 | . 19776 | 268,6 | . 80224 |
| 0.160 | 9.20597 | 273,7 | 0.00554 | 6,9 | 9.20044 | 266,9 | 0.79956 |
| .161 | . 20870 | 272,I | . 00560 | 6,9 | . 20310 | 265,1 | . 79690 |
| . 162 | .2114I | 270,4 | . 00567 | 7,0 | . 20574 | 263,4 | . 79426 |
| .163 | . 21411 | 268,8 | . 00574 | 7,0 | . 20837 | 26I, 8 | . 79163 |
| . 164 | . 21679 | 267,2 | .00581 | 7,I | . 21097 | 260,1 | . 78903 |
| 0. 165 | 9.21945 | 265,6 | 0.00589 | 7,I | 9.21357 | 258,5 | 0.78643 |
| . 166 | . 22210 | 264,0 | . 00596 | 7,I | .21614 | 256,9 | . 78386 |
| . 167 | . 22473 | 262,5 | . 00603 | 7,2 | .21871 | 255,3 | .78129 |
| . 168 | . 22735 | 260,9 | .00610 | 7,2 | . 22125 | 253,7 | . 77875 |
| .169 | . 22995 | 259,4 | .00617 | 7,3 | . 22378 | 252,2 | . 77622 |
| 0.170 | 9.23254 | 257,9 | 0.00625 | 7,3 | 9.22629 | 250,6 | 0.77371 |
| . 171 | .2351 I | 256,4 | . 00632 | 7,4 | . 22879 | 249, I | . 77121 |
| . 172 | . 23767 | 255,0 | . 00639 | 7,4 | .23128 | 247,6 | . 76872 |
| . 173 | . 2402 I | 253,5 | . 00647 | 7,4 | . 23374 | 246, 1 | . 76626 |
| . 174 | . 24274 | 252, I | . 00654 | 7,5 | . 23620 | 244,6 | . 76380 |
| 0.175 | 9.24525 | 250,7 | 0.00662 | 7,5 | 9.23864 | 243,2 | 0.76136 |
| . 176 | . 24775 | 249,3 | . 00669 | 7,6 | . 24106 | 241,7 | . 75894 |
| . 177 | . 25024. | 247,9 | . 00677 | 7,6 | . 24347 | 240,3 | . 75653 |
| . 178 | .2527I | 246,5 | . 00684 | 7,6 | . 24587 | 238,9 | . 75413 |
| . 179 | . 25517 | 245,2 | . 00692 | 7,7 | . 24825 | 237,5 | . 75175 |
| 0.180 | 9.25762 | 243,9 | 0.00700 | 7,7 | 9.25062 | 236,1 | 0.74938 |
| . 181 | . 26005 | 242,5 | . 00708 | 7,8 | . 25297 | 234,8 | . 74703 |
| . 182 | . 26247 | 241,3 | . 00715 | 7,8 | . 25531 | 233,4 | . 74469 |
| .183 | . 26487 | 240,0 | . 00723 | 7,9 | . 25764 | 232,I | .74236 |
| . 184 | . 26727 | 238,7 | . 0073 I | 7,9 | . 25996 | 230,8 | . 74004 |
| 0. 185 | 9.26965 | 237,4 | 0.00739 | 7,9 | 9.26226 | 229,5 | 0.73774 |
| . 186 | . 27201 | 236,2 | . 00747 | 8,0 | . 26454 | 228,2 | . 73546 |
| .187 | . 27437 | 234,9 | . 00755 | 8,0 | . 26682 | 226,9 | . 733 I8 |
| . 188 | .2767I | 233,7 | .00763 | 8 , I | . 26908 | 225,7 | . 73092 |
| . 189 | . 27904 | 232,5 | . 00771 | 8, I | . 27133 | 224,4 | . 72867 |
| 0.190 | 9.28 I 36 | 23I,3 | 0.00779 | 8,2 | 9.27357 | 223,2 | 0.72643 |
| . 191 | . 28367 | 230,1 | . 00787 | 8,2 | . 27580 | 22I,9 | . 72420 |
| . 192 | . 28597 | 229,0 | . 00796 | 8,2 | . 27801 | 220,7 | . 72199 |
| . 193 | . 28825 | 227,8 | . 00804 | 8,3 | .2802I | 219,5 | . 71979 |
| . 194 | .29052 | 226,7 | .00812 | 8,3 | .28240 | 218,3 | . 71760 |
| 0. 195 | 9.29278 | 225,5 | 0.00821 | 8,4 | 9.28458 | 217,2 | 0.71542 |
| . 196 | . 29503 | 224,4 | . 00829 | 8,4 | . 28674 | 216,0 | . 71326 |
| . 197 | . 29727 | 223,3 | . 00837 | 8,4 | . 28890 | 214,9 | . 71110 |
| . 198 | . 29950 | 222,2 | . 00846 | 8,5 | . 29104 | 213,7 | . 70896 |
| . 199 | . 30172 | 22I, I | . 00854 | 8,5 | . 29317 | 212,6 | . 70683 |
| 0.200 | 9.30392 | 220,0 | 0.00863 | 8,6 | 9.29529 | 2II,5 | 0.70471 |
| 4 | $\log \tan \mathrm{gd} u$ | ' $\omega$ F ${ }_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathbf{u}$ |

[^12]Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.200 | 9.30392 | 220,0 | 0.00863 | 8,6 | 9.29529 | 2II,5 | 0.70471 |
| . 201 | . 30612 | 219,0 | . 00871 | 8,6 | . 29740 | 210,4 | . 70260 |
| . 202 | . 30830 | 217,9 | . 00880 | 8,7 | . 29950 | 209,3 | . 70050 |
| . 203 | . 31047 | 216,9 | . 00889 | 8,7 | . 30159 | 208,2 | . 6984 I |
| . 204 | . 31264 | 215,8 | . 00897 | 8,7 | . 30366 | 207, I | . 69634 |
| 0.205 | 9.31479 | 214,8 | 0.00906 | 8,8 | $9 \cdot 30573$ | 206,0 | 0.69427 |
| . 206 | . 31693 | 213,8 | .009I5 | 8,8 | . 30778 | 205,0 | . 69222 |
| . 207 | . 31907 | 212,8 | . 00924 | 8,9 | . 30983 | 203,9 | . 69017 |
| . 208 | -32II9 | 211,8 | . 00933 | 8,9 | - 31186 | 202,9 | .68814 |
| . 209 | . 32330 | 210,8 | . 00942 | 8,9 | . 31389 | 201,9 | .686I I |
| 0.210 | 9.32541 | 209,8 | 0.00951 | 9,0 | 9.31590 | 200,8 | 0.68410 |
| . 211 | . 32750 | 208,9 | . 00960 | 9,0 | . 31790 | 199,8 | . 68210 |
| . 212 | . 32958 | 207,9 | . 00969 | 9, I | . 31990 | 198,8 | .68010 |
| . 213 | . 33166 | 207,0 | . 00978 | 9,I | - 32188 | 197,9 | . 67812 |
| . 214 | . 33372 | 206,0 | . 00987 | 9,2 | . 32385 | 196,9 | . 67615 |
| 0.215 | 9.33578 | 205, I | 0.00996 | 9,2 | 9.32582 | 195,9 | 0.67418 |
| . 216 | . 33783 | 204,2 | . 01005 | 9,2 | . 32777 | 194,9 | . 67223 |
| . 217 | . 33986 | 203,3 | . 01015 | 9,3 | . 32972 | 194,0 | . 67028 |
| . 218 | . 34189 | 202,4 | .01024 | 9,3 | . 33165 | 193,0 | . 66835 |
| . 219 | .3439I | 201,5 | . 01033 | 9,4 | - 33358 | 192, I | . 66642 |
| 0.220 | $9 \cdot 34592$ | 200,6 | 0.01043 | 9,4 | 9.33549 | 191,2 | 0.66451 |
| . 22 I | . 34792 | 199,7 | . 01052 | 9,4 | . 33740 | 190,3 | . 66260 |
| . 222 | . 34991 | 198,8 | . 01062 | 9,5 | . 33930 | 189,3 | . 66070 |
| . 223 | . 35190 | 198,0 | . 01071 | 9,5 | -34119 | 188,4 | . 6588 I |
| . 224 | . 35387 | 197, I | . 01081 | 9,6 | . 34307 | 187,5 | . 65693 |
| 0.225 | 9.35584 | 196,3 | 0.01090 | 9,6 | 9.34494 | 186,7 | 0.65506 |
| . 226 | . 35780 | 195,4 | . 01100 | 9,7 | . 34680 | 185,8 | . 65320 |
| . 227 | . 35975 | 194,6 | . OIIO9 | 9,7 | . 34865 | 184,9 | . 65135 |
| . 228 | . 36169 | 193,8 | . OIII9 | 9,7 | . 35050 | 184,0 | . 64950 |
| . 229 | . 36362 | 193,0 | . OII 29 | 9,8 | . 35234 | 183,2 | . 64766 |
| 0.230 | 9.36555 | 192, I | 0.01139 | 9,8 | 9.35416 | 182,3 | 0.64584 |
| . 231 | . 36747 | 191,3 | . OII49 | 9,9 | . 35598 | 181,5 | . 64402 |
| . 232 | . 36938 | 190,5 | . 01158 | 9,9 | . 35779 | 180,6 | . 6422 I |
| . 233 | . 37128 | 189,8 | . 01168 | 9,9 | . 35959 | I79,8 | . 64047 |
| . 234 | .37317 | 189,0 | . 01178 | 10,0 | -36I39 | I79,0 | . 63861 |
| 0.235 | 9.37506 | 188,2 | 0.01188 | 10,0 | 9.36317 | 178,2 | 0.63683 |
| . 236 | . 37694 | 187,4 | . 01198 | 10, 1 | . 36495 | 177,4 | . 63505 |
| . 237 | .3788I | 186,7 | . 01208 | 10, I | . 36672 | 176,6 | . 63328 |
| . 238 | . 38067 | 185,9 | . 01219 | 10, I | -36848 | I75,8 | . 63152 |
| . 239 | . 38252 | 185,2 | . 01229 | 10,2 | . 37024 | 175,0 | . 62976 |
| 0.240 | 9.38437 | 184,4 | 0.01239 | 10,2 | 9.37198 | 174,2 | 0.62802 |
| . 241 | . 3862 I | 183,7 | . 01249 | 10,3 | . 37372 | 173,4 | . 62628 |
| . 242 | -38805 | 183,0 | . 01259 | 10,3 | - 37545 | 172,6 | . 62455 |
| . 243 | . 38987 | 182,2 | . 01270 | 10,4 | - 37717 | I71,9 | . 62283 |
| . 244 | . 39169 | I8I,5 | . 01280 | IO,4 | . 37889 | I7I, I | .62III |
| 0.245 | 9.39350 | 180,8 | 0.01291 | 10,4 | 9.38060 | I70,4 | 0.61940 |
| . 246 | -3953I | 180,1 | . 01301 | 10,5 | - 38230 | 169,6 | . 61770 |
| . 247 | . 39710 | 179,4 | . O1312 | 10,5 | - 38399 | 168,9 | . 61601 |
| . 248 | . 39889 | 178,7 | . O1322 | 10,6 | . 38567 | 168, 1 | . 61433 |
| . 249 | . 40068 | 178,0 | . O1333 | 10,6 | -38735 | 167,4 | .61265 |
| 0.250 | 9.40245 | 177,3 | 0.01343 | 10,6 | 9.38902 | 166,7 | 0.61098 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | : $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} \mathrm{u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.250 | 9.40245 | 177,3 | 0.01343 | I0,6 | 9.38902 | 166,7 | 0.61098 |
| .25I | . 40422 | 175,6 | . OI354 | 10,7 | . 39069 | 166,0 | . 60931 |
| . 252 | . 40599 | 176,0 | . 01365 | 10,7 | . 39234 | 165,3 | . 60766 |
| . 253 | . 40774 | 175,3 | . OI375 | 10,8 | . 39399 | 164,5 | . 60601 |
| . 254 | . 40949 | 174,6 | .01386 | 10,8 | - 39563 | 163,8 | . 60437 |
| 0.255 | 9.41124 | 174,0 | 0.01397 | 10,8 | 9.39727 | 163, 1 | 0.60273 |
| . 256 | . 41297 | 173,3 | . 01408 | 10,9 | . 39890 | 162,5 | . 60110 |
| . 257 | . 41470 | 172,7 | . 01419 | 10,9 | . 40052 | 161,8 | . 59948 |
| . 258 | . 41643 | 172,0 | . 01430 | I I,O | . 40213 | 161, 1 | . 59787 |
| . 259 | .41814 | I7I,4 | . 0144 I | I I, 0 | . 40374 | 160,4 | . 59626 |
| 0.260 | 9.41986 | 170,8 | 0.01452 | II,O | 9.40534 | I 59,7 | 0.59466 |
| .26I | . 42156 | 170,2 | . 01463 | II, I | . 40693 | I 59, I | . 59307 |
| . 262 | . 42326 | 169,5 | . 01474 | II, I | . 40852 | 158,4 | . 59148 |
| . 263 | . 42495 | 168,9 | . OI485 | II, 2 | .41010 | 157,8 | . 58990 |
| . 264 | . 42664 | 168,3 | . OI496 | II, 2 | . 41168 | 157, I | . 58832 |
| 0.265 | 9.42832 | 167,7 | 0.01507 | II, 2 | 9.41324 | 156,5 | 0.58676 |
| . 266 | . 42999 | 167, 1 | . OI519 | II,3 | . 41480 | 155,8 | . 58520 |
| . 267 | . 43166 | 166,5 | . OI530 | II,3 | . 41636 | 155,2 | . 58364 |
| . 268 | . 43332 | 165,9 | .OI54I | II,4 | .41791 | I54,5 | . 58209 |
| .269 | . 43498 | 165,3 | . O1553 | II,4 | . 41945 | 153,9 | . 58055 |
| 0.270 | 9.43663 | 164,7 | 0.01564 | II, 4 | 9.42099 | I 53,3 | 0.57901 |
| . 271 | . 43827 | 164,2 | . OI 576 | II,5 | . 42252 | 152,7 | . 57748 |
| . 272 | . 4399 I | 163,6 | .OI587 | I 1 ,5 | . 42404 | 152, I | . 57596 |
| . 273 | . 44154 | 163,0 | . 01599 | I I, 6 | . 42556 | 151,4 | . 57444 |
| . 274 | . 44317 | 162,4 | .01610 | I I, 6 | . 42707 | 150,8 | . 57293 |
| 0.275 | 9.44479 | 161,9 | 0.01622 | I I, 7 | 9.42857 | 150,2 | 0.57143 |
| . 276 | . 4464 I | 16I,3 | . 01634 | II,7 | . 43007 | 149,6 | . 56993 |
| . 277 | . 44802 | 160,8 | .01645 | II,7 | . 43157 | 149,0 | . 56843 |
| . 278 | . 44962 | 160,2 | .01657 | I I, 8 | . 43305 | 148,5 | . 56695 |
| . 279 | . 45122 | 159,7 | .01669 | I 1,8 | . 43454 | 147,9 | . 56546 |
| 0.280 | 9.45282 | I59, I | 0.01681 | II,9 | 9.43601 | 147,3 | 0.56399 |
| .28I | . 45441 | 158,6 | .01693 | I I,9 | . 43748 | 146,7 | . 56252 |
| . 282 | . 45599 | 158,1 | . O1704 | II,9 | . 43895 | 146, I | . 56105 |
| .283 | . 45757 | 157,5 | .01716 | 12,0 | . 44040 | 145,6 | . 55960 |
| . 284 | . 45914 | 157,0 | .01728 | 12,0 | .44186 | 145,0 | . 55814 |
| 0.285 | 9.46071 | 156,5 | 0.01740 | 12,I | 9.44330 | 144,4 | 0.55670 |
| . 285 | . 46227 | 156,0 | . 01752 | 12,I | . 44475 | 143,9 | . 55525 |
| .287 | . 46383 | I 55,5 | .01765 | I2, 1 | . 44618 | 143,3 | . 55382 |
| . 288 | . 46538 | 154,9 | .01777 | 12,2 | . 4476 I | 142,8 | . 55239 |
| .289 | . 46693 | 154,4 | .01789 | 12,2 | . 44904 | 142,2 | . 55096 |
| 0.290 | 9.46847 | 153,9 | 0.01801 | 12,3 | 9.45046 | 141,7 | 0.54954 |
| . 291 | . 47001 | ${ }^{1} 53,4$ | .018ı3 | 12,3 | . 45187 | 141, 1 | -54813 |
| . 292 | . 47154 | I 52,9 | .01826 | 12,3 | . 45328 | 140,6 | . 54672 |
| . 293 | . 47306 | 152,4 | .01838 | 12,4 | . 45468 | 140, 1 | - 54532 |
| . 294 | . 47459 | 1 52,0 | . 01851 | 12,4 | . 45608 | 1 39,5 | . 54392 |
| 0.295 | 9.47610 | 151,5 | 0.01863 | 12,5 | 9.45747 | I 39,0 | 0.54253 |
| . 296 | . 47762 | 151,0 | . 01875 | 12,5 | . 45886 | 138,5 | . 54114 |
| . 297 | . 47912 | I 50,5 | . 01888 | 12,5 | . 46024 | I 38,0 | . 53976 |
| . 298 | . 48063 | I50,0 | . 01900 | 12,6 | . 46162 | ${ }^{1} 37,5$ | - 53838 |
| . 299 | . 48212 | 149,6 | . 01913 | 12,6 | .46299 | 136,9 | . 53701 |
| 0.300 | 9.48362 | 149, I | 0.01926 | 12,7 | 9.46436 | 136,4 | 0.53564 |
| u | $l o g t a n g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.300 | 9.48352 | I49, I | 0.01926 | 12,7 | 9.46436 | 136,4 | 0.53564 |
| . 301 | . 48510 | 148,6 | . 01938 | 12,7 | . 46572 | 135,9 | . 53428 |
| . 302 | . 48559 | 148,2 | . 01951 | 12,7 | . 46708 | 135,4 | . 53292 |
| . 303 | . 48807 | 147,7 | . 01964 | 12,8 | . 46843 | 134,9 | . 53157 |
| . 304 | . 48954 | 147,2 | . 01977 | 12,8 | . 45978 | 134,4 | . 53022 |
| 0.305 | 9.49101 | I46,8 | 0.01989 | 12,8 | 9.47112 | 133,9 | 0.52888 |
| . 305 | . 49248 | 146,3 | . 02002 | 12,9 | . 47245 | 133,4 | . 52755 |
| . 307 | . 49394 | 145,9 | . 02015 | 12,9 | . 47379 | I 33, 0 | . 5262 I |
| . 308 | . 49540 | 145,4 | . 02028 | 13,0 | .4751 1 | 132,5 | . 52489 |
| . 309 | . 49685 | 145,0 | . 0204 I | 13,0 | . 47644 | 132,0 | . 52356 |
| 0.310 | 9.49830 | 144,6 | 0.02054 | 13,0 | 9.47775 | 131,5 | 0.52225 |
| . 311 | . 49974 | I.44, I | . 02067 | I3, I | . 47907 | 131,0 | . 52093 |
| . 312 | . 50118 | 143,7 | . 02080 | I3, I | . 48037 | I 30,6 | . 51963 |
| . 313 | . 5025 I | 143,3 | .02094 | 13,2 | .48168 | I30, I | . 51832 |
| . 314 | . 50404 | 142,8 | .02107 | 13,2 | . 48298 | 129,6 | . 51702 |
| 0.315 | 9.50547 | 142,4 | 0.02120 | 13,2 | 9.48427 | 129,2 | 0.51573 |
| . 316 | . 50589 | 142,0 | .02133 | 13,3 | . 48556 | 128,7 | . 51444 |
| -317 | . 50831 | 141,6 | . 02145 | I3,3 | . 48684 | 128,2 | . 51316 |
| . 318 | . 50972 | I4I, I | .02160 | I 3,4 | .48812 | 127,8 | . 51188 |
| . 319 | . 51113 | 140,7 | .02173 | 13,4 | . 48940 | 127,3 | . 51060 |
| 0.320 | 9.51254 | 140,3 | 0.02187 | 13,4 | 9.49067 | 126,9 | 0.50933 |
| . 321 | . 51394 | 139,9 | . 02200 | 13,5 | . 49194 | 126,4 | . 50806 |
| . 322 | . $5153+$ | 1 39,5 | .02214 | I 3,5 | . 49320 | 126,0 | . 50680 |
| . 323 | . 51673 | 139, I | . 02227 | 13,6 | . 49446 | 125,5 | . 50554 |
| . 324 | . 51812 | 138,7 | .0224I | 13,6 | . 4957 I | 125, I | . 50429 |
| 0.325 | 9.51950 | 138,3 | 0.02254 | I3,6 | 9.49696 | 124,7 | 0.50304 |
| . 325 | . 52088 | 137,9 | . 02268 | 13,7 | . 49820 | 124,2 | . 50180 |
| . 327 | . 52225 | 137,5 | . 02282 | I3,7 | . 49944 | 123,8 | . 50056 |
| . 328 | . 52363 | 137, I | . 02295 | I 3,8 | . 50068 | 123,4 | . 49932 |
| . 329 | . 52500 | 136,7 | . 02309 | I3,8 | . 50191 | 122,9 | . 49809 |
| 0.330 | 9.52637 | 136,3 | 0.02323 | 13,8 | 9.50314 | 122,5 | 0.49686 |
| . 331 | . 52773 | 136,0 | . 02337 | I3,9 | . 50436 | 122, I | . 49564 |
| . 332 | . 52909 | 135,6 | .0235I | 13,9 | . 50558 | 121,7 | . 49442 |
| . 333 | . 53044 | 135,2 | . 02365 | I 4,0 | . 50679 | 121,3 | . 4932 I |
| . 334 | . 53179 | 134,8 | . 02379 | 14,0 | . 50800 | 120,8 | . 49200 |
| 0.335 | 9.53314 | 134,5 | 0.02393 | 14,0 | 9.50921 | 120,4 | 0.49079 |
| . 336 | . 53448 | . I34, I | . 02407 | 14, I | .5104I | 120,0 | . 48959 |
| . 337 | . 53582 | 1 33,7 | .0242I | 14, I | . 51161 | I 19,6 | . 48839 |
| . 338 | . 53715 | 133,3 | . 02435 | 14, 1 | . 5128 I | I 19,2 | . 48719 |
| . 339 | . 53849 | 133,0 | . 02449 | 14,2 | . 51400 | I 18,8 | . 48600 |
| 0.340 | 9.53981 | 132,6 | 0.02463 | 14,2 | 9.51518 | I 18,4 | 0.48482 |
| . 341 | .54114 | I 32,3 | . 02478 | 14,3 | . 51636 | I 18,0 | . 48364 |
| . 342 | . 54246 | 131,9 | . 02492 | 14,3 | . 51754 | 1 17,6 | . 48246 |
| - 343 | . 54378 | 131,5 | . 02506 | 14,3 | . 51872 | II7,2 | . 48128 |
| - 344 | . 54509 | 131,2 | . 02520 | 14,4 | . 51989 | I 16,8 | . 4801 I |
| 0.345 | 9.54640 | I30,8 | 0.02535 | 14,4 | 9.52105 | I 16,4 | 0.47895 |
| . 346 | . 5477 I | 130,5 | .02549 | 14,5 | . 5222 I | 116,0 | . 47779 |
| - 347 | . 54901 | I 30, 1 | . 02564 | 14,5 | - 52337 | I 1 5,7 | . 47653 |
| . 348 | . 5503 I | 129,8 | . 02578 | 14,5 | . 52453 | II 5,3 | . 47547 |
| . 349 | . 55161 | 129,5 | . 02593 | 14,6 | . 52568 | 114,9 | . 47432 |
| 0.350 | 9.55290 | 129,1 | 0.02607 | 14,6 | 9.52682 | I 14,5 | 0.47318 |
| $u$ | $\log \tan g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F^{\prime}{ }^{\prime}$ | $\log \csc g d u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.350 | 9.55290 | 129, I | 0.02607 | 14,6 | 9.52682 | I I 4,5 | 0.47318 |
| .351 | . 55419 | 128,8 | . 02622 | 14,6 | . 52797 | II4, 1 | . 47203 |
| . 352 | . 55547 | 128,4 | . 02637 | 14,7 | . 529 I I | 113,7 | . 47089 |
| - 353 | . 55676 | 128, I | . 02651 | 14,7 | . 53024 | I I 3,4 | . 46976 |
| - 354 | . 55804 | 127,8 | . 02666 | 14,8 | . 53137 | II3,0 | . 46863 |
| 0.355 | 9.55931 | 127,4 | 0.02681 | 14,8 | 9.53250 | I I 2,6 | 0.46750 |
| - 356 | . 56059 | 127, 1 | . 02696 | 14,8 | . 53363 | I 12,3 | . 46637 |
| . 357 | . 56185 | 126,8 | .027II | 14,9 | . 53475 | I I I, 9 | . 46525 |
| . 358 | . 56312 | 126,5 | .02726 | 14,9 | . 53586 | III,5 | . 46414 |
| . 359 | . 56438 | 126, 1 | . 02740 | 15,0 | . 53698 | III,2 | . 46302 |
| 0.360 | 9.56564 | 125,8 | 0.02755 | 15,0 | 9.53809 | I 10,8 | 0.46191 |
| . 361 | . 56690 | 125,5 | . 02770 | 15,0 | . 53919 | I10,5 | . 46081 |
| . 362 | . 568 I 5 | 125,2 | . 02786 | 15, I | . 54030 | I IO, I | . 45970 |
| . 363 | . 56940 | 124,8 | .02801 | 15, I | . 54140 | 109,7 | . 45860 |
| . 364 | . 57065 | 124,5 | .02816 | 15, 1 | . 54249 | 109,4 | . 45751 |
| 0.365 | 9.57189 | 124,2 | 0.02831 | 15,2 | 9.54358 | 109,0 | 0.45642 |
| . 366 | . 57313 | 123,9 | . 02846 | 15,2 | . 54467 | 108,7 | . 45533 |
| . 367 | . 57437 | 123,6 | .0286I | 15,3 | . 54576 | 108,3 | . 45424 |
| . 368 | . 57561 | 123,3 | .02877 | 15,3 | . 54684 | 108,0 | . 45316 |
| . 369 | . 57684 | 123,0 | . 02892 | 15,3 | . 54792 | 107,7 | . 45208 |
| 0.370 | 9.57807 | 122,7 | 0.02907 | I 5,4 | 9.54899 | 107,3 | 0.45 IOI |
| . 371 | . 57929 | 122,4 | . 02923 | I 5,4 | . 55006 | 107,0 | . 44994 |
| . 372 | -58051 | 122,I | . 02938 | I5,4 | . 55113 | 106,6 | . 44887 |
| . 373 | . 58173 | 121,8 | . 02954 | 15,5 | . 55220 | 106,3 | . 44780 |
| . 374 | . 58295 | 121,5 | . 02969 | 15,5 | . 55326 | 106,0 | . 44674 |
| 0.375 | 9.58416 | 121,2 | 0.02985 | I 5,6 | 9.55432 | 105,6 | 0.44568 |
| . 376 | . 58537 | 120,9 | . 03000 | I 5,6 | . 55537 | 105,3 | . 44463 |
| . 377 | . 58658 | I20,6 | . 03016 | 15,6 | . 55642 | 105,0 | . 44358 |
| . 378 | . 58779 | 120,3 | .03031 | 15,7 | . 55747 | 104,6 | . 44253 |
| . 379 | . 58899 | 120,0 | . 03047 | I 5,7 | . 55852 | 104,3 | . 44148 |
| 0.380 | 9.59019 | 119,7 | 0.03063 | I 5,8 | 9.55956 | 104,0 | 0.44044 |
| . 381 | . 59138 | I 19,5 | . 03079 | I 5,8 | . 56059 | 103,7 | . 4394 I |
| . 382 | . 59257 | 119,2 | . 03095 | I 5,8 | . 56163 | 103,3 | . 43837 |
| . 383 | . 59377 | 1 18,9 | .03110 | 15,9 | . 56266 | 103,0 | . 43734 |
| . 384 | . 59495 | I 18,6 | .03125 | 15,9 | . 56369 | 102,7 | . 4363 I |
| 0.385 | 9.59614 | I 18,3 | 0.03142 | I5,9 | 9.56472 | 102,4 | 0.43528 |
| . 386 | . 59732 | I 18,0 | .03158 | 16,0 | . 56574 | 102, 1 | . 43426 |
| . 387 | . 59850 | I I 7,8 | .03174 | 16,0 | . 56676 | IOI,8 | . 43324 |
| - 388 | . 59967 | 117,5 | . 03190 | 16, I | . 56777 | IOI,4 | . 43223 |
| -389 | . 60085 | 1 17,2 | . 03206 | 16, I | . 56879 | IOI, I | .43121 |
| 0.390 | 9.60202 | I 16,9 | 0.03222 | 16, 1 | 9.56980 | 100,8 | 0.43020 |
| . 391 | . 60319 | 116,7 | . 03238 | 16,2 | . 57080 | 100,5 | . 42920 |
| - 392 | . 60435 | 116,4 | . 03255 | 16,2 | . 57181 | 100,2 | .42819 |
| . 393 | . 60551 | I I6, I | .0327I | 16,2 | . 5728 I | 99,9 | . 42719 |
| . 394 | . 60668 | I 15,9 | .03287 | 16,3 | . 57380 | 99,6 | . 42620 |
| 0.395 | 9.60783 | I I 5,6 | 0.03303 | 16,3 | 9.57480 | 99,3 | 0.42520 |
| . 396 | . 60899 | II 5,3 | . 03320 | 16,4 | . 57579 | 99,0 | . 42421 |
| . 397 | .61014 | II 5, I | . 03336 | 16,4 | . 57678 | 98,7 | . 42322 |
| . 398 | .61129 .61244 | II 4,8 I 4,6 | . 03353 | 16,4 | . 57776 | 98,4 | . 42224 |
| - 399 | . 61244 | I 14,6 | . 03369 | 16,5 | . 57875 | 98, I | . 42125 |
| 0.400 | 9.61358 | I 14,3 | 0.03385 | 16,5 | 9.57973 | 97,8 | 0.42027 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.400 | 9.61358 | II 4,3 | 0.03385 | 16,5 | 9.57973 | 97,8 | 0.42027 |
| . 401 | .61472 | I 14, 0 | . 03402 | 16,5 | . 58070 | 97,5 | . 41930 |
| . 402 | . 61586 | I I3,8 | . 03419 | - 16,6 | . 58168 | 97,2 | . 41832 |
| . 403 | .6I700 | I 13,5 | . 03435 | 16,6 | . 58265 | 96,9 | .41735 |
| . 404 | .618I3 | 113,3 | . 03452 | 16,6 | . 5836 I | 96,6 | . 41639 |
| 0.405 | 9.61926 | II3,0 | 0.03468 | 16,7 | 9.58458 | 96,3 | 0.41542 |
| . 406 | . 62039 | I I2,8 | . 03485 | 16,7 | . 58554 | 96, 1 | . 41446 |
| . 407 | . 62152 | 112,5 | . 03502 | 16,8 | . 58650 | 95,8 | . 41350 |
| . 408 | . 62264 | I 12,3 | . 03519 | 16,8 | . 58746 | 95,5 | .41254 |
| . 409 | . 62376 | I 12,0 | . 03535 | 16,8 | . 58841 | 95,2 | . 41159 |
| 0.410 | 9.62488 | III, 8 | 0.03552 | 16,9 | 9.58936 | 94,9 | 0.41064 |
| . 411 | . 62600 | III, 6 | . 03569 | 16,9 | . 59031 | 94,6 | . 40969 |
| . 412 | . 62711 | III, 3 | . 03586 | 16,9 | . 59125 | 94,4 | . 40875 |
| .4I3 | . 62823 | I I I, I | . 03603 | 17,0 | - 59220 | 94, I | . 40780 |
| . 414 | . 62934 | IIIO,8 | . 03620 | 17,0 | . 59314 | 93,8 | . 40686 |
| 0.415 | 9.63044 | I 10,6 | 0.03637 | 17,I | 9.59407 | 93,5 | 0.40593 |
| . 416 | . 63155 | 110,4 | . 03654 | 17,I | -59501 | 93,3 | . 40499 |
| .417 | . 63265 | I 10, I | . 03671 | 17,1 | - 59594 | 93,0 | . 40406 |
| . 418 | . 63375 | 109,9 | . 03688 | 17,2 | . 59587 | 92,7 | . 40313 |
| . 419 | . 63485 | 109,6 | . 03706 | 17,2 | - 59779 | 92,4 | . 4022 I |
| 0.420 | 9.63594 | 109,4 | 0.03723 | 17,2 | 9.59871 | 92,2 | 0.40129 |
| . 42 I | . 63704 | 109,2 | . 03740 | 17,3 | . 59963 | 91,9 | . 40037 |
| . 422 | . 63813 | 109,0 | . 03757 | 17,3 | . 60055 | 91,6 | - 39945 |
| . 423 | . 63922 | 108,7 | . 03775 | 17,3 | . 60147 | 9I,4 | - 39853 |
| . 424 | . 64030 | 108,5 | . 03792 | 17,4 | . 60238 | 91, I | . 39762 |
| 0.425 | 9.64139 | 108,3 | 0.03810 | 17,4 | 9.60329 | 90,8 | 0.39671 |
| . 426 | . 64247 | 108,0 | . 03827 | 17,5 | . 60420 | 90,6 | . 39580 |
| . 427 | . 64355 | 107,8 | . 03844 | 17,5 | . 60510 | 90,3 | . 39490 |
| . 428 | . 64462 | 107,6 | . 03862 | 17,5 | . 60600 | 90, I | . 39400 |
| .429 | . 64570 | 107,4 | . 03880 | 17,6 | . 60690 | 89,8 | . 39310 |
| 0.430 | 9.64677 | 107,1 | 0.03897 | 17,6 | 9.60780 | 80,6 | 0.39220 |
| . 431 | . 64784 | 106,9 | . 03915 | 17,6 | . 60869 | 89,3 | .3913I |
| . 432 | . 64891 | 105,7 | . 03932 | 17,7 | . 60959 | 89,0 | . 39041 |
| . 433 | . 64997 | 106,5 | . 03950 | 17,7 | .61047 | 88,8 | . 38953 |
| . 434 | .65104 | 106,3 | . 03968 | 17,7 | . 61136 | 88,5 | . 38864 |
| 0.435 | 9.65210 | 106,0 | 0.03986 | 17,8 | 9.61224 | 88,3 | 0.38776 |
| . 436 | . 65316 | 105,8 | . 04003 | 17,8 | .613I3 | 88,0 | . 38687 |
| . 437 | . 65422 | 105,6 | . 04021 | 17,9 | .6I40I | 87,8 | . 38599 |
| . 438 | . 65527 | 105,4 | . 04039 | 17,9 | .6I488 | 87,5 | . 38512 |
| . 439 | . 65633 | 105,2 | . 04057 | 17,9 | .61576 | 87,3 | . 38424 |
| 0.440 | 9.65738 | 105,0 | 0.04075 | 18,0 | 9.61663 | 87,0 | 0. 38337 |
| . 441 | . 65843 | 104,8 | . 04093 | 18,0 | . 61750 | 86,8 | . 38250 |
| . 442 | . 65947 | 104,6 | .04III | 18,0 | . 61836 | 86,5 | .38164 |
| . 443 | . 66052 | 104,4 | .04129 | I8, I | . 61923 | 86,3 | . 38077 |
| . 444 | . 66156 | 104,2 | .04147 | 18, 1 | . 62009 | 86, I | -3799I |
| 0.445 | 9.66260 | 104,0 | 0.04165 | 18, 1 | 9.62095 | 85,8 | 0.37905 |
| .446 | . 66364 | 103,7 | .04183 | 18,2 | . 62180 | 85,6 | . 37820 |
| . 447 | . 66468 | 103,5 | . 04202 | 18,2 | . 62266 | 85,3 | . 37734 |
| . 448 | . 66571 | 103,3 | .04220 | 18,3 | . 62351 | 85,1 | . 37649 |
| . 449 | . 66674 | 103, I | . 04238 | 18,3 | . 62436 | 84,9 | . 37564 |
| 0.450 | 9.66777 | 102,9 | 0.04256 | 18,3 | 9.62521 | 84,6 | 0.37479 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \mathbf{\operatorname { c o s h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.450 | 9.66777 | 102,9 | 0.04256 | 18,3 | 9.6252 I | 84,6 | 0.37479 |
| . 451 | . 66880 | 102,7 | . 04275 | 18,4 | . 62605 | 84,4 | . 37395 |
| . 452 | . 66983 | 102,5 | . 04293 | 18,4 | . 62690 | 84,1 | . 37310 |
| . 453 | . 67085 | 102,3 | .04312 | 18,4 | . 62774 | 83,9 | . 37226 |
| . 454 | .67187 | 102,I | . 04330 | 18,5 | . 62857 | 83,7 | . 37143 |
| 0.455 | 9.67289 | IOI,9 | 0.04348 | 18,5 | 9.62941 | 83,4 | 0.37059 |
| . 456 | .67391 | 101,8 | . 04367 | 18,5 | . 63024 | 83,2 | . 36976 |
| . 457 | . 67493 | 101,6 | . 04385 | 18,6 | . 63107 | 83,0 | . 36893 |
| . 458 | . 67594 | IOI,4 | . 04404 | 18,6 | . 63190 | 82,8 | . 36810 |
| . 459 | . 67696 | 101,2 | . 04423 | 18,6 | . 63273 | 82,5 | . 36727 |
| 0.460 | 9.67797 | IOI, 0 | 0.04441 | 18,7 | 9.63355 | 82,3 | 0.36645 |
| . 461 | . 67898 | 100,8 | . 04460 | 18,7 | . 63438 | 82, 1 | . 36562 |
| . 462 | . 67998 | 100,6 | . 04479 | 18,7 | . 63519 | 8I,8 | . 3648 I |
| . 463 | . 68099 | 100,4 | . 04498 | 18,8 | .63601 | 8I,6 | . 36399 |
| . 464 | .68199 | 100,2 | .04516 | 18,8 | . 63683 | 8I,4 | . 36317 |
| 0.465 | 9.68299 | 100,0 | 0.04535 | 18,9 | 9.63764 | 81,2 | 0.36236 |
| . 466 | . 68399 | 99,8 | . 04554 | 18,9 | . 63845 | 81,0 | .36I55 |
| . 467 | . 68499 | 99,7 | . 04573 | 18,9 | . 63926 | 80,7 | . 36074 |
| . 468 | . 68599 | 99,5 | . 04592 | 19,0 | .64007 | 80,5 | . 35993 |
| . 469 | . 68698 | 99,3 | .046I I | 19,0 | . 64087 | 80,3 | . 35913 |
| 0.470 | 9.68797 | 99, I | 0.04630 | 19,0 | 9.64167 | 80,1 | 0. 35833 |
| . 471 | . 68896 | 98,9 | . 04649 | 19,1 | . 64247 | 79,9 | - 35753 |
| . 472 | . 68995 | 98,7 | .04668 | 19, I | .64327 | 79,6 | . 35673 |
| . 473 | . 69094 | 98,6 | .04687 | 19,I | . 64406 | 79,4 | - 35594 |
| . 474 | . 69192 | 98,4 | . 04706 | 19,2 | .64486 | 79,2 | . 35514 |
| 0.475 | 9.69290 | 98,2 | 0.04726 | 19,2 | 9.64565 | 79,0 | 0.35435. |
| . 476 | . 69388 | 98,0 | . 04745 | 19,2 | . 64644 | 78,8 | . 35356 |
| . 477 | . 69486 | 97,8 | . 04764 | 19,3 | . 64722 | 78,6 | . 35278 |
| . 478 | . 69584 | 97,7 | . 04783 | 19,3 | . 64801 | 78,4 | -35199 |
| . 479 | . 69682 | 97,5 | . 04803 | 19,3 | . 64879 | 78,2 | .35121 |
| 0.480 | 9.69779 | 97,3 | 0.04822 | 19,4 | 9.64957 | 77,9 | 0.35043 |
| .481 | . 69876 | 97, I | . 04841 | 19,4 | . 65035 | 77,7 | . 34965 |
| . 482 | . 69973 | 97,0 | .0486I | 19,4 | .65113 | 77,5 | - 34887 |
| . 483 | . 70070 | 96,8 | . 04880 | 19,5 | . 65190 | 77,3 | -34810 |
| . 484 | . 70167 | 96,6 | . 04900 | 19,5 | . 65267 | 77, 1 | - 34733 |
| 0.485 | 9.70264 | 65,5 | 0.04919 | 19,6 | 9.65344 | 76,9 | 0.34656 |
| . 486 | . 70360 | 96,3 | . 04939 | 19,6 | . 6542 I | 76,7 | . 34579 |
| . 487 | . 70456 | 96, | . 04959 | 19,6 | . 65498 | 76,5 | . 34502 |
| . 488 | . 70552 | 95,9 | . 04978 | 19,7 | . 65574 | 76,3 | - 34426 |
| . 489 | . 70648 | 95,8 | . 04998 | 19,7 | . 65650 | 76, 1 | - 34350 |
| 0.490 | 9.70744 | 95,6 | 0.05018 | 19,7 | 9.65726 | 75,9 | 0.34274 |
| .49I | . 70839 | 95,4 | . 05037 | 19,8 | . 65802 | 75,7 | . 34198 |
| . 492 | . 70935 | 95,3 | . 05057 | 19,8 | . 65878 | 75,5 | . 34122 |
| . 493 | . 71030 | 95, I | . 05077 | 19,8 | . 65953 | 75,3 | - 34047 |
| . 494 | . 71125 | 95,0 | . 05097 | 19,9 | . 66028 | 75, I | - 33972 |
| 0.495 | 9.71220 | 94,8 | 0.05117 | 19,9 | 9.66103 | 74,9 | 0.33897 |
| . 496 | .71315 | 94,6 | .05137 | 19,9 | . 66178 | 74,7 | . 33822 |
| . 497 | . 71409 | 94,5 | .05156 | 20,0 | . 66253 | 74,5 | . 33747 |
| . 498 | . 71503 | 94,3 | .05176 | 20,0 | . 66327 | 74,3 | - 33673 |
| . 499 | . 71598 | 94, I | .05196 | 20,0 | .6640I | 74, I | - 33599 |
| 0.500 | 9.71692 | 94,0 | 0.05217 | 20,1 | 9.66475 | 73,9 | 0.33525 |
| u | $l o g t a n g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { c o s h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.500 | 9.71692 | 94,0 | 0.05217 | 20,1 | 9.66475 | 73,9 | 0.33525 |
| . 501 | .71786 | 93,8 | . 05237 | 20, I | . 66549 | 73,7 | . 3345 I |
| . 502 | . 71879 | 93,7 | . 05257 | 20, I | . 66623 | 73,5 | . 33377 |
| . 503 | . 71973 | 93,5 | . 05277 | 20,2 | . 66696 | 73,3 | . 33304 |
| . 504 | . 72066 | 93,3 | . 05297 | 20,2 | . 66769 | 73, I | . 3323 I |
| 0.505 | 9.72160 | 93,2 | 0.05317 | 20,2 | 9.66842 | 72,9 | 0.33158 |
| . 506 | . 72253 | 93,0 | . 05338 | 20,3 | . 66915 | 72,8 | . 33085 |
| . 507 | . 72346 | 92,9 | . 05358 | 20,3 | . 66988 | 72,6 | . 33012 |
| . 508 | . 72438 | 92,7 | . 05378 | 20,3 | . 67060 | 72,4 | - 32940 |
| . 509 | . 72531 | 92,6 | . 05399 | 20,4 | . 67133 | 72,2 | . 32867 |
| 0.510 | 9.72624 | 92,4 | 0.05419 | 20,4 | 9.67205 | 72,0 | 0.32795 |
| .511 | . 72716 | 92,3 | . 05439 | 20,4 | . 67277 | 71,8 | . 32723 |
| . 512 | . 72808 | 92, | . 05460 | 20,5 | . 67348 | 71,6 | . 32652 |
| . 513 | . 72900 | 92,0 | . 05480 | 20,5 | . 67420 | 71,5 | . 32580 |
| . 514 | . 72992 | 91,8 | .05501 | 20,5 | .6749I | 71,3 | . 32509 |
| 0.515 | 9.73084 | 91,7 | 0.0552 I | 20,6 | 9.67562 | 71,1 | 0.32438 |
| . 516 | .73175 | 91,5 | . 05542 | 20,6 | . 67633 | 70,9 | . 32367 |
| . 517 | . 73267 | 91,4 | . 05563 | 20,6 | . 67704 | 70,7 | . 32296 |
| . 518 | . 73358 | 91,2 | . 05583 | 20,7 | . 67775 | 70,5 | - 32225 |
| . 519 | . 73449 | 91,I | . 05604 | 20,7 | . 67845 | 70,3 | . 32155 |
| 0.520 | 9.73540 | 90,9 | 0.05625 | 20,7 | 9.67916 | 70,2 | 0.32084 |
| . 52 I | . 73631 | 90,8 | .05645 | 20,8 | . 67986 | 70,0 | . 32014 |
| . 522 | . 73722 | 90,6 | . 05666 | 20,8 | . 68056 | 69,8 | . 31944 |
| . 523 | . 73812 | 90,5 | . 05687 | 20,8 | .68125 | 69,6 | . 31875 |
| . 524 | . 73903 | 90,3 | . 05708 | 20,9 | .68I95 | 69,5 | . 31805 |
| 0.525 | 9.73993 | 90,2 | 0.05729 | 20,9 | 9.68264 | 69,3 | 0.31736 |
| . 526 | . 74083 | 90,0 | . 05750 | 20,9 | . 68333 | 69, I | . 31667 |
| . 527 | . 74173 | 89,9 | . 05771 | $2 \mathrm{I}, 0$ | . 68402 | 68,9 | - 31598 |
| . 528 | . 74263 | 89,8 | . 05792 | 21,0 | . 6847 I | 68,7 | -3I529 |
| . 529 | . 74353 | 89,6 | .058I3 | 21,0 | . 68540 | 68,6 | . 31460 |
| 0.530 | 9.74442 | 89,5 | 0.05834 | 2I, I | 9.68608 | 68,4 | 0.31392 |
| . 53 I | . 74532 | 89,3 | . 05855 | 2I, I | . 68677 | 68,2 | . 31323 |
| . 532 | . 7462 I | 89,2 | . 05876 | 2I, I | . 68745 | 68,0 | . 31255 |
| . 533 | . 74710 | 89,I | . 05897 | 2I,2 | .688I3 | 67,9 | . 31187 |
| . 534 | . 74799 | 88,9 | .05918 | 21,2 | . 68880 | 67,7 | .31120 |
| 0.535 | 9.74888 | 88,8 | 0.05940 | 2I, 2 | 9.68948 | 67,5 | 0.31052 |
| . 536 | . 74976 | 88,6 | .0596I | 2I,3 | . 69016 | 67,4 | . 30984 |
| . 537 | . 75065 | 88,5 | .05982 | 2I,3 | . 69083 | 67,2 | -30917 |
| . 538 | . 75153 | 88,4 | . 06004 | 21,3 | . 69150 | 67,0 | . 30850 |
| . 539 | . 75242 | 88,2 | . 06025 | 2I,4 | . 69217 | 66,9 | . 30783 |
| 0.540 | 9.75330 | 88,1 | 0.06046 | 2I,4 | 9.69284 | 66,7 | 0.30716 |
| . 541 | . 75418 | 88,0 | . 06068 | 2I,4 | . 69350 | 66,5 | . 30650 |
| . 542 | . 75506 | 87,8 | .06089 | 2I,5 | . 69417 | 66,3 | - 30583 |
| . 543 | . 75594 | 87,7 | .06III | $2 \mathrm{I}, 5$ | . 69483 | 66,2 | - 30517 |
| . 544 | .7568I | 87,6 | .06132 | 21,5 | . 69549 | 66,0 | -3045I |
|  | 9.75769 | 87,4 | 0.06154 | 21,6 | 9.69615 | 65,9 | 0.30385 |
| . 546 | . 75856 | 87,3 | .06I75 | 21,6 | . 6968 I | 65,7 | . 30319 |
| . 547 | . 75943 | 87,2 | .06197 | 21,6 | . 69746 | 65,5 | . 30254 |
| . 548 | . 76030 | 87,0 | .06219 | 21,7 | . 69812 | 65,4 | - 30188 |
| . 549 | .76117 | 86,9 | . 06240 | 21,7 | . 69877 | 65,2 | . 30123 |
| 0.550 | 9.76204 | 86,8 | 0.06262 | 21,7 | 9.69942 | 65,0 | 0.30058 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.550 | 9.76204 | 86,8 | 0.06262 | 21,7 | 9.69942 | 65,0 | 0.30058 |
| . 551 | .76291 | 86,6 | .06284 | 21,8 | . 70007 | 64,9 | . 29993 |
| . 552 | . 76377 | 86,5 | . 06306 | 21,8 | . 70072 | 64,7 | . 29928 |
| . 553 | . 76464 | 86,4 | . 06327 | 21,8 | . 70137 | 64,5 | . 29863 |
| . 554 | . 76550 | 86,3 | . 06349 | 21,9 | . 70201 | 64,4 | . 29799 |
| 0.555 | 9.76636 | 86,I | 0.06371 | 21,9 | 9.70265 | 64,2 | 0.29735 |
| . 556 | . 76722 | 86,0 | . 06393 | 21,9 | . 70329 | 64,1 | . 29671 |
| . 557 | . 76808 | 85,9 | . 06415 | 22,0 | . 70393 | 63,9 | . 29607 |
| . 558 | . 76894 | 85,7 | . 06437 | 22,0 | . 70457 | 63,7 | . 29543 |
| . 559 | . 76980 | 85,6 | . 06459 | 22,0 | . 7052 I | 63,6 | . 29479 |
| 0.560 | 9.77065 | 85,5 | 0.0648 I | 22, I | 9.70584 | 63,4 | 0.29416 |
| . 561 | . 7715 I | 85,4 | . 06503 | 22, I | . 70648 | 63,3 | . 29352 |
| . 562 | . 77236 | 85,2 | . 06525 | 22, 1 | . 70711 | 63,1 | . 29289 |
| . 563 | . 7732 I | 85,1 | . 06547 | 22,2 | . 70774 | 63,0 | . 29226 |
| . 564 | . 77406 | 85,0 | . 06570 | 22,2 | . 70837 | 62,8 | . 29163 |
| 0.565 | 9.77491 | 84,9 | 0.06592 | 22,2 | 9.70900 | 62,7 | . 29100 |
| . 566 | . 77576 | 84,8 | .06614 | 22,3 | . 70962 | 62,5 | . 29038 |
| . 567 | . 7766 I | 84,6 | . 06636 | 22,3 | . 71025 | 62,3 | . 28975 |
| . 568 | . 77745 | 84,5 | . 06659 | 22,3 | . 71087 | 62,2 | .28913 |
| . 569 | .77830 | 84,4 | .0668I | 22,3 | .71149 | 62,0 | .2885I |
| 0.570 | 9.77914 | 84,3 | 0.06703 | 22,4 | 9.71211 | 6I,9 | 0. 28789 |
| -571 | . 77998 | 84,2 | . 06725 | 22,4 | . 71273 | 61,7 | -. 28727 |
| . 572 | . 78083 | 84,0 | . 06748 | 22,4 | . 71334 | 6i,6 | . 28666 |
| . 573 | .78167 | 83,9 | . 06771 | 22,5 | . 71396 | 6I,4 | . 28604 |
| . 574 | . 78250 | 83,8 | . 06793 | 22,5 | . 71457 | 6I,3 | . 28543 |
| 0.575 | 9.78334 | 83,7 | 0.06816 | 22,5 | 9.71519 | 6I, 1 | 0.2848I |
| . 576 | . 78418 | 83,6 | . 06838 | 22,6 | . 71580 | 6I,0 | . 28.420 |
| . 577 | . 78501 | 83,4 | .0686I | 22,6 | . 71641 | 60,8 | . 28359 |
| . 578 | . 78585 | 83,3 | . 06883 | 22,6 | . 71701 | 60,7 | . 28299 |
| . 579 | . 78668 | 83,2 | . 06906 | 22,7 | . 71762 | 60,5 | . 28238 |
| 0.580 | 9.78751 | 83, 1 | 0.06929 | 22,7 | 9.71822 | 60,4 | 0.28ı78 |
| . 58 I | . 78834 | 83,0 | .0695I | 22,7 | . 71883 | 60,2 | .28117 |
| . 582 | . 78917 | 82,9 | . 06974 | 22,8 | . 71943 | 60, 1 | . 28057 |
| . 583 | . 79000 | 82,7 | . 06997 | 22,8 | .72003 | 60,0 | . 27997 |
| . 584 | . 79082 | 82,6 | . 07020 | 22,8 | .72063 | 59,8 | . 27937 |
| 0.585 | 9.79165 | 82,5 | 0.07043 | 22,9 | 9.72123 | 59,7 | 0.27877 |
| . 586 | . 79247 | 82,4 | . 07065 | 22,9 | . 72182 | 59,5 | .27818 |
| . 587 | . 79330 | 82,3 | . 07088 | 22,9 | . 72242 | 59,4 | . 27758 |
| . 588 | . 79412 | 82,2 | . 07 III | 23,0 | . 72301 | 59,2 | . 27699 |
| . 589 | . 79494 | 82,I | .07134 | 23,0 | .72360 | 59, I | . 27640 |
| 0.590 | 9.79576 | 82,0 | 0.07157 | 23,0 | 9.72419 | 58,9 | 0.2758 I |
| . 591 | . 79658 | 8ı,8 | . 07180 | 23,0 | . 72478 | 58,8 | . 27522 |
| . 592 | . 79740 | 81,7 | . 07203 | 23, I | . 72537 | 58,7 | . 27463 |
| . 593 | . 79822 | 8ı,6 | . 07226 | 23, I | . 72595 | 58,5 | . 27405 |
| . 594 | . 79903 | 8I,5 | . 07249 | 23, I | . 72654 | 58,4 | . 27346 |
| 0.595 | 9.79985 | 8r,4 | 0.07273 | 23,2 | 9.72712 | 58,2 | 0.27288 |
| . 596 | . 80066 | 81,3 | . 07296 | 23,2 | . 72770 | 58, | . 27230 |
| . 597 | . 80147 | 8I,2 | . 07319 | 23,2 | . 72828 | 58,0 | . 27172 |
| . 598 | . 80228 | 8I, I | . 07342 | 23,3 | . 72886 | 57,8 | . 27114 |
| . 599 | .80309 | 8I,0 | . 07366 | 23,3 | . 72944 | 57,7 | . 27056 |
| 0.600 | 9.80390 | 80,9 | 0.07389 | 23,3 | 9.73001 | 57,5 | 0.25999 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.600 | 9.80390 | 80,9 | 0.07389 | 23,3 | 9.73001 | 57,5 | 0.26999 |
| . 601 | . 8047 I | 80,8 | .07412 | 23,4 | . 73059 | 57,4 | . 26941 |
| . 602 | . 80552 | 80,7 | . 07436 | 23,4 | .73116 | 57,3 | . 26884 |
| . 603 | . 80632 | 80,5 | . 07459 | 23,4 | . 73173 | 57, 1 | . 26827 |
| . 604 | . 80713 | 80,4 | . 07482 | 23,4 | .7323I | 57,0 | . 26769 |
| 0.605 | 9.80793 | 80,3 | 0.07506 | 23,5 | 9.73287 | 56,9 | 0.26713 |
| . 606 | . 80874 | 80,2 | . 07529 | 23,5 | . 73344 | 56,7 | . 26656 |
| . 607 | . 80954 | 80,1 | . 07553 | 23,5 | . 73401 | 56,6 | . 26599 |
| . 608 | .81034 | 80,0 | . 07576 | 23,6 | . 73457 | 56,5 | . 26543 |
| . 609 | .8III4 | 79,9 | . 07600 | 23,6 | .73514 | 56,3 | . 26486 |
| 0.610 | 9.81194 | 79,8 | 0.07624 | 23,6 | 9.73570 | 56,2 | 0.26430 |
| .6II | .81273 | 79,7 | . 07647 | 23,7 | . 73626 | 56,0 | . 26374 |
| .612 | .81353 | 79,6 | .07671 | 23,7 | . 73682 | 55,9 | . 26318 |
| .613 | .81433 | 79,5 | . 07695 | 23,7 | . 73738 | 55,8 | . 26262 |
| .6I4 | .81512 | 79,4 | . 07718 | 23,8 | . 73794 | 55,7 | . 26206 |
| 0.615 | 9.81591 | 79,3 | 0.07742 | 23,8 | 9.73849 | 55,5 | 0.26151 |
| . 616 | .81671 | 79,2 | . 07766 | 23,8 | . 73905 | 55,4 | . 26095 |
| . 617 | .81750 | 79, 1 | . 07790 | 23,8 | . 73960 | 55,3 | . 26040 |
| . 618 | . 81829 | 79,0 | .07814 | 23,9 | . 74015 | 55, I | . 25985 |
| . 619 | .81908 | 78,9 | . 07838 | 23,9 | . 74070 | 55,0 | . 25930 |
| 0.620 | 9.81987 | 78,8 | 0.07861 | 23,9 | 9.74125 | 54,9 | 0.25875 |
| . 621 | . 82065 | 78,7 | . 07885 | 24,0 | . 74180 | 54,7 | . 25820 |
| . 622 | .82I44 | 78,6 | . 07909 | 24,0 | . 74235 | 54,6 | . 25765 |
| . 623 | . 82223 | 78,5 | . 07933 | 24,0 | . 74289 | 54,5 | . 25711 |
| . 624 | . 82301 | 78,4 | . 07957 | 24,1 | . 74344 | 54,3 | . 25656 |
| 0.625 | 9.82380 | 78,3 | 0.07982 | 24,1 | 9.74398 | 54,2 | 0.25602 |
| . 626 | . 82458 | 78,2 | . 08006 | 24, I | . 74452 | 54, I | . 25548 |
| . 627 | . 82536 | 78,1 | . 08030 | 24, I | . 74506 | 54,0 | . 25494 |
| . 628 | .82614 | 78,0 | . 08054 | 24,2 | . 74560 | 53,8 | . 25440 |
| . 629 | . 82692 | 77,9 | .08078 | 24,2 | .74614 | 53,7 | . 25386 |
| 0.630 | 9.82770 | 77,8 | 0.08 IO 2 | 24,2 | 9.74667 | 53,6 | 0.25333 |
| . 631 | . 82848 | 77,7 | .08126 | 24,3 | . 74721 | 53,5 | . 25279 |
| . 632 | . 82925 | 77,6 | .08I51 | 24,3 | . 74774 | 53,3 | . 25226 |
| . 633 | .83003 | 77,5 | .08I75 | 24,3 | . 74828 | 53,2 | . 25172 |
| . 634 | . 83080 | 77,4 | . 08200 | 24,4 | . 7488 I | 53,1 | .25119 |
| 0.635 | 9.83158 | 77,3 | 0.08224 | 24,4 | 9.74934 | 53,0 | 0.25066 |
| . 636 | . 83235 | 77,3 | . 08248 | 24,4 | . 74987 | 52,8 | . 25013 |
| . 637 | . 83312 | 77,2 | . 08273 | 24,4 | . 75040 | 52,7 | . 24960 |
| . 638 | . 83389 | 77, 1 | . 08297 | 24,5 | . 75092 | 52,6 | . 24908 |
| . 639 | . 83466 | 77,0 | . 08322 | 24,5 | . 75145 | 52,5 | . 24855 |
| 0.640 | 9.83543 | 76,9 | 0.08346 | 24,5 | 9.75197 | 52,3 | 0.24803 |
| . 641 | . 83620 | 76,8 | .0837I | 24,6 | . 75249 | 52,2 | .24751 |
| . 642 | . 83697 | 76,7 | .08395 | 24,6 | . 75302 | 52, I | . 24698 |
| . 643 | . 83774 | 76,6 | . 08420 | 24,6 | . 75354 | 52,0 | . 24646 |
| . 644 | . 83850 | 76,5 | . 08445 | 24,7 | . 75406 | 51,9 | . 24594 |
| 0.645 | 9.83927 | 76,4 | 0.08469 | 24,7 | 9.75457 | 51,7 | 0.24543 |
| . 646 | . 84003 | 76,3 | . 08494 | 24,7 | . 75509 | 51,6 | . 24491 |
| . 647 | . 84079 | 76,2 | . 08519 | 24,7 | .7556I | 5I,5 | . 24439 |
| . 648 | .84155 | 76, | . 08543 | 24,8 | .75612 | 5I,4 | . 24388 |
| . 649 | . 84232 | 76, 1 | . 08568 | 24,8 | . 75663 | 51,3 | . 24337 |
| 0.650 | 9.84308 | 76,0 | 0.08593 | 24,8 | 9.75715 | 51,1 | 0.24285 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.650 | 9.84308 | 76,0 | 0.08593 | 24,8 | 9.75715 | 51, I | 0.24285 |
| . 651 | . 84383 | 75,9 | .086I8 | 24,9 | . 75766 | 51,0 | . 24234 |
| . 652 | . 84459 | 75,8 | . 08643 | 24,9 | .75817 | 50,9 | . 24183 |
| . 653 | . 84535 | 75,7 | . 08668 | 24,9 | . 75867 | 50,8 | . 24133 |
| . 654 | .846II | 75,6 | . 08693 | 24,9 | .75918 | 50,7 | . 24082 |
| 0.655 | 9.84686 | 75,5 | 0.08718 | 25,0 | 9.75969 | 50,6 | 0.24031 |
| . 656 | . 84762 | 75,4 | . 08742 | 25,0 | . 76019 | 50,4 | . 23981 |
| . 657 | . 84837 | 75,4 | . 08768 | 25,0 | . 76070 | 50,3 | . 23930 |
| . 658 | . 84912 | 75,3 | . 08793 | 25, I | . 76120 | 50,2 | . 23880 |
| . 659 | . 84988 | 75,2 | .088I8 | 25, I | .76170 | 50, I | .23830 |
| 0.660 | 9.85063 | 75, I | 0.08843 | 25, 1 | 9.76220 | 50,0 | 0.23780 |
| . 661 | . 85138 | 75,0 | . 08868 | 25, I | . 76270 | 49,9 | . 23730 |
| . 662 | . 85213 | 74,9 | . 08893 | 25,2 | . 76320 | 49,7 | . 23680 |
| . 663 | . 85288 | 74,8 | .08918 | 25,2 | . 76369 | 49,6 | . 2363 I |
| . 664 | . 85362 | 74,7 | . 08943 | 25,2 | . 76419 | 49,5 | . 2358 I |
| 0.665 | 9.85437 | 74,7 | 0.08969 | 25,3 | 9.76469 | 49,4 | 0.23531 |
| . 666 | .85512 | 74,6 | . 08994 | 25,3 | . 76518 | 49,3 | . 23482 |
| . 667 | . 85586 | 74,5 | . 09019 | 25,3 | . 76567 | 49,2 | . 23433 |
| . 668 | .8566I | 74,4 | . 09045 | 25,3 | . 76616 | 49, I | . 23384 |
| . 669 | . 85735 | 74,3 | . 09070 | 25,4 | . 76665 | 48,9 | . 23335 |
| 0.670 | 9.85809 | 74,2 | 0.09095 | 25,4 | 9.76714 | 48,8 | 0.23286 |
| . 671 | . 85884 | 74,2 | .09121 | 25,4 | . 76763 | 48,7 | . 23237 |
| . 672 | . 85958 | 74,1 | . 09146 | 25,5 | . 76812 | 48,6 | .23188 |
| . 673 | . 86032 | 74,0 | .09172 | 25,5 | . 76860 | 48,5 | . 23140 |
| . 674 | .86106 | 73,9 | . 09197 | 25,5 | . 76909 | 48,4 | . 23091 |
| 0.675 | 9.86180 | 73,8 | 0.09223 | 25,5 | 9.76957 | 48,3 | 0.23043 |
| . 676 | . 86253 | 73,7 | . 09248 | 25,6 | . 77005 | 48,2 | . 22995 |
| . 677 | . 86327 | 73,7 | . 09274 | 25,6 | . 77053 | 48, | . 22947 |
| . 678 | .86401 | 73,6 | . 09300 | 25,6 | .77101 | 47,9 | . 22899 |
| . 679 | . 86474 | 73,5 | . 09325 | 25,7 | . 77149 | 47,8 | . 22851 |
| 0.680 | 9.86548 | 73,4 | 0.09351 | 25,7 | 9.77197 | 47,7 | 0.22803 |
| .681 | . 86621 | 73,3 | . 09377 | 25,7 | . 77245 | 47,6 | . 22755 |
| . 682 | . 86694 | 73,3 | . 09402 | 25,7 | . 77292 | 47,5 | 22708 |
| . 683 | . 86768 | 73,2 | . 09428 | 25,8 | . 77340 | 47,4 | 22660 |
| . 684 | . 8684 J | 73,1 | . 09454 | 25,8 | . 77387 | 47,3 | . 226I3 |
| 0.685 | 9.86914 | 73,0 | 0.09480 | 25,8 | 9.77434 | 47,2 | 0.22566 |
| . 686 | . 86987 | 72,9 | . 09505 | 25,9 | . 7748 I | 47,1 | . 22519 |
| . 687 | . 87060 | 72,9 | .0953I | 25,9 | . 77528 | 47,0 | . 22472 |
| . 688 | . 87133 | 72,8 | . 09557 | 25,9 | . 77575 | 46,9 | . 22425 |
| . 689 | . 87205 | 72,7 | . 09583 | 25,9 | . 77622 | 46,8 | . 22378 |
| 0.690 | 9.87278 | 72,6 | 0.09609 | 26,0 | 9.77669 | 46,7 | 0.22331 |
| . 691 | .87351 | 72,5 | . 09635 | 26,0 | . 77715 | 46,6 | . 22285 |
| . 692 | . 87423 | 72,5 | . 0966 I | 26,0 | . 77762 | 46,4 | . 22238 |
| . 693 | . 87495 | 72,4 | . 09687 | 26, | . 77808 | 46,3 | . 22192 |
| . 694 | . 87568 | 72,3 | . 09713 | 26,1 | . 77855 | 46,2 | . 22145 |
| 0.695 | 9.87640 | 72,2 | 0.09739 | 26, I | 9.77901 | 46, 1 | 0.22099 |
| . 696 | . 87712 | 72,2 | . 09765 | 26, 1 | . 77947 | 46,0 | . 22053 |
| . 697 | . 87784 | 72,1 | . 09792 | 26,2 | . 77993 | 45,9 | . 22007 |
| . 698 | . 87856 | 72,0 | .09818 | 26,2 | . 78039 | 45,8 | . 21961 |
| . 699 | . 87928 | 71,9 | . 09844 | 26,2 | . 78084 | 45,7 | . 21916 |
| 0.700 | 9.88000 | 71,9 | 0.09870 | 26,2 | 9.78 I 30 | 45,6 | 0.21870 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{cscgd} u$ |

Smithsonian Tables

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.700 | 9.88000 | 71,9 | 0.09870 | 26,2 | 9.78130 | 45,6 | 0.21870 |
| . 701 | . 88072 | 71,8 | .0989' | 26,3 | .78176 | 45,5 | . 21824 |
| . 702 | . 88144 | 71,7 | . 09923 | 26,3 | . 78221 | 45,4 | .21779 |
| . 703 | . 88216 | 71,6 | . 09949 | 26,3 | . 78266 | 45,3 | . 21734 |
| . 704 | . 88287 | 71,6 | . 09975 | 26,4 | .78312 | 45,2 | . 21688 |
| 0.705 | 9.88359 | 71,5 | 0.10002 | 26,4 | 9.78357 | 45, I | 0.21643 |
| . 706 | . 88430 | 7I,4 | . 10028 | 26,4 | . 78402 | 45,0 | . 21598 |
| . 707 | . 88502 | 71,3 | . 10055 | 26,4 | . 78447 | 44,9 | . 21553 |
| . 708 | . 88573 | 71,3 | . 1008I | 26,5 | . 78492 | 44,8 | . 21508 |
| . 709 | . 88544 | 71,2 | . 10108 | 26,5 | . 78536 | 44,7 | . 21464 |
| 0.710 | 9.88715 | 71,1 | 0.10134 | 26,5 | 9.7858 I | 44,6 | 0.21419 |
| .7II | . 88786 | 71,0 | . 10161 | 26,5 | . 78626 | 44,5 | . 21374 |
| . 712 | . 88857 | 71,0 | . 10187 | 26,6 | . 78670 | 44,4 | . 21330 |
| . 713 | . 88928 | 70,9 | . 10214 | 26,6 | . 78714 | 44,3 | . 21286 |
| . 714 | . 88999 | 70,8 | . 10240 | 26,6 | . 78759 | 44,2 | . 21241 |
| 0.715 | 9.89070 | 70,8 | 0. 10267 | 26,7 | 9.78803 | 44, I | 0.21197 |
| . 716 | .8914I | 70,7 | . 10294 | 26,7 | . 78847 | 44,0 | .21153 |
| . 717 | . 8921 I | 70,6 | . 10320 | 26,7 | .78891 | 43,9 | . 21109 |
| . 718 | . 89282 | 70,5 | . 10347 | 26,7 | . 78935 | 43,8 | . 21065 |
| . 719 | . 89352 | 70,5 | . 10374 | 26,8 | . 78978 | 43,7 | . 21022 |
| 0.720 | 9.89423 | 70,4 | $0.104 Q 1$ | 26,8 | 9.79022 | 43,6 | 0.20978 |
| .721 | . 89493 | 70,3 | . 10427 | 26,8 | . 79066 | 43,5 | . 20934 |
| . 722 | . 89563 | 70,3 | . 10454 | 26,8 | . 79109 | 43,4 | . 20891 |
| . 723 | . 89634 | 70,2 | . 10481 | 26,9 | . 79153 | 43,3 | . 20847 |
| . 724 | . 89704 | 70, I | . 10508 | 26,9 | . 79196 | 43,2 | . 20804 |
| 0.725 | 9.89774 | 70,0 | 0. 10535 | 26,9 | 9.79239 | 43,1 | 0.20761 |
| . 726 | . 89844 | 70,0 | . 10562 | 27,0 | . 79282 | 43,0 | . 20718 |
| . 727 | . 89914 | 69,9 | . 10589 | 27,0 | . 79325 | 42,9 | . 20675 |
| . 728 | . 89984 | 69,8 | . 10616 | 27,0 | . 79368 | 42,8 | . 20632 |
| . 729 | . 90054 | 69,8 | . 10643 | 27,0 | .794II | 42,7 | . 20589 |
| 0.730 | 9.90123 | 69,7 | 0. 10670 | 27,1 | 9.79453 | 42,6 | 0.20547 |
| .731 | . 90193 | 69,6 | . 10697 | 27, I | . 79496 | 42,5 | . 20504 |
| . 732 | . 90263 | 69,6 | . 10724 | 27, I | . 79538 | 42,5 | . 20462 |
| . 733 | . 90332 | 69,5 | . 10751 | 27, I | .7958I | 42,4 | . 20419 |
| . 734 | . 90402 | 69,4 | . 10778 | 27,2 | . 79623 | 42,3 | . 20377 |
| 0.735 | 9.9047 I | 69,4 | 0. 10805 | 27,2 | 9.79665 | 42,2 | 0.20335 |
| . 736 | . 90540 | 69,3 | . 10833 | 27,2 | . 79708 | 42, I | . 20292 |
| . 737 | .90610 | 69,2 | . 10860 | 27,2 | . 79750 | 42,0 | . 20250 |
| . 738 | . 90679 | 69,2 | . 10887 | 27,3 | .79791 | 41,9 | . 20209 |
| . 739 | . 90748 | 69, I | . 10915 | 27,3 | . 79833 | 4I,8 | . 20167 |
| 0.740 | 9.90817 | 69,0 | 0.10942 | 27,3 | 9.79875 | 41,7 | 0.20125 |
| .74I | . 90886 | 69,0 | . 10969 | 27,3 | . 79917 | 41,6 | . 20083 |
| . 742 | . 90955 | 68,9 | . 10997 | 27,4 | . 79958 | 41,5 | . 20042 |
| . 743 | . 91024 | 68,8 | . 11024 | 27,4 | . 80000 | 41,4 | . 20000 |
| . 744 | . 91092 | 68,8 | . I 1051 | 27,4 | . 80041 | 41,3 | . 19959 |
| 0.745 | 9.91161 | 68,7 | 0.11079 | 27,5 | 9.80082 | 41,2 | 0.19918 |
| . 746 | .91230 | 68,6 | . 11106 | 27,5 | . 80124 | 41,2 | . 19876 |
| . 747 | .91298 | 68,6 | . III34 | 27,5 | . 80165 | 4I, I | . 19835 |
| . 748 | .91367 | 68,5 | . III6I | 27,5 | . 80206 | 41,0 | . 19794 |
| . 749 | .91436 | 68,4 | . 11189 | 27,6 | . 80247 | 40,9 | . 19753 |
| 0.750 | 9.91504 | 68,4 | 0.11216 | 27,6 | 9.80288 | 40,8 | 0.19712 |
| 4 | $\log \tan \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \operatorname{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.750 | 9.91504 | 68,4 | 0.11216 | 27,6 | 9.80288 | 40,8 | 0.19712 |
| . 751 | .91572 | 68,3 | . II244 | 27,6 | . 80328 | 40,7 | . 19672 |
| . 752 | .9164I | 68,2 | . I I272 | 27,6 | . 80369 | 40,6 | . 19631 |
| . 753 | .91709 | 68,2 | . I I299 | 27,7 | . 80410 | 40,5 | . 19590 |
| . 754 | .91777 | 68, 1 | . II327 | 27,7 | . 80450 | 40,4 | . 19550 |
| 0.755 | 9.91845 | 68,1 | O. II355 | 27,7 | 9.80490 | 40,3 | 0. 195IO |
| . 756 | .91913 | 68,0 | - IoI 382 | 27,7 | . 80531 | 40,3 | . 19469 |
| . 757 | .9198I | 67,9 | . II4IO | 27,8 | . 80571 | 40,2 | . 19429 |
| . 758 | . 92049 | 67,9 | . II438 | 27,8 | .806II | 40, I | . 19389 |
| . 759 | .92II7 | 67,8 | . I I 466 | 27,8 | . 80651 | 40,0 | . 19349 |
| 0.760 | 9.92185 | 67,7 | O. II493 | 27,8 | 9.8069 I | 39,9 | O. 19309 |
| .76I | . 92252 | 67,7 | . II52I | 27,9 | . 80731 | 39,8 | . 19269 |
| . 762 | . 92320 | 67,6 | . II549 | 27,9 | . 80771 | 39,7 | . 19229 |
| . 763 | . 92387 | 67,6 | . II577 | 27,9 | .80810 | 39,6 | . 19190 |
| . 764 | . 92455 | 67,5 | . 11605 | 27,9 | . 80850 | 39,6 | . 19150 |
| 0.765 | 9.92522 | 67,4 | 0. II633 | 28,0 | 9.80889 | 39,5 | O. I9II I |
| . 766 | . 92590 | 67,4 | . 11661 | 28,0 | . 80929 | 39,4 | . 19071 |
| . 767 | . 92657 | 67,3 | . II689 | 28,0 | . 80968 | 39,3 | . 19032 |
| . 768 | . 92724 | 67,3 | . II7I7 | 28,0 | .81007 | 39,2 | . 18993 |
| .769 | . 92792 | 67,2 | . II74. | 28, I | .81047 | 39, I | . 18953 |
| 0.770 | 9.92859 | 67,1 | 0.11773 | 28, I | 9.81086 | 39,0 | 0. 18914 |
| . 771 | . 92926 | 67, 1 | . II80I | 28,1 | .81125 | 39,0 | . 18875 |
| . 772 | . 92993 | 67,0 | . 11829 | 28, I | .81164 | 38,9 | . 18836 |
| . 773 | . 93060 | 67,0 | . 11858 | 28,2 | .81202 | 38,8 | . 18798 |
| -7.74 | .93127 | 66,9 | . 11886 | 28,2 | .8I24I | 38,7 | . 18759 |
| 0.775 | 9.93194 | 66,8 | O. IIgI4 | 28,2 | 9.81280 | 38,6 | 0. 18720 |
| . 776 | .9326I | 66,8 | . II942 | 28,2 | .81318 | 38,5 | . 18682 |
| . 777 | . 93327 | 66,7 | . I 1970 | 28,3 | .81357 | 38,4 | . 18643 |
| . 778 | . 93394 | 66,7 | . II999 | 28,3 | . 81395 | 38,4 | . 18605 |
| . 779 | .9346I | 66,6 | . 12027 | 28,3 | . 81434 | 38,3 | . 18566 |
| 0.780 | 9.93527 | 66,5 | O. 12055 | 28,3 | 9.81472 | 38,2 | 0. 18528 |
| .78I | . 93594 | 66,5 | . 12084 | 28,4 | .81510 | 38, 1 | . 18490 |
| . 782 | . 93660 | 66,4 | . 12112 | 28,4 | .81548 | 38,0 | . 18452 |
| .783 | . 93727 | 66,4 | . 12141 | 28,4 | . 81586 | 37,9 | . 18414 |
| .784 | . 93793 | 66,3 | . 12169 | 28,4 | .81624 | 37,9 | . 18376 |
| 0.785 | 9.93859 | 66,2 | 0.12197 | 28,5 | 9.81662 | 37,8 | o. 18338 |
| . 786 | . 93925 | 66,2 | . 12226 | 28,5 | .81699 | 37,7 | . 18301 |
| . 787 | . 93992 | 66, 1 | . 12254 | 28,5 | .81737 | 37,6 | . 18263 |
| . 788 | . 94058 | 66, 1 | . 12283 | 28,5 | .81775 | 37,5 | . 18225 |
| . 789 | . 94124 | 66,0 | . 12312 | 28,6 | .81812 | 37,4 | . 18188 |
| 0.790 | 9.94190 | 66,0 | 0.12340 | 28,6 | 9.81850 | 37,4 | 0.18I50 |
| .791 | . 94256 | 65,9 | . 12369 | 28,6 | .81887 | 37,3 | . 18113 |
| . 792 | -9432I | 65,8 | . 12397 | 28,6 | . 81924 | 37,2 | . 18076 |
| -793 | -94387 | 65,8 | . 12426 | 28,7 | .8196I | 37, I | . 18039 |
| . 794 | . 94453 | 65,7 | . 12455 | 28,7 | . 8I998 | 37,0 | . 18002 |
| 0.795 | 9.94519 | 65,7 | 0.12483 | 28,7 | 9.82035 | 37,0 |  |
| . 796 | . 94584 | 65,6 | . 12512 | 28,7 | . 82072 | 36,9 | . I7928 |
| . 797 | . 94650 | 65,6 | . 1254 I | 28,8 | . 82109 | 36,8 | . I7891 |
| . 798 | -947I6 | 65,5 | . I2570 | 28,8 | . 82146 | 36,7 | . 17854 |
| . 799 | .94781 | 65,5 | . 12598 | 28,8 | . 82183 | 36,6 | . 17817 |
| 0.800 | 9.94846 | 65,4 | 0.12627 | 28,8 | 9.82219 | 36,6 | 0.17781 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.800 | 9.94846 | 65,4 | 0.12627 | 28,8 | 9.82219 | 36,6 | 0.17781 |
| . 801 | . 94912 | 65,3 | . 12656 | 28,9 | . 82256 | 36,5 | . I7744 |
| . 802 | . 94977 | 65,3 | . 12685 | 28,9 | . 82292 | 36,4 | . 17708 |
| . 803 | . 95042 | 65,2 | . 12714 | 28,9 | . 82329 | 36,3 | . 17671 |
| . 804 | .95108 | 65,2 | . 12743 | 28,9 | . 82365 | 36,2 | . 17635 |
| 0.805 | 9.95173 | 65,1 | 0.12772 | 29,0 | 9.82401 | 36,2 | 0.17599 |
| . 806 | . 95238 | 65, 1 | . 12801 | 29,0 | . 82437 | 36, 1 | . 17563 |
| . 807 | . 95303 | 65,0 | . 12830 | 29,0 | . 82473 | 36,0 | . 17527 |
| . 808 | . 95368 | 65,0 | . 12859 | 29,0 | . 82509 | 35,9 | . 17491 |
| . 809 | . 95433 | 64,9 | . 12888 | 29, I | . 82545 | 35,9 | . 17455 |
| 0.810 | 9.95498 | 64,9 | 0.12917 | 29, 1 | 9.8258 I | 35,8 | 0.17419 |
| .8II | . 95563 | 64,8 | . 12946 | 29, I | . 82617 | 35,7 | . 17383 |
| . 812 | . 95627 | 64,8 | . 12975 | 29, I | . 82652 | 35,6 | . 17348 |
| . 813 | . 95692 | 64,7 | . 13004 | 29,2 | . 82688 | 35,5 | . 17312 |
| . 814 | . 95757 | 64,6 | . 13033 | 29,2 | . 82723 | 35,5 | . 17277 |
| 0.815 | 9.9582 I | 64,6 | 0.13063 | 29,2 | 9.82759 | 35,4 | 0.17241 |
| .816 | . 95886 | 64,5 | . I3092 | 29,2 | . 82794 | 35,3 | . 17206 |
| .8I7 | . 95950 | 64,5 | . 13121 | 29,2 | . 82829 | 35,2 | .17171 |
| . 818 | .96015 | 64,4 | - I3I50 | 29,3 | . 82865 | 35,2 | . I7I35 |
| . 819 | . 96079 | 64,4 | . 13180 | 29,3 | . 82900 | 35, I | . 17100 |
| 0.820 | 9.96144 | 64,3 | 0.13209 | 29,3 | 9.82935 | 35,0 | 0.17065 |
| . 821 | . 96208 | 64,3 | . 13238 | 29,3 | . 82970 | 34,9 | . 17030 |
| . 822 | . 96272 | 64,2 | . 13268 | 29,4 | . 83005 | 34,9 | . 16995 |
| . 823 | . 96336 | 64,2 | . I3297 | 29,4 | . 83040 | 34,8 | . 16960 |
| . 824 | .9640I | 64, I | . 13326 | 29,4 | . 83074 | 34,7 | . 16926 |
| 0.825 | 9.96465 | 64,1 | 0.13356 | 29,4 | 9.83109 | 34,6 | 0. 16891 |
| . 826 | . 96529 | 64,0 | . 13385 | 29,5 | . 83144 | 34,6 | . 16856 |
| . 827 | . 96593 | 64,0 | . 13415 | 29,5 | . 83178 | 34,5 | . 16822 |
| . 828 | . 96657 | 63,9 | . 13444 | 29,5 | . 83213 | 34,4 | . 16787 |
| . 829 | .9672I | 63,9 | . I3474 | 29,5 | . 83247 | 34,3 | . 16753 |
| 0.830 | 9.96784 | 63,8 | 0.13503 | 29,6 | 9.83281 | 34,3 | 0.16719 |
| . 831 | . 96848 | 63,8 | . I 3533 | 29,6 | . 83316 | 34,2 | . 16684 |
| . 832 | .96912 | 63,7 | . 13562 | 29,6 | . 83350 | 34,1 | . 16650 |
| . 833 | . 96976 | 63,7 | . 13592 | 29,6 | . 83384 | 34,0 | . 16616 |
| . 834 | . 97039 | 63,6 | . 13622 | 29,6 | . 83418 | 34,0 | . 16582 |
| 0.835 | 9.97103 | 63,6 | 0.13651 | 29,7 | 9.83452 | 33,9 | 0. 16548 |
| . 836 | . 97167 | 63,5 | . 13681 | 29,7 | . 83486 | 33,8 | . 16514 |
| . 837 | . 97230 | 63,5 | . 13711 | 29,7 | . 83519 | 33,8 | . 16481 |
| . 838 | . 97293 | 63,4 | . 13740 | 29,7 | . 83553 | 33,7 | . 16447 |
| . 839 | . 97357 | 63,4 | . 13770 | 29,8 | . 83587 | 33,6 | . 16413 |
| 0.840 | 9.97420 | 63,3 | 0.13800 | 29,8 | 9.83620 | 33,5 | 0. 16380 |
| .84I | . 97484 | 63,3 | . 13830 | 29,8 | . 83654 | 33,5 | . 16346 |
| . 842 | . 97547 | 63,2 | . 13860 | 29,8 | . 83687 | 33,4 | . 16313 |
| . 843 | .97610 | 63,2 | - I3889 | 29,9 | . 83721 | 33,3 | . 16279 |
| . 844 | . 97673 | 63,1 | . 13919 | 29,9 | . 83754 | 33,3 | . 16246 |
| 0.845 | 9.97736 | 63,1 | 0. 13949 | 29,9 | 9.83787 | 33,2 | 0. 16213 |
| . 846 | . 97799 | 63,0 | . 13979 | 29,9 | . 83820 | 33, 1 | . 16180 |
| . 847 | . 97862 | 63,0 | . 14009 | 29,9 | . 83853 | 33,0 | . 16147 |
| . 848 | . 97925 | 62,9 | . 14039 | 30,0 | . 83886 | 33,0 | . 16II4 |
| . 849 | . 97988 | 62,9 | . 14069 | 30,0 | . 83919 | 32,9 | . 1608I |
| 0.850 | 9.98051 | 62,8 | 0. 14099 | 30,0 | 9.83952 | 32,8 | 0. 16048 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.850 | 9.98051 | 62,8 | 0. I4099 | 30,0 | 9.83952 | 32,8 | 0. 16048 |
| . 851 | .98II4 | 62,8 | . 14129 | 30,0 | . 83985 | 32,8 | . 16015 |
| . 852 | .98177 | 62,7 | . 14159 | 30, I | . 84018 | 32,7 | . 15982 |
| . 853 | . 98239 | 62,7 | . 14189 | 30, I | . 84050 | 32,6 | . I 5950 |
| . 854 | . 98302 | 62,7 | . 14219 | 30, I | . 84083 | 32,6 | . 15917 |
| 0.855 | 9.98365 | 62,6 | 0.14249 | 30, I | 9.84115 | 32,5 | 0.15885 |
| . 856 | . 98427 | 62,6 | . I4279 | 30, I | . 84148 | 32,4 | . 15852 |
| . 857 | . 98490 | 62,5 | .14310 | 30,2 | .84180 | 32,3 | . 15820 |
| . 858 | . 98552 | 62,5 | . 14340 | 30,2 | . 84213 | 32,3 | . 15787 |
| . 859 | .986I5 | 62,4 | . 14370 | 30,2 | . 84245 | 32,2 | . 15755 |
| 0.860 | 9.98677 | 62,4 | 0.14400 | 30,2 | 9.84277 | 32, 1 | 0. 15723 |
| . 86 I | . 98739 | 62,3 | . 14430 | 30,3 | . 84309 | 32,1 | . 15691 |
| . 862 | . 98802 | 62,3 | . I446I | 30,3 | . 84341 | 32,0 | . 15659 |
| . 863 | . 98864 | 62,2 | . I449I | 30,3 | . 84373 | 31,9 | . 15627 |
| . 864 | . 98926 | 62,2 | . I452I | 30,3 | . 84405 | 31,9 | . 15595 |
| 0.865 | 9.98988 | 62, 1 | 0.14552 | 30,3 | 9.84437 | 3I,8 | -. 15563 |
| . 866 | . 9905 I | 62, 1 | . I4582 | 30,4 | . 84469 | 31,7 | . 1553 I |
| . 867 | .99113 | 62,1 | . 14612 | 30,4 | . 84500 | 31,7 | . 15500 |
| . 868 | . 99175 | 62,0 | . I4643 | 30,4 | . 84532 | 31,6 | . I 5468 |
| . 869 | . 99237 | 62,0 | . 14673 | 30,4 | . 84563 | 31,5 | . 15437 |
| 0.870 | 9.99299 | 6I,9 | 0.14704 | 30,5 | 9.84595 | 31,5 | 0. 15405 |
| . 871 | . 99361 | 6I,9 | . 14734 | 30,5 | . 84626 | 31,4 | . I5374 |
| . 872 | . 99422 | 6I,8 | . 14765 | 30,5 | . 84658 | 31,3 | . 15342 |
| . 873 | . 99484 | 61,8 | . 14795 | 30,5 | . 84689 | 3I,3 | . 153 II |
| . 874 | . 99546 | 6I,7 | . 14826 | 30,5 | . 84720 | 31,2 | . 15280 |
| 0.875 | 9.99608 | 6I,7 | 0.14856 | 30,6 | 9.84751 | 3I, I | 0. 15249 |
| . 876 | . 99669 | 61,7 | . 14887 | 30,6 | . 84783 | 31, I | . 15217 |
| . 877 | . 9973 I | 6I,6 | . 14917 | 30,6 | .84814 | 31,0 | . 15186 |
| . 878 | . 99793 | 6I,6 | . 14948 | 30,6 | . 84845 | 30,9 | . 15155 |
| . 879 | . 99854 | 6I,5 | . 14979 | 30,7 | . 84875 | 30,9 | . 15125 |
| 0.880 | 9.99916 | 6I,5 | 0.15009 | 30,7 | 9.84906 | 30,8 | 0. 15094 |
| .88I | . 99977 | 6I,4 | . 15040 | 30,7 | . 84937 | 30,7 | . 15063 |
| . 882 | 0.00038 | 6I,4 | . 1507 I | 30,7 | . 84968 | 30,7 | . 15032 |
| . 883 | . 00100 | 6I,3 | . 15101 | 30,7 | . 84998 | 30,6 | . 15002 |
| . 884 | .00161 | 6r,3 | . 5152 | 30,8 | . 85029 | 30,5 | . 14971 |
| 0.885 | 0.00222 | 6r,3 | 0.15163 | 30,8 | 9.85059 | 30,5 | 0. I494I |
| . 886 | . 00284 | 6I,2 | .15194 | 30,8 | . 85090 | 30,4 | . 14910 |
| . 887 | . 00345 | 61,2 | . 15225 | 30,8 | . 85120 | 30,3 | . 14880 |
| . 888 | . 00406 | 61, 1 | . 15255 | 30,9 | .85I5I | 30,3 | . 14849 |
| . 889 | . 00467 | 6I,I | . 15285 | 30,9 | .85181 | 30,2 | .148I9 |
| 0.890 | 0.00528 | 61,0 | 0.15317 | 30,9 | 9.852 II | 30,2 | 0.14789 |
| . 891 | . 00589 | 61,0 | . 15348 | 30,9 | . 85241 | 30,1 | . 14759 |
| . 892 | . 00650 | 6i,0 | . 15379 | 30,9 | . 8527 I | 30,0 | . 14729 |
| . 893 | .007II | 60,9 | . 15410 | 31,0 | . 85301 | 30,0 | . I4699 |
| . 894 | . 00772 | 60,9 | . 1544 I | 31,0 | . 8533 I | 29,9 | . I4669 |
| 0.895 | 0.00833 | 60,8 | 0. I 5472 | 31,0 | 9.85361 | 29,8 | 0. 14639 |
| . 896 | . 00894 | 60,8 | . I5503 | 31,0 | . 85391 | 29,8 | . I4609 |
| . 897 | . 00955 | 60,8 | . 15534 | 31,0 | . 8542 I | 29,7 | . I4579 |
| . 898 | . OIOI5 |  | . 15565 | $3 \mathrm{I}, \mathrm{I}$ | . 85450 | 29,6 | . I4550 |
| . 899 | . 01076 | 60,7 | . 15556 | 3I, I | . 85480 | 29,6 | . I4520 |
| 0.800 | 0.01137 | 60,6 | 0.15627 | 3I, I | 9.85509 | 29,5 | 0.14491 |
| u | $\log \tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \mathrm{csc} \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.900 | 0.01137 | 60,6 | 0. 15627 | 3I, I | 9.85509 | 29,5 | 0. I4491 |
| . 901 | . 01197 | 60,6 | . I5658 | 3I, I | . 85539 | 29,5 | .1446I |
| . 902 | .01258 | 60,5 | . 15689 | 3I,2 | . 85568 | 29,4 | . 14432 |
| . 903 | .01318 | 60,5 | . 1572 I | 3I,2 | . 85598 | 29,3 | . 14402 |
| . 904 | .OI379 | 60,5 | . 15752 | 31,2 | . 85627 | 29,3 | . 14373 |
| 0.905 | 0.01439 | 60,4 | 0. 15783 | 3I,2 | 9.85656 | 29,2 | O. I4344 |
| . 906 | .OI500 | 60,4 | . 15814 | 31,2 | . 85685 | 29,2 | . 14315 |
| . 907 | . 01560 | 60,3 | . 15846 | $3 \mathrm{I}, 3$ | . 85715 | 29, I | . 14285 |
| . 908 | .01620 | 60,3 | . 15877 | $3 \mathrm{I}, 3$ | . 85744 | 29,0 | . 14256 |
| . 909 | .0168I | 60,3 | . 15908 | 3I,3 | . 85773 | 29,0 | . I4227 |
| 0.910 | 0.01741 | 60,2 | 0.15939 | 31,3 | 9.85801 | 28,9 | 0.14199 |
| .91I | . 01801 | 60,2 | . I5971 | 3I,3 | . 85830 | 28,8 | . 14170 |
| . 912 | .0186I | 60,1 | . 16002 | 3I,4 | . 85859 | 28,8 | . 14141 |
| . 913 | .0192I | 60, 1 | . 16033 | 3I,4 | . 85888 | 28,7 | . 14112 |
| . 914 | .0198I | 60, 1 | . 16065 | 3I,4 | . 85917 | 28,7 | . I4083 |
| 0.915 | 0.0204 I | 60,0 | 0.16096 | 3I,4 | 9.85945 | 28,6 | 0.14055 |
| . 916 | .02101 | 60,0 | . 16128 | 31,4 | . 85974 | 28,5 | . 14026 |
| .917 | .0216I | 59,9 | . 16159 | 31,5 | . 86002 | 28,5 | . I3998 |
| . 918 | .0222I | 59,9 | . 16191 | 3I,5 | . 8603 I | 28,4 | . 13969 |
| . 919 | .0228I | 59,9 | . 16222 | 3I,5 | . 85059 | 28,4 | . I394I |
| 0.920 | 0.0234 I | 59,8 | 0.16254 | 3I,5 | 9.86088 | 28,3 | 0.13912 |
| .92I | . 02401 | 59,8 | . 16285 | 31,5 | .86ir6 | 28,2 | . 13884 |
| . 922 | .02461 | 59,8 | . 16317 | 31,6 | .86I44 | 28,2 | . I3856 |
| .923 | . 02520 | 59,7 | . 16348 | 31,6 | .86r72 | 28, I | . 13828 |
| . 924 | . 02580 | 59,7 | . 16380 | 3I,6 | . 86200 | 28, I | . 13800 |
| 0.925 | 0.02640 | 59,6 | 0.164II | 31,6 | 9.86228 | 28,0 | 0. I3772 |
| . 926 | . 02699 | 59,6 | . 16443 | 31,6 | . 86256 | 27,9 | . I3744 |
| .927 | . 02759 | 59,6 | . 16475 | $3 \mathrm{I}, 7$ | . 86284 | 27,9 | . 13716 |
| . 928 | .02819 | 59,5 | . 16506 | $3 \mathrm{I}, 7$ | . 86312 | 27,8 | . 13688 |
| . 929 | .02878 | 59,5 | . 16538 | 31,7 | . 86340 | 27,8 | . I3660 |
| 0.930 | 0.02937 | 59,4 | 0. 16570 | 3I,7 | 9.86368 | 27,7 | 0.13632 |
| .93I | . 02997 | 59,4 | . 16602 | 31,7 | . 86395 | 27,7 | . 13605 |
| . 932 | . 03056 | 59,4 | . 16633 | 3I,8 | . 86423 | 27,6 | . I3577 |
| . 933 | .03116 | 59,3 | . 16665 | $3 \mathrm{I}, 8$ | . 86450 | 27.5 | . I3550 |
| . 934 | .03175 | 59,3 | . 16697 | 31,8 | . 86478 | 27,5 | . 13522 |
| 0.935 | 0.03234 | 59,3 | 0.16729 | 31,8 | 9.86505 | 27,4 | 0.13495 |
| . 936 | . 03293 | 59,2 | . 16761 | 31,9 | . 86533 | 27,4 | . I3467 |
| . 937 | . 03353 | 59,2 | . 16792 | 31,9 | . 86560 | 27,3 | - I3440 |
| . 938 | .03412 | 59, I | . 16824 | 3I,9 | . 86587 | 27,3 | . 13413 |
| . 939 | . 0347 I | 59, I | . 16856 | 31,9 | .866I5 | 27,2 | . 13385 |
| 0.940 | 0.03530 | 59,1 | 0. 16888 | 31,9 | 9.86642 | 27, I | 0. 13358 |
| .94I | . 03589 | 59,0 | . 16920 | 32,0 | . 86669 | 27, I | . I333I |
| .942 | . 03648 | 59,0 | . 16952 | 32,0 | . 86696 | 27,0 | . 13304 |
| . 943 | .03707 | 59,0 | . 16984 | 32,0 | . 86723 | 27,0 | . 13277 |
| . 944 | . 03766 | 58,9 | . 17016 | 32,0 | . 86750 | 26,9 | . 13250 |
| 0.945 | 0.03825 | 58,9 | 0.17048 | 32,0 | 9.86777 | 26,9 | 0. I3223 |
| . 946 | . 03884 | 58,9 | . 17080 | 32,0 | . 86804 | 26,8 | . I3196 |
| . 947 | . 03943 | 58,8 | . 17112 | $32, \mathrm{I}$ | . 86830 | 26,7 | .13170 |
| .948 | .04001 | 58,8 | . I7I44 | 32, I | . 85857 | 26,7 | . 13143 |
| . 949 | . 04060 | 58,7 | . 17176 | 32, I | . 86884 | 26,6 | . 13116 |
| 0.950 | 0.04119 | 58,7 | 0.17208 | 32,I | 9.86910 | 26,6 | 0.13090 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.950 | 0.04119 | 58,7 | 0. 17208 | 32, I | 9.86910 | 26,6 | 0. I3090 |
| .95I | .04178 | 58,7 | . 17241 | 32, I | . 86937 | 26,5 | . 13063 |
| . 952 | . 04236 | 58,6 | . 17273 | 32,2 | . 86963 | 26,5 | . 13037 |
| . 953 | . 04295 | 58,6 | . 17305 | 32,2 | . 86990 | 26,4 | . 13010 |
| . 954 | . 04353 | 58,6 | . 17337 | 32,2 | . 87016 | 26,4 | . 12984 |
| 0.955 | 0.04412 | 58,5 | 0.17369 | 32,2 | 9.87043 | 26,3 | 0. 12957 |
| . 956 | . 04470 | 58,5 | . 17402 | 32,2 | . 87069 | 26,2 | . 12931 |
| . 957 | . 04529 | 58,5 | . I7434 | 32,3 | . 87095 | 26,2 | . 12905 |
| . 958 | . 04587 | 58,4 | . 17466 | 32,3 | . 87121 | 26, I | . 12879 |
| . 959 | . 04646 | 58,4 | . 17498 | 32,3 | . 87147 | 26, I | . 12853 |
| 0.960 | 0.04704 | 58,4 | 0.1753I | 32,3 | 9.87173 | 26,0 | 0. 12827 |
| . 961 | . 04763 | 58,3 | . 17563 | 32,3 | . 87199 | 26,0 | . 12801 |
| . 962 | .0482I | 58,3 | . 17595 | 32,4 | . 87225 | 25,9 | . 12775 |
| . 963 | . 04879 | 58,2 | . 17628 | 32,4 | . 8725 I | 25,9 | . 12749 |
| . 964 | . 04937 | 58,2 | . 17660. | 32,4 | . 87277 | 25,8 | . 12723 |
| 0.965 | 0.04996 | 58,2 | 0.17693 | 32,4 | 9.87303 | 25,8 | 0. 12697 |
| . 966 | . 05054 | 58, I | . 17725 | 32,4 | . 87329 | 25,7 | . 12671 |
| . 967 | .05112 | 58, I | . I7757 | 32,5 | . 87354 | 25,7 | . 12646 |
| . 968 | .05170 | 58, I | . 17790 | 32,5 | . 87380 | 25,6 | . 12620 |
| . 969 | . 05228 | 58,0 | . 17822 | 32,5 | . 87406 | 25,5 | . 12594 |
| 0.970 | 0.05286 | 58,0 | 0. 17855 | 32,5 | 9.87431 | 25,5 | 0. 12569 |
| . 971 | . 05344 | 58,0 | . 17887 | 32,5 | . 87456 | 25,4 | . 12544 |
| . 972 | . 05402 | 57,9 | . 17920 | 32,6 | . 87482 | 25,4 | . 12518 |
| . 973 | . 05460 | 57,9 | . 17953 | 32,6 | . 87507 | 25,3 | . 12493 |
| . 974 | .05518 | 57,9 | . 17985 | 32,6 | . 87533 | 25,3 | . 12467 |
| 0.975 | 0.05576 | 57,8 | -. 18018 | 32,6 | 9.87558 | 25,2 | 0.12442 |
| . 976 | . 05633 | 57,8 | . 18050 | 32,6 | . 87583 | 25,2 | . 12417 |
| . 977 | .0569I | 57,8 | . 18083 | 32,6 | . 87608 | 25, I | . 12392 |
| . 978 | . 05749 | 57,7 | . 18ir6 | 32,7 | . 87633 | 25, I | . 12367 |
| . 979 | . 05807 | 57,7 | . 18148 | 32,7 | . 87658 | 25,0 | . 12342 |
| 0.980 | 0.05864 | 57,7 | 0.1818 I | 32,7 | 9.87683 | 25,0 | 0.12317 |
| .98I | . 05922 | 57,6 | . 18214 | 32,7 | . 87708 | 24,9 | . 12292 |
| . 982 | . 05980 | 57,6 | . 18246 | 32,7 | . 87733 | 24,9 | . 12267 |
| . 983 | . 06037 | 57,6 | . 18279 | 32,8 | . 87758 | 24,8 | . 12242 |
| . 984 | . 06095 | 57,5 | .18312 | 32,8 | . 87783 | 24,8 | . 12217 |
| 0.985 | 0.06152 | 57,5 | 0. 18345 | 32,8 | 9.87807 | 24,7 | 0.12193 |
| . 986 | .06210 | 57,5 | . 18378 | 32,8 | . 87832 | 24,7 | . 12168 |
| . 987 | . 06267 | 57,4 | . 18410 | 32,8 | . 87857 | 24,6 | . 12143 |
| . 988 | . 06325 | 57,4 | . 18443 | 32,9 | . 8788 I | 24,6 | . 12119 |
| .989 | . 06382 | 57,4 | . 18476 | 32,9 | . 87906 | 24,5 | . 12094 |
| 0.990 | 0.06439 | 57,3 | 0.18509 | 32,9 | 9.87930 | 24,5 | 0.12070 |
| .99I | . 06497 | 57,3 | . 18542 | 32,9 | . 87955 | 24,4 | . 12045 |
| . 992 | . 06554 | 57,3 | . 18575 | 32,9 | . 87979 | 24,3 | . 12021 |
| . 993 | .066I I | 57,2 | . 18608 | 32,9 | . 88003 | 24,3 | . 11997 |
| . 994 | . 06669 | 57,2 | . 18641 | 33,0 | . 88028 | 24,2 | . I 1972 |
| 0.995 | 0.06726 | 57,2 | 0.18674 | 33,0 | 9.88052 | 24,2 | 0. 11948 |
| . 996 | . 06783 | 57,2 | . 18707 | 33,0 | . 88076 | 24,1 | . 11924 |
| . 997 | . 06840 | 57, I | . 18740 | 33,0 | .88100 | 24, I | . 11900 |
| . 998 | . 06897 | 57, I | . 18773 | 33,0 | .88I24 | 24,0 | . 11876 |
| . 999 | . 06954 | 57, I | . 18806 | 33, I | .88I48 | 24,0 | . 11852 |
| 1.000 | 0.07011 | 57,0 | 0.18839 | 33, 1 | 9.88 I 72 | 23,9 | 0. 11828 |
| u | $\log \tan g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.0701 I | 57,0 | 0.18839 | 33, I | 9.88172 | 23,9 | 0.11828 |
| .001 | . 07068 | 57,0 | . 18872 | 33, I | .88196 | 23,9 | . 11804 |
| . 002 | . 07125 | 57,0 | . 18905 | 33, I | . 88220 | 23,8 | . 11780 |
| . 003 | . 07182 | 56,9 | . 18938 | 33,I | . 88244 | 23,8 | . 11756 |
| . 004 | . 07239 | 56,9 | . I8971 | 33, 1 | . 88268 | 23,8 | . 11732 |
| 1.005 | 0.07296 | 56,9 | 0. 19004 | 33,2 | 9.88291 | 23,7 | 0. 11709 |
| . 006 | . 07353 | 56,8 | . 19038 | 33,2 | .88315 | 23,7 | . 11685 |
| . 007 | .07410 | 56,8 | . 19071 | 33,2 | . 88339 | 23,6 | . 11661 |
| . 008 | . 07466 | 56,8 | . 19104 | 33,2 | . 88362 | 23,6 | . 11638 |
| . 009 | . 07523 | 56,7 | . 18137 | 33,2 | . 88386 | 23,5 | . 11614 |
| 1.010 | 0.07580 | 56,7 | 0.19171 | 33,3 | 9.88409 | 23,5 | 0.11591 |
| . OII | . 07637 | 56,7 | . 19204 | 33,3 | . 88433 | 23,4 | . II567 |
| . 012 | . 07693 | 56,7 | . 19237 | 33,3 | . 88456 | 23,4 | . II544 |
| . 013 | . 07750 | 56,6 | . 19270 | 33,3 | . 88480 | 23,3 | . II520 |
| . 014 | . 07807 | 56,6 | . 19304 | 33,3 | . 88503 | 23,3 | . I 1497 |
| 1.015 | 0.07863 | 56,6 | o. 19337 | 33,3 | 9.88526 | 23,2 | O. II474 |
| . 016 | . 07920 | 56,5 | . 19370 | 33,4 | . 88549 | 23,2 | . II45I |
| . 017 | . 07976 | 56,5 | . 19404 | 33,4 | . 88572 | 23, I | . 11428 |
| . 018 | . 08033 | 56,5 | . 19437 | 33,4 | . 88595 | 23, I | . II405 |
| . 019 | . 08089 | 56,4 | . 1947I | 33,4 | . 88619 | 23,0 | . II38I |
| 1.020 | 0.08146 | 56,4 | 0.19504 | 33,4 | 9.88642 | 23,0 | 0.11358 |
| .02I | . 08202 | 56,4 | . 19537 | 33,5 | . 88664 | 22,9 | . 11336 |
| . 022 | . 08258 | 56,4 | . 1957I | 33,5 | . 88687 | 22,9 | . II313 |
| . 023 | . 08315 | 56,3 | . 19604 | 33,5 | . 88710 | 22,8 | . I1290 |
| . 024 | . 08371 | 56,3 | . 19638 | 33,5 | . 88733 | 22,8 | . 11267 |
| 1.025 | 0.08427 | 56,3 | 0. 19671 | 33,5 | 9.88756 | 22,7 | 0.11244 |
| . 026 | . 08483 | 56,2 | . 19705 | 33,5 | . 88779 | 22,7 | . II22I |
| . 027 | . 08540 | 56,2 | . 19738 | 33,6 | .8880I | 22,6 | . 11199 |
| . 028 | . 08596 | 56,2 | . 19772 | 33,6 | . 88824 | 22,6 | . 11176 |
| . 029 | . 08652 | 56, I | . 19806 | 33,6 | . 88846 | 22,6 | . III 54 |
| 1.030 | 0.08708 | 56, I | o. 19839 | 33,6 | 9.88859 | 22,5 | O.III3I |
| .03I | . 08764 | 56, I | . 19873 | 33,6 | .8889I | 22,5 | . II 109 |
| . 032 | . 08820 | 56, I | . 19906 | 33,6 | . 88914 | 22,4 | . 11086 |
| . 033 | . 08876 | 56,0 | . 19940 | 33,7 | . 88936 | 22,4 | . 11064 |
| . 034 | . 08932 | 56,0 | . 19974 | 33,7 | . 88959 | 22,3 | . IIO4I |
| 1.035 | 0.08988 | 56,0 | 0.20007 | 33,7 | 9.88981 | 22,3 | 0.11019 |
| . 036 | . 09044 | 55,9 | . 2004 I | 33,7 | . 89003 | 22,2 | . 10997 |
| . 037 | . 09100 | 55,9 | . 20075 | 33,7 | . 89025 | 22,2 | . 10975 |
| . 038 | . 09156 | 55,9 | . 20109 | 33,7 | . 89048 | 22,1 | . 10952 |
| . 039 | . 09212 | 55,9 | .20142 | 33,8 | . 89070 | 22,I | . 10930 |
| 1.040 | 0.09268 | 55,8 | 0.20176 | 33,8 | 9.89092 | 22,0 | 0. 10908 |
| .04I | . 09324 | 55,8 | . 20210 | 33,8 | . 89114 | 22,0 | . 10886 |
| . 042 | . 09379 | 55,8 | . 20244 | 33,8 | . 89136 | 22,0 | . 10864 |
| . 043 | . 09435 | 55,7 | . 20278 | 33,8 | . 89158 | 21,9 | . 10842 |
| . 044 | . 09491 | 55,7 | .203II | 33,9 | . 89180 | 21,9 | . 10820 |
| 1.045 | 0.09547 | 55,7 | 0.20345 | 33,9 | 9.89201 | 21,8 | 0. 10799 |
| . 046 | . 09602 | 55,7 | . 20379 | 33,9 | . 89223 | 21,8 | . 10777 |
| . 047 | . 09658 | 55,6 | . 20413 | 33,9 | . 89245 | 21,7 | . 10755 |
| . 048 | . 09714 | 55,6 | . 20447 | 33,9 | . 89267 | 21,7 | . 10733 |
| . 049 | . 09769 | 55,6 | . 2048I | 33,9 | . 89288 | 21,6 | . 10712 |
| 1.050 | 0.09825 | 55,6 | 0.20515 | 34,0 | 9.89310 | 21,6 | 0. 10690 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathrm{u}$ |

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| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.050 | 0.09825 | 55,6 | 0.20515 | 34,0 | 9.89310 | 21,6 | 0. 10690 |
| .05I | . 09880 | 55,5 | . 20549 | 34,0 | . 8933 I | 21,6 | . 10669 |
| . 052 | . 09936 | 55,5 | .20583 | 34,0 | . 89353 | 21,5 | . 10647 |
| . 053 | .09991 | 55,5 | . 20617 | 34,0 | . 89375 | 21,5 | . 10625 |
| . 054 | . 10047 | 55,4 | . 20651 | 34,0 | . 89396 | 2I,4 | . 10604 |
| 1.055 | 0.10102 | 55,4 | 0.20685 | 34,0 | 9.89417 | 2I,4 | 0. 10583 |
| . 056 | . 10158 | 55,4 | . 20719 | 34,1 | . 89439 | 21,3 | . 10561 |
| . 057 | . 10213 | 55,4 | . 20753 | 34, I | . 89460 | 21,3 | . 10540 |
| . 058 | . 10268 | 55,3 | . 20787 | $34, \mathrm{I}$ | . 8948 I | 2I,2 | . 10519 |
| . 059 | . 10324 | 55,3 | . 20821 | 34, I | . 89502 | 21,2 | . 10498 |
| 1.060 | 0.10379 | 55,3 | 0.20855 | 34,I | 9.89524 | 2I,2 | 0.10476 |
| .06I | . 10434 | 55,3 | . 20889 | 34, I | . 89545 | 2I, I | . 10455 |
| . 062 | . 10489 | 55,2 | . 20924 | 34,2 | . 89566 | 2I, I | . 10434 |
| . 063 | . 10545 | 55,2 | . 20958 | 34,2 | . 89587 | 21,0 | . 10413 |
| . 064 | . 10600 | 55,2 | . 20992 | 34,2 | . 89608 | 21,0 | . 10392 |
| 1.065 | 0. 10655 | 55,1 | 0.21026 | 34,2 | 9.89629 | 20,9 | 0.10371 |
| . 066 | . 10710 | 55, 1 | . 21060 | 34,2 | . 89650 | 20,9 | . 10350 |
| . 067 | . 10765 | 55, I | . 21094 | 34,2 | . 89671 | 20,9 | . IO329 |
| . 068 | . 10820 | 55, I | . 21129 | 34,3 | . 89692 | 20,8 | . 10308 |
| . 069 | . 10875 | 55,0 | . 21163 | 34,3 | . 89712 | 20,8 | . 10288 |
| 1.070 | 0. 10930 | 55,0 | 0.21197 | 34,3 | 9.89733 | 20,7 | 0. 10267 |
| . 071 | . 10985 | 55,0 | . 21232 | 34,3 | . 89754 | 20,7 | . 10246 |
| . 072 | . 11040 | 55,0 | . 21266 | 34,3 | . 89774 | 20,6 | . 10226 |
| . 073 | . 11095 | 54,9 | . 21300 | 34,3 | . 89795 | 20,6 | . 10205 |
| . 074 | . III 50 | 54,9 | . 21335 | 34,4 | . 89816 | 20,6 | . 10184 |
| 1.075 | 0.11205 | 54,9 | 0.21369 | 34,4 | 9.89836 | 20,5 | 0. 10164 |
| . 076 | . II260 | 54,9 | . 21403 | 34,4 | . 89857 | 20,5 | . IOI43 |
| . 077 | . II3I5 | 54,8 | . 21438 | 34,4 | . 89877 | 20,4 | . 10123 |
| . 078 | . I I 370 | 54,8 | . 21472 | 34,4 | . 89898 | 20,4 | . 10102 |
| . 079 | . II424 | 54,8 | .21507. | 34,4 | . 89918 | 20,3 | . 10082 |
| 1.080 | O. II479 | 54,8 | 0.2154 I | 34,4 | 9.89938 | 20,3 | 0. 10062 |
| .081 | . II 534 | 54,7 | - .21575 | 34,5 | . 89959 | 20,3 | . 1004 I |
| . 082 | . II589 | 54,7 | . 21610 | 34,5 | . 89979 | 20,2 | . 1002 I |
| . 083 | . 11643 | 54,7 | . 21644 | 34,5 | . 89999 | 20,2 | . 10001 |
| . 084 | . 11698 | 54,7 | . 21679 | 34,5 | .90019 | 20, I | . 09981 |
| 1.085 | 0. II753 | 54,6 | 0.21713 | 34,5 | 9.90039 | 20,1 | 0.0996 I |
| . 086 | . 11807 | 54,6 | . 21748 | 34,5 | . 90059 | 20,1 | . 09941 |
| . 087 | . 11862 | 54,6 | . 21782 | 34,6 | . 90079 | 20,0 | . 0992 I |
| . 088 | . 11916 | 54,5 | .21817 | 34,6 | . 90099 | 20,0 | . 0990 I |
| . 089 | . 11971 | 54,5 | . 21852 | 34,6 | .90119 | 19,9 | .0988I |
| 1.090 | 0.12025 | 54,5 | 0.21886 | 34,6 | 9.90139 | 19,9 | 0.09861 |
| .091 | . 12080 | 54,5 | . 21921 | 34,6 | .90159 | 19,9 | . 09841 |
| . 092 | . 12134 | 54,4 | . 21955 | 34,6 | .90179 | 19,8 | . 09821 |
| . 093 | . 12189 | 54,4 | . 21990 | 34,7 | .90199 | 19,8 | . 09881 |
| . 094 | . 12243 | 54,4 | . 22025 | 34,7 | .902I8 | 19,7 | . 09782 |
| 1.095 | 0.12298 | 54,4 | 0.22059 | 34,7 | 9.90238 | 19,7 | 0.09762 |
| . 096 | . 12352 | 54,4 | . 22094 | 34,7 | . 90258 | 19,6 | . 09742 |
| . 097 | . 12406 | 54,3 | . 22 I29 | 34,7 | . 90277 | 19,6 | . 09723 |
| . 098 | . 12461 | 54,3 | . 22164 | 34,7 | . 90297 | 19,6 | . 09703 |
| . 099 | . 12515 | 54,3 | . 22198 | 34,7 | . 90317 | 19,5 | . 09683 |
| 1. 100 | 0.12569 | 54,3 | 0.22233 | 34,8 | 9.90336 | 19,5 | 0.09664 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

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Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 100 | 0. 12569 | 54,3 | 0.22233 | 34,8 | 9.90336 | 19,5 | 0.09664 |
| . IOI | . 12623 | 54,2 | . 22268 | 34,8 | . 90356 | 19,4 | . 09644 |
| . 102 | .. 12678 | 54,2 | . 22303 | 34,8 | . 90375 | 19,4 | . 09625 |
| . 103 | . 12732 | 54,2 | . 22337 | 34,8 | . 90394 | 19,4 | . 09606 |
| . 104 | . 12786 | 54,2 | . 22372 | 34,8 | .904I4 | 19,3 | . 09586 |
| 1. 105 | 0. 12840 | 54,1 | 0.22407 | 34,8 | 9.90433 | 19,3 | 0.09567 |
| . 106 | . I2894 | 54, I | . 22442 | 34,9 | . 90452 | 19,2 | . 09548 |
| . 107 | . I2948 | 54, I | . 22477 | 34,9 | . 90472 | 19,2 | . 09528 |
| . 108 | . I3002 | 54, I | . 22512 | 34,9 | .90491 | 19,2 | . 09509 |
| . 109 | . 13056 | 54,0 | . 22547 | 34,9 | . 90510 | 19,I | . 09490 |
| I.IIC | O.I3III | 54,0 | 0.22582 | 34,9 | 9.90529 | 19, 1 | 0.09471 |
| . 111 | . 13165 | 54,0 | . 22616 | 34,9 | . 90548 | 19, 1 | . 09452 |
| . 112 | . 13218 | 54,0 | . 22651 | 35,0 | . 90567 | 19,0 | . 09433 |
| . II3 | . 13272 | 53,9 | . 22686 | 35,0 | . 90586 | 19,0 | . 09414 |
| . 114 | . 13326 | 53,9 | . 22721 | 35,0 | . 90605 | 18,9 | . 09395 |
| I. II5 | 0. 13380 | 53,9 | 0.22756 | 35,0 | 9.90624 | 18,9 | 0.09376 |
| . 116 | . I3434 | 53,9 | . 22791 | 35,0 | . 90643 | 18,9 | . 09357 |
| . II7 | - I3488 | 53,8 | . 22826 | 35,0 | . 90662 | 18,8 | . 09338 |
| . 118 | . I3542 | 53,8 | . 2286 I | 35,0 | . 90680 | 18,8 | . 09320 |
| . 119 | . 13596 | 53,8 | . 22896 | 35, I | . 90699 | 18,7 | .09301 |
| I. 120 | 0.13649 | 53,8 | 0.22931 | 35, I | 9.90718 | 18,7 | 0.09282 |
| . 12 I | . 13703 | 53,8 | . 22967 | 35, I | . 90737 | 18,7 | . 09263 |
| . 122 | . 13757 | 53,7 | . 23002 | 35, I | . 90755 | 18,6 | . 09245 |
| . 123 | . 1381 I | 53,7 | . 23037 | 35, I | . 90774 | 18,6 | . 09226 |
| . 124 | . 13864 | 53,7 | . 23072 | 35, I | . 90792 | 18,6 | . 09208 |
| I. 125 | 0.13918 | 53,7 | 0.23107 | 35, I | 9.908 II | 18,5 | 0.09189 |
| . 125 | . 13972 | 53,6 | . 23142 | 35,2 | . 90830 | 18,5 | .09170 |
| . 127 | . 14025 | 53,6 | . 23177 | 35,2 | . 90848 | I8,4 | .09152 |
| . 128 | . 14079 | 53,6 | . 23213 | 35,2 | .90866 | 18,4 | .09134 |
| . 129 | .14133 | 53,6 | . 23248 | 35,2 | . 90885 | 18,4 | .09II5 |
| I. I30 | 0.14186 | 53,5 | 0.23283 | 35,2 | 9.90903 | 18,3 | 0.09097 |
| . 131 | . 14240 | 53,5 | . 23318 | 35,2 | .9092I | 18,3 | . 09079 |
| . 132 | . I4293 | 53,5 | . 23353 | 35,3 | . 90940 | 18,3 | . 09060 |
| . 133 | . 14347 | 53,5 | . 23389 | 35,3 | . 90958 | 18,2 | . 09042 |
| . 134 | . 14400 | 53,5 | . 23424 | 35,3 | . 90976 | 18,2 | . 09024 |
| I. 135 | O. I4454 | 53,4 | 0.23459 | 35,3 | 9.90994 | 18,1 | 0.09006 |
| . 136 | . 14507 | 53,4 | . 23495 | 35.3 | .91012 | 18, 1 | . 08988 |
| . 137 | . 14560 | 53,4 | . 23530 | 35,3 | . 91030 | I8, 1 | . 08970 |
| . 138 | . 14614 | 53,4 | . 23565 | 35,3 | . 91049 | 18,0 | . 08951 |
| . 139 | . 14667 | 53,3 | .2360I | 35,4 | .91067 | 18,0 | . 08933 |
| I. I40 | 0.14720 | 53,3 | 0.23636 | 35,4 | 9.91085 | 18,0 | 0.08915 |
| . 141 | . 14774 | 53,3 | . 23671 | 35,4 | .91102 | 17,9 | . 08898 |
| . 142 | . I4827 | 53,3 | . 23707 | 35,4 | .91120 | I7,9 | . 08880 |
| . I43 | . I4880 | 53,3 | . 23742 | 35,4 | .91I38 | 17,8 | . 08862 |
| . I44 | . 14934 | 53,2 | . 23778 | 35,4 | .91I56 | 17,8 | . 08844 |
| I. 145 | 0. 14987 | 53,2 | 0.238I3 | 35,4 | 9.91174 | 17,8 | 0.08826 |
| . 146 | . 15040 | 53,2 | . 23848 | 35,5 | .91192 | 17,7 | . 08808 |
| . 147 | . 15093 | 53,2 | . 23884 | 35,5 | .91209 | 17,7 | .08791 |
| . I48 | . 15146 | 53,2 | . 23919 | 35,5 | .91227 | 17,7 | . 08773 |
| . 149 | . 15200 | 53, I | . 23955 | 35,5 | .91245 | 17,6 | . 08755 |
| I. 150 | 0.15253 | 53, I | 0.23990 | 35,5 | 9.91262 | 17,6 | 0.08738 |
| u | $\log \operatorname{tangd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 150 | 0. 15253 | 53, I | 0.23990 | 35,5 | 9.91262 | 17,6 | 0.08738 |
| . 151 | . 15305 | 53, I | . 24026 | 35,5 | . 91280 | 17,6 | . 08720 |
| . 152 | . 15359 | 53, I | . 24061 | 35,5 | .91297 | 17,5 | . 08703 |
| . 153 | . 15412 | 53,0 | . 24097 | 35,6 | .91315 | 17,5 | . 08685 |
| . 154 | . 15465 | 53,0 | .24133 | 35,6 | .91332 | 17,5 | . 08668 |
| 1.155 | 0.15518 | 53,0 | 0.24168 | 35,6 | 9.91350 | 17,4 | 0.08650 |
| . 156 | . 15571 | 53,0 | . 24204 | 35,6 | .91367 | 17,4 | . 08633 |
| . 157 | . 15624 | 53,0 | . 24239 | 35,6 | .91385 | 17,3 | .08615 |
| . 158 | . 15677 | 52,9 | . 24275 | 35,6 | .91402 | 17,3 | .08598 |
| . 159 | . 15730 | 52,9 | . 243 II | 36,6 | .91419 | 17,3 | .0858I |
| 1.160 | 0. 15783 | 52,9 | 0.24346 | 35,7 | 9.91436 | 17,2 | 0.08564 |
| .16I | . 15836 | 52,9 | . 24382 | 35,7 | . 91454 | 17,2 | . 08546 |
| . 162 | . 15888 | 52,9 | . 24418 | 35,7 | .91471 | 17,2 | . 08529 |
| .163 | . 15941 | 52,8 | . 24453 | 35,7 | . 91488 | 17,I | .08512 |
| . 164 | . 15994 | 52,8 | . 24489 | 35,7 | .91505 | 17,1 | . 08495 |
| I. 165 | 0. 16047 | 52,8 | 0.24525 | 35,7 | 9.91522 | I7,I | 0.08478 |
| . 166 | . 16100 | 52,8 | . 24560 | 35,7 | . 91539 | 17,0 | .0846I |
| .167 | .16152 | 52,7 | . 2.4596 | 35,8 | .91556 | I7,0 | . 08444 |
| . 168 | . 16205 | 52,7 | . 24632 | 35,8 | .91573 | 17,0 | .08427 |
| . 169 | . 16258 | 52,7 | . 24668 | 35,8 | .91590 | I6,9 | .08410 |
| 1.170 | 0.163II | 52,7 | 0.24703 | 35,8 | 9.91607 | 16,9 | 0.08393 |
| .171 | .16363 | 52,7 | . 24739 | 35,8 | . 91624 | 16,9 | . 08376 |
| . 172 | . 16416 | 52,6 | . 24775 | 35,8 | .9164I | 16,8 | . 08359 |
| . 173 | . 16469 | 52,6 | .248II | 35,8 | . 91658 | 16,8 | . 08342 |
| . 174 | . 1652 I | 52,6 | . 24847 | 35,9 | . 91674 | 16,8 | . 08326 |
| 1.175 | 0.16574 | 52,6 | 0.24883 | 35,9 | 9.91691 | 16,7 | 0.08309 |
| . 176 | . 16626 | 52,6 | . 24919 | 35,9 | .91708 | 16,7 | . 08292 |
| . 177 | . 16679 | 52,5 | . 24954 | 35,9 | .91724 | 16,7 | . 08276 |
| . 178 | . 16731 | 52,5 | . 24990 | 35,9 | .9174I | 16,6 | . 08259 |
| . 179 | . 16784 | 52,5 | .25026 | 35,9 | .91758 | 16,6 | . 08242 |
| 1. 180 | 0.16836 | 52,5 | 0.25062 | 35,9 | 9.91774 | 16,6 | 0.08226 |
| . 18 I | . 16889 | 52,5 | . 25098 | 35,9 | .91791 | 16,5 | . 08209 |
| . 182 | . 16941 | 52,4 | . 25134 | 36,0 | .91807 | 16,5 | .08193 |
| .183 | . 16994 | 52,4 | .25I70 | 36,0 | .91824 | 16,4 | .08r76 |
| . 184 | . 17046 | 52,4 | .25206 | 36,0 | .91840 | 16,4 | .08160 |
| 1. 185 | 0.17099 | 52,4 | 0.25242 | 36,0 | 9.91857 | 16,4 | 0.08143 |
| . 186 | . 17151 | 52,4 | . 25278 | 36,0 | . 91873 | 16,3 | .08127 |
| . 187 | . 17203 | 52,3 | . 25314 | 36,0 | . 91889 | 16,3 | .08III |
| . 188 | . 17256 | 52,3 | . 25350 | 36,0 | .91906 | 16,3 | . 08094 |
| . 189 | . 17308 | 52,3 | . 25386 | 36, 1 | . 91922 | 16,2 | . 08078 |
| I. 190 | 0.17360 | 52,3 | 0.25422 | 36, 1 | 9.91938 | 16,2 | 0.08062 |
| . 191 | . 17413 | 52,3 | . 25458 | 36, | . 91954 | 16,2 | . 08046 |
| . 192 | . 17465 | 52,2 | . 25494 | 36, 1 | . 91970 | 16,2 | .08030 |
| . 193 | . 17517 | 52,2 | . 25530 | 36, | .91987 | 16,1 | . 08013 |
| . 194 | . 17569 | 52,2 | . 25567 | 36, 1 | . 92003 | 16, 1 | . 07997 |
| 1. 195 | 0.17621 | 52,2 | 0.25603 | 36, 1 | 9.92019 | 16,1 | 0.07981 |
| . 196 | . 17674 | 52,2 | . 25639 | 36,2 | . 92035 | 16,0 | . 07965 |
| . 197 | . 17726 | 52,2 | . 25675 | 36,2 | . 9205 I | 16,0 | . 07949 |
| . 198 | . 17778 | 52,1 | . 2571 I | 36,2 | . 92067 | 16,0 | . 07933 |
| . 199 | . 17830 | 52,I | . 25747 | 36,2 | . 92083 | I5,9 | .07917 |
| I. 200 | 0. 17882 | 52, I | 0.25784 | 36,2 | 9.92099 | I5,9 | 0.07901 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.200 | 0.17882 | 52,I | 0.25784 | 36,2 | 9.92099 | 15,9 | 0.07901 |
| . 201 | . 17934 | 52,I | . 25820 | 36,2 | .92II4 | 15,9 | . 07886 |
| . 202 | . 17986 | 52,I | . 25856 | 36,2 | . 92130 | 15,8 | . 07870 |
| . 203 | . 18038 | 52,0 | . 25892 | 36,2 | . 92146 | I 5,8 | . 07854 |
| . 204 | . 18090 | 52,0 | . 25929 | 36,3 | . 92162 | I 5,8 | . 07838 |
| 1.205 | 0.18142 | 52,0 | 0.25965 | 36,3 | 9.92178 | 15,7 | 0.07822 |
| . 206 | . 18194 | 52,0 | . 26001 | 36,3 | .92193 | 15,7 | . 07807 |
| . 207 | . 18246 | 52,0 | . 26037 | 36,3 | -92209 | 15,7 | .07791 |
| . 208 | . 18298 | 51,9 | . 26074 | 36,3 | . 92225 | I5,6 | . 07775 |
| . 209 | . 18350 | 51,9 | .261 10 | 36,3 | . 92240 | 15,6 | . 07760 |
| 1.210 | 0.18402 | 51,9 | 0.26146 | 36,3 | 9.92256 | 15,6 | 0.07744 |
| . 211 | . 18454 | 51,9 | . 26183 | 36,3 | . 9227 I | 15,5 | . 07729 |
| . 212 | . 18506 | 51,9 | . 26219 | 36,4 | . 92287 | 15,5 | . 07713 |
| . 213 | . 18558 | 51,9 | . 26255 | 36,4 | . 92302 | 15,5 | . 07698 |
| . 214 | . 18610 | 51,8 | . 26292 | 36,4 | . 92318 | I5,4 | . 07682 |
| 1.215 | 0.18662 | 5I,8 | 0.26328 | 36,4 | 9.92333 | 15,4 | 0.07667 |
| . 216 | . 18713 | 51,8 | . 26365 | 36,4 | . 92349 | 15,4 | .0765I |
| . 217 | . 18765 | 51,8 | . 26401 | 36,4 | . 92364 | I 5,4 | . 07636 |
| . 218 | . 18817 | 51,8 | . 26437 | 36,4 | . 92379 | I 5,3 | .07621 |
| . 219 | . 18869 | 5I,7 | . 26474 | 36,5 | . 92395 | I5,3 | . 07605 |
| 1.220 | 0.18920 | 51,7 | 0.26510 | 36,5 | 9.92410 | 15,3 | 0.07590 |
| . 22 I | . 18972 | 51,7 | . 26547 | 36,5 | . 92425 | 15,2 | . 07575 |
| . 222 | . 19024 | 51,7 | .26583 | 36,5 | . 92440 | I5,2 | . 07560 |
| . 223 | . 19075 | 51,7 | . 26620 | 36,5 | . 92456 | 15,2 | . 07544 |
| . 224 | . 19127 | 51,7 | . 26656 | 36,5 | . 9247 I | I5,I | . 07529 |
| I. 225 | 0. 19179 | 51,6 | 0.26693 | 36,5 | 9.92486 | 15,I | 0.07514 |
| . 226 | . 19230 | 51,6 | . 26729 | 36,5 | .92501 | I5, I | . 07499 |
| . 227 | . 19282 | 51,6 | . 26766 | 36,6 | . 92516 | 15,0 | . 07484 |
| . 228 | . 19334 | 51,6 | . 26802 | 36,6 | . 9253 I | I 5,0 | . 07469 |
| . 229 | . 19385 | 51,6 | . 26839 | 36,6 | . 92546 | I5,0 | . 07454 |
| 1.230 | 0. 19437 | 51,5 | 0.26876 | 36,6 | 9.92561 | 15,0 | 0.07439 |
| . 231 | . 19488 | 51,5 | . 26912 | 36,6 | . 92576 | 14,9 | . 07424 |
| . 232 | . 19540 | 51,5 | . 26949 | 36,6 | . 92591 | 14,9 | . 07409 |
| . 233 | . I9591 | 51,5 | . 26985 | 36,6 | . 92606 | 14,9 | . 07394 |
| . 234 | . I9643 | 51,5 | . 27022 | 36,6 | . 92621 | 14,8 | . 07379 |
| 1.235 | 0. 19694 | 51,5 | 0.27059 | 36,7 | 9.92635 | 14,8 | 0.07365 |
| . 236 | . 19746 | 51,4 | . 27095 | 36,7 | . 92650 | 14,8 | . 07350 |
| . 237 | . 19797 | 51,4 | .27132 | 36,7 | . 92665 | 14,7 | . 07335 |
| . 238 | . 19848 | 5I,4 | .27169 | 36,7 | . 92680 | 14,7 | . 07320 |
| . 239 | . 19900 | 51,4 | . 27205 | 36,7 | . 92694 | 14,7 | . 07306 |
| 1.240 | 0.19951 | 5I,4 | 0.27242 | 36,7 | 9.92709 | 14,7 | 0.07291 |
| .24I | . 20003 | 5I,4 | . 27279 | 36,7 | . 92724 | 14,6 | . 07276 |
| . 242 | . 20054 | 5I,3 | . 27316 | 36,7 | . 92738 | 14,6 | . 07262 |
| . 243 | . 20105 | 51,3 | . 27352 | 36,8 | . 92753 | 14,6 | . 07247 |
| . 244 | . 20157 | 51,3 | . 27389 | 36,8 | . 92767 | 14,5 | . 07233 |
| 1.245 | 0.20208 | 51,3 | 0.27426 | 36,8 | 9.92782 | 14,5 | 0.07218 |
| . 246 | . 20259 | 51,3 | . 27463 | 36,8 | . 92796 | 14,5 | . 07204 |
| . 247 | . 20310 | 51,2 | . 27499 | 36,8 | .928II | 14,4 | . 07189 |
| . 248 | . 20362 | 51,2 | .27536 | 36,8 | .92825 | 14,4 | .07175 |
| . 249 | . 20413 | 51,2 | . 27573 | 36,8 | . 92840 | 14,4 | . 07160 |
| 1.250 | 0.20464 | 5I,2 | 0.27610 | 36,8 | 9.92854 | 14,4 | 0.07146 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { c o s h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.250 | 0.20464 | 51,2 | 0.27610 | 36,8 | 9.92854 | 14,4 | 0.07146 |
| . 251 | . 20515 | 51,2 | . 27647 | 36,9 | . 92868 | 14,3 | . 07132 |
| . 252 | . 20566 | 51,2 | . 27684 | 36,9 | . 92883 | 14,3 | .07117 |
| . 253 | . 20618 | 51,I | . 2772 I | 36,9 | . 92897 | 14,3 | . 07103 |
| . 254 | . 20669 | 5I, I | . 27757 | 36,9 | .929II | 14,2 | . 07089 |
| I. 255 | 0.20720 | 51, I | 0.27794 | 36,9 | 9.92926 | 14,2 | 0.07074 |
| . 256 | . 20771 | 51,I | . 2783 I | 36,9 | . 92940 | I4,2 | . 07060 |
| . 257 | . 20822 | 51,1 | . 27868 | 36,9 | . 92954 | 14,2 | . 07046 |
| . 258 | . 20873 | 51, I | . 27905 | 36,9 | . 92968 | 14,I | . 07032 |
| . 259 | . 20924 | 51,0 | . 27942 | 36,9 | . 92982 | 14,I | .07018 |
| 1.260 | 0.20975 | 51,0 | 0.27979 | 37,0 | 9.92996 | 14,1 | 0.07004 |
| . 261 | . 21026 | 51,0 | . 28016 | 37,0 | . 93010 | 14,0 | . 06990 |
| . 262 | . 21077 | 51,0 | . 28053 | 37,0 | . 93024 | 14,0 | . 06976 |
| . 263 | . 21128 | 51,0 | . 28090 | 37,0 | . 93038 | 14,0 | .06962 |
| . 264 | .21179 | 51,0 | .28I27 | 37,0 | . 93052 | 14,0 | . 06948 |
| 1.265 | 0.21230 | 50,9 | 0.28164 | 37,0 | 9.93066 | 13,9 | 0.06934 |
| . 266 | . 21281 | 50,9 | . 28201 | 37,0 | . 93080 | 13,9 | . 06920 |
| . 267 | . 21332 | 50,9 | . 28238 | 37,0 | . 93094 | 13,9 | . 06906 |
| . 268 | . 21383 | 50,9 | . 28275 | 37, I | .93108 | I3,8 | . 06892 |
| . 269 | . 21434 | 50,9 | . 28312 | 37, I | .93122 | 13,8 | . 06878 |
| 1.270 | 0.21485 | 50,9 | 0.28349 | 37, I | 9.93135 | 13,8 | 0.06865 |
| . 271 | . 21536 | 50,9 | . 28386 | 37, 1 | .93149 | 13,8 | . 0685 I |
| . 272 | . 21586 | 50,8 | . 28423 | 37, I | .93163 | 13,7 | . 06837 |
| . 273 | . 21637 | 50,8 | . 28460 | 37,1 | . 93177 | 13,7 | . 06823 |
| . 274 | . 21688 | 50,8 | . 28498 | 37, I | .93190 | 13,7 | .06810 |
| 1.275 | 0.21739 | 50,8 | 0.28535 | 37, I | 9.93204 | 13,6 | 0.06796 |
| . 276 | . 21790 | 50,8 | . 28572 | 37,2 | . 93218 | 13,6 | . 06782 |
| . 277 | . 21840 | 50,8 | . 28609 | 37,2 | .9323I | 13,6 | . 06769 |
| . 278 | . 21891 | 50,7 | . 28646 | 37,2 | -93245 | 13,6 | . 06755 |
| . 279 | . 21942 | 50,7 | . 28683 | 37,2 | . 93258 | 13,5 | . 06742 |
| 1.280 | 0.21993 | 50,7 | 0.28721 | 37,2 | 9.93272 | 13,5 | 0.06728 |
| . 281 | . 22043 | 50,7 | . 28758 | 37,2 | . 93285 | I3,5 | . 06715 |
| . 282 | . 22094 | 50,7 | . 28795 | 37,2 | . 93299 | I 3,5 | . 06701 |
| . 283 | . 22145 | 50,7 | . 28832 | 37,2 | . 93312 | I3,4 | . 06688 |
| . 284 | . 22195 | 50,6 | . 28869 | 37,2 | . 93326 | I3,4 | . 06674 |
| 1.285 | 0.22246 | 50,6 | 0.28907 | 37,3 | 9.93339 | 13,4 | 0.06661 |
| . 286 | . 22296 | 50,6 | . 28944 | 37,3 | . 93353 | 13,3 | . 06647 |
| . 287 | . 22347 | 50,6 | . 28981 | 37,3 | . 93366 | I3,3 | . 06634 |
| . 288 | . 22398 | 50,6 | . 29018 | 37,3 | -93379 | 13,3 | . 06621 |
| . 289 | . 22448 | 50,6 | . 29056 | 37,3 | -93392 | 13,3 | . 06608 |
| 1.290 | 0.22499 | 50,6 | 0.29093 | 37,3 | 9.93406 | 13,2 | 0.06594 |
| . 291 | . 22549 | 50,5 | . 29130 | 37,3 | . 93419 | 13,2 | . 0658 I |
| . 292 | . 22600 | 50,5 | . 29168 | 37,3 | . 93432 | I3,2 | . 06568 |
| . 293 | . 22650 | 50,5 | . 29205 | 37,3 | . 93445 | I3,2 | . 06555 |
| . 294 | .22701 | 50,5 | . 29242 | 37,4 | -93458 | I3, I | . 06542 |
| I. 295 | 0.22751 | 50,5 | 0.29280 | 37,4 | 9.93472 | I3, I | 0.06528 |
| . 296 | . 22802 | 50,5 | . 29317 | 37,4 | . 93485 | I3, I | . 06515 |
| . 297 | . 22852 | 50,4 | . 29355 | 37,4 | . 93498 | I3,1 | . 06502 |
| . 298 | . 22903 | 50,4 | . 29392 | 37,4 | .935II | 13,0 | . 06489 |
| . 299 | . 22953 | 50,4 | . 29429 | 37,4 | . 93524 | 13,0 | . 06476 |
| 1.300 | 0.23004 | 50,4 | 0.29467 | 37,4 | 9.93537 | 13,0 | 0.06463 |
| U | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec g d u$ | - $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{~d} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.300 | 0.23004 | 50,4 | 0.29467 | 37,4 | 9.93537 | 13,0 | 0.06463 |
| . 301 | . 23054 | 50,4 | . 29504 | 37,4 | . 93550 | I2,9 | . 06450 |
| . 302 | .23104 | 50,4 | . 29542 | 37,4 | . 93563 | 12,9 | . 06437 |
| . 303 | .23155 | 50,4 | . 29579 | 37,5 | . 93576 | 12,9 | . 06424 |
| . 304 | . 23205 | 50,3 | . 29617 | 37,5 | . 93588 | 12,9 | . 06412 |
| I. 305 | 0.23255 | 50,3 | 0.29654 | 37,5 | 9.93601 | 12,8 | 0.06399 |
| . 306 | . 23306 | 50,3 | . 29692 | 37,5 | .936I4 | 12,8 | . 06386 |
| . 307 | . 23356 | 50,3 | . 29729 | 37,5 | . 93627 | 12,8 | . 06373 |
| . 308 | . 23406 | 50,3 | . 29767 | 37,5 | . 93640 | 12,8 | . 06360 |
| . 309 | . 23457 | 50,3 | . 29804 | 37,5 | . 93652 | 12,7 | . 06348 |
| 1.310 | 0.23507 | 50,2 | 0.29842 | 37,5 | 9.93665 | 12,7 | 0.06335 |
| .311 | . 23557 | 50,2 | .29879 | 37,5 | . 93678 | 12,7 | . 06322 |
| . 312 | . 23607 | 50,2 | . 29917 | 37,6 | . 93691 | 12,7 | . 06309 |
| . 313 | . 23657 | 50,2 | . 29954 | 37,6 | . 93703 | 12,6 | . 06297 |
| .314 | . 23708 | 50,2 | . 29992 | 37,6 | .93716 | 12,6 | . 06284 |
| I.3I5 | 0.23758 | 50,2 | 0.30029 | 3\%,6 | 9.93728 | 12,6 | 0.06272 |
| . 316 | . 23808 | 50,2 | . 30067 | 37,6 | .9374I | 12,6 | . 06259 |
| -317 | . 23858 | 50, I | - 30105 | 37,6 | -93754 | 12,5 | . 06246 |
| . 318 | . 23908 | 50, I | . 30142 | 37,6 | . 93766 | 12,5 | . 06234 |
| . 319 | . 23958 | 50, I | . 30180 | 37,6 | . 93779 | 12,5 | . 06221 |
| 1.320 | 0.24009 | 50, I | 0.30217 | 37,6 | 9.93791 | 12,5 | 0.06209 |
| .32I | . 24059 | 50, I | . 30255 | 37,7 | . 93804 | 12,4 | . 06196 |
| . 322 | . 24109 | 50, I | - 30293 | 37,7 | .93816 | 12,4 | . 06184 |
| . 323 | . 24159 | 50, I | - 30330 | 37,7 | .93828 | 12,4 | .06I72 |
| . 324 | . 24209 | 50,0 | . 30368 | 37,7 | .9384I | 12,4 | .06I 59 |
| 1.325 | 0.24259 | 50,0 | 0.30406 | 37,7 | 9.93853 | 12,3 | 0.06147 |
| . 326 | . 24309 | 50,0 | . 30444 | 37,7 | . 93865 | 12,3 | . 06135 |
| . 327 | . 24359 | 50,0 | -3048I | 37,7 | . 93878 | 12,3 | . 06122 |
| . 328 | . 24409 | 50,0 | . 30519 | 37,7 | . 93890 | 12,3 | .06I 10 |
| . 329 | . 24459 | 50,0 | - 30557 | 37,7 | . 93902 | 12,2 | . 06098 |
| I. 330 | 0.24509 | 50,0 | 0.30594 | 37,8 | 9.93914 | 12,2 | 0.06086 |
| .33I | . 24559 | 49,9 | . 30632 | 37,8 | . 93927 | 12,2 | . 06073 |
| . 332 | . 24609 | 49,9 | . 30670 | 37,8 | . 93939 | 12,2 | . 0606 I |
| . 333 | . 24659 | 49,9 | -30708 | 37,8 | .9395I | I2,I | . 06049 |
| . 334 | . 24709 | 49,9 | . 30746 | 37,8 | . 93963 | I2, I | . 06037 |
| I. 335 | 0.24759 | 49,9 | 0.30783 | 37,8 | 9.93975 | 12, I | 0.06025 |
| . 336 | . 24808 | 49,9 | . 3082 I | 37,8 | . 93987 | 12,I | . 06013 |
| . 337 | . 24858 | 49,9 | . 30859 | 37,8 | . 93999 | 12,0 | . 06001 |
| . 338 | . 24908 | 49,9 | . 30897 | 37,8 | .940I I | 12,0 | . 05989 |
| . 339 | . 24958 | 49,8 | . 30935 | 37,8 | . 04023 | 12,0 | . 05977 |
| 1.340 | 0.25008 | 49,8 | 0.30972 | 37,9 | 9.94035 | 12,0 | 0.05965 |
| . 34 I | . 25058 | 49,8 | -31010 | 37,9 | . 94047 | II,9 | . 05953 |
| . 342 | .25107 | 49,8 | -31048 | 37,9 | . 94059 | I I,9 | . 05941 |
| . 343 | . 25157 | 49,8 | -31086 | 37,9 | . 94071 | I I,9 | . 05929 |
| . 344 | . 25207 | 49,8 | -31124 | 37,9 | -94083 | I I,9 | . 05917 |
| I. 345 | 0.25257 | 49,8 | 0.31162 | 37,9 | 9.94095 | I 1,8 | 0.05905 |
| . 346 | . 25306 | 49,7 | . 31200 | 37,9 | .94107 | I I, 8 | . 05893 |
| . 347 | . 25356 | 49,7 | -31238 | 37,9 | .94119 | II,8 | .0588I |
| - 348 | . 25406 | 49,7 | . 31276 | 37,9 | .94130 | II,8 | .05870 |
| - 349 | . 25456 | 49,7 | -31314 | 37,9 | . 94142 | I I,8 | . 05858 |
| 1. 350 | 0.25505 | 49,7 | 0.31352 | 38,0 | 9.94154 | 11,7 | 0.05846 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ * | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I . 350 | 0.25505 | 49,7 | 0.31352 | 38,0 | 9.94154 | II,7 | 0.05846 |
| . 351 | . 25555 | 49,7 | . 31390 | 38,0 | .94166 | II,7 | . 05834 |
| . 352 | . 25605 | 49,7 | . 31428 | 38,0 | .94177 | II,7 | . 05823 |
| . 353 | . 25654 | 49,6 | . 31465 | 38,0 | .94189 | II,7 | .058II |
| . 354 | . 25704 | 49,6 | . 31503 | 38,0 | .9420I | II,6 | . 05799 |
| 1. 355 | 0.25754 | 49,6 | 0.31541 | 38,0 | 9.94212 | I 1,6 | 0.05788 |
| . 356 | . 25803 | 49,6 | -31580 | 38,0 | . 94224 | II,6 | . 05776 |
| . 357 | . 25853 | 49,6 | . 31618 | 38,0 | . 94235 | I I, 6 | . 05765 |
| . 358 | . 25902 | 49,6 | . 31656 | 38,0 | . 94247 | I I,5 | . 05753 |
| . 359 | . 25952 | 49,6 | . 31694 | 38,1 | . 94258 | II,5 | . 05742 |
| 1.360 | 0.26002 | 49,6 | 0.31732 | 38, 1 | 9.94270 | II,5 | 0.05730 |
| . 361 | . 26051 | 49,5 | . 31770 | 38, | .94281 | II,5 | . 05719 |
| . 362 | .26101 | 49,5 | . 31808 | 38, 1 | . 94293 | II,4 | . 05707 |
| .363 | . 26150 | 49,5 | . 31846 | 38, I | . 94304 | II,4 | . 05696 |
| . 364 | . 26200 | 49,5 | . 31884 | 38, 1 | .94316 | II, 4 | . 05684 |
| 1.365 | 0.26249 | 49,5 | 0.31922 | 38, I | 9.94327 | II,4 | 0.05673 |
| . 366 | . 26299 | 49,5 | . 31960 | 38, I | . 94338 | II,4 | . 05662 |
| . 367 | . 26348 | 49,5 | . 31998 | 38,1 | . 94350 | II,3 | . 05650 |
| . 368 | . 26398 | 49,5 | . 32036 | 38, 1 | .9436I | II,3 | . 05639 |
| .369 | . 26447 | 49,4 | . 32075 | 38,2 | . 94372 | II,3 | . 05628 |
| 1.370 | 0.26496 | 49,4 | 0.32 II 3 | 38,2 | 9.94384 | I I, 3 | 0.05616 |
| . 371 | . 26546 | 49,4 | .3215I | 38,2 | . 94395 | II, 2 | . 05605 |
| . 372 | . 26595 | 49,4 | -32189 | 38,2 | . 94406 | II,2 | . 05594 |
| . 373 | + . 26645 | 49,4 | - 32227 | 38,2 | . 94417 | II, 2 | . 05583 |
| . 374 | . 26694 | 49,4 | . 32266 | 38,2 | . 94429 | I I, 2 | . 05571 |
| 1.375 | 0.26743 | 49,4 | 0.32304 | 38,2 | 9.94440 | I 1,2 | 0.05560 |
| . 376 | . 26793 | 49,3 | - 32342 | 38,2 | .9445I | II, I | . 05549 |
| . 377 | . 26842 | 49,3 | . 32380 | 38,2 | . 94462 | II, I | . 05538 |
| . 378 | . 26891 | 49,3 | . 32418 | 38,2 | . 94473 | II, I | . 05527 |
| . 379 | . 26941 | 49,3 | . 32457 | 38,2 | . 94484 | II, I | .05516 |
| I. 380 | 0.26990 | 49,3 | 0.32495 | 38,3 | 9.94495 | I I, 0 | 0.05505 |
| .381 | . 27039 | 49,3 | . 32533 | 38,3 | . 94506 | I I, O | . 05494 |
| - 382 | . 27089 | 49,3 | . 32571 | 38,3 | . 94517 | II,O | . 05483 |
| . 383 | . 27138 | 49,3 | . 32610 | 38,3 | . 94528 | II,O | . 05472 |
| . 384 | . 27187 | 49,2 | . 32648 | 38,3 | . 94539 | I I,O | .0546I |
| 1. 385 | 0.27236 | 49,2 | 0.32686 | 38,3 | 9.94550 | 10,9 | 0.05450 |
| . 386 | . 27286 | 49,2 | . 32725 | 38,3 | .9456I | 10,9 | . 05439 |
| . 387 | . 27335 | 49,2 | . 32763 | 38,3 | . 94572 | 10,9 | . 05428 |
| . 388 | . 27384 | 49,2 | . 32801 | 38,3 | . 94583 | 10,9 | .05417 |
| . 389 | .27433 | 49,2 | . 32840 | 38,3 | . 94594 | 10,8 | . 05406 |
| I. 390 | 0.27482 | 49,2 | 0.32878 | 38,4 | 9.94604 | 10,8 | 0.05396 |
| .391 | . 27532 | 49,2 | . 32916 | 38,4 | .946I5 | 10,8 | . 05385 |
| . 392 | .2758I | 49,2 | . 32955 | 38,4 | . 94626 | 10,8 | . 05374 |
| . 393 | . 27630 | 49, I | - 32993 | 38,4 | . 94637 | 10,8 | . 05363 |
| - 394 | . 27679 | 49, I | . 33031 | 38,4 | . 94648 | 10,7 | . 05352 |
| 1. 395 | 0.27728 | 49, I | 0.33070 | 38,4 | 9.94658 | 10,7 | 0.05342 |
| . 396 | . 27777 | 49, I | . 33108 | 38,4 | . 94669 | 10,7 | . 0533 I |
| . 397 | . 27826 | 49, I | .33147 | 38,4 | . 94680 | 10,7 | . 05320 |
| . 398 | . 27875 | 49, I | . 33185 | 38,4 | . 94690 | 10,6 | .05310 |
| . 399 | . 27925 | 49, I | . 33224 | 38,4 | .9470I | 10,6 | . 05299 |
| 1.400 | 0.27974 | 49, I | 0.33262 | 38,5 | 9.94712 | 10,6 | 0.05288 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log tanh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log eoth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.400 | 0.27974 | 49, I | 0.33262 | 38,5 | 9.94712 | 10,6 | 0.05288 |
| . 401 | . 28023 | 49,0 | . 33300 | 38,5 | . 94722 | 10,6 | . 05278 |
| . 402 | . 28072 | 49,0 | - 33339 | 38,5 | . 94733 | 10,6 | . 05267 |
| . 403 | . 28121 | 49,0 | - 33377 | 38,5 | . 94743 | 10,5 | . 05257 |
| . 404 | .28170 | 49,0 | -33416 | 38,5 | . 94754 | 10,5 | . 05246 |
| 1. 405 | 0.28219 | 49,0 | 0. 33454 | 38,5 | 9.94764 | 10,5 | 0.05236 |
| . 406 | . 28268 | 49,0 | . 33493 | 38,5 | . 94775 | 10,5 | . 05225 |
| . 407 | . 28317 | 49,0 | - 33531 | 38,5 | . 94785 | 10,5 | . 05215 |
| . 408 | . 28366 | 49,0 | - 33570 | 38,5 | . 94796 | 10,4 | . 05204 |
| . 409 | . 28415 | 48,9 | - 33608 | 38,5 | . 94806 | 10,4 | . 05194 |
| 1.410 | 0.28464 | 48,9 | 0.33647 | 38,5 | 9.94817 | 10,4 | 0.05183 |
| . 411 | . 28512 | 48,9 | . 33686 | 38,6 | . 94827 | 10,4 | . 05173 |
| . 412 | . 28561 | 48,9 | . 33724 | 38,6 | . 94837 | 10,3 | . 05153 |
| . 413 | . 28610 | 48,9 | . 33763 | 38,6 | . 94848 | 10,3 | .05152 |
| . 414 | . 28659 | 48,9 | . 33801 | 38,6 | . 94858 | 10,3 | . 05142 |
| 1.415 | 0. 28708 | 48,9 | 0. 33840 | 38,6 | 9.94868 | 10,3 | 0.05132 |
| . 416 | . 28757 | 48,9 | . 33878 | 38,6 | . 94879 | 10,3 | . 05121 |
| .417 | . 28806 | 48,9 | - 33917 | 38,6 | . 94889 | 10,2 | . 05111 |
| .418 | . 28855 | 48,8 | 33956 | 38,6 | . 94899 | 10,2 | .05101 |
| .419 | . 28903 | 48,8 | - 33994 | 38,6 | . 94909 | 10,2 | .05091 |
| 1.420 | 0. 28952 | 48,8 | 0.34033 | 38,6 | 9.94919 | 10,2 | 0.05081 |
| . 421 | .29001 | 48,8 | . 34071 | 38,6 | . 94930 | 10,2 | . 05070 |
| . 422 | . 29050 | 48,8 | . 34110 | 38,7 | . 94940 | 10,1 | . 05060 |
| . 423 | . 29099 | 48,8 | -34149 | 38,7 | . 94950 | 10, 1 | . 05050 |
| . 424 | . 29147 | 48,8 | . 34187 | 38,7 | . 94960 | IO,I | . 05040 |
| 1. 425 | 0.29196 | 48,8 | 0.34226 | 38,7 | 9.94970 | 10,1 | 0.05030 |
| . 426 | . 29245 | 48,8 | - 34265 | 38,7 | . 94980 | 10,1 | . 05020 |
| . 427 | . 29294 | 48,7 | - 34304 | 38,7 | . 94990 | 10,0, | . 05010 |
| . 428 | . 29342 | 48,7 | - 34342 | 38,7 | . 95000 | 10,0 | . 05000 |
| . 429 | . 29391 | 48,7 | -3438I | 38,7 | .95010 | 10,0 | . 04990 |
| 1. 430 | 0.29440 | 48,7 | 0. 34420 | 38,7 | 9.95020 | 10,0 | 0.04980 |
| .43I | . 29489 | 48,7 | - 34458 | 38,7 | . 95030 | 10,0 | . 04970 |
| . 432 | . 29537 | 48,7 | - 34497 | 38,7 | . 95040 | 9,9 | . 04960 |
| . 433 | . 29586 | 48,7 | - 34536 | 38,8 | . 95050 | 9,9 | . 04950 |
| -434 | . 29635 | 48,7 | - 34575 | 38,8 | . 95060 | 9,9 | . 04940 |
| 1. 435 | 0.29683 | 48,7 | 0.34613 |  | 9.95070 | 9,9 | 0.04930 |
| . 436 | . 29732 | 48,6 | . 34652 | 38,8 | . 95080 | 9,9 | . 04920 |
| . 437 | . 29781 | 48,6 | . 34691 | 38,8 | . 95090 | 9,8 | . 04910 |
| . 438 | . 29829 | 48,6 | - 34730 | 38,8 | . 95099 | 9,8 | . 04901 |
| . 439 | . 29878 | 48,6 | - 34769 | 38,8 | .95109 | 9,8 | .04891 |
| 1. 440 | 0.29926 | 48,6 | 0.34807 | 38,8 | 9.95119 | 9,8 | 0.0488I |
| .44I | . 29975 | 48,6 | . 34846 | 38,8 | .95129 | 9,8 | .04871 |
| . 442 | . 30024 | 48,6 | - 34885 | 38,8 | . 95139 | 9,7 | . 04861 |
| -443 | -30072 | 48,6 | - 34924 | 38,8 | . 95148 | 9,7 | . 04852 |
| . 444 | .30121 | 48,6 | - 34963 | 38,8 | . 95158 | 9,7 | . 04842 |
| 1. 445 | 0.30169 | 48,5 | 0.35002 | 38,9 | 9.95168 | 9,7 | 0.04832 |
| . 446 | . 30218 | 48,5 | . 35040 | 38,9 | . 95177 | 9,7 | . 04823 |
| . 447 | -30266 | 48,5 | - 35079 | 38,9 | . 95187 | 9,6 | .04813 |
| . 448 | . 30315 | 48,5 | -35118 | 38,9 | . 95197 | 9,6 | . 04803 |
| . 449 | -30363 | 48,5 | -35157 | 38,9 | . 95206 | 9,6 | . 04794 |
| 1.450 | 0.30412 | 48,5 | 0.35196 | 38,9 | 9.95216 | 9,6 | 0.04784 |
| u | $\log \tan$ gd u | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | log sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | log csc gd u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.450 | 0.30412 | 48,5 | 0.35196 | 38,9 | 9.95216 | 9,6 | 0.04784 |
| .45I | . 30460 | 48,5 | . 35235 | 38,9 | . 95225 | 9,6 | . 04775 |
| . 452 | . 30509 | 48,5 | . 35274 | 38,9 | . 95235 | 9,5 | . 04765 |
| . 453 | . 30557 | 48,5 | . 35313 | 38,9 | . 95245 | 9,5 | . 04755 |
| . 454 | . 30606 | 48,4 | . 35352 | 38,9 | . 95254 | 9,5 | . 04746 |
| I. 455 | 0.30654 | 48,4 | 0.3539 I | 38,9 | 9.95264 | 9,5 | 0.04736 |
| . 456 | . 30703 | 48,4 | . 35429 | 39,0 | . 95273 | 9,5 | . 04727 |
| . 457 | . 30751 | 48,4 | . 35468 | 39,0 | . 95283 | 9,5 | . 04717 |
| . 458 | . 30799 | 48,4 | . 35507 | 39,0 | . 95292 | 9,4 | . 04708 |
| . 459 | . 30848 | 48,4 | . 35546 | 39,0 | .9530I | 9,4 | . 04699 |
| 1.460 | 0.30896 | 48,4 | 0.35585 | 39,0 | 9.953 II | 9,4 | 0.04689 |
| .461 | . 30945 | 48,4 | . 35624 | 39,0 | . 95320 | 9,4 | . 04680 |
| . 462 | . 30993 | 48,4 | . 35663 | 39,0 | . 95330 | 9,4 | . 04670 |
| .463 | .3104I | 48,3 | . 35702 | 39,0 | . 95339 | 9,3 | . 04661 |
| . 464 | . 31090 | 48,3 | . 35741 | 39,0 | . 95348 | 9,3 | . 04652 |
| 1.465 | 0.31138 | 48,3 | 0.35780 | 39,0 | 9.95358 | 9,3 | 0.04642 |
| . 466 | . 31186 | 48,3 | .35819 | 39,0 | . 95367 | 9,3 | . 04633 |
| . 467 | . 31235 | 48,3 | . 35858 | 39,0 | . 95376 | 9,3 | . 04624 |
| . 468 | -31283 | 48,3 | . 35897 | 39, I | . 95385 | 9,2 | .046I5 |
| .469 | .3133I | 48,3 | . 35937 | 39, I | . 95395 | 9,2 | .04605 |
| 1.470 | 0.31379 | 48,3 | 0.35976 | 39,1 | 9.95404 | 9,2 | 0.04596 |
| . 471 | . 31428 | 48,3 | .36015 | 39,1 | . 95413 | 9,2 | . 04587 |
| . 472 | . 31476 | 48,3 | . 36054 | 39, I | . 95422 | 9,2 | . 04578 |
| . 473 | . 31524 | 48,2 | . 36093 | 39, I | .9543I | 9,2 | . 04569 |
| . 474 | .31572 | 48,2 | . 36132 | 39, I | .9544I | 9,1 | . 04559 |
| 1.475 | 0.31621 | 48,2 | 0.36171 | 39,1 | 9.95450 | 9,I | 0.04550 |
| . 476 | . 31669 | 48,2 | .36210 | 39, I | . 95459 | 9,I | . 04541 |
| . 477 | . 31717 | 48,2 | - 36249 | 39, I | . 95468 | 9, I | . 04532 |
| . 478 | .31765 | 48,2 | - 36288 | 39, I | . 95477 | 9,1 | . 04523 |
| . 479 | .318I4 | 48,2 | . 36328 | 39, I | . 95486 | 9,0 | .045I4 |
| 1.480 | 0.31862 | 48,2 | 0.36367 | 39,2 | 9.95495 | 9,0 | 0.04505 |
| .48I | . 31910 | 48,2 | . 36406 | 39,2 | . 95504 | 9,0 | . 04496 |
| . 482 | . 31958 | 48,2 | . 36445 | 39,2 | .95513 | 9,0 | . 04487 |
| . 483 | . 32006 | 48, I | . 36484 | 39,2 | . 95522 | 9,0 | . 04478 |
| . 484 | . 32054 | 48, I | . 36523 | 39,2 | .9553 I | 9,0 | . 04469 |
| 1.485 | 0.32102 | 48, 1 | 0.36563 | 39,2 | . 95540 | 8,9 | . 04460 |
| . 486 | .32151 | 48, I | . 36602 | 39,2 | . 95549 | 8,9 | . 04451 |
| . 487 | . 32199 | 48, I | . 36641 | 39,2 | . 95558 | 8,9 | . 04442 |
| . 488 | . 32247 | 48, I | . 36680 | 39,2 | . 95567 | 8,9 | . 04433 |
| .489 | . 32295 | 48,1 | .36719 | 39,2 | . 95576 | 8,9 | . 04424 |
| 1. 490 | 0.32343 | 48, 1 | 0.36759 | 39,2 | 9.95584 | 8,8 | 0.04416 |
| . 491 | . 32391 | 48, I | . 36798 | 39,2 | . 95593 | 8,8 | . 04407 |
| . 492 | . 32439 | 48, 1 | . 36837 | 39,2 | . 95602 | 8,8 | . 04398 |
| . 493 | . 32487 | 48,0 | . 36876 | 39,3 | .956II | 8,8 | . 04389 |
| . 494 | . 32535 | 48,0 | . 36916 | 39,3 | . 95620 | 8,8 | . 04380 |
| 1. 495 | 0.32583 | 48,0 | 0.36955 | 39,3 | 9.95628 | 8,8 | 0.04372 |
| . 496 | . 32631 | 48,0 | . 36994 | 39,3 | . 95637 | 8,7 | . 04363 |
| . 497 | . 32679 | 48,0 | . 37033 | 39,3 | . 95646 | 8,7 | . 04354 |
| . 498 | . 32727 | 48,0 | . 37073 | 39,3 | . 95655 | 8,7 | . 04345 |
| . 499 | . 32775 | 48,0 | -37112 | 39,3 | . 95663 | 8,7 | . 04337 |
| 1.500 | 0.32823 | 48,0 | 0.37151 | 39,3 | 9.95672 | 8,7 | 0.04328 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| U | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{t a n h} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g}$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.500 | 0.32823 | 48,0 | 0.37151 | 39,3 | 9.95672 | 8,7 | 0.04328 |
| . 501 | . 32871 | 48,0 | . 37191 | 39,3 | .95681 | 8,7 | .04319 |
| . 502 | . 32919 | 48,0 | - 37230 | 39,3 | . 95689 | 8,6 | .043II |
| . 503 | . 32967 | 48,0 | . 37269 | 39,3 | . 95698 | 8,6 | . 04302 |
| . 504 | . 33015 | 47,9 | . 37309 | 39,3 | . 95707 | 8,6 | . 04293 |
| 1.505 | 0.33063 | 47,9 | 0.37348 | 39,3 | 9.95715 | 8,6 | 0.04285 |
| . 506 | .33III | 47,9 | . 37387 | 39,4 | . 95724 | 8,6 | . 04276 |
| . 507 | -33159 | 47,9 | . 37427 | 39,4 | . 95732 | 8,5 | . 04268 |
| . 508 | . 33207 | 47,9 | . 37466 | 39,4 | .9574I | 8,5 | . 04259 |
| . 509 | - 33255 | 47,9 | . 37505 | 39,4 | . 95749 | 8,5 | . 04251 |
| 1.510 | 0.33303 | 47,9 | 0.37545 | 39,4 | 9.95758 | 8,5 | 0.04242 |
| . 511 | . 33350 | 47,9 | - 37584 | 39,4 | . 95766 | 8,5 | . 04234 |
| . 512 | . 33398 | 47,9 | . 37624 | 39,4 | . 95775 | 8,5 | . 04225 |
| . 513 | . 33446 | 47,9 | . 37663 | 39,4 | . 95783 | 8,4 | . 04217 |
| . 514 | -33494 | 47,8 | . 37702 | 39,4 | . 95792 | 8,4 | . 04208 |
| 1.515 | 0.33542 | 47,8 | 0.37742 | 39,4 | 9.95800 | 8,4 | 0.04200 |
| . 516 | . 33590 | 47,8 | .3778I | 39,4 | .95808 | 8,4 | .04192 |
| . 517 | . 33638 | 47,8 | . 3782 I | 39,4 | .95817 | 8,4 | . 04183 |
| . 518 | . 33685 | 47,8 | -37860 | 39,4 | . 95825 | 8,4 | . 04175 |
| . 519 | . 33733 | 47,8 | . 37900 | 39,5 | . 95834 | 8,3 | . 04166 |
| I. 520 | 0.33781 | 47,8 | 0.37939 | 39,5 | 9.95842 | 8,3 | 0.04158 |
| . 521 | . 33829 | 47,8 | . 37979 | 39,5 | . 95850 | 8,3 | . 04150 |
| . 522 | . 33877 | 47,8 | . 38018 | 39,5 | . 95859 | 8,3 | .04I41 |
| . 523 | . 33924 | 47,8 | . 38057 | 39,5 | . 95867 | 8,3 | .04133 |
| . 524 | . 33972 | 47,8 | . 38097 | 39,5 | . 95875 | 8,3 | .04125 |
| I. 525 | 0.34020 | 47,7 | 0.38136 | 39,5 | 9.95883 | 8,2 | 0.04117 |
| . 526 | . 34068 | 47,7 | .38176 | 39,5 | . 95892 | 8,2 | .04108 |
| . 527 | -34II5 | 47,7 | . 38215 | 39,5 | . 95900 | 8,2 | . 04100 |
| . 528 | . 34163 | 47,7 | -3825, | 39,5 | . 95908 | 8,2 | . 04092 |
| . 529 | -342II | 47,7 | . 38295 | 39,5 | . 95916 | 8,2 | . 04084 |
| 1.530 | 0.34258 | 47,7 | 0.38334 | 39,5 | 9.95924 | 8,2 | 0.04076 |
| . 531 | . 34306 | 47,7 | . 38374 | 39,5 | . 95933 | 8,I | . 04067 |
| . 532 | - 34354 | 47,7 | -38413 | 39,6 | . 95941 | 8,1 | . 04059 |
| . 533 | . 34402 | 47,7 | . 38453 | 39,6 | . 95949 | 8,I | . 04051 |
| . 534 | - 34449 | 47,7 | -38492 | 39,6 | . 95957 | 8,1 | . 04043 |
| 1.535 | 0.34497 | 47,7 | 0.38532 | 39,6 | 9.95965 | 8, 1 | 0.04035 |
| . 536 | - 34545 | 47,6 | . 38571 | 39,6 | . 95973 | 8, I | . 04027 |
| . 537 | . 34592 | 47,6 | . 386 II | 39,6 | .95981 | 8,0 | . 04019 |
| - 538 | - 34640 | 47,6 | . 38651 | 39,6 | . 95989 | 8,0 | . 0401 I |
| . 539 | . 34687 | 47,6 | . 38690 | 39,6 | . 95997 | 8,0 | . 04003 |
| 1.540 | 0.34735 | 47,6 | 0.38730 | 39,6 | 9.96005 | 8,0 | 0.03995 |
| . 541 | . 34783 | 47,6 | . 38769 | 39,6 | .96013 | 8,0 | . 03987 |
| . 542 | . 34830 | 47,6 | . 38809 | 39,6 | .96021 | 8,0 | . 03979 |
| . 543 | . 34878 | 47,6 | - 38849 | 39,6 | . 96029 | 8,0 | . 03971 |
| . 544 | . 34925 | 47,6 | . 38888 | 39,6 | . 96037 | 7,9 | . 03963 |
| 1.545 | 0.34973 | 47,6 | 0.38928 | 39,6 | 9.96045 | 7,9 | 0.03955 |
| . 546 | -3502I | 47,6 | . 38968 | 39,7 | . 96053 | 7,9 | . 03947 |
| . 547 | . 35068 | 47,6 | - 39007 | 39,7 | .9606I | 7,9 | . 03939 |
| - 548 | -35116 | 47,5 | - 39047 | 39,7 | . 96069 | 7,9 | . 03931 |
| . 549 | .35163 | 47,5 | - 39087 | 39,7 | . 96077 | 7,9 | . 03923 |
| 1.550 | 0.35211 | 47,5 | 0.39126 | 39,7 | 9.96084 | 7,8 | 0.03916 |
| u | $\boldsymbol{l o g} \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 550 | 0.35211 | 47,5 | 0.39126 | 39,7 | 9.96084 | 7,8 | 0.03916 |
| . 551 | . 35258 | 47,5 | . 39166 | 39,7 | . 96092 | 7,8 | . 03908 |
| . 552 | -35306 | 47,5 | . 39206 | 39,7 | .96100 | 7,8 | . 03900 |
| . 553 | . 35353 | 47,5 | . 39245 | 39,7 | .96108 | 7,8 | . 03892 |
| . 554 | -3540I | 47,5 | - 39285 | 39,7 | .961 16 | 7,8 | . 03884 |
| I. 555 | 0.35448 | 47,5 | 0.39325 | 39,7 | 9.96123 | 7,8 | 0.03877 |
| . 556 | . 35496 | 47,5 | - 39365 | 39,7 | .96I3I | 7,7 | . 03869 |
| . 557 | - 35543 | 47,5 | - 39404 | 39,7 | -.96I39 | 7,7 | . 03861 |
| . 558 | .3559I | 47,5 | . 39444 | 39,7 | .96147 | 7,7 | . 03853 |
| . 559 | . 35638 | 47,5 | . 39484 | 39,7 | . 96154 | 7,7 | . 03846 |
| I. 560 | 0.35686 | 47,4 | 0.39524 | 39,8 | 9.96162 | 7,7 | 0.03838 |
| . 561 | . 35733 | 47,4 | . 39563 | 39,8 | .96I70 | 7,7 | . 03830 |
| . 562 | 35780 | 47,4 | . 39603 | 39,8 | .96I77 | 7,7 | . 03823 |
| . 563 | 35828 | 47,4 | . 39643 | 39,8 | . 96185 | 7,6 | .03815 |
| . 564 | . 35875 | 47,4 | - 39683 | 39,8 | .96I93 | 7,6 | . 03807 |
| 1.565 | 0.35923 | 47,4 | 0.39722 | 39,8 | 9.96200 | 7,6 | 0.03800 |
| . 566 | . 35970 | 47,4 | . 39762 | 39,8 | . 96208 | 7,6 | . 03792 |
| . 567 | . 36017 | 47,4 | . 39802 | 39,8 | .962 5 | 7,6 | . 03785 |
| . 568 | . 36065 | 47,4 | . 39842 | 39,8 | . 96223 | 7,6 | . 03777 |
| . 569 | .36112 | 47,4 | . 39882 | 39,8 | .9623I | 7,5 | . 03769 |
| I. 570 | 0.36160 | 47,4 | 0.39921 | 39,8 | 9.96238 | 7,5 | 0.03762 |
| . 571 | . 36207 | 47,4 | . 39961 | 39,8 | . 96246 | 7,5 | . 03754 |
| . 572 | . 36254 | 47,3 | . 4000 I | 39,8 | . 96253 | 7,5 | . 03747 |
| . 573 | . 36302 | 47,3 | . 40041 | 39,8 | .96261 | 7,5 | . 03739 |
| . 574 | . 36349 | 47,3 | .4008I | 39,9 | .96268 | 7,5 | . 03732 |
| 1.575 | 0.36396 | 47,3 | 0.40121 | 39,9 | 9.96276 | 7,5 | 0.03724 |
| . 576 | . 36444 | 47,3 | . 4016 I | 39,9 | . 96283 | 7,4 | . 03717 |
| . 577 | - 36491 | 47,3 | . 40200 | 39,9 | .96291 | 7,4 | . 03709 |
| . 578 | . 36538 | 47,3 | . 40240 | 39,9 | .96298 | 7,4 | . 03702 |
| . 5.79 | . 36585 | 47,3 | . 40280 | 39,9 | . 96305 | 7,4 | . 03695 |
| I. 580 | 0.36633 | 47,3 | 0.40320 | 39,9 | 9.96313 | 7,4 | 0.03687 |
| . 58 I | . 36680 | 47,3 | . 40360 | 39,9 | . 96320 | 7,4 | . 03680 |
| . 582 | . 36727 | 47,3 | . 40400 | 39,9 | . 96327 | 7,4 | . 03673 |
| . 583 | -36775 | 47,3 | . 40440 | 39,9 | .96335 | 7,3 | . 03665 |
| . 584 | . 36822 | 47,2 | . 40480 | 39,9 | . 96342 | 7,3 | . 03658 |
| I. 585 | 0.36869 | 47,2 | 0.40520 | 39,9 | 9.96349 | 7,3 | 0.03651 |
| . 586 | . 36916 | 47,2 | . 40560 | 39,9 | . 96357 | 7,3 | . 03643 |
| . 587 | . 36964 | 47,2 | . 40599 | 39,9 | . 96364 | 7,3 | . 03636 |
| . 588 | . 37011 | 47,2 | . 40639 | 39,9 | .9637I | 7,3 | . 03629 |
| . 589 | . 37058 | 47,2 | . 40679 | 40,0 | . 96379 | 7,3 | . 03621 |
| I. 590 | 0.37105 | 47,2 | 0.40719 | 40,0 | 9.96386 | 7,2 | 0.03614 |
| . 591 | . 37152 | 47,2 | . 40759 | 40,0 | . 96393 | 7,2 | . 03607 |
| . 592 | . 37200 | 47,2 | . 40799 | 40,0 | . 96400 | 7,2 | . 03600 |
| . 593 | - 37247 | 47,2 | . 40839 | 40,0 | . 96407 | 7,2 | . 03593 |
| . 594 | . 37294 | 47,2 | . 40879 | 40,0 | .96415 | 7,2 | . 03585 |
| I. 595 | 0.37341 | 47,2 | 0.40919 | 40,0 | 9.96422 | 7,2 | 0.03578 |
| . 596 | . 37388 | 47,2 | . 40959 | 40,0 | . 96429 | 7,2 | . 03571 |
| . 597 | - 37435 | 47, I | . 40999 | 40,0 | . 96436 | 7, I | . 03564 |
| . 598 | - 37482 | 47, I | . 41039 | 40,0 | . 96443 | 7,I | . 03557 |
| . 599 | . 37530 | 47, I | . 41079 | 40,0 | . 96450 | 7,I | . 03550 |
| 1. 600 | 0.37577 | 47, I | 0.41119 | 40,0 | 9.96457 | 7,I | 0.03543 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.600 | 0.37577 | 47, I | 0.41119 | 40,0 | 9.96457 | 7,1 | 0.03543 |
| . 601 | . 37624 |  | .41159 |  | . 96465 |  | . 03535 |
| . 602 | . 37671 |  | .41199 |  | . 96472 |  | . 03528 |
| . 603 | -37718 |  | . 41239 |  | . 96479 |  | . 0352 I |
| . 604 | . 37765 |  | . 41279 | 40, I | . 96486 | 7,0 | . 03514 |
| 1.605 | 0.37812 | 47,I | 0.41319 | 40,1 | 9.96493 | 7,0 | 0.03507 |
| . 606 | . 37859 |  | . 41360 |  | . 96500 |  | . 03500 |
| . 607 | . 37906 |  | . 41400 |  | . 96507 |  | . 03493 |
| . 608 | . 37953 |  | . 41440 |  | .96514 |  | . 03486 |
| . 609 | . 38001 |  | . 41480 |  | .9652 I |  | . 03479 |
| 1.610 | 0.38048 | 47,0 | 0.41520 | 40,1 | 9.96528 | 7,0 | 0.03472 |
| . 611 | .38095 |  | . 41560 |  | . 96535 | 6,9 | . 03465 |
| . 612 | -38I42 |  | . 41600 |  | . 96542 |  | . 03458 |
| . 613 | . 38189 |  | . 41640 |  | . 96548 |  | . 03452 |
| . 614 | . 38236 |  | . 41680 |  | . 96555 |  | . 03445 |
| 1.615 | 0.38283 | 47,0 | 0.41720 | 40, I | 9.96562 | 6,9 | 0.03438 |
| . 616 | .38330 |  | .4176I |  | . 96569 |  | . 03431 |
| . 617 | . 38377 |  | . 41801 |  | . 96576 |  | . 03424 |
| .618 | -38424 |  | . 41841 |  | . 96583 | 6,8 | . 03417 |
| . 619 | . 38471 |  | . 4188 I |  | . 96590 |  | . 03410 |
| 1.620 | 0.38518 | 47,0 | 0.4192 I | 40,2 | 9.96597 | 6,8 | 0.03403 |
| . 621 | . 38565 |  | .4196I |  | . 96603 |  | . 03397 |
| . 622 | . 38612 |  | . 42001 |  | .96610 |  | . 03390 |
| . 623 | . 38659 | 46,9 | . 42042 |  | .96617 |  | . 03383 |
| . 624 | . 38705 |  | . 42082 |  | .96624 |  | . 03376 |
| 1.625 | 0.38752 | 46,9 | 0.42122 | 40,2 | 9.96630 | 6,7 | 0.03370 |
| . 626 | . 38799 |  | . 42162 |  | . 96637 |  | . 03363 |
| . 627 | - 38846 |  | . 42202 |  | .96644 |  | . 03356 |
| . 628 | - 38893 |  | . 42243 |  | . 9665 I |  | . 03349 |
| . 629 | . 38940 |  | . 42283 |  | . 96657 |  | . 03343 |
| 1.630 | 0.38987 | 46,9 | 0.42323 | 40,2 | 9.96664 | 6,7 | 0.03336 |
| . 631 | . 39034 |  | . 42363 |  | .9667 I |  | . 03329 |
| . 632 | .39081 |  | . 42403 |  | . 96677 |  | . 03323 |
| . 633 | .39128 |  | . 42444 |  | . 96684 | 6,6 | . 03316 |
| . 634 | . 39175 |  | . 42484 |  | .9669I |  | . 03309 |
| 1.635 | 0.39221 | 46,9 | 0.42524 | 40,2 | 9.96697 | 6,6 | 0.03303 |
| . 636 | . 39268 |  | . 42564 | 40,3 | . 96704 |  | . 03296 |
| . 637 | . 39315 | 46,8 | . 42605 |  | .96710 |  | . 03290 |
| . 638 | - 39362 |  | . 42645 |  | .96717 |  | . 03283 |
| . 639 | . 39409 |  | . 42685 |  | . 96724 |  | . 03276 |
| 1.640 | 0.39456 | 46,8 | 0.42725 | 40,3 | 9.96730 | 6,5 |  |
| . 641 | - 39502 |  | . 42766 |  | . 96737 |  | . 03263 |
| .642 | . 39549 |  | . 42806 |  | . 96743 |  | . 03257 |
| . 643 | - 39596 |  | . 42846 |  | . 96750 |  | . 03250 |
| . 644 | . 39643 |  | . 42887 |  | . 96756 |  | . 03244 |
| I. 645 | 0.39690 | 46,8 | 0.42927 | 40,3 | 9.96763 | 6,5 | 0.03237 |
| . 646 | . 39736 |  | . 42967 |  | . 96769 |  | . 0323 I |
| . 647 | - 39783 |  | . 43008 |  | . 96776 |  | . 03224 |
| . 648 | . 39830 |  | . 43048 |  | . 96782 | 6,4 | . 03218 |
| . 649 | -39877 |  | . 43088 |  | . 96788 |  | . 03212 |
| 1.650 | 0.39923 | 46,8 | 0.43129 | 40.3 | 9.96795 | 6,4 | 0.03205 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.650 | 0.39923 | 46,8 | 0.43129 | 40,3 | 9.96795 | 6,4 | 0.03205 |
| . 651 | - 39970 | 46,7 | . 43169 |  | . 96801 |  | . 03199 |
| . 652 | . 40017 |  | . 43209 | 40,4 | . 96808 |  | . 03192 |
| . 653 | . 40064 |  | . 43250 |  | . 96814 |  | . 03186 |
| . 654 | .40110 |  | . 43290 |  | . 96820 |  | .03180 |
| 1. 655 | 0.40157 | 46,7 | 0.43330 | 40,4 | 9.96827 | 6,4 | 0.03173 |
| . 656 | . 40204 |  | . 43371 |  | . 96833 | 6,3 | . 03167 |
| . 657 | . 40251 |  | -434II |  | . 96840 |  | . 03160 |
| . 658 | . 40297 |  | -4345I |  | . 96846 |  | . 03154 |
| . 659 | . 40344 |  | -43492 |  | . 96852 |  | . 03148 |
| 1.660 | 0.40391 | 46,7 | 0.43532 | 40,4 | 9.96858 | 6,3 | 0.03142 |
| . 661 | . 40437 |  | . 43573 |  | . 96865 |  | . 03135 |
| . 662 | . 40484 |  | . 43613 |  | . 96871 |  | . 03129 |
| . 663 | .40531 |  | . 43653. |  | . 96887 |  | .03123 |
| . 664 | . 40577 |  | . 43694 |  | . 96883 | 6,2 | . 03117 |
| 1. 665 | 0.40624 | 46,7 | 0.43734 | 40,4 | 9.96890 | 6,2 | 0.03110 |
| . 666 | . 40671 | 46,6 | . 43775 |  | . 96896 |  | .03104 |
| . 667 | . 40717 |  | . 43815 |  | . 96902 |  | . 03098 |
| . 668 | . 40764 |  | -43856 |  | . 96908 |  | . 03092 |
| . 669 | .40811 |  | . 43896 | 40,5 | . 96915 |  | . 03085 |
| 1.670 | 0.40857 | 46,6 | 0.43937 | 40,5 | 9.96921 | 6,2 | 0.03079 |
| . 671 | . 40904 |  | . 43977 |  | . 96927 |  | . 03073 |
| . 672 | . 40950 |  | -44017 |  | . 96933 | 6,1 | . 03067 |
| . 673 | -40997 |  | . 44058 |  | . 96939 |  | . 03061 |
| . 674 | . 41044 |  | . 44098 |  | . 96945 |  | . 03055 |
| 1. 675 | 0.41090 | 46,6 | 0.44139 | 40,5 | 9.96951 | 6,1 | 0.03049 |
| . 676 | .41137 |  | . 44179 |  | . 96957 |  | . 03043 |
| . 677 | . 41183 |  | . 44220 |  | . 96964 |  | . 03036 |
| . 678 | . . 41230 |  | . 44260 |  | . 96970 |  | . 03030 |
| . 679 | . 41277 |  | . 44301 |  | . 96976 |  | . 03024 |
| 1.680 | 0.41323 | 46,6 | 0.44341 | 40,5 | 9.96982 | 6,0 | 0.03018 |
| . 681 | . 41370 | 46,5 | . 44382 |  | . 96988 |  | . 03012 |
| . 682 | .41416 |  | . 44422 |  | . 96994 |  | . 03006 |
| . 683 | . 41463 |  | . 44463 |  | . 97000 |  | . 03000 |
| . 684 | . 41509 |  | . 44503 |  | . 97006 |  | . 02994 |
| 1.685 | 0.41556 | 46,5 | 0.44544 | 40,5 | 9.97012 | 6,0 | 0.02988 |
| . 686 | .41602 |  | . 44585 |  | . 97018 |  | . 02982 |
| . 687 | . 41649 |  | . 44625 | 40,6 | . 97024 |  | . 02976 |
| . 688 | . 41695 |  | . 44666 |  | . 97030 | 5,9 | . 02970 |
| . 689 | . 41742 |  | . 44706 |  | . 97036 |  | . 02964 |
| 1.690 | 0.41788 | 46,5 | 0.44747 | 40,6 | 9.97042 | 5,9 | 0.02958 |
| .691 | . 41835 |  | . 44787 |  | -97047 |  | . 02953 |
| . 692 | .4188I |  | . 44828 |  | . 97053 |  | . 02947 |
| . 693 | . 41928 |  | . 44869 |  | . 97059 |  | . 02941 |
| . 694 | . 41974 |  | . 44909 |  | . 97065 |  | . 02935 |
| 1.695 | 0.42021 | 46,5 | 0.44950 | 40,6 | 9.97071 | 5,9 | 0.02929 |
| . 696 | . 42067 |  | . 44990 |  | . 97077 |  | . 02923 |
| . 697 | . 42114 | 46,4 | .45031 |  | . 97083 | 5,8 | . 02917 |
| . 698 | . 42160 |  | . 45072 |  | . 97089 |  | .02911 |
| . 699 | . 42207 |  | .45112 |  | -97094 |  | . 02906 |
| 1.700 | 0.42253 | 46,4 | 0.45153 | 40,6 | 9.97100 | 5,8 | 0.02900 |
| $u$ | log $\tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log csc gd u |

Logarithms of Hyperbolic Functions.

| U | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.700 | 0.42253 | 46,4 | 0.45153 | 40,6 | 9.97100 | 5,8 | 0.02900 |
| . 701 | . 42299 |  | . 45193 |  | .97106 |  | . 02894 |
| . 702 | . 42346 |  | . 45234 |  | .97112 |  | . 02888 |
| . 703 | . 42392 |  | . 45275 |  | .97118 |  | . 02882 |
| . 704 | . 42439 |  | . 45315 |  | . 97123 |  | . 02877 |
| 1.705 | 0.42485 | 46,4 | 0.45356 | 40,7 | 9.97129 | 5,7 | 0.02871 |
| . 706 | . 4253 I |  | . 45397 |  | . 97135 |  | . 02865 |
| . 707 | . 42578 |  | . 45437 |  | .9714I |  | . 02859 |
| . 708 | . 42624 |  | . 45478 |  | . 97146 |  | . 02854 |
| . 709 | . 42671 |  | .45519 |  | .97152 |  | . 02848 |
| 1.710 | 0.42717 | 46,4 | 0.45559 | 40,7 | 9.97158 | 5,7 | 0.02842 |
| . 711 | . 42763 |  | . 45600 |  | .97163 |  | . 02837 |
| . 712 | . 42810 |  | . 4564 I |  | . 97169 |  | .02831 |
| . 713 | . 42856 | 46,3 | .45681 |  | .97175 |  | . 02825 |
| . 714 | . 42902 |  | . 45722 |  | . 97180 | 5,6 | . 02820 |
| 1.715 | 0.42949 | 46,3 | 0.45763 | 40,7 | 9.97186 | 5,6 | 0.02814 |
| . 716 | . 42995 |  | . 45803 |  | . 97192 |  | . 02808 |
| . 717 | . 43041 |  | . 45844 |  | . 97197 |  | .02803 |
| . 718 | . 43088 |  | .45885 |  | . 97203 |  | . 02797 |
| . 719 | .43134 |  | . 45926 |  | . 97208 |  | . 02792 |
| 1.720 | 0.43180 | 46,3 | 0.45966 | 40,7 | 9.97214 | 5,6 | 0.02786 |
| . 721 | . 43227 |  | . 46007 |  | . 97220 |  | . 02780 |
| . 722 | . 43273 |  | . 46048 |  | . 97225 |  | . 02775 |
| . 723 | . 43319 |  | . 46089 |  | .97231 | 5,5 | . 02769 |
| . 724 | . 43365 |  | .46129 | 40,8 | . 97236 |  | . 02764 |
| 1.725 | 0.43412 | 46,3 | 0.46170 | 40,8 | 9.97242 | 5,5 | 0.02758 |
| . 726 | . 43458 |  | .462 I |  | . 97247 |  | . 02753 |
| . 727 | . 43504 |  | . 46252 |  | . 97253 |  | . 02747 |
| . 728 | . 43551 |  | . 46292 |  | . 97258 |  | .02742 |
| . 729 | . 43597 |  | . 46333 |  | . 97264 |  | . 02736 |
| 1.730 | 0.43643 | 46,2 | 0.46374 | 40,8 | 9.97269 | 5,5 | 0.02731 |
| . 731 | . 43689 |  | . 46415 |  | . 97275 |  | . 02725 |
| . 732 | . 43736 |  | . 46455 |  | . 97280 | 5,4 | . 02720 |
| . 733 | . 43782 |  | . 46496 |  | . 97285 |  | . 02715 |
| . 734 | . 43828 |  | . 46537 |  | .9729I |  | . 02709 |
| 1.735 | 0.43874 | 46,2 | 0.46578 | 40,8 | 9.97296 | 5,4 | 0.02704 |
| . 736 | . 43920 |  | . 46619 |  | . 97302 |  | . 02698 |
| . 737 | . 43967 |  | . 46660 |  | . 97307 |  | . 02693 |
| . 738 | . 44013 |  | . 46700 |  | . 97313 |  | . 02687 |
| . 739 | . 44059 |  | . 46741 |  | .97318 |  | .02682 |
| 1.740 | 0.44105 | 46,2 | 0.46782 | 40,8 | 9.97323 | 5,4 | 0.02677 |
| . 74 I | .4415I |  | . 46823 |  | . 97329 | 5,3 | . 02671 |
| . 742 | . 44198 |  | . 46864 | . | . 97334 |  | . 02666 |
| . 743 | . 44244 |  | . 46905 |  | . 97339 |  | . 02661 |
| . 744 | . 44290 |  | . 46945 | 40,9 | . 97345 |  | . 02655 |
| 1.745 | 0.44336 | 46,2 | 0.46986 | 40,9 | 9.97350 | 5,3 | 0.02650 |
| . 746 | . 44382 |  | . 47027 |  | . 97355 |  | . 02645 |
| . 747 | . 44428 |  | . 47068 | - | . 97360 |  | . 02640 |
| . 748 | . 44475 | 46, I | . 47109 |  | . 97366 |  | . 02634 |
| . 749 | . 44521 |  | . 47150 |  | . 9737 I |  | . 02629 |
| 1.750 | 0.44567 | 46, I | 0.47191 | 40,9 | 9.97376 | 5,3 | 0.02624 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.750 | 0.44567 | 46, 1 | 0.47191 | 40,9 | 9.97376 | 5,3 | 0.02624 |
| . 751 | . 44613 |  | .4723I |  | . 97382 | 5,2 | . 02618 |
| . 752 | . 44659 |  | . 47272 |  | . 97387 |  | .02613 |
| . 753 | . 44705 |  | . 47313 |  | . 97392 |  | .02608 |
| . 754 | . 4475 I |  | . 47354 |  | . 97397 |  | . 02603 |
| 1.755 | 0.44797 | 46,1 | 0.47395 | 40,9 | 9.97402 | 5,2 | 0.02598 |
| . 756 | . 44844 |  | . 47436 |  | . 97408 |  | . 02592 |
| . 757 | . 44890 |  | . 47477 |  | . 97413 |  | . 02587 |
| . 758 | . 44936 |  | . 47518 |  | . 97418 |  | . 02582 |
| . 759 | . 44982 |  | . 47559 |  | . 97423 |  | . 02577 |
| 1.760 | 0.45028 | 46,1 | 0.47600 | 40,9 | 9.97428 | 5, I | 0.02572 |
| . 761 | . 45074 |  | . 47641 |  | . 97433 |  | . 02567 |
| . 762 | . 45120 |  | . 47682 |  | . 97439 |  | . 02561 |
| .763 | . 45166 |  | . 47722 |  | . 97444 |  | . 02556 |
| . 764 | . 45212 |  | . 47763 | 41,0 | . 97449 |  | . 02551 |
| 1.765 | 0.45258 | 46, 1 | 0.47804 | 41,0 | 9.97454 | 5,I | 0.02546 |
| . 766 | . 45304 | 46,0 | . 47845 |  | . 97459 |  | . 02541 |
| .767 | . 45350 |  | . 47886 |  | . 97464 |  | . 02536 |
| . 768 | . 45396 |  | . 47927 |  | . 97469 |  | .0253I |
| .769 | . 45442 |  | . 47968 |  | . 97474 |  | . 02526 |
| 1.770 | 0.45488 | 46,0 | 0.48009 | 41,0 | 9.97479 | 5,0 | 0.02521 |
| . 771 | . 45534 |  | . 48050 |  | . 97484 |  | . 02516 |
| . 772 | . 45580 |  | . 48091 |  | . 97489 |  | .025II |
| . 773 | . 45627 |  | .48I32 |  | . 97494 |  | . 02506 |
| . 774 | . 45673 |  | .48173 |  | . 97499 |  | . 02501 |
| 1.775 | 0.45719 | 46,0 | 0.48214 | 41,0 | 9.97504 | 5,0 | 0.02496 |
| . 776 | . 45765 |  | . 48255 |  | . 97509 |  | . 02491 |
| . 777 | .45810 |  | . 48296 |  | .97514 |  | . 02486 |
| . 778 | . 45856 |  | . 48337 |  | . 97519 |  | .0248I |
| . 779 | . 45902 |  | . 48378 |  | . 97524 |  | . 02476 |
| 1.780 | 0.45948 | 46,0 | 0.48419 | 41,0 | 9.97529 | 4,9 | 0.02471 |
| . 781 | . 45994 |  | . 48460 |  | . 97534 |  | . 02466 |
| . 782 | . 46040 |  | . 48501 |  | . 97539 |  | .0246I |
| .783 | . 46086 |  | . 48542 |  | . 97544 |  | . 02456 |
| . 784 | . 46132 |  | . 48583 |  | . 97549 |  | .02451 |
| 1.785 | 0.46178 | 45,9 | 0.48624 | 41,1 | 9.97554 | 4,9 | 0.02446 |
| . 786 | . 46224 |  | . 48666 |  | . 97559 |  | . 02441 |
| . 787 | . 46270 |  | . 48707 |  | . 97564 |  | . 02436 |
| . 788 | . 46316 |  | . 48748 |  | . 97568 |  | . 02432 |
| .789 | . 46362 |  | . 48789 |  | . 97573 |  | . 02427 |
| 1.790 | 0.46408 | 45,9 | 0.48830 | 41, I | 9.97578 | 4,8 | 0.02422 |
| . 791 | . 46454 |  | . 48871 |  | . 97583 |  | . 02417 |
| . 792 | . 46500 |  | . 48912 |  | . 97588 |  | . 02412 |
| . 793 | . 46546 |  | . 48953 |  | . 97593 |  | . 02407 |
| . 794 | . 46592 |  | . 48994 |  | . 97597 |  | . 02403 |
| 1.795 | 0.46637 | 45,9 | 0.49035 | 41, I | 9.97602 | 4,8 | 0.02398 |
| . 796 | . 46683 |  | . 49076 |  | . 97607 |  | . 02393 |
| . 797 | . 46729 |  | . 49117 |  | .97612 |  | . 02388 |
| . 798 | . 46775 |  | . 49159 |  | .97617 |  | .02383 |
| . 799 | . 4682 I |  | . 49200 |  | .97621 |  | . 02379 |
| 1.800 | 0.46867 | 45,9 | 0.49241 | 41.1 | 9.97626 | 4,8 | 0.02374 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.800 | 0.46867 | 45,9 | 0.4924 I | 41,I | 9.97626 | 4,8 | 0.02374 |
| . 801 | . 46913 |  | . 49282 |  | .97631 | 4,7 | . 02369 |
| . 802 | . 46959 |  | . 49323 |  | . 97636 |  | . 02364 |
| . 803 | . 47004 |  | . 49364 |  | . 97640 |  | . 02360 |
| . 804 | . 47050 | 45,8 | . 49405 |  | . 97645 |  | . 02355 |
| 1.805 | 0.47096 | 45,8 | 0.49446 | 4I, I | 9.97650 | 4,7 | 0.02350 |
| . 806 | . 47142 |  | . 49488 |  | . 97654 |  | . 02346 |
| . 807 | . 47188 |  | . 49529 | 4I,2 | . 97659 |  | . 02341 |
| . 808 | . 47234 |  | . 49570 |  | . 97664 |  | . 02336 |
| . 809 | . 47279 |  | . 4961 I |  | . 97668 |  | . 02332 |
| 1.810 | 0.47325 | 45,8 | 0.49652 | 41,2 | 9.97673 | 4,7 | 0.02327 |
| .8II | . 47371 |  | . 49693 |  | . 97678 | 4,6 | . 02322 |
| . 812 | . 47417 |  | . 49734 |  | . 97682 |  | . 02318 |
| . 813 | . 47463 |  | . 49776 | . | . 97687 |  | . 02313 |
| .814 | . 47509 |  | . 49817 |  | . 97692 |  | . 02308 |
| 1.815 | 0.47554 | 45,8 | 0.49858 | 41,2 | 9.97696 | 4,6 | 0.02304 |
| .816 | . 47600 |  | . 49899 |  | .97701 |  | . 02299 |
| .817 | . 47646 |  | . 49940 |  | . 97705 |  | . 02295 |
| .818 | . 47692 |  | . 49982 |  | . 97710 |  | . 02290 |
| .819 | . 47737 |  | . 50023 |  | . 97715 |  | . 02285 |
| 1.820 | 0.47783 | 45,8 | 0.50064 | 41,2 | 9.97719 | 4,6 | 0.0228 I |
| . 82 I | . 47829 |  | . 50105 |  | . 97724 |  | . 02276 |
| . 822 | . 47875 |  | . 50146 |  | . 97728 | 4.5 | . 02272 |
| . 823 | . 47921 |  | . 50188 |  | . 97733 |  | . 02267 |
| . 824 | . 47966 |  | . 50229 |  | . 97737 |  | . 02263 |
| 1.825 | 0.48012 | 45,7 | 0.50270 | 4I,2 |  | 4,5 | 0.02258 |
| . 826 | . 48058 |  | . 5031 I |  | . 97746 |  | . 02254 |
| . 827 | .48104 |  | . 50353 |  | . 97751 |  | . 02249 |
| . 828 | .48149 |  | . 50394 |  | . 97755 |  | . 02245 |
| . 829 | .48195 |  | . 50435 |  | . 97760 |  | . 02240 |
| 1.830 | 0.48241 | 45,7 | 0.50476 | 41,3 | 9.97764 | 4,5 | 0.02236 |
| .83I | . 48286 |  | . 50518 |  | . 97769 |  | . 02231 |
| . 832 | . 48332 |  | . 50559 |  | . 97773 |  | . 02227 |
| . 833 | . 48378 |  | . 50600 | $\cdots$ | . 97778 | 4,4 | . 02222 |
| . 834 | . 48424 |  | . 5064 I |  | . 97782 |  | . 022218 |
| 1.835 | 0.48469 | 45,7 | 0.50683 | 41,3 | 9.97787 | 4,4 | 0.02213 |
| . 836 | . 48515 |  | . 50724 |  | . 97791 |  | . 02209 |
| . 837 | . 48561 |  | . 50765 |  | . 97796 |  | . 02204 |
| . 838 | . 48606 |  | . 50806 |  | . 97800 |  | . 02200 |
| . 839 | . 48652 | - | - 50848 |  | . 97804 |  | . 02196 |
| 1.840 | 0.48698 | 45,7 | 0.50889 | 4I,3 | 9.97809 | 4,4 | 0.02191 |
| .841 | . 48743 |  | . 50930 | 41,3 | .97813 |  | .02187 |
| . 842 | . 48789 |  | . 50972 |  | . 97817 |  | . 02183 |
| . 843 | . 48835 |  | . 51013 |  | . 97822 | . | .02178 |
| . 844 | . 48880 |  | . 51054 |  | . 97826 | 4,3 | .02174 |
| 1.845 | 0.48926 | 45,7 | 0.51096 | 4I,3 | 9.9783 I | 4,3 | 0.02169 |
| . 846 | . 48972 | 45,6 | . 51137 |  | . 97835 |  | . 02165 |
| .847 | . 49017 |  | - 51178 |  | . 97839 |  | .0216I |
| . 848 | . 49063 |  | . 51219 |  | . 97843 |  | . 02157 |
| . 849 | . 49109 |  | . 5126 I |  | . 97848 |  | . 02152 |
| I. 850 | 0.49154 | 45,6 | 0.51302 | 41,3 | 9.97852 | 4,3 | 0.02148 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ cosh u | $\omega \mathrm{Fo}^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.850 | 0.49154 | 45,6 | 0.51302 | 41,3 | 9.97852 | 4,3 | 0.02148 |
| .851 | . 49200 |  | . 51343 |  | . 97856 |  | . 02144 |
| . 852 | . 49246 |  | . 51385 |  | .97861 |  | . 02139 |
| . 853 | . 49291 |  | . 51426 |  | . 97865 |  | . 02135 |
| . 854 | . 49337 |  | . 51468 | 41,4 | . 97869 |  | .02131 |
| 1. 855 | 0.49382 | 45,6 | 0.51509 | 41,4 | 9.97873 | 4.3 | 0.02127 |
| . 856 | . 49428 |  | . 51550 |  | . 97878 | 4,2 | . 02122 |
| . 857 | . 49474 |  | . 51592 |  | . 97882 |  | . 02118 |
| . 858 | . 49519 |  | . 51633 |  | . 97886 |  | . 02114 |
| . 859 | . 49565 |  | . 51674 |  | . 97890 |  | .02110 |
| 1.860 | 0.49610 | 45,6 | 0.51716 | 41,4 | 9.97895 | 4,2 | 0.02105 |
| . 861 | . 49656 |  | . 51757 |  | . 97899 |  | . 02101 |
| . 862 | . 49702 |  | . 51798 |  | . 97903 |  | . 02097 |
| . 863 | . 49747 |  | . 51840 |  | . 97907 |  | 02093 |
| . 864 | . 49793 |  | . 51881 |  | .97911 |  | . 02089 |
| 1.865 | 0.49838 | 45,6 | 0.51923 | 41,4 | 9.97916 | 4,2 | 0.02084 |
| . 866 | . 49884 |  | . 51964 |  | . 97920 |  | . 02080 |
| . 867 | . 49929 |  | . 52005 |  | . 97924 |  | . 02076 |
| . 868 | . 49975 |  | . 52047 |  | . 97928 | 4, I | . 02072 |
| . 869 | . 50020 | 45,5 | . 52088 |  | . 97932 |  | . 02068 |
| 1.870 | 0.50066 | 45,5 | 0.52130 | 41,4 | 9.97936 | 4, I | 0.02064 |
| . 871 | . 50112 |  | . 52171 |  | . 97940 |  | . 02060 |
| . 872 | . 50157 |  | . 52212 |  | . 97945 |  | . 02055 |
| . 873 | . 50203 |  | . 52254 |  | . 97949 |  | . 02051 |
| . 874 | . 50248 |  | . 52295 |  | . 97953 |  | . 02047 |
| 1.875 | 0.50294 | 45,5 | 0.52337 | 41,4 | 9.97957 | 4, I | 0.02043 |
| . 876 | . 50339 |  | . 52378 |  | .97961 |  | . 02039 |
| . 877 | . 50385 |  | . 52420 |  | . 97965 |  | . 02035 |
| . 878 | . 50430 |  | . 5246I |  | . 97969 |  | .0203I |
| . 879 | . 50476 |  | . 52503 |  | . 97973 |  | . 02027 |
| 1.880 | 0.50521 | 45,5 | 0.52544 | 41,5 | 9.97977 | 4,0 | 0.02023 |
| . 88 I | . 50567 |  | . 52585 |  | .97981 |  | . 02019 |
| . 882 | . 50612 |  | . 52627 |  | . 97985 |  | . 02015 |
| . 883 | . 50658 |  | . 52668 |  | . 97989 |  | . 02011 |
| . 884 | . 50703 |  | . 52710 | - | . 97993 |  | . 02007 |
| 1.885 | 0.50749 | 45,5 | 0.52751 | 41,5 | 9.97997 | 4,0 | 0.02003 |
| . 886 | . 50794 |  | . 52793 |  | .9800I |  | . 01999 |
| . 887 | . 50840 |  | . 52834 |  | . 98005 |  | . 01995 |
| . 888 | . 50885 |  | . 52876 |  | . 98009 |  | . 01991 |
| . 889 | . 50931 |  | . 52917 | . | .98013 |  | . 01987 |
| 1. 890 | 0. 50976 | 45,5 | 0.52959 | 41,5 | 9.98017 | 4,0 | 0.01983 |
| . 891 | . 51021 |  | . 53000 |  | . 98021 |  | . 01979 |
| . 892 | . 51067 | 45,4 | . 53042 |  | . 98025 |  | . 01975 |
| . 893 | . 51112 |  | . 53083 |  | . 98029 | 3.9 | . 01971 |
| . 894 | . 51158 |  | . 53125 |  | . 98033 |  | . 01967 |
| 1. 895 | 0.51203 | 45,4 | 0.53166 | 41,5 | 9.98037 | 3,9 | 0.01963 |
| . 896 | . 51249 |  | . 53208 |  | .9804I |  | . 01959 |
| . 897 | . 51294 |  | . 53249 |  | . 98045 |  | . 01955 |
| . 898 | . 51340 |  | . 53291 |  | . 98049 |  | . 01951 |
| . 899 | . 51385 |  | . 53332 |  | . 98053 |  | . 01947 |
| 1.900 | 0.51430 | 45,4 | 0.53374 | 41,5 | 9.98057 | 3,9 | 0.01943 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc$ gd u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.900 | 0.51430 | 45,4 | 0.53374 | 41,5 | 9.98057 | 3,9 | 0.01943 |
| . 901 | . 51476 |  | . 53415 |  | . 98060 |  | . 01940 |
| . 902 | . 5152 I |  | - 53457 |  | . 98064 |  | . 01936 |
| . 903 | .51567 |  | . 53498 |  | . 98068 |  | . 01932 |
| . 904 | . 51612 |  | . 53540 |  | . 98072 |  | . 01928 |
| 1.905 | 0.51657 | 45,4 | 0.5358I | 41,5 | 9.98076 | 3,8 | 0.01924 |
| . 906 | . 51703 |  | . 53623 | 41,6 | . 98080 |  | . 01920 |
| . 907 | . 51748 |  | . 53665 |  | . 98084 |  | . 01916 |
| . 908 | . 51794 |  | - 53706 |  | . 98087 |  | . 01913 |
| . 909 | . 51839 |  | . 53748 |  | .9809I |  | . 01909 |
| 1.910 | 0.51884 | 45,4 | 0.53789 | 41,6 | 9.98095 | 3,8 | 0.01905 |
| .91I | . 51930 |  | . 5383 I |  | . 98099 |  | . 01901 |
| . 912 | .51975 | - | - 53872 |  | .98103 |  | . 01897 |
| .913 | . 52020 |  | . 53914 |  | .98106 |  | . 01894 |
| .914 | . 52066 |  | - 53956 |  | .98i 10 |  | . 01890 |
| 1.915 | 0.5211 I | 45,4 | 0.53997 | 41,6 | 9.98II4 | 3,8 | 0.01886 |
| . 916 | . 52157 |  | . 54039 |  | .98il8 |  | . 01882 |
| . 917 | . 52202 | 45,3 | . 54080 |  | .98122 |  | . 01878 |
| .918 | . 52247 |  | . 54122 |  | .98125 | 1 | . 01875 |
| . 919 | . 52293 |  | . 54164 |  | .98I29 | 3,7 | . 01871 |
| 1.920 | 0.52338 | 45,3 | 0.54205 | 41,6 | 9.98133 | 3,7 | 0.01867 |
| . 92 I | . 52383 |  | . 54247 |  | .98137 |  | . 01863 |
| . 922 | . 52429 |  | . 54288 |  | .98140 |  | . 01860 |
| . 923 | . 52474 |  | . 54330 |  | .98144 |  | . 01856 |
| . 924 | . 52519 |  | . 54372 |  | .98148 |  | . 01852 |
| 1.925 | 0.52565 | 45,3 | 0.54413 | 41,6 | 9.98151 | 3,7 | 0.01849 |
| . 926 | . 52610 |  | . 54455 |  | .98I55 |  | . 01845 |
| . 927 | . 52655 |  | . 54496 |  | . 98159 |  | . 01841 |
| . 928 | . 52700 |  | - 54538 |  | .98162 |  | . 01838 |
| . 929 | . 52746 |  | - 54580 |  | .98166 |  | . 01834 |
| 1.930 | 0.52791 | 45,3 | 0.54621 | 41,6 | 9.98170 | 3,7 | 0.01830 |
| . 931 | . 52836 |  | . 54663 |  | .98173 |  | . 01827 |
| . 932 | . 52882 |  | . 54705 |  | .98177 | 3,6 | . 01823 |
| . 933 | . 52927 |  | - 54746 |  | .98181 |  | .01819 |
| . 934 | . 52972 |  | . 54788 | 41,7 | .98I84 |  | .01816 |
| 1.935 | 0.53018 | 45,3 | 0.54830 | 41,7 |  | 3,6 | 0.01812 |
| . 936 | . 53063 |  | . 54871 |  | . 98192 |  | . 01808 |
| . 937 | . 53108 |  | . 54913 |  | .98195 |  | . 01805 |
| . 938 | . 53153 |  | . 54955 |  | .98199 |  | . O I801 |
| . 939 | . 53199 |  | . 54996 |  | . 98202 |  | . 01798 |
| 1.940 | 0.53244 | 45,3 | 0.55038 | 41,7 | 9.98206 | 3,6 | 0.01794 |
| .94I | . 53289 |  | . 55080 |  | . 98210 |  | . 01790 |
| . 942 | . 53334 |  | . 55121 |  | . 98213 |  | . 01787 |
| . 943 | . 53380 | 45,2 | . 55163 |  | . 98217 |  | . 01783 |
| . 944 | - 53425 |  | . 55205 |  | . 98220 |  | . 01780 |
| 1.945 | 0.53470 | 45,2 | 0.55246 | 41,7 | 9.98224 | 3,6 | 0.01776 |
| . 946 | . 53515 |  | . 55288 |  | . 98227 | 3,5 | . Q1773 |
| . 947 | . 5356 I |  | . 55330 |  | .9823I |  | . 01769 |
| . 948 | . 53606 |  | -55371 |  | . 98235 |  | . 01765 |
| . 949 | . 53651 |  | -55413 |  | . 98238 |  | . 01762 |
| 1.950 | 0.53696 | 45,2 | 0.55455 | 41,7 | 9.98242 | 3,5 | 0.01758 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \operatorname{cscgd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.950 | 0.53696 | 45,2 | 0.55455 | 41,7 | 9.98242 | 3,5 | 0.01758 |
| .95I | . 53742 |  | . 55496 |  | . 98245 |  | . 01755 |
| . 952 | . 53787 |  | - 55538 |  | . 98249 |  | . 01751 |
| . 953 | . 53832 |  | - 55580 |  | . 98252 |  | . 01748 |
| . 954 | . 53877 |  | . 55622 |  | . 98256 |  | . 01744 |
| 1.955 | 0.53922 | 45,2 | 0.55663 | 41,7 | 9.98259 | 3,5 | 0.01741 |
| . 956 | . 53968 |  | . 55705 |  | . 98263 |  | . 01737 |
| . 957 | . 54013 |  | . 55747 |  | . 98266 |  | . 01734 |
| . 958 | . 54058 |  | . 55788 |  | . 98269 |  | . 01731 |
| . 959 | . 54103 |  | . 55830 |  | . 98273 |  | . 01727 |
| 1.960 | 0. 54148 | 45,2 | 0.55872 | 41,7 | 9.98276 | 3,4 | 0.01724 |
| . 961 | . 54194 |  | . 55914 |  | . 98280 |  | . 01720 |
| . 962 | . 54239 |  | . 55955 |  | . 98283 |  | . 01717 |
| . 963 | . 54284 |  | . 55997 |  | . 98287 |  | . OI713 |
| . 964 | . 54329 |  | . 56039 | 41,8 | . 98290 |  | . 01710 |
| 1.965 | 0.54374 | 45,2 | 0.5608I | 4I,8 | 9.98294 | 3,4 | 0.01706 |
| . 966 | . 54419 |  | . 56122 |  | . 98297 |  | . 01703 |
| . 967 | . 54465 |  | . 56164 |  | . 98300 |  | . 01700 |
| . 968 | . 54510 |  | . 56206 |  | . 98304 |  | . 01696 |
| . 969 | . 54555 |  | . 56248 |  | . 98307 |  | . 01693 |
| 1.970 | 0.54600 | 45,2 | 0.56290 | 41,8 | 9.983 II | 3,4 | 0.01689 |
| .971 | . 54645 | 45, 1 | . 56331 |  | . 98314 |  | . 01686 |
| . 972 | . 54690 |  | . 56373 |  | . 98317 |  | . 01683 |
| . 973 | . 54736 |  | . 56415 |  | .98321 |  | .01679 |
| . 974 | . 5478 I |  | . 56457 |  | . 98324 |  | . 01676 |
| 1.975 | 0.54826 | 45,1 | 0.56498 | 4I,8 | 9.98327 | 3,3 | 0.01673 |
| . 976 | . 54871 |  | . 56540 |  | . 9833 I |  | . 01669 |
| . 977 | . 54916 |  | - 56582 |  | . 98334 |  | . 01666 |
| . 978 | . 54961 |  | . 56624 |  | . 98337 |  | . 01663 |
| . 979 | . 55006 |  | . 56666 |  | .9834I |  | . 01659 |
| 1.980 | 0.55051 | 45,1 | 0.56707 | 41,8 | 9.98344 | 3,3 | 0.01656 |
| .981 | . 55097 |  | . 56749 |  | . 98347 |  | . 01653 |
| . 982 | .55142 |  | . 56791 |  | .9835I |  | . 01649 |
| . 983 | . 55187 |  | . 56833 |  | . 98354 |  | . 01646 |
| . 984 | . 55232 |  | . 56875 |  | . 98357 |  | . 01643 |
|  | 0.55277 | 45,1 | 0.56916 | 41,8 |  | 3,3 |  |
| . 986 | . 55322 |  | . 56958 |  | $.98364$ |  | . 01636 |
| . 987 | . 55367 |  | . 57000 |  | . 98367 |  | . 01633 |
| . 988 | . 55412 |  | . 57042 |  | . 98370 |  | . 01630 |
| . 989 | . 55457 |  | . 57084 |  | . 98374 |  | . 01626 |
| 1.990 | 0.55502 | 45, I | 0.57126 | 41,8 | 9.98377 | 3,2 | 0.01623 |
| .991 | . 55547 |  | . 57167 |  | . 98380 |  | . 01620 |
| . 992 | . 55593 |  | . 57209 |  | . 98383 |  | . 01617 |
| . 993 | . 55638 |  | . 5725 I |  | . 98387 |  | . 01613 |
| . 994 | . 55683 |  | . 57293 |  | . 98390 |  | .01610 |
| I. 995 | 0.55728 | 45, I | 0.57335 | 41,9 | 9.98393 | 3,2 | 0.01607 |
| . 996 | . 55773 |  | . 57377 |  | . 98396 |  | . 01604 |
| . 997 | . 55818 |  | . 57419 |  | . 98399 |  | . 01601 |
| . 998 | . 55863 |  | . 57460 |  | . 98403 |  | . O1597 |
| . 999 | . 55908 |  | . 57502 |  | . 98406 |  | . OI 594 |
| 2.000 | 0.55953 | 45,0 | 0.57544 | 41,9 | 9.98409 | 3,2 | 0.01591 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.000 | 0.55953 | 45,0 | 0.57544 | 41,9 | 9.98409 | 3,2 | 0.01591 |
| . 001 | . 55998 |  | . 57586 |  | . 98412 |  | . 01588 |
| . 002 | . 56043 |  | . 57628 |  | . 98415 |  | . 01585 |
| . 003 | . 56088 | . | . 57670 |  | . 98418 |  | . 01582 |
| . 004 | . 56133 |  | . 57712 |  | . 98422 |  | . 01578 |
| 2.005 | 0. 56178 | 45,0 | 0.57754 | 41,9 | 9.98425 | 3,2 | 0.01575 |
| . 006 | . 56223 |  | . 57795 |  | . 98428 | 3,1 | . 01572 |
| . 007 | . 56268 |  | . 57837 |  | . 98431 |  | . 01569 |
| . 008 | . 56313 |  | . 57879 |  | . 98434 |  | . 01566 |
| . 009 | . 56358 |  | . 57921 |  | . 98437 |  | . 01563 |
| 2.010 | 0.56403 | 45,0 | 0.57963 | 41,9 | 9.98440 | 3,i | 0.01560 |
| . 011 | . 56448 |  | . 58005 |  | . 98444 |  | . 01556 |
| . 012 | . 56493 |  | . 58047 |  | . 98447 |  | . 01553 |
| . 12 | . 56538 |  | . 58089 |  | . 98450 |  | . 01550 |
| . 014 | . 56583 |  | .58131 |  | . 98453 |  | . 01547 |
| 2.015 | 0. 56628 | 45,0 | 0.58172 | 41,9 | 9.98456 | 3, I | 0.01544 |
| . 016 | . 56673 |  | . 58214 |  | . 98459 |  | . 01541 |
| . 017 | . 56718 |  | . 58256 |  | . 98462 |  | . 01538 |
| . 018 | . 56723 |  | . 58298 |  | . 98465 |  | . 01535 |
| . 019 | . 56808 |  | . 58340 |  | . 98468 |  | .or532 |
| 2.020 | 0. 56853 | 45,0 | 0.58382 | 41,9 | 9.98471 | 3,1 | 0.01529 |
| . 021 | . 56898 |  | . 58424 |  | . 98474 |  | . 01526 |
| . 022 | . 56943 |  | . 58466 |  | . 98477 | 3,0 | . 01523 |
| . 023 | . 56988 |  | . 58508 |  | . 98480 |  | . 01520 |
| . 024 | . 57033 |  | . 58550 |  | . 98484 |  | . 01516 |
| 2.025 | 0.57078 | 45,0 | 0.58592 | 41,9 | 9.98487 | 3,0 | 0.01513 |
| . 026 | . 57123 |  | . 58634 |  | . 98490 |  | . 01510 |
| . 027 | . 57168 |  | . 58676 |  | . 98493 |  | . 01507 |
| . 028 | . 57213 |  | . 58718 | 42,0 | . 98496 |  | . 01504 |
| . 029 | . 57258 |  | . 58760 |  | . 98499 |  | . 01501 |
| 2.030 | 0.57303 | 45,0 | 0.58802 | 42,0 | 9.98502 | 3,0 | 0.01498 |
| .031 | . 57348 |  | . 58843 |  | . 98505 |  | . 01495 |
| . 032 | . 57393 | 44,9 | . 58885 |  | . 98508 |  | . 01492 |
| . 033 | -57438 |  | . 58927 |  | . 9851 I |  | . 01489 |
| . 034 | . 57483 |  | . 58969 |  | . 28514 |  | . 01486 |
| 2.035 | 0.57528 | 44,9 | 0.59011 | 42,0 |  | 3,0 |  |
| . 036 | . 57573 |  | . 59053 |  | . 98519 |  | .01481 |
| . 037 | . 57618 |  | . 59095 |  | . 98522 |  | . 01478 |
| . 038 | . 57663 |  | . 59137 |  | . 98525 | 2,9 | . 01475 |
| . 039 | - 57708 |  | . 59179 |  | . 98528 |  | . 01472 |
| 2.040 | 0.57753 | 44.9 | 0.59221 | 42,0 | 9.98531 | 2,9 | 0.01469 |
| .041 | . 57797 |  | . 59263 |  | . 98534 |  | . 01466 |
| . 042 | . 57842 |  | . 59305 |  | . 98537 |  | . 01463 |
| . 043 | . 57887 |  | - 59347 |  | . 98540 |  | . 01460 |
| . 044 | . 57932 |  | . 59389 |  | . 98543 |  | . 01457 |
| 2.045 | 0.57977 | 44,9 | 0.59431 | 42,0 | 9.98546 | 2,9 | 0.01454 |
| . 046 | . 58022 |  | . 59473 |  | . 98549 |  | . 01451 |
| . 047 | . 58067 |  | - 59515 |  | . 98552 |  | . 01448 |
| . 048 | . 58112 | . | - 59557 |  | . 98555 |  | . 01445 |
| . 049 | . 58157 |  | . 59599 |  | . 98558 |  | . 01442 |
| 2.050 | 0.58202 | 44,9 | 0. 59641 | 42,0 | 9.98560 | 2,9 | 0.01440 |
| $u$ | log tan gdu | $\omega \mathrm{Fo}^{\prime}$ | log sec ad u | $\omega \mathrm{Fo}^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log csc od u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.050 | 0.58202 | 44.9 | 0.59641 | 42,0 | 9.98560 | 2,9 | 0.01440 |
| . 051 | . 58246 |  | . 59683 |  | . 98563 |  | . 01437 |
| . 052 | . 58291 |  | . 59725 |  | . 98566 |  | . 01434 |
| . 053 | . 58336 |  | . 59767 |  | . 98569 |  | .01431 |
| . 054 | .58381 |  | . 59809 |  | . 98572 |  | .01428 |
| 2.055 | 0.58426 | 44,9 | 0.59851 | 42,0 | 9.98575 | 2,9 | 0.01425 |
| . 056 | . 58471 |  | . 59893 |  | . 98578 | 2,8 | . 01422 |
| . 057 | . 58516 |  | . 59935 |  | . 98580 |  | . 01420 |
| . 058 | . 58561 |  | . 59977 |  | . 98583 |  | .01417 |
| . 059 | . 58606 |  | . 60019 |  | . 98586 |  | . 01414 |
| 2.060 | 0.58650 | 449 | 0.60061 | 42,0 | 9.98589 | 2,8 | 0.01411 |
| . 061 | . 58695 |  | . 60104 |  | . 98592 |  | . 01408 |
| . 062 | . 58740 |  | . 60146 |  | . 98595 |  | . 01405 |
| . 063 | .58785 |  | . 60188 |  | . 98597 |  | . 01403 |
| . 064 | . 58830 |  | . 60230 | 42, I | . 98600 |  | . 01400 |
| 2.065 | 0.58875 | 44,8 | 0.60272 | 42, I | 9.98603 | 2,8 | 0.01397 |
| . 066 | . 58920 |  | . 60314 |  | . 98606 | - | . O1394 |
| . 067 | . 58964 |  | . 60356 |  | . 98609 |  | . 01391 |
| . 068 | . 59009 |  | . 60398 |  | .986I I |  | . 01389 |
| . 069 | . 59054 |  | . 60440 |  | . 98614 |  | . 01386 |
| 2.070 | 0.59099 | 44,8 | 0.60482 | 42, I | 9.98617 | 2,8 | 0.01383 |
| . 071 | . 59144 |  | . 60524 |  | . 98620 |  | . 01380 |
| . 072 | . 59189 |  | . 60566 |  | . 98622 |  | . 01378 |
| . 073 | . 59233 |  | . 60608 |  | . 98625 |  | . 01375 |
| . 074 | . 59278 |  | . 60650 |  | . 98628 | 2,7 | . 01372 |
| 2.075 | 0.59323 | 44,8 | 0.60692 | 42, I | 9.98631 | 2,7 | 0.01369 |
| . 076 | . 59368 |  | . 60734 |  | . 98633 |  | . 01367 |
| . 077 | . 59413 |  | . 60777 |  | . 98636 |  | .01364 |
| . 078 | . 59457 |  | . 60819 |  | . 98639 |  | . 01361 |
| . 079 | . 59502 |  | .60861 |  | . 98642 |  | .OI358 |
| 2.080 | 0.59547 | 44,8 | 0.60903 | 42, I | 9.98644 | 2,7 | 0.01356 |
| . 081 | . 59592 |  | . 60945 | 42,1 | . 98647 |  | . 01353 |
| . 082 | . 59637 |  | . 60987 |  | . 98650 |  | . 01350 |
| . 083 | . 5968 I |  | . 61029 |  | . 98652 |  | . 01348 |
| . 084 | . 59726 |  | .6107 I |  | . 98655 |  | . 01345 |
| 2.085 | 0.59771 | 44,8 | 0.61113 | 42, I | 9.98658 | 2,7 | 0.01342 |
| . 086 | . 59816 |  | .6II55 |  | . 98660 |  | . 01340 |
| .087 | . 5986 I |  | . 61198 |  | . 98663 |  | . 01337 |
| . 088 | . 59905 |  | . 61240 |  | . 98666 |  | .OI334 |
| . 089 | . 59950 |  | .61282 |  | . 98668 |  | . 01332 |
| 2.090 | 0.59995 | 44,8 | 0.61324 | 42, I | - 9.98671 | 2,7 |  |
| .091 | . 60040 |  | .61366 |  | . 98674 |  | . 01326 |
| . 092 | . 60085 |  | .61408 |  | . 98676 | 2,6 | . 01324 |
| . 093 | . 60129 |  | .6I450 |  | . 98679 |  | . 01321 |
| . 094 | . 60174 |  | . 61492 |  | . 98682 |  | . 01318 |
| 2.095 | 0.60219 | 44,8 | 0.61535 | 42, I | 9.98684 | 2,6 | 0.01316 |
| . 096 | . 60264 |  | .6I577 |  | . 98687 |  | . 01313 |
| . 097 | . 60308 |  | . 61619 |  | . 98690 |  | . 01310 |
| . 098 | . 60353 |  | .6166I |  | . 98692 |  | . 01308 |
| . 099 | . 60398 |  | .61703 |  | . 98695 |  | . 01305 |
| 2. 100 | 0.60443 | 44,8 | 0.61745 | 42, 1 | 9.98597 | 2,6 | 0.01303 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log tanh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2. 100 | 0.60443 | 44,8 | 0.61745 | 42, 1 | 9.98697 | 2,6 | 0.01303 |
| . 101 | . 60487 | 44,7 | . 61787 |  | . 98700 |  | . 01300 |
| . 102 | . 60532 |  | . 61830 | 42,2 | . 98703 |  | . 01297 |
| . 103 | . 60577 |  | . 61872 |  | . 98705 |  | . 01295 |
| . 104 | . 60622 |  | . 61914 |  | . 98708 |  | . 01292 |
| 2.105 | 0.60666 | 44,7 | 0.61956 | 42,2 | 9.98710 | 2,6 | 0.01290 |
| . 106 | . 60711 |  | . 61998 |  | . 98713 |  | . 01287 |
| . 107 | . 60756 |  | . 62040 |  | . 98716 |  | . 01284 |
| . 108 | . 60801 |  | . 62083 |  | . 98718 |  | . 01282 |
| . 109 | . 60845 |  | . 62125 |  | . 98721 |  | . 01279 |
| 2.110 | 0.60890 | 44,7 | 0.62167 | 42,2 | 9.98723 | 2,6 | 0.01277 |
| . III | . 60935 |  | . 62209 |  | . 98726 | 2,5 | . 01274 |
| . 112 | . 60979 |  | .62251 |  | . 98728 |  | . 01272 |
| . 113 | . 61024 |  | . 62293 |  | . 98731 |  | . 01269 |
| . 114 | . 61069 |  | . 62336 |  | .98733 |  | . 01267 |
| 2.115 | 0.61114 | 44,7 | 0.62378 | 42,2 | 9.98736 | 2,5 | 0.01264 |
| . 116 | . 61158 |  | . 62420 |  | . 98738 |  | . 01262 |
| . 117 | . 61203 |  | . 62462 |  | . 98741 |  | . 01259 |
| . 118 | . 61248 |  | . 62504 |  | . 98743 |  | . 01257 |
| . 119 | .61292 |  | . 62546 |  | . 98746 |  | . 01254 |
| 2.120 | 0.61337 | 44,7 | 0.62589 | 42,2 | 9.98748 | 2,5 | 0.01252 |
| . 121 | . 61382 |  | . 62631 |  | . 98751 |  | . 01249 |
| . 122 | . 61427 |  | . 62673 |  | . 98753 |  | . 01247 |
| . 123 | . 61471 |  | . 62715 |  | . 98756 |  | . 01244 |
| . 124 | .61516 |  | . 62757 |  | . 98758 |  | . 01242 |
| 2.125 | 0.61561 | 44,7 | 0.62800 | 42,2 | 9.98761 | 2,5 | 0.01239 |
| . 126 | . 61605 |  | . 62842 |  | . 98763 |  | . 01237 |
| . 127 | . 61650 |  | . 62884 |  | . 98766 |  | . 01234 |
| . 128 | . 61695 |  | . 62926 |  | . 98768 |  | . 01232 |
| . 129 | . 61739 |  | . 62969 |  | . 98771 |  | . 01229 |
| 2.130 | 0.61784 | 44,7 | 0.63011 | 42,2 | 9.98773 |  |  |
| .131 | . 61829 |  | . 63053 |  | . 98776 | 2,4 | . 01224 |
| . 132 | . 61873 |  | . 63095 |  | . 98778 |  | . 01222 |
| .133 | . 61918 |  | . 63137 |  | . 98781 |  | . 01219 |
| . 134 | . 61963 |  | . 63180 |  | . 98783 |  | . 01217 |
| 2.135 | 0.62007 | 44,7 | 0.63222 | 42,2 | 9.98785 | 2,4 | 0.01215 |
| . 136 | . 62052 |  | . 63264 |  | . 98788 |  | . 01212 |
| . 137 | . 62097 |  | . 63306 |  | . 98790 |  | . 01210 |
| . 138 | .62141 |  | . 63349 |  | . 98793 |  | . 01207 |
| . 139 | . 62186 |  | . 63391 |  | . 98795 |  | . 01205 |
| 2.140 | 0.62231 | 44,6 | -0.63433 | 42,2 | 9.98798 | 2,4 | 0.01202 |
| . 141 | . 62275 |  | . 63475 |  | . 98800 |  | . 01200 |
| . 142 | . 62320 |  | . 63518 |  | . 98802 |  | . 01198 |
| . 143 | . 62365 |  | . 63560 | 42,3 | . 98805 |  | . 01195 |
| . 144 | . 62409 |  | . 63602 |  | . 98807 |  | . 01193 |
| 2.145 | 0.62454 | 44,6 | 0.63644 | 42,3 | 9.988io | 2,4 | 0.01190 |
| . 146 | . 62498 |  | . 63687 |  | . 98812 |  | . 01188 |
| . 147 | . 62543 |  | . 63729 |  | .98814 |  | . 01186 |
| . 148 | . 62588 |  | . 63771 |  | . 98817 |  | . 01183 |
| . 149 | . 62632 |  | .63813 |  | . 98819 |  | .01181 |
| 2.150 | 0.62677 | 44,6 | 0.63856 | 42,3 | 9.98821 | 2,4 | 0.01179 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \sec$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\mathbf{l o g} \csc$ gd u |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.150 | 0.62677 | 44,6 | 0.63856 | 42,3 | 9.98821 | 2,4 | 0.01179 |
| . 151 | . 62722 |  | . 63898 |  | . 98824 |  | . 01176 |
| . 152 | . 62766 |  | . 63940 |  | . 98825 | 2,3 | . 01174 |
| . 153 | . 62811 |  | . 63982 |  | . 98828 |  | . 01172 |
| . 154 | . 62855 |  | . 64025 |  | . 98831 |  | . 01169 |
| 2.155 | 0.62900 | 44,6 | 0.64067 | 42,3 | 9.98833 | 2,3 | 0.01167 |
| . 156 | . 62945 |  | . 64109 |  | . 98835 |  | . 01165 |
| . 157 | . 62989 |  | . 64152 |  | . 98838 |  | . 01162 |
| . 158 | . 63034 |  | . 64194 |  | . 98840 |  | . 01160 |
| - 159 | . 63079 |  | . 64236 |  | . 98842 |  | . 01158 |
| 2.160 | 0.63123 | 44,6 | 0.64278 | 42,3 | 9.98845 | 2,3 | 0.01155 |
| . 161 | . 63168 |  | . 6432 I |  | . 98847 |  | . 01153 |
| . 162 | . 63212 |  | . 64363 |  | . 98849 |  | . 01151 |
| . 163 | . 63257 |  | . 64405 |  | . 98852 |  | . 01148 |
| . 164 | . 63302 |  | . 64448 |  | . 98854 |  | . 01146 |
| 2. 165 | 0.63346 | 44,6 | 0.64490 | 42,3 | 9.98856 | 2,3 | 0.01144 |
| . 166 | . 63391 |  | . 64532 |  | . 98859 |  | . 01141 |
| . 167 | . 63435 |  | . 64574 |  | .98861 |  | . 01139 |
| . 168 | . 63480 |  | . 64617 |  | . 98853 |  | . 01137 |
| . 169 | . 63524 |  | . 64659 |  | . 98865 |  | . 01135 |
| 2.170 | 0.63569 | 44,6 | 0.64701 | 42,3 | 9.98868 | 2,3 | 0.01132 |
| . 171 | . 63614 |  | . 64744 |  | . 98870 |  | . 01130 |
| . 172 | . 63658 |  | . 64785 |  | . 98872 |  | . 01128 |
| . 173 | . 63703 |  | . 64828 |  | . 98874 |  | . 01126 |
| . 174 | . 63747 |  | . 64871 |  | . 98877 | 2,2 | . 01123 |
| 2. 175 | 0.63792 | 44,6 | 0.64913 | 42,3 | 9.98879 | 2,2 | 0.01121 |
| . 176 | . 63836 |  | . 64955 |  | .9888I |  | . 01119 |
| . 177 | . 63881 |  | . 64998 |  | . 98883 |  | . 01117 |
| . 178 | . 63926 |  | . 65040 |  | . 98886 |  | . 01114 |
| . 179 | . 63970 |  | . 65082 |  | . 98888 |  | .01112 |
| 2. 180 | 0.64015 | 44,6 | 0.65125 | 42,3 | 9.98890 | 2,2 | 0.01110 |
| . 181 | . 64059 |  | . 65167 |  | . 98892 |  | . 01108 |
| . 182 | . 64104 | 44,5 | . 65209 |  | . 98894 |  | . 01106 |
| .183 | . 64148 |  | . 65252 |  | . 98897 |  | . 01103 |
| . 184 | . 64193 |  | . 65294 |  | . 98899 |  | .orioi |
| 2.185 | 0.64237 | 44.5 | 0.65336 | - 42,3 | 9.98901 | 2,2 | 0.01099 |
| . 185 | . 64282 |  | . 65379 |  | . 98903 |  | . 01097 |
| . 187 | . 64326 |  | . 65421 | 42,4 | . 98905 |  | . 01095 |
| . 188 | . 64371 |  | . 65463 |  | . 98908 |  | . 01092 |
| . 189 | . 64416 |  | . 65506 |  | . 98910 |  | . 01090 |
| 2. 190 | 0.64460 | 44,5 | 0. 65548 | 42,4 | 9.98912 | 2,2 | 0.01088 |
| . 191 | . 64505 |  | . 65590 |  | . 98914 |  | . 01086 |
| . 192 | . 64549 |  | . 65633 | - | . 98916 |  | . 01084 |
| . 193 | . 64594 |  | . 65675 |  | . 98919 |  | . 01081 |
| . 194 | . 64638 |  | . 65718 |  | . 9892 I |  | . 01079 |
| 2. 195 | 0.64683 | 44,5 | 0.65760 | 42,4 | 9.98923 | 2,2 | 0.01077 |
| . 196 | . 64727 |  | . 65802 |  | . 98925 |  | . 01075 |
| . 197 | . 64772 |  | . 65845 |  | - 08927 | 2,1 | . 01073 |
| . 198 | . 64816 |  | . 65887 |  | . 98929 |  | . 01071 |
| . 199 | . 64861 |  | . 65929 |  | .9893r |  | . 01069 |
| 2.200 | 0.64905 | 44,5 | 0.65972 | 42,4 | 9.98934 | 2,1 | 0.01066 |
| $u$ | 10 tan gd u | ar $\mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log $\sin \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \mathrm{csc} \mathrm{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.200 | 0.64905 | 44,5 | 0.65972 | 42,4 | 9.98934 | 2,1 | 0.01066 |
| . 201 | . 64950 |  | . 66014 |  | . 98936 |  | . 01064 |
| . 202 | . 64994 |  | . 66056 |  | . 98938 |  | . 01062 |
| . 203 | . 65039 |  | . 66099 |  | . 98940 |  | . 01060 |
| . 204 | . 65083 |  | .6614I |  | . 98942 |  | . 01058 |
| 2.205 | 0.65128 | 44,5 | 0.66184 | 42,4 | 9.98944 | 2,I | 0.01056 |
| . 206 | . 65172 |  | . 66226 |  | . 98946 |  | . 01054 |
| . 207 | . 65217 |  | . 66268 |  | . 98948 |  | . 01052 |
| . 208 | . 65261 |  | . 663 I I |  | . 98950 |  | . 01050 |
| . 209 | .65306 |  | . 66353 |  | . 98953 |  | . 01047 |
| 2.210 | 0.65350 | 44,5 | 0.66396 | 42,4 | 9.98955 | 2, I | 0.01045 |
| . 211 | . 65395 |  | . 66438 |  | . 98957 |  | . 01043 |
| . 212 | . 65439 |  | . 66480 |  | - 98959 |  | . 01041 |
| . 213 | . 65484 |  | . 66523 |  | . 98961 |  | . 01039 |
| . 214 | . 65528 |  | . 66565 |  | . 98963 |  | . 01037 |
| 2.215 | 0.65573 | 44,5 | 0.66608 | 42,4 | 9.98965 | 2,I | 0.01035 |
| . 216 | . 65617 |  | . 66650 |  | . 98967 |  | . 01033 |
| . 217 | . 65662 |  | . 66692 |  | . 98969 |  | .01031 |
| . 218 | . 65706 |  | . 66735 |  | . 98971 |  | . 01029 |
| . 219 | . 6575 I |  | . 66777 |  | . 98973 |  | . 01027 |
| 2.220 | 0.65795 | 44,5 | 0.66820 | 42,4 | 9.98975 | 2,0 | 0.01025 |
| . 22 I | . 65840 |  | . 66862 |  | . 98977 |  | . 01023 |
| . 222 | . 65884 |  | . 66905 |  | . 98979 |  | . 01021 |
| . 223 | . 65928 |  | . 66947 |  | . 98982 |  | . 01018 |
| . 224 | . 65973 |  | . 66989 |  | . 98984 |  | . 01016 |
| 2.225 | 0.66017 | 44.5 | 0.67032 | 42,4 | 9.98986 | 2,0 | 0.01014 |
| . 225 | . 66062 |  | . 67074 |  | . 98988 |  | . 01012 |
| . 227 | .66106 |  | . 67117 |  | . 98990 |  | . 01010 |
| . 223 | .6615I | 44,4 | . 67159 |  | . 98992 |  | . 01008 |
| . 229 | .66195 |  | . 67202 |  | . 98994 |  | . 01006 |
| 2.230 | 0.66240 | 44,4 | 0.67244 | 42,4 | 9.98996 | 2,0 | 0.01004 |
| . 231 | . 66284 |  | . 67285 |  | . 98998 |  | . 01002 |
| . 232 | . 66328 |  | . 67329 |  | . 99000 |  | . 01000 |
| . 233 | . 66373 |  | . 6737 I |  | . 99002 |  | . 00998 |
| . 234 | .66417 |  | . 67414 |  | . 99004 |  | . 00996 |
| 2.235 | 0.66462 | 44,4 | 0.67456 | 42,4 | 9.99006 | 2,0 | 0.00994 |
| . 236 | . 66506 |  | . 67499 |  | . 99008 |  | . 00992 |
| . 237 | . 66551 |  | . 67541 | 42,5 | . 99010 |  | . 00990 |
| . 238 | . 66595 |  | . 67583 |  | . 99012 |  | . 00988 |
| . 239 | . 66640 |  | .67626 |  | . 99014 |  | . 00986 |
| 2.240 | 0.66684 | 44,4 | 0.67668 | 42,5 | 9.99016 | 2,0 | 0.00984 |
| . 241 | . 66728 |  | . 67711 |  | . 99018 |  | . 00982 |
| . 242 | . 66773 |  | . 67753 |  | . 99019 |  | .00981 |
| . 243 | .668I7 |  | . 67796 |  | . 99021 |  | . 00979 |
| . 244 | . 66862 |  | . 67838 |  | . 99023 |  | . 00977 |
|  | 0.66906 | 44,4 |  | 42,5 |  | I,9 | 0.00975 |
| . 246 | . 66950 |  | . 67923 |  | . 99027 |  | . 00973 |
| . 247 | . 66995 |  | . 67966 |  | . 99029 |  | . 00971 |
| . 248 | . 67039 |  | . 68008 |  | . 99031 |  | . 00969 |
| . 249 | . 67084 |  | .6805I |  | . 99033 |  | . 00967 |
| 2.250 | 0.67128 | 44,4 | 0.68093 | 42,5 | 9.99035 | 1,9 | 0.00965 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { l o g }} \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega F_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.250 | 0.67128 | 44,4 | 0.68093 | 42,5 | 9.99035 | I,9 | 0.00965 |
| . 251 | . 67173 |  | .68ı36 |  | .99037 |  | . 00963 |
| . 252 | . 67217 |  | .68ı78 |  | . 99039 |  | .00961 |
| . 253 | . 67261 |  | . 68220 |  | . 9904 I |  | . 00959 |
| . 254 | . 67306 |  | . 68263 |  | . 99043 |  | . 00957 |
| 2.255 | 0.67350 | 44,4 | 0.68305 | 42,5 | 9.99045 | I,9 | 0.00955 |
| . 256 | . 67394 |  | . 68348 |  | . 99047 |  | . 00953 |
| . 257 | . 67439 |  | . 68390 |  | . 99048 |  | . 00952 |
| . 258 | .67483 |  | . 68433 |  | . 99050 |  | . 00950 |
| . 259 | . 67528 |  | . 68475 |  | . 99052 |  | . 00948 |
| 2.260 | 0.67572 | 44,4 | 0.68518 | 42,5 | 9.99054 | I,9 | 0.00946 |
| . 261 | . 67616 |  | . 68560 |  | . 99056 |  | . 00944 |
| . 262 | . 67661 |  | . 68603 |  | . 99058 |  | . 00942 |
| . 263 | . 67705 |  | . 68645 |  | . 99060 |  | . 00940 |
| . 264 | . 67750 |  | . 68688 |  | . 99062 |  | . 00938 |
| 2.265 | 0.67794 | 44,4 | 0.68730 | 42,5 | 9.99064 | 1,9 | 0.00936 |
| . 266 | . 67838 |  | . 68773 |  | . 99065 |  | . 00935 |
| .267 | . 67883 |  | .68815 |  | . 99067 |  | . 00933 |
| . 268 | . 67927 |  | . 68858 |  | . 99069 |  | . 0093 I |
| .269 | . 67971 |  | . 68900 |  | . 9907 I |  | . 00929 |
| 2.270 | 0.68016 | 44,4 | 0.68943 | 42,5 | 9.99073 | I,9 | 0.00927 |
| . 271 | . 68060 |  | . 68985 |  | . 99075 |  | . 00925 |
| . 272 | .68105 |  | . 69028 |  | . 99077 | I,8 | . 00923 |
| .273 | .68149 |  | . 69070 |  | . 99078 |  | . 00922 |
| . 274 | .68193 |  | . 69113 |  | . 99080 |  | . 00920 |
| 2.275 | 0.68238 | 44,4 | 0.69156 | 42,5 | 9.99082 | 1,8 | 0.00918 |
| . 276 | . 68282 |  | . 69198 |  | . 99084 |  | . 00916 |
| . 277 | . 68326 |  | . 6924 I |  | . 99086 |  | . 00914 |
| . 278 | .68371 |  | . 69283 |  | . 99088 |  | . 00912 |
| . 279 | . 68415 | 44,3 | .69326 |  | . 99089 | - | .009II |
| 2.280 | 0.68459 | 44,3 | 0.69368 | 42,5 | 9.99091 | 1,8 | 0.00909 |
| .281 | . 68504 |  | . 6941 I |  | . 99093 |  | . 00907 |
| . 282 | . 68548 |  | . 69453 |  | . 99095 |  | . 00905 |
| .283 | . 68592 |  | . 69496 |  | . 99097 |  | . 00903 |
| .284 | . 68637 |  | . 69538 |  | . 99098 |  | . 00902 |
| 2.285 | 0.6868I | 44,3 | 0.69581 | 42,5 | 9.99100 | 1,8 | 0.00900 |
| . 286 | . 68725 |  | . 69623 |  | . 99102 |  | . 00898 |
| . 287 | .68770 |  | . 69666 |  | . 99104 |  | . 00896 |
| . 288 | .68814 |  | . 69708 |  | .99106 |  | . 00894 |
| . 289 | . 68858 |  | . 69751 |  | .99107 |  | . 00893 |
| 2.290 | 0.68903 | 44,3 | 0.69794 | 42,5 | 9.99109 | I,8 | 0.00891 |
| . 291 | . 68947 |  | . 69836 |  | . 99111 |  | . 00889 |
| . 292 | . 68991 |  | . 69879 | 42,6 | . 99113 |  | . 00887 |
| . 293 | . 69036 |  | . 69921 |  | .99115 |  | . 00885 |
| . 294 | . 69080 |  | . 69964 |  | .99116 |  | . 00884 |
| 2.295 | 0.69124 | 44,3 | 0.70006 | 42,6 | 9.99118 | 1,8 | 0.00882 |
| . 296 | . 69169 |  | . 70049 |  | . 99120 |  | . 00880 |
| . 297 | . 69213 |  | . 70091 |  | . 99122 |  | . 00878 |
| . 298 | . 69257 |  | . 70134 |  | . 99123 |  | . 00877 |
| . 299 | . 69302 |  | .70177 |  | . 99125 | 1,7 | . 00875 |
| 2.300 | 0.69346 | 44,3 | 0.70219 | 42,6 | 9.99127 | I,7 | 0.00873 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.300 | 0.69346 | 44,3 | 0.70219 | 42,6 | 9.99127 | 1,7 | 0.00873 |
| . 301 | . 69390 |  | . 70262 |  | . 99129 |  | . 00871 |
| . 302 | . 69435 |  | . 70304 |  | . 99130 |  | . 00870 |
| . 303 | . 69479 |  | . 70347 |  | . 99132 |  | . 00868 |
| . 304 | . 69523 |  | . 70389 |  | .99134 |  | . 00866 |
| 2.305 | 0. 69568 | 44,3 | 0.70432 | 42,6 | 9.99136 | 1,7 | 0.00864 |
| . 306 | . 69612 |  | . 70475 |  | . 99137 |  | . 00863 |
| . 307 | . 69656 |  | . 70517 |  | .99139 |  | . 00861 |
| . 308 | . 69700 |  | . 70560 |  | .9914I |  | . 00859 |
| . 309 | . 69745 |  | .70602 |  | . 99142 |  | . 00858 |
| 2.310 | 0.69789 | 44,3 | 0.70645 | 42,6 | 9.99144 | 1,7 | 0.00856 |
| . 3 II | . 69833 |  | . 70687 |  | . 99146 |  | . 00854 |
| . 312 | . 69878 |  | . 70730 |  | . 99148 |  | . 00852 |
| . 313 | . 69922 |  | . 70773 |  | . 99149 |  | . 00851 |
| . 314 | . 69966 |  | . 708 I 5 |  | .99151 |  | . 00849 |
| 2.315 | 0.70010 | 44,3 | 0.70858 | 42,6 | 9.99153 | 1,7 | 0.00847 |
| . 316 | . 70055 |  | . 70900 |  | .99154 |  | . 00846 |
| -317 | . 70099 |  | . 70943 |  | .99156 |  | . 00844 |
| . 318 | . 70143 |  | . 70986 |  | . 99158 |  | . 00842 |
| . 319 | . 70188 |  | . 71028 |  | .99159 |  | . 00841 |
| 2.320 | 0.70232 | 44,3 | 0.71071 | 42,6 | 9.99161 | 1,7 | 0.00839 |
| . 321 | . 70276 |  | .71113 |  | .99163 |  | . 00837 |
| . 322 | . 70320 |  | .71156 |  | . 99164 |  | . 00836 |
| . 323 | . 70365 |  | .71199 |  | .99166 |  | . 00834 |
| . 324 | . 70409 |  | .71241 |  | .99168 |  | . 00832 |
| 2.325 | 0.70453 | 44,3 | 0.71284 | 42,6 | 9.99169 | 1,7 | 0.00831 |
| . 326 | . 70497 |  | . 71326 |  | .99171 |  | . 00829 |
| . 327 | . 70542 |  | . 71369 |  | . 99173 |  | . 00827 |
| . 328 | . 70586 |  | . 71412 |  | . 99174 |  | . 00826 |
| . 329 | . 70630 |  | . 717454 |  | .99176 | 1,6 | . 00824 |
| -2.330 | 0.70675 | 44,3 | 0.71497 | 42,6 | 9.99178 | 1,6 | 0.00822 |
| . 331 | . 70719 |  | . 71539 | . | .99179 |  | . 00821 |
| . 332 | . 70763 |  | . 71582 |  | .99181 |  | .00819 |
| . 333 | . 70807 |  | . 71625 |  | .99183 |  | .00817 |
| . 334 | . 70852 |  | .71667 |  | . 99184 |  | .00816 |
| 2.335 | 0.70896 |  | 0.71710 | 42,6 | 9.99186 | 1,6 | 0.00814 |
| . 336 | . 70940 | 44,2 | . 71753 |  | . 99188 |  | .008í 2 |
| . 337 | . 70984 |  | . 71795 |  | . 99189 |  | .008II |
| . 338 | .71029 |  | . 71838 |  | .99191 |  | . 00809 |
| . 339 | . 71073 |  | . 71880 |  | . 99192 |  | . 00808 |
| 2.340 | 0.71117 | 44,2 | 0.71923 | 42,6 | 9.99194 | 1,6 | 0.00806 |
| . 341 | .71161 |  | . 71966 |  | . 99196 |  | . 00804 |
| . 342 | . 71206 |  | . 72008 |  | . 99197 |  | . 00803 |
| . 343 | . 71250 |  | . 72051 |  | . 99199 |  | . 00801 |
| . 344 | . 71294 |  | . 72094 |  | . 99200 |  | . 00800 |
| 2.345 | 0.71338 | 44,2 | 0.72136 | 42,6 | 9.99202 | 1,6 | 0.00798 |
| . 346 | -71382 |  | . 72179 |  | . 99204 |  | . 00796 |
| - 347 | . 71427 |  | . 72221 |  | . 99205 |  | . 00795 |
| - 348 | . 71471 |  | . 72264 |  | . 99207 | 1 | . 00793 |
| . 349 | .71515 |  | . 72307 |  | . 99208 |  | . 00792 |
| 2.350 | 0.71559 | 44,2 | 0.72349 | 42,6 | 9.99210 | I,6 | 0.00790 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin g d u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.350 | 0.71559 | 44,2 | 0.72349 | 42,6 | 9.99210 | I,6 | 0.00790 |
| . 351 | . 71604 |  | . 72392 |  | . 99212 |  | . 00788 |
| . 352 | . 71648 |  | . 72435 |  | . 99213 |  | . 00787 |
| . 353 | . 71692 |  | . 72477 | 42,7 | . 99215 |  | . 00785 |
| . 354 | . 71736 |  | . 72520 |  | . 992 I6 |  | . 00784 |
| 2.355 | 0.7178 I | 44,2 | 0.72563 | 42,7 | 9.99218 | 1,6 | 0.00782 |
| . 356 | . 71825 |  | . 72605 |  | . 99219 |  | .00781 |
| . 357 | . 71869 |  | . 72648 |  | -9922I |  | . 00779 |
| . 358 | . 71913 |  | -72691 |  | -99223 |  | . 00777 |
| . 359 | . 71957 |  | . 72733 |  | - 99224 |  | . 00776 |
| 2.360 | 0.72002 | 44,2 | 0.72776 | 42,7 | 9.99226 | 1,5 | 0.00774 |
| . 361 | . 72046 |  | . 72819 |  | . 99227 |  | . 00773 |
| . 362 | . 72090 |  | . 72861 |  | . 99229 |  | . 00771 |
| . 363 | . 72134 |  | . 72904 |  | -99230 |  | . 00770 |
| . 364 | . 72178 |  | . 72947 |  | . 99232 |  | .00768 |
| 2.365 | 0.72223 | 44,2 | 0.72989 | 42,7 | 9.99233 | 1,5 | 0.00767 |
| . 366 | . 72267 |  | . 73032 |  | . 99235 |  | . 00765 |
| . 367 | . 72311 |  | . 73075 |  | . 99236 |  | . 00764 |
| . 368 | . 72355 |  | . 73117 |  | - 99238 |  | . 00762 |
| . 369 | . 72399 |  | .73160 |  | -99239 |  | .00761 |
| 2.370 | 0.72444 | 44,2 | 0.73203 | 42,7 | 9.9924 I | 1,5 | 0.00759 |
| . 371 | . 72488 |  | . 73245 |  | . 99242 |  | . 00758 |
| . 372 | . 72532 |  | . 73288 |  | . 99244 |  | . 00756 |
| . 373 | . 72576 |  | .73331 |  | . 99245 |  | . 00755 |
| . 374 | . 72620 |  | . 73373 |  | . 9924 |  | . 00753 |
| 2.375 | 0.72665 | 44,2 | 0.73416 | 42,7 | 9.99249 | 1,5 | 0.00751 |
| . 376 | . 72709 |  | . 73459 |  | . 99250 |  | . 00750 |
| . 377 | . 72753 |  | . 73501 |  | . 99252 |  | . 00748 |
| . 378 | . 72797 |  | . 73544 |  | . 99253 |  | . 00747 |
| -379 | .7284I |  | . 73587 |  | . 99254 |  | . 00746 |
| 2.380 | 0.72885 | 44,2 | 0.73630 | 42,7 | 9.99256 | I,5 | 0.00744 |
| .381 | . 72930 |  | . 73672 |  | . 99257 |  | . 00743 |
| . 382 | . 72974 |  | . 73715 |  | . 99259 |  | .00741 |
| . 383 | . 73018 |  | . 73758 |  | . 99260 |  | . 00740 |
| . 384 | . 73062 |  | . 73800 |  | . 99262 |  | . 00738 |
| 2.385 | 0.73106 | 44,2 | 0.73843 | 42,7 | 9.99263 | 1,5 | 0.00737 |
| . 386 | .7315I |  | . 73886 |  | . 99265 |  | . 00735 |
| . 387 | . 73195 |  | . 73928 |  | . 99266 |  | . 00734 |
| -388 | . 73239 |  | . 73971 |  | . 99268 |  | . 00732 |
| . 389 | . 73283 |  | . 74014 |  | - 99269 |  | . 00731 |
| 2.390 | 0.73327 | 44,2 | 0.74056 | 42,7 | 9.9927 I | 1,5 | 0.00729 |
| -391 | . 73371 |  | . 74099 |  | . 99272 |  | . 00728 |
| - 392 | . 73416 |  | . 74142 |  | - 99274 |  | . 00726 |
| - 393 | . 73460 |  | . 74185 |  | . 99275 | 1,4 | . 00725 |
| - 394 | . 73504 |  | . 74227 |  | . 99277 |  | . 00723 |
| 2.395 | 0.73548 | 44,2 | 0.74270 | 42,7 | 9.99278 | 1,4 | 0.00722 |
| . 396 | . 73592 |  | . 743 I 3 |  | . 99279 |  | . 00721 |
| - 397 | . 73636 |  | . 74355 |  | .9928I |  | . 00719 |
| - 398 | . 73680 |  | . 74398 |  | - 99282 |  | . 00718 |
| - 399 | . 73725 |  | .74441 |  | . 99284 |  | . 00716 |
| 2.400 | 0.73769 | 44,2 | 0.74484 | 42,7 | 9.99285 | 1,4 | 0.00715 |
| $u$ | log tan gd u | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | log sec gd u | $\omega \mathrm{Fo}^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | log csc od u |

Logarithms of Hyperbolic Functions.

| U | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.400 | 0.73769 | 44,2 | 0.74484 | 42,7 | 9.99285 | I,4 | 0.00715 |
| . 401 | .73813 | 44,1 | . 74526 |  | . 99287 |  | . 00713 |
| . 402 | . 73857 |  | . 74569 |  | . 99288 |  | . 00712 |
| . 403 | . 73901 |  | . 74612 |  | . 99289 |  | .00711 |
| . 404 | . 73945 |  | . 74655 |  | .9929I |  | . 00709 |
| 2.405 | 0.73990 | 44, I | 0.74697 | 42,7 | 9.99292 | I,4 | 0.00708 |
| . 406 | . 74034 |  | . 74740 |  | . 99294 |  | . 00706 |
| . 407 | . 74078 |  | . 74783 |  | . 99295 |  | . 00705 |
| . 408 | .74122 |  | . 74825 |  | . 99297 |  | . 00703 |
| . 409 | .74166 |  | . 74868 |  | . 99298 |  | . 00702 |
| 2.410 | 0.74210 | 44,1 | 0.74911 | 42,7 | 9.99299 | 1,4 | 0.00701 |
| .4II | . 74254 |  | . 74954 |  | .99301 |  | . 00699 |
| . 412 | . 74298 |  | . 74996 |  | . 99302 |  | . 00698 |
| . 413 | . 74343 |  | . 75039 |  | . 99304 |  | . 00696 |
| .4I4 | . 74387 |  | . 75082 |  | . 99305 |  | . 00695 |
| 2.415 | 0.74431 | 44, I | 0.75125 | 42,7 | 9.99306 | I,4 | 0.00694 |
| . 416 | . 74475 |  | .75167 |  | . 99308 |  | . 00692 |
| . 417 | . 74519 |  | . 75210 |  | . 99309 |  | .0069I |
| . 418 | .74563 |  | . 75253 |  | . 99310 |  | . 00690 |
| .419 | .74607 |  | . 75296 |  | . 99312 |  | . 00688 |
| 2.420 | 0.74652 | 44, 1 | 0.75338 | 42,7 | 9.993I3 | I,4 | 0.00687 |
| . 421 | . 74696 |  | .75381 |  | . 99315 |  | . 00685 |
| . 422 | . 74740 |  | . 75424 | 42,8 | . 99316 |  | . 00684 |
| . 423 | . 74784 |  | . 75467 |  | . 99317 |  | . 00683 |
| . 424 | . 74828 |  | . 75509 |  | .99319 |  | . 0068 I |
| 2.425 | 0.74872 | 44,1 | 0.75552 | 42,8 | 9.99320 | 1,4 | 0.00680 |
| . 426 | . 74916 |  | . 75595 |  | . 9932 I |  | . 00679 |
| . 427 | . 74960 |  | . 75638 |  | . 99323 |  | . 00677 |
| . 428 | . 75004 |  | . 75680 |  | . 99324 |  | . 00676 |
| . 429 | . 75049 |  | . 75723 |  | . 99325 | I,3 | . 00675 |
| 2.430 | 0.75093 | 44, 1 | 0.75766 | 42,8 | 9.99327 | 1,3 | 0.00673 |
| . 431 | .75137 |  | . 75809 |  | . 99328 |  | . 00672 |
| . 432 | .7518I |  | .7585I |  | . 99329 |  | . 00671 |
| . 433 | . 75225 |  | . 75894 |  | .9933I |  | . 00669 |
| . 434 | . 75269 |  | . 75937 |  | . 99332 |  | . 00668 |
| 2.435 | 0.75313 | 44, 1 | 0.75980 | 42,8 | 9.99333 | 1,3 | 0.00667 |
| . 436 | . 75357 |  | . 76022 |  | . 99335 |  | . 00665 |
| . 437 | .75401 |  | . 76065 |  | . 99336 |  | . 00664 |
| . 438 | . 75445 |  | .76108 |  | . 99337 |  | . 00663 |
| . 439 | . 75490 |  | .76151 |  | . 99339 |  | . 00661 |
| 2.440 | 0.75534 | 44,1 | 0.76194 | 42,8 | 9.99340 | I,3 | 0.00660 |
| . 441 | . 75578 |  | . 76236 |  | . 9934 I |  | . 00659 |
| . 442 | . 75622 |  | . 76279 |  | . 99343 |  | . 00657 |
| . 443 | . 75666 |  | . 76322 |  | . 99344 |  | . 00656 |
| . 444 | . 75710 |  | . 76365 |  | . 99345 |  | . 00655 |
| 2.445 | 0.75754 | 44, 1 | 0.76407 | 42,8 | 9.99347 | I,3 | 0.00653 |
| . 446 | .75798 |  | . 76450 |  | . 99348 |  | . 00652 |
| . 447 | . 75842 |  | . 76493 |  | . 99349 |  | .0065I |
| . 448 | . 75886 |  | . 76536 |  | . 9935 I |  | $.00649$ |
| . 449 | . 75930 |  | . 76579 |  | . 99352 |  | . 00648 |
| 2.450 | 0.75975 | 44, I | 0.76621 | 42,8 | 9.99353 | I,3 | 0.00647 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \cdot F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.450 | 0.75975 | 44, I | 0.76621 | 42,8 | 9.99353 | 1,3 | 0.00647 |
| . 451 | . 76019 |  | . 76664 |  | . 99354 |  | . 00646 |
| . 452 | . 76063 |  | . 76707 |  | . 99356 |  | . 00644 |
| . 453 | . 76107 |  | . 76750 |  | -99357 |  | . 00643 |
| . 454 | .76151 |  | . 76793 |  | . 99358 |  | . 00642 |
| 2.455 | 0.76195 | 44,1 | 0.76835 | 42,8 | 9.99360 | I,3 | 0.00640 |
| . 456 | . 76239 |  | . 76878 |  | . 99361 |  | . 00639 |
| . 457 | . 76283 |  | . 76921 |  | . 99362 |  | . 00638 |
| . 458 | . 76327 |  | . 76964 |  | -. 99363 |  | . 00637 |
| . 459 | . 76371 |  | . 77006 |  | . 99365 |  | . 00635 |
| 2.460 | 0.76415 | 44, I | 0.77049 | 42,8 | 9.99366 | 1,3 | 0.00634 |
| . 461 | . 76459 |  | . 77092 |  | . 99367 |  | . 00633 |
| . 462 | . 76503 |  | . 77135 |  | -99369 |  | . 00631 |
| . 463 | . 76547 |  | . 77178 |  | . 99370 |  | . 00630 |
| . 464 | . 76592 |  | . 77220 |  | . 99371 |  | . 00629 |
| 2.465 | 0.76636 | 44,1 | 0.77263 | 42,8 | 9.99372 | I,3 | 0.00628 |
| . 466 | . 76680 |  | . 77306 |  | . 99374 |  | . 00626 |
| . 467 | . 76724 |  | . 77349 |  | . 99375 |  | . 00625 |
| -468 | . 76768 |  | . 77392 |  | -99376 | 1,2 | . 00662 |
| . 469 | .76812 |  | . 77435 |  | -99377 |  | . 00623 |
| 2.470 | 0.76856 | 44,1 | 0.77477 | 42,8 | 9.99379 | 1,2 | 0.00621 |
| .471 | . 76900 |  | . 77520 |  | . 99380 |  | . 00620 |
| . 472 | . 76944 |  | . 77563 |  | .99381 |  | . 00619 |
| . 473 | . 76988 |  | . 77606 |  | . 99382 |  | . 00618 |
| . 474 | . 77032 |  | . 77649 |  | -99384 |  | . 00616 |
| 2.475 | 0.77076 | 44,0 | 0.77691 | 42,8 | 9.99385 | 1,2 | 0.00615 |
| . 476 | . 77120 |  | . 77734 |  | . 99386 |  | . 00614 |
| . 477 | . 77164 |  | . 77777 |  | . 99387 |  | . 006613 |
| . 478 | . 77208 |  | . 77820 |  | . 99388 |  | . 00612 |
| . 479 | . 77252 |  | . 77863 |  | . 99390 |  | . 00610 |
| 2.480 | 0.77296 | 44,0 | 0.77906 | 42,8 | 9.99391 | 1,2 | 0.00609 |
| .481 | . 77340 |  | . 77948 |  | . 99392 |  | . 00608 |
| . 482 | . 77384 |  | . 77991 |  | -99393 |  | . 00607 |
| . 483 | . 77429 |  | . 78034 |  | -99394 |  | . 00606 |
| . 484 | . 77473 |  | . 78077 |  | . 99396 |  | . 00604 |
| 2.485 | 0.77517 | 44,0 | 0.78120 | 42,8 | 9.99397 | 1,2 | 0.00603 |
| . 486 | . 7756 r |  | .78163 |  | . 99398 |  | . 00602 |
| . 487 | . 77605 |  | . 78205 |  | . 99399 |  | . 00601 |
| . 488 | . 77649 |  | . 78248 |  | . 99401 |  | $.00599$ |
| . 489 | . 77693 |  | . 78292 |  | . 99402 |  | . 00598 |
| 2.490 | 0.77737 | 44,0 | 0.78334 | 42,8 | 9.99403 | 1,2 | 0.00597 |
| . 491 | .77781 |  | . 78377 |  | . 99404 |  | . 00596 |
| - 492 | . 77825 |  | . 78420 | , | . 99405 |  | . 00595 |
| - 493 | . 77869 |  | . 78462 |  | . 99406 |  | . 00594 |
| -494 | . 77913 |  | . 78505 |  | -99408 |  | . 00592 |
| 2.495 | 0.77957 | 44,0 | 0.78548 | 42,8 | 9.99409 | 1,2 | 0.00591 |
| . 496 | . 78001 |  | . 78591 |  | .99410 |  | . 00590 |
| . 497 | . 78045 |  | . 78634 |  | . 9941 I |  | . 00589 |
| . 498 | $\bullet .78089$ |  | . 78677 |  | . 99412 |  | .00588 |
| . 499 | .78133 |  | . 78719 |  | . 99414 |  | . 00586 |
| 2.500 | 0.78177 | 44,0 | 0.78762 | 42,8 | 9.99415 | 1,2 | 0.00585 |
| u | $\log \tan \mathrm{ad} u$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | log sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log csc gdu |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.500 | 0.78177 | 44,0 | 0.78762 | 42,8 | 9.99415 | I,2 | 0.00585 |
| . 501 | . 78221 |  | .78803 |  | . 99416 |  | . 00584 |
| . 502 | . 78265 |  | . 78848 | 42,9 | . 99417 |  | . 00583 |
| . 503 | . 78309 |  | .78891 |  | . 99418 |  | . 00582 |
| . 504 | . 78353 |  | . 78934 |  | . 99419 |  | . 0058 I |
| 2.505 | 0.78397 | 44,0 | 0.78977 | 42,9 | 9.99421 | 1,2 | 0.00579 |
| . 506 | . 78441 |  | . 79019 |  | . 99422 |  | . 00578 |
| . 507 | . 78485 |  | . 79062 |  | . 99423 |  | . 00577 |
| . 508 | . 78529 |  | . 79105 |  | . 99424 |  | . 00576 |
| . 509 | . 78573 |  | .79148 |  | . 99425 | I, I | . 00575 |
| 2.510 | 0.78617 | 44,0 | 0.79191 | 42,9 | 9.99426 | I, I | 0.00574 |
| .51I | .7866I |  | -79234 |  | . 99427 |  | . 00573 |
| . 512 | . 78705 |  | . 79277 |  | . 99429 |  | . 0057 I |
| . 513 | . 78749 |  | . 79319 |  | . 99430 |  | . 00570 |
| . 514 | . 78793 |  | . 79362 |  | . 9943 I |  | . 00569 |
| 2.515 | 0.78837 | 44,0 | 0.79405 | 42,9 | 9.99432 | I,I | 0.00568 |
| . 516 | . 7888 I |  | . 79448 |  | . 99433 |  | . 00567 |
| . 517 | . 78925 |  | .7949I |  | . 99434 |  | . 00566 |
| . 518 | . 78969 |  | . 79534 |  | . 99435 |  | . 00565 |
| . 519 | . 79013 |  | . 79577 |  | .99437 |  | . 00563 |
| 2.520 | 0.79057 | 44,0 | 0.79619 | 42,9 | 9.99438 | I, I | 0.00562 |
| . 521 | .79101 |  | . 79662 |  | . 99439 |  | .0056I |
| . 522 | . 79145 |  | . 79705 |  | . 99440 |  | . 00560 |
| . 523 | . 79189 |  | . 79748 |  | . 9944 I |  | . 00559 |
| . 524 | . 79233 |  | .79791 |  | . 99442 |  | . 00558 |
| 2.525 | 0.79277 | 44,0 | 0.79834 | 42,9 | 9.99443 | I, I | 0.00557 |
| . 526 | . 7932 I |  | . 79877 |  | . 99444 |  | . 00556 |
| . 527 | . 79365 |  | . 79920 |  | . 99446 |  | . 00554 |
| . 528 | . 79409 |  | . 79962 |  | . 99447 |  | . 00553 |
| . 529 | . 79453 |  | . 80005 |  | . 99448 |  | . 00552 |
| 2.530 | 0.79497 | 44,0 | 0.80048 | 42,9 | 9.99449 | I, I | 0.00551 |
| . 531 | . 7954 I |  | . 80091 |  | . 99450 |  | . 00550 |
| . 532 | . 79585 |  | . 80134 |  | .9945I |  | . 00549 |
| . 533 | . 79629 |  | . 80177 |  | . 99452 |  | . 00548 |
| . 534 | . 79673 |  | . 80220 |  | . 99453 | - | . 00547 |
| 2.535 | 0.79717 | 44,0 | 0.80263 | 42,9 | 9.99454 | I, I | 0.00546 |
| . 536 | .7976I |  | . 80306 |  | . 99455 |  | . 00545 |
| . 537 | . 79805 |  | . 80348 |  | . 99456 |  | . 00544 |
| . 538 | . 79849 |  | . 80391 |  | . 99458 |  | . 00542 |
| . 539 | . 79893 |  | . 80434 |  | . 99459 |  | . 00541 |
| 2.540 | 0.79937 | 44,0 | 0.80477 | 42,9 | 9.99460 | I, I | 0.00540 |
| . 54 I | . 7998 I |  | . 80520 |  | . 99461 |  | . 00539 |
| . 542 | . 80025 |  | . 80563 |  | . 99462 |  | . 00538 |
| . 543 | . 80069 |  | . 80606 |  | . 99463 |  | . 00537 |
| . 544 | . 80113 |  | . 80649 |  | . 99464 |  | . 00536 |
| 2. 545 | 0.80157 | 44,0 | 0.80692 | 42,9 | 9.99465 | I, I | 0.00535 |
| . 546 | . 80201 |  | . 80734 |  | . 99466 |  | . 00534 |
| . 547 | . 80245 |  | . 80777 |  | . 99467 |  | . 00533 |
| . 548 | . 80289 |  | . 80820 |  | . 99468 |  | . 00532 |
| . 549 | . 80333 |  | . 80863 |  | . 99469 |  | . 00531 |
| 2.550 | 0.80377 | 44,0 | 0.80906 | 42,9 | 9.99470 | I, I | 0.00530 |
| u | $\log \tan \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.550 | 0.80377 | 44,0 | 0.80906 | 42,9 | 9.99470 | I,I | 0.00530 |
| . 55 I | . 80420 |  | . 80949 |  | . 9947 I |  | . 00529 |
| . 552 | . 80464 |  | :80992 |  | . 99473 |  | . 00527 |
| . 553 | . 80508 |  | . 81035 |  | . 99474 |  | . 00526 |
| . 554 | . 80552 |  | .81078 |  | . 99475 |  | . 00525 |
| 2.555 | 0.80596 | 44,0 | 0.81121 | 42,9 | 9.99476 | 1,0 | 0.00524 |
| . 556 | . 80640 |  | .81164 |  | . 99477 |  | . 00523 |
| . 557 | . 80684 |  | -. 81206 |  | . 99478 |  | . 00522 |
| . 558 | . 80728 |  | . 81249 |  | . 99479 |  | .00521 |
| . 559 | . 80772 |  | .81292 |  | . 99480 |  | . 00520 |
| 2.560 | 0.80816 | 44,0 | 0.81335 | 42,9 | 9.99481 | I,O | 0.00519 |
| . 56 I | . 80860 |  | . 81378 |  | . 99482 |  | . 00518 |
| . 562 | . 80904 | 43,9 | .8142I |  | .99483 |  | .00517 |
| . 563 | . 80948 |  | .81464 |  | . 99484 |  | .00516 |
| . 564 | . 80992 |  | .81507 |  | . 99485 |  | . 00515 |
| 2.565 | 0.81036 | 43,9 | 0.81550 | 42,9 | 9.99486 | 1,0 | 0.00514 |
| . 566 | .81080 |  | . 8I 593 |  | . 99487 |  | .00513 |
| . 567 | .81124 |  | .81636 |  | . 99488 |  | . 005 I 2 |
| . 568 | .81168 |  | .81678 |  | . 99489 |  | .005II |
| . 569 | .81212 |  | .8172I |  | . 99490 |  | . 00510 |
| 2.570 | 0.81256 | 43,9 | 0.81764 | 42,9 | 9.99491 | 1,0 | 0.00509 |
| . 571 | .81299 |  | .81807 |  | . 99492 |  | . 00508 |
| . 572 | .8I343 |  | .81850 |  | . 99493 |  | . 00507 |
| . 573 | . 81387 |  | .81893 |  | . 99494 |  | . 00506 |
| . 574 | .8I43I |  | .81936 |  | . 99495 |  | . 00505 |
| 2.575 | 0.81475 | 43,9 | 0.81979 | 42,9 | 9.99496 | 1,0 | 0.00504 |
| . 576 | .81519 |  | . 82022 | 42, | . 99497 |  | . 00503 |
| . 577 | .81563 |  | . 82065 |  | . 99498 |  | . 00502 |
| . 578 | .81607 |  | . 82108 |  | . 99499 |  | . 00501 |
| . 579 | .8165I |  | .8215I |  | . 99500 |  | . 00500 |
| 2.580 | 0.8 I 695 | 43,9 | 0.82194 | 42,9 | 9.99501 | 1,0 | 0.00499 |
| . 58 I | .81739 |  | . 82237 | 4,9 | . 99502 |  | . 00498 |
| . 582 | . 81783 |  | . 82279 |  | . 99503 |  | . 00497 |
| . 583 | .81827 |  | . 82322 |  | . 99504 |  | . 00496 |
| . 584 | .81871 |  | . 82365 |  | . 99505 |  | . 00495 |
|  |  | 43,9 |  | 42,9 | 9.99506 | 1,0 | 0.00494 |
| . 586 | .81958 |  | . 82451 | 42,9 | . 9.99507 |  | . 00493 |
| . 587 | . 82002 |  | . 82494 |  | . 99508 |  | . 00492 |
| . 588 | . 82046 | - | . 82537 |  | . 99509 |  | . 00491 |
| . 589 | . 82090 |  | . 82580 |  | . 99510 |  | . 00490 |
| 2.590 | 0.82134 | 43,9 | 0.82623 | 42,9 | 9.995 II | 1,O | 0.00489 |
| . 591 | . 82178 |  | . 82666 |  | . 99512 |  | . 00488 |
| . 592 | . 82222 |  | . 82709 |  | . 99513 |  | . 00487 |
| . 593 | . 82266 |  | . 82752 |  | . 99514 |  | . 00486 |
| . 594 | . 82310 |  | . 82795 |  | . 99515 |  | . 00485 |
| 2.595 | 0.82354 | 43,9 | 0.82838 | 42,9 | 9.99516 | I,O | 0.00484 |
| . 596 | . 82398 |  | .8288I |  | .99517 |  | . 00483 |
| . 597 | . 82442 |  | . 82924 | 43,0 | . 99518 |  | . 00482 |
| . 598 | . 82485 |  | . 82967 |  | . 99519 |  | .0048I |
| . 599 | . 82529 |  | . 83010 |  | . 99520 |  | . 00480 |
| 2.600 | 0.82573 | 43,9 | 0.83052 | 43,0 | 9.9952 I | 1,O | 0.00479 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} \mathrm{u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.600 | 0.82573 | 43,9 | 0.83052 | 43,0 | 9.9952 I | 1,0 | 0.00479 |
| . 601 | . 82617 |  | . 83095 |  | . 99522 |  | . 00478 |
| . 602 | .8266I |  | .83138 |  | . 99523 |  | . 00477 |
| . 603 | . 82705 |  | .83181 |  | . 99524 |  | . 00476 |
| . 604 | . 82749 |  | . 83224 |  | . 99525 |  | . 00475 |
| 2.605 | 0.82793 | 43,9 | 0.83267 | 43,0 | 9.99526 | 0,9 | 0.00474 |
| . 606 | . 82837 |  | . 83310 |  | . 99527 |  | . 00473 |
| . 607 | .8288I |  | . 83353 |  | . 99527 |  | . 00473 |
| . 608 | . 82925 |  | . 83396 |  | .99528 |  | . 00472 |
| . 609 | . 82968 |  | . 83439 |  | . 99529 |  | . 00471 |
| 2.610 | 0.83012 | 43,9 | 0.83482 | 43,0 | 9.99530 | 0,9 | 0.00470 |
| .6II | . 83056 |  | . 83525 |  | . 9953 I |  | . 00469 |
| . 612 | . 83100 |  | . 83568 |  | . 99532 |  | . 00468 |
| .613 | .83144 |  | .8361 I |  | . 99533 |  | . 00467 |
| . 614 | .83188 |  | . 83654 |  | . 99534 |  | . 00466 |
| 2.615 | 0.83232 | 43,9 | 0.83697 | 43,0 | 9.99535 | 0,9 | 0.00465 |
| . 616 | . 83276 |  | . 83740 |  | . 99536 |  | . 00464 |
| . 617 | . 83320 |  | . 83783 |  | . 99537 |  | . 00463 |
| . 618 | . 83364 |  | . 83826 |  | . 99538 | - | . 00462 |
| .619 | . 83407 |  | . 83869 |  | . 99539 |  | . 0046 I |
| 2.620 | 0.83451 | 43,9 | 0.83912 | 43,0 | 9.99540 | 0,9 | 0.00460 |
| .621 | . 83495 |  | . 83955 |  | . 9954 I |  | . 00459 |
| . 622 | . 83539 |  | . 83998 |  | .9954I |  | . 00459 |
| . 623 | . 83583 |  | . 84041 |  | . 99542 |  | . 00458 |
| . 624 | . 83627 |  | . 84084 |  | . 99543 |  | . 00457 |
| 2.625 | 0.83671 | 43,9 | 0.84127 | 43,0 | 9.99544 | 0,9 | 0.00456 |
| . 626 | . 83715 |  | . 84170 |  | . 99545 |  | . 00455 |
| . 627 | . 83759 |  | . 84213 |  | . 99546 |  | . 00454 |
| . 628 | . 83802 |  | . 84256 |  | . 99547 |  | . 00453 |
| . 629 | . 83846 |  | . 84299 |  | . 99548 |  | . 00452 |
| 2.630 | 0.83890 | 43,9 | 0.8434 I | 43,0 | 9.99549 | 0,9 | 0.00451 |
| .631 | . 83934 |  | . 84384 |  | . 99550 |  | . 00450 |
| . 632 | . 83978 |  | . 84427 |  | . 9955 I |  | . 00449 |
| . 633 | . 84022 |  | . 84470 |  | . 9955 I |  | . 00449 |
| . 634 | . 84066 |  | . 84513 |  | . 99552 |  | . 00448 |
| 2.635 | 0.84110 | 43,9 | 0.84556 | 43,0 | 9.99553 | 0,9 | 0.00447 |
| . 636 | . 84154 |  | . 84599 |  | . 99554 |  | . 00446 |
| . 637 | .84197 |  | . 84642 |  | . 99555 |  | . 00445 |
| . 638 | . 84241 |  | . 84685 |  | . 99556 |  | . 00444 |
| . 639 | . 84285 |  | . 84728 |  | . 99557 |  | . 00443 |
| 2.640 | 0.84329 | 43,9 | 0.84771 | 43,0 | 9.99558 | 0,9 | 0.00442 |
| .64I | . 84373 |  | .84814 |  | . 99559 |  | . 00441 |
| . 642 | . 84417 |  | . 84857 |  | . 99559 |  | . 00441 |
| . 643 | . 84461 |  | . 84900 |  | . 99560 |  | . 00440 |
| . 644 | . 84505 |  | . 84943 |  | . 99561 |  | . 00439 |
| 2.645 | 0.84548 | 43,9 | 0.84986 | 43,0 | 9.99562 | 0,9 | 0.00438 |
| . 646 | . 84592 |  | . 85029 |  | . 99563 |  | . 00437 |
| . 647 | . 84636 |  | . 85072 |  | . 99564 |  | . 00436 |
| . 648 | . 84680 |  | .85115 |  | $.99565$ |  | . 00435 |
| . 649 | . 84724 |  | . 85158 |  | -99566 |  | . 00434 |
| 2.650 | 0.84768 | 43,9 | 0.85201 | 43,0 | 9.99566 | 0,9 | 0.00434 |
| 4 | $\log \tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc$ gd u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.650 | 0.84768 | 43,9 | 0.85201 | 43,0 | 9.99566 | 0,9 | 0.00434 |
| . 651 | . 84812 |  | . 85244 |  | . 99567 |  | . 00433 |
| . 652 | . 84855 |  | . 85287 |  | . 99568 |  | . 00432 |
| 653 | . 84899 |  | . 85330 |  | - 99569 |  | . 00431 |
| . 654 | . 84943 |  | . 85373 |  | -99570 |  | . 00430 |
| 2.655 | 0.84987 | 43,9 | 0.85416 | 43,0 | 9.99571 | 0,9 | 0.00429 |
| . 656 | .85031 |  | . 85459 |  | . 99572 |  | . 00428 |
| . 657 | . 85075 |  | . 85502 |  | . 99572 |  | . 00428 |
| . 658 | . 85119 |  | . 85545 |  | . 99573 |  | . 00427 |
| . 659 | . 85162 |  | . 85588 |  | . 99574 |  | . 00426 |
| 2.660 | 0:85206 | 43,9 | 0.85631 | 43,0 | 9.99575 | o,8 | 0.00425 |
| . 661 | . 85250 |  | . 85674 |  | . 99576 |  | . 00424 |
| . 662 | . 85294 |  | . 85717 |  | . 99577 |  | . 00423 |
| . 663 | . 85338 |  | . 85760 |  | . 99578 |  | . 00422 |
| . 664 | . 85382 |  | . 85803 |  | . 99578 |  | . 00422 |
| 2.665 | 0.85426 | 43,9 | 0.85846 | 43,0 | 9.99579 | 0,8 | 0.0042 I |
| . 666 | . 85469 |  | . 85889 |  | . 99580 |  | . 00420 |
| . 667 | . 85513 |  | . 85932 |  | .99581 |  | . 00419 |
| . 668 | . 85557 | 43,8 | . 85975 |  | . 99582 |  | . 00418 |
| . 669 | . 85601 |  | . 86018 |  | . 99583 |  | . 00417 |
| 2.670 | 0.85645 | 43,8 | 0.86061 | 43,0 | 9.99583 | 0,8 | 0.00417 |
| . 671 | . 85689 |  | . 86104 |  | . 99584 |  | . 00416 |
| . 672 | . 85733 |  | . 86147 |  | . 99585 |  | . 00415 |
| . 673 | . 85776 |  | - . 86190 |  | . 99586 |  | .004I4 |
| . 674 | . 85820 |  | . 86233 |  | . 99587 |  | . 00413 |
| 2.675 | 0. 85864 | 43,8 | 0.86276 | 43,0 | 9.99588 | 0,8 | 0.00412 |
| . 676 | . 85908 |  | . 86320 |  | . 99588 |  | .00412 |
| . 677 | . 85952 |  | . 86363 |  | . 99589 |  | .004II |
| . 678 | . 85996 |  | . 86406 |  | . 99590 |  | .00410 |
| . 679 | . 86039 |  | . 86449 |  | . 99591 |  | . 00409 |
| 2.680 | 0.86083 | 43,8 | 0.86492 | 43,0 | 9.99592 | 0,8 | 0.00408 |
| .681 | . 86127 |  | . 86535 |  | . 99592 |  | . 00408 |
| . 682 | .86171 |  | . 86578 |  | . 99593 |  | . 00407 |
| . 683 | . 86215 |  | . 86621 |  | . 99594 |  | . 00406 |
| . 684 | . 86259 |  | . 85664 |  | -99595 |  | . 00405 |
| 2.685 | 0.86302 | 43,8 | 0.86707 | 43,0 | 9.99596 | 0,8 | 0.00404 |
| . 685 | . 86346 |  | . 86750 |  | . 99597 |  | . 00403 |
| . 687 | . 86390 |  | . 86793 |  | . 99597 |  | . 00403 |
| . 688 | . 86434 |  | . 86836 |  | . 99598 |  | . 00402 |
| . 689 | . 86478 |  | . 86879 |  | . 99599 |  | .00401 |
| 2.690 | 0.86522 | 43,8 | 0.85922 | 43,0 | 9.99600 | 0,8 | 0.00400 |
| . 691 | . 86565 |  | . 86955 |  | . 99601 |  | . 00399 |
| . 692 | . 86609 |  | . 87008 |  | .99601 |  | .00399 |
| . 693 | . 86653 |  | . 87051 |  | . 99602 |  | . 00398 |
| . 694 | . 86697 |  | . 87094 |  | . 99603 |  | . 00397 |
| 2.695 | 0.85741 | 43,8 | 0.87137 | 43,0 | 9.99604 | 0,8 | 0.00396 |
| . 696 | . 86785 |  | . 87180 |  | . 99605 |  | . 00395 |
| . 697 | . 85828 |  | . 87223 |  | . 99605 |  | . 00395 |
| . 698 | . 86872 |  | . 87266 |  | . 99605 |  | . 00394 |
| . 699 | . 86916 |  | . 87309 |  | . 99607 |  | . 00393 |
| 2.700 | Q. 86960 | 43,8 | 0.87352 | 43,0 | 9.99508 | 0,8 | 0.00392 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log sec od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 10 sin gd u | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | $\log ^{\cosh } \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | $\underline{l o g} \tanh u$ | $\omega \mathrm{Fo}^{\prime}$ | log coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.700 | 0.86960 | 43,8 | 0.87352 | 43,0 | 9.99608 | 0,8 | 0.00392 |
| . 701 | . 87004 |  | . 87395 |  | . 99608 |  | . 00392 |
| . 702 | . 87048 |  | . 87438 |  | . 99609 |  | . 00391 |
| . 703 | . 87091 |  | . 8748 I |  | . 99610 |  | . 00390 |
| . 704 | . 87135 |  |  |  | .996II |  | .00389 |
| 2.705 | 0.87179 | 43,8 | 0.87567 | 43,0 | 9.99612 | 0,8 | 0.00388 |
| . 706 | . 87223 |  | . 87610 |  | . 99612 |  | . 00388 |
| . 707 | . 87267 |  | . 87654 |  | . 996613 |  | . 00387 |
| . 708 | . 87310 |  | . 87697 |  | . 996614 |  | .00386 |
| . 709 | . 87354 |  | . 87740 |  | . 99615 |  | . 00385 |
| 2.710 | 0.87398 | 43,8 | 0.87783 | 43,0 | 9.99615 | 0,8 | 0.00385 |
| . 711 | . 87442 |  | . 87825 |  | . 99616 |  | . 00384 |
| . 712 | . 87486 |  | . 87869 |  | . 99617 |  | .00383 |
| . 713 | . 87530 |  | . 87912 |  | . 996618 |  | .00382 |
| . 714 | . 87573 |  | . 87955 |  | . 99619 |  | .00381 |
| 2.715 | 0.87617 | 43,8 | 0.87998 | 43,1 | 9.99619 | 0,8 | 0.0038 I |
| . 716 | .87661 |  | . 88041 |  | . 99620 |  | . 00380 |
| . 717 | . 87705 |  | . 88084 |  | -99621 |  | . 00379 |
| . 718 | . 87749 |  | . 88127 |  | . 99622 |  | . 00378 |
| . 719 | . 87792 |  | .88170 |  | . 99622 |  | . 00378 |
| 2.720 | 0.87836 | 43,8 | 0.88213 | 43,I | 9.99623 | o,8 | 0.00377 |
| . 721 | . 87880 |  | . 88256 |  | . 99624 |  | . 00376 |
| . 722 | . 87924 |  | . 88299 |  | . 99625 |  | . 00375 |
| . 723 | . 87968 |  | . 888342 |  | . 99625 | 0,7 | . 00375 |
| . 724 | . 88011 |  | . 88385 |  | . 99626 |  | . 00374 |
| 2.725 | 0.88055 | 43,8 | 0.88428 | 43, I | 9.99627 | 0,7 | 0.00373 |
| . 726 | . 88899 |  | .88471 |  | . 99628 |  | . 00372 |
| . 727 | . 888143 |  | . 88515 |  | . 99628 |  | . 00372 |
| . 728 | . 88187 |  | . 88558 |  | . 99629 |  | . 00371 |
| . 729 | . 88230 |  | . 88601 |  | . 99630 |  | . 00370 |
| 2.730 | 0.88274 | 43,8 | 0.88644 | 43,1 | 9.9963 I | 0,7 | 0.00369 |
| . 731 | . 88318 |  | . 88687 |  | . 99631 |  | . 00369 |
| . 732 | . 88362 |  | . 88730 |  | . 99632 |  | . 00368 |
| . 733 | . 88406 |  | . 88773 |  | . 99633 |  | . 00367 |
| . 734 | . 88449 |  | . 88816 |  | . 99633 |  | . 00367 |
| 2.735 | 0.88493 | 43,8 | 0.88859 | 43, I | 9.99634 | 0,7 | 0.00366 |
| . 736 | . 88537 |  | . 88902 |  | . 99635 |  | . 00365 |
| . 737 | .88581 |  | . 88945 |  | . 99636 |  | .00364 |
| . 738 | . 88825 |  | . 88988 |  | . 99636 |  | .00364 |
| . 739 | . 88668 |  | . 8903 I |  | . 99637 |  | .00363 |
| 2.740 | 0.88712 | 43,8 |  | 43, I |  | 0,7 |  |
| . 741 | . 88756 |  | . 89117 |  | . 99639 |  | . 00361 |
| . 742 | . 88800 |  | . 89161 |  | . 99639 |  | . 00361 |
| . 743 | . 88844 |  | . 89204 |  | . 99640 |  | .00360 |
| . 744 | . 88887 |  | . 89247 |  | -9964I |  | . 00359 |
| 2.745 | 0.88931 | 43,8 | 0.89290 | 43, I | 9.9964 I | 0,7 | 0.00359 |
| . 746 | . 88975 |  | . 89333 |  | . 99642 |  | . 00358 |
| . 747 | . 89019 |  | . 89376 |  | . 99643 |  | . 00357 |
| . 748 | . 89063 |  | . 89419 |  | . 99644 |  | . 003556 |
| . 749 | .89106 |  | . 89462 |  | . 99644 |  | . 00356 |
| 2.750 | 0.89150 | 43,8 | 0.89505 | 43,I | 9.99645 | 0,7 | 0.00355 |
| $u$ | log tan odu | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}$ | log csc gd u |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.750 | 0.89150 | 43,8 | 0.89505 | 43, I | 9.99645 | 0,7 | 0.00355 |
| . 751 | . 89194 |  | . 89548 |  | . 99646 |  | . 00354 |
| . 752 | . 89238 |  | . 89591 |  | . 99646 | . | . 00354 |
| . 753 | . 8928 I |  | . 89634 |  | . 99647 |  | . 00353 |
| . 754 | . 89325 |  | . 89677 |  | . 99648 |  | . 00352 |
| 2.755 | 0.89369 | 43,8 | 0.89720 | 43, I | 9.99649 | 0,7 | 0.00351 |
| . 756 | . 89413 |  | . 89764 |  | . 99649 |  | . 00351 |
| . 757 | . 89457 |  | . 89807 |  | . 99650 |  | . 00350 |
| . 758 | . 89500 |  | . 89850 |  | . 99651 |  | . 00349 |
| . 759 | . 89544 |  | . 89893 |  | .9965I |  | . 00349 |
| 2.760 | 0.89588 | 43,8 | 0.89936 | 43, I | 9.99652 | 0,7 | 0.00348 |
| . 761 | . 89632 |  | . 89979 |  | . 99653 |  | . 00347 |
| . 762 | . 89675 |  | . 90022 |  | . 99653 |  | . 00347 |
| . 763 | . 89719 |  | . 90065 |  | . 99654 |  | . 00346 |
| . 764 | . 89753 | . | .90108 |  | . 99655 |  | . 00345 |
| 2.765 | 0.89807 | 43,8 | 0.90151 | 43, I | 9.99656 | 0,7 | 0.00344 |
| . 766 | . 8985 I |  | . 9019.4 |  | . 99656 |  | . 00344 |
| . 767 | . 89894 |  | . 90237 |  | . 99657 |  | . 00343 |
| . 768 | . 89938 |  | .90281 |  | . 99658 |  | . 00342 |
| .769 | . 89982 |  | . 90324 |  | . 99658 |  | . 00342 |
| 2.770 | 0.90026 | 43,8 | 0.90367 | 43, I | 9.99659 | 0,7 | 0.00341 |
| . 771 | . 90069 |  | .90410 |  | . 99660 |  | . 00340 |
| . 772 | .901 I3 |  | . 90453 |  | . 99660 |  | . 00340 |
| . 773 | . 90157 |  | . 90496 |  | .9966I |  | . 00339 |
| . 774 | .90201 |  | . 90539 |  | . 99662 |  | . 00338 |
| 2.775 | 0.90245 | 43,8 | 0.90582 | 43, I | 9.99662 | 0,7 | 0.00338 |
| . 776 | . 90288 |  | . 90625 |  | . 99663 |  | . 00337 |
| . 777 | . 90332 |  | . 90668 |  | . 99664 |  | . 00336 |
| . 778 | . 90376 |  | . 90712 |  | . 99664 |  | . 00336 |
| . 779 | . 90420 |  | . 90755 |  | . 99665 |  | . 00335 |
| . 2.780 | 0.90463 | 43,8 | 0.90798 | 43, I | 9.99666 | 0,7 | 0.00334 |
| .78I | . 90507 |  | .90841 |  | . 99666 |  | . 00334 |
| . 782 | . 90551 |  | . 90884 |  | . 99667 |  | . 00333 |
| . 783 | . 90595 |  | . 90927 |  | . 99668 |  | . 00332 |
| . 784 | . 90638 |  | . 90970 |  | . 99668 |  | . 00332 |
| 2.785 | 0.90682 | 43,8 | 0.91013 | 43, I | 9.99669 | 0,7 | 0.00331 |
| . 786 | . 90726 |  | . 91056 |  | . 99670 |  | . 00330 |
| . 787 | . 90770 |  | .91099 |  | . 99670 |  | . 00330 |
| . 788 | .908I3 |  | .91142 |  | . 99671 |  | . 00329 |
| . 789 | .90857 |  | .91186 |  | . 99672 |  | . 00328 |
| 2.790 | 0.90901 | 43,8 | 0.91229 | 43, I | 9.99672 | 0,7 | 0.00328 |
| . 791 | . 90945 |  | . 91272 |  | . 99673 |  | . 00327 |
| . 792 | . 90989 |  | .91315 |  | . 99674 |  | . 00326 |
| . 793 | . 91032 |  | .91358 |  | . 99674 |  | . 00326 |
| . 794 | .91076 |  | .9140I |  | . 99675 |  | . 00325 |
| 2.795 | 0.91120 | 43,8 | 0.91444 | 43, I | 9.99676 | 0,6 | 0.00324 |
| . 796 | .91164 |  | .91487 |  | . 99676 |  | . 00324 |
| . 797 | .91207 |  | .91530 |  | . 99677 |  | . 00323 |
| . 798 | .91251 |  | .91574 |  | . 99678 |  | . 00322 |
| . 799 | .91295 |  | .91617 |  | . 99678 |  | . 00322 |
| 2.800 | 0.91339 | 43,8 | 0.91660 | 43, I | 9.99579 | 0,6 | 0.00321 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { t a n h }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.800 | 0.91339 | 43,8 | 0.91660 | 43, I | 9.99679 | 0,6 | 0.0032 I |
| . 801 | .91382 |  | .91703 |  | . 99679 |  | .0032I |
| . 802 | .91426 |  | . 91746 |  | . 99680 |  | . 00320 |
| . 803 | . 91470 | 43,7 | .91789 |  | .9968I |  | .00319 |
| . 804 | .91514 |  | .91832 |  | .9968I |  | . 00319 |
| 2.805 | 0.91557 | 43,7 | 0.91875 | 43,1 | 9.99682 | 0,6 | 0.00318 |
| . 806 | .9160I |  | . 91918 |  | . 99683 |  | . 00317 |
| . 807 | .91645 |  | . 91962 |  | . 99683 |  | . 00317 |
| . 808 | . 91689 |  | . 92005 |  | . 99684 |  | . .00316 |
| . 809 | . 91732 |  | . 92048 |  | . 99685 |  | . .00315 |
| 2.810 | 0.91776 | 43,7 | 0.92091 | 43, I | 9.99685 | 0,6 | 0.00315 |
| .8II | . 91820 |  | . 92134 |  | . 99686 |  | .003I4 |
| .8I2 | .91864 |  | .92I77 |  | . 99686 |  | . 00314 |
| . 8 I 3 | . 91907 |  | . 92220 |  | . 99687 |  | . 00313 |
| .814 | .9195I |  | . 92263 |  | . 99688 |  | . 00312 |
| 2.815 | 0.91995 | 43,7 | 0.92306 | 43, I | 9.99688 | 0,6 | 0.00312 |
| .816 | . 92039 |  | . 92350 |  | . 99689 |  | . 003 II |
| .817 | . 92082 |  | . 92393 |  | . 99690 |  | . 00310 |
| .818 | . 92126 |  | . 92436 |  | . 99690 |  | . 00310 |
| . 819 | .92170 |  | . 92479 |  | .9969I |  | . 00309 |
| 2.820 | 0.92213 | 43,7 | 0.92522 | 43, I | 9.99691 | 0,6 | 0.00309 |
| . 82 I | . 92257 |  | . 92565 |  | . 99692 |  | . 00308 |
| . 822 | . 92301 |  | - .92608 |  | . 99693 |  | . 00307 |
| . 823 | . 92345 |  | . 92651 |  | . 99693 |  | . 00307 |
| . 824 | . 92388 |  | . 92695 |  | . 99694 |  | . 00306 |
| 2.825 | 0.92432 | 43,7 | 0.92738 | 43, I | 9.99694 | 0,6 | 0.00306 |
| . 826 | . 92476 |  | .92781 |  | . 99695 |  | . 00305 |
| . 827 | . 92520 |  | . 92824 |  | . 99696 |  | . 00304 |
| . 828 | . 92563 |  | . 92867 |  | . 99696 |  | . 00304 |
| . 829 | . 92607 |  | . 92910 |  | . 99697 |  | . 00303 |
| 2.830 | 0.92651 | 43,7 | 0.92953 | 43, I | 9.99698 | 0,6 | 0.00302 |
| . 831 | . 92695 |  | . 92996 |  | . 99698 |  | . 00302 |
| . 832 | . 92738 |  | . 93040 |  | . 99699 |  | . 00301 |
| . 833 | . 92782 |  | . 93083 |  | . 99699 |  | .00301 |
| . 834 | . 92826 |  | .93126 |  | . 99700 |  | . 00300 |
| 2.835 | 0.92869 | 43,7 | 0.93169 | 43, 1 | 9.99701 | 0,6 | 0.00299 |
| . 836 | . 92913 |  | .93212 |  | .99701 |  | . 00299 |
| . 837 | . 92957 |  | . 93255 |  | . 99702 |  | . 00298 |
| . 838 | . .93001 |  | . 93298 |  | . 99702 |  | . 00298 |
| . 839 | . 93044 |  | .9334I |  | . 99703 |  | . 00297 |
| 2.840 | 0.93088 | 43,7 |  | 43, I | 9.99704 | 0,6 |  |
| . 841 | .93132 |  | . 93428 |  | . 99704 |  | . 00296 |
| . 842 | .93176 |  | .9347I |  | . 99705 |  | . 00295 |
| . 843 | . 93219 |  | .93514 |  | . 99705 |  | . 00295 |
| . 844 | . 93263 |  | . 93557 |  | . 99706 |  | . 00294 |
| 2.845 | 0.93307 | 43,7 | 0.93600 | 43, I | 9.99706 | 0,6 | 0.00294 |
| . 846 | . 93350 |  | . 93643 |  | . 99707 |  | . 00293 |
| . 847 | . 93394 |  | . 93687 |  | . 99708 |  | . 00292 |
| . 848 | . 93438 |  | . 93730 |  | . 99708 |  | . 00292 |
| . 849 | . 93482 |  | . 93773 |  | . 99709 |  | . 00291 |
| - 2.850 | 0.93525 | 43,7 | 0.93816 | 43, I | 9.99709 | 0,6 | 0.00291 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Smithsonian Tables

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.850 | 0.93525 | 43,7 | 0.93816 | 43, I | 9.99709 | 0,6 | 0.00291 |
| . 851 | . 93569 |  | . 93859 |  | . 99710 |  | .00290 |
| . 852 | . 93613 |  | . 93902 |  | . 9971 I |  | . 00289 |
| . 853 | . 93657 |  | . 93945 |  | . 997 I I |  | . 00289 |
| . 854 | . 93700 |  | . 93989 |  | . 99712 |  | . 00288 |
| 2.855 | 0.93744 | 43,7 | 0.94032 | 43, I | 9.99712 | 0,6 | 0.00288 |
| . 856 | . 93788 |  | . 94075 |  | . 99713 |  | . 00287 |
| . 857 | . 93831 |  | .94II8 |  | . 99713 |  | . 00287 |
| . 858 | . 93875 |  | .9416I |  | . 99714 |  | . 00286 |
| . 859 | . 93919 |  | . 94204 |  | . 99715 |  | . 00285 |
| 2.860 | 0.93963 | 43,7 | 0.94247 | 43,I | 9.99715 | 0,6 | 0.00285 |
| .861 | . 94006 |  | . 94291 |  | . 99716 |  | . 00284 |
| . 862 | . 94050 |  | . 94334 |  | . 99716 |  | . 00284 |
| . 863 | . 94094 |  | . 94377 |  | . 99717 |  | .00283 |
| . 854 | .94137 |  | . 94420 |  | . 99717 |  | . 00283 |
| 2.865 | 0.94181 | 43,7 | 0.94463 | 43,1 | 9.99718 | 0,6 | 0.00282 |
| . 865 | . 94225 |  | . 94506 |  | . 99719 |  | .0028I |
| . 867 | . 94269 |  | - 94549 |  | . 99719 |  | .00281 |
| . 858 | . 94312 |  | . 94593 |  | . 99720 |  | . 00280 |
| . 869 | . 94356 |  | . 94636 | 43,2 | . 99720 |  | . 00280 |
| 2.870 | 0.94400 | 43,7 | 0.94679 | 43,2 | 9.99721 | 0,6 | 0.00279 |
| . 871 | . 94443 |  | . 94722 |  | .9972I |  | . 00279 |
| . 872 | . 94487 |  | . 94765 |  | . 99722 |  | . 00278 |
| . 873 | .9453I |  | . 94808 |  | . 99722 |  | . 00278 |
| . 874 | . 94575 |  | . 94852 |  | . 99723 |  | . 00277 |
| 2.875 | 0.94618 | 43,7 | 0.94895 | 43,2 | 9.99724 | 0,6 | 0.00276 |
| . 876 | . 94662 |  | . 94938 |  | . 99724 |  | . 00276 |
| . 877 | . 94706 |  | .9498I |  | . 99725 |  | . 00275 |
| . 878 | . 94749 |  | . 95024 |  | . 99725 | 0,5 | . 00275 |
| . 879 | . 94793 |  | . 95067 |  | . 99726 |  | . 00274 |
| 2.880 | 0.94837 | 43,7 | 0.95110 | 43,2 | 9.99726 | 0,5 | 0.00274 |
| .88I | . 94880 |  | .95I54 |  | . 99727 |  | . 00273 |
| . 882 | . 94924 |  | .95197 |  | . 99727 |  | . 00273 |
| . 883 | . 94968 |  | . 95240 |  | . 99728 |  | . 00272 |
| . 884 | . 95012 |  | . 95283 |  | . 99728 |  | . 00272 |
| 2.885 | 0.95055 | 43,7 | 0.95326 | 43,2 | 9.99729 | 0,5 | 0.00271 |
| . 886 | . 95099 |  | . 95369 |  | . 99730 |  | . 00270 |
| . 887 | .95143 |  | . 95413 |  | . 99730 |  | . 00270 |
| . 888 | .95186 |  | . 95456 |  | .9973I |  | . 00269 |
| . 889 | . 95230 |  | . 95499 |  | .9973I |  | . 00269 |
| 2.890 | 0.95274 | 43,7 | 0.95542 | 43,2 | 9.99732 | 0,5 | 0.00268 |
| . 891 | . 95317 |  | . 95585 |  | . 99732 |  | . 00268 |
| . 892 | .9536I |  | . 95628 |  | . 99733 |  | . 00267 |
| . 893 | . 95405 |  | . 95672 |  | . 99733 |  | . 00267 |
| . 894 | . 95449 |  | . 95715 |  | . 99734 |  | . 00266 |
| 2.895 | 0.95492 | 43,7 | 0.95758 | 43,2 | 9.99734 | 0,5 | 0.00266 |
| . 896 | . 95536 |  | .95801 |  | . 99735 |  | . 00265 |
| . 897 | . 95580 |  | . 95844 |  | . 99735 |  | . 00265 |
| . 898 | . 95623 |  | . 95887 |  | . 99736 | - | . 00264 |
| . 899 | . 95667 |  | -9593I |  | . 99737 |  | . 00263 |
| 2.900 | 0.95711 | 43,7 | 0.95974 | 43,2 | 9.99737 | 0,5 | 0.00263 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{~d} \mathbf{u}$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.900 | 0.95711 | 43,7 | 0.95974 | 43,2 | 9.99737 | 0,5 | 0.00263 |
| . 901 | . 95754 |  | .96017 |  | . 99738 |  | . 00262 |
| . 902 | . 95798 |  | . 96060 |  | . 99738 | , | . 00262 |
| . 903 | . 95842 |  | .96103 |  | . 99739 |  | .0026I |
| . 904 | . 95885 |  | .96146 |  | . 99739 |  | .0026I |
| 2.905 | 0.95929 | 43,7 | 0.96190 | 43,2 | 9.99740 | 0,5 | 0.00260 |
| . 906 | . 95973 |  | . 96233 |  | . 99740 |  | . 00260 |
| . 907 | . 96017 |  | . 96276 |  | .9974I |  | . 00259 |
| . 908 | . 96060 |  | . 96319 |  | . 99741 |  | . 00259 |
| . 909 | .96104 |  | . 96362 |  | . 99742 |  | . 00258 |
| 2.910 | 0.96148 | 43,7 | 0.96405 | 43,2 | 9.99742 | 0,5 | 0.00258 |
| . 911 | .96191 |  | . 96449 |  | . 99743 |  | 600257 |
| . 912 | . 96235 |  | . 96492 |  | . 99743 |  | .00257 |
| . 913 | . 96279 |  | .96535 |  | . 99744 |  | . 00256 |
| .914 | .96322 |  | . 96578 |  | . 99744 |  | . 00256 |
| 2.915 | 0.96366 | 43,7 | 0.96621 | 43,2 | 9.99745 | 0,5 | 0.00255 |
| . 916 | .96410 |  | . 96664 |  | . 99745 |  | . 00255 |
| . 917 | . 96453 |  | . 96708 |  | . 99746 |  | . 00254 |
| . 918 | .96497 |  | .9675I |  | . 99746 |  | . 00254 |
| . 919 | .9654I |  | . 96794 |  | . 99747 |  | . 00253 |
| 2.920 | 0.96584 | 43,7 | $0.968,37$ | 43,2 | 9.99747 | 0,5 | 0.00253 |
| . 92 I | . 96628 |  | . 96880 |  | . 99748 |  | . 00252 |
| . 922 | . 96672 |  | . 96923 |  | . 99748 |  | . 00252 |
| . 923 | . 96716 |  | . 96967 |  | . 99749 |  | . 0025 I |
| . 924 | . 96759 |  | .97010 |  | . 99749 |  | . 0025 I |
| 2.925 | 0.96803 | 43,7 | 0.97053 | 43,2 | 9.99750 | 0,5 | 0.00250 |
| . 926 | . 96847 |  | . 97096 |  | . 99750 |  | . 00250 |
| . 927 | . 96890 |  | . 97139 |  | .9975 |  | . 00249 |
| . 928 | . 96934 |  | .97183 |  | . 99751 |  | . 00249 |
| . 929 | . 96978 |  | . 97226 |  | . 99752 |  | . 00248 |
| 2.930 | 0.9702 I | 43,7 | 0.97269 | 43,2 | 9.99752 | 0,5 | 0.00248 |
| .931 | . 97065 |  | . 97312 |  | . 99753 |  | . 00247 |
| . 932 | .97109 |  | . 97355 |  | . 99753 |  | . 00247 |
| . 933 | . 97152 |  | . 97398 |  | . 99754 |  | . 00246 |
| . 934 | . 97196 |  | . 97442 |  | . 99754 |  | . 00246 |
| 2.935 | 0.97240 | 43,7 | 0.97485 | 43,2 | 9.99755 | 0,5 | 0.00245 |
| . 936 | . 97283 |  | . 97528 |  | . 99755 |  | . 00245 |
| . 937 | . 97327 |  | . 97571 |  | . 99756 |  | . 00244 |
| . 938 | .9737 I |  | . 97614 |  | . 99756 |  | . 00244 |
| . 939 | . 97414 |  | . 97658 |  | . 99757 |  | . 00243 |
| 2.940 | 0.97458 | 43,7 | 0.97701 | 43,2 | 9.99757 | 0,5 | 0.00243 |
| .94I | . 97502 |  | . 97744 |  | . 99758 |  | . 00242 |
| . 942 | . 97545 |  | . 97787 |  | . 99758 |  | . 00242 |
| . 943 | . 97589 |  | . 97830 |  | . 99759 |  | .0024I |
| . 944 | . 97633 |  | . 97874 |  | . 99759 |  | . 0024 I |
| 2.945 | 0.97676 | 43,7 | 0.97917 | 43,2 | 9.99760 | 0,5 | 0.00240 |
| . 946 | . 97720 |  | . 97960 |  | . 99760 |  | . 00240 |
| . 947 | . 97764 |  | . 98003 |  | .99761 |  | . 00239 |
| . 948 | . 97807 |  | . 98046 |  | .99761 |  | . 00239 |
| . 949 | .9785I |  | . 98089 |  | . 99762 |  | . 00238 |
| 2.950 | 0.97895 | 43,7 | 0.98 r 33 | 43,2 | 9.99762 | 0,5 | 0.00238 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.950 | 0.97895 | 43,7 | 0.98133 | 43,2 | 9.99762 | 0,5 | 0.00238 |
| -951 | . 97938 |  | .98i76 |  | . 99763 |  | . 00237 |
| . 952 | . 97982 |  | .98219 |  | . 99763 |  | . 00237 |
| . 953 | . 98026 |  | . 98262 |  | . 99763 |  | . 00237 |
| -. 954 | . 98069 |  | . 98305 |  | . 99764 |  | . 00236 |
| 2.955 | 0.98113 | 43,7 | 0.98349 | 43,2 | 9.99764 | 0,5 | 0.00236 |
| . 956 | .98157 |  | . 98392 |  | . 99765 |  | . 00235 |
| . 957 | . 98200 |  | . 98435 |  | . 99765 |  | . 00235 |
| . 958 | . 98244 |  | . 98478 |  | . 99766 |  | . 00234 |
| . 959 | . 98288 |  | .9852I |  | . 99766 |  | . 00234 |
| 2.960 | 0.98331 | 43,7 | 0.98565 | 43,2 | 9.99767 | 0,5 | 0.00233 |
| .96I | . 98375 |  | . 98608 |  | . 99767 |  | . 00233 |
| . 962 | . 98419 |  | .9865I |  | . 99768 |  | . 00232 |
| . 963 | . 98462 |  | . 98694 |  | . 99768 |  | . 00232 |
| . 964 | . 98506 |  | . 98737 |  | . 99769 |  | .00231 |
| 2.965 | 0.98550 | 43,7 | 0.98781 | 43,2 | 9.99769 | 0,5 | 0.00231 |
| . 966 | . 98593 |  | . 98824 |  | . 99770 |  | .00230 |
| . 967 | . 98637 | , | . 98867 |  | . 99770 |  | . 00230 |
| . 968 | .9868I |  | . 98910 |  | . 99770 |  | . 00230 |
| . 969 | . 98724 |  | . 98953 |  | .9977I |  | . 00229 |
| 2.970 | 0.98768 | 43,7 | 0.98997 | 43,2 | 9.99771 | 0,5 | 0.00229 |
| . 971 | . 98812 |  | . 99040 |  | . 99772 |  | . 00228 |
| . 972 | . 08855 |  | . 99083 |  | . 99772 |  | . 00228 |
| . 973 | . 98899 |  | .99126 |  | . 99773 |  | . 00227 |
| . 974 | . 98943 |  | . 99169 |  | . 99773 |  | . 00227 |
| 2.975 | 0.98986 | 43,7 | 0.99213 | 43,2 | 9.99774 | 0,5 | 0.00226 |
| . 976 | . 99030 |  | . 99256 |  | . 99774 |  | . 00226 |
| . 977 | . 99074 |  | . 99299 |  | . 99775 |  | . 00225 |
| . 978 | .99117 |  | . 99342 |  | . 99775 | 0,4 | . 00225 |
| . 979 | .9916I |  | . 99385 |  | . 99775 |  | . 00225 |
| 2.980 | 0.99205 | 43,7 | 0.99429 | 43,2 | 9.99776 | 0,4 | 0.00224 |
| .981 | . 99248 |  | . 99472 |  | . 99776 |  | . 00224 |
| . 982 | . 99292 |  | .99515 |  | . 99777 |  | . 00223 |
| .983 | . 99336 |  | . 99558 |  | . 99777 |  | . 00223 |
| . 984 | . 99379 |  | .9960I |  | . 99778 |  | . 00222 |
| 2.985 | 0.99423 | 43,7 | 0.99645 | 43,2 | 9.99778 | 0,4 | 0.00222 |
| . 986 | . 99466 |  | . 99688 |  | . 99779 |  | . 00221 |
| . 987 | . 99510 |  | . 9973 I |  | . 99779 |  | . 0022 I |
| . 988 | . 99554 |  | . 99774 | - | . 99779 |  | .0022I |
| .989 | .99597 |  | .99818 |  | . 99780 |  | . 00220 |
| 2.990 | 0.99641 | 43,6 | 0.99861 | 43,2 | 9.99780 | 0,4 | 0.00220 |
| .991 | . 99685 |  | . 99904 |  | .9978I |  | .00219 |
| . 992 | . 99728 |  | . 99947 |  | .9978I |  | .00219 |
| . 993 | . 99772 |  | . 99990 |  | . 99782 |  | .00218 |
| . 994 | .99816 |  | 1.00034 |  | . 99782 |  | . 00218 |
| 2.995 | 0.99859 | 43,6 | 1.00077 | 43,2 | 9.99783 | 0,4 | 0.00217 |
| . 996 | . 99903 |  | . 00120 |  | . 99783 |  | . 00217 |
| . 997 | . 99947 | - | . 00163 |  | . 99783 |  | . 00217 |
| . 998 | . 99990 |  | . 00206 |  | . 99784 |  | . 00216 |
| . 999 | 1.00034 |  | . 00250 |  | . 99784 |  | . 00216 |
| 3.000 | 1.00078 | 43,6 | 1.00293 | 43,2 | 9.99785 | 0,4 | 0.00215 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g d u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \operatorname{coth} u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.00 | I. 00078 | 436,5 | 1.00293 | 432,I | 9.99785 | 4,3 | 0.00215 |
| . OI | . 00514 | 436,4 | . 00725 | 432,2 | . 99789 | 4,2 | . 002 II |
| . 02 | . 00950 | 436,4 | . OII57 | 432,2 | . 99793 | 4,I | . 00207 |
| . 03 | . 01387 | 436,3 | .OI589 | 432,3 | . 99797 | 4, I | .00203 |
| . 04 | . 01823 | 436,3 | . 02022 | 432,3 | . 99801 | 4,0 | .00199 |
| 3.05 | 1.02259 | 436,2 | I. 02454 | 432,4 | 9.99805 | 3,9 | 0.00195 |
| . 06 | . 02696 | 436,2 | . 02886 | 432,4 | . 99809 | 3,8 | .00191 |
| . 07 | . 03132 | 436,2 | .03319 | 432,4 | .998I3 | 3,7 | . 00187 |
| . 08 | . 03568 | 436, I | .0375I | 432,5 | .998I7 | 3,7 | . 00183 |
| . 09 | . 04004 | 436, 1 | .04I84 | 432,5 | . 99820 | 3,6 | .00180 |
| 3.10 | I. 04440 | 436, I | 1.04616 | 432,5 | 9.99824 | 3,5 | 0.00176 |
| . II | . 04876 | 436,0 | . 05049 | 432,6 | . 99827 | 3,4 | . 00173 |
| . 12 | .05312 | 436,0 | .0548I | 432,6 | . 99831 | 3,4 | . 00169 |
| . 13 | . 05748 | 436,0 | . 05914 | 432,6 | . 99834 | 3,3 | . 00166 |
| . 14 | . 06184 | 435,9 | . 06347 | 432,7 | . 99837 | 3,3 | . 00163 |
| 3.15 | 1. 06620 | 435,9 | 1.06779 | 432,7 | 9.99841 | 3,2 | 0.00159 |
| . 16 | . 07056 | 435,9 | . 07212 | 432,7 | . 99844 | 3,1 | .00156 |
| . 17 | . 07492 | 435,8 | . 07645 | 432,8 | . 99847 | 3, I | .00153 |
| . 18 | . 07927 | 435,8 | .08078 | 432,8 | . 99850 | 3,0 | . 00150 |
| . 19 | . 08363 | 435,8 | . 08510 | 432,8 | . 99853 | 2,9 | . 00147 |
| 3.20 | 1. 08799 | 435,7 | 1.08943 | 432,9 | 9.99856 | 2,9 | 0.00144 |
| . 21 | . 09235 | 435,7 | . 09376 | 432,9 | . 99859 | 2,8 | . 00141 |
| . 22 | . 09670 | 435,7 | . 09809 | 432,9 | .9986I | 2,8 | .00139 |
| . 23 | . 10106 | 435,7 | . 10242 | 432,9 | . 99864 | 2,7 | .00I36 |
| . 24 | . 10542 | 435,6 | . 10675 | 433,0 | . 99867 | 2,7 | . O0I33 |
| 3.25 | 1. 10977 | 435,6 | I. 11108 | 433,0 | 9.99869 | 2,6 | 0.00131 |
| . 26 | . II413 | 435,6 | . I I 54I | 433,0 | -. 99872 | 2,6 | .00128 |
| . 27 | . II849 | 435,6 | . 11974 | 433,0 | . 99875 | 2,5 | .00125 |
| . 28 | . 12284 | 435,5 | . 12407 | 433, I | . 99877 | 2,5 | . 00123 |
| . 29 | . 12720 | 435,5 | . 12840 | 433, 1 | . 99879 | 2,4 | . 0012 I |
| $3 \cdot 30$ | I. I3I55 | 435,5 | I. 13273 | 433,1 | 9.99882 | 2,4 | 0.00118 |
| . 31 | . I3591 | 435,5 | . 13706 | 433, I | . 99884 | 2,3 | .001 16 |
| . 32 | . 14026 | 435,4 | . 14139 | 433,2 | . 99886 | 2,3 | .00114 |
| . 33 | . I446I | 435,4 | . 14573 | 433,2 | . 99889 | 2,2 | . 0011 I |
| . 34 | . 14897 | 435,4 | . 15006 | 433,2 | .99891 | 2,2 | . 00109 |
| $3 \cdot 35$ | 1. 15332 | 435;4 | I. I5439 | 433,2 | 9.99893 | 2,I | 0.00107 |
| . 36 | . 15768 | 435,3 | . 15872 | 433,2 | . 99895 | 2,I | . 00105 |
| . 37 | . 16203 | 435,3 | . 16306 | 433,3 | . 99897 | 2,1 | . 00103 |
| . 38 | . 16638 | 435,3 | . 16739 | 433,3 | . 99899 | 2,0 | . 00101 |
| . 39 | . 17073 | 435,3 | .17172 | 433,3 | .99901 | 2,0 | . 00099 |
| 3.40 | I. I7509 | 435,3 | 1. 17605 | 433,3 | 9.99903 | 1,9 | 0.00097 |
| . 41 | . 17944 | 435,2 | . 18039 | 433,3 | . 99905 | I,9 | . 00095 |
| .42 | . 18379 | 435,2 | . 18472 | 433,4 | . 99907 | I,9 | . 00093 |
| . 43 | . 18814 | 435,2 | . 18906 | 433,4 | . 999009 | I,8 | . 00091 |
| . 44 | . 19250 | 435,2 | . 19339 | 433,4 | . 9991 I | 1,8 | . 00089 |
| 3.45 | I. 19685 | 435,2 | I. 19772 | 433,4 | 9.99912 | 1,8 | 0.00088 |
| . 46 | . 20120 | 435,2 | . 20206 | 433,4 | . 99914 | 1,7 | . 00086 |
| . 47 | . 20555 | 435, I | . 20639 | 433,5 | . 99916 | 1,7 | . 00084 |
| . 48 | . 20990 | 435, I | . 21073 | 433,5 | .99918 | 1,6 | . 00082 |
| . 49 | .21425 | 435, 1 | . 21506 | 433,5 | .99919 | 1,6 | .0008I |
| $3 \cdot 50$ | 1.21860 | 435,1 | 1. 21940 | 433,5 | 9.9992 I | 1,6 | 0.00079 |
| $u$ | $\log \tan g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.50 | I. 21860 | 435, 1 | 1.21940 | 433,5 | 9.9992 I | 1,6 | 0.00079 |
| . 51 | . 22296 |  | . 22373 |  | . 99922 |  | . 00078 |
| . 52 | . 22731 |  | . 22807 |  | . 99924 | I,5 | . 00076 |
| . 53 | .23166 | 435,0 | . 23240 |  | . 99925 |  | . 00075 |
| . 54 | .2360I |  | . 23674 | 433,6 | . 99927 |  | . 00073 |
| 3.55 | 1. 24036 | 435,0 | 1.24107 | 433,6 | 9.99928 | I,4 | 0.00072 |
| . 56 | . 24471 |  | . 24541 |  | . 99930 |  | . 00070 |
| . 57 | . 24906 |  | . 24975 |  | . 9993 I |  | . 00069 |
| . 58 | . 25341 |  | . 25408 |  | . 99933 | 1,3 | . 00067 |
| . 59 | . 25776 |  | . 25842 |  | . 99934 |  | . 00066 |
| 3.60 | 1.262 II | 434,9 | 1.26275 | 433,6 | 9.99935 | 1,3 | 0.00065 |
| .61 | . 26646 |  | . 26709 | 433,7 | . 99936 |  | . 00064 |
| . 62 | . 27080 |  | . 27143 |  | . 99938 | 1,2 | . 00062 |
| . 63 | . 27515 |  | .27576 |  | . 99939 |  | . 00061 |
| . 64 | . 27950 |  | . 28010 |  | . 99940 |  | . 00060 |
| 3.65 | $\text { 1. } 28385$ | 434,9 | $\text { I. } 28444$ | 433,7 | 9.99941 | 1,2 | 0.00059 |
| . 66 | $.28820$ |  | $.28878$ |  | . 99942 |  | . 00058 |
| . 67 | . 29255 |  | . 29311 |  | . 99944 | I, I | . 00056 |
| . 68 | . 29690 | 434,8 | . 29745 |  | . 99945 |  | . 00055 |
| . 69 | . 30125 |  | . 30179 | 433,8 | . 99946 |  | . 00054 |
| 3.70 | I. 30559 | 434,8 | 1.30612 | 433,8 | 9.99947 | I, I | 0.00053 |
| . 71 | . 30994 |  | . 31046 |  | . 99948 | 1,0 | . 00052 |
| . 72 | . 31429 |  | . 31480 |  | . 99949 |  | . 0005 I |
| . 73 | . 31864 |  | . 31914 |  | . 99950 |  | . 00050 |
| . 74 | . 32299 |  | . 32348 |  | .9995I |  | . 00049 |
| 3.75 | I. 32733 | 434,8 | 1.32781 | 433,8 | 9.99952 | 1,0 | 0.00048 |
| . 76 | . 33 I68 |  | . 33215 |  | . 99953 | 0,9 | . 00047 |
| . 78 | . 33603 |  | . 33649 |  | . 99954 |  | . 00046 |
| . 78 | . 34038 | 434,7 | - 34083 |  | . 99955 |  | . 00045 |
| . 79 | . 34472 |  | . 34517 | 433,9 | . 99956 |  | . 00044 |
| 3.80 | 1.34907 | 434,7 | 1.34951 | 433,9 | 9.99957 | 0,9 | 0.00043 |
| . 8 I | . 35342 |  | . 35384 |  | . 99957 |  | . 00043 |
| . 82 | . 35777 |  | -35818 |  | . 99958 | 0,8 | . 00042 |
| . 83 | . 36211 |  | . 36252 |  | $\text { . } 99959$ |  | . 000041 |
| . 84 | . 36646 |  | . 36686 |  | . 99960 |  | . 00040 |
| 3.85 | 1.3708I | 434,7 | 1. 37120 | 433,9 | 9.9996 I | 0,8 | 0.00039 |
| . 86 | -37515 |  | . 37554 |  | . 99961 |  | . 00039 |
| . 87 | . 37950 |  | . 37988 |  | . 99962 |  | . 00038 |
| . 88 | -38385 |  | -38422 |  | . 99963 | 0,7 | . 00037 |
| . 89 | . 38819 |  | . 38856 |  | . 99964 |  | . 00036 |
| 3.90 | I. 39254 | 434,7 | 1. 39290 | 433,9 | 9.99964 | 0,7 | 0.00036 |
| .91 | . 39689 | 434,6 | - 39724 |  | . 99965 |  | . 00035 |
| . 92 | . 40123 |  | . 40158 | 434,0 | . 99966 |  | . 00034 |
| . 93 | . 40558 |  | . 40591 |  | . 99966 |  | . 00034 |
| . 94 | . 40993 |  | . 41025 |  | . 99967 |  | . 00033 |
|  | I. 41427 | 434,6 | 1.41459 | 434,0 |  | 0,6 | 0.00032 |
| . 96 | . 41862 |  | . 41893 |  | . 99968 |  | . 00032 |
| . 97 | . 42296 |  | . 42327 |  | . 99969 |  | . 00031 |
| . 98 | . 42731 |  | . 42761 |  | . 99970 |  | . 00030 |
| . 99 | .43166 |  | . 43195 |  | . 99970 |  | . 00030 |
| 4.00 | 1.43600 | 434,6 | 1. 43629 | 434,0 | 9.9997 I | 0,6 | 0.00029 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} u$ |

Logarithms of Hyperbolic Functions.

| $u$ | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.00 | I. 43600 | 434,6 | 1.43629 | 434,0 | 9.99971 | 0,6 | 0.00029 |
| . OI | . 44035 |  | . 44063 |  | .9997I |  | . 00029 |
| . 02 | . 44469 |  | . 44497 |  | . 99972 |  | . 00028 |
| . 03 | . 44904 |  | . 4493 I |  | . 99973 | 0,5 | . 00027 |
| . 04 | . 45339 |  | . 45365 |  | . 99973 |  | . 00027 |
| 4.05 | I. 45773 | 434,6 | 1.45799 | 434,0 | 9.99974 | 0,5 | 0.00026 |
| . 06 | . 46208 |  | . 46233 |  | . 99974 |  | . 00026 |
| . 07 | . 46642 | 434,5 | . 46668 |  | . 99975 |  | . 00025 |
| . 08 | . 47077 |  | .47102 |  | . 99975 |  | . 00025 |
| . 09 | .475II |  | .47536 | 434, I | . 99976 |  | . 00024 |
| 4.10 | 1.47946 | 434,5 | 1.47970 | 434, 1 | 9.99976 | 0,5 | 0.00024 |
| . II | . 48380 |  | . 48404 |  | . 99977 |  | . 00023 |
| . 12 | .488I5 |  | . 48838 |  | . 99977 |  | . 00023 |
| . 13 | . 49249 |  | . 49272 |  | . 99978 | 0,4 | . 00022 |
| . 14 | . 49684 |  | . 49706 |  | . 99978 |  | . 00022 |
| 4.15 | 1.50118 | 434,5 | I. 50140 | 434, I | 9.99978 | 0,4 | 0.00022 |
| . 16 | . 50553 |  | . 50574 |  | . 99979 |  | . 0002 I |
| . 17 | . 50987 |  | . 51008 |  | . 99979 |  | . 0002 I |
| . 18 | . 51422 |  | . 51442 |  | . 99980 |  | . 00020 |
| . 19 | .51856 |  | .51876 |  | . 99980 | - | . 00020 |
| 4.20 | 1.52291 | 434,5 | 1.52310 | 434, I | 9.99980 | 0,4 | 0.00020 |
| . 21 | . 52725 |  | . 52745 |  | . 99981 |  | . 00019 |
| . 22 | . 53160 |  | . 53179 |  | .9998I |  | .00019 |
| . 23 | . 53594 |  | . 53613 |  | . 99982 |  | . 00018 |
| . 24 | . 54029 |  | . 54047 |  | . 99982 |  | . 00018 |
| 4.25 | 1. 54463 | 434,5 | 1. 5448 | 434, 1 | 9.99982 | 0,4 | 0.00018 |
| . 26 | . 54898 |  | . 54915 |  | . 99983 | 0,3 | . 00017 |
| . 27 | - 55332 |  | - 55349 |  | . 99983 |  | .00017 |
| . 28 | . 55767 |  | . 55783 |  | . 99983 |  | .00017 |
| . 29 | . 56201 |  | . 56217 |  | . 99984 |  | . 00016 |
| $4 \cdot 30$ | 1. 56636 | 434,5 | 1.56652 | 434, I | 9.99984 | 0,3 | 0.00016 |
| . 31 | . 57070 |  | . 57086 |  | . 99984 |  | . 00016 |
| . 32 | . 57505 | 434,4 | . 57520 |  | . 99985 |  | . 00015 |
| . 33 | . 57939 |  | . 57954 | - | . 99985 |  | . 00015 |
| . 34 | . 58373 |  | . 58388 |  | . 99985 |  | . 00015 |
| $4 \cdot 35$ | 1. 58808 | 434,4 | 1.58822 | 434, I | 9.99986 | 0,3 | 0.00014 |
| . 36 | . 59242 |  | . 59256 | 434,2 | . 99986 |  | . 00014 |
| . 37 | . 59677 |  | . 59691 |  | . 99986 |  | . 00014 |
| . 38 | . 6011 I |  | . 60125 |  | . 99986 |  | . 00014 |
| . 39 | . 60546 |  | . 60559 |  | . 99987 |  | .00013 |
| 4.40 | 1. 60980 | 434,4 |  | 434,2 |  | 0,3 | 0.00013 |
| . 41 | .6I414 |  | .6I427 |  | . 99987 |  | .00013 |
| . 42 | . 61849 |  | . 61851 |  | . 99987 |  | .00013 |
| . 43 | . 62283 |  | . 62296 |  | . 99988 | 0,2 | .00012 |
| . 44 | . 62718 |  | . 62730 |  | . 99988 |  | . 00012 |
| 4.45 |  | 434,4 | $1.63164$ | 434,2 | $9.99988$ | 0,2 | 0.00012 |
| . 46 | . 63587 |  | . 63598 |  | . 99988 |  | . 00012 |
| . 47 | . 64021 |  | . 64032 |  | . 99989 |  | . 00011 |
| . 48 | . 64455 |  | . 64467 |  | . 99989 |  | .00011 .00011 |
| . 49 | . 64890 |  | .64901 |  | -99989 |  | . 0001 I |
| 4.50 | 1. 65324 | 434,4 | 1.65335 | 434,2 | 9.99989 | 0,2 | 0.0001 I |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \operatorname{gd} u$ |

Logarithms of Hyperbolic Functions.

| u | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $4 \cdot 50$ | 1.65324 | 434,4 | 1. 65335 | 434,2 | 9.99989 | 0,2 | 0.0001 I |
| . 51 | . 65759 |  | . 65769 |  | . 99989 |  | .000I I |
| . 52 | . 66193 |  | . 66203 |  | . 99990 |  | .00010 |
| . 53 | . 66627 |  | . 66637 |  | . 99990 |  | .00010 |
| . 54 | . 67062 |  | . 67072 |  | . 99990 |  | .00010 |
| $4 \cdot 55$ | I. 67496 | 434,4 | 1.67506 | 434,2 | 9.99990 | 0,2 | 0.00010 |
| . 56 | . 6793 I |  | . 67940 |  | . 99990 |  | .00010 |
| . 57 | . 68365 |  | . 68374 |  | .99991 |  | . 00009 |
| . 58 | . 68799 |  | . 68808 |  | .99991 |  | . 00009 |
| . 59 | . 69234 |  | . 69243 |  | . 99991 |  | . 00009 |
| 4.60 | 1. 69668 | 434,4 | - 1. 69677 | 434,2 | 9.99991 | 0,2 | 0.00009 |
| .61 | . 70102 |  | . 70111 |  | . 99991 |  | . 00009 |
| . 62 | . 70537 |  | . 70545 |  | . 99992 |  | . 00008 |
| . 63 | . 70971 |  | . 70979 |  | . 99992 |  | . 00008 |
| . 64 | . 71406 |  | .71414 |  | . 99992 |  | . 00008 |
| 4.65 | 1.71840 | 434,4 | 1.71848 | 434,2 | 9.99992 | 0,2 | 0.00008 |
| . 66 | . 72274 |  | . 72282 |  | . 99992 |  | . 00008 |
| . 67 | . 72709 |  | . 72716 |  | - . 99992 |  | . 00008 |
| . 68 | .73143 |  | .7315I |  | . 99993 | O,I | . 00007 |
| . 69 | . 73577 |  | . 73585 |  | . 99993 |  | . 00007 |
| 4.70 | 1.74012 | 434,4 | 1.74019 | 434,2 | 9.99993 | O,I | 0.00007 |
| . 71 | . 74446 |  | . 74453 |  | . 99993 |  | . 00007 |
| . 72 | .7488I |  | . 74887 |  | . 99993 |  | . 00007 |
| . 73 | . 75315 |  | . 75322 |  | . 99993 |  | . 00007 |
| . 74 | . 75749 |  | . 75756 |  | . 99993 |  | . 00007 |
| 4.75 | 1.76184 | 434,4 | 1.76190 | 434,2 | 9.99993 | O, I | 0.00007 |
| . 76 | . 76618 |  | . 76624 |  | . 99994 |  | . 00006 |
| . 77 | . 77052 |  | . 77059 |  | . 99994 |  | . 00006 |
| . 78 | . 77487 |  | . 77493 |  | . 99994 |  | . 00006 |
| . 79 | .7792I |  | . 77927 |  | . 99994 |  | . 00006 |
| 4.80 | 1.78355 | 434,4 | I.78361 | 434,2 | 9.99994 | O,I | 0.00006 |
| .8I | . 78790 |  | . 78796 |  | . 99994 |  | . 00006 |
| . 82 | . 79224 |  | . 79230 |  | . 99994 |  | . 00006 |
| . 83 | . 79658 | 434,3 | . 79664 |  | . 99994 |  | . 00006 |
| . 84 | . 80093 |  | . 80098 |  | . 99995 |  | . 00005 |
|  |  | 434,3 |  | 434,2 | 9.99995 | O,I | 0.00005 |
| . 86 | . 80962 |  | . 80967 |  | . 99995 |  | . 00005 |
| . 87 | . 81396 |  | :81401 |  | . 99995 |  | .00005 |
| . 88 | .81830 |  | . 81835 |  | . 99995 |  | . 00005 |
| . 89 | . 82265 |  | . 82269 |  | . 99995 |  | . 00005 |
| 4.90 | 1.82699 | 434,3 | 1.82704 | 434,2 | 9.99995 | 0,I | 0.00005 |
| .91 | . 83133 |  | . 83138 |  | . 99995 |  | . 00005 |
| . 92 | . 83568 |  | . 83572 |  | . 99995 |  | . 00005 |
| . 93 | . 84002 |  | . 84006 |  | . 99995 |  | . 00005 |
| . 94 | . 84436 |  | . 84441 | 434,3 | . 99996 |  | . 00004 |
| 4.95 | 1.84871 | 434,3 | 1.84875 | 434,3 | 9.99996 | O,I | 0.00004 |
| . 96 | . 85305 |  | . 85309 |  | . 99996 |  | . 00004 |
| . 97 | . 85739 |  | . 85743 |  | . 99996 |  | . 00004 |
| . 98 | . 86174 |  | . 86178 |  | . 99996 |  | . 00004 |
| . 99 | . 86608 |  | . 86612 |  | . 99996 |  | . 00004 |
| 5.00 | 1.87042 | 434,3 | 1. 87046 | 434,3 | 9.99996 | O,I | 0.00004 |
| $u$ | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc g \mathrm{~d} u$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.00 | 1.87042 | 434,3 | 1.87046 | 434,3 | 9.99996 | O, I | 0.00004 |
| . 01 | . 87477 |  | . 87480 |  | . 99996 |  | . 00004 |
| . 02 | . 87911 |  | . 87915 |  | . 99996 |  | . 00004 |
| . 03 | . 88345 |  | . 88349 |  | . 99996 |  | . 00004 |
| . 04 | . 88780 |  | .88783 |  | . 99996 |  | . 00004 |
| 5.05 | 1.89214 | 434,3 | 1.89217 | 434,3 | 9.99996 | O,I | 0.00004 |
| . 06 | . 89648 |  | . 89652 |  | . 99997 |  | . 00003 |
| . 07 | . 90083 |  | . 90086 |  | . 99997 |  | . 00003 |
| . 08 | . 90517 |  | . 90520 |  | . 99997 |  | . 00003 |
| . 09 | . 90951 |  | . 90955 |  | . 99997 |  | . 00003 |
| 5.10 | 1.91386 | 434,3 | 1.91389 | 434,3 | 9.99997 | O,I | 0.00003 |
| . II | . 91820 |  | .91823 |  | . 99997 |  | . 00003 |
| . 12 | . 92254 |  | . 92257 |  | . 99997 |  | . 00003 |
| . 13 | . 92689 |  | . 92692 |  | . 99997 |  | . 00003 |
| . 14 | . 93123 |  | .93126 |  | . 99997 |  | .00003 |
| 5.15 | 1.93557 | 434,3 | 1.93560 | 434,3 | 9.99997 | O,I | 0.00003 |
| . 16 | . 93992 |  | . 93994 |  | . 99997 |  | . 00003 |
| . 17 | . 94426 |  | - . 94429 |  | . 99997 |  | . 00003 |
| . 18 | . 94860 |  | . 94863 |  | . 99997 |  | . 00003 |
| . 19 | . 95294 |  | . 95297 |  | . 99997 |  | . 00003 |
| 5.20 | 1. 95729 | 434,3 | 1.95731 | 434,3 | 9.99997 | O,I | 0.00003 |
| . 21 | . 96163 |  | .95166 |  | . 99997 |  | . 00003 |
| . 22 | . 96597 |  | . 96600 |  | . 99997 |  | . 00003 |
| .23 | . 97032 |  | . 97034 |  | . 99998 | 0,0 | . 00002 |
| . 24 | . 97466 |  | . 97469 |  | . 99998 |  | . 00002 |
| 5.25 | 1.97900 | 434,3 | 1.97903 | 434,3 | 9.99998 | 0,0 | 0.00002 |
| . 26 | . 98335 |  | . 98337 |  | . 99998 |  | . 00002 |
| . 27 | . 98769 |  | .98771 |  | . 99998 |  | . 00002 |
| . 28 | . 99203 |  | . 99206 |  | . 99998 |  | . 00002 |
| . 29 | . 99638 |  | . 99640 |  | . 99998 |  | . 00002 |
| $5 \cdot 30$ | 2.00072 | 434,3 | 2.00074 | 434,3 | 9.99998 | 0,0 | 0.00002 |
| . 31 | . 00506 |  | . 00508 |  | . 99998 |  | . 00002 |
| . 32 | . 00941 |  | . 00943 |  | . 99998 |  | . 00002 |
| . 33 | .01375 |  | . 01377 |  | . 99998 |  | . 00002 |
| . 34 | . 01809 |  | .018II |  | . 99998 |  | . 00002 |
|  |  | 434,3 | 2.02246 | 434,3 | 9.99998 | 0,0 | 0.00002 |
| . 36 | $.02678$ |  | . 02680 |  | . 99998 |  | . 00002 |
| . 37 | .03112 |  | .03II4 |  | . 99998 |  | . 00002 |
| . 38 | . 03547 |  | . 03548 |  | . 99998 |  | . 00002 |
| . 39 | .0398I |  | .03983 |  | . 99998 |  | . 00002 |
| 5.40 | 2.04415 | 434,3 | 2.04417 | 434,3 |  | 0,0 | 0.00002 |
| . 41 | . 04849 |  | . 04851 |  | . 99998 |  | . 00002 |
| .42 | . 05284 |  | . 05285 |  | . 99998 |  | . 00002 |
| . 43 | .05718 |  | . 05720 |  | . 99998 |  | . 00002 |
| . 44 | . 06152 |  | .06154 |  | . 99998 |  | . 00002 |
| 5.45 | 2.06587 | 434,3 | 2.06588 | 434,3 | 9.99998 | 0,0 | 0.00002 |
| . 46 | . 07021 |  | . 07023 |  | . 99998 |  | . 00002 |
| . 47 | . 07455 |  | . 07457 |  | . 99998 |  | . 00002 |
| . 48 | . 07890 |  | $.07891$ |  | . 99998 |  | . 00002 |
| . 49 | . 08324 |  | . 08325 |  | . 99999 |  | .00001 |
| 5.50 | 2.08758 | 434,3 | 2.08760 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| u | $\log \operatorname{tangd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \csc \mathrm{gd} \mathrm{u}$ |

Logarithms of Hyperbolic Functions.

| 4 | $\log \sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cosh u$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{l o g} \tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ coth u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.50 | 2.08758 | 434,3 | 2.08760 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 51 | . 09193 |  | . 09194 |  | . 99999 |  | .0000I |
| . 52 | . 09627 |  | . 09628 |  | . 99999 |  | .0000I |
| . 53 | . 1006I |  | . 10063 |  | . 99999 |  | .00001 |
| . 54 | . 10495 |  | . 10497 |  | . 99999 |  | .00001 |
| 5.55 | 2. 10930 | 434,3 | 2. 10931 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 56 | . II364 |  | . 11365 |  | . 99999 |  | .00001 |
| . 57 | . 11798 |  | . 11800 |  | . 99999 |  | .00001 |
| . 58 | . 12233 |  | . 12234 |  | . 99999 |  | . 00001 |
| . 59 | . I2667 |  | . 12668 |  | . 99999 |  | .0000I |
| 5.60 | 2.13101 | 434,3 | 2.13103 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 61 | . 13536 |  | . I3537 |  | . 99999 |  | .0000I |
| . 62 | . I3970 |  | . I397I |  | . 99999 |  | .0000I |
| . 63 | . 14404 |  | . 14405 |  | . 99999 |  | .0000I |
| . 64 | . 14839 |  | . 14840 |  | . 99999 |  | .0000I |
| 5.65 | 2. 15273 | 434,3 | 2. 15274 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 66 | . 15707 |  | . 15708 |  | -99999 |  | . 00001 |
| . 67 | .16141 |  | .16142 |  | . 99999 |  | .0000I |
| . 68 | . 16576 |  | . 16577 |  | . 99999 |  | .0000I |
| . 69 | .17010 |  | . 1701 I |  | . 99999 |  | .0000I |
| 5.70 | 2.17444 | 434,3 | 2.17445 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 71 | . 17879 |  | . 17880 |  | . 99999 |  | . 00001 |
| . 72 | .18313 |  | .183I4 |  | . 99999 |  | . 0000 I |
| . 73 | . 18747 |  | . 18748 |  | . 99999 |  | .0000I |
| . 74 | . 19182 |  | . 19182 |  | . 99999 |  | . 00001 |
| 5.75 | 2.19616 | 434,3 | 2.19617 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 76 | . 20050 |  | . 20051 |  | . 99999 |  | .00001 |
| . 77 | . 20484 |  | . 20485 |  | . 99999 |  | .0000I |
| . 78 | . 20919 |  | . 20920 |  | - 99999 |  | . 00001 |
| . 79 | . 21353 |  | . 21354 |  | . 99999 |  | . 0000I |
| 5.80 | 2.21787 | 434,3 | 2.21788 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| .81 | . 22222 |  | . 22222 |  | . 99999 |  | . 00001 |
| . 82 | . 22656 |  | . 22657 |  | . 99999 |  | . 00001 |
| . 83 | . 23090 |  | . 23091 |  | . 99999 |  | . 00001 |
| . 84 | . 23525 |  | . 23525 |  | . 99999 |  | . 00001 |
| 5.85 | 2.23959 | 434,3 | 2.23960 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 85 | . 24393 |  | . 24394 |  | . 99999 |  | . 00001 |
| . 87 | . 24828 |  | . 24828 |  | . 99999 |  | . 00001 |
| . 88 | . 25262 |  | . 25262 |  | . 99999 |  | . 00001 |
| . 89 | . 25696 |  | . 25697 |  | . 99999 |  | . 00001 |
| 5.90 | 2.26130 | 434,3 | 2.26131 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| .91 | . 26565 |  | . 26565 |  | . 99999 |  | . 00001 |
| . 92 | . 26999 |  | . 27000 |  | . 99999 |  | . 00001 |
| . 93 | . 27433 |  | . 27434 |  | . 99999 |  | . 00001 |
| . 94 | . 27868 |  | .27868 |  | . 99999 |  | . 00001 |
| 5.95 | 2.28302 | 434,3 | 2.28303 | 434,3 | 9.99999 | 0,0 | 0.00001 |
| . 96 | . 28736 |  | . 28737 |  | . 99999 |  | . 00001 |
| . 97 | . 29171 |  | . 29171 |  | . 99999 |  | . 00001 |
| . 98 | . 29605 |  | . 29605 |  | . 99999 |  | . 00001 |
| . 99 | - 30039 |  | - 30040 |  | . 99999 |  | . 00001 |
| 6.00 | 2.30473 | 434,3 | $2.3047 \hat{4}$ | 434,3 | 9.99999 | 0,0 | 0.00001 |
| u | $\log \tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sec \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin g d u$ | $\omega F^{\prime}{ }^{\prime}$ | $\log \csc g \mathrm{gd} u$ |

## TABLE II

## NATURAL HYPERBOLIC FUNCTIONS

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathrm{Fo}^{\prime}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0000 | 0.00000 | 10,0 | 1.00000 | 0,0 | 0.00000 | 10,0 | $\infty$ | $\infty$ |
| . 0001 | .00010 |  | . 00000 |  | . .00010 |  | 10000.00 | 1000000,0 |
| . 0002 | . 00020 | - | . 00000 |  | . 00020 |  | 5000.00 | 250000,0 |
| . 0003 | . 00030 |  | . 00000 |  | . 00030 |  | 3333.33 | IIIIII, I |
| . 0004 | . 00040 |  | . 00000 |  | . 00040 |  | 2500.00 | 62500,0 |
| 0.0005 | 0.00050 | 10,0 | 1.00000 | 0,0 | 0.00050 | 10,0 | 2000.00 | 40000,0 |
| . 0006 | . 00060 |  | . 00000 |  | . 00060 |  | 1666.67 | 27777,8 |
| . 0007 | . 00070 |  | . 00000 |  | . 00070 |  | 1428.57 | 20408,2 |
| . 0008 | . 00080 |  | . 00000 |  | . 00080 |  | 1250.00 | 15625,0 |
| . 0009 | . 00090 |  | . 00000 |  | . 00090 |  | IIII.II | 12345,7 |
| 0.0010 | 0.00100 | 10,0 | 1.00000 | 0,0 | 0.00100 | 10,0 | 1000.00 | 10000,0 |
| .001 I | .001 10 |  | . 00000 |  | .001 10 |  | 909.09 | 8264,5 |
| .0012 | .00120 |  | . 00000 |  | .00120 |  | 833.33 | 6944,4 |
| . 0013 | .00130 |  | . 00000 |  | .00130 |  | 769.23 | 5917,2 |
| . 0014 | .00140 |  | . 00000 |  | .00140 |  | 714.29 | 5102,0 |
| 0.0015 | 0.00150 | 10,0 | 1.00000 | 0,0 | 0.00150 | 10,0 | 666.67 | 4444, 4 |
| .0016 | .00160 |  | . 00000 |  | . 00160 |  | 625.00 | 3906,2 |
| .0017 | .00170 |  | . 00000 |  | .00170 |  | 588.24 | 3460,2 |
| .0018 | .00180 |  | . 00000 |  | . 00180 |  | 555.56 | 3086,4 |
| .0019 | .00190 |  | . 00000 |  | .00190 |  | 526.32 | 2770, I |
| 0.0020 | 0.00200 | 10,0 | 1.00000 | 0,0 | 0.00200 | 10,0 | 500.00 | 2500,0 |
| . 0021 | .00210 |  | . 00000 |  | . 00210 |  | 476.19 | 2267,6 |
| . 0022 | . 00220 |  | . 00000 |  | . 00220 |  | 454.55 | 2066, I |
| . 0023 | . 00230 |  | . 00000 |  | . 00230 |  | 434.78 | 1890,4 |
| . 0024 | . 00240 |  | . 00000 |  | . 00240 |  | 416.67 | 1736,1 |
| 0.0025 | 0.00250 | 10,0 | 1.00000 | 0,0 | 0.00250 | 10,0 | 400.00 | 1600,0 |
| . 0026 | . 00260 |  | . 00000 |  | . .00260 | : | 384.62 | 1479,3 |
| . 0027 | . 00270 |  | . 00000 |  | . 00270 |  | 370.37 | 1371,7 |
| . 0028 | . 00280 |  | . 00000 |  | . 00280 |  | 357.14 | 1275,5 |
| . 0029 | . 00290 |  | . 00000 |  | . 00290 |  | 344.83 | 1189,1 |
| 0.0030 | 0.00300 | 10,0 | 1.00000 | 0,0 | 0.00300 | 10,0 | $333 \cdot 33$ | IIII, 1 |
| . 0031 | .00310 |  | . 00000 |  | . 00310 |  | 322.58 | IO40,6 |
| . 0032 | . 00320 |  | . 00001 |  | . 00320 |  | 312.50 | 976,6 |
| . 0033 | . 00330 |  | .00001 |  | . 00330 |  | 303.03 | 918,3 |
| . 0034 | . 00340 |  | .0000I |  | . 00340 |  | 294.12 | 865, I |
| 0.0035 | 0.00350 | 10,0 | 1.00001 | 0,0 | 0.00350 | 10,0 | 285.72 | 816,3 |
| . 0036 | . 00360 |  | . 00001 |  | . 00360 |  | 277.78 | 771,6 |
| . 0037 | . 00370 |  | . 00001 |  | . 00370 |  | 270.27 | 730,5 |
| . 0038 | . 00380 |  | .0000I |  | . 00380 |  | 263.16 | 692,5 |
| . 0039 | . 00390 |  | .0000I |  | . 00390 |  | 256.41 | 657,5 |
| 0.0040 | 0.00400 | 10,0 | 1.00001 | 0,0 | 0.00400 | 10,0 | 250.00 | 625,0 |
| .004I | . 00410 |  | . 00001 |  | .00410 |  | 243.90 | 594,9 |
| . 0042 | . 00420 |  | . 00001 |  | . 00420 |  | 238.10 | 560,9 |
| . 0043 | . 00430 |  | . 00001 |  | . 00430 |  | 232.56 | 540,8 |
| . 0044 | . 00440 |  | .0000I |  | . 00440 |  | 227.27 | 516,5 |
| 0.0045 | 0.00450 | 10,0 | 1.00001 | 0,0 | 0.00450 | 10,0 | 222.22 | 493,8 |
| . 0046 | . 00460 |  | . 00001 |  | . 00460 |  | 217.39 | 472,6 |
| . 0047 | . 00470 |  | . 00001 |  | . 00470 |  | 212.77 | 452,7 |
| . 0048 | . 00480 |  | . 00001 |  | . 00480 |  | 208.33 | 434,0 |
| . 0049 | . 00490 |  | . 00001 |  | . 00490 |  | 204.08 | 416,5 |
| 0.0050 | 0.00500 | 10,0 | 1.00001 | O, I | 0.00500 | 10,0 | 200.00 | 400,0 |
| U | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0050 | 0.00500 | 10,0 | 1.00001 | O,I | 0.00500 | 10,0 | 200.00 | 400,0 |
| .0051 | . 00510 |  | .00001 |  | . 00510 |  | 196.08 | 384,5 |
| . 0052 | . 00520 |  | .0000I |  | . 00520 |  | 192.31 | 369,8 |
| . 0053 | . 00530 |  | . 00001 |  | . 00530 |  | 188.68 | 356,0 |
| . 0054 | . 00540 |  | .00001 |  | . 00540 |  | 185.19 | 342,9 |
| 0.0055 | 0.00550 | 10,0 | 1.00002 | O, I | 0.00550 | 10,0 | 181.82 | 330,6 |
| . 0056 | . 00560 |  | . 00002 |  | . 00560 |  | 178.57 | 318,9 |
| . 0057 | . 00570 |  | . 00002 |  | . 00570 |  | 175.44 | 307,8 |
| . 0058 | . 00580 |  | . 00002 |  | . 00580 |  | 172.42 | 297,3 |
| . 0059 | . 00590 |  | . 00002 |  | . 00590 |  | 169.49 | 287,3 |
| 0.0060 | 0.00600 | 10,0 | 1.00002 | O,I | 0.00600 | 10,0 | 166.67 | 277,8 |
| .0061 | . 00510 |  | . 00002 |  | . 00610 |  | 163.94 | 268,7 |
| . 0062 | . 00620 |  | . 00002 |  | . 00520 |  | 161.29 | 260, I |
| . 0063 | . 00530 |  | . 00002 |  | . 00630 |  | 158.73 | 25I,9 |
| . 0064 | . 00640 |  | . 00002 |  | . 00640 |  | 156.25 | 244, I |
| 0.0065 | 0.00650 | 10,0 | 1.00002 | O,I | 0.00650 | 10,0 | 153.85 | 236,7 |
| . 0066 | . 00660 |  | . 00002 |  | . 00660 |  | 151.52 | 229,6 |
| . 0067 | . 00670 |  | . 00002 |  | . 00570 |  | 149.26 | 222,8 |
| . 0068 | . 00680 |  | . 00002 |  | . 00580 |  | 147.06 | 216,3 |
| . 0069 | . 00690 |  | . 00002 |  | .00690 |  | 144.93 | 210,0 |
| 0.0070 | 0.00700 | 10,0 | 1.00002 | O,I | 0.00700 | 10,0 | 142.86 | 204, I |
| .0071 | . 00710 |  | . 00003 |  | . 00710 |  | 140.85 | 198,4 |
| . 0072 | . 00720 |  | . 00003 |  | . 00720 |  | 138.89 | 192,9 |
| . 0073 | . 00730 |  | . 00003 |  | . 00730 |  | 136.99 | 187,6 |
| . 0074 | . 00740 |  | . 00003 |  | :00740 |  | I 35.14 | 182,6 |
| 0.0075 | 0.00750 | 10,0 | 1.00003 | O,I | 0.00750 | 10,0 | 133.34 | 177,8 |
| . 0076 | . 00760 |  | . 00003 |  | . 00760 |  | 131.58 | 173,1 |
| . 0077 | . 00770 |  | . 00003 |  | . 00770 |  | 129.87 | 168,7 |
| .0078 | . 00780 |  | . 00003 |  | . 00780 |  | 128.21 | 164,4 |
| . 0079 | . 00790 |  | . 00003 |  | . 00790 |  | 126.58 | 160,2 |
| 0.0080 | 0.00800 | 10,0 | 1.00003 | OI, | 0.00800 | 10,0 | 125.00 | 156,2 |
| . 0081 | .00810 |  | . 00003 |  | .00810 |  | 123.46 | 152,4 |
| . 0082 | . 00820 |  | . 00003 |  | . 00820 |  | 121.95 | 148,7 |
| . 0083 | . 00830 |  | . 00003 |  | . 00830 |  | 120.48 | 145,2 |
| . 0084 | . 00840 |  | . 00004 |  | . 00840 |  | 119.05 | 141,7 |
| 0.0085 | 0.00850 | 10,0 | 1.00004 | O,I | 0.00850 | 10,0 | 117.65 | 138,4 |
| . 0086 | . 00860 |  | . 00004 |  | . 00860 |  | 116.28 | 135,2 |
| . 0087 | . 00870 |  | . 00004 |  | . 00870 |  | 114.95 | I32, I |
| . 0088 | . 00880 |  | . 00004 |  | . 00880 |  | 113.64 | I29, I |
| . 0089 | . 00890 |  | . 00004 |  | . 00890 |  | 112.36 | 126,2 |
| 0.0090 | 0.00900 | 10,0 | 1.00004 | O,I | 0.00900 | 10,0 | III. II | 123,5 |
| .0091 | .00910 |  | . 00004 |  | . 00910 |  | 109.89 | I20,8 |
| . 0092 | . 00920 |  | . 00004 |  | . 00920 |  | 108.70 | 118,1 |
| . 0093 | . 00930 |  | . 00004 |  | . 00930 |  | 107.53 | I 15,6 |
| . 0094 | . 00940 |  | . 00004 |  | . 00940 |  | 106.39 | II3,2 |
| 0.0095 | 0.00950 | 10,0 | 1.00005 | O,I | 0.00950 | 10,0 | 105.27 | I 10,8 |
| . 0096 | . 00960 |  | . 00005 |  | . 00960 |  | 104. 17 | 108,5 |
| . 0097 | . 00970 |  | . 00005 |  | . 00970 |  | 103.10 | 106,3 |
| . 0098 | . 00980 |  | . 00005 |  | .00980 |  | 102.04 | 104, 1 |
| . 0099 | . 00990 |  | . 00005 |  | . 00990 |  | 101.OI | 102,0 |
| 0.0100 | 0.01000 | 10,0 | 1.00005 | 0,1 | 0.01000 | 10,0 | 100.00 | 100,0 |
| u | $\boldsymbol{t a n g d} u$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | - F ${ }_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\infty \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0100 | 0.01000 | 10,0 | 1.00005 | 0,1 | 0.01000 | 10,0 | 100.003 | 1000,0 |
| . 0101 | . 01010 |  | . 00005 |  | . 01010 |  | 99.013 | 980,3 |
| . 0102 | . 01020 |  | . 00005 |  | . 01020 |  | 98.043 | 961, |
| . 0103 | . 01030 |  | . 00005 |  | . 01030 |  | 97.091 | 942,6 |
| . 0104 | . 01040 |  | . 00005 |  | . 01040 |  | 96.157 | 924,5 |
| 0.0105 | 0.01050 | 10,0 | 1.00006 | 0,1 | 0.01050 | 10,0 | 95.242 | 907,0 |
| . 0106 | . 01060 |  | . 00006 |  | . 01060 |  | 94.343 | 890,0 |
| . 0107 | .01070 |  | . 00006 |  | . 01070 |  | 93.462 | 873,4 |
| . 0108 | .01080 |  | . 00006 |  | . 01080 |  | 92.595 | 857,3 |
| . 0109 | .01090 |  | . 00006 |  | . 01090 |  | 91.747 | 841,6 |
| 0.0110 | 0.01100 | 10,0 | 1.00005 | O,I | 0.01100 | 10,0 | 90.913 | 826,4 |
| . OIII | .01IIO |  | . 00006 |  | .OIIIO |  | 90.094 | 8il,6 |
| . 0112 | . O1 I20 |  | . 00006 |  | . O1120 |  | 89.289 | 797,2 |
| .OII3 | .01130 |  | . 00006 |  | .OII30 |  | 88.499 | 783,1 |
| .OII4 | . OI I40 |  | . 00006 |  | . OII 40 |  | 87.723 | 769,4 |
| 0.0115 | 0.01150 | 10,0 | 1.00007 | 0,1 | 0.01150 | 10,0 | 86.960 | 756, 1 |
| .0116 | . 01160 |  | . 00007 |  | . 01160 |  | 86.211 | 743, I |
| . 0117 | . O1I70 |  | . 00007 |  | . 01170 |  | 85.474 | 730,5 |
| .0118 | .01180 |  | . 00007 |  | . 01180 |  | 84.750 | 718,2 |
| . 0119 | . 01190 |  | . 00007 |  | . OII90 |  | 84.038 | 706,1 |
| 0.0120 | 0.01200 | 10,0 | 1.00007 | O,I | 0.01200 | 10,0 | 83.337 | 694,4 |
| . OI 21 | . 01210 |  | . 00007 |  | .01210 |  | 82.649 | 683,0 |
| . 0122 | . 01220 |  | . 00007 |  | . 01220 |  | 81.971 | 671,8 |
| . 0123 | . 01230 |  | . 00008 |  | . 01230 |  | 81. 305 | 660,9 |
| . 0124 | . 01240 |  | . 00008 |  | . 01240 |  | 80.649 | 650,3 |
| 0.0125 | 0.01250 | 10,0 | 1.00008 | O, I | 0.01250 | 10,0 | 80.004 | 640,0 |
| . 0126 | . 01260 |  | . 00008 |  | . 01260 |  | 79.369 | 629,8 |
| . 0127 | . 01270 |  | . 00008 |  | . 01270 |  | 78.744 | 620,0 |
| . 0128 | . 01280 |  | . 00008 |  | . 01280 |  | 78.129 | 610,3 |
| . 0129 | . 01290 |  | . 00008 |  | . 01290 |  | 77.524 | 600,9 |
| 0.0130 | 0.01300 | 10,0 | 1.00008 | 0,I | 0.01300 | 10,0 | 76.927 | 591,7 |
| .OI3I | .01310 |  | . 00009 |  | . 01310 |  | 76.340 | 582,7 |
| . 0132 | . 01320 |  | . 00009 |  | . 01320 |  | 75.762 | 573,9 |
| . 0133 | . 01330 |  | . 00009 |  | .01330 |  | 75.192 | 565,3 |
| . 0134 | . 01340 |  | . 00009 |  | . 01340 |  | 74.631 | 556,9 |
| 0.0135 | 0.01350 | 10,0 | 1.00009 | O,I | 0.01350 | 10,0 | 74.079 | 548,7 |
| .0136 | . 01360 |  | . 00009 |  | . 01360 |  | 73.534 | 540,6 |
| . 0137 | . 01370 |  | . 00009 |  | .01370 |  | 72.997 | 532,8 |
| .0138 | . 01380 |  | .00010 |  | . 01380 |  | 72.468 | 525, 1 |
| .OI39 | . 01390 |  | .00010 |  | . 01390 |  | 71.947 | 517,5 |
| 0.0140 | 0.01400 | 10,0 | 1.00010 | O,I | 0.01400 | 10,0 | 71.433 | 510,2 |
| .0141 | .01410 |  | .00010 |  | .01410 |  | 70.927 | 503,0 |
| . 0142 | . 01420 |  | . 00010 |  | . 01420 |  | 70.427 | 495,9 |
| . 0143 | . 01430 |  | .00010 |  | .01430 |  | 69.935 | 489,0 |
| . 0144 | . 01440 |  | .00010 |  | . 01440 |  | 69.449 | 482,2 |
| 0.0145 | 0.01450 | 10,0 | 1.00011 | 0,I | 0.01450 | 10,0 | 68.970 | 475,6 |
| . 0146 | . 01460 |  | .00011 |  | . 01460 |  | 68.498 | 469, 1 |
| . 0147 | . 01470 |  | .0001 I |  | . 01470 |  | 68.032 | 462,7 |
| . 0148 | . 01480 |  | .0001 I |  | . 01480 |  | 67.573 | 456,5 |
| . 0149 | . 01490 |  | . 00011 |  | . 01490 |  | 67.119 | 450,4 |
| 0.0150 | 0.01500 | 10,0 | 1.00011 | 0,2 | 0.01500 | 10,0 | 66.672 | 444,4 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0150 | 0.01500 | 10,0 | 1.00011 | 0,2 | 0.01500 | 10,0 | 66.672 | 444,4 |
| .0151 | . 01510 |  | . 00011 |  | . OI510 |  | 66.230 | 438,5 |
| . 0152 | . OI 520 |  | . 00012 |  | . OI 520 |  | 65.795 | 432,8 |
| . 0153 | . O1530 |  | . 00012 |  | . OI530 |  | 65.365 | 427,2 |
| .OI54 | . 01540 |  | . 00012 |  | . O1540 |  | 64.940 | 421,6 |
| 0.0155 | 0.01550 | 10,0 | 1.00012 | 0,2 | 0.01550 | 10,0 | 64.521 | 416,2 |
| . 0156 | . 01560 |  | . 00012 |  | . 01560 |  | 64.108 | 410,9 |
| . 0157 | . 01570 |  | . 00012 |  | . 01570 |  | 63.699 | 405,7 |
| . 0158 | . 01580 |  | . 00012 |  | . 01580 |  | 63.296 | 400,5 |
| . OI59 | . 01590 |  | .00013 |  | . 01590 |  | 62.898 | 395,5 |
| 0.0160 | 0.01600 | 10,0 | 1.00013 | 0,2 | 0,01600 | 10,0 | 62.505 | 390,6 |
| . 0161 | . 01610 |  | . 00013 |  | . 01610 |  | 62.117 | 385,8 |
| . 0162 | . 01620 |  | .00013 |  | . 01620 |  | 61.734 | 381,0 |
| . 0163 | . 01630 |  | .00013 |  | . 01630 |  | 61.355 | 376,3 |
| . 0164 | . 01640 |  | . 00013 |  | . 01640 |  | 60.981 | 371,8 |
| 0.0165 | 0.01650 | 10,0 | 1.00014 | 0,2 | 0.01650 | 10,0 | 60.612 | 367,3 |
| . 0166 | . 01660 |  | . 00014 |  | . 01660 |  | 60.247 | 362,9 |
| . 0167 | . 01670 |  | . 00014 |  | . 01670 |  | 59.886 | 358,5 |
| . 0168 | . 01680 |  | .000I4 |  | . 01680 |  | 59.529 | 354,3 |
| . 0169 | . 01690 |  | .00014 |  | . 01690 |  | 59.177 | 350, I |
| 0.0170 | 0.01700 | 10,0 | 1.00014 | 0,2 | 0.01700 | 10,0 | 58.829 | 346,0 |
| . 0171 | .01710 |  | . 00015 |  | .01710 |  | 58.485 | 342,0 |
| . 0172 | . 01720 |  | . 00015 |  | . 01720 |  | 58.145 | 338,0 |
| . 0173. | .01730 |  | .00015 |  | .01730 |  | 57.809 | 334, I |
| . 0174 | . 01740 |  | . 00015 |  | . 01740 |  | 57.477 | 330,3 |
| 0.0175 | 0.01750 | 10,0 | 1.00015 | 0,2 | 0.01750 | 10,0 | 57. 149 | 326,5 |
| . 0176 | . 01760 |  | . 00015 |  | .01760 |  | 56.824 | 322,8 |
| . 0177 | .01770 |  | .00016 |  | . 01770 |  | 56.503 | 319,2 |
| . 0178 | . 01780 |  | .00016 |  | . 01780 |  | 56.186 | 315,6 |
| . 0179 | . 01790 |  | . 00016 |  | . 01790 |  | 55.872 | 312, 1 |
| 0.0180 | 0.01800 | 10,0 | 1.00016 | 0,2 | 0.01800 | 10,0 | 55.562 | 308,6 |
| .0181 | . 01810 |  | .00016 |  | .01810 |  | 55.255 | 305,2 |
| . 0182 | . 01820 |  | .00017 |  | . 01820 |  | 54.951 | 301,9 |
| . 0183 | .01830 |  | .00017 |  | .01830 |  | 54.65 I | 298,6 |
| . 0184 | .01840 |  | .00017 |  | . 01840 |  | 54.354 | 295,3 |
| 0.0185 | 0.01850 | 10,0 | 1.00017 | 0,2 | 0.01850 | 10,0 | 54.060 | 292,2 |
| . 0186 | . 01860 |  | .00017 |  | . 01860 |  | 53.770 | 289,0 |
| . 0187 | . 01870 |  | .00017 |  | . 01870 |  | 53.482 | 285,9 |
| . 0188 | . 01880 |  | .00018 |  | . 01880 |  | 53.198 | 282,9 |
| . 0189 | . 01800 |  | .00018 |  | . 01800 |  | 52.916 | 279,9 |
| 0.0190 | 0.01900 | 10,0 | I. 00018 | 0,2 | 0.01900 | 10,0 | 52.638 | 277,0 |
| . 0191 | . 01910 |  | .00018 |  | . 01910 |  | 52.362 | 274, I |
| . 0192 | . 01920 |  | .00018 |  | . 01920 |  | 52.090 | 271,2 |
| . 0193 | . 01930 |  | .00019 |  | . 01930 |  | 51.820 | 268,4 |
| . 0194 | . 01940 |  | . 00019 |  | . 01940 |  | 5 I .553 | 265,7 |
| 0.0195 | 0.01950 | 10,0 | 1.00019 | 0,2 | 0.01950 | 10,0 | 51.289 | 263,0 |
| . 0196 | . 01960 |  | . 00019 |  | . 01960 |  | 51.027 | 260,3 |
| . 0197 | . 01970 |  | . 00019 |  | . 01970 |  | 50.768 | 257,6 |
| . 0198 | . 01980 |  | . 00020 |  | . 01980 |  | 50.512 | 255,0 |
| . 0199 | . 01990 |  | . 00020 |  | . 01990 |  | 50.258 | 252,5 |
| 0.0200 | 0.02000 | 10,0 | 1.00020 | 0,2 | 0.02000 | 10,0 | 50.007 | 250,0 |
| u | tan od $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0200 | 0.02000 | 10,0 | 1.00020 | 0,2 | 0.02000 | 10,0 | 50.007 | 250,0 |
| . 0201 | .02010 |  | . 00020 |  | . 02010 |  | 49.758 | 247,5 |
| . 0202 | . 02020 |  | . 00020 |  | . 02020 |  | 49.512 | 245,0 |
| . 0203 | . 02030 |  | .0002I |  | . 02030 |  | 49.268 | 242,6 |
| . 0204 | . 02040 |  | . 0002 I |  | . 02040 |  | 49.026 | 240,3 |
| 0.0205 | 0.02050 | 10,0 | I. 00021 | Q,2 | 0.02050 | 10,0 | 48.787 | 237,9 |
| . 0206 | . 02060 |  | . 00021 |  | . 02060 |  | 48.551 | 235,6 |
| . 0207 | . 02070 |  | . 0002 I |  | . 02070 |  | 48.316 | 233,3 |
| . 0208 | . 02080 |  | . 00022 |  | . 02080 |  | 48.084 | 23I, I |
| . 0209 | . 02090 |  | . 00022 |  | . 02090 |  | 47.854 | 228,9 |
| 0.0210 | 0.02100 | 10,0 | 1.00022 | 0,2 | 0.02100 | 10,0 | 47.626 | 226,7 |
| . 02 I I | .02110 |  | . 00022 |  | . 02110 |  | 47.400 | 224,6 |
| . 0212 | . 02120 |  | . 00022 |  | . 02120 |  | 47. 177 | 222,5 |
| . 0213 | . 02130 |  | . 00023 |  | . 02130 |  | 46.955 | 220,4 |
| .0214 | .02140 |  | . 00023 |  | . 02140 |  | 46.736 | 218,3 |
| 0.0215 | 0.02150 | 10,0 | 1.00023 | 0,2 | 0.02150 | 10,0 | 46.519 | 216,3 |
| . 0216 | .02160 |  | . 00023 |  | . 02160 |  | 46.303 | 214,3 |
| . 0217 | .02170 |  | . 00024 |  | .02170 |  | 46.090 | 212,3 |
| .0218 | . 02180 |  | . 00024 |  | . 02180 |  | 45.879 | 210,4 |
| .0219 | .02190 |  | . 00024 |  | . 02190 |  | 45.669 | 208,5 |
| 0.0220 | 0.02200 | 10,0 | 1.00024 | 0,2 | 0.02200 | 10,0 | 45.462 | 206,6 |
| .022I | . 02210 |  | . 00024 |  | . 02210 |  | 45.256 | 204,7 |
| . 0222 | . 02220 |  | . 00025 |  | . 02220 |  | 45.052 | 202,9 |
| . 0223 | . 02230 |  | . 00025 |  | . 02230 |  | 44.850 | 201, I |
| . 0224 | . 02240 |  | . 00025 |  | . 02240 |  | 44.650 | 199,3 |
| 0.0225 | 0.02250 | 10,0 | 1.00025 | 0,2 | 0.02250 | 10,0 | 44.452 | 197,5 |
| . 0226 | . 02260 |  | . 00026 |  | . 02260 |  | 44.255 | 195,7 |
| . 0227 | . 02270 |  | . 00026 |  | . 02270 |  | 44.060 | 194,0 |
| . 0228 | . 02280 |  | . 00026 |  | . 02280 |  | 43.867 | 192,3 |
| . 0229 | . 02290 |  | . 00026 |  | . 02290 |  | 43.676 | 190,7 |
| 0.0230 | 0.02300 | 10,0 | 1.00026 | 0,2 | 0.02300 | 10,0 | 43.486 | 189,0 |
| .023I | .02310 |  | . 00027 |  | . 02310 |  | 43.298 | 187,4 |
| . 0232 | . 02320 |  | . 00027 |  | . 02320 |  | 43.11 1 | 185,8 |
| . 0233 | . 02330 |  | . 00027 |  | . 02330 |  | 42.926 | 184,2 |
| . 0234 | . 02340 |  | . 00027 |  | . 02340 |  | 42.743 | 182,6 |
| 0.0235 | 0.02350 | 10,0 | 1.00028 | 0,2 | 0.02350 | 10,0 | 42.56 I | 181, 1 |
| . 0236 | . 02360 |  | . 00028 |  | . 02360 |  | $42 \cdot 38 \mathrm{I}$ | 179,5 |
| . 0237 | . 02370 |  | . 00028 |  | . 02370 |  | 42.202 | 178,0 |
| . 0238 | .02380 |  | . 00028 |  | . 02380 |  | 42.025 | 176,5 |
| . 0239 | .023y0 |  | . 00029 |  | . 02390 |  | 41.849 | 175,0 |
| 0.0240 | 0.02400 | 10,0 | 1.00029 | 0,2 | 0.02400 | 10,0 | 41.675 | 173,6 |
| .024I | .02410 |  | . 00029 |  | . 02410 |  | 41.502 | 172, 1 |
| . 0242 | . 02420 |  | . 00029 |  | . 02420 |  | 4 I .330 | 170,7 |
| . 0243 | . 02430 |  | . 00030 |  | . 02430 |  | 41.160 | 169,3 |
| . 0244 | . 02440 |  | . 00030 |  | . 02440 |  | 40.992 | 167,9 |
| 0.0245 | 0.02450 | 10,0 | 1.00030 | 0,2 | 0.02450 | 10,0 | 40.824 | 166,6 |
| . 0246 | . 02460 |  | . 00030 |  | . 02460 |  | 40.659 | 165,2 |
| . 0247 | . 02470 |  | . 00031 |  | . 02469 |  | 40.494 | 163,9 |
| . 0248 | . 02480 |  | . 0003 I |  | . 02479 |  | 40.33 I | 162,6 |
| . 0249 | . 02490 |  | . 00031 |  | . 02489 |  | 40.169 | 161,3 |
| 0.0250 | 0.02500 | 10,0 | 1.00031 | 0,3 | 0.02499 | 10,0 | 40.008 | 160,0 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

## Smithsonian Tables

Natural Hyperbolic Functions.

| U | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0250 | 0.02500 | 10,0 | 1.00031 | 0,3 | 0.02499 | 10,0 | 40.008 | 160,0 |
| .025I | . 02510 |  | . 00032 |  | . 02509 |  | 39.849 | 158,7 |
| . 0252 | . 02520 |  | . 00032 |  | .02519 |  | 39.691 | 157,4 |
| . 0253 | . 02530 |  | . 00032 |  | . 02529 |  | 39.534 | 156,2 |
| . 0254 | . 02540 |  | . 00032 |  | . 02539 |  | 39.379 | 155,0 |
| 0.0255 | 0.02550 | 10,0 | 1.00033 | 0,3 | 0.02549 | 10,0 | 39.224 | I 53, 8 |
| . 0256 | . 02560 |  | . 00033 |  | . 02559 |  | 39.071 | 152,6 |
| . 0257 | . 02570 |  | . 00033 |  | . 02569 |  | 38.919 | 151,4 |
| . 0258 | . 02580 |  | . 00033 |  | . 02579 |  | 38.768 | 150,2 |
| . 0259 | . 02590 |  | . 00034 |  | . 02589 |  | 38.619 | 149,0 |
| 0.0260 | 0.02600 | 10,0 | 1.00034 | 0,3 | 0.02599 | 10,0 | 38.470 | 147,9 |
| .026I | .02610 |  | . 00034 |  | . 02609 |  | 38.323 | 146,8 |
| . 0262 | . 02620 |  | . 00034 |  | . 02619 |  | 38.177 | 145,7 |
| . 0263 | . 02630 |  | . 00035 |  | . 02629 |  | 38.032 | I44,5 |
| . 0264 | . 02640 |  | . 00035 |  | . 02639 |  | 37.888 | 143,4 |
| 0.0265 | 0.02650 | 10,0 | 1.00035 | 0,3 | 0.02649 | 10,0 | 37.745 | 142,4 |
| . 0266 | . 02660 |  | . 00035 |  | . 02659 |  | 37.603 | I41,3 |
| . 0257 | . 02670 |  | . 00036 |  | . 02669 |  | 37.462 | 140,2 |
| . 0268 | . 02680 |  | . 00036 |  | . 02679 |  | 37.322 | I39,2 |
| . 0269 | . 02690 |  | -. 00036 |  | . 02689 |  | 37.184 | 138,2 |
| 0.0270 | 0.02700 | 10,0 | 1.00036 | 0,3 | 0.02699 | 10,0 | 37.046 | 137, 1 |
| . 0271 | . .02710 |  | . 00037 |  | . 02709 |  | 36.909 | 136, I |
| . 0272 | . 02720 |  | . 00037 |  | . 02719 |  | 36.774 | I $35, \mathrm{I}$ |
| . 0273 | . 02730 |  | . 00037 |  | . 02729 |  | 36.639 | 134, I |
| . 0274 | . 02740 |  | . 00038 |  | . 02739 |  | 36.505 | 133,2 |
| 0.0275 | 0.02750 | 10,0 | 1.00038 | 0,3 | 0.02749 | 10,0 | 36.373 | 132,2 |
| . 0276 | . 02760 |  | . 00038 |  | . 02759 |  | 36.24 I | 131,2 |
| . 0277 | . 02770 |  | . 00038 |  | . 02769 |  | 36.110 | 130,3 |
| . 0278 | . 02780 |  | . 00039 |  | . 02779 |  | 35.980 | 129,4 |
| . 0279 | . 02790 |  | . 00039 |  | . 02789 |  | 35.852 | 128,4 |
| 0.0280 | 0.02800 | 10,0 | 1.00039 | 0,3 | 0.02799 | 10,0 | 35.724 | 127,5 |
| .028I | .02810 |  | . 00039 |  | . 02809 |  | 35.597 | 126,6 |
| . 0282 | . 02820 |  | . 00040 |  | .02819 |  | 35.470 | 125,7 |
| . 0283 | .02830 |  | . 00040 |  | . 02829 |  | 35.345 | 124,8 |
| . 0284 | . 02840 |  | . 00040 |  | . 02839 |  | 35.22 I | 124,0 |
| 0.0285 | 0.02850 | 10,0 | 1.00041 | 0,3 | 0.02849 | 10,0 | 35.097 | 123,2 |
| . 0286 | . 02860 |  | . 0004 I |  | . 02859 |  | 34.975 | 122,2 |
| . 0287 | . 02870 |  | . 0004 I |  | . 02859 |  | 34.853 | 121,4 |
| . 0288 | . 02880 |  | . 00041 |  | . 02879 |  | 34.732 | 120,5 |
| . 0289 | . 02890 |  | . 00042 |  | . 02889 |  | 34.612 | 1 19,7 |
| 0.0290 | 0.02900 | 10,0 | 1.00042 | 0,3 | 0.02899 | 10,0 | 34.492 | 1 18,9 |
| .0291 | . 02910 |  | . 00042 |  | . 02909 |  | 34.374 | 118, 1 |
| . 0292 | . 02920 |  | . 00043 |  | . 02919 |  | 34.256 | 117,2 |
| . 0293 | . 02930 |  | . 00043 |  | . 02929 |  | 34.139 | 116,4 |
| . 0294 | . 02940 |  | . 00043 |  | . 02939 |  | 34.023 | II 5,7 |
| 0.0295 | 0.02950 | 10,0 | 1.00044 | 0,3 | 0.02949 | 10,0 | 33.908 | II 4,9 |
| . 0296 | . 02960 |  | . 00044 |  | . 02959 |  | 33.794 | II4, I |
| . 0297 | . 02970 |  | . 00014 |  | . 02969 |  | 33.680 | I 13,3 |
| . 0298 | . 02980 |  | . 00044 |  | . 02979 |  | 33.567 | I I 2,6 |
| . 0299 | . 02990 |  | . 00045 |  | . 02989 |  | 33.455 | I I I , 8 |
| 0.0300 | 0.03000 | 10,0 | 1. 00045 | 0,3 | 0.02999 | 10,0 | 33.343 | I I I, I |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | $\cosh u$ | $\omega \mathbf{F}_{0}{ }^{\text {g }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0300 | 0.03000 | 10,0 | 1.00045 | 0,3 | 0.02999 | 10,0 | $33 \cdot 343$ | III, I |
| . 0301 | . 03010 |  | . 00045 |  | . 03009 |  | 33.233 | 1 10,3 |
| . 0302 | . 03020 |  | . 00046 |  | .03019 |  | 33.123 | 109,6 |
| . 0303 | . 03030 |  | . 00046 |  | . 03029 |  | 33.013 | 108,9 |
| . 0304 | . 03040 |  | . 00046 |  | . 03039 |  | 32.905 | 108,2 |
| 0.0305 | 0.03050 | 10,0 | 1.00047 | 0,3 | 0.03049 | 10,0 | 32.797 | 107,5 |
| . 0306 | . 03060 |  | . 00047 |  | . 03059 |  | 32.690 | 106,8 |
| . 0307 | . 03070 |  | . 00047 |  | . 03069 |  | 32.584 | 106, I |
| . 0308 | . 03080 |  | . 00047 |  | . 03079 |  | 32.478 | 105,4 |
| . 0309 | . 03090 |  | . 00048 |  | . 03089 |  | 32.373 | 104,7 |
| 0.0310 | 0.03100 | 10,0 | 1.00048 | 0,3 | 0.03099 | 10,0 | 32.268 | 104,0 |
| .03II | .031II |  | . 00048 |  | .03109 |  | 32.165 | 103,4 |
| . 0312 | .03121 |  | . 00049 |  | .03119 |  | 32.062 | 102,7 |
| .03I3 | .0313I |  | . 00049 |  | .03129 |  | 31.959 | 102,0 |
| . 0314 | .03I4I |  | . 00049 |  | .03I39 |  | 31.858 | 1OI,4 |
| 0.0315 | 0.03151 | 10,0 | 1.00050 | 0,3 | 0.03149 | 10,0 | 31.757 | 100,7 |
| . 0316 | .0316I |  | . 00050 |  | .03159 |  | 31.656 | 100, 1 |
| .0317 | .03171 |  | . 00050 |  | .03169 |  | 3 I .556 | 99,5 |
| -.0318 | .03181 |  | .0005I |  | .03179 |  | 3 I .457 | 98,9 |
| .0319 | .0319I |  | . 00051 |  | .03189 |  | 31.359 | 98,2 |
| 0.0320 | 0.03201 | 10,0 | 1.0005 1 | 0,3 | 0.03199 | 10,0 | 31.261 | 97,6 |
| . 0321 | . 03211 |  | . 00052 |  | . 03209 |  | 31.163 | 97,0 |
| . 0322 | . 03221 |  | . 00052 |  | .03219 |  | 31.067 | 96,4 |
| . 0323 | .0323I |  | . 00052 |  | . 03229 |  | 30.971 | 95,8 |
| . 0324 | .0324I |  | . 00052 |  | . 03239 |  | 30.875 | 95,2 |
| 0.0325 | 0.03251 | 10,0 | 1.00053 | 0,3 | 0.03249 | 10,0 | 30.780 | 94,6 |
| . 0326 | . 03261 |  | . 00053 |  | . 03259 |  | 30.686 | 94, I |
| . 0327 | . 03271 |  | . 00053 |  | . 03269 |  | 30.592 | 93,5 |
| . 0328 | .0328I |  | . 00054 |  | . 03279 |  | 30.499 | 92,9 |
| . 0329 | .03291 |  | . 00054 |  | . 03289 |  | 30.406 | 92,4 |
| 0.0330 | 0.03301 | 10,0 | 1.00054 | 0,3 | 0.03299 | 10,0 | 30.314 | 91,8 |
| .033I | .033I I |  | . 00055 |  | . 03309 |  | 30.223 | 91,2 |
| . 0332 | . 0332 I |  | . 00055 |  | .03319 |  | 30.132 | 90,7 |
| . 0333 | . 0333 I |  | . 00055 |  | . 03329 |  | 30.041 | 90, 1 |
| . 0334 | . 03341 |  | . 00056 |  | . 03339 |  | 29.95 I | 89,6 |
| 0.0335 | 0.0335 I | 10,0 | 1.00056 | 0,3 | 0.03349 | 10,0 | 29.862 | 89, I |
| . 0336 | .0336I |  | . 00056 |  | . 03359 |  | 29.773 | 88,5 |
| . 0337 | . 03371 |  | . 00057 |  | . 03369 |  | 29.685 | 88,0 |
| . 0338 | . 0338 I |  | . 00057 |  | . 03379 |  | 29.597 | 87,5 |
| . 0339 | . 03391 |  | . 00057 |  | . 03389 |  | 29.510 | 87,0 |
| 0.0340 | 0.03401 | 10,0 | 1.00058 | 0,3 | 0.03399 | 10,0 | 29.423 | 86,6 |
| . 0341 | . 0341 I |  | . 00058 |  | . 03409 |  | 29.337 | 86,0 |
| . 0342 | . 0342 I |  | . 00058 |  | .03419 |  | 29.251 | 85,5 |
| . 0343 | . 0343 I |  | . 00059 |  | . 03429 |  | 29.166 | 85,0 |
| . 0344 | .0344I |  | . 00059 |  | . 03439 |  | 29.08I | 84,5 |
| 0.0345 | 0.0345 I | 10,0 | 1.00060 | 0,3 | 0.03449 | 10,0 | 28.997 | 84,0 |
| . 0346 | . 03461 |  | . 00060 |  | . 03459 |  | 28.913 | 83,5 |
| . 0347 | . 03471 |  | . 00060 |  | . 03469 |  | 28.830 | 83,0 |
| . 0348 | . 0348 I |  | . 00061 |  | . 03479 |  | 28.747 | 82,5 |
| . 0349 | . 03491 |  | .0006I |  | . 03489 |  | 28.665 | 82, I |
| 0.0350 | 0.03501 | 10,0 | 1.0006I | 0,4 | 0.03499 | 10,0 | 28.583 | 81,6 |
| $u$ | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\pm \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0350 | 0.03501 | 10,0 | 1.0006I | 0,4 | 0.03499 | 10,0 | 28.583 | 8I,6 |
| .035I | .035II |  | . 00062 |  | . 03509 |  | 28.502 | $8 \mathrm{I}, \mathrm{I}$ |
| . 0352 | . 03521 |  | . 00052 |  | .03519 |  | 28.42 I | 80,7 |
| . 0353 | .0353I |  | . 00062 |  | . 03529 |  | 28.340 | 80,2 |
| . 0354 | . 0354 I |  | . 00063 |  | . 03539 |  | 28.260 | 79,8 |
| 0.0355 | 0.0355 I | 10,0 | 1.00053 | 0,4 | 0.03549 | 10,0 | 28.18I | 79,3 |
| . 0356 | . 03561 |  | . 00063 |  | . 03558 |  | 28.102 | 78,9 |
| . 0357 | . 03571 |  | . 00064 |  | . 03568 |  | 28.023 | 78,4 |
| . 0358 | .0358I |  | .00054 |  | . 03578 |  | 27.945 | 78,0 |
| . 0359 | .0359I |  | .00054 |  | . 03583 |  | 27.857 | 77,6 |
| 0.0360 | 0.03601 | 10,0 | 1.00065 | 0,4 | 0.03598 | 10,0 | 27.790 | 77, 1 |
| .0361 | .036II |  | . 00065 |  | . 03608 |  | 27.713 | 76,7 |
| . 0362 | . 03621 |  | . 00055 |  | . 03618 |  | 27.636 | 76,3 |
| . 0363 | . 0363 I |  | . 00056 |  | . 03628 |  | 27.560 | 75,9 |
| . 0364 | .0364I |  | . 00056 |  | . 03638 |  | 27.485 | 75,4 |
| 0.0365 | 0.03651 | 10,0 | 1.00057 | 0,4 | 0.03648 | 10,0 | 27.409 | 75,0 |
| . 0366 | . 03661 |  | . 00067 |  | . 03658 |  | 27.335 | 74,6 |
| . 0367 | . 03671 |  | . 00057 |  | . 03668 |  | 27.260 | 74,2 |
| . 0368 | .0368I |  | . 00068 |  | . 03678 |  | 27.186 | 73,8 |
| . 0369 | .0369I |  | . 00068 |  | . 03688 |  | 27.113 | 73,4 |
| 0.0370 | 0.03701 | 10,0 | 1.00058 | 0,4 | 0.03698 | 10,0 | 27.039 | 73,0 |
| . 0371 | . 03711 |  | . 00069 |  | . 03708 |  | 26.967 | 72,6 |
| . 0372 | . 0372 I |  | . 00069 |  | . 03718 |  | 26.894 | 72,2 |
| . 0373 | .0373I | - | . 00070 |  | . 03728 |  | 26.822 | 71,8 |
| . 0374 | .0374I |  | . 00070 |  | . 03738 |  | 26.750 | 71,5 |
| 0.0375 | 0.0375 I | 10,0 | I. 00070 | 0,4 | 0.03748 | 10,0 | 26.679 | 71, 1 |
| . 0376 | .0376I | 1 | . 00071 |  | . 03758 |  | 26.608 | 70,7 |
| . 0377 | . 03771 |  | . 0007 I |  | . 03768 |  | 26.538 | 70,3 |
| . 0378 | .0378I |  | . 00071 |  | . 03778 |  | 26.468 | 70,0 |
| . 0379 | .0379I |  | . 00072 |  | . 03788 |  | 26.398 | 69,6 |
| 0.0380 | 0.03801 | 10,0 | 1.00072 | 0,4 | 0.03798 | 10,0 | 26.328 | 69,2 |
| .038I | .038II |  | . 00073 |  | . 03808 |  | 26.259 | 68,9 |
| . 0382 | .0382I |  | . 00073 |  | .03818 |  | 26. 191 | 68,5 |
| . 0383 | .0383I |  | . 00073 |  | . 03828 |  | 26.122 | 68, I |
| . 0384 | . 0384 I |  | . 00074 |  | . 03838 |  | 26.054 | 67,8 |
| 0.0385 | 0.0385 I | 10,0 | I. 00074 | 0,4 | 0.03848 | IO,O | 25.987 | 67,4 |
| . 0385 | . 0385 I |  | . 00075 |  | . 03858 |  | 25.920 | 67, I |
| . 0387 | . 03871 |  | . 00075 |  | . 03868 |  | 25.853 | 66,7 |
| . 0388 | .0388I |  | . 00075 |  | . 03878 |  | 25.786 | 66,4 |
| . 0389 | .0389I |  | . 00076 |  | . 03888 |  | 25.720 | 66, I |
| 0.0390 | 0.03901 | 10,0 | 1.00076 | 0,4 | 0.03898 | 10,0 | 25.654 | 65,7 |
| .0391 | . 0391 I |  | . 00076 |  | . 03908 |  | 25.588 | 65,4 |
| . 0392 | . 0392 I |  | . 00077 |  | . 03918 |  | 25.523 | 64,0 |
| . 0393 | . 03931 |  | . 00077 |  | . 03928 |  | 25.458 | 64,7 |
| . 0394 | . 03941 |  | . 00078 |  | . 03938 |  | 25.394 | 64,4 |
| 0.0395 | 0.0395 I | 10,0 | 1.00078 | 0,4 | 0.03948 | 10,0 |  |  |
| . 0396 | . 03961 |  | . 00078 |  | . 03958 |  | 25.266 | 63,7 |
| . 0397 | . 03971 |  | . 00079 |  | . 03968 |  | 25.202 | 63,4 |
| . 0398 | . 03981 |  | . 00079 |  | . 03978 |  | 25.139 | 63,1 |
| . 0399 | . 03991 |  | . 00080 |  | . 03988 |  | 25.076 | 62,8 |
| 0.0400 | 0.04001 | 10,0 | 1.00080 | 0,4 | 0.03998 | 10,0 | 25.013 | 62,5 |
| u | $\tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0400 | 0.04001 | 10,0 | 1.00080 | 0,4 | 0.03998 | 10,0 | 25.013 | 62,5 |
| . 0401 | . 04011 |  | . 00080 |  | . 04008 |  | 24.951 | 62,2 |
| . 0402 | . 04021 |  | .0008I |  | . 04018 |  | 24.889 | 6I,8 |
| . 0403 | . 0403 I |  | .0008I |  | . 04028 |  | 24.827 | 6I,5 |
| . 0404 | . 04041 |  | . 00082 |  | .04038 |  | 24.766 | 6I,2 |
| 0.0405 | 0.04051 | 10,0 | 1.00082 | 0,4 | 0.04048 | 10,0 | 24.705 | 60,8 |
| . 0406 | . 04061 |  | . 00082 |  | . 04058 |  | 24.644 | 60,6 |
| . 0407 | . 04071 |  | . 00083 |  | . 04058 |  | 24.584 | 60,3 |
| . 0408 | .0408I |  | . 00083 |  | . 04078 |  | 24.523 | 60,0 |
| . 0409 | . 04091 |  | . 00084 |  | . 04088 |  | 24.464 | 59,7 |
| 0.0410 | 0.04101 | 10,0 | 1.00084 | 0,4 | 0.04098 | 10,0 | 24.404 | 59,5 |
| .04II | . 04111 |  | . 00084 |  | .04108 |  | 24.345 | 59,2 |
| .0412 | . 04121 |  | . 00085 |  | .041 18 |  | 24.286 | 58,9 |
| . 0413 | .0413I |  | . 00085 |  | .04128 |  | 24.227 | 58,7 |
| . 0414 | .04141 |  | . 00086 |  | .04138 |  | 24.168 | 58,3 |
| 0.0415 | 0.04151 | 10,0 | 1. 00086 | 0,4 | 0.04148 | 10,0 | 24. IIO | 58,0 |
| . 0416 | . 04161 |  | . 00087 |  | . 04158 |  | 24.052 | 57,8 |
| .0417 | .04171 |  | . 00087 |  | . 04168 |  | 23.995 | 57,5 |
| .0418 | .04181 |  | . 00087 |  | .04178 |  | 23.937 | 57,2 |
| .0419 | .04191 |  | . 00088 |  | .04I88 |  | 23.880 | 56,9 |
| 0.0420 | 0.04201 | 10,0 | 1. 00088 | 0,4 | 0.04198 | 10,0 | 23.824 | 56,7 |
| . 0421 | . 04211 |  | . 00089 |  | . 04208 |  | 23.767 | 56,4 |
| . 0422 | . 0422 I |  | . 00089 |  | . 04217 |  | 23.711 | 56, I |
| . 0423 | .0423I |  | . 00089 |  | . 04227 |  | 23.655 | 55,9 |
| . 0424 | . 0424 I |  | . 00090 |  | . 04237 |  | 23.599 | 55,6 |
| 0.0425 | 0.04251 | 10,0 | 1.00090 | 0,4 | 0.04247 | 10,0 |  | 55,3 |
| . 0426 | . 0426 I |  | . 00091 |  | . 04257 |  | 23.488 | 55, 1 |
| . 0427 | . 0427 I |  | .0009I |  | . 04267 |  | 23.433 | 54,8 |
| . 0428 | .0428I |  | . 00092 |  | . 04277 |  | 23.379 | 54,6 |
| . 0429 | . 04291 |  | . 00092 |  | . 04287 |  | 23.324 | 54,3 |
| 0.0430 | 0.04301 | 10,0 | 1.00092 | 0,4 | 0.04297 | 10,0 | 23.270 | 54,0 |
| . 0431 | . 0431 I |  | . 00093 |  | . 04307 |  | 23.216 | 53,8 |
| . 0432 | . 0432 I |  | . 00093 |  | .04317 |  | 23.163 | 53,6 |
| . 0433 | . 0433 I | , | . 00094 |  | . 04327 |  | 23.109 | 53,3 |
| . 0434 | . 04341 |  | . 00094 |  | . 04337 |  | 23.056 | 53, I |
| 0.0435 | 0.0435 I | 10,0 | 1.00095 | 0,4 | 0.04347 | 10,0 | 23.003 | 52,8 |
| . 0436 | . 04361 |  | . 00095 |  | . 04357 |  | 22.950 | 52,6 |
| . 0437 | . 04371 |  | . 00095 |  | . 04367 |  | 22.898 | 52,3 |
| . 0438 | .0438I |  | . 00096 |  | . 04377 |  | 22.846 | 52, 1 |
| . 0439 | . 04391 |  | . 00096 |  | . 04387 |  | 22.794 | 51,9 |
| 0.0440 | 0.04401 | 10,0 | 1.00097 | 0,4 | 0.04397 | 10,0 | 22.742 | 51,6 |
| . 0441 | . 0441 I |  | . 00097 |  | . 04407 |  | 22.690 | 5I,4 |
| . 0442 | . 04421 |  | . 00098 |  | . 04417 |  | 22.639 | 51,2 |
| . 0443 | . 0443 I |  | . 00098 |  | . 04427 |  | 22.588 | 50,9 |
| . 0444 | . 04441 |  | . 00099 |  | . 04437 |  | 22.537 | 50,7 |
| 0.0445 | 0.04451 | 10,0 | I. 00099 | 0,4 | 0.04447 | 10,0 | 22.487 | 50,5 |
| . 0446 | .0446I |  | . 00099 |  | . 04457 |  | 22.436 | 50,2 |
| . 0447 | . 04471 |  | . 00100 |  | . 04467 |  | 22.386 | 50,0 |
| . 0448 | . 0448 I |  | . 00100 |  | . 04477 |  | 22.336 | 49,8 |
| . 0449 | . 04492 |  | .00101 |  | . 04487 |  | 22.287 | 49,6 |
| 0.0450 | 0.04502 | 10,0 | 1.00101 | 0,5 | 0.04497 | 10,0 | 22.237 | 49,3 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\sec$ gd $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\tanh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0450 | 0.04502 | 10,0 | 1.00101 | 0,5 | 0.04497 | 10,0 | 22.237 | 49,3 |
| .045I | . 04512 |  | . 00102 |  | . 04507 |  | 22.188 | 49, I |
| . 0452 | . 04522 |  | . 00102 |  | . 04517 |  | 22.139 | 48,9 |
| . 0453 | . 04532 |  | . 00103 |  | . 04527 |  | 22.090 | 48,7 |
| . 0454 | . 04542 |  | . 00103 |  | . 04537 |  | 22.042 | 48,5 |
| 0.0455 | 0.04552 | 10,0 | 1.00104 | 0,5 | 0.04547 | 10,0 | 21. 993 | 48,3 |
| . 0456 | . 04562 |  | . 00104 |  | . 04557 |  | 21.945 | 48, I |
| . 0457 | . 04572 |  | . 00104 |  | . 04567 |  | 21.897 | 47,8 |
| . 0458 | . 04582 |  | . 00105 |  | . 04577 |  | 21.849 | 47,6 |
| . 0459 | . 04592 |  | . 00105 |  | . 04587 |  | 21.802 | 47,4 |
| 0.0460 | 0.04602 | 10,0 | 1.00106 | 0,5 | 0.04597 | 10,0 | 21.754 | 47,2 |
| .046I | . 04612 |  | . 00106 |  | . 04607 |  | 21.707 | 47,0 |
| . 0462 | . 04622 |  | . 00107 |  | .046I7 |  | 21.660 | 46,8 |
| . 0463 | . 04632 |  | . 00107 |  | . 04627 |  | 21.6I4 | 46,6 |
| . 0464 | . 04642 |  | . 00108 | 。 | . 04637 |  | 21.567 | 46,4 |
| 0.0465 | 0.04652 | . 10,0 | 1.00108 | 0,5 | 0.04647 | 10,0 | 21.521 | 46,2 |
| . 0466 | . 04662 |  | .00109 |  | . 04657 |  | 21. 475 | 46,0 |
| . 0467 | . 04672 |  | .00109 |  | . 04667 |  | 21.429 | 45,8 |
| . 0468 | . 04682 |  | . 00110 |  | . 04677 |  | 21.383 | 45,6 |
| . 0469 | . 04692 |  | .00110 |  | . 04687 |  | 2I. 338 | 45,4 |
| 0.0470 | 0.04702 | 10,0 | 1.00110 | 0,5 | 0.04697 | 10,0 | 21.292 | 45,2 |
| . 0471 | . 04712 |  | .001 II |  | . 04707 |  | 21.247 | 45,0 |
| . 0472 | . 04722 |  | .001 II |  | . 04716 |  | 21. 202 | 44,9 |
| . 0473 | . 04732 |  | .001 12 |  | . 04726 |  | 21.157 | 44,7 |
| . 0474 | . 04742 |  | .001 12 |  | . 04736 |  | 21.113 | 44,5 |
| 0.0475 | 0.04752 | 10,0 | I. 00113 | 0,5 | 0.04746 | 10,0 | 21. 068 | 44,3 |
| . 0476 | . 04762 |  | .00113 |  | . 04756 |  | 21.024 | 44, I |
| . 0477 | . 04772 |  | .00114 |  | . 0.4766 |  | 20.980 | 43,9 |
| . 0478 | . 04782 |  | .00114 |  | . 04776 |  | 20.936 | 43,7 |
| . 0479 | . 04792 |  | .00115 |  | . 04786 |  | 20.893 | 43,6 |
| 0.0480 | 0.04802 | 10,0 | 1.00115 | 0,5 | 0.04796 | 10,0 | 20.849 | 43,4 |
| .0481 | .04812 |  | .00116 |  | . 04806 |  | 20.806 | 43,2 |
| . 0482 | . 04822 |  | .00116 |  | .048I6 |  | 20.763 | 43,0 |
| . 0483 | . 04832 |  | .001 17 |  | . 04826 |  | 20.720 | 42,8 |
| . 0484 | . 04842 |  | .00117 |  | . 04836 |  | 20.677 | 42,7 |
| 0.0485 | 0.04852 | 10,0 | 1.00118 | 0,5 | 0.04846 | 10,0 | 20.635 | 42,5 |
| . 0486 | . 04862 |  | .00118 |  | . 04856 |  | 20.592 | 42,3 |
| .0487 | . 04872 |  | .00119 |  | . 04866 |  | 20.550 | 42, I |
| . 0488 | . 04882 | . | . 00119 |  | . 04876 |  | 20.508 | 42,0 |
| . 0489 | . 04892 |  | . 00120 |  | . 04886 |  | 20.466 | 4I,8 |
| 0.0490 | 0.04902 | 10,0 | 1.00120 | 0,5 | 0.04896 | 10,0 | 20.424 | 41,6 |
| .049I | . 04912 |  | . 00121 |  | . 04906 |  | 20.383 | 4I,4 |
| . 0492 | . 04922 |  | .0012I |  | . 04916 |  | 20.342 | 4I,3 |
| . 0493 | . 04932 |  | . 00122 |  | . 04926 |  | 20.300 | 41, I |
| . 0494 | . 04942 |  | . 00122 |  | . 04936 |  | 20.259 | 40,9 |
| 0.0495 | 0.04952 | 10,0 | 1.00123 | 0,5 | 0.04946 | 10,0 | 20.219 | 40,8 |
| . 0496 | . 04952 |  | . 00123 |  | . 04956 |  | 20.178 | 40,6 |
| . 0497 | . 04972 |  | . 00124 |  | . 04966 |  | 20.137 | 40,5 |
| . 0498 | . 04982 |  | . 00124 |  | . 04976 |  | 20.097 | 40,3 |
| . 0499 | . 04992 |  | . 00125 |  | . 04985 |  | 20.057 | 40, I |
| 0.0500 | 0.05002 | 10,0 | 1.00125 | 0,5 | 0.04996 | 10,0 | 20.017 | 40,0 |
| U | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh 4$ | $\omega \mathrm{F}_{0}{ }^{\text {g }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0500 | 0.05002 | 10,0 | 1.00125 | 0,5 | 0.04996 | 10,0 | 20.017 | 40,0 |
| .0501 | . 05012 |  | .00126 |  | . 05006 |  | 19.977 | 39,8 |
| . 0502 | . 05022 |  | .00126 |  | .05016 |  | 19.937 | 39,6 |
| . 0503 | . 05032 |  | .00127 |  | . 05026 |  | 19.897 | 39,5 |
| . 0504 | . 05042 |  | . 00127 |  | . 05036 |  | 19.858 | 39,3 |
| 0.0505 | 0.05052 | 10,0 | I. 00128 | 0,5 | 0.05046 | 10,0 | 19.819 | 39,2 |
| . 0506 | . 05062 |  | .00128 |  | .05056 |  | 19.780 | 39,0 |
| . 0507 | . 05072 |  | .00129 |  | . 05066 |  | 19.741 | 38,9 |
| . 0508 | . 05082 |  | .00129 |  | . 05076 |  | 19.702 | 38,7 |
| . 0509 | . 05092 |  | .00130 |  | . 05086 |  | 19.663 | 38,6 |
| 0.0510 | 0.05102 | 10,0 | 1.00130 | 0,5 | 0.05096 | 10,0 | 19.625 | 38,4 |
| .05II | .05112 |  | .00131 |  | .05106 |  | 19.587 | 38,3 |
| . 0512 | .05122 |  | . OOI3I |  | .05116 |  | 19.548 | 38, 1 |
| .0513 | .05132 |  | .00132 |  | .05126 |  | 19.510 | 38,0 |
| .0514 | .05142 |  | .00132 |  | .05135 |  | 19.472 | 37,8 |
| 0.0515 | 0.05152 | 10,0 | 1.00133 | 0,5 | 0.05145 | 10,0 | . 19.435 | 37,7 |
| .0516 | .05162 |  | .00133 |  | .05155 |  | 19.397 | 37,5 |
| .0517 | .05172 |  | .00134 |  | .05165 |  | 19.360 | 37,4 |
| .0518 | .05182 |  | .00134 |  | .05175 |  | 19.322 | 37,2 |
| .0519 | .05192 |  | .00135 |  | .05185 |  | 19.285 | 37, I |
| 0.0520 | 0.05202 | 10,0 | 1.00135 | 0,5 | 0.05195 | 10,0 | 19.248 | 36,9 |
| .0521 | .05212 |  | .00136 |  | . 05205 |  | 19.211 | 36,8 |
| . 0522 | . 05222 |  | .00136 |  | .05215 |  | 19.174 | 36,7 |
| . 0523 | . 05232 |  | .00137 |  | . 05225 |  | 19.138 | 36,5 |
| . 0524 | . 05242 |  | .00137 |  | . 05235 |  | 19.101 | 36,4 |
| 0.0525 | 0.05252 | 10,0 | 1.00138 | 0,5 | 0.05245 | 10,0 | 19.065 | 36,2 |
| . 0526 | . 05262 |  | .00138 |  | . 05255 |  | 19.029 | 36, I |
| . 0527 | . 05272 |  | .00139 |  | . 05265 |  | 18.993 | 36,0 |
| . 0528 | . 05282 |  | .00139 |  | . 05275 |  | 18.957 | 35,8 |
| . 0529 | . 05292 |  | .00140 |  | . 05285 |  | 18.92 I | 35,7 |
| 0.0530 | 0.05302 | 10,0 | 1.00140 | 0,5 | 0.05295 | 10,0 | 18.886 | 35,6 |
| . 0531 | . 05312 |  | .00141 |  | . 05305 |  | 18.850 | 35,4 |
| . 0532 | . 05323 |  | .00142 |  | .05315 |  | 18.815 | 35,3 |
| . 0533 | . 05333 |  | .00142 |  | . 05325 | , | 18.779 | 35,2 |
| . 0534 | . 05343 |  | .00143 |  | . 05335 |  | 18.744 | 35.0 |
| 0.0535 | 0.05353 | 10,0 | 1.00143 | 0,5 | 0.05345 | 10,0 | 18.709 | 34,9 |
| . 0536 | . 05363 |  | . 00144 |  | . 05355 |  | 18.675 | 34,8 |
| . 0537 | . 05373 |  | .00144 |  | . 05365 |  | 18.640 | 34,6 |
| . 0538 | . 05383 |  | .00145 |  | . 05375 |  | 18.605 | 34,5 |
| . 0539 | . 05393 |  | .00145 |  | . 05385 |  | 18.57 I | 34,4 |
| 0.0540 | 0.05403 | 10,0 | 1.00146 | 0,5 | 0.05395 | 10,0 | 18.537 | 34,3 |
| .054I | .05413 |  | . 00146 |  | . 05405 |  | 18.502 | 34, I |
| . 0542 | . 05423 |  | .00147 |  | . 05415 |  | 18.468 | 34,0 |
| . 0543 | . 05433 |  | .00147 |  | . 05425 |  | 18.434 | 33,9 |
| . 0544 | . 05443 |  | . 00148 |  | . 05435 |  | 18.400 | 33,8 |
| 0.0545 | 0.05453 | 10,0 | 1.00149 | 0,5 | 0.05445 | 10,0 | 18.367 | 33,6 |
| . 0546 | . 05463 |  | .00149 |  | . 05455 |  | 18.333 | 33,5 |
| . 0547 | . 05473 |  | . 00150 |  | . 05465 |  | 18.300 | 33,4 |
| . 0548 | . 05483 |  | .00150 |  | . 05475 |  | 18.266 | 33,3 |
| . 0549 | . 05493 |  | .00151 |  | . 05484 |  | 18.233 | 33, I |
| 0.0550 | 0.05503 | 10,0 | 1.0015I | 0,6 | 0.05494 | 10,0 | 18.200 | 33,0 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0550 | 0.05503 | 10,0 | 1.00151 | 0,6 | 0.05494 | 10,0 | 18.200 | 33,0 |
| .055I | .05513 |  | . 00152 |  | . 05504 |  | 18.167 | 32,9 |
| . 0552 | . 05523 |  | . 00152 |  | .05514 |  | 18.134 | 32,8 |
| . 0553 | . 05533 |  | .00153 |  | . 05524 |  | 18.102 | 32,7 |
| . 0554 | . 05543 |  | . 00153 |  | . 05534 |  | 18.069 | 32,5 |
| 0.0555 | 0.05553 | 10,0 | 1.00154 | 0,6 | 0.05544 | 10,0 | 18.037 | 32,4 |
| . 0556 | . 05563 |  | .00155 |  | . 05554 |  | 18.004 | 32,3 |
| . 0557 | . 05573 |  | . 00155 |  | . 05564 |  | 17.972 | 32,2 |
| . 0558 | . 05583 |  | . 00156 |  | . 05574 |  | 17.940 | 32, I |
| . 0559 | . 05593 |  | . 00156 |  | . 05584 |  | 17.908 | 32,0 |
| 0.0560 | 0.05603 | 10,0 | 1.00157 | 0,6 | 2.05594 | 10,0 | 17.876 | 31,9 |
| .0561 | .05613 |  | . 00157 |  | . 05604 |  | 17.844 | 31,7 |
| . 0562 | . 05623 |  | . 00158 |  | .05614 |  | 17.812 | 31,6 |
| .0563 | . 05633 |  | .00159 |  | . 05624 |  | 17.781 | 3I,5 |
| . 0564 | . 05643 |  | . 00159 |  | . 05634 |  | 17.749 | 31,4 |
| 0.0565 | 0.05653 | 10,0 | 1.00160 | 0,6 | 0.05644 | 10,0 | 17.718 | 31,3 |
| . 0565 | . 05663 |  | . 00160 |  | . 05654 |  | 17.687 | $3 \mathrm{I}, 2$ |
| . 0567 | . 05673 |  | .0016I |  | . 05664 |  | 17.656 | $3 \mathrm{I}, \mathrm{I}$ |
| . 0568 | . 05683 |  | .0016I |  | . 05674 |  | 17.625 | $3 \mathrm{I}, 0$ |
| .0569 | . 05693 |  | . 00162 |  | . 05684 |  | 17. 594 | 30,9 |
| 0.0570 | 0.05703 | 10,0 | 1.00162 | 0,6 | 0.05694 | 10,0 | 17.563 | 30,7 |
| .0571 | . 05713 |  | . 00163 |  | . 05704 |  | 17.532 | 30,6 |
| . 0572 | . 05723 |  | . 00164 |  | . 05714 |  | 17.502 | 30,5 |
| . 0573 | . 05733 |  | . 00164 |  | . 05724 |  | 17.47 I | 30,4 |
| . 0574 | . 05743 |  | . 00165 |  | . 05734 |  | I7.44 | 30,3 |
| 0.0575 | 0.05753 | 10,0 | 1.00165 | 0,6 | 0.05744 | 10,0 | 17.410 | 30,2 |
| . 0575 | . 05763 |  | .00166 |  | . 05754 |  | 17.380 | 30,1 |
| . 0577 | . 05773 |  | . 00167 |  | . 05764 |  | 17.350 | 30,0 |
| . 0578 | .05783 |  | . 00167 |  | .05774 |  | $17 \cdot 320$ | 29,9 |
| . 0579 | . 05793 |  | . 00168 |  | . 05784 |  | 17.290 | 29,8 |
| 0.0580 | 0.05803 | 10,0 | 1.00168 | 0,6 | 0.05794 | 10,0 | 17.26I | 29,7 |
| .0581 | .05813 |  | . 00169 |  | .05803 |  | 17.23 I | 29,6 |
| . 0582 | . 05823 |  | .00169 |  | .05813 |  | 17.202 | 29,5 |
| . 0583 | . 05833 |  | .00170 |  | . 05823 |  | 17.172 | 29,4 |
| . 0584 | . 05843 |  | .00171 |  | . 05833 | - | 17.143 | 29,3 |
| 0.0585 | 0.05853 | 10,0 | 1.00171 | 0,6 | 0.05843 | 10,0 | 17.114 | 29,2 |
| . 0586 | . 05863 |  | .00172 |  | . 05853 |  | 17.084 | 29, I |
| . 0587 | .05873 |  | .00172 |  | . 05863 |  | 17.055 | 29,0 |
| . 0588 | .05883 |  | .00173 |  | .05873 |  | 17.026 | 28,9 |
| . 0589 | . 05893 |  | .00174 |  | . 05883 |  | 16.998 | 28,8 |
| 0.0590 | 0.05903 | 10,0 | 1.00174 | 0,6 | 0.05893 | IO,O | 16.969 | 28,7 |
| .0591 | . 05913 |  | .00175 |  | . 05903 |  | 16.940 | 28,6 |
| . 0592 | .05923 |  | .00175 |  | . 05913 |  | 16.912 | 28,5 |
| . 0593 | . 05933 |  | .00176 |  | . 05923 |  | 16.883 | 28,4 |
| . 0594 | . 05943 |  | .00176 |  | . 05933 |  | 16.855 | 28,3 |
| 0.0595 | 0.05954 | 10,0 | 1.00177 | 0,6 | 0.05943 | 10,0 | 16.827 | 28,2 |
| . 0596 | . 05964 |  | .00178 |  | . 05953 |  | 16.798 | 28, I |
| . 0597 | . 05974 |  | .00178 |  | . 05963 |  | 16.770 | 28,0 |
| . 0598 | . 05984 |  | .00179 |  | . 05973 |  | 16.742 | 27,9 |
| . 0599 | . 05994 |  | .00179 |  | . 05983 |  | 16.714 | 27,8 |
| 0.0600 | 0.05004 | 10,0 | 1.00180 | 0,6 | 0.05993 | 10,0 | 16.687 | 27,7 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables.

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0600 | 0.06004 | 10,0 | 1.00180 | 0,6 | 0.05993 | 10,0 | 16.687 | 27,7 |
| .0601 | .06014 |  | .00181 |  | . 06003 |  | 16.659 | 27,7 |
| . 0602 | . 06024 |  | .00181 |  | . 06013 |  | 16.631 | 27,6 |
| . 0603 | . 06034 |  | .00182 |  | . 06023 |  | 16.604 | 27,5 |
| . 0604 | . 06044 |  | .00182 |  | . 06033 |  | 16.576 | 27,4 |
| 0.0605 | 0.06054 | 10,0 | 1.00183 | 0,6 | 0.06043 | 10,0 | 16. 549 | 27,3 |
| . 0606 | . 06064 |  | .00184 |  | . 06053 |  | 16.522 | 27,2 |
| . 0607 | . 06074 |  | .00184 |  | . 06063 |  | 16.495 | 27, I |
| . 0608 | . 06084 |  | .00185 |  | . 06073 |  | 16.468 | 27.0 |
| . 0609 | . 06094 |  | .00185 |  | . 06082 |  | 16.44 I | 26,9 |
| 0.0610 | 0.06104 | 10,0 | 1.00186 | 0,6 | 0.06092 | 10,0 | 16.414 | 26,8 |
| .06II | .06II4 |  | . 00187 |  | .06102 |  | 16.387 | 26,8 |
| .06I2 | .06124 |  | .00187 |  | .06II2 |  | 16.360 | 26,7 |
| .06I3 | .06I34 |  | . 00188 |  | .06122 |  | 16.334 | 26,6 |
| .06I4 | .06I44 |  | .00189 |  | .06I32 |  | 16.307 | 26,5 |
| 0.0615 | 0.06154 | 10,0 | 1.00189 | 0,6 | 0.06142 | 10,0 | 16.28I | 26,4 |
| .0616 | . 06164 |  | . 00190 |  | .06I52 |  | 16.254 | 26,3 |
| .06I7 | .06I74 |  | .00190 |  | .06162 |  | 16.228 | 26,2 |
| .06I8 | .06184 |  | .00191 |  | .06172 |  | 16.202 | 26, I |
| .06I9 | .06194 |  | .00192 |  | .06182 |  | 16.176 | 26, I |
| 0.0620 | 0.06204 | 10,0 | 1.00192 | 0,6 | 0.06192 | 10,0 | 16.150 | 26,0 |
| . 0621 | . 06214 |  | . 00193 |  | . 06202 |  | 16. 124 | 25,9 |
| . 0622 | . 06224 |  | .00194 |  | . 06212 |  | 16.098 | 25,8 |
| . 0623 | . 06234 |  | .00194 |  | . 06222 |  | 16.072 | 25,7 |
| . 0624 | . 06244 |  | .00195 |  | . 06232 |  | 16.046 | 25,6 |
| 0.0625 | 0.06254 | 10,0 | 1.00195 | 0,6 | 0.06242 | 10,0 | 16.021 | 25,6 |
| . 0626 | . 06264 |  | . 00196 |  | . 06252 |  | 15.995 | 25,5 |
| . 0627 | . 06274 |  | .00197 |  | . 06262 |  | 15.970 | 25,4 |
| . 0628 | . 06284 |  | . 00197 |  | . 06272 |  | 15.944 | 25,3 |
| . 0629 | . 06294 |  | .00198 |  | . 06282 |  | 15.919 | 25,2 |
| 0.0630 | 0.06304 | 10,0 | 1.00199 | 0,6 | 0.06292 | 10,0 | 15.894 | 25,2 |
| . 0631 | . 06314 |  | . 00199 |  | . 06302 |  | 15.869 | 25, I |
| . 0632 | . 06324 |  | . 00200 |  | . 06312 |  | 15.844 | 25,0 |
| . 0633 | . 06334 |  | . 00200 |  | . 06322 |  | 15.819 | 24,9 |
| . 0634 | . 06344 |  | . .00201 |  | . 06332 |  | 15.794 | 24,8 |
| 0.0635 | 0.06354 | 10,0 | 1.00202 | 0,6 | 0.06342 | 10,0 | 15.769 | 24,8 |
| . 0636 | . 06364 |  | . 00202 |  | .0635I |  | 15.744 | 24,7 |
| . 0637 | . 06374 |  | . 00203 |  | . 06361 |  | 15.720 | 24,6 |
| . 0638 | . 06384 |  | . 00204 |  | . 06371 |  | 15.695 | 24,5 |
| . 0639 | . 06394 |  | . 00204 |  | .0638I |  | 15.67 I | 24,5 |
| 0.0640 | 0.06404 | 10,0 | 1.00205 | 0,6 | 0.06391 | 10,0 | 15.646 | 24,4 |
| .0641 | .06414 |  | . 00206 |  | .0640I |  | 15.622 | 24,3 |
| . 0642 | . 06424 |  | . 00206 |  | . 0641 I |  | 15.598 | 24,2 |
| . 0643 | . 06434 |  | . 00207 |  | . 0642 I |  | 15.574 | 24,2 |
| . 0644 | . 06444 |  | . 00207 |  | . 06431 |  | 15.549 | 24, I |
| 0.0645 | 0.06454 | 10,0 | 1.00208 | 0,6 | 0.06441 | 10,0 | 15.525 | 24,0 |
| . 0646 | . 06464 |  | . 00209 |  | .06451 |  | 15.501 | 23,9 |
| . 0647 | . 06475 |  | . 00209 |  | . 066461 |  | 15.478 | 23,9 |
| . 0648 | . 06485 |  | . 00210 |  | . 06471 |  | 15.454 | 23,8 |
| . 0649 | . 06495 |  | . 00211 |  | .06481 |  | 15.430 | 23,7 |
| 0.0650 | 0.06505 | 10,0 | I.002II | 0,7 | 0.06491 | 10,0 | 15.406 | 23,6 |
| 4 | $\boldsymbol{t a n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions

| 4 | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h}{ }^{\circ}$ | ${ }^{3} \boldsymbol{\omega}, \mathbf{F}_{0}{ }^{\prime}{ }^{\circ}$ | 'coitr' ${ }^{\prime}$ | $\omega^{\omega} F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0650 | 0.06505 | 10,0 | 1.00211 | 0,7 | 0.06491 | 10,0 | 15.406 | 23,6 |
| . 0651 | . 05515 |  | .002I2 |  | .06501 |  | 15.383 | 23,6 |
| . 0652 | . 06525 |  | . 00213 |  | . 0651 I |  | 15.359 | 23,5 |
| . 0653 | . 06535 |  | .00213 |  | . 06521 |  | 15.336 | 23,4 |
| . 0654 | . 06545 |  | .00214 |  | .0653I |  | 15.312 | 23,3 |
| 0.0655 | 0.06555 | 10,0 | 1.00215 | 0,7 | 0.06541 | 10,0 | 15.289 | 23,3 |
| . 0656 | . 06565 |  | . 00215 |  | .05551 |  | 15.266 | 23,2 |
| . 0657 | . 06575 |  | . 00216 |  | .06561 |  | 15.243 | 23, I |
| . 0658 | . 06585 |  | .00217 |  | . 06571 |  | 15.219 | 23, I |
| . 0659 | . 06595 |  | .00217 |  | . 06580 |  | 15.196 | 23,0 |
| 0.0660 | 0.06605 | 10,0 | 1.00218 | 0,7 | 0.06590 | 10,0 | 15.174 | 22,9 |
| .066I | . 06615 |  | .00219 |  | . 06600 |  | 15.151 | 22,9 |
| . 0662 | . 06625 |  | . 00219 |  | . 06610 |  | 15.128 | 22,8 |
| . 0663 | . 06635 |  | . 00220 |  | . 06620 |  | 15.105 | 22,7 |
| . 0664 | . 06645 |  | .0022I |  | . 06630 |  | 15.082 | 22,6 |
| 0.0665 | 0.06655 | 10,0 | I. 0022 I | 0,7 | 0.06640 | 10,0 | 15.060 | 22,6 |
| . 0666 | . 06665 |  | . 00222 |  | . 06650 |  | 15.037 | 22,5 |
| . 0667 | . 06675 |  | . 00223 |  | . 06660 |  | 15.015 | 22,4 |
| . 0668 | . 06685 |  | . 00223 |  | . 06670 |  | 14.992 | 22,4 |
| . 0669 | . 06695 |  | . 00224 |  | . 06680 |  | 14.970 | 22,3 |
| 0.0670 | 0.06705 | 10,0 | 1.00225 | 0,7 | 0.06690 | 10,0 | 14.948 | 22,2 |
| . 0671 | . 06715 |  | . 00225 |  | . 06700 |  | 14.925 | 22,2 |
| . 0672 | . 06725 |  | . 00226 |  | . 06710 |  | 14.903 | 22, I |
| . 0673 | . 06735 |  | . 00227 |  | . 06720 |  | 14.88 I | 22,0 |
| . 0674 | . 06745 |  | . 00227 |  | . 06730 |  | 14.859 | 22,0 |
| 0.0675 | 0.06755 | 10,0 | 1.00228 | 0,7 | 0.06740 | 10,0 | 14.837 | 21,9 |
| . 0676 | . 06765 |  | . 00229 |  | . 06750 |  | 14.815 | 21,8 |
| . 0677 | . 06775 |  | . 00229 |  | . 06760 |  | 14.794 | 2I,8 |
| . 0678 | . 06785 |  | . 00230 |  | . 06770 |  | 14.772 | 21,7 |
| . 0679 | . 06795 |  | .0023I |  | . 06780 |  | 14.750 | 21,7 |
| 0.0680 | 0.06805 | 10,0 | 1.00231 | 0,7 | 0.05790 | 10,0 | 14.729 | 21,6 |
| .068I | .068r5 |  | . 00232 |  | . 06799 |  | 14.707 | 21,5 |
| . 0682 | . 06825 |  | . 00233 |  | . 06809 |  | 14.685 | 2I,5 |
| . 0683 | . 06835 |  | . 00233 |  | .06819. |  | 14.664 | 2I,4 |
| . 0684 | . 06845 |  | . 00234 |  | . 06829 |  | 14.643 | 2I,3 |
| 0.0685 | 0.06855 | 10,0 | 1.00235 | 0,7 | 0.05839 | 10,0 | 14.621 | 21,3 |
| . 0686 | . 06865 |  | . 00235 |  | . 06849 |  | 14.600 | 21,2 |
| . 0687 | . 06875 |  | . 00236 |  | . 06859 |  | 14.579 | 21,2 |
| . 0688 | . 06885 |  | . 00237 |  | . 06869 |  | 14.558 | 2I, I |
| . 0689 | . 06895 |  | . 00237 |  | . 06879 |  | 14.537 | 21,0 |
| 0.0690 | 0.06905 | 10,0 | 1.00238 | 0,7 | 0.06889 | 10,0 | 14.516 | 21,0 |
| . 0691 | . 06916 |  | . 00239 |  | . 06899 | . | 14.495 | 20,9 |
| . 0692 | . 06926 |  | . 00240 |  | .06909 |  | 14.474 | 20,8 |
| . 0693 | . 06936 |  | . 00240 |  | . 06919 |  | 14.453 | 20,8 |
| . 0694 | . 06946 |  | . 00241 |  | . 06929 |  | 14.432 | 20,7 |
| 0.0695 | 0.06956 | 10,0 | 1.00242 | 0,7 | 0.06939 | 10,0 | 14.412 | 20,7 |
| . 0696 | . 06966 |  | . 00242 |  | . 06949 |  | 14.391 | 20,6 |
| . 0697 | . 06976 |  | . 00243 |  | . 06959 |  | 14.370 | 20,6 |
| . 0698 | . 06986 |  | . 00244 |  | . 06969 |  | 14.350 | 20,5 |
| . 0699 | . 06996 |  | . 00244 |  | . 06979 |  | 14.329 | 20,4 |
| 0.0700 | 0.07006 | 10,0 | I. 00245 | 0,7 | 0.06989 | 10,0 | 14.309 | 20,4 |
| $u$ | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| U.: | "Sinh ${ }^{\text {a }}$ : | -6. $\mathrm{F}_{0}$ | cosb. 4 | $\omega \mathrm{F}_{0}{ }^{\prime}$ | tanh u | $\omega^{\boldsymbol{N}} \mathrm{F}^{\prime}$ | coth u | $\omega^{*} \mathrm{~F}^{\prime}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0700 | 0.07006 | 10,0 | 1. 00245 | 0,7 | 0.06989 | 10,0 | 14.309 | 20,4 |
| . 0701 | .07016 |  | . 00246 |  | . 06999 |  | 14.289 | 20,3 |
| . 0702 | . 07026 |  | . 00247 |  | . 07008 |  | 14.268 | 20,3 |
| . 0703 | . 07036 |  | . 00247 | - | . 07018 |  | 14.248 | 20,2 |
| . 0704 | . 07046 |  | . 00248 |  | . 07028 |  | 14.228 | 20,1 |
| 0.0705 | 0.07056 | 10,0 | 1.00249 | 0,7 | 0.07038 | 10,0 | 14.208 | 20,1 |
| . 0706 | . 07056 |  | . 00249 |  | . 07048 |  | 14.188 | 20,0 |
| . 0707 | . 07076 |  | . 00250 |  | . 07058 |  | 14.168 | 20,0 |
| . 0708 | . 07086 |  | .0025I |  | . 07058 |  | 14. 148 | 19,9 |
| . 0709 | . 07096 |  | .0025I |  | . 07078 | 9,9 | 14.128 | 19,9 |
| 0.0710 | 0.07106 | 10,0 | 1.00252 | 0,7 | 0.07088 | 9,9 | 14. 108 | 19,8 |
| .071I | . 07116 |  | . 00253 |  | . 07098 |  | 14.088 | 19,7 |
| . 0712 | . 07126 |  | . 00254 |  | . 07108 |  | 14.069 | 19,7 |
| . 0713 | .07136 |  | . 00254 |  | . 07118 |  | 14.049 | 19,6 |
| . 0714 | . 07146 |  | . 00255 |  | . 07128 |  | 14.029 | 19,6 |
| 0.0715 | 0.07156 | 10,0 | 1.00256 | 0,7 | 0.07138 | 9,9 | 14.010 | 19,5 |
| . 0716 | . 07166 |  | . 00256 |  | . 07148 |  | 13.990 | 19,5 |
| - .0717 | . 07176 |  | . 00257 |  | . 07158 |  | 13.971 | 19,4 |
| . 0718 | . 07186 |  | . 00258 |  | . 07168 |  | 13.952 | 19,4 |
| . 0719 | . 07196 |  | . 00259 |  | . 07178 |  | 13.932 | 19,3 |
| 0.0720 | 0.07206 | 10,0 | 1. 00259 | 0,7 | 0.07188 | 9,9 | 13.913 | 19,3 |
| . 0721 | . 07216 |  | . 00260 |  | . 07198 |  | 13.894 | 19,2 |
| . 0722 | . 07226 |  | .00261 |  | . 07207 |  | 13.874 | 19,2 |
| . 0723 | . 07236 |  | .00261 |  | . 07217 |  | 13.855 | 19, I |
| . 0724 | . 07246 |  | . 00262 |  | . 07227 |  | 13.836 | 19,0 |
| 0.0725 | 0.07256 | 10,0 | 1.00263 | 0,7 | 0.07237 | 9,9 | 13.817 | 19,0 |
| . 0726 | . 07266 |  | . 00264 |  | . 07247 |  | 13.798 | 18,9 |
| . 0727 | . 07276 |  | . 00264 |  | . 07257 |  | 13.779 | 18,9 |
| . 0728 | . 07286 |  | . 00265 |  | . 07267 |  | 13.761 | 18,8 |
| . 0729 | . 07296 |  | . 00266 |  | . 07277 |  | 13.742 | 18,8 |
| 0.0730 | 0.07306 | 10,0 | 1.00267 | 0,7 | 0.07287 | 9,9 | 13.723 | 18,7 |
| .0731 | . 07317 |  | . 00267 |  | . 07297 |  | 13.704 | 18,7 |
| . 0732 | . 07327 |  | . 00268 |  | . 07307 |  | 13.686 | 18,6 |
| . 0733 | . 07337 |  | . 00269 |  | . 07317 |  | 13.667 | 18,6 |
| . 0734 | . 07347 |  | . 00269 |  | . 07327 |  | 13.648 | 18,5 |
| 0.0735 | 0.07357 | 10,0 | 1.00270 | 0,7 | 0.07337 | 9,9 | 13.630 | 18,5 |
| . 0736 | . 07367 |  | . 00271 |  | . 07347 |  | 13.611 | 18,4 |
| . 0737 | . 07377 |  | . 00272 |  | . 07357 |  | 13.593 | 18,4 |
| . 0738 | . 07387 |  | . 00272 |  | . 07367 |  | 13.575 | 18,3 |
| . 0739 | . 07397 |  | . 00273 |  | . 07377 |  | I3.556 | 18,3 |
| 0.0740 | 0.07407 | 10,0 | 1.00274 | 0,7 | 0.07387 | 9,9 | 13.538 | 18,2 |
| . 0741 | . 07417 |  | . 00275 |  | . 07396 |  | 13.520 | 18,2 |
| . 0742 | . 07427 |  | . 00275 |  | . 07406 |  | 13.502 | 18, 1 |
| . 0743 | . 07437 |  | . 00276 |  | . 07416 |  | 13.484 | 18, 1 |
| . 0744 | . 07447 |  | . 00277 |  | . 07426 |  | 13.466 | 18,0 |
| 0.0745 | 0.07457 | 10,0 | 1.00278 | 0,7 | 0.07436 | 9,9 | 13.448 | 18,0 |
| . 0746 | . 07467 |  | . 00278 |  | . 07446 |  | 13.430 | 17,9 |
| . 0747 | . 07477 |  | . 00279 |  | . 07456 |  | 13.412 | 17,9 |
| . 0748 | . 07487 |  | . 00288 |  | . 07466 |  | 13.394 | 17,8 178 |
| . 0749 | . 07497 |  | .0028I |  | . 07476 |  | 13.376 | 17,8 |
| 0.0750 | 0.07507 | 10,0 | 1.00281 | 0,8 | 0.07486 | 9,9 | 13.358 | 17,7 |
| $u$ | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | sec gd u | $\omega \mathrm{Fo}^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | csc gd u | ~ $\mathrm{Fo}^{\prime}$ |

Natural Hyperbolic Functions.

| u | sinh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\circ}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0750 | 0.07507 | 10,0 | I.0028I | 0,8 | 0.07486 | 9,9 | 13.358 | 17,7 |
| . 0751 | . 07517 |  | . 00282 |  | . 07496 |  | I3.34I | 17,7 |
| . 0752 | . 07527 |  | . 00283 |  | . 07506 |  | 13.323 | 17,7 |
| . 0753 | . 07537 |  | . 00284 |  | .07516 |  | 13.305 | 17,6 |
| . 0754 | . 07547 |  | . 00284 |  | . 07526 |  | 13.288 | 17,6 |
| 0.0755 | 0.07557 | 10,0 | 1.00285 | 0,8 | 0.07536 | 9,9 | 13.270 | 17,5 |
| . 0756 | . 07567 |  | . 00286 |  | . 07546 |  | 13.253 | 17,5 |
| . 0757 | . 07577 |  | .00287 |  | . 07556 |  | 13.235 | 17,4 |
| . 0758 | . 07587 |  | . 00287 |  | . 07566 |  | 13.218 | I7,4 |
| . 0759 | . 07597 |  | . 00288 |  | . 07575 |  | 13.201 | 17,3 |
| 0.0760 | 0.07607 | 10,0 | 1.00289 | 0,8 | 0.07585 | 9,9 | 13.183 | 17,3 |
| .0761 | .07617 |  | . 00290 |  | . 07595 |  | 13.166 | 17,2 |
| . 0762 | . 07627 |  | . 00290 |  | . 07605 |  | 13.149 | 17,2 |
| . 0763 | . 07637 |  | .0029I |  | .07615 |  | 13.132 | 17,I |
| . 0764 | . 07647 |  | . 00292 |  | . 07625 |  | 13.114 | 17,I |
| 0.0765 | 0.07657 | 10,0 | 1.00293 | 0,8 | 0.07635 | 9,9 | 13.097 | 17, 1 |
| . 0766 | . 07667 |  | . 00294 |  | . 07645 |  | 13.080 | I7,0 |
| . 0767 | . 07678 |  | . 00294 |  | . 07655 |  | 13.063 | 17,0 |
| . 0768 | . 07688 |  | . 00295 |  | . 07665 |  | 13.046 | 16,9 |
| . 0769 | . 07698 |  | . 00296 |  | .07675 |  | 13.030 | 16,9 |
| 0.0770 | 0.07708 | 10,0 | 1.00297 | 0,8 | 0.07685 | 9,9 | 13.013 | 16,8 |
| .0771 | . 07718 |  | . 00297 |  | . 07695 |  | 12.996 | 16,8 |
| . 0772 | . 07728 |  | . 00298 |  | . 07705 |  | 12.979 | 16,7 |
| . 0773 | . 07738 |  | . 00299 |  | . 07715 |  | 12.962 | 16,7 |
| . 0774 | . 07748 |  | . 00300 |  | . 07725 |  | 12.946 | 16,7 |
| 0.0775 | 0.07758 | 10,0 | 1.00300 | 0,8 | 0.07735 | 9,9 | 12.929 | 16,6 |
| . 0776 | . 07768 |  | .00301 |  | . 07744 |  | 12.912 | 16,6 |
| . 0777 | . 07778 |  | . 00302 |  | . 07754 |  | 12.896 | 16,5 |
| . 0778 | . 07788 |  | . 00303 |  | . 07764 |  | 12.879 | 16,5 |
| . 0779 | . 07798 |  | . 00304 |  | . 07774 |  | 12.863 | 16,5 |
| 0.0780 | 0.07808 | 10,0 | 1.00304 | 0,8 | 0.07784 | 9,9 | 12.847 | 16,4 |
| .0781 | . 07818 |  | . 00305 |  | . 07794 |  | 12.830 | 16,4 |
| . 0782 | . 07828 |  | . 00306 |  | . 07804 |  | 12.814 | 16,3 |
| . 0783 | . 07838 |  | . 00307 |  | .07814 |  | 12.797 | 16,3 |
| . 0784 | . 07848 |  | . 00307 |  | . 07824 |  | 12.78 I | 16,2 |
| 0.0785 | 0.07858 | 10,0 | 1.00308 | 0,8 | 0.07834 | 9,9 | 12.765 | 16,2 |
| . 0786 | . 07868 |  | . 00309 |  | . 07844 |  | 12.749 | 16,2 |
| . 0787 | . 07878 |  | .00310 |  | . 07854 |  | 12.733 | 16,1 |
| . 0788 | . 07888 |  | .003II |  | . 07864 |  | 12.717 | 16, |
| . 0789 | . 07898 |  | .003II |  | . 07874 |  | 12.701 | 16,0 |
| 0.0790 | 0.07908 | 10,0 | 1.00312 | 0,8 | 0.07884 | - 9,9 | 12.685 | 16,0 |
| . 0791 | . 07918 |  | .00313 |  | . 07894 |  | 12.669 | 15,9 |
| . 0792 | . 07928 |  | .00314 |  | . 07903 |  | 12.653 | 15,9 |
| . 0793 | . 07938 |  | .00315 |  | .079r3 |  | 12.637 | I5,9 |
| . 0794 | . 07948 |  | .00315 |  | . 07923 |  | 12.621 | I5,8 |
| $0.0795^{\circ}$ | 0.07958 | 10,0 | 1.00316 | 0,8 | 0.07933 | 9,9 | 12.605 | I5,8 |
| . 0796 | . 07968 |  | . 00317 |  | . 07943 |  | 12.589 | 15,7 |
| . 0797 | . 07978 |  | . 00318 |  | . 07953 |  | 12.574 | 15,7 |
| . 0798 | . 07988 |  | .00319 |  | . 07963 |  | 12.558 | 15,7 |
| . 0799 | . 07999 |  | .00319 |  | . 07973 |  | 12.542 | 15,6 |
| 0.0800 | 0.08009 | 10,0 | 1.00320 | 0,8 | 0.07983 | 9,9 | 12.527 | 15,6 |
| $u$ | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h}$ u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathbf{F o}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0800 | 0.08009 | 10,0 | 1.00320 | 0,8 | 0.07983 | 9,9 | 12.527 | 15,6 |
| .0801 | . 08019 |  | . 00321 |  | . 07993 |  | 12.511 | 15,6 |
| . 0802 | . 08029 |  | . 00322 |  | . 08003 |  | 12.496 | 15,5 |
| . 0803 | . 08039 |  | . 00323 |  | . 08013 |  | 12.480 | 15,5 |
| . 0804 | . 08049 |  | . 00323 |  | . 08023 |  | 12.465 | 15,4 |
| 0.0805 | 0.08059 | 10,0 | 1.00324 | 0,8 | 0.08033 | 9,9 | 12.449 | 15,4 |
| . 0806 | . 08069 |  | . 00325 |  | . 08043 |  | 12.434 | 15,4 |
| . 0807 | . 08079 |  | . 00326 |  | . 08053 |  | 12.418 | 15,3 |
| . 0808 | . 08089 |  | . 00327 |  | . 08062 |  | 12.403 | 15,3 |
| . 0809 | . 08099 |  | . 00327 |  | . 08072 |  | 12.388 | 15,2 |
| 0.0810 | 0.08 r 09 | 10,0 | 1.00328 | 0,8 | 0.08082 | 9,9 | 12.373 | 15,2 |
| .08II | .08119 |  | . 00329 |  | . 08092 |  | 12.357 | 15,2 |
| .0812 | . 08129 |  | . 00330 |  | .08102 |  | 12.342 | 15, I |
| .0813 | .08139 |  | .00331 |  | .08112 |  | 12.327 | 15, 1 |
| .0814 | . 08149 |  | . 00331 |  | . 08122 |  | 12.312 | 15, 1 |
| 0.0815 | 0.08159 | 10,0 | 1.00332 | 0,8 | 0.08132 | 9,9 | 12.297 | 15,0 |
| . 0816 | . 08169 |  | . 00333 |  | .08142 |  | 12.282 | 15,0 |
| .0817 | .08179 |  | . 00333 |  | . 08152 |  | 12.267 | I4,9 |
| .0818 | . 08189 |  | . 00335 |  | . 08162 |  | 12.252 | 14,9 |
| .0819 | .08199 |  | . 00336 |  | . 08172 |  | 12.237 | 14,9 |
| 0.0820 | 0.08209 | 10,0 | 1.00336 | 0,8 | 0.08182 | 9,9 | 12.222 | 14,8 |
| .0821 | . 08219 |  | . 00337 |  | .08192 |  | 12.208 | 14,8 |
| . 0822 | . 08229 |  | . 00338 |  | . 08202 |  | 12.193 | 14,8 |
| . 0823 | . 08239 |  | . 00339 |  | . 08211 |  | 12.178 | 14,7 |
| . 0824 | . 08249 |  | . 00340 |  | .0822I |  | 12.163 | 14,7 |
| 0.0825 | 0.08259 | 10,0 | 1.00341 | 0,8 |  | 9,9 |  |  |
| . 0826 | . 08269 |  | . 00341 |  | . 08241 |  | 12.134 | 14,6 |
| . 0827 | . 08279 |  | . 00342 |  | .08251 |  | 12.119 | 14,6 |
| . 0828 | . 08289 |  | . 00343 |  | . 08261 |  | 12. 105 | 14,6 |
| . 0829 | . 08299 |  | . 00344 |  | . 08271 |  | 12.090 | 14,5 |
| 0.0830 | 0.08310 | 10,0 | 1.00345 | 0,8 | 0.08281 | 9,9 | 12.076 | 14,5 |
| . 0831 | . 08320 |  | . 00345 |  | .08291 |  | 12.061 | 14,4 |
| . 0832 | . 08330 |  | . 00346 |  | .08301 |  | 12.047 | 14,4 |
| . 0833 | . 08340 |  | . 00347 |  | .083II |  | 12.033 | 14,4 |
| . 0834 | . 08350 |  | . 00348 |  | .08321 |  | 12.018 | 14,3 |
| 0.0835 | 0.08360 | 10,0 | 1.00349 | 0,8 | 0.08331 | 9,9 | 12.004 | 14,3 |
| . 0836 | . 08370 |  | . 00350 |  | . 08341 |  | 11.990 | 14,3 |
| . 0837 | . 08380 |  | . 00350 |  | .08351 |  | 11.975 | 14,2 |
| . 0838 | . 08390 |  | .00351 |  | . 08360 |  | 11.961 | 14,2 |
| . 0839 | . 08400 |  | . 00352 |  | . 08370 |  | 11.947 | 14,2 |
| 0.0840 | 0.08410 | 10,0 | 1.00353 | 0,8 | 0.08380 | 9,9 | 11.933 | 14,1 |
| . 0841 | . 08420 |  | . 00354 |  | . 08390 |  | 11.919 | I4, I |
| . 0842 | . 08430 |  | . 00355 |  | . 08400 |  | 11.905 | 14, 1 |
| . 0843 | . 08440 |  | . 00356 |  | .08410 |  | 11.890 | 14,0 |
| . 0844 | . 08450 |  | . 00356 |  | . 08420 |  | 11.876 | 14,0 |
| 0.0845 | 0.08460 | 10,0 | 1.00357 | 0,8 | 0.08430 | 9,9 | 11.852 | 14,0 |
| . 0846 | . 08470 |  | . 00358 |  | . 08440 |  | 11.849 | 13,9 |
| . 0847 | . 08480 |  | . 00359 |  | . 08450 |  | 11.835 | 13,9 |
| . 0848 | . 08490 |  | . 00360 |  | . 08460 |  | 11.821 | 13,9 |
| . 0849 | . 08500 |  | .00361 | 0,9 | . 08470 |  | 11.807 | :3,8 |
| 0.0850 | 0.08510 | 10,0 | 1.00361 | 0,9 | 0.08480 | 9,9 | 11.793 | 13,8 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{od} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec od u | $\omega \mathrm{Fo}_{0}$ | $\boldsymbol{s i n}$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc od u | $\omega \mathrm{Fo}^{\prime}$ |

Smithbonian Tables

Natural Hypsrbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0850 | 0.08510 | 10,0 | 1.00361 | 0,9 | 0.08480 | 9,9 | I 1.793 | 13,8 |
| . 0851 | . 08520 |  | . 00362 |  | . 08490 |  | 11.779 | I 3,8 |
| . 0852 | . 08530 |  | . 00363 |  | . 08499 |  | 11.765 | 13,7 |
| . 0853 | . 08540 |  | . 00364 |  | . 08509 | - | 11.752 | 13,7 |
| . 0854 | . 08550 |  | . 00365 |  | .08519 |  | 11.738 | I 3,7 |
| 0.0855 | 0.08560 | 10,0 | 1.00366 | 0,9 | 0.08529 | 9,9 | II. 724 | 13,6 |
| . 0856 | . 08570 |  | . 00367 |  | . 08539 |  | II.711 | 13,6 |
| . 0857 | . 08580 |  | . 00367 |  | . 08549 |  | 11.697 | 13,6 |
| . 0858 | . 08591 |  | . 00368 |  | . 08559 |  | I I . 684 | 13,6 |
| .0859 | .08601 |  | . 00369 |  | . 08569 |  | II. 670 | 13,5 |
| 0.0860 | 0.086 II | 10,0 | 1.00370 | 0,9 | 0.08579 | 9,9 | 11.657 | 13,5 |
| . 0861 | . 08621 |  | . 00371 |  | . 08589 |  | 11.643 | 13,5 |
| . 0862 | . 08631 |  | . 00372 |  | . 08599 |  | 11.630 | I3,4 |
| . 0863 | . 08641 |  | . 00373 |  | . 08609 |  | II. 616 | I 3,4 |
| . 0864 | .0865I |  | . 00373 |  | .08619 |  | 11.603 | 13,4 |
| 0.0865 | 0.08661 | 10,0 | 1.00374 | 0,9 | 0.08528 | 9,9 | II .590 | 13,3 |
| . 0856 | . 08671 |  | . 00375 |  | . 08638 |  | I I. 576 | I3,3 |
| . 0867 | .08681 |  | . 00376 |  | . 08648 |  | II. 563 | I3,3 |
| . 0868 | .08691 |  | . 00377 |  | . 08658 |  | II. 550 | I3,2 |
| . 0869 | . 08701 |  | . 00378 |  | . 08668 |  | 11.536 | 13,2 |
| 0.0870 | 0.08711 | 10,0 | 1.00379 | 0,9 | 0.08678 | 9,9 | 11.523 | I3,2 |
| . 0871 | .08721 |  | . 00380 |  | . 08688 |  | II. 510 | I3, I |
| . 0872 | .08731 |  | . 00380 |  | . 08698 |  | 11.497 | I3, I |
| . 0873 | . 08741 |  | . 0038 I |  | .08708 |  | II . 484 | I3, I |
| . 0874 | .08751 |  | . 00382 |  | . 08718 |  | II. 471 | I3, I |
| 0.0875 | 0.08761 | 10,0 | 1.00383 | 0,9 | 0.08728 | 9,9 | II. 458 | 13,0 |
| . 0876 | . 08771 |  | . 00384 |  | . 08738 |  | II. 445 | I3,0 |
| . 0877 | .08781 |  | . 00385 | , | . 08748 |  | 11.432 | I3,0 |
| . 0878 | .08791 |  | . 00386 |  | . 08758 |  | II. 419 | 12,9 |
| . 0879 | .0880I |  | . 00387 |  | . 08767 |  | II. 406 | 12,9 |
| 0.0880 | 0.088 II | 10,0 | 1.00387 | 0,9 | 0.08777 | 9,9 | II. 393 | 12,9 |
| .0881 | . 0882 I |  | . 00388 |  | . 08787 |  | 11.380 | 12,8 |
| . 0882 | .0883I |  | . 00389 |  | . 08797 |  | II. 367 | 12,8 |
| . 0883 | .08841 |  | . 00390 |  | . 08807 |  | II. 354 | 12,8 |
| . 0884 | . 08852 |  | . 00391 |  | .08817 |  | II. 342 | I2,8 |
| 0.0885 | 0.08862 | 10,0 | 1.00392 | 0,9 | 0.08827 | 9,9 | II. 329 | 12,7 |
| . 0886 | . 08872 |  | . 00393 |  | . 08837 |  | II. 316 | 12,7 |
| . 0887 | . 08882 |  | . 00394 |  | . 08847 |  | II. 304 | 12,7 |
| . 0888 | . 08892 |  | . 00395 |  | . 08857 |  | II. 291 | 12,6 |
| . 0889 | . 08902 |  | . 00395 |  | . 08867 |  | II. 278 | 12,6 |
| 0.0890 | 0.08912 | 10,0 | 1.00396 | 0,9 | 0.08877 | 9,9 | I 1. 266 | 12,6 |
| . 0891 | . 08922 |  | . 00397 |  | . 08886 |  | II . 253 | 12,6 |
| . 0892 | . 08932 |  | . 00398 |  | . 08895 |  | II. 240 | 12,5 |
| . 0893 | . 08942 |  | . 00399 |  | .08906 |  | II . 228 | 12,5 |
| . 0894 | . 08952 |  | . 00400 |  | . 08916 |  | II. 215 | 12,5 |
| 0.0895 | 0.08962 | 10,0 | 1.00401 | 0,9 | 0.08926 | 9,9 | 11.203 | 12,5 |
| . 0896 | . 08972 |  | . 00402 |  | . 08936 |  | II. 191 | 12,4 |
| . 0897 | . 08982 |  | . 00403 |  | . 08946 |  | II. 178 | I2,4 |
| . 0898 | . 08992 |  | . 00403 |  | . 08956 |  | II. 166 | 12,4 |
| . 0899 | . 09002 |  | . 00404 |  | . 08966 |  | II. 153 | 12,3 |
| 0.0900 | 0.09012 | 10,0 | 1.00405 | 0,9 | 0.08976 | 9,9 | II.I4I | 12,3 |
| u | $\boldsymbol{t a n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text {g }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0900 | 0.09012 | 10,0 | 1.00405 | 0,9 | 0.08976 | 9,9 | II. 141 | 12,3 |
| .0901 | . 09022 |  | . 00406 |  | . 08986 |  | II. 129 | 12,3 |
| . 0902 | . 09032 |  | . 00407 |  | . 08996 |  | II. II7 | 12,3 |
| . 0903 | . 09042 |  | . 00408 |  | . 09006 |  | II. 104 | 12,2 |
| . 0904 | . 09052 |  | . 00409 |  | .09015 |  | 11.092 | 12,2 |
| 0.0905 | 0.09062 | 10,0 | 1.00410 | 0,9 | 0.09025 | 9,9 | 11.080 | 12,2 |
| . 0906 | . 09072 |  | .004II |  | . 09035 |  | 11.068 | 12, 1 |
| . 0907 | . 09082 |  | .00412 |  | . 09045 |  | 11.056 | 12, I |
| . 0908 | . 09092 |  | .00413 |  | . 09055 |  | 11.043 | 12, I |
| . 0909 | . 09103 |  | .004I3 |  | . 09065 |  | 11.031 | 12, 1 |
| 0.0910 | 0.09113 | 10,0 | 1.00414 | 0,9 | 0.09075 | 9,9 | 11.019 | 12,0 |
| .09II | .09123 |  | . 00415 |  | . 09085 |  | 11.007 | 12,0 |
| . 0912 | .09133 |  | .00416 |  | . 09095 |  | 10.995 | 12,0 |
| .0913 | .09143 |  | . 00417 |  | . 09105 |  | 10.983 | 12,0 |
| .0914 | .09153 |  | . 00418 |  | .091 15 |  | 10.971 | II,9 |
| 0.0915 | 0.09163 | 10,0 | 1.00419 | 0,9 | 0.09125 | 9,9 | 10.959 | I 1,9 |
| .0916 | .09173 |  | . 00420 |  | .09I34 |  | 10.948 | I I,9 |
| .0917 | .09183 |  | .0042I |  | .09144 |  | 10.936 | I I,9 |
| . 0918 | . 09193 |  | . 00422 |  | .09I54 |  | 10.924 | II,8 |
| . 0919 | . 09203 |  | . 00423 |  | .09164 |  | 10.912 | II,8 |
| 0.0920 | 0.09213 | 10,0 | 1.00423 | 0,9 | 0.09174 | 9,9 | 10.900 | II, 8 |
| . 0921 | . 09223 |  | . 00424 |  | . 09184 |  | 10.888 | II,8 |
| . 0922 | . 09233 |  | . 00425 |  | . 09194 |  | 10.877 | I 1,7 |
| . 0923 | . 09243 |  | . 00426 |  | . 09204 |  | 10.865 | II,7 |
| . 0924 | . 09253 |  | . 00427 |  | . 09214 |  | 10.853 | I 1,7 |
| 0.0925 | 0.09263 | 10,0 | 1. 00428 | 0,9 | 0.09224 | 9,9 | 10.842 | I I,7 |
| . 0926 | . 09273 |  | . 00429 |  | . 09234 |  | 10.830 | I 1,6 |
| . 0927 | . 09283 |  | . 00430 |  | . 09244 |  | 10.818 | 11,6 |
| . 0928 | . 09293 |  | .0043I |  | . 09253 |  | 10.807 | I 1,6 |
| . 0929 | . 09303 |  | . 00432 |  | . 09263 |  | 10.795 | I I, 6 |
| 0.0930 | 0.09313 | 10,0 | 1.00433 | 0,9 | 0.09273 | 9,9 | 10.784 | II,5 |
| .093I | . 09323 |  | . 00434 |  | . 09283 |  | 10.772 | II,5 |
| . 0932 | . 09333 |  | . 00435 |  | . 09293 |  | 10.761 | II,5 |
| . 0933 | . 09344 |  | . 00436 |  | . 09303 |  | 10.749 | I I,5 |
| . 0934 | . 09354 |  | . 00436 |  | . 09313 |  | 10.738 | II,4 |
| 0.0935 | 0.09364 | 10,0 | 1.00437 | 0,9 | 0.09323 | 9,9 | 10.726 | II,4 |
| . 0936 | . 09374 |  | . 00438 |  | . 09333 |  | 10.715 | I I, 4 |
| . 0937 | . 09384 |  | . 00439 |  | . 09343 |  | 10.704 | II,4 |
| . 0938 | . 09394 |  | . 00440 |  | . 09353 |  | 10.692 | II,3 |
| . 0939 | . 09404 |  | . 00441 |  | . 09362 |  | 10.68 I | II,3 |
| 0.0940 | 0.09414 | 10,0 | 1.00442 | 0,9 | 0.09372 | 9,9 | 10.670 | II,3 |
| . 0941 | . 09424 |  | . 00443 |  | . 09382 |  | 10.658 | II,3 |
| . 0942 | . 09434 |  | . 00444 |  | . 09392 |  | 10.647 | II,2 |
| . 0943 | . 09444 |  | . 00445 |  | . 09402 |  | 10.636 | II,2 |
| . 0944 | . 09454 |  | . 00446 |  | . 09412 |  | 10.625 | 11,2 |
| 0.0945 | 0.09464 | 10,0 | 1.00447 | 0,9 | 0.09422 | 9,9 | 10.613 | II,2 |
| . 0946 | . 09474 |  | . 00448 |  | . 09432 |  | 10.602 | II, I |
| . 09.47 | . 09484 |  | . 00449 |  | . 09442 |  | 10.591 | II, I |
| . 0948 | . 09494 |  | . 00450 | 0,9 | . 09452 |  | 10.580 | II, I |
| . 0949 | . 09504 |  | . 0045 I | I,0 | . 09462 |  | 10.569 | II, I |
| 0.0950 | 0.09514 | 10,0 | 1.00452 | 1,0 | 0.09472 | 9,9 | 10.558 | 11,0 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0950 | 0.09514 | 10,0 | 1.00452 | 1,0 | 0.09472 | 9,9 | 10. 558 | II,O |
| .095I | . 09524 |  | . 00453 |  | .0948I |  | 10.547 | I I,O |
| . 0952 | . 09534 |  | . 00453 |  | . 09491 |  | 10.536 | I I,O |
| . 0953 | . 09544 |  | . 00454 |  | .09501 |  | 10.525 | I I,O |
| . 0954 | . 09554 |  | . 00455 |  | . 09511 |  | 10.514 | I I,O |
| 0.0955 | 0.09565 | 10,0 | 1.00456 | 1,0 | 0.09521 | 9,9 | 10.503 | 10,9 |
| . 0956 | . 09575 |  | . 00457 |  | .0953I |  | 10.492 | 10,9 |
| . 0957 | . 09585 |  | . 00458 |  | . 09541 |  | 10.481 | 10,9 |
| . 0958 | . 09595 |  | . 00459 |  | . 09551 |  | 10.470 | 10,9 |
| . 0959 | . 09605 |  | . 00460 |  | . 09561 |  | 10.459 | 10,8 |
| 0.0960 | 0.09615 | 10,0 | 1.00461 | 1,0 | 0.09571 | 9,9 | 10.449 | 10,8 |
| .0961 | . 09625 |  | . 00462 |  | .0958I |  | 10.438 | 10,8 |
| . 0962 | . 09635 |  | . 00463 |  | . 09590 |  | 10.427 | 10,8 |
| . 0963 | . 09645 |  | . 00464 |  | . 09600 |  | 10.416 | 10,7 |
| . 0964 | . 09655 |  | . 00465 |  | . 09610 |  | 10.406 | 10,7 |
| 0.0965 | 0.09665 | 10,0 | 1.00466 | 1,0 | 0.09620 | 9,9 | 10.395 | 10,7 |
| . 0966 | . 09675 |  | . 00467 |  | . 09630 |  | 10.384 | 10,7 |
| . 0967 | . 09685 |  | . 00468 |  | . 09640 |  | 10.373 | 10,7 |
| . 0968 | . 09695 |  | . 00469 |  | . 09650 |  | 10.363 | 10,6 |
| . 0969 | . 09705 |  | . 00470 |  | . 09660 |  | 10.352 | 10,6 |
| 0.0970 | 0.09715 | 10,0 | 1.00471 | 1,0 | 0.09670 | 9,9 | 10.342 | 10,6 |
| . 0971 | . 09725 |  | . 00472 |  | . 09680 |  | 10.331 | 10,6 |
| . 0972 | . 09735 |  | . 00473 |  | . 09689 |  | 10.320 | 10,6 |
| . 0.0973 | . 09745 |  | . 00474 |  | . 09699 |  | 10.310 | 10,5 |
| . 0974 | . 09755 |  | . 00475 |  | . 09709 |  | 10.299 | 10,5 |
| 0.0975 | 0.09765 | 10,0 | 1.00476 | 1,0 | 0.09719 | 9,9 | 10.289 | 10,5 |
| . 0976 | . 09776 |  | . 00477 |  | . 09729 |  | 10.278 | 10,5 |
| . 0977 | . 09786 |  | . 00478 |  | . 09739 |  | 10.268 | 10,4 |
| . 0978 | . 09796 |  | . 00479 |  | . 09749 |  | 10.258 | 10,4 |
| . 0979 | . 09806 |  | . 00480 |  | . 09759 |  | 10.247 | 10,4 |
| 0.0980 | 0.09816 | 10,0 | I. 0048 I | 1,0 | 0.09769 | 9,9 | 10.237 | 10,4 |
| . 0981 | . 09882 |  | . 00482 |  | . 09779 |  | 10.226 | 10,4 |
| . 0982 | . 09836 |  | .00483 |  | . 09788 |  | 10.216 | 10,3 |
| . 0983 | . 09846 |  | . 00484 |  | . 09798 |  | 10.206 | 10,3 |
| . 0984 | . 09856 |  | . 00485 |  | . 09808 |  | 10. 195 | 10,3 |
| 0.0985 | 0.09866 | 10,0 | 1.00486 | 1,0 | 0.09818 | 9,9 | 10.185 | 10,3 |
| . 0986 | . 09876 |  | . 00486 |  | . 09828 |  | 10.175 | 10,3 |
| . 0987 | . 09886 |  | . 00487 |  | . 09838 |  | 10.165 | 10,2 |
| . 0988 | . 09896 |  | . 00488 |  | . 09848 |  | 10. I54 | 10,2 |
| . 0989 | . 09906 |  | . 00489 |  | . 09858 |  | 10.144 | 10,2 |
| 0.0990 | 0.09916 | 10,0 | 1.00490 | 1,0 | 0.09868 | 9,9 | 10. 134 | 10,2 |
| . 0991 | . 09926 |  | .00491 |  | . 09878 |  | 10.124 | IO, I |
| . 0992 | . 09936 |  | . 00492 |  | . 09888 |  | 10. 114 | IO, I |
| . 0993 | . 09946 |  | . 00493 |  | . 09897 |  | 10.104 | 10, I |
| . 0994 | . 09956 |  | . 00494 |  | . 09907 |  | 10.093 | 10, I |
| 0.0995 | 0.09966 | 10,0 | 1.00495 | I,O | 0.09917 | 9,9 | 10.083 | IO,I |
| . 0996 | . 09976 |  | . 00496 |  | . 09927 |  | 10.073 | 10,0 |
| . 0997 | . 09987 |  | . 00497 |  | . 09937 |  | 10.063 | 10,0 |
| . 0998 | . 09997 |  | . 00498 |  | . 09947 |  | 10.053 | 10,0 |
| . 0999 | . 10007 |  | . 00499 |  | . 09957 |  | 10.043 | 10,0 |
| 0.1000 | 0.10017 | 10,I | 1.00500 | I,O | 0.09967 | 9,9 | 10.033 | 10,0 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0:100 | 0.10017 | 100,5 | 1.00500 | 10,0 | 0.09967 | 99,0 | 10.0333 | 996,7 |
| . IOI | . 10117 | 100,5 | .00510 | 10, 1 | . 10066 | 99,0 | 9.9346 | 977,0 |
| . 102 | . 10218 | 100,5 | .0052I | 10,2 | . 10165 | 99,0 | . 8379 | 957,9 |
| . 103 | . 10318 | 100,5 | . 0053 I | 10,3 | . 10264 | 98,9 | . 7430 | 939,3 |
| . 104 | . 10419 | 100,5 | . 0054 I | 10,4 | . 10363 | 98,9 | . 6500 | 921,2 |
| 0.105 | 0.10519 | 100,6 | 1.00552 | 10,5 | 0. 10462 | 98,9 | 9.5588 | 903,7 |
| . 106 | . 10620 | 100,6 | . 00562 | 10,6 | . 10560 | 98,9 | . 4693 | 886,7 |
| . 107 | . 10720 | 100,6 | . 00573 | 10,7 | . 10659 | 98,9 | . 3814 | 870, I |
| . 108 | . 1082 I | 100,6 | . 00584 | 10,8 | . 10758 | 98,8 | . 2952 | 854,0 |
| . 109 | . 10922 | 100,6 | . 00595 | 10,9 | . 10857 | 98,8 | . 2106 | 838,4 |
| 0.110 | 0.11022 | 100,6 | 1.00606 | II,O | 0. 10956 | 98,8 | 9.1275 | 823, 1 |
| . III | . III23 | 100,6 | .00617 | II, I | . 11055 | 98,8 | . 0460 | 808,3 |
| . II2 | . II223 | 100,6 | . 00628 | II,2 | . III53 | 98,8 | 8.9659 | 793,9 |
| . 113 | . II324 | 100,6 | . 00639 | II,3 | . II252 | 98,7 | . 8872 | 779,8 |
| . 114 | . II425 | 100,7 | . 00651 | II,4 | . II351 | 98,7 | . 8099 | 766, |
| 0.115 | 0.11525 | 100,7 | 1.00662 | II,5 | 0.11450 | 98,7 | 8.7340 | 752,8 |
| . 116 | . 11626 | 100,7 | . 00674 | II,6 | . II548 | 98,7 | . 6593 | 739,8 |
| . 117 | . II727 | 100,7 | . 00685 | II,7 | . 11647 | 98,6 | . 5860 | 727,2 |
| . 118 | . 11827 | 100,7 | . 00697 | II,8 | . II746 | 98,6 | . 5139 | 714,9 |
| . 119 | . 11928 | 100,7 | . 00709 | II,9 | . I 1844 | 98,6 | . 4430 | 702,8 |
| 0.120 | 0.12029 | 100,7 | 1.00721 | 12,0 | 0.11943 | 98,6 | 8.3733 | 691, 1 |
| . 121 | . 12130 | 100,7 | . 00733 | 12,I | . 12041 | 98,6 | . 3048 | 679,7 |
| . 122 | . 12230 | 100,7 | . 00745 | 12,2 | . 12140 | 98,5 | . 2373 | 668,5 |
| . 123 | . I233I | 100,8 | . 00757 | 12,3 | . 12238 | 98,5 | . 1710 | 657,7 |
| . 124 | . 12432 | 100,8 | . 00770 | 12,4 | . 12337 | 98,5 | . 1058 | 647,0 |
| 0. 125 | 0. 12533 | 100,8 | 1.00782 | 12,5 | 0. 12435 | 98,5 | 8.0416 | 636,7 |
| . 126 | . 12633 | 100,8 | . 00795 | 12,6 | . I2534 | 98,4 | 7.9785 | 626,6 |
| . 127 | . 12734 | 100,8 | . 00808 | 12,7 | . 12632 | 98,4 | . 9163 | 616,7 |
| . 128 | . 12835 | 100,8 | . 00820 | 12,8 | . 12731 | 98,4 | .8551 | 607,0 |
| . 129 | . 12936 | 100,8 | . 00833 | 12,9 | . 12829 | 98,4 | . 7949 | 597,6 |
| 0.130 | 0. 13037 | 100,8 | 1.00846 | 13,0 | 0.12927 | 98,3 | 7.7356 | 588,4 |
| . 131 | . I3I38 | 100,9 | . 00859 | 13, I | . I3026 | c8,3 | . 6772 | 579,4 |
| . I32 | . 13238 | 100,9 | . 00872 | I3,2 | . 13124 | c8,3 | . 6197 | 570,6 |
| . I33 | . 13339 | 100,9 | . 00886 | 13,3 | . I3222 | 98,3 | . 563 I | 562,0 |
| . I34 | . 13440 | 100,9 | . 00899 | 13,4 | . 13320. | 98,2 | . 5073 | 553,6 |
| 0. I35 | 0. I354I | 100,9 | 1.00913 | 13,5 | 0.13419 | 98,2 | 7.4524 | 545,4 |
| . 136 | . 13642 | 100,9 | . 00926 | 13,6 | . 13517 | 98,2 | . 3982 | 537,3 |
| . 137 | . 13743 | 100,9 | . 00940 | 13,7 | . 13615 | 98, | - 3449 | 529,5 |
| . I38 | . 13844 | IOI, 0 | . 00954 | 13,8 | . 13713 | 98, I | . 2923 | 521,8 |
| . I39 | . I 3945 | 101,0 | . 00968 | 13,9 | . 13811 | 98, I | . 2405 | 514,3 |
| 0.140 | 0.14046 | 101,0 | 1.00982 | 14,0 | 0. I3909 | 98, 1 | 7.1895 | 506,9 |
| . 141 | . 14147 | 101,0 | . 00996 | I4, I | . 14007 | 98,0 | . 1391 | 499,7 |
| . 142 | . I4248 | 101,0 | . 01010 | 14,2 | . 14105 | 98,0 | . 0895 | 492,6 |
| . I43 | . I4349 | IOI, 0 | . 01024 | 14,3 | . 14203 | 98,0 | . 0406 | 485,7 |
| . 144 | . 14450 | IOI, 0 | . 01039 | 14,4 | . 14301 | 98,0 | 6.9924 | 478,9 |
| 0. 145 | 0.14551 | IOI, 1 | 1.01053 | 14,6 | 0. 14399 | 97,9 | 6.9448 | 472,3 |
| . I46 | . 14652 | IOI, I | . 01068 | 14,7 | . I4497. | 97,9 | . 8979 | 465,8 |
| . 147 | . 14753 | IOI, I | . 01082 | 14,8 | . I4595 | 97,9 | . 8517 | 459,5 |
| . 148 | . 14854 | IOI, I | . 01097 | 14,9 | . I4693 | 97,8 | . 8060 | 453,2 |
| . 149 | . 14955 | 101, I | . O1\% 12 | 15,0 | . 14791 | 97,8 | . 7610 | 447, 1 |
| 0.150 | 0. 15056 | IOI,I | 1.01127 | 15, I | 0.14889 | 97,8 | 6.7166 | 441, I |
| U | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | C: $F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.150 | 0.15056 | IOI, I | 1.01127 | 15,1 | 0.14889 | 97,8 | 6.7166 | 441, I |
| . 151 | . 15157 | IOI, I | . OII 42 | 15,2 | . 14986 | 97,8 | . 6728 | 435,3 |
| . 152 | . 15259 | IOI, 2 | .OII57 | 15,3 | . 15084 | 97,7 | . 6295 | 429,5 |
| . 153 | . 15360 | IOI, 2 | . O1173 | I5,4 | . 15182 | 97,7 | . 5869 | 423,9 |
| . 154 | . 1546 I | 101,2 | . 01188 | 15,5 | . 15279 | 97,7 | . 5448 | 418,3 |
| 0.155 | 0.15562 | 101,2 | 1.01204 | 15,6 | 0. 15377 | 97,6 | 6.5032 | 412,9 |
| . 156 | . 15663 | 101, 2 | . 01219 | 15,7 | . 15475 | 97,6 | . 4622 | 407,6 |
| . 157 | . 15765 | 101,2 | . 01235 | 15,8 | . 15572 | 97,6 | . 4217 | 402,4 |
| . I58 | . 15866 | IOI,3 | . OI 251 | 15,9 | . 15670 | 97,5 | .3817 | 397,3 |
| . 159 | . 15967 | IOI,3 | . 01267 | 16,0 | . 15767 | 97,5 | - 3422 | 392,2 |
| 0.160 | 0.16068 | 101,3 | 1.01283 | 16,1 | 0.15865 | 97,5 | 6.3032 | 387,3 |
| .161 | . 16I70 | 101,3 | . 01299 | 16,2 | . 15952 | 97,5 | . 2648 | 382,5 |
| . 162 | . 16271 | IOI,3 | .OI3I5 | 16,3 | . 16060 | 97,4 | . 2267 | 377,7 |
| . 163 | . 16372 | 101,3 | .01331 | 16,4 | . 16157 | 97,4 | . 1892 | 373, 1 |
| . 164 | . 16474 | 101,3 | . OI348 | 16,5 | . 16254 | 97,4 | . 1521 | 368,5 |
| 0. 165 | 0.16575 | IOI, 4 | I. 01364 | 16,6 | 0.16352 | 97,3 | 6.1155 | 364,0 |
| . 166 | . 16676 | 10I,4 | .0138I | 16,7 | . 16449 | 97,3 | . 0793 | 359,6 |
| . 167 | . 16778 | IOI,4 | . OI 398 | 16,8 | . 16546 | 97,3 | . 0436 | 355,2 |
| . 168 | . 16879 | IOI, 4 | .OI4I5 | 16,9 | . 16644 | 97,2 | . 0083 | 351,0 |
| . 169 | . 16981 | IOI,4 | . 0143 I | 17,0 | . I674I | 97,2 | 5.9734 | 346,8 |
| 0.170 | 0.17082 | 101,4 | I. 01448 | 17,I | 0. 16838 | 97,2 | 5.9389 | 342,7 |
| .171 | . 17183 | IOI,5 | . 01466 | 17,2 | . 16935 | 97, I | . 9048 | 338,7 |
| . 172 | . 17285 | IOI,5 | . OI483 | 17,3 | .17032 | 97, I | . 8712 | 334,7 |
| .173 | . 17386 | 1OI,5 | . 01500 | 17,4 | . 17129 | 97, I | . 8379 | 330,8 |
| . 174 | . 17488 | IOI,5 | . 01518 | 17,5 | . 17226 | 97,0 | . 8050 | 327,0 |
| 0.175 | 0.17589 | 101,5 | I. 01535 | 17,6 | 0.17324 | 97,0 | 5.7725 | 323,2 |
| . 176 | . 17691 | 101,6 | . OI 553 | 17,7 | . 17420 | 97,0 | . 7404 | 319,5 |
| . 177 | . 17793 | IOI,6 | . O1571 | 17,8 | . 17517 | 96,9 | . 7086 | 315,9 |
| .178 | . 17894 | IOI,6 | .OI588 | I7,9 | .176I4 | 96,9 | . 6772 | 312,3 |
| . 179 | . 17996 | 101,6 | .01606 | 18,0 | .177II | 96,9 | . 6461 | 308,8 |
| 0.180 | 0.18097 | 101,6 | 1.01624 | I8,1 | 0. 17808 | 96.8 | 5.6154 | 305,3 |
| .181 | .18199 | IOI,6 | . 01643 | 18,2 | . I7905 | 96,8 | . 585 I | 301,9 |
| . 182 | . 18301 | 101,7 | .0166I | 18,3 | . 18002 | 96,8 | . 5550 | 298,6 |
| .183 | . 18402 | IOI,7 | .01679 | 18,4 | . 18098 | 96,7 | . 5253 | 295,3 |
| . 184 | . 18504 | 101,7 | .01698 | 18,5 | .18I95 | 96,7 | . 4960 | 292, I |
| 0. 185 | 0.18606 | 101,7 | 1.01716 | 18,6 | 0.18292 | 96,7 | 5.4669 | 288,9 |
| . 186 | . 18707 | 101,7 | . OI735 | 18,7 | . 18388 | 96,6 | . 4382 | 285,8 |
| . 187 | . 18809 | IOI, 8 | . OI754 | 18,8 | . 18485 | 96,6 | . 4098 | 282,7 |
| . 188 | . 1891 I | IOI, 8 | . 01772 | 18,9 | . 18582 | 96,5 | . 3817 | 279,6 |
| . 189 | . 19013 | IOI,8 | .01791 | 19,0 | . 18678 | 96,5 | . 3539 | 276,6 |
| 0.190 | -.1915 | IOI, 8 | I. 01810 | 19,I | 0. 18775 | 96,5 | $5 \cdot 3263$ |  |
| . 191 | . 19216 | IOI,8 | . 01830 | 19,2 | . 18871 | 96,4 | . 2991 | 270,8 |
| . 192 | . 19318 | IOI,8 | . 01849 | 19,3 | . 18967 | 96,4 | . 2722 | 268,0 |
| . I93 | . 19420 .19522 | IOI,9 | . 01868 | 19,4 | . 19064 | 96,4 | . 2455 | 265,2 |
| . 194 | . 19522 | 101,9 | . 01888 | 19,5 | . 19160 | 96,3 | .2191 | 262,4 |
| 0.195 | 0.19624 | 101,9 | I. 01907 | 19,6 | 0. 19257 | 96,3 | 5.1930 | 259,7 |
| . 196 | . 19726 | IOI,9 | . 01927 | 19,7 | . 19353 | 96,3 | . 1672 | 257,0 |
| . 197 | . 19828 | 101,9 | . 01947 | 19,8 | . 19449 | 96,2 | . I416 | 254,4 |
| .198 .199 | . 19930 | 102,0 102,0 | . 01967 | 19,9 | . 19545 | 96,2 | . II63 | 251,8 |
| - 199 | . 20032 | 102,0 | . 01987 | 20,0 | . 1964 I | 96, I | . 0913 | 249,2 |
| 0.200 | 0.20134 | 102,0 | 1.02007 | 20, I | 0. 19738 | 96, 1 | 5.0665 | 246,7 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| 4 | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.200 | 0.20134 | 102,0 | 1.02007 | 20,1 | 0. 19738 | 96, I | 5.0665 | 246,7 |
| . 201 | . 20236 | 102,0 | . 02027 | 20,2 | . 19834 | 96, 1 | .0419 | 244,2 |
| . 202 | . 20338 | 102,0 | . 02047 | 20,3 | . 19930 | 96,0 | .0176 | 241,8 |
| . 203 | . 20440 | 102,I | . 02068 | 20,4 | . 20026 | 96,0 | 4.9936 | 239,4 |
| . 204 | . 20542 | 102, I | . 02088 | 20,5 | . 20122 | 96,0 | . 9698 | 237,0 |
| 0.205 | 0.20644 | 102, 1 | 1.02109 | 20,6 | 0.20218 | 95,9 | 4.9462 | 234,6 |
| . 206 | . 20746 | 102,I | . 02129 | 20,7 | .20313 | 95,9 | . 9228 | 232,3 |
| . 207 | . 20848 | 102,2 | .02150 | 20,8 | . 20409 | 95,8 | . 8997 | 230,1 |
| . 208 | . 20950 | 102,2 | .02171 | 21,0 | . 20505 | 95,8 | . 8768 | 227,8 |
| . 209 | . 21052 | 102,2 | .02192 | 2I, I | .2060I | 95,8 | . 8542 | 225,6 |
| 0.210 | 0.21155 | 102,2 | I. 02213 | 21,2 | 0.20697 | 95,7 | 4.8317 | 223,5 |
| . 211 | . 21257 | 102,2 | . 02234 | 21,3 | . 20792 | 95,7 | . 8095 | 221,3 |
| . 212 | . 21359 | 102,3 | . 02256 | 21,4 | . 20888 | 95,6 | . 7874 | 219,2 |
| . 213 | . 21461 | 102,3 | . 02277 | 21,5 | . 20984 | 95,6 | . 7656 | 217,I |
| . 214 | . 21564 | 102,3 | . 02299 | 21,6 | . 21079 | 95,6 | . 7440 | 215,I |
| 0.215 | 0.21666 | 102,3 | 1.02320 | 21,7 | 0.21175 | 95,5 | 4.7226 | 213,0 |
| . 216 | .21768 | 102,3 | . 02342 | 21,8 | . 21270 | 95,5 | . 7014 | 211,0 |
| . 217 | . 21871 | 102,4 | . 02364 | 21,9 | . 21366 | 95,4 | . 6804 | 209,1 |
| . 218 | . 21973 | 102,4 | . 02386 | 22,0 | . 21461 | 95,4 | . 6596 | 207, I |
| . 219 | . 22075 | 102,4 | . 02408 | 22, I | . 21556 | 95,4 | . 6390 | 205,2 |
| 0.220 | 0.22178 | 102,4 | I. 02430 | 22,2 | 0.21652 | 95,3 | 4.6186 | 203,3 |
| . 221 | . 22280 | 102,5 | . 02452 | 22,3 | . 21747 | 95,3 | . 5983 | 201,4 |
| . 222 | . 22383 | 102,5 | . 02474 | 22,4 | . 21842 | 95,2 | . 5783 | 199,6 |
| . 223 | . 22485 | 102,5 | . 02497 | 22,5 | . 21938 | 95,2 | . 5584 | 197,8 |
| . 224 | . 22588 | 102,5 | .02519 | 22,6 | . 22033 | 95, I | . 5387 | 196,0 |
| 0.225 | 0.22690 | 102,5 | 1.02542 | 22,7 | 0.22128 | 95, I | $4 \cdot 5192$ | 194,2 |
| . 226 | . 22793 | 102,6 | . 02565 | 22,8 | . 22223 | 95, I | . 4999 | 192,5 |
| . 227 | . 22895 | 102,6 | . 02588 | 22,9 | . 223 I8 | 95,0 | . 4807 | 190,8 |
| . 228 | . 22998 | 102,6 | .02610 | 23,0 | . 22413 | 95,0 | .46I7 | 189, 1 |
| . 229 | .23IOI | 102,6 | . 02634 | 23,1 | . 22508 | 94,9 | . 4429 | 187,4 |
| 0.230 | 0.23203 | 102,7 | 1.02657 | 23,2 | 0.22603 | 94.9 | 4.4242 | 185,7 |
| . 231 | . 23306 | 102,7 | . 02680 | 23,3 | . 22698 | 94,8 | . 4057 | 184 , I |
| . 232 | . 23409 | 102,7 | . 02703 | 23,4 | . 22793 | 94,8 | . 3874 | 182,5 |
| . 233 | .235II | 102,7 | . 02727 | 23,5 | . 22887 | 94,8 | . 3692 | 180,9 |
| . 234 | . 23614 | 102,8 | . 02750 | 23,6 | . 22982 | 94,7 | . 3512 | 179,3 |
| 0.235 | 0.23717 | 102,8 | 1.02774 | 23,7 | 0.23077 | 94,7 | 4.3334 | 477,8 |
| . 236 | . 23820 | I02,8 | . 02798 | 23,8 | . 23171 | 94,6 | . 3157 | 176,2 |
| . 237 | . 23922 | I02,8 | . 02822 | 23,9 | . 23266 | 94,6 | .298I | 174,7 |
| . 238 | . 24025 | 102,8 | . 02846 | 24,0 | . 2336 I | 94,5 | . 2807 | 173,2 |
| . 239 | . 24128 | 102,9 | .02870 | 24, I | . 23455 | 94,5 | . 2635 | I71,8 |
| 0.240 | 0.2423 I | 102,9 | 1.02894 | 24,2 | 0.23550 | 94,5 | 4.2464 | I70,3 |
| . 241 | . 24334 | 102,9 | . 02918 | 24,3 | . 23644 | 94,4 | . 2294 | 168,9 |
| . 242 | . 24437 | I02,9 | . 02943 | 24,4 | . 23738 | 94,4 | . 2126 | 167,5 |
| . 243 | . 24540 | 103,0 | . 02967 | 24,5 | . 23833 | 94,3 | . 1959 | 166, I |
| . 244 | . 24643 | 103,0 | . 02992 | 24,6 | . 23927 | 94,3 | . 1794 | 164,7 |
|  | 0.24746 | 103,0 | 1.03016 |  | 0.24021 | 94,2 | 4.1630 |  |
| . 246 | . 24849 | 103,0 | .03041 | 24,8 | . 24115 | 94,2 | . 1467 | 162,0 |
| . 247 | . 24952 | 103, I | . 03066 | 25,0 | . 24210 | 94, I | . 1306 | 160,6 |
| . 248 | . 25055 | 103, I | .03091 | 25, I | . 24304 | 94, 1 | . II46 | I 59,3 |
| . 249 | . 25158 | 103, I | .03II6 | 25,2 | . 24398 | 94,0 | .0987 | 158,0 |
| 0.250 | 0.25261 | 103, 1 | 1.0314 | 25,3 | 0.24492 | 94,0 | 4.0830 | 156,7 |
| U | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.250 | 0.25261 | 103, I | 1,03I4I | 25,3 | 0.24492 | 94,0 | 4.0830 | 156,7 |
| . 251 | . 25364 | 103,2 | .03167 | 25,4 | . 24585 | 94,0 | . 0674 | 155,4 |
| . 252 | . 25468 | 103,2 | .03192 | 25,5 | . 24680 | 93,9 | . 0519 | 154,2 |
| . 253 | . 25571 | 103,2 | .03218 | 25,6 | . 24774 | 93,9 | . 0365 | 152,9 |
| . 254 | . 25674 | 103,2 | . 03243 | 25,7 | . 24867 | 93,8 | . 0213 | 151,7 |
| 0.255 | 0.25777 | 103,3 | 1.03269 | 25,8 | 0.2496 I | 93,8 | 4.0062 | 150,5 |
| . 256 | . 2588 I | 103,3 | . 03295 | 25,9 | . 25055 | 93,7 | 3.9912 | I49,3 |
| . 257 | . 25984 | 103,3 | .0332I | 26,0 | . 25149 | 93,7 | . 9763 | I48.1 |
| . 258 | . 26087 | 103,3 | . 03347 | 26,1 | . 25242 | 93,6 | . 9616 | 146,9 |
| . 259 | .26191 | 103,4 | . 03373 | 26,2 | . 25336 | 93,6 | . 9470 | 145,8 |
| 0.260 | 0.26294 | 103,4 | 1.03399 | 26,3 | 0.25430 | 93,5 | 3.9324 | 144,6 |
| . 261 | . 26397 | 103,4 | . 03425 | 26,4 | . 25523 | 93,5 | . 9180 | I43,5 |
| . 262 | . 26501 | 103,5 | . 03452 | 26,5 | . 25617 | 93,4 | . 9037 | 142,4 |
| .263 | . 26604 | 103,5 | . 03478 | 26,6 | . 25710 | 93,4 | . 8895 | 141,3 |
| . 264 | . 26708 | 103,5 | . 03505 | 26,7 | . 25803 | 93,3 | . 8755 | 140,2 |
| 0.265 | 0.268II | 103,5 | 1.03532 | 26,8 | 0.25897 | 93,3 | 3.8615 | I 39, 1 |
| . 266 | . 26915 | 103,6 | . 03559 | 26,9 | . 25990 | 93,2 | . 8476 | 138,0 |
| . 267 | . 27018 | 103,6 | . 03586 | 27,0 | . 26083 | 93,2 | .8339 | 137,0 |
| . 268 | . 27122 | 103,6 | .03613 | 27,1 | .26176 | 93, 1 | . 8203 | 135,9 |
| . 269 | . 27226 | 103,6 | . 03640 | 27,2 | . 26269 | 93, 1 | . 8067 | 134,9 |
| 0.270 | 0.27329 | 103,7 | 1.03667 | 27,3 | 0.26362 | 93, I | 3.7933 | 133,9 |
| . 271 | . 27433 | 103,7 | . 03695 | 27,4 | . 26456 | 93,0 | . 7799 | I32,9 |
| . 272 | . 27537 | 103,7 | . 03722 | 27,5 | . 26548 | 93,0 | . 7667 | 131,9 |
| . 273 | . 27640 | 103,7 | . 03750 | 27,6 | . 26641 | 92,9 | . 7536 | I 30,9 |
| . 274 | . 27744 | 103,8 | . 03777 | 27,7 | . 26734 | 92,9 | .7405 | I29,9 |
| 0.275 | 0.27848 | 103,8 | 1.03805 | 27,8 | 0.26827 | 92,8 | 3.7276 | 128,9 |
| . 276 | . 27952 | 103,8 | . 03833 | 28,0 | . 26920 | 92,8 | . 7147 | 128,0 |
|  | . 28056 | 103,9 | . 0386 I | 28,1 | . 27013 | 92,7 | . 7020 | 127,0 |
| . 278 | .28159 | 103,9 | . 03889 | 28,2 | . 27105 | 92,7 | . 6893 | 126, 1 |
| . 279 | . 28263 | 103,9 | .03917 | 28,3 | . 27198 | 92,6 | . 6768 | 125,2 |
| 0.280 | 0.28367 | 103,9 | 1.03946 | 28,4 | 0.27291 | 92,6 | 3.6643 | 124,3 |
| . 281 | . 28471 | 104,0 | . 03974 | 28,5 | . 27383 | 92,5 | . 6519 | 123,4 |
| . 282 | . 28575 | 104,0 | . 04003 | 28,6 | . 27476 | 92,5 | . 6396 | 122,5 |
| . 283 | . 28679 | 104,0 | . 04031 | 28,7 ${ }^{\circ}$ | . 27568 | 92,4 | . 6274 | I21,6 |
| . 284 | .28783 | 104, 1 | . 04060 | 28,8 | . 27660 | Q2,4 | .6153 | 120,7 |
| 0.285 | 0.28887 | 104, 1 | 1.04089 | 28,9 | 0.27753 | 92,3 | 3.6033 | I 19,8 |
| . 286 | . 28991 | 104, 1 | . 04118 | 29,0 | . 27845 | 92,2 | . 5913 | I 19,0 |
| . 287 | . 29096 | 104, I | . 04147 | 29, I | . 27937 | 92,2 | . 5795 | I 18, 1 |
| . 288 | . 29200 | 104,2 | .04176 | 29,2 | . 28029 | 92,I | . 5677 | 117,3 |
| . 289 | . 29304 | 104,2 | . 04205 | 29,3 | .28121 | 92,I | . 5560 | I16,5 |
| 0.290 | 0.29408 | 104,2 | 1.04235 | 29,4 | 0.28213 | 92,0 | 3.5444 | 115,6 |
| . 291 | . 29512 | 104,3 | . 04264 | 29,5 | . 28305 | 92,0 | . 5329 | II 4,8 |
| . 292 | . 29617 | 104,3 | . 04294 | 29,6 | . 28397 | 91,9 | . 5214 | I I4, 0 |
| . 293 | . 2972 I | 104,3 | . 04323 | 29,7 | . 28489 | 91,9 | . 5101 | II3,2 |
| . 294 | . 29825 | 104,4 | . 04353 | 29,8 | .28581 | 91,8 | . 4988 | II2,4 |
| 0.295 | 0.29930 | 104,4 | 1. 04383 | 29,9 | 0.28673 | 91,8 | 3.4876 | III, 6 |
| . 296 | . 30034 | 104,4 | . 04413 | 30,0 | .28765 | 91,7 | . 4765 | 1 10,9 |
| . 297 | . 30139 | 104,4 | . 04443 | 30, I | . 28856 | 91,7 | . 4654 | I 10, 1 |
| . 298 | . 30243 | 104,5 | . 04473 | 30,2 | . 28948 | 91,6 | . 4545 | 109,3 |
| . 299 | . 30348 | 104,5 | . 04503 | 30,3 | . 29040 | 91,6 | . 4436 | 108,6 |
| 0.300 | 0.30452 | 104,5 | 1.04534 | 30,5 | 0.29131 | 91,5 | 3.4327 | 107,8 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c}$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | tanh u | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ | coth u | $\omega^{*} \mathrm{Fo}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.300 | 0.30452 | 104,5 | 1.04534 | 30,5 | 0.29131 | - 91,5 | 3.4327 | 107,8 |
| . 301 | . 30557 | 104,6 | . 04564 | 30,6 | . 29223 | 91,5 | . 4220 | 107, 1 |
| . 302 | - 30661 | 104,6 | . 04595 | 30,7 | . 29314 | 9I,4 | .4113 | 106,4 |
| - 303 | - 30766 | 104,6 | . 04626 | 30,8 | . 29406 | 91,4 | . 4007 | 105,6 |
| - 304 | - 30870 | 104,7 | . 04656 | 30,9 | . 29497 | 91,3 | . 3902 | 104,9 |
| 0.305 | 0.30975 | 104,7 | 1.04687 | 31,0 | 0.29588 | 91,2 | 3.3797 | 104,2 |
| . 306 | . 31080 | 104,7 | . 04718 | 31,I | . 29679 | 91,2 | . 3693 | 103,5 |
| - 307 | - 31185 | 104,7 | . 04750 | 31,2 | . 29771 | 91, I | . 3590 | 102,8 |
| . 308 | -31289 | 104,8 | .04781 | 31,3 | . 29862 | 91, I | . 3488 | 102, 1 |
| -309 | - 31394 | 104,8 | .04812 | 31,4 | . 29953 | 91,0 | . 3386 | 101,5 |
| 0.310 | 0.31499 | 104,8 | 1.04844 | 31,5 | 0.30044 | 91,0 | 3.3285 | 100,8 |
| . 311 | . 31604 | 104,9 | . 04875 | 31,6 | . 30135 | 90,9 | . 3184 | 100, 1 |
| -312 | - 31709 | 104,9 | . 04907 | 31,7 | . 30225 | 90,9 | . 3085 | 99,5 |
| . 313 | - 31814 | 104,9 | . 04939 | 3I,8 | . 30316 | 90,8 | . 2985 | 98,8 |
| . 314 | -31919 | 105,0 | . 04970 | 31,9 | . 30407 | 90,8 | . 2887 | 98,2 |
| 0.315 | 0.32024 | 105,0 | 1.05002 | 32,0 | 0.30498 | 90,7 | 3.2789 | 97,5 |
| . 316 | . 32129 | 105,0 | . 05034 | 32,1 | . 30589 | 90,6 | . 2692 | 96,9 |
| -317 | . 32234 | 105, I | . 05067 | 32,2 | - 30679 | 90,6 | . 2595 | 96,2 |
| -318 | . 32339 | 105, I | . 05099 | 32,3 | - 30770 | 90,5 | . 2499 | 95,6 |
| -319 | . 32444 | 105, 1 | .05131 | 32,4 | . 30860 | 90,5 | . 2404 | 95,0 |
| 0.320 | 0.32549 | 105,2 | 1.05164 | 32,5 | 0.30951 | 90,4 | 3.2309 | 94,4 |
| . 321 | - 32654 | 105,2 | . 05196 | 32,7 | .3104I | 90,4 | . 2215 | 93,8 |
| - 322 | . 32759 | 105,2 | . 05229 | 32,8 | . 31131 | 90,3 | . 2122 | 93,2 |
| . 323 | - 32865 | 105,3 | . 05262 | 32,9 | . 31222 | 90,3 | . 2029 | 92,6 |
| -324 | - 32970 | 105,3 | . 05295 | 33,0 | . 31312 | 90,2 | . 1937 | 92,0 |
| 0.325 | 0.33075 | 105,3 | 1.05328 | 33, 1 | 0.31402 | 90, I | 3.1845 | 91,4 |
| . 326 | -33181 | 105,4 | .05361 | 33,2 | . 31492 | 90, I | . 1754 | 90,8 |
| . 327 | . 33285 | 105,4 | . 05394 | 33,3 | . 31582 | 90,0 | . 1663 | 90,3 |
| - 328 | -33391 | 105,4 | . 05428 | 33,4 | - 31672 | 90,0 | . 1573 | 89,7 |
| - 329 | - 33497 | 105,5 | .0546I | 33,5 | . 31762 | 89,9 | . 1484 | 89, I |
| 0.330 | 0.33602 | 105,5 | 1. 05495 | 33,6 | 0.31852 |  | 3.1395 | 88,6 |
| . 331 | - 33708 | 105,5 | . 05528 | 33,7 | . 31942 | 89,8 | . 1307 | 88,0 |
| . 332 | . 33813 | 105,6 | . 05562 | 33,8 | - 32032 | 89,7 | . 1219 | 87,5 |
| . 333 | - 33919 | 105,6 | . 05596 | 33,9 | -32121 | 89,7 | . 1132 | 86,9 |
| - 334 | - 34024 | 105,6 | . 05630 | 34,0 | -32211 | 89,6 | . 1045 | 86,4 |
| - 0.335 | 0.34130 | 105,7 | 1.05664 | 34, I | 0.32301 | 89,6 | 3.0959 | 85,8 |
| . 336 | . 34236 | 105,7 | . 05698 | 34,2 | . 32390 | 89,5 | . 0874 | 85,3 |
| - 337 | - 34342 | 105,7 | . 05732 | 34,3 | - 32480 | 89,5 | . 0789 | 84,8 |
| - 338 | - 34447 | 105,8 | . 05767 | 34,4 | - 32569 | 89,4 | . 0704 | 84,3 |
| . 339 | - 34553 | 105,8 | .05801 | 34,6 | - 32658 | 89,3 | . 0620 | 83,8 |
| 0.340 | 0.34659 | 105,8 | 1.05836 | 34,7 | 0.32748 | 89,3 | 3.0536 | 83,2 |
| . 341 | - 34765 | 105,9 | .05871 | 34,8 | . 32837 | 89,2 | . 0453 | 82,7 |
| . 342 | - 34871 | 105,9 | . 05905 | 34,9 | . 32926 | 89,2 | .0371 | 82,2 |
| - 343 | - 34977 | 105,9 | . 05940 | 35,0 | - 33015 | 89,1 | . 0289 | $8 \mathrm{I}, 7$ |
| -344 | - 35082 | 106,0 | . 05975 | 35, 1 | . 33104 | 89,0 | . 0207 | 81,2 |
| 0.345 | 0.35188 | 106,0 | 1.06011 | 35,2 | 0.33193 | 89,0 | 3.0126 | 80,8 |
| . 346 | . 35295 | 106,0 | . 06046 | 35,3 | . 33282 | 88,9 | . 0046 | 80,3 |
| - 347 | - 35401 | 106,1 | .0608I | 35,4 | . 33371 | 88,9 | 2.9966 | 79,8 |
| -348 | - 35507 | 106, 1 | . 066117 | 35,5 | . 33460 | 88,8 | . 9886 | 79,3 |
| -349 | -35613 | 106,2 | . 06152 | 35,6 | - 33549 | 88,7 | . 9807 | 78,8 |
| 0.350 | 0.35719 | 106,2 | 1.06188 | 35,7 | 0.33638 | 88,7 | 2.9729 | 78,4 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathbf{s e c}$ gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n}$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{Fo}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.350 | 0.35719 | 106,2 | 1.06188 | 35,7 | 0.33638 | 88,7 | 2.9729 | 78,4 |
| . 351 | . 35825 | 106,2 | . 06224 | 35,8 | . 33726 | 88,6 | . 9651 | 77,9 |
| - 352 | - 3593I | 106,3 | . 06259 | 35,9 | -33815 | 88,6 | . 9573 | 77,5 |
| - 353 | . 36038 | 106,3 | . 06295 | 36,0 | - 33903 | 88,5 | . 9496 | 77,0 |
| - 354 | . 36144 | 106,3 | . 06332 | 36,1 | -33992 | 88,4 | .9419 | 76,5 |
| 0.355 | 0.36250 | 106,4 | 1.06368 | 36,3 | 0.34080 | 88,4 | 2.9343 | 76, r |
| . 356 | . 36357 | 106,4 | . 06404 | 36,4 | . 34169 | 88,3 | . 9267 | 75,7 |
| - 357 | . 36463 | 106,4 | . 06440 | 36,5. | - 34257 | 88,3 | .9191 | 75,2 |
| . 358 | - 36570 | 106,5 | . 06477 | 36,6 | - 34345 | 88,2 | .9116 | 74,8 |
| - 359 | . 36676 | 106,5 | . 06514 | 36,7 | - 34433 | 88, 1 | . 9042 | 74,3 |
| 0.360 | 0.36783 | 106,6 | 1. 06550 | 36,8 | 0.34521 | 88,1 | 2.8968 | 73,9 |
| . 361 | . 36889 | 106,6 | . 06587 | 36,9 | - 34609 | 88,0 | . 8894 | 73,5 |
| - 362 | . 36996 | 106,6 | . 06624 | 37,0 | - 34697 | 88,0 | . 8821 | 73, 1 |
| . 363 | -37102 | 106,7 | . 06661 | 37,I | - 34785 | 87,9 | . 8748 | 72,6 |
| - 364 | . 37209 | 106,7 | . 06698 | 37,2 | - 34873 | 87,8 | . 8675 | 72,2 |
| 0. 365 | 0.37316 | 106,7 | 1. 06736 | 37,3 | 0.34961 | 87,8 | 2.8603 | 71,8 |
| . 366 | . 37423 | 106,8 | . 06773 | 37,4 | - 35049 | 87,7 | . 8532 | 71,4 |
| - 367 | - 37529 | 106,8 | .06810 | 37,5 | - 35136 | 87,7 | . 8460 | 71,0 |
| - 368 | -37635 | 106,8 | . 06848 | 37,6 | - 35224 | 87,6 | . 8390 | 70,6 |
| . 369 | - 37743 | 106,9 | . 06886 | 37,7 | -35312 | 87,5 | .8319 | 70,2 |
| 0.370 | 0.37850 | 106,9 | 1. 06923 | 37,9 | 0.35399 | 87,5 | 2.8249 | 69,8 |
| . 371 | . 37957 | 107,0 | . 06961 | 38,0 | . 35487 | 87,4 | . 8180 | 69,4 |
| . 372 | . 38064 | 107,0 | . 06999 | 38,1 | . 35574 | 87,3 | .8110 | 69,0 |
| - 373 | -38171 | 107,0 | . 07037 | 38,2 | - 35661 | 87,3 | . 8042 | 68,6 |
| - 374 | -38278 | 107, I | . 07076 | 38,3 | - 35749 | 87,2 | . 7973 | 68,2 |
| 0.375 | 0.38385 | 107, 1 | 1.07114 | 38,4 | 0.35836 | 87,2 | 2.7905 | 67,9 |
| . 376 | -38492 | 107,2 | . 07152 | 38,5 | - 35923 | 87, 1 | . 7837 | 67,5 |
| - 377 | - 38599 | 107,2 | .07191 | 38,6 | - 36010 | 87,0 | . 7770 | 67, 1 |
| -378 | -38707 | 107,2 | . 07230 | 38,7 38 | - 36007 | 87,0 | . 7703 | 66,7 |
| -379 | -388I4 | 107,3 | . 07268 | 38,8 | - 36184 | 86,9 | .7637 | 66,4 |
| 0.380 | 0.38921 | 107,3 | 1. 07307 | 38,9 | 0.36271 | 86,8 | 2.7570 | 66,0 |
| . 381 | . 39028 | 107,3 | . 07346 | 39,0 | . 36358 | 86,8 | . 7505 | 65,7 |
| - 382 | - 39136 | 107,4 | . 07385 | 39, I | - 36444 | 86,7 | . 7439 | 65,3 |
| - 383 | - 39243 | 107,4 | . 07425 | 39,2 | -3653I | 86,7 | . 7374 | 64,9 |
| -384 | -3935 | 107,5 | . 07464 | 39,4 | . 36618 | 86,6 | . 7309 | 64,6 |
| 0.385 | 0.39458 | 107,5 | 1.07503 | 39,5 | 0.36704 | 86,5 | 2.7245 | 64,2 |
| . 386 | - 39566 | 107,5 | . 07543 | 39,6 | . 36791 | 86,5 | .718I | 63,9 |
| - 387 | . 39673 | 107,6 | . 07582 | 39,7 | . 36877 | 86,4 | . 7117 | 63,5 |
| - 388 | - 39781 | 107,6 | . 07622 | 39,8 | - 36963 | 86,3 | . 7054 | 63,2 |
| - 389 | - 39889 | 107,7 | . 07662 | 39,9 | - 37050 | 86,3 | . 6991 | 62,8 |
| 0.390 | 0.39996 | 107,7 | 1.07702 | 40,0 | 0.37136 | 86,2 | 2.6928 | 62,5 |
| -391 | . 40102 | 107,7 | . 07742 | 40, 1 | - 37222 | 86, I | . 6866 | 62,2 |
| - 392 | . 40212 | 107,8 | . 07782 | 40,2 | - 37308 | 86, I | . 6804 | 61,8 |
| - 393 | . 40319 | 107,8 | . 07822 | 40,3 | - 37394 | 86,0 | . 6742 | 61,5 |
| - 394 | . 40427 | 107,9 | . 07863 | 40,4 | - 37480 | 86,0 | .6681 | 61,2 |
| 0.395 | 0.40535 | 107,9 | 1.07903 | 40,5 | 0.37566 | 85,9 | 2.6620 | 60,9 |
| . 396 | . 40643 | 107,9 | . 07944 | 40,6 | . 37652 | 85,8 | . 6559 | 60,5 |
| - 397 | . 40751 | 108,0 | . 07984 | 40,8 | . 37738 | 85,8 | . 6499 | 60,2 |
| - 398 | . 40859 | 108,0 | . 08025 | 40,9 | -37824 | 85,7 | . 6438 | 59,9 |
| -399 | . 40967 | 108, 1 | . 08066 | 41,0 | -37909 | 85,6 | . 6379 | 59,6 |
| 0.400 | 0.41075 | 108,1 | 1.08107 | 41,1 | 0.37995 | 85,6 | 2.6319 | 59,3 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd}{ }^{\circ} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{FO}^{\prime}$ |

Natural Hyperbolic Functions.

| 0 | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.400 | 0.41075 | 108, 1 | 1.08107 | 41,I | 0.37995 | 85,6 | 2.6319 | 59,3 |
| . 401 | . 41183 | 108, 1 | .08148 | 41,2 | . 38080 | 85,5 | . 6260 | 59,0 |
| . 402 | . 41292 | 108,2 | .08190 | 41,3 | . 38166 | 85,4 | . 6201 | 58,7 |
| . 403 | . 41400 | 108,2 | .0823I | 4I,4 | . 38251 | 85,4 | . 6143 | 58,3 |
| . 404 | . 41508 | 108,3 | . 08272 | 41,5 | . 38337 | 85,3 | .6085 | 58,0 |
| 0.405 | 0.41616 | 108,3 | 1.08314 | 41,6 | 0.38422 | 85,2 | 2.6027 | 57,7 |
| . 406 | . 41725 | 108,4 | . 08356 | 41,7 | . 38507 | 85,2 | . 5969 | 57,4 |
| . 407 | .41833 | 108,4 | . 08397 | 4I,8 | -38592 | 85,1 | . 5912 | 57, I |
| . 408 | . 41941 | 108,4 | . 08439 | 41,9 | . 38677 | 85,0 | . 5855 | 56,8 |
| . 409 | . 42050 | 108,5 | .0848I | 42,0 | . 38762 | 85,0 | . 5798 | 56,6 |
| 0.410 | 0.42158 | 108,5 | 1. 08523 | 42,2 | 0.38847 | 84,9 | 2.5742 | 56,3 |
| .4II | . 42267 | 108,6 | . 08566 | 42,3 | . 38932 | 84,8 | . 5686 | 56,0 |
| . 412 | . 42376 | 108,6 | . 08608 | 42,4 | . 39017 | 84,8 | . 5630 | 55,7 |
| . 413 | . 42484 | 108,7 | . 08650 | 42,5 | . 39102 | 84,7 | . 5574 | 55,4 |
| . 414 | . 42593 | 108,7 | . 08693 | 42,6 | -39186 | 84,6 | . 5519 | 55, 1 |
| 0.415 | 0.42702 | 108,7 | 1. 08736 | 42,7 | 0.39271 | 84,6 | 2.5464 | 54,8 |
| . 416 | . 42810 | 108,8 | . 08778 | 42,8 | . 39356 | 84,5 | . 5409 | 54,6 |
| .417 | . 42919 | 108,8 | . 08821 | 42,9 | . 39440 | 84,4 | . 5355 | 54,3 |
| -. 418 | . 43028 | 108,9 | . 08864 | 43,0 | . 39524 | 84,4 | . 5301 | 54,0 |
| . 419 | . 43 I 37 | 108,9 | . 08907 | 43,I | - 39609 | 84,3 | . 5247 | 53,7 |
| 0.420 | 0.43246 | 109,0 | 1. 08950 | 43,2 | 0.39693 | 84,2 | 2.5193 | 53,5 |
| . 421 | . 43355 | 109,0 | . 08994 | 43,4 | . 39777 | 84,2 | . 5140 | 53,2 |
| . 422 | . 43464 | 109,0 | . 09037 | 43,5 | . 3986 I | 84, I | . 5087 | 52,9 |
| . 423 | . 43573 | 109, I | .0908I | 43,6 | - 39945 | 84,0 | . 5034 | 52,7 |
| . 424 | - 43682 | 109, I | .09124 | 43,7 | . 40029 | 84,0 | . 4982 | 52,4 |
| 0.425 | 0.43791 | 109,2 | 1. 09168 | 43,8 | 0.40113 | 83,9 | 2.4929 | 52,2 |
| . 426 | . 43900 | 109,2 | . 09212 | 43,9 | . 40197 | 83,8 | . 4877 | 51,9 |
| . 427 | . 44009 | 109,3 | . 09256 | 44,0 | . 4028 I | 83,8 | . 4826 | 51,6 |
| . 428 | . 44119 | 109,3 | . 09300 | 44, 1 | . 40365 | 83,7 | . 4774 | 5I,4 |
| . 429 | . 44228 | 109,3 | . 09344 | 44,2 | . 40449 | 83,6 | . 4723 | 5I, I |
| 0.430 | 0.44337 | 109,4 | 1. 09388 | 44,3 | 0.40532 | 83,6 | 2.4672 | 50,9 |
| .43I | . 44447 | 109,4 | . 09433 | 44,4 | . 40616 | 83,5 | . 4621 | 50,6 |
| . 432 | . 44556 | 109,5 | . 09477 | 44,6 | . 40699 | 83,4 | . 4571 | 50,4 |
| . 433 | . 44666 | 109,5 | . 09522 | 44,7 | . 40783 | 83,4 | . 4520 | 50, I |
| . 434 | . 44775 | 109,6 | . 09567 | 44,8 | . 40866 | 83,3 | . 4470 | 49,9 |
| 0.435 | 0.44885 | 109,6 | 1.096II | 44,9 | 0.40949 | 83,2 | 2.4421 | 49,6 |
| . 436 | . 44995 | 109,7 | . 09656 | 45,0 | .41032 | 83,2 | . 4371 | 49,4 |
| . 437 | . 45104 | 109,7 | .09701 | 45, I | -4III5 | 83,1 | . 4322 | 49,2 |
| . 438 | . 45214 | 109,7 | . 09747 | 45,2 | -41199 | 83,0 | . 4273 | 48,9 |
| . 439 | . 45324 | 109,8 | . 09792 | 45,3 | . 41282 | 83,0 | . 4224 | 48,7 |
| 0.440 | 0.45434 | 109,8 | 1. 09837 | 45,4 | 0.41364 | 82,9 | 2.4175 | 48,4 |
| . 441 | . 45543 | 109,9 | . 09883 | 45,5 | . 41447 | 82,8 | . 4127 | 48,2 |
| . 442 | . 45653 | 109,9 | . 09928 | 45,7 | . 41530 | - 82,8 | . 4079 | 48,0 |
| . 443 | . 45763 | I 10,0 | . 09974 | 45,8 | .416I3 | 82,7 | . 4031 | 47,7 |
| . 444 | . 45873 | I 10,0 | . 10020 | 45,9 | . 41695 | 82,6 | . 3983 | 47,5 |
| 0.445 | 0.45983 | IIO, I | 1. 10066 | 46,0 | 0.41778 | 82,5 | 2.3936 | 47,3 |
| . . 446 | . 46093 | 110,1 | . 10112 | 46,1 | . 41861 | 82,5 | . 3889 | 47, 1 |
| . 447 | . 46204 | I 10,2 | . 10158 | 46,2 | . 41943 | 82,4 | . 3842 | 46,8 |
| . 448 | . 46314 | 110,2 110,3 | .10204 .10251 | 46,3 46,4 | . 42025 | 82,3 82,3 | . 3795 | 46,6 |
| . 449 | . 46424 | 110,3 | . 10251 | 46,4 | . 42108 | 82,3 | - 3749 | 46,4 |
| 0.450 | 0.46534 | 1 10,3 | I. 10297 | 46,5 | 0.42190 | 82,2 | 2.3702 | 46,2 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\infty \mathrm{FO}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.450 | 0.46534 | I 10,3 | I. 10297 | 46,5 | 0.42190 | 82,2 | 2.3702 | 46,2 |
| . 45 I | . 46645 | I 10,3 | . 10344 | 46,6 | . 42272 | 82,I | . 3656 | 46,0 |
| . 452 | . 46755 | I 10,4 | . 10390 | 46,8 | . 42354 | 82,I | -3610 | 45,7 |
| . 453 | . 46865 | I 10,4 | . 10437 | 46,9 | . 42436 | 82,0 | - 3565 | 45,5 |
| . 454 | . 46976 | I 10,5 | . 10484 | 47,0 | .42518 | 8I,9 | . 3519 | 45,3 |
| 0.455 | 0.47086 | I 10,5 | I. $1053 \mathrm{I}^{\prime}$ | 47,1 | 0.42600 | 81,9 | 2.3474 | 45, I |
| . 456 | . 47197 | I 10,6 | . 10578 | 47,2 | . 42682 | 81,8 | . 3429 | 44,9 |
| . 457 | . 47307 | I 10,6 | . 10625 | 47,3 | . 42764 | 81,7 | - 3384 | 44,7 |
| . 458 | . 47418 | 110,7 | . 10673 | 47,4 | . 42845 | 81,6 | - 3340 | 44,5 |
| . 459 | . 47529 | I 10,7 | . 10720 | 47,5 | . 42927 | 8ı,6 | - 3295 | 44,3 |
| 0.460 | 0.47640 | I Io,8 | 1. 10768 | 47,6 | 0.43008 | $8 \mathrm{I}, 5$ | 2.325 I | 44, I |
| . 46 I | . 47750 | I 10,8 | . 10816 | 47,8 | . 43090 | 8r,4 | . 3207 | 43,9 |
| . 462 | . 47861 | I 10,9 | . 10863 | 47,9 | . 43171 | 81,4 | - 3164 | 43,7 |
| . 463 | . 47972 | I IO,9 | . 1091 I | 48,0 | . 43253 | 8.r,3 | . 3120 | 43,5 |
| . 464 | . 48083 | I I I, 0 | . 10959 | 48, I | . 43334 | 81,2 | - 3077 | 43,3 |
| 0.465 | 0.48194 | I I 1,0 | I. 11007 | 48,2 | 0.43415 | 81,2 | 2.3033 | 43, I |
| . 466 | . 48305 | III, I | . 11056 | 48,3 | . 43496 | $8 \mathrm{I}, \mathrm{I}$ | . 2991 | 42,9 |
| . 467 | . 48416 | III, I | . IIIO4 | 48,4 | . 43577 | 81,0 | . 2948 | 42,7 |
| . 468 | . 48527 | III, 2 | . III53 | 48,5 | . 43658 | 80,9 | . 2905 | 42,5 |
| .469 | . 48638 | III,2 | . II201 | 48,6 | . 43739 | 80,9 | . 2863 | 42,3 |
| 0.470 | 0.48750 | III,2 | I. II250 | 48,7 | 0.43820 | 80,8 | 2.2821 | 42, I |
| . 471 | . 48861 | III, 3 | . I I299 | 48,9 | . 43901 | 80,7 | . 2779 | 41,9 |
| . 472 | . 48972 | I II, 3 | . II 348 | 49,0 | . 43981 | 80,7 | . 2737 | 41,7 |
| . 473 | . 49084 | III, 4 | . II 397 | 49, I | . 44062 | 80,6 | . 2695 | 4I,5 |
| . 474 | . 49195 | III, 4 | . I 1446 | 49,2 | . 44143 | 80,5 | . 2654 | 4I,3 |
| 0.475 | 0.49306 | II I, 5 | I. I I495 | 49,3 | 0.44223 | 80,4 | 2.2613 | 4I, I |
| . 476 | . 49418 | III,5 | . II 544 | 49,4 | . 44303 | 80,4 | . 2572 | 40,9 |
| . 477 | . 49530 | III, 6 | . I I 594 | 49,5 | . 44384 | 80,3 | . 253 I | 40,8 |
| . 478 | . 49641 | III, 6 | . II643 | 49,6 | . 44464 | 80,2 | . 2490 | 40,6 |
| . 479 | . 49753 | I I I,7 | . I I693 | 49,8 | . 44544 | 80,2 | . 2450 | 40,4 |
| 0.480 | 0.49865 | III,7 | I. II743 | 49,9 | 0.44624 | 80,1 | 2.2409 | 40,2 |
| .48I | . 49976 | III, 8 | . II793 | 50,0 | . 44704 | 80,0 | . 2369 | 40,0 |
| . 482 | . 50088 | I I I , 8 | . I I843 | 50,1 | . 44784 | 79,9 | . 2329 | 39,9 |
| . 483 | . 50200 | II I, 9 | . 11893 | 50,2 | . 44864 | 79,9 | . 2289 | 39,7 |
| . 484 | . 50312 | II I,9 | . 11943 | 50,3 | . 44944 | 79,8 | . 2250 | 39,5 |
| 0.485 | 0.50424 | I 12,0 | I. 11994 | 50,4 | 0.45024 | 79,7 | 2.2210 | 39,3 |
| . 486 | . 50536 | I 12,0 | . 12044 | 50,5 | .45104 | 79,7 | . 2171 | 39,2 |
| . 487 | . 50648 | I12, 1 | . 12095 | 50,6 | . 45183 | 79,6 | . 2132 | 39,0 |
| . 488 | . 50760 | 112,1 | . 12145 | 50,8 | .45263 | 79,5 | . 2093 | 38,8 |
| .489 | . 50872 | I 12,2 | . 12196 | 50,9 | . 45342 | 79,4 | . 2054 | 38,6 |
| 0.490 | 0.50984 | I 1 2,2 | I. I2247 | 51,0 | 0.45422 | 79,4 | 2.2016 | 38,5 |
| . 49 I | . 51097 | 1 12,3 | . 12298 | 5I, I | . 45501 | 79,3 | . 1978 | 38,3 |
| . 492 | . 51209 | 112,3 | . 12349 | 51,2 | . 45580 | 79,2 | . 1939 | 38, |
| . 493 | . 51321 | I 12,4 | . 12401 | 51,3 | . 45659 | 79,2 | . 1901 | 38,0 |
| . 494 | . 51434 | I 12,5 | . 12452 | 5I,4 | . 45739 | 79, I | . 1863 | 37,8 |
| 0.495 | 0.51546 | I I2,5 | I. 12503 | 51,5 | 0.45818 | 79,0 | 2. 1826 | 37,6 |
| . 495 | . 51659 | I 12,6 | . 12555 | 51,7 | . 45897 | 78,9 | . I788 | 37,5 |
| . 497 | .51771 | I I 2,6 | . 12607 | 51,8 | . 45975 | 78,9 | . I7,5I | 37,3 |
| . 498 | . 51884 | I12,7 | . 12659 | 51,9 | . 46054 | 78,8 | . 1714 | 37, I |
| . 499 | . 51997 | I 12,7 | . 127 II | 52,0 | .46133 | 78,7 | . 1676 | 37,0 |
| 0.500 | 0.52110 | I 12,8 | 1. 12763 | 52, I | 0.46212 | 78,6 | 2.1640 | 36,8 |
|  | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| 4 | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.500 | 0.52110 | I I 2,8 | 1. 12763 | 52,I | 0.46212 | 78,6 | 2.1640 | 36,8 |
| . 501 | . 52222 | I I2,8 | . 12815 | 52,2 | . 46290 | 78,6 | . 1603 | 36,7 |
| . 502 | . 52335 | I I2,9 | . 12867 | 52,3 | . 46369 | 78,5 | . 1566 | 36,5 |
| . 503 | . 52448 | I I2,9 | . 12919 | 52,4 | . 46447 | 78,4 | . 1530 | 36,4 |
| . 504 | . 5256 I | I I3,0 | . 12972 | 52,6 | . 46526 | 78,4 | . I493 | 36,2 |
| 0.505 | 0.52674 | II3,0 | I.I3025 | 52,7 | 0.46604 | 78,3 | 2. 1457 | 36,0 |
| . 506 | . 52787 | II3, I | . 13077 | 52,8 | . 46682 | 78,2 | . 1421 | 35,9 |
| . 507 | . 52900 | II3, I | . 13130 | 52,9 | . 46760 | 78, I | . 1386 | 35,7 |
| . 508 | . 53013 | II3,2 | .13183 | 53,0 | . 46839 | 78, | . 1350 | 35,6 |
| . 509 | . 53127 | II3,2 | . 13236 | 53, I | . 46917 | 78,0 | .13I4 | 35,4 |
| 0.510 | 0.53240 | 113,3 | I. 13289 | 53,2 | 0.46995 | 77,9 | 2. 1279 | 35,3 |
| . 5II | . 53353 | II3,3 | . I3343 | 53,4 | . 47072 | 77,9 | . 1244 | 35, I |
| . 512 | . 53466 | II3,4 | . 13396 | 53,5 | . 47150 | 77,8 | . 1209 | 35,0 |
| . 513 | . 53580 | II3,4 | . I3450 | 53,6 | . 47228 | 77,7 | . II74 | 34,8 |
| . 514 | . 53693 | I 1 3,5 | . 13503 | 53,7 | . 47306 | 77,6 | . II39 | 34,7 |
| 0.515 | 0.53807 | I 13,6 | I. I3557 | 53,8 | 0.47383 | 77,5 | 2.1105 | 34,5 |
| .516 | . 53920 | II3,6 | . 13611 | 53,9 | . 47461 | 77,5 | . 1070 | 34,4 |
| . 517 | . 54034 | I 13,7 | . I3665 | 54,0 | . 47538 | 77,4 | . 1036 | 34,3 |
| . 518 | . 54148 | I 13,7 | . 13719 | 54, I | . 47615 | 77,3 | . 1002 | 34,1 |
| . 519 | . 54262 | I I 3,8 | . 13773 | 54,3 | . 47693 | 77,3 | . 0968 | 34,0 |
| 0.520 | 0.54375 | 113,8 | I. 13827 | 54,4 | 0.47770 | 77,2 | 2.0934 | 33,8 |
| . 52 I | . 54489 | I 13,9 | . 13882 | 54,5 | . 47847 | 77, 1 | . 0900 | 33.7 |
| . 522 | . 54603 | I 1 3,9 | . I3936 | 54,6 | . 47924 | 77,0 | . 0866 | 33,5 |
| . 523 | . 54717 | I I4, 0 | . I3991 | 54,7 | . 48001 | 77,0 | . 0833 | 33,4 |
| . 524 | . 54831 | I 14,0 | . 14046 | 54,8 | . 48078 | 76,9 | . 0799 | 33,3 |
| 0.52 .5 | 0.54945 | II4, I | 1.14101 | 54,9 | 0.48155 | 76,8 | 2.0766 | 33, I |
| . 526 | . 55059 | II 4,2 | . 14156 | 55, I | . 48232 | 26,7 | . 0733 | 33,0 |
| . 527 | . 55173 | I I 4,2 | . 14211 | 55,2 | . 48308 | 76,7 | . 0700 | 32,9 |
| . 528 | . 55288 | II4,3 | . I4266 | 55,3 | . 48385 | 76,6 | . 0668 | 32,7 |
| . 529 | . 55402 | II4,3 | . I432I | 55,4 | . 48462 | 76,5 | . 0635 | 32,6 |
| 0.530 | 0.55516 | II4,4 | I. 14377 | 55,5 | 0.48538 | 76,4 | 2.0602 | 32,4 |
| . 53 I | . 5563 I | II 4,4 | . 14432 | 55,6 | . 48615 | 76,4 | . 0570 | 32,3 |
| . 532 | . 55745 | II4,5 | . 14488 | 55,7 | . 48691 | 76,3 | . 0538 | 32,2 |
| . 533 | . 55860 | II 4,5 | . 14544 | 55,9 | . 48767 | 76,2 | . 0506 | 32,0 |
| . 534 | . 55974 | I 14,6 | . 14600 | 56,0 | . 48843 | 76, 1 | . 0474 | 31,9 |
| 0.535 | 0.56089 | I 14,7 | 1. 14656 | 56, I | 0.48919 | 76, | 2.0442 | 31,8 |
| . 536 | . 56204 | 114,7 | . 14712 | 56,2 | . 48995 | 76,0 | . 0410 | $3 \mathrm{I}, 7$ |
| . 537 | . 56318 | I 14,8 | . 14768 | 56,3 | . 49071 | 75,9 | . 0378 | 3I,5 |
| . 538 | . 56433 | I I 4,8 | . 14825 | 56,4 | . 49147 | 75,8 | . 0347 | $3 \mathrm{I}, 4$ |
| . 539 | . 56548 | I I4,9 | . 1488 I | 56,5 | . 49223 | 75,8 | . 0316 | 3I,3 |
| 0.540 | 0.56663 | I I4,9 | I. 14938 | 56,7 | 0.49299 | 75,7 | 2.0284 | 3I, 1 |
| . 541 | . 56778 | I I 5,0 | . 14994 | 56,8 | . 49374 | 75,6 | . 0253 | $3 \mathrm{I}, 0$ |
| . 542 | . 56893 | II5, I | . 15051 | 56,9 | . 49450 | 75,5 | . 0222 | 30,9 |
| . 543 | . 57008 | II5, I | . 15108 | 57,0 | . 49526 | 75,5 | . 0192 | 30,8 |
| . 544 | . 57123 | II 5,2 | . 15165 | 57, I | . 49601 | 75,4 | . 0161 | 30,6 |
| 0.545 | 0.57238 | I 15,2 | I. I5223 | 57,2 | 0.49676 | 75,3 | 2.0130 | 30,5 |
| . 546 | . 57354 | I I 5,3 | . 15280 | 57,4 | . 49752 | 75,2 | . 0100 | 30,4 |
| . 547 | . 57469 | II 5,3 | . 15337 | 57,5 | . 49827 | 75,2 | . 0070 | 30,3 |
| - 548 | . 57584 | I I 5,4 | . 15395 | 57,6 | . 49902 | 75, 1 | . 0039 | 30,2 |
| . 549 | . 57700 | I 15,5 | . 15452 | 57,7 | . 49977 | 75,0 | . 0009 | 30,0 |
| 0.550 | 0.578I5 | I 15,5 | I. 15510 | 57,8 | 0.50052 | 74,9 | 1. 9979 | 29,9 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega$ Fo' |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\circ}$ | $\boldsymbol{t a n h} u$ | a $\mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.550 | 0.57815 | II5,5 | I. 15510 | 57,8 | 0.50052 | 74,9 | 1. 9979 | 29,9 |
| . 551 | . 57931 | I I 5,6 | . 15568 | 57,9 | . 50127 | 74,9 | . 9949 | 29,8 |
| . 552 | . 58046 | I I 5,6 | . 15626 | 58,0 | . 50202 | 74,8 | . 9920 | 29,7 |
| . 553 | . 58162 | I 15,7 | . 15684 | 58,2 | . 50277 | 74,7 | . 9890 | 29,6 |
| . 554 | . 58278 | II5,7 | . 15742 | 58,3 | . 5035 I | 74,6 | . 9860 | 29,4 |
| 0.555 | 0.58393 | II 5,8 | I. 15801 | 58,4 | 0.50426 | 74,6 | r.983I | 29,3 |
| . 556 | . 58509 | I 15,9 | . 15859 | 58,5 | . 50500 | 74,5 | . 9802 | 29,2 |
| . 557 | . 58625 | I 15,9 | . 15918 | 58,6 | . 50575 | 74,4 | . 9773 | 29, I |
| . 558 | . 58741 | I 16,0 | . 15976 | 58,7 | . 50649 | 74,3 | . 9744 | 29,0 |
| . 559 | . 58857 | I 16,0 | . 16035 | 58,9 | . 50724 | 74,3 | .9715 | 28,9 |
| 0.560 | 0.58973 | 116, 1 | 1. 16094 | 59,0 | 0.50798 | 74,2 | 1.9686 | 28,8 |
| . 561 | . 59089 | II6,2 | . 16I53 | 59, I | . 50872 | 74, I | . 9657 | 28,6 |
| . 562 | . 59205 | I 16,2 | . 16.212 | 59,2 | . 50946 | 74,0 | . 9629 | 28,5 |
| . 563 | . 59322 | 1 16,3 | . 16272 | 59,3 | . 51020 | 74,0 | . 9600 | 28,4 |
| . 564 | . 59438 | 116,3 | . 1633 I | 59,4 | . 5 Ir994 | 73,9 | . 9572 | 28,3 |
| 0.565 | 0.59554 | II6,4 | 1. 16390 | 59,6 | 0.51168 | 73,8 | I. 9544 | 28,2 |
| . 566 | . 59671 | 116,5 | . 16450 | 59,7 | . 51242 | 73,7 | . 9515 | 28, I |
| . 567 | . 59787 | I 16,5 | . 16510 | 59,8 | . 51315 | 73,7 | . 9487 | 28,0 |
| . 568 | . 59904 | I 16,6 | . 16570 | 59,9 | . 51389 | 73,6 | . 9459 | 27,9 |
| . 569 | . 60020 | I 16,6 | . 16630 | 60,0 | . 51462 | 73,5 | . 9432 | 27,8 |
| 0.570 | 0.60137 | 1 16,7 | 1. 16690 | 60, 1 | 0.51536 | 73,4 | 1.9404 | 27,7 |
| . 571 | . 60254 | 116,7 | . 16750 | 60,3 | . 51609 | 73,4 | . 9376 | 27,5 |
| . 572 | . 60371 | I 16,8 | . 16810 | 60,4 | . 51683 | 73,3 | . 9349 | 27,4 |
| . 573 | . 60487 | 1 16,9 | . 16871 | 60,5 | . 51756 | 73,2 | .932I | 27,3 |
| . 574 | . 60604 | 116,9 | . 16931 | 60,6 | . 51829 | 73, 1 | . 9294 | 27,2 |
| 0.575 | 0.60721 | II7,0 | 1. 16992 | 60,7 | 0.51902 | 73,1 | I. 9267 | 27, I |
| . 576 | . 60838 | II7, I | . 17053 | 60,8 | . 51975 | 73,0 | . 9240 | 27,0 |
| . 577 | . 60955 | II7, I | . I7113 | 6I,O | . 52048 | 72,9 | .9213 | 26,9 |
| . 578 | . 61073 | II7,2 | .17174 | 6I, I | . 52121 | 72,8 | . 9186 | 26,8 |
| . 579 | .6ı190 | II7,2 | . 17236 | 61,2 | . 52194 | 72,8 | .9159 | 26,7 |
| 0.580 | 0.61307 | 117,3 | 1. 17297 | 6I,3 | 0.52267 | 72,7 | I.9133 | 26,6 |
| . 58 I | .6I424 | II7,4 | . 17358 | 6I,4 | . 52339 | 72,6 | .9106 | 26,5 |
| . 582 | . 61542 | II7,4 | . 17420 | 6I,5 | . 52412 | 72,5 | . 9080 | 26,4 |
| . 583 | . 61659 | II7,5 | . 17481 | 61,7 | . 52484 | 72,5 | . 9053 | 26,3 |
| . 584 | .61777 | I 77.5 | . 17543 | 6r,8 | . 52557 | 72,4 | . 9027 | 26,2 |
| 0.585 | 0.61894 | 117,6 | 1. 17605. | 6I,9 | 0.52629 | 72,3 | 1.900I | 26, I |
| . 586 | . 62012 | II7,7 | . I7667 | 62,0 | . 52701 | 72,2 | . 8975 | 26,0 |
| . 587 | . 62130 | 117,7 | . 17729 | 62,1 | . 52773 | 72,2 | . 8949 | 25,9 |
| . 588 | . 62247 | I I 7,8 | . 17791 | 62,2 | . 52846 | 72,1 | . 8923 | 25,8 |
| . 589 | . 62365 | I 17,9 | . 17853 | 62,4 | . 52918 | 72,0 | . 8897 | 25,7 |
| 0.590 | 0.62483 | I 17,9 | 1.17916 | 62,5 | 0.52990 | 71,9 | 1. 8872 | 25,6 |
| . 591 | . 62601 | 1 18,0 | . 17978 | 62,6 | . 53051 | 71,8 | . 8846 | 25,5 |
| . 592 | . 62719 | I 18,0 | . 18041 | 62,7 | . 53133 | 71,8 | .882I | 25,4 |
| . 593 | . 62837 | I I8, I | . 18104 | 62,8 | . 53205 | 71,7 | . 8795 | 25,3 |
| . 594 | . 62955 | II8,2 | . 18167 | 63,0 | . 53277 | 71,6 | . 8770 | 25,2 |
| 0.595 | 0.63073 | 118,2 | I. 18230 | 63,1 | 0.53348 | 71,5 | 1. 8745 | 25, I |
| . 596 | . 63192 | I 18,3 | . 18293 | 63,2 | . 53420 | 71,5 | . 8720 | 25,0 |
| . 597 | . 63310 | II8,4 | . 18356 | 63,3 | . 53491 | 71,4 | . 8695 | 24,9 |
| . 598 | . 63428 | I 18,4 | . 18419 | 63,4 | . 53562 | 71,3 | . 8670 | 24,9 |
| . 599 | . 63547 | I 18,5 | . 18483 | 63,5 | . 53634 | 71,2 | . 8645 | 24,8 |
| 0.600 | 0.63665 | I 18,5 | I. 18547 | 63,7 | 0.53705 | 71,2 | 1. 8620 | 24,7 |
| $u$ | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n}$ gd u | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

## Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\text {d }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{Fo}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.600 | 0.63665 | I18,5 | I. 18547 | 63,7 | 0.53705 | 71,2 | 1.8620 | 24,7 |
| . 601 | . 63784 | 118,6 | . 18610 | 63,8 | . 53776 | 71,1 | . 8596 | 24,6 |
| . 602 | . 63903 | 118,7 | . 18674 | 63,9 | . 53847 | 71,0 | . 8571 | 24,5 |
| . 603 | . 64021 | 118,7 | . 18738 | 64,0 | . 53918 | 70,9 | . 8547 | 24,4 |
| . 604 | . 64140 | II8,8 | . 18802 | 64, I | . 53989 | 70,9 | . 8522 | 24,3 |
| 0.605 | 0.64259 | 118,9 | 1. 18866 | 64,3 | 0. 54060 | 70,8 | 1.8498 | 24,2 |
| . 606 | . 64378 | 118,9 | . 18931 | 64,4 | . 5413 I | 70,7 | . 8474 | 24,1 |
| . 607 | . 64497 | 119,0 | . 18995 | 64,5 | . 54201 | 70,6 | . 8450 | 24,0 |
| . 608 | . 64616 | 119, I | . 19060 | 64,6 | . 54272 | 70,5 | . 8426 | 24,0 |
| . 609 | . 64735 | II9, I | . 19124 | 64,7 | - 54342 | 70,5 | . 8402 | 23,9 |
| 0.610 | 0.64854 | 119,2 | 1. 19189 | 64,9 | 0.54413 | 70,4 | 1.8378 | 23,8 |
| . 611 | . 64973 | 119,3 | . 19254 | 65,0 | . 54483 | 70,3 | . 8354 | 23,7 |
| . 612 | . 65093 | 119,3 | . 19319 | 65,1 | . 54553 | 70,2 | . 833 I | 23,6 |
| . 613 | . 65212 | 119,4 | . 19384 | 65,2 | - 54624 | 70,2 | . 8307 | 23,5 |
| . 614 | . 65331 | 119,4 | . 19449 | 65,3 | . 54694 | 70,1 | . 8284 | 23,4 |
| 0.615 | 0.65451 | 119,5 | 1. 19515 | 65,5 | 0. 54764 | 70,0 | 1.8260 | 23,3 |
| . 616 | . 65570 | 119,6 | . 19580 | 65,6 | . 54834 | 69,9 | . 8237 | 23,3 |
| . 617 | . 65690 | 119,6 | . 19646 | 65,7 | . 54904 | 69,9 | . 8214 | 23,2 |
| . 618 | .65810 | 119,7 | . 19712 | 65,8 | . 54973 | 69,8 | .8191 | 23,1 |
| . 619 | . 65929 | 119,8 | . 19778 | 65,9 | - 55043 | 69,7 | .8168 | 23,0 |
| 0.620 | 0.66049 | 119,8 | I. 19844 | 66,0 | 0.55113 | 69,6 | 1.8145 | 22,9 |
| . 621 | . 66169 | 119,9 | . 19910 | 66,2 | . 55182 | 69,5 | .8122 | 22,8 |
| . 622 | . 66289 | 120,0 | . 19976 | 66,3 | . 55252 | 69,5 | . 8099 | 22,8 |
| . 623 | . 66409 | 120,0 | . 20042 | 66,4 | . 55321 | 69,4 | . 8076 | 22,7 |
| . 624 | . 66529 | 120,1 | . 20109 | 66,5 | . 55391 | 69,3 | . 8054 | 22,6 |
| 0.625 | 0.66649 | 120,2 | 1.20175 | 66,6 | 0.55460 | 69,2 | 1.8031 | 22,5 |
| . 626 | . 66769 | 120,2 | . 20242 | 66,8 | . 55529 | 69,2 | . 8009 | 22,4 |
| . 627 | . 66890 | 120,3 | . 20309 | 66,9 | . 55598 | 69,1 | . 7986 | 22,4 |
| . 628 | . 67010 | 120,4 | . 20376 | 67,0 | . 55667 | 69,0 68,0 | . 7964 | 22,3 |
| . 629 | . 67130 | 120,4 | . 20443 | 67,I | . 55736 | 68,9 | . 7942 | 22,2 |
| 0.630 | 0.67251 | 120,5 | 1. 20510 | 67,3 | 0.55805 | 68,9 | 1.7919 | 22,1 |
| . 631 | . 67371 | 120,6 | . 20577 | 67,4 | . 55874 | 68,8 | . 7897 | 22,0 |
| . 632 | . 67492 | 120,6 | . 20645 | 67,5 | . 55943 | 68,7 | . 7875 | 22,0 |
| . 633 | . 67613 | 120,7 | . 20712 | 67,6 | . 56011 | 68,6 | . 7853 | 21,9 |
| . 634 | . 67734 | 120,8 | . 20780 | 67,7 | . 56080 | 68,6 | . 7832 | 21,8 |
| 0.635 | 0.67854 | 120,8 | 1. 20848 | 67,9 | 0. 56149 | 68,5 | 1.7810 | 21,7 |
| . 636 | . 67975 | 120,9 | . 20916 | 68,0 | . 56217 | 68,4 | . 7788 | 21,6 |
| . 637 | . 68096 | 121,0 | . 20984 | 68,1 | . 56285 | 68,3 | . 7767 | 21,6 |
| . 638 | . 68217 | 121,1 | . 21052 | 68,2 | . 56354 | 68,2 | .7745 | 21,5 |
| . 639 | . 68338 | 121,1 | . 21120 | 68,3 | . 56422 | 68,2 | . 7724 | 21,4 |
| 0.640 | 0.68459 | 121,2 | 1. 21189 | 68,5 | 0. 56490 | 68,1 | 1.7702 | 21,3 |
| . 641 | . 6858 I | 121,3 | . 21257 | 68,6 | . 56558 | 68,0 | .7681 | 21,3 |
| . 642 | . 68702 | 121,3 | . 21326 | 68,7 | . 56626 | 67,9 | . 7660 | 21,2 |
| . 643 | . 68823 | 121,4 | . 21395 | 68,8 | . 56694 | 67,9 | . 7639 | 21,1 |
| . 644 | . 68945 | 121,5 | . 21463 | 68,9 | . 56762 | 67,8 | .7618 | 21,0 |
| 0.645 | 0.69066 | 121,5 | I. 21532 | 69,1 | 0.56829 | 67,7 | 1.7597 | 21,0 |
| . 646 | . 69188 | 121,6 | . 21602 | 69,2 | . 56897 | 67,6 | . 7576 | 20,9 |
| . 647 | . 69309 | 121,7 | . 21671 | 69,3 | . 56965 | 67,6 | . 7555 | 20,8 |
| . 648 | . 69431 | 121,7 | . 21740 | 69,4 | . 57032 | 67,5 | . 7534 | 20,7 |
| . 649 | . 69553 | 121,8 | . 21810 | 69,6 | . 57100 | 67,4 | .7513 | 20,7 |
| 0.650 | 0.69675 | 121,9 | 1.21879 | 69,7 | 0.57167 | 67,3 | 1.7493 | 20,6 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega^{\text {F }}{ }_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | csc gd u. | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\text {g }}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.650 | 0.69675 | 121,9 | 1. 21879 | 69,7 | 0.57167 | 67,3 | 1.7493 | 20,6 |
| .65I | . 69797 | 121,9 | . 21949 | 69,8 | . 57234 | 67,2 | . 7472 | 20,5 |
| . 652 | . 69919 | 122,0 | . 22019 | 69,9 | . 57301 | 67,2 | . 7452 | 20,5 |
| . 653 | . 7004 I | 122, I | . 22089 | 70,0 | . 57369 | 67, 1 | . 7431 | 20,4 |
| . 654 | . 70163 | 122,2 | . 22159 | 70,2 | . 57436 | 67,0 | .74II | 20,3 |
| 0.655 | 0.70285 | 122,2 | I. 22229 | 70,3 | 0.57503 | 66,9 | I. 7391 | 20,2 |
| . 656 | . 70407 | 122,3 | . 22300 | 70,4 | . 57570 | 66,9 | . 7370 | 20,2 |
| . 657 | . 70530 | I22,4 | . 22370 | 70,5 | . 57636 | 66,8 | . 7350 | 20,1 |
| . 658 | . 70652 | 122,4 | . 22441 | 70,7 | . 57703 | 66,7 | . 7330 | 20,0 |
| . 659 | . 70775 | I22,5 | . 225 II | 70,8 | . 57770 | 66,6 | . 7310 | 20,0 |
| 0.660 | 0.70897 | 122,6 | 1.22582 | 70,9 | 0.57836 | 66,5 | 1.7290 | 19,9 |
| . 661 | . 71020 | 122,7 | . 22653 | 71,0 | . 57903 | 66,5 | . 7270 | 19,8 |
| . 662 | .71142 | 122,7 | . 22724 | 71,1 | . 57969 | 66,4 | . 7251 | 19,8 |
| . 663 | . 71265 | 122,8 | . 22795 | 71,3 | . 58036 | 66,3 | . 723 I | 19,7 |
| . 664 | . 71388 | 122,9 | . 22867 | 71,4 | . 58102 | 66,2 | .72II | 19,6 |
| 0.665 | 0.71511 | 122,9 | 1.22938 | 71,5 | 0.58168 | 66,2 | 1.7192 | 19,6 |
| . 666 | . 71634 | I23,0 | . 23010 | 71,6 | . 58234 | 66,1 | . 7172 | 19,5 |
| . 667 | . 71757 | I23, I | . 2308 I | 71,8 | . 58300 | 66,0 | . 7153 | 19,4 |
| . 668 | . 71880 | 123,2 | . 23153 | 71,9 | . 58366 | 65,9 | . 7133 | 19,4 |
| . 669 | . 72003 | 123,2 | . 23225 | 72,0 | . 58432 | 65,9 | .7114 | 19,3 |
| 0.670 | 0.72126 | 123,3 | 1. 23297 | 72,I | 0.58498 | 65,8 | 1. 7095 | 19,2 |
| .671 | . 72250 | 123,4 | . 23369 | 72,2 | . 58564 | 65,7 | . 7075 | 19,2 |
| . 672 | . 72373 | 123,4 | . 23442 | 72,4 | . 58629 | 65,6 | . 7056 | 19, I |
| . 673 | . 72497 | 123,5 | . 23514 | 72,5 | . 58695 | 65,5 | . 7037 | 19,0 |
| . 674 | . 72620 | 123,6 | . 23587 | 72,6 | . 58760 | 65,5 | . 7018 | 19,0 |
| 0.675 | 0.72744 | 123,7 | I. 23659 | 72,7 | 0.58826 | 65,4 | 1. 6999 | 18,9 |
| . 676 | . 72868 | 123,7 | . 23732 | 72,9 | . 5889 I | 65,3 | . 6980 | 18,8 |
| . 677 | . 72991 | 123,8 | . 23805 | 73,0 | . 58957 | 65,2 | . 6962 | 18,8 |
| . 678 | .73115 | 123,9 | . 23878 | 73, I | . 59022 | 65,2 | . 6943 | 18,7 |
| . 679 | . 73239 | 124,0 | . 23951 | 73,2 | . 59087 | 65, 1 | . 6924 | 18,6 |
| 0.680 | 0.73363 | 124,0 | I. 24025 | 73,4 | 0.59152 | 65,0 | 1. 6906 | 18,6 |
| .681 | . 73487 | 124, I | . 24098 | 73,5 | . 59217 | 64,9 | . 6887 | 18,5 |
| . 682 | . 73611 | I24,2 | . 24172 | 73,6 | . 59282 | 64,9 | . 6869 | 18,5 |
| . 683 | . 73735 | I24,2 | . 24245 | 73,7 | . 59347 | 64,8 | . 6850 | 18,4 |
| . 684 | . 73860 | I24,3 | . 24319 | 73,9 | . 594 II | 64,7 | . 6832 | 18,3 |
| 0.685 | 0.73984 | 124,4 | I. 24393 | 74,0 | 0.59476 | 64,6 | I. 6813 | 18,3 |
| . 686 | .74109 | 124,5 | . 24467 | 74, I | . 5954 I | 64,5 | . 6795 | 18,2 |
| . 687 | . 74233 | 124,5 | . 2454 I | 74,2 | . 59605 | 64,5 | . 6777 | 18, 1 |
| . 688 | . 74358 | 124,6 | . 24616 | 74,4 | . 59670 | 64,4 | . 6759 | 18, 1 |
| . 689 | . 74482 | 124,7 | . 24690 | 74,5 | . 59734 | 64,3 | . 6741 | 18,0 |
| 0.690 | 0.74607 | 124,8 | 1.24765 | 74,6 | 0.59798 | 64,2 | 1.6723 | 18,0 |
| . 691 | . 74732 | 124,8 | . 24839 | 74,7 | . 59862 | 64,2 | . 6705 | 17,9 |
| . 692 | . 74857 | 124,9 | . 24914 | 74,9 | . 59927 | 64,1 | . 6687 | I7,8 |
| . 693 | . 74982 | 125,0 | . 24989 | 75,0 | . 5999 I | 64,0 | . 6669 | I7,8 |
| . 694 | . 75107 | I25, I | . 25064 | 75, 1 | .60055 | 63,9 | . 6652 | 17,7 |
| 0.695 | 0.75232 | 125, I | 1.25139 | 75,2 | 0.60118 | 63,9 | I. 6634 | 17,7 |
| . 696 | . 75357 | 125,2 | . 25214 | 75,4 | . 60182 | 63,8 | . 6616 | 17,6 |
| . 697 | . 75482 | 125,3 | . 25290 | 75,5 | . 60246 | 63,7 | . 6599 | 17,6 |
| . 698 | . 75607 | I25,4 | . 25365 | 75,6 | .60310 | 63,6 | .6581 | I7,5 |
| . 699 | . 75733 | 125,4 | . 2544 I | 75,7 | . 60373 | 63,6 | . 6564 | 17,4 |
| 0.700 | 0.75858 | 125,5 | 1.25517 | 75,9 | 0.60437 | 63,5 | I. 6546 | 17,4 |
| 4 | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.700 | 0.75858 | 125,5 | 1.25517 | 75,9 | 0.60437 | 63,5 | 1. 6546 | 17,4 |
| .701 | . 75984 | 125,6 | . 25593 | 76,0 | . 60500 | 63,4 | . 6529 | 17,3 |
| . 702 | .76i 10 | 125,7 | . 25669 | 76,1 | . 60.564 | 63,3 | . 6512 | 17,3 |
| . 703 | . 76235 | 125,7 | . 25745 | 76,2 | . 60627 | 63,2 | . 6494 | 17,2 |
| . 704 | . 76361 | 125,8 | . 2582 I | 76,4 | . 60690 | 63,2 | . 6477 | I7,1 |
| 0.705 | 0.76487 | 125,9 | 1. 25898 | 76,5 | 0.60753 | 63,1 | 1.6460 | 17,I |
| . 706 | .766I3 | 126,0 | . 25974 | 76,6 | . 60816 | 63,0 | . 6443 | 17,0 |
| . 707 | .76739 | 126, I | . 26051 | 76,7 | . 60879 | 62,9 | . 6426 | 17,0 |
| . 708 | . 76855 | 126,1 | . 26128 | 76,9 | . 60942 | 62,9 | . 6409 | 16,9 |
| . 709 | . 76991 | 126,2 | . 26205 | 77,0 | . 61005 | 62,8 | . 6392 | 16,9 |
| 0.710 | 0.77117 | 126,3 | 1. 26282 | 77,I | 0.61068 | 62,7 | 1. 6375 | 16,8 |
| . 711 | . 77244 | 126,4 | . 206359 | 77,2 | .61130 | 62,6 | . 6358 | 16,8 |
| . 712 | . 77370 | 126,4 | . 26436 | 77,4 | .61193 | 62,6 | . 6342 | 16,7 |
| . 713 | . 77497 | 126,5 | . 26514 | 77,5 | . 61255 | 62,5 | . 6325 | 16,7 |
| . 714 | . 77623 | 126,6 | . 26591 | 77,6 | . 61318 | 62,4 | . 6308 | 16,6 |
| 0.715 | 0.77750 | 126,7 | 1. 26669 | 77,7 | 0.61380 | 62,3 | 1. 6292 | 16,5 |
| . 716 | . 77876 | 126,7 | . 26747 | 77,9 | .61443 | 62,2 | . 6275 | 16,5 |
| . 717 | . 78003 | 126,8 | . 26825 | 78,0 | . 61505 | 62,2 | . 6259 | 16,4 |
| . 718 | .78130 | 126,9 | . 26903 | 78, 1 | . 61567 | 62,1 | . 6242 | 16,4 |
| . 719 | . 78257 | 127,0 | . 26981 | 78,3 | . 61629 | 62,0 | . 6226 | 16,3 |
| 0.720 | 0.78384 | 127, I | 1.27059 | 78,4 | 0.61691 | 6I,9 | 1.6210 | 16,3 |
| . 721 | . 78511 | 127, I | . 27138 | 78,5 | . 61753 | 61,9 | .6194 | 16,2 |
| . 722 | . 78538 | 127,2 | . 27216 | 78,6 | .61815 | 6I,8 | . 6177 | 16,2 |
| . 723 | . 78766 | 127,3 | . 27295 | 78,8 | . 61876 | 6I,7 | . 6161 | 16, |
| . 724 | . 78893 | 127,4 | . 27374 | 78,9 | .6I938 | 6I,6 | . 6145 | 16, 1 |
| 0.725 | 0.79020 | 127,5 | 1. 27453 | 79,0 | 0.62000 | 6I,6 | 1.6129 | 16,0 |
| . 726 | . 79148 | 127,5 | . 27532 | 79, 1 | .6206r | 6r,5 | .6Ir3 | 16,0 |
| . 727 | . 79275 | 127,6 | .276II | 79,3 | . 62123 | 6I,4 | .6097 | 15,9 |
| . 728 | . 79403 | 127,7 | . 27690 | 79,4 | . 62184 | 6I,3 | . 608I | 15,9 |
| . 729 | .79531 | 127,8 | . 27770 | 79,5 | . 62245 | 61,3 | . 6065 | 15,8 |
| 0.730 | 0.79659 | 127,8 | 1.27849 | 79,7 | 0.62307 | 61,2 | 1. 6050 | 15,8 |
| .73I | . 79786 | 127,9 | . 27929 | 79,8 | . 62368 | 6I, | . 6034 | 15,7 |
| . 732 | . 79914 | 128,0 | . 28009 | 79,9 | . 62429 | 61,0 | . 6018 | 15,7 |
| . 733 | . 80042 | 128, I | . 28089 | 80,0 | . 62.490 | 61,0 | . 6003 | 15,6 |
| . 734 | . 80171 | 128,2 | .28169 | 80,2 | . 6255 I | 60,9 | . 5987 | 15,6 |
| 0.735 | 0.80299 | 128,2 | I. 28249 | 80,3 | 0.626 II | 60,8 | 1.5972 | 15,5 |
| . 736 | . 80.427 | 128,3 | . 28330 | 80,4 | . 62672 | 60,7 | . 5956 | 15,5 |
| . 737 | . 80555 | 128,4 | .28410 | 80,6 | . 62733 | 60,6 | . 5941 | 15,4 |
| . 738 | . 80684 | 128.5 | .28491 | 80,7 | . 62794 | 60,6 | . 5925 | 15,4 |
| . 739 | .80812 | 128,6 | . 28572 | 80,8 | .62854 | 60,5 | . 5910 | 15,3 |
| 0.740 | 0.80941 | 128,7 | I. 28652 | 80,9 | 0.62915 | 60,4 | 1. 5895 | 15,3 |
| . 741 | .81070 | 128,7 | . 28733 | 81, 1 | . 62975 | 60,3 | . 5879 | 15,2 |
| . 742 | .81 199 | 128,8 | . 28815 | $8 \mathrm{I}, 2$ | . 63035 | 60,3 | . 5864 | 15,2 |
| . 743 | .81327 | 128,9 | . 28896 | 8I,3 | . 63095 | 60,2 | . 5849 | 15, I |
| . 744 | .81456 | 129,0 | . 28977 | 8I,5 | . 63156 | 60, 1 | . 5834 | 15, 1 |
| 0.745 | 0.8 I 585 | 129, I | 1.29059 | 8r,6 | 0.63216 | 60,0 | 1.5819 | 15,0 |
| .746 | .8i7I4 | 129, I | . 29140 | 81,7 | . 63276 | 60,0 | . 5804 | 15,0 |
| .747 | .81844 | 129,2 | . 29222 | 8r,8 | . 63336 | 59,9 | . 5789 | 14,9 |
| . 748 | . 81973 | 129,3 | . 29304 | 82,0 | . 63395 | 59,8 | . 5774 | 14,9 |
| . 749 | . 82102 | 129,4 | . 29386 | 82,I | . 63455 | 59,7 | . 5759 | 14,8 |
| 0.750 | 0.82232 | 129,5 | 1.29468 | 82.2 | 0.63515 | 59,7 | I. 5744 | 14,8 |
| u | $\boldsymbol{t a n} \mathbf{g d} \mathbf{u}$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.750 | 0.82232 | 129,5 | I. 29468 | 82,2 | 0.63515 | 59,7 | I. 5744 | 14,8 |
| .751 | . 82361 | 129,6 | . 29551 | 82,4 | . 63575 | 59,6 | . 5730 | 14,7 |
| . 752 | . 8249 I | 129,6 | . 29633 | 82,5 | . 63634 | 59,5 | . 5715 | 14,7 |
| . 753 | . 82620 | 129,7 | . 29716 | 82,6 | . 63694 | 59,4 | . 5700 | 14,6 |
| . 754 | . 82750 | 129,8 | . 29798 | 82,8 | . 63753 | 59,4 | . 5686 | 14,6 |
| 0.755 | 0.82880 | 129,9 | I. 2988I | 82,9 | 0.638 I 2 | 59,3 | I. 567 I | 14,6 |
| . 756 | . 83010 | 130,0 | . 29964 | 83,0 | . 63871 | 59,2 | . 5656 | 14,5 |
| . 757 | . 83140 | I30,0 | . 30047 | 83, 1 | . 6393 I | 59, 1 | . 5642 | 14,5 |
| . 758 | . 83270 | 130, 1 | . 30130 | 83,3 | . 63990 | 59, I | . 5628 | 14,4 |
| . 759 | . 83400 | 130,2 | . 30214 | 83,4 | . 64049 | 59,0 | . 5613 | I4,4 |
| 0.760 | 0.83530 | 130,3 | 1.30297 | 83,5 | 0.64108 | 58,9 | I. 5599 | 14,3 |
| .76I | . 83661 | 130,4 | . 30381 | 83,7 | . 64167 | 58,8 | . 5584 | 14,3 |
| . 762 | . 83791 | I30,5 | . 30464 | 83,8 | . 64225 | 58,8 | . 5570 | 14,2 |
| . 763. | . 83922 | 130,5 | . 30548 | 83,9 | . 64284 | 58,7 | . 5556 | 14,2 |
| .764 | . 84052 | I30,6 | . 30632 | 84, I | . 64343 | 58,6 | . 5542 | 14,2 |
| 0.765 | 0.84183 | 130,7 | 1. 30716 | 84,2 | 0.64401 | 58,5 | I. 5528 | I4,I |
| . 766 | . 84314 | I 30,8 | . 30801 | 84,3 | . 64460 | 58,4 | . 5514 | I4,I |
| . 767 | . 84445 | 130,9 | . 30885 | 84,4 | . 64518 | 58,4 | . 5500 | 14,0 |
| . 768 | . 84576 | I3I,0 | . 30970 | 84,6 | . 64576 | 58,3 | . 5486 | 14,0 |
| . 769 | . 84707 | I3I, I | . 31054 | 84,7 | . 64635 | 58,2 | . 5472 | 13,9 |
| 0.770 | 0.84838 | 131,1 | I.3II39 | 84,8 | 0.64693 | 58, I | I. 5458 | 13,9 |
| . 771 | . 84969 | I31,2 | . 31224 | 85,0 | . 6475 I | 58, I | . 5444 | I 3,9 |
| . 772 | . 85100 | I3I,3 | - 31309 | 85,1 | . 64809 | 58,0 | . 5430 | I3,8 |
| . 773 | . 85231 | I3I,4 | . 31394 | 85,2 | . 64867 | 57,9 | . 5416 | 13,8 |
| . 774 | . 85363 | I3I,5 | -31479 | 85,4 | . 64925 | 57,8 | . 5402 | 13,7 |
| 0.775 | 0.85494 | I3I,6 | I. 31565 | 85,5 | 0.64983 | 57,8 | 1.5389 | 13,7 |
| . 776 | . 85626 | 131,7 | . 31650 | 85,6 | . 65040 | 57,7 | . 5375 | 13,6 |
| . 777 | . 85758 | 131,7 | . 31736 | 85,8 | . 65098 | 57,6 | . 5361 | I3,6 |
| . 778 | . 85889 | 131,8 | . 31822 | 85,9 | . 65156 | 57,5 | . 5348 | 13,6 |
| . 779 | . 8602 I | I3I,9 | . 31908 | 86,0 | . 652 I 3 | 57,5 | . 5334 | 13,5 |
| 0.780 | 0.86 I 53 | 132,0 | I. 31994 | 86,2 | 0.65271 | 57,4 | I. 532 I | I3,5 |
| . 78 I | . 86285 | I 32, 1 | . 32080 | 86,3 | . 65328 | 57,3 | . 5307 | I3,4 |
| . 782 | . 86417 | 132,2 | . 32166 | 86,4 | . 65385 | 57,2 | . 5294 | 13,4 |
| .783 | . 86550 | I 32,3 | . 32253 | 86,5 | . 65443 | 57,2 | . 5281 | I3,3 |
| .784 | . 86682 | I 32,3 | . 32340 | 86,7 | . 65500 | 57, I | . 5267 | 13,3 |
| 0.785 | 0.86814 | 132,4 | I. 32426 | 86,8 | 0.65557 | 57,0 | I. 5254 | 13,3 |
| - 786 | . 86947 | I 32,5 | . 32513 | 86,9 | . 65614 | 56,9 | . 5241 | 13,2 |
| .787 | . 87079 | 132,6 | . 32600 | 87,I | . 65671 | 56,9 | . 5228 | 13,2 |
| . 788 | . 87212 | 132,7 | . 32687 | 87,2 | . 65727 | 56,8 | . 5214 | I3, 1 |
| .789 | . 87345 | I 32,8 | . 32775 | 87,3 | . 65784 | 56,7 | . 5201 | I3, I |
| 0.790 | 0.87478 | 132,9 | I. 32862 | 87,5 | 0.65841 | 56,6 | 1. 5188 | I3,I |
| . 791 | . 87610 | 132,9 | . 32950 | 87,6 | . 65898 | 56,6 | . 5175 | 13,0 |
| . 792 | . 87743 | 133,0 | . 33037 | 87,7 | . 65954 | 56,5 | . 5162 | 13,0 |
| . 793 | . 87877 | I33, I | . 33125 | 87,9 | . 66011 | 56,4 | . 5149 | 12,9 |
| . 794 | .88010 | 133,2 | . 33213 | 88,0 | . 66067 | 56,4 | . 5136 | 12,9 |
| 0.795 | 0.88 I 43 | 133,3 | 1.33301 | 88, I | 0.66123 | 56,3 | 1.5123 | 12,9 |
| . 796 | . 88276 | I33,4 | . 33389 | 88,3 | . 66179 | 56,2 | . 5110 | 12,8 |
| . 797 | $\bigcirc .88410$ | 133,5 | - 33478 | 88,4 | . 66236 | 56, | . 5098 | 12,8 |
| . 798 | . 88543 | I 33,6 | - 33566 | 88,5 | . 66292 | 56, | . 5085 | 12,8 |
| . 799 | . 88677 | 133,7 | . 33655 | 88,7 | . 66348 | 56,0 | . 5072 | 12,7 |
| 0.800 | 0.888II | 133,7 | I. 33743 | 88,8 | 0.66404 | 55,9 | I. 5059 | 12,7 |
| U | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{Fo}^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.800 | 0.888I I | 133,7 | I. 33743 | 88,8 | 0.66404 | 55,9 | I. 5059 | 12,7 |
| . 801 | . 88944 | 133,8 | . 33832 | 88,9 | . 66460 | 55,8 | . 5047 | 12,6 |
| . 802 | . 89078 | 133,9 | . 3392 I | 89, I | . 65515 | 55,8 | . 5034 | 12,6 |
| . 803 | . 89212 | 134,0 | .3401 I | 89,2 | . 66571 | 55,7 | . 5022 | 12,6 |
| . 804 | . 89346 | I34, I | . 34100 | 89,3 | . 66627 | 55,6 | . 5009 | 12,5 |
| 0.805 | 0.89480 | 134,2 | 1.34189 | 89,5 | 0.66682 | 55,5 | 1. 4996 | 12,5 |
| . 806 | . 89615 | 134,3 | . 34279 | 89,6 | . 66738 | 55,5 | . 4984 | 12,5 |
| . 807 | . 89749 | 134,4 | . 34368 | 89,7 | . 56793 | 55,4 | . 4972 | 12,4 |
| . 808 | . 89883 | I 34,5 | . 34458 | 89,9 | . 66849 | 55,3 | . 4959 | 12,4 |
| . 809 | . 90018 | I 34,5 | - 34548 | 90,0 | . 66904 | 55,2 | . 4947 | 12,3 |
| 0.810 | 0.90152 | 134,6 | I. 34638 | 90,2 | 0.66959 | 55,2 | I. 4935 | 12,3 |
| .8II | . 90287 | 134,7 | . 34729 | 90,3 | . 67014 | 55, I | . 4922 | 12,3 |
| .812 | . 90422 | 134,8 | .34819 | 90,4 | . 67059 | 55,0 | . 4910 | 12,2 |
| .813 | . 90557 | I 34,9 | . 34909 | 90,6 | . 67124 | 54,9 | . 4898 | 12,2 |
| .814 | . 90692 | 135,0 | . 35000 | 90,7 | . 67179 | 54,9 | . 4886 | 12,2 |
| 0.815 | 0.90827 | I35, I | I.35091 | 90,8 | 0.67234 | 54,8 | 1. 4873 | 12,I |
| .816 | . 90962 | 135,2 | . 35182 | 91,0 | . 67289 | 54,7 | . 4861 | 12, I |
| .8I7 | . 91097 | I 35, 3 | . 35273 | 91, 1 | . 67343 | 54,6 | . 4849 | 12,0 |
| .818 | . 91232 | 135,4 | . 35364 | 91,2 | . 67398 | 54,6 | . 4837 | 12,0 |
| .819 | .91368 | 135,5 | . 35455 | 9I,4 | . 67453 | 54,5 | . 4825 | 12,0 |
| 0.820 | 0.91503 | 1 35,5 | I. 35547 | 91,5 | 0.67507 | 54,4 | 1.48I3 | I I,9 |
| .821 | . 91639 | I 35,6 | . 35638 | 91,6 | . 67561 | 54,4 | . 4801 | II,9 |
| . 822 | . 91775 | 1 35,7 | . 35730 | 91,8 | . 67616 | 54,3 | . 4789 | II,9 |
| . 823 | . 91910 | 135,8 | . 35822 | 91,9 | . 67670 | 54,2 | . 4778 | I I, 8 |
| . 824 | .92046 | 135,9 | . 35914 | 92,0 | . 67724 | 54, I | . 4766 | I I, 8 |
| 0.825 | 0.92182 | 136,0 | 1. 36006 | 92,2 | 0.67778 | 54, I | I. 4754 | 11,8 |
| . 826 | . 92318 | I36,1 | . 36098 | 92,3 | . 67832 | 54,0 | . 4742 | I I,7 |
| . 827 | . 92454 | 136,2 | . 36190 | 92,5 | . 67886 | 53,9 | . 4731 | 11,7 |
| . 828 | .92591 | 136,3 | . 36283 | 92,6 | . 67940 | 53,8 | . 4719 | II,7 |
| . 829 | . 92727 | 136,4 | . 36376 | 92,7 | . 67994 | 53,8 | . 4707 | I I,6 |
| 0.830 | 0.92863 | 136,5 | 1. 36468 | 92,9 | 0.68048 | 53,7 | 1. 4696 | I I, 6 |
| . 831 | . 93000 | 136,6 | . 36561 | 93,0 | .68ioi | 53,6 | . 4684 | I I, 6 |
| . 832 | . 93137 | 136,7 | . 36654 | 93, I | .68155 | 53,5 | . 4672 | II,5 |
| . 833 | . 93273 | I36,7 | . 36748 | 93,3 | . 68208 | 53,5 | . 4661 | II,5 |
| . 834 | . 93410 | 136,8 | . 36841 | 93,4 | . 68262 | 53,4 | . 4649 | I I, 5 |
| 0.835 | 0.93547 | 136,9 | 1. 36934 | 93,5 | 0.68315 | 53,3 | 1. 4638 | II,4 |
| . 836 | . 93684 | 137,0 | . 37028 | 93,7 | . 68368 | 53,3 | . 4627 | I I, 4 |
| . 837 | .9382I | I37, 1 | . 37122 | 93,8 | . 68422 | 53,2 | . 4615 | II, 4 |
| . 838 | . 93958 | 137,2 | . 37216 | 94,0 | . 68475 | 53, I | . 4604 | II,3 |
| . 839 | . 94095 | 137,3 | . 37310 | 94, | . 68528 | 53,0 | . 4593 | II, 3 |
| 0.840 | 0.94233 | 137,4 | I . 37404 | 94,2 | 0.68581 | 53,0 | I. 458 I | II,3 |
| . 841 | . 94370 | 1 37,5 | . 37498 | 94,4 | . 68634 | 52,9 | . 4570 | II,2 |
| . 842 | . 94508 | 137,6 | . 37593 | 94,5 | . 68687 | 52,8 | . 4559 | II,2 |
| . 843 | . 94645 | ${ }^{1} 37,7$ | . 37687 | 94,6 | . 68739 | 52,7 | . 4548 | II,2 |
| . 844 | . 94783 | 137,8 | . 37782 | 94,8 | . 68792 | 52,7 | . 4537 | I I, I |
| 0.845 | 0.9492 I | 1 37,9 | I. 37877 | 94,9 | 0.68845 | 52,6 | I. 4525 | I I, I |
| . 846 | . 95059 | 138,0 | . 37972 | 95, I | . 68897 | 52,5 | . 4514 | I I, I |
| . 847 | . 95197 | 138,1 | . 38067 | 95,2 | . 68950 | 52,5 | . 4503 | II,O |
| . 848 | . 95335 | 138,2 | . 38162 | 95,3 | . 69002 | 52,4 | . 4492 | II,O |
| . 949 | . 95473 | I 38,3 | . 38258 | 95,5 | . 69055 | 52,3 | .448I | 11,0 |
| 0.850 | 0.95612 | 1 38,4 | 1. 38353 | 95,6 | 0.69107 | 52,2 | 1. 4470 | 10,9 |
| 4 | $\boldsymbol{t a n g d} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathbf{s e c} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.850 | 0.95612 | 138,4 | 1.383,53 | 95,6 | 0.69107 | 52,2 | 1.4470 | 10,9 |
| . 851 | . 95750 | 138,4 | . 38449 | 95,7 | . 69159 | 52,2 | . 4459 | 10,9 |
| . 852 | . 95888 | 138,5 | . 38545 | 95,9 | . 692 I I | 52, I | . 4449 | 10,9 |
| . 853 | . 96027 | 138,6 | . 38641 | 96,0 | . 69253 | 52,0 | . 4438 | 10,8 |
| . 854 | . 96166 | I 38,7 | . 38737 | 96,2 | . 69315 | 52,0 | . 4427 | 10,8 |
| 0.855 | 0.96305 | I 38,8 | I. 38833 | 96,3 | 0.69367 | 51,9 | 1.4416 | 10,8 |
| . 856 | . 96443 | 138,9 | . 38929 | 96,4 | . 69419 | $5 \mathrm{I}, 8$ | . 4405 | I0,8 |
| . 857 | . 96582 | I 39,0 | . 39026 | 96,6 | . 69471 | 51,7 | . 4395 | 10,7 |
| . 858 | . 9672 I | I39, I | . 39122 | 96,7 | .69523 | 51,7 | . 4384 | 10,7 |
| . 859 | .9686I | 139,2 | . 39219 | 96,9 | . 69574 | 51,6 | . 4373 | 10,7 |
| 0.860 | 0.97000 | I 39,3 | 1.39316 | 97,0 | 0.69626 | 51,5 | I. 4362 | 10,6 |
| . 86 I | .97139 | 1 39,4 | . 39413 | 97, 1 | . 69677 | 51,5 | . 4352 | 10,6 |
| . 862 | . 97279 | I 39,5 | . 39510 | 97,3 | . 69729 | 5I,4 | . 434 I | 10,6 |
| . 863 | . 97418 | I 39,6 | . 39608 | 97,4 | . 69780 | 5I,3 | . 433 I | 10,5 |
| . 864 | . 97558 | 139,7 | - 39705 | 97,6 | . 69831 | 51,2 | . 4320 | 10,5 |
| 0.865 | 0.97698 | I39,8 | 1. 39803 | 97,7 | 0.69882 | 51,2 | I. 4310 | 10,5 |
| . 866 | . 97838 | 1 39,9 | . 39901 | 97,8 | . 69934 | $5 \mathrm{I}, \mathrm{I}$ | . 4299 | 10,4 |
| . 867 | . 97978 | I40,0 | - 39999 | 98,0 | . 69985 | 51,0 | . 4289 | 10,4 |
| . 868 | .98118 | 140, I | .40097 | 98, I | . 70036 | 51,0 | . 4278 | 10,4 |
| . 869 | . 98258 | 140,2 | . 40195 | 98,3 | . 70087 | 50,9 | . 4268 | 10,4 |
| 0.870 | 0.98398 | 140,3 | 1. 40293 | 98,4 | 0.70137 | 50,8 | 1. 4258 | 10,3 |
| . 871 | . 98538 | 140,4 | . 40392 | 98,5 | . 70188 | 50,7 | . 4247 | 10,3 |
| . 872 | . 98679 | 140,5 | . 40490 | 98,7 | . 70239 | 50,7 | . 4237 | 10,3 |
| . 873 | .98819 | 140,6 | . 40589 | 98,8 | . 70290 | 50,6 | . 4227 | 10,2 |
| . 874 | . 98960 | 140,7 | . 40688 | 99,0 | . 70340 | 50,5 | . 4217 | 10,2 |
| 0.875 | 0.99 IOI | 140,8 | 1.40787 | 99, I | 0.70391 | 50,5 | 1. 4206 | 10,2 |
| . 876 | . 99241 | 140,9 | . 40886 | 99,2 | . 70441 | 50,4 | . 4196 | 10,2 |
| . 877 | . 99382 | I41,0 | . 40985 | 99,4 | . 70491 | 50,3 | . 4186 | 10, I |
| . 878 | . 99523 | I4I, I | . 41085 | 99,5 | . 70542 | 50,2 | . 4176 | 10, I |
| . 879 | . 99665 | 141,2 | .41184 | 99,7 | . 70592 | 50,2 | . 4166 | 10, I |
| 0.880 | 0.99806 | 141,3 | I. 41284 | 99,8 | 0.70642 | 50, I | I. 4156 | 10,0 |
| . 88 I | . 99947 | 141,4 | . 41384 | 99,9 | :70692 | 50,0 | . 4146 | 10,0 |
| . 882 | 1.00089 | 141,5 | . 41484 | 100, I | . 70742 | 50,0 | . 4136 | 10,0 |
| . 883 | . 00230 | 141,6 | . 41584 | 100,2 | . 70792 | 49,9 | . 4126 | 10,0 |
| . 884 | . 00372 | 141,7 | . 41684 | 100,4 | .70842 | 49,8 | . 4116 | 9,9 |
| 0.885 | 1.00514 | 141,8 | 1.41785 | 100,5 | 0.70892 | 49,7 | I. 4106 | 9,9 |
| . 885 | . 00655 | 141,9 | . 41886 | 100,7 | . 70941 | 49,7 | . 4096 | 9,9 |
| . 887 | . 00797 | 142,0 | .41986 | 100,8 | . 70991 | 49,6 | . 4086 | 9,8 |
| . 888 | . 00939 | 142, 1 | . 42087 | 100,9 | . 71040 | 49,5 | . 4076 | 9,8 |
| . 889 | . 01081 | 142,2 | . 42188 | IOI, I | .71090 | 49,5 | . 4067 | 9,8 |
| 0.890 | 1.01224 | 142,3 | I. 42289 | IOI, 2 | 0.71139 | 49,4 | I. 4057 | 9,8 |
| . 891 | . 01366 | 142,4 | . 42391 | IOI, 4 | . 71189 | 49,3 | . 4047 | 9,7 |
| . 892 | . 01508 | 142,5 | . 42492 | IOI,5 | -71238 | 49,3 | . 4037 | 9,7 |
| . 893 | . 01651 | 142,6 | . 42594 | IOI, 7 | . 71287 | 49,2 | . 4028 | 9,7 |
| . 894 | . 01794 | 142,7 | . 42695 | IOI,8 | . 71336 | 49, I | . 4018 | 9,7 |
| 0.895 | 1.01936 | 142,8 | I. 42797 | 101,9 | 0.71385 | 49,0 | I. 4008 | 9,6 |
| . 896 | . 02079 | 142,9 | . 42899 | 102, I | . 71434 | 49,0 | . 3999 | 9,6 |
| . 897 | . 02222 | 143,0 | . 43001 | 102,2 | . 71483 | 48,9 | . 3989 | 9,6 |
| . 898 | . 02365 | 143, I | .43104 | 102,4 | . 71532 | 48,8 | . 3980 | 9,5 |
| . 899 | . 02508 | I 43, 2 | . 43206 | 102,5 | .7158I | 48,8 | - 3970 | 9,5 |
| 0.900 | 1.02652 | I43,3 | 1. 43309 | 102,7 | 0.71630 | 48,7 | I. 396 I | 9,5 |
| 4 | $\tan \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec$ gd u | $\omega F_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| 4 | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.900 | 1. 02652 | 143 | 1. 43309 | 103 | 0.71630 | 48,7 | I. 3961 | 9,5 |
| .901 | . 02795 | 143 | . 4341 I | 103 | . 71678 | 48,6 | . 3951 | 9,5 |
| . 902 | . 02938 | 144 | . 43514 | 103 | .71727 | 48,6 | . 3942 | 9,4 |
| . 903 | . 03082 | 144 | . 43617 | 103 | . 71776 | 48,5 | . 3932 | 9,4 |
| . 904 | . 03226 | 144 | . 43720 | 103 | .71824 | 48,4 | . 3923 | 9,4 |
| 0.905 | 1.03370 | 144 | 1.43824 | 103 | 0.71872 | 48,3 | I. 3914 | 9,4 |
| . 906 | . 03513 | 144 | . 43927 | 104 | . 71921 | 48,3 | . 3904 | 9,3 |
| . 907 | . 03657 | 144 | . 4403 I | 104 | . 71969 | 48,2 | . 3895 | 9,3 |
| . 908 | . 03801 | 144 | .44134 | 104 | . 72017 | 48,1 | . 3886 | 9,3 |
| . 909 | . 03946 | 144 | . 44238 | 104 | . 72065 | 48,1 | . 3876 | 9,3 |
| 0.910 | 1. 04090 | 144 | I. 44342 | 104 | 0.72113 | 48,0 | I. 3867 | 9,2 |
| .9II | . 04234 | 144 | . 44446 | 104 | .72161 | 47,9 | . 3858 | 9,2 |
| .912 | . 04379 | 145 | . 44551 | 104 | . 72209 | 47,9 | - 3849 | 9,2 |
| .913 | . 04523 | 145 | . 44655 | 105 | . 72257 | 47,8 | -3840 | 9,2 |
| . 914 | . 04668 | 145 | . 44760 | 105 | . 72305 | 47,7 | .3830 | 9, I |
| 0.915 | 1.04813 | 145 | 1. 44865 | 105 | 0.72352 | 47,7 | I. 3821 | 9, I |
| . 916 | . 04958 | 145 | . 44969 | 105 | . 72400 | 47,6 | . 3812 | 9, I |
| .917 | . 05103 | 145 | . 45075 | 105 | . 72448 | 47,5 | . 3803 | 9,1 |
| .918 | . 05248 | 145 | . 45180 | 105 | . 72495 | 47,4 | . 3794 | 9,0 |
| . 919 | . 05393 | 145 | . 45285 | 105 | . 72542 | 47,4 | . 3785 | 9,0 |
| 0.920 | 1.05539 | 145 | I. 45390 | 106 | 0.72590 | 47,3 | 1.3776 | 9,0 |
| .92I | . 05684 | 145 | . 45496 | 106 | . 72637 | 47,2 | . 3767 | 9,0 |
| . 922 | .05830 | 146 | - . 45602 | 106 | . 72684 | 47,2 | . 3758 | 8,9 |
| . 923 | . 05975 | 146 | . 45708 | 106 | . 72731 | 47, I | . 3749 | 8,9 |
| . 924 | .06121 | 146 | . 45814 | 106 | . 72778 | 47,0 | . 3740 | 8,9 |
| 0.925 | 1. 06267 | 146 | 1. 45920 | 106 | 0.72825 | 47,0 | I. 3731 | 8,9 |
| . 926 | . 06413 | 146 | . 46026 | 106 | . 72872 | 46,9 | . 3723 | 8,8 |
| . 927 | . 06559 | 146 | . 46133 | 107 | . 72919 | 46,8 | . 3714 | 8,8 |
| . 928 | .06705 | 146 | . 46239 | 107 | . 72966 | 46,8 | . 3705 | 8,8 |
| . 929 | .0685I | 146 | . 46346 | 107 | .73013 | 46,7 | . 3696 | 8,8 |
| 0.930 | 1.06998 | 146 | 1. 46453 | 107 | 0.73059 | 46,6 | 1.3687 | 8,7 |
| .93I | . 07144 | 147 | . 46560 | 107 | .73106 | 46,6 | . 3679 | 8,7 |
| . 932 | .07291 | 147 | . 46667 | 107 | .73153 | 46,5 | . 3670 | 8,7 |
| . 933 | . 07438 | 147 | . 46775 | 107 | . 73199 | 46,4 | . 3661 | 8,7 |
| . 934 | . 07584 | 147 | . 46882 | 108 | . 73245 | 46,4 | . 3653 | 8,6 |
| 0.935 | 1.0773I | 147 | 1.46590 | 108 | 0.73292 | 46,3 | 1. 3644 | 8,6 |
| . 936 | . 07878 | 147 | . 47098 | 108 | . 73338 | 46,2 | . 3636 | 8,6 |
| . 937 | .08025 | 147 | . 47.206 | 108 | . 73384 | 46, I | . 3627 | 8,6 |
| . 938 | .08173 | 147 | . 47314 | 108 | . 73430 | 46, | . 3618 | 8,5 |
| . 939 | . 08320 | 147 | . 47422 | 108 | . 73476 | 46,0 | . 3610 | 8,5 |
| 0.940 | 1.08468 | 148 | 1.47530 | 108 | 0.73522 | 45,9 | 1.3601 | 8,5 |
| . 941 | .08615 | 148 | . 47639 | 109 | . 73568 | 45,9 | . 3593 | 8,5 |
| . 942 | . 08863 | 148 | . 47748 | 109 | . 73614 | 45,8 | . 3584 | 8,5 |
| . 943 | .0891 1 | 148 | . 47857 | 109 | . 73660 | 45,7 | - 3576 | 8,4 |
| . 944 | . 09059 | 148 | . 47966 | 109 | . 73705 | 45,7 | . 3568 | 8,4 |
| 0.945 | 1.09207 | 148 | 1.48075 | 109 | 0.73751 | 45,6 | I. 3559 | 8,4 |
| . 946 | . 09355 | 148 | . 48184 | 109 | . 73797 | 45,5 | . 3551 | 8,4 |
| . 947 | . 09503 | 148 | . 48293 | 110 | . 73842 | 45,5 | - 3542 | 8,3 |
| . 948 | .09651 | 148 | .48403 | 110 | . 73888 | 45,4 | . 3534 | 8,3 |
| . 949 | . 09800 | 149 | . 48513 | 110 | . 73933 | 45,3 | . 3526 | 8,3 |
| 0.950 | 1. 09948 | 149 | 1.48623 | 110 | 0.73978 | 45,3 | I. 3517 | 8,3 |
| $u$ | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{v^{\prime}}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.950 | 1.09948 | 149 | 1.48623 | 110 | 0.73978 | 45,3 | 1.3517 | 8,3 |
| .95I | . 10097 | 149 | . 48733 | 110 | . 74024 | 45,2 | . 3509 | 8,2 |
| . 952 | . 10246 | 149 | . 48843 | 110 | . 74069 | 45, 1 | . 3501 | 8,2 |
| . 953 | . 10395 | 149 | . 48953 | 110 | .74114 | 45, I | - 3493 | 8,2 |
| . 954 | . 10544 | 149 | . 49064 | III | .74159 | 45,0 | . 3485 | 8,2 |
| 0.955 | I. 10693 | 149 | 1.49174 | III | 0.74204 | 44,9 | 1. 3476 | 8,2 |
| . 956 | . 10842 | 149 | . 49285 | III | . 74249 | 44,9 | . 3468 | 8,1 |
| . 957 | . 10991 | 149 | . 49396 | III | .74294 | 44,8 | . 3460 | 8, I |
| . 958 | . III4I | 150 | . 49507 | III | . 74338 | 44,7 | . 3452 | 8, I |
| . 959 | . I I29I | 150 | . 49618 | III | . 74383 | 44,7 | . 3444 | 8,I |
| 0.960 | I. II440 | 150 | 1. 49729 | III | 0.74428 | 44,6 | 1. 3436 | 8,I |
| .96I | . II 590 | 150 | . 4984 I | 112 | . 74472 | 44,5 | . 3428 | 8,o |
| . 962 | . II740 | 150 | . 49953 | 112 | . 74517 | 44,5 | . 3420 | 8,0 |
| . 963 | . 11890 | 150 | . 50064 | 112 | .74561 | 44,4 | . 3412 | 8,0 |
| . 964 | . 12040 | 150 | . 50176 | 112 | .74606 | 44,3 | - 3404 | 8,0 |
| 0.965 | 1.12190 | 150 | 1.50289 | 112 | 0.74650 | 44,3 | 1. 3396 | 7,9 |
| . 956 | . 12341 | 150 | . 50401 | II2 | . 74694 | 44,2 | . 3388 | 7,9 |
| . 967 | . 12491 | 151 | . 50513 | II2 | . 74738 | 44, I | - 3380 | 7,9 |
| . 968 | . 12642 | 151 | . 50526 | II3 | . 74782 | 44, I | . 3372 | 7.9 |
| . 969 | . 12792 | 151 | . 50739 | II3 | . 74826 | 44,0 | . 3364 | 77 |
| 0.970 | I. 12943 | 151 | I. $5085 \mathrm{I}^{\prime}$ | II3 | 0.74870 | 43,9 | I. 3356 | 7,8 |
| . 971 | . 13094 | 15 I | . 50964 | II3 | .74914 | 43,9 | . 3349 | 7,8 |
| . 972 | . 13245 | 151 | . 51078 | II3 | . 74958 | 43,8 | . 334 I | 7,8 |
| . 973 | . I3396 | 151 | . 51191 | II3 | . 75002 | 43,7 | - 3333 | 7,8 |
| . 974 | . 13547 | 15 I | .51304 | II4 | . 75046 | 43,7 | - 3325 | 7,8 |
| 0.975 | 1. 13699 | 151 | 1.51418 | II4 | 0.75089 | 43,6 | I.33I7 | 7,7 |
| . 976 | . 13850 | 152 | . 51532 | II4 | . 75133 | 43,6 | . 3310 | 7,7 |
| . 977 | . 14002 | 152 | . 51646 | II4 | .75176 | 43,5 | . 3302 | 7,7 |
| . 978 | . 14154 | 152 | . 51760 | II4 | . 75220 | 43,4 | . 3294 | 7,7 |
| . 979 | . I4305 | 152 | . 51874 | II4 | . 75263 | 43,4 | . 3287 | 7,7 |
| 0.980 | I. I4457 | 152 | 1. 51988 | 144 | 0.75307 | 43,3 | I. 3279 | 7,6 |
| .98I | . I4609 | 152 | . 52103 | II5 | . 75350 | 43,2 | . 327 I | 7,6 |
| . 982 | . 14761 | 152 | . 52218 | II5 | . 75393 | 43,2 | . 3264 | 7,6 |
| .983 | . 14914 | 152 | . 52332 | II 5 | . 75436 | 43, I | . 3256 | 7,6 |
| . 984 | . 15066 | 152 | . 52447 | II5 | . 75479 | 43,0 | . 3249 | 7,6 |
| 0.985 | 1. 15219 | 153 | 1. 52563 | 115 | 0.75522 | 43,0 | I. 324 I | 7,5 |
| . 986 | . 15371 | 153 | . 52678 | II5 | . 75565 | 42,9 | . 3234 | 7,5 |
| . 987 | . 15524 | I53 | . 52793 | 116 | . 75608 | 42,8 | . 3226 | 7,5 |
| . 988 | . 15677 | I53 | . 52909 | 1 I 6 | . 75651 | 42,8 | . 3219 | 7,5 |
| . 989 | . 15830 | 153 | . 53025 | I 16 | . 75694 | 42,7 | . 3211 | 7,5 |
| 0.990 | 1. 15983 | 153 | 1.53141 | II6 | 0.75736 | 42,6 | I. 3204 | 7,4 |
| . 991 | . 16I36 | 153 | . 53257 | 116 | . 75779 | 42,6 | . 3196 | 7,4 |
| . 992 | . 16289 | 153 | . 53373 | I 16 | . 75821 | 42,5 | . 3189 | 7,4 |
| . 993 | . 16443 | 153 | . 53489 | 116 | . 75864 | 42,4 | . 3182 | 7,4 |
| . 994 | . 16596 | 154 | . 53606 | 117 | . 75906 | 42,4 | -3174 | 7,4 |
|  | I. 16750 | 154 | 1. 53722 | 117 | 0.75949 | 42,3 | 1.3167 | 7,3 |
| . 996 | . 16904 | 154 | . 53839 | 117 | . 75991 | 42,3 | -3I59 | 7,3 |
| . 997 | . 17058 | 154 | . 53956 | II7 | . 76033 | 42,2 | . 3152 | 7.3 |
| . 998 | . 17212 | 154 | . 54073 | II7 | . 76075 | 42, I | .3I45 | 7,3 |
| . 999 | . 17366 | 154 | . 5419 I | 117 | .76117 | 42, I | . 3138 | 7,3 |
| 1.000 | I. 17520 | 154 | I. 54308 | 118 | 0.76159 | 42,0 | 1.3130 | 7,2 |
| $u$ | $\boldsymbol{t a n g d} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n g d u}$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\circ}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | I. I7520 | 154 | 1.54308 | 118 | 0.76159 | 42,0 | 1.3130 | 7,2 |
| . 001 | . 17674 | 154 | . 54426 | 118 | . 76201 | 41,9 | . 3123 | 7,2 |
| . 002 | . 17829 | 155 | . 54543 | II8 | . 76243 | 41,9 | . 3116 | 7,2 |
| . 003 | . 17984 | 155 | . 5466 I | 118 | . 76285 | 41,8 | . 3109 | 7,2 |
| . 004 | . 18138 | 155 | . 54779 | 118 | . 76327 | 41,7 | .3102 | 7,2 |
| 1.005 | I. 18293 | 155 | 1. 54898 | 118 | 0.76369 | 41,7 | I. 3094 | 7,I |
| . 006 | . 18448 | 155 | . 55016 | 118 | . 76410 | 41,6 | . 3087 | 7, 1 |
| . 007 | . 18603 | 155 | . 55134 | 119 | . 76452 | 41,6 | . 3080 | 7, I |
| . 008 | . 18758 | 155 | . 55253 | 119 | . 76493 | 4I,5 | . 3073 | 7, I |
| . 009 | . 18914 | 155 | - 55372 | 119 | . 76535 | 4I,4 | . 3066 | 7,1 |
| 1.010 | 1. 19069 | 155 | I. 55491 | 119 | 0.76576 | 41,4 | 1. 3059 | 7,1 |
| . OII | . 19225 | 156 | . 55610 | 119 | . 76618 | 4I,3 | . 3052 | 7,0 |
| . OI 2 | . 19380 | 156 | . 55729 | 119 | . 76659 | 41,2 | . 3045 | 7,0 |
| . 013 | . 19536 | 156 | . 55849 | 120 | . 76700 | 41,2 | . 3038 | 7,0 |
| . 014 | . 19692 | 156 | . 55969 | 120 | . 76741 | 4I, I | . 3031 | 7,0 |
| 1.015 | 1. 19848 | 156 | 1. 56088 | 120 | 0.76782 | 41,0 | 1.3024 | 7,0 |
| . 016 | . 20004 | 156 | . 56208 | 120 | . 76823 | 41,0 | . 3017 | 6,9 |
| . 017 | . 20160 | 156 | . 56328 | 120 | . 76864 | 40,9 | . 3010 | 6,9 |
| . 018 | . 20317 | 156 | . 56449 | 120 | . 76905 | 40,9 | . 3003 | 6,9 |
| . 019 | . 20473 | 157 | . 56569 | 120 | . 76946 | 40,8 | . 2996 | 6,9 |
| 1.020 | 1.20630 | 157 | 1. 56689 | 12 I | 0.76987 | 40,7 | 1. 2989 | 6,9 |
| .02I | . 20787 | 157 | . 56810 | 121 | . 77027 | 40,7 | . 2982 | 6,9 |
| . 022 | . 20944 | 157 | . 56931 | 12 I | . 77068 | 40,6 | . 2976 | 6,8 |
| . 023 | . 21IOI | 157 | . 57052 | 12 I | . 77109 | 40,5 | . 2969 | 6,8 |
| . 024 | . 21258 | 157 | . 57173 | 12 I | . 77149 | 40,5 | . 2962 | 6,8 |
| 1.025 | 1.21415 | 157 | I. 57295 | 121 | 0.77190 | 40,4 | I. 2955 | 6,8 |
| . 026 | . 21572 | 157 | . 57416 | 122 | . 77230 | 40,4 | . 2948 | 6,8 |
| . 027 | . 21730 | 158 | . 57538 | 122 | . 77270 | 40,3 | . 2942 | 6,7 |
| . 028 | . 21887 | 158 | . 57660 | 122 | . 77310 | 40,2 | . 2935 | 6,7 |
| . 029 | . 22045 | 158 | . 57782 | 122 | .77351 | 40,2 | . 2928 | 6,7 |
| 1.030 | 1.22203 | 158 | 1. 57904 | 122 | 0.7739 I | 40, I | I. 2921 | 6,7 |
| .03I | . 22361 | 158 | . 58026 | 122 | .77431 | 40,0 | . 2915 | 6,7 |
| . 032 | . 22519 | 158 | -58148 | 123 | . 7747 I | 40,0 | . 2908 | 6,7 |
| . 033 | . 22677 | 158 | . 58271 | 123 | . 77511 | 39,9 | . 2901 | 6,6 |
| . 034 | . 22836 | 158 | . 58394 | 123 | .7755I | 39,9 | . 2895 | 6,6 |
| 1.035 | I. 22994 | 159 | 1. 58517 | 123 | 0.77591 | 39,8 | I. 2888 | 6,6 |
| . 036 | . 23I53 | 159 | . 58640 | 123 | . 77630 | 39,7 | . 2882 | 6,6 |
| . 037 | . 23311 | 159 | . 58763 | 123 | . 77670 | 39,7 | . 2875 | 6,6 |
| .038 | . 23470 | 159 | . 58886 | 123 | . 77710 | 39,6 | . 2868 | 6,6 |
| . 039 | . 23629 | 159 | . 59010 | 124 | . 77749 | 39,6 | . 2862 | 6,5 |
| 1.040 | I. 23788 | 159 | I. 59134 | 124 | 0.77789 | 39,5 | 1. 2855 | 6,5 |
| . 041 | . 23947 | 159 | . 59257 | 124 | . 77828 | 39,4 | . 2849 | 6,5 |
| . 042 | . 24107 | 159 | . 5938 I | 124 | . 77868 | 39,4 | . 2842 | 6,5 |
| . 043 | . 24266 | 160 | . 59506 | 124. | . 77907 | 39,3 | . 2836 | 6,5 |
| . 044 | . 24426 | 160 | . 59630 | 124 | . 77946 | 39,2 | . 2829 | 6,5 |
| 1.045 | I. 24585 | 160 | I. 59755 | 125 | 0.77985 | 39,2 | 1.2823 | 6,4 |
| . 046 | . 24745 | 160 | . 59879 | 125 | . 78025 | 39, 1 | .2816 | 6,4 |
| . 047 | . 24905 | 160 | . 60004 | 125 | . 78064 | 39, 1 | .2810 | 6,4 |
| . 048 | .25065 | 160 | . 60129 | 125 | .78103 | 39,0 | . 2804 | 6,4 |
| . 049 | . 25225 | 160 | . 60254 | 125 | .78142 | 38,9 | . 2797 | 6,4 |
| 1.050 | 1. 25386 | 160 | 1.60379 | 125 | 0.7818I | 38,9 | I. 279I | 6,4 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n g d} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\tanh u$ | $\omega F_{0}{ }^{\text {d }}$ | coth $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.050 | 1.25386 | 160 | 1. 60379 | 125 | 0.78181 | 38,9 | 1.2791 | 6,4 |
| . 051 | . 25546 | 161 | . 60505 | 126 | . 78219 | 38,8 | . 2785 | 6,3 |
| . 052 | . 25707 | I6I | . 60531 | 126 | . 78258 | 38,8 | . 2778 | 6,3 |
| . 053 | . 25857 | 16 I | . 60756 | 126 | . 78297 | 38,7 | . 2772 | 6,3 |
| . 054 | . 26028 | I6I | . 60882 | 126 | . 78336 | 38,6 | .2766 | 6,3 |
| 1.055 | I. 26189 | 161 | 1. 61008 | 126 | 0.78374 | 38,6 | 1.2759 | 6,3 |
| . 056 | . 26350 | 161 | . 61135 | 126 | .78413 | 38,5 | . 2753 | 6,3 |
| . 057 | . 2651 I | 161 | .61251 | 127 | . 78451 | 38,4 | . 2747 | 6,2 |
| . 058 | . 26673 | 161 | . 61388 | 127 | .78450 | 38,4 | . 2741 | 6,2 |
| . 059 | . 26834 | 162 | .6I5I4 | 127 | . 78528 | 38,3 | . 2734 | 6,2 |
| 1.060 | 1. 26996 | 162 | 1.61641 | 127 | 0.78556 | 38,3 | 1.2728 | 6,2 |
| .06I | . 27157 | 162 | . 61768 | 127 | . 78605 | 38,2 | . 2722 | 6,2 |
| . 062 | . 27319 | 162 | . 61896 | 127 | . 78643 | 38,2 | . 2716 | 6,2 |
| . 063 | . 2748 I | 162 | . 62023 | 127 | . 7868 I | 38,1 | . 2710 | 6,2 |
| . 064 | . 27643 | 162 | . 6215 I | 128 | . 78719 | 38,0 | .2703 | 6,1 |
| 1.065 | 1.27806 | 162 | 1. 62278 | 128 | 0.78757 | 38,0 | 1. 2697 | 6,1 |
| . 065 | . 27968 | 162 | . 62406 | 128 | . 78795 | 37,9 | . 2691 | 6,1 |
| . 067 | . 28130 | 163 | . 62534 | 128 | . 78833 | 37,9 | . 2685 | 6,1 |
| . 068 | . 28293 | 163 | . 62562 | 128 | . 78871 | 37,8 | . 2679 | 6, I |
| . 069 | . 28456 | 163 | .62791 | 128 | .78¢08 | 37,7 | . 2673 | 6,1 |
| 1.070 | 1.28519 | 163 | 1.62919 | 129 | 0.78946 | 37,7 | 1.2667 | 6,0 |
| . 071 | . 28782 | 163 | . 63048 | 129 | . 78984 | 37,6 | . 2661 | 6,0 |
| . 072 | . 28945 | 163 | . 63177 | 129 | . 79021 | 37,6 | . 2655 | 6,0 |
| . 073 | . 29108 | 163 | . 63306 | 129 | . 79059 | 37,5 | . 2649 | 6,0 |
| . 074 | . 2927 I | 163 | . 63435 | 129 | . 79096 | 37,4 | . 2643 | 6,0 |
| 1.075 | I. 29435 | 164 | 1. 63565 | 129 | 0.79134 | 37,4 | 1.2637 | 6,0 |
| . 076 | . 29598 | 164 | . 63694 | 130 | . 79171 | 37,3 | . 2631 | 6,0 |
| . 077 | . 29762 | 164 | . 63824 | 130 | . 79208 | 37,3 | . 2625 | 5,9 |
| . 078 | . 29926 | 164 | . 63954 | 130 | . 79246 | 37,2 | . 2619 | 5,9 |
| . 079 | . 30090 | 164 | . 64084 | 130 | . 79283 | 37, 1 | . 2613 | 5,9 |
| 1.080 | I. 30254 | 164 | 1. 64214 | 130 | 0.79320 | 37,1 | 1. 2607 | 5,9 |
| . .081 | . 30418 | 164 | . 64344 | 130 | . 79357 | 37,0 | . 2601 | 5,9 |
| - . 082 | . 30583 | 164 | . 64475 | 13 I | . 79394 | 37,0 | . 2595 | 5,9 |
| . 083 | . 30747 | 165 | .64605 | 131 | . 7943 I | 36,9 | . 2590 | 5,8 |
| . 084 | . 30912 | 165 | . 64736 | 131 | . 79468 | 36,8 | . 2584 | 5,8 |
| 1.085 | 1.31077 | 165 | 1. 64867 | 131 | 0.79505 | 36,8 | I. 2578 | 5,8 |
| . 086 | . 31242 | 165 | . 64998 | 13 I | . 79541 | 36,7 | . 2572 | 5,8 |
| . 087 | -31407 | 165 | . 65130 | 131 | . 79578 | 36,7 | . 2566 | 5,8 |
| . 088 | -31572 | 165 | . 65261 | 132 | .79615 | 36,6 | . 2560 | 5,8 |
| . 089 | . 31737 | 165 | . 65393 | 132 | .7955I | 36,6 | . 2555 | 5,8 |
| 1.090 | 1.31903 | 166 | 1.65525 | 132 | 0.79688 | 36,5 | 1. 2549 | 5,7 |
| .091 | . 32068 | 166 | . 65657 | 132 | . 79724 | 36,4 | . 2543 | 5,7 |
| . 092 | . 32234 | 166 | . 65789 | 132 | .7976I | 36,4 | . 2538 | 5,7 |
| . 093 | . 32400 | 166 | . 65921 | 132 | . 79797 | 36,3 | . 2532 | 5,7 |
| . 094 | . 32566 | 166 | . 66053 | 133 | . 79833 | 36,3 | . 2526 | 5,7 |
| 1.095 | 1. 32732 | 166 | 1. 66186 | 133 | 0.79870 | 36,2 | 1.2520 | 5,7 |
| . 096 | . 32898 | 166 | . 66319 | 133 | . 79906 | 36,2 | . 2515 | 5,7 |
| . 097 | . 33065 | 166 | . 66452 | 133 | . 79942 | 36, | . 2509 | 5,6 |
| . 098 | . 3323 I | 167 | . 66585 | 133 | . 79978 | 36,0 | . 2503 | 5,6 |
| . 099 | - 33398 | 167 | . 66718 | 133 | .80014 | 36,0 | . 2498. | 5,6 |
| I. 100 | 1. 33565 | 167 | 1.66852 | I34 | 0.80050 | 35,9 | I. 2492 | 5,6 |
| u | $\boldsymbol{t a n g d} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\operatorname{coth} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 100 | I. 33565 | 167 | 1. 66852 | I34 | 0.80050 | 35,9 | I. 2492 | 5,6 |
| . IOI | . 33732 | 167 | . 66986 | I 34 | . 80085 | 35,9 | . 2487 | 5,6 |
| . 102 | . 33899 | 167 | . 67119 | 134 | . 80122 | 35,8 | . 248I | 5,6 |
| . 103 | - 34066 | 167 | . 67253 | I 34 | . 80157 | 35,7 | . 2475 | 5,6 |
| . 104 | . 34233 | 167 | . 67387 | I 34 | . 80193 | 35,7 | . 2470 | 5,5 |
| I. 105 | I. 34401 | 168 | 1. 67522 | I34 | 0.80229 | 35,6 | I. 2464 | 5,5 |
| . 106 | . 34568 | 168 | . 67656 | 135 | . 80264 | 35,6 | . 2459 | 5,5 |
| . 107 | . 34736 | 168 | . 67791 | I 35 | . 80300 | 35,5 | . 2453 | 5,5 |
| . 108 | . 34904 | 168 | . 67926 | I35 | . 80335 | 35,5 | . 2448 | 5,5 |
| . 109 | . 35072 | 168 | .6806I | 135 | . 8037 I | 35,4 | . 2442 | 5,5 |
| I. IIO | I. 35240 | 168 | 1.68196 | 135 | 0.80406 | 35,3 | I. 2437 | 5,5 |
| . III | . 35408 | 168 | . 68331 | 135 | . 80442 | 35,3 | . 2431 | 5,5 |
| . II2 | . 35577 | 168 | . 68467 | 136 | . 80477 | 35,2 | . 2426 | 5,4 |
| . II 3 | . 35745 | 169 | . 68602 | I36 | . 80512 | 35,2 | . 242 I | 5,4 |
| . II4 | . 35914 | 169 | . 68738 | I 36 | . 80547 | 35, I | . 2415 | 5,4 |
| I.II5 | 1. 36083 | 169 | 1. 68874 | I36 | 0.80582 | 35, 1 | 1. 2410 | 5,4 |
| . 116 | . 36252 | 169 | . 69010 | 136 | . 80617 | 35,0 | . 2404 | 5,4 |
| . II7 | . 3642 I | 169 | . 69147 | I36 | . 80652 | 35,0 | . 2399 | 5,4 |
| . 118 | . 36590 | 169 | . 69283 | 137 | . 80687 | 34,9 | . 2394 | 5,4 |
| . II9 | . 36759 | 169 | . 69420 | 137 | . 80722 | 34,8 | . 2388 | 5,3 |
| ${ }^{\text {r. }} 120$ | 1. 36929 | 170 | I. 69557 | 137 | 0.80757 | 34,8 | I. 2383 | 5,3 |
| - -1 | . 37098 | 170 | . 69694 | 137 | . 80792 | 34,7 | . 2378 | 5,3 |
| . 122 | . 37268 | 170 | . 69831 | 137 | . 80826 | 34,7 | . 2372 | 5,3 |
| . 123 | . 37438 | 170 | . 69968 | 137 | . 8085 I | 34,6 | . 2367 | 5,3 |
| . 124 | . 37608 | 170 | . 70106 | I38 | . 80896 | 34,6 | . 2362 | 5,3 |
| I. 125 | 1. 37778 | 170 | 1.70243 | 138 | 0.80930 | 34,5 | I. 2356 | 5,3 |
| . 125 | . 37949 | 170 | . 70381 | 138 | . 80965 | 34,4 | . 2351 | 5,3 |
| .127 | .38119 | 171 | . 70519 | 138 | . 80999 | 34,4 | . 2346 | 5,2 |
| . 128 | . 38290 | 171 | . 70658 | 138 | . 81033 | 34,3 | . 2341 | 5,2 |
| . 129 | . 38460 | 171 | .70796 | 138 | .81068 | 34,3 | . 2335 | 5,2 |
| I. I30 | 1. 38531 | 171 | 1.70934 | 139 | 0.81102 | 34,2 | I. 2330 | 5,2 |
| . I3I | . 38802 | 171 | . 71073 | 139 | .8is 36 | 34,2 | . 2325 | 5,2 |
| . 132 | - 38973 | 171 | . 71212 | 139 | .8il70 | $34, \mathrm{I}$ | . 2320 | 5,2 |
| . 133 | . 39145 | I7 I | .71351 | 139 | . 81204 | 34, I | .2315 | 5,2 |
| . 134 | . 39316 | 171 | . 71490 | 139 | .81238 | 34,0 | . 2309 | 5,2 |
| I. 135 | I. 39488 | 172 | 1.71630 | I39 | 0.81272 | 33,9 | I. 2304 | 5, I |
| . 136 | . 39559 | 172 | . 71769 | 140 | .81306 | 33,9 | . 2299 | 5, I |
| . 137 | . 39831 | 172 | . 71909 | 140 | . SI 340 | 33,8 | . 2294 | 5, I |
| . 138 | . 40003 | 172 | . 72049 | 140 | . 81374 | 33,8 | . 2289 | 5,I |
| . 139 | . 40175 | 172 | . 72189 | 140 | .8I408 | 33,7 | . 2284 | 5, I |
| I. 140 | I. 40347 | 172 | 1.72329 | 140 | 0.81441 | 33,7 | 1. 2279 | 5, I |
| . 141 | . 40520 | 172 | . 72470 | 141 | .81475 | 33,6 | . 2274 | 5, I |
| . 142 | . 40692 | 173 | . 72610 | I4I | .81509 | 33,6 | . 2269 | 5, I |
| . I43 | . 40855 | 173 | . 72751 | 141 | . 81542 | 33,5 | . 2264 | 5,0 |
| . 144 | . 41038 | 173 | . 72892 | 14 I | .81576 | 33,5 | . 2259 | 5,0 |
| I. I45 | I.412II | 173 | I. 73033 | 141 | 0.81609 | 33,4 | 1. 2254 | 5,0 |
| . 146 | . 41384 | 173 | . 73175 | 141 | . 81642 | 33,3 | . 2249 | 5,0 |
| . 147 | . 41557 | 173 | . 73316 | 142 | . 81676 | 33,3 | . 2244 | 5,0 |
| . 148 | .4173I | 173 | . 73458 | 142 | . 81709 | 33,2 | . 2239 | 5,0 |
| . 149 | . 41904 | 174 | . 73599 | 142 | .81742 | 33,2 | . 2234 | 5,0 |
| I. 150 | I. 42078 | I74 | I.7374I | 142 | 0.81775 | 33,1 | I .2229 | 5,0 |
| $u$ | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 150 | I. 42078 | 174 | 1.73741 | - 142 | 0.81775 | 33, I | I. 2229 | 5,0 |
| . 151 | . 42252 | 174 | . 73884 | 142 | .81809 | 33,I | . 2224 | 4,9 |
| . 152 | . 42426 | 174 | . 74026 | 142 | .81842 | 33,0 | . 2219 | 4,9 |
| . 153 | . 42600 | 174 | .74168 | 143 | .81875 | 33,0 | . 2214 | 4,9 |
| . 154 | . 42774 | 174 | . 74311 | 143 | .81907 | 32,9 | . 2209 | 4,9 |
| 1. 155 | 1. 42948 | 174 | I. 74454 | 143 | 0.81940 | 32,9 | 1.2204 | 4,9 |
| . 156 | . 43123 | 175 | . 74597 | 143 | . 81973 | 32,8 | . 2199 | 4,9 |
| . 157 | . 43297 | 175 | . 74740 | 143 | . 82006 | 32,8 | . 2194 | 4,9 |
| . 158 | . 43472 | 175 | . 74884 | 143 | . 82039 | 32,7 | . 2189 | 4,9 |
| . 159 | . 43647 | 175 | . 75027 | 144 | . 82071 | 32,6 | . 2185 | 4,8 |
| I. 160 | I. 43822 | I75 | I.75171 | 144 | 0.82104 | 32,6 | 1.2180 | 4,8 |
| .16I | . 43998 | 175 | . 75315 | 144 | .82137 | 32,5 | . 2175 | 4,8 |
| . 162 | . 44173 | 175 | . 75459 | 144 | . 82169 | 32,5 | . 2170 | 4,8 |
| . 163 | . 44349 | 176 | . 75603 | 144 | . 82202 | 32,4 | . 2165 | 4,8 |
| . 164 | . 44524 | 176 | . 75748 | 145 | . 82234 | 32,4 | . 2160 | 4,8 |
| 1. 165 | I. 44700 | 176 | 1.75892 | 145 | 0.82266 | 32,3 | I. 2156 | 4,8 |
| . 166 | . 44876 | 176 | . 76037 | 145 | . 82299 | 32,3 | . 2151 | 4,8 |
| . 167 | . 45052 | 176 | . 76182 | 145 | . 82331 | 32,2 | . 2146 | 4,8 |
| . 168 | . 45228 | 176 | . 76327 | 145 | . 82363 | 32,2 | .2141 | 4,7 |
| . 169 | . 45405 | 176 | . 76472 | 145 | . 82395 | 32,I | . 2137 | 4,7 |
| 1.170 | I.4558I | 177 | 1.76618 | 146 | 0.82427 | 32,I | I. 2132 | 4,7 |
| -171 | . 45758 | 177 | . 76764 | 146 | . 82459 | 32,0 | . 2127 | 4,7 |
| . 172 | . 45935 | 177 | . 76909 | 146 | . 82491 | 32,0 | . 2123 | 4,7 |
| . 173 | .461 12 | 177 | . 77056 | 146 | . 82523 | $3 \mathrm{I}, 9$ | . 21 I8 | 4,7 |
| . 174 | . 46289 | 177 | . 77202 | 146 | . 82555 | 31,8 | . 2113 | 4,7 |
| I. 175 | I. 46466 | 177 | 1. 77348 | 146 | 0.82587 . | 31,8 | 1. 2108 | 4,7 |
| . 176 | . 46644 | 177 | . 77495 | 147 | . 82619 | $3 \mathrm{I}, 7$ | . 2104 | 4,7 |
| . 177 | . 46821 | 178 | . 77641 | 147 | . 82650 | 31,7 | . 2099 | 4,6 |
| . 178 | . 46999 | 178 | . 77788 | 147 | . 82682 | 31,6 | . 2095 | 4,6 |
| . 179 | . 47 I 77 | 178 | . 77935 | 147 | .82714 | 31,6 | . 2090 | 4,6 |
| 1.180 | 1. 47355 | 178 | 1.78083 | 147 | 0.82745 | 31,5 | I. 2085 | 4,6 |
| . 18 I | . 47533 | 178 | . 78230 | 148 | . 82777 | 31,5 | .208I | 4,6 |
| . 182 | .4771 | 178 | . 78378 | 148 | . 82808 | 3I,4 | . 2076 | 4,6 |
| .183 | . 47890 | 179 | . 78525 | 148 | . 82840 | $3 \mathrm{I}, 4$ | .2072 | 4,6 |
| . 184 | . 48068 | 179 | . 78673 | 148 | .82871 | 31,3 | . 2067 | 4,6 |
| I. 185 | I. 48247 | 179 | 1.78822 | 148 | 0.82902 | 3I,3 | 1. 2062 | 4,6 |
| . 186 | . 48426 | 179 | . 78970 | 148 | . 82933 | $3 \mathrm{I}, 2$ | . 2058 | 4,5 |
| . 187 | . 48605 | 179 | . 79119 | 149 | . 82965 | $3 \mathrm{I}, 2$ | . 2053 | 4,5 |
| . 188 | . 48784 | 179 | . 79267 | 149 | . 82996 | $3 \mathrm{I}, \mathrm{I}$ | . 2049 | 4,5 |
| . 189 | . 48964 | 179 | .79416 | 149 | .83027 | 3I, I | . 2044 | 4,5 |
| 1. 190 | I. 49143 | 180 | 1.79565 | 149 | 0.83058 | 31,0 | 1. 2040 | 4,5 |
| . 191 | . 49323 | 180 | . 79714 | 149 | . 83089 | 31,0 | . 2035 | 4,5 |
| . 192 | . 49502 | 180 | . 79864 | 150 | . 83120 | 30,9 | . 2031 | 4,5 |
| . 193 | . 49682 | 180 | . 80013 | 150 | .8315I | 30,9 | . 2026 | 4.5 |
| . 194 | . 49862 | 180 | . 80163 | 150 | . 83182 | 30,8 | . 2022 | 4,5 |
| I. 195 | 1.50043 | 180 | 1.80313 | 150 | 0.83212 | 30,8 | 1.2017 | 4,4 |
| . 196 | . 50223 | 180 | . 80463 | 150 | . 83243 | 30,7 | . 2013 | 4,4 |
| . 197 | . 50404 | 18 I | . 80614 | 150 | . 83274 | 30,7 | . 2009 | 4,4 |
| . 198 | . 50584 | 18 I | . 80764 | 151 | . 83304 | 30,6 | . 2004 | 4,4 |
| . 199 | . 50765 | 181 | . 80915 | 151 | . 83335 | 30,6 | . 2000 | 4,4 |
| 1.200 | I. 50946 | 181 | 1.81066 | 151 | 0.83365 | 30,5 | I. 1995 | 4,4 |
| 4 | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.200 | 1. 50946 | 181 | 1.81066 | 15 I | 0.83355 | 30,5 | I. 1995 | 4,4 |
| . 201 | . 51127 | I8I | . 812 I 7 | 151 | . 83396 | 30,5 | . 1991 | 4,4 |
| . 202 | . 51309 | 181 | .81368 | 151 | . 83426 | 30,4 | . 1987 | 4,4 |
| . 203 | . 51490 | 182 | .81519 | 151 | . 83457 | 30,3 | . 1982 | 4,4 |
| . 204 | . 51672 | 182 | .81671 | 152 | . 83487 | 30,3 | . 1978 | 4,3 |
| 1.205 | 1. 51853 | 182 | 1.81823 | 152 | 0.83517 | 30,2 | I. 1974 | 4,3 |
| . 206 | . 52035 | 182 | .81974 | 152 | . 83548 | 30,2 | . 1969 | 4,3 |
| . 207 | . 52217 | 182 | . 82127 | 152 | . 83578 | 30,1 | . 1965 | 4,3 |
| . 208 | . 52400 | 182 | . 82279 | 152 | . 83608 | 30,1 | . 1961 | 4,3 |
| . 209 | . 52582 | 182 | . 8243 I | 153 | . 83538 | 30,0 | . 1956 | 4,3 |
| 1.210 | 1. 52764 | 183 | 1.82584 | 153 | 0.83668 | 30,0 | I. 1952 | 4,3 |
| . 211 | . 52947 | 183 | . 82737 | ${ }^{1} 53$ | . 83698 | 29,9 | . 1948 | 4,3 |
| . 212 | . 53130 | 183 | . 82890 | 153 | . 83728 | 29,9 | . 1943 | 4,3 |
| .213 | . 53313 | 183 | . 83043 | 153 | . 83758 | 29,8 | . 1939 | 4,3 |
| . 214 | . 53496 | 183 | . 83197 | 153 | . 83788 | 29,8 | . 1935 | 4,2 |
| 1.215 | 1. 53679 | 183 | 1.83350 | 154 | 0.83817 | 29,7 | I. 193I | 4,2 |
| . 216 | . 53863 | 184 | . 83504 | 154 | . 83847 | 29,7 | . 1926 | 4,2 |
| . 217 | . 54046 | 184 | . 83658 | 154 | . 83877 | 29,6 | . 1922 | 4,2 |
| . 218 | . 54230 | 184 | . 83812 | 154 | . 83906 | 29,6 | . 1918 | 4,2 |
| . 219 | . 54414 | 184 | . 83966 | 154 | . 83936 | 29,5 | . 1914 | 4,2 |
| 1.220 | I. 54598 | 184 | I. 8412 I | 155 | 0.83965 | 29,5 | I. 1910 | 4,2 |
| . 22 I | . 54782 | 184 | . 84276 | 155 | . 83995 | 29,4 | . 1905 | -4,2 |
| . 222 | . 54966 | 184 | . 84430 | 155 | . 84024 | 29,4 | . 1901 | 4,2 |
| .223 | . 55151 | 185 | . 84586 | 155 | . 84054 | 29,3 | . 1897 | 4,2 |
| . 224 | . 55336 | 185 | . 84741 | 155 | . 84083 | 29,3 | . 1893 | 4, I |
| I. 225 | I. 55520 | 185 | 1. 84896 | 156 | 0.84112 | 29,3 | I. 1889 | 4,I |
| . 226 | . 55705 | 185 | . 85052 | 156 | . 84142 | 29,2 | . 1885 | 4, I |
| . 227 | . 55891 | 185 | . 85208 | 156 | .84I7I | 29,2 | . I88I | 4, I |
| . 228 | . 56076 | 185 | . 85364 | 156 | . 84200 | 29, I | . 1877 | 4, I |
| . 229 | . 5626 I | 186 | . 85520 | 156 | . 84229 | 29,1 | . 1872 | 4, I |
| I. 230 | I. 56447 | 186 | I. 85676 | 156 | 0.84258 | 29,0 | I. 1868 | 4, I |
| . 231 | . 56633 | 186 | . 85833 | 157 | . 84287 | 29,0 | . 1864 | 4, I |
| . 232 | . 568 I9 | 186 | . 85989 | 157 | . 84316 | 28,9 | . 1860 | 4, I |
| . 233 | . 57005 | 186 | . 86146 | 157 | . 84345 | 28,9 | . 1856 | 4, I |
| . 234 | . 57191 | 186 | . 86303 | 157 | . 84374 | 28,8 | . 1852 | 4, I |
| I. 235 | 1. 57377 | 186 | I. 86461 | 157 | 0.84402 | 28,8 | I. 1848 | 4,0 |
| . 236 | . 57564 | 187 | . 86618 | 158 | . 84431 | 28,7 | . I844 | 4,0 |
| .237 | . 57750 | 187 | . 86776 | 158 | . 84460 | 28,7 | . 1840 | 4,0 |
| . 238 | . 57937 | 187 | . 86934 | 158 | . 84488 | 28,6 | . 1836 | 4,0 |
| . 239 | . 58124 | 187 | . 87092 | 158 | . 84517 | 28,6 | . 1832 | 4,0 |
| I. 240 | I. 583 II | 187 | 1. 87250 | 158 | 0.84546 | 28,5 | I. 1828 | 4,0 |
| . 241 | . 58499 | 187 | . 87408 | 158 | . 84574 | 28,5 | . 1824 | 4,0 |
| . 242 | . 58686 | 188 | . 87567 | 159 | . 84602 | 28,4 | . 1820 | 4,0 |
| .243 | . 58874 | 188 | . 87726 | 159 | . 84631 | 28,4 | . 1816 | 4,0 |
| . 244 | . 59062 | 188 | . 87885 | 159 | . 84659 | 28,3 | . 1812 | 4,0 |
| I. 245 | I. 59250 | 188 | 1. 88044 | 159 | 0.84688 | 28,3 | 1. 1808 | 3,9 |
| . 246 | . 59438 | 188 | . 88203 | 159 | . 84716 | 28,2 | . 1804 | 3,9 |
| . 247 | . 59626 | 188 | . 88363 | 160 | . 84744 | 28,2 | . 1800 | 3,9 |
| . 248 | . 59815 | 189 | . 88522 | 160 | . 84772 | 28, 1 | . 1796 | 3,9 |
| . 249 | . 60003 | 189 | . 88682 | 160 | . 84800 | 28, I | . 1792 | 3,9 |
| I 250 | 1.60192 | 189 | 1.88842 | 160 | 0.84828 | 28,0 | 1.1789 | 3,9 |
| u | $\boldsymbol{t a n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}$. | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 250 | 1.60192 | 189 | 1. 88842 | 160 | 0.84828 | 28,0 | I. 1789 | 3,9 |
| .25I | .6038I | 189 | . 89003 | 160 | . 84856 | 28,0 | . 1785 | 3,9 |
| . 252 | . 60570 | 189 | . 89163 | 161 | . 84884 | 27,9 | . 1781 | 3,9 |
| . 253 | . 60759 | 189 | . 89324 | 161 | . 84912 | 27,9 | . 1777 | 3,9 |
| . 254 | . 60949 | 189 | . 89485 | 161 | . 84940 | 27,9 | . 1773 | 3,9 |
| I. 255 | 1.61138 | 190 | 1.89646 | 161 | 0.84968 | 27,8 | 1. 1769 | 3,9 |
| . 256 | . 61328 | 190 | . 89807 | 161 | . 84996 | 27,8 | . 1765 | 3,8 |
| . 257 | . 61518 | 190 | . 89968 | 162 | . 85023 | 27,7 | . 1761 | 3,8 |
| . 258 | .61708 | 190 | .90130 | 162 | . 85051 | 27,7 | . 1758 | 3,8 |
| . 259 | . 61898 | 190 | . 90292 | 162 | . 85079 | 27,6 | . I754 | 3,8 |
| 1. 260 | 1.62088 | 190 | I. 90454 | 162 | 0.85106 | 27,6 | I. 1750 | 3,8 |
| . 261 | . 62279 | I9I | . 90616 | 162 | . 85134 | 27,5 | . 1746 | 3,8 |
| . 262 | . 62470 | I9I | . 90778 | 162 | .85161 | 27,5 | . 1742 | 3,8 |
| . 263 | . 6266 I | I9I | .9094I | 163 | . 85189 | 27,4 | . I739 | 3,8 |
| . 264 | . 62851 | 19I | .91104 | 163 | . 85216 | 27,4 | . I735 | 3,8 |
| 1. 265 | 1.63043 | 191 | 1.91267 | 163 | 0.85244 | 27,3 | 1.173I | 3,8 |
| . 266 | . 63234 | 191 | . 91430 | 163 | .8527I | 27,3 | .1727 | 3,8 |
| . 267 | . 63426 | 192 | .91593 | 163 | . 85298 | 27,2 | . 1724 | 3,7 |
| . 268 | . 63617 | 192 | .91757 | 164 | . 85325 | 27,2 | . I720 | 3,7 |
| . 269 | . 63809 | 192 | . 91920 | 164 | . 85353 | 27, I | . 1716 | 3,7 |
| 1.270 | 1.64001 | 192 | 1.92084 | 164 | 0.85380 | 27,I | I. I7I2 | 3,7 |
| . 27 I | . 64193 | 192 | . 92248 | 164 | . 85407 | 27,I | . I709 | 3,7 |
| . 272 | . 64386 | 192 | .92413 | 164 | . 85434 | 27,0 | . 1705 | 3,7 |
| . 273 | . 64578 | 193 | . 92577 | 165 | .8546I | 27,0 | . 1701 | 3,7 |
| . 274 | . 64771 | 193 | . 92742 | 165 | . 85488 | 26,9 | . 1698 | 3,7 |
| 1.275 | I. 64964 | 193 | I. 92907 | 165 | 0.85515 | 26,9 | I. 1694 | 3,7 |
| . 276 | . 65157 | 193 | . 93072 | 165 | . 85542 | 26,8 | . 1690 | 3,7 |
| . 277 | . 65350 | 193 | . 93237 | 165 | . 85568 | 26,8 | . 1687 | 3,7 |
| . 278 | . 65543 | 193 | . 93402 | 166 | . 85595 | 26,7 | . 1683 | 3,6 |
| . 279 | . 65736 | 194 | . 93568 | 166 | . 85622 | 26,7 | . 1679 | 3,6 |
| 1.280 | 1. 65930 | 194 | I. 93734 | 166 | 0.85648 | 26,6 | 1. 1676 | 3,6 |
| .28I | . 66124 | 194 | . 93900 | 166 | . 85675 | 26,6 | . 1672 | 3,6 |
| . 282 | .66318 | 194 | . 94066 | 166 | . 85702 | 26,6 | . 1568 | 3,6 |
| .283 | . 66512 | 194 | . 94233 | 167 | . 85728 | 26,5 | . 1665 | 3,6 |
| . 284 | . 66706 | 194 | . 94399 | 167 | . 85755 | 26,5 | . 1661 | 3,6 |
| I. 285 | 1.66901 | 195 | 1.94566 | 167 | 0.8578 I | 26,4 | 1. 1658 | 3,6 |
| . 286 | . 67096 | 195 | . 94733 | 167 | . 85808 | 26,4 | . 1654 | 3,6 |
| . 287 | . 67290 | 195 | . 94900 | 167 | . 85834 | 26,3 | . 1650 | 3,6 |
| . 288 | .67485 | 195 | . 95068 | 167 | . 85860 | 26,3 | . 1647 | 3,6 |
| . 289 | . 67680 | 195 | . 95235 | 168 | . 85886 | 26,2 | . 1643 | 3,6 |
| 1.290 | 1.67876 | 195 | 1.95403 | 168 | 0.85913 | 26,2 | I. 1640 | 3,5 |
| . 291 | . 68071 | 196 | . 95571 | 168 | . 85939 | 26,1 | . 1636 | 3,5 |
| . 292 | . 68267 | 196 | . 95739 | 168 | . 85965 | 26,1 | . I633 | 3,5 |
| . 293 | . 68463 | 196 | . 95907 | 168 | . 85991 | 26,1 | . 1629 | 3,5 |
| . 294 | . 68659 | 196 | . 96076 | 169 | .86017 | 26,0 | . 1626 | 3,5 |
|  | 1. 68855 | 196 | 1.96245 | 169 | 0.86043 | 26,0 | 1. 1622 | 3,5 |
| . 296 | . 69051 | 196 | . 96414 | 169 | . 86069 | 25,9 | . 1619 | 3,5 |
| . 297 | . 69248 | 197 | .96583 | 169 | . 86095 | 25,9 | . I6I5 | 3,5 |
| . 298 | . 69444 | 197 | . 96752 | 169 | .86I2I | 25,8 | . 1612 | 3,5 |
| . 299 | . 69641 | 197 | . 96922 | 170 | . 86147 | 25,8 | . 1608 | 3,5 |
| 1.300 | I. 69838 | 197 | 1.97091 | 170 | 0.86172 | 25,7 | 1.1005 | 3,5 |
| $u$ | $\boldsymbol{t a n} \mathrm{g} \mathrm{d} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{c s c} \boldsymbol{g d} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.300 | I. 69838 | 197 | 1.97091 | 170 | 0.86172 | 25,7 | 1.1605 | 3,5 |
| . 301 | . 70035 | 197 | .9726I | 170 | .85i98 | 25,7 | . Ifoi | 3,5 |
| - 302 | . 70233 | 197 | .9743I | 170 | . 86224 | 25,7 | . 1598 | 3,5 |
| . 303 | . 70430 | 198 | . 97602 | 170 | . 86249 | 25,6 | . I594 | 3,4 |
| . 304 | . 70628 | 198 | . 97772 | 171 | . 86275 | 25,6 | . I59I | 3,4 |
| 1.305 | I. 70826 | 198 | I. 97943 | 171 | 0.86300 | 25,5 | 1. 1587 | 3,4 |
| . 306 | . 71024 | 198 | .98II4 | 171 | . 86326 | 25,5 | . 1584 | 3,4 |
| . 307 | . 71222 | 198 | . 98285 | 171 | .8635I | 25,4 | . 158 I | 3,4 |
| . 308 | . 71420 | 198 | . 98456 | 171 | . 86377 | 25,4 | . 1577 | 3,4 |
| . 309 | .71619 | 199 | . 98628 | 172 | . 86402 | 25,3 | . 1574 | 3,4 |
| 1.310 | 1.718I8 | 199 | 1.98800 | 172 | 0.86428 | 25,3 | I. 1570 | 3,4 |
| . 311 | . 72017 | 199 | . 98972 | 172 | . 86453 | 25,3 | . 1567 | 3,4 |
| . 312 | . 72216 | 199 | .99I44 | 172 | . 86478 | 25,2 | . 1564 | 3,4 |
| . 313 | . 72415 | 199 | . 99316 | 172 | . 85503 | 25,2 | . 1560 | 3,4 |
| . 314 | . 72614 | 199 | . 99489 | 173 | . 86528 | 25, I | . 1557 | 3,4 |
| 1.315 | 1.72814 | 200 | I.9966I | 173 | 0.86554 | 25, I | I. 1554 | 3,3 |
| . 316 | . 73014 | 200 | . 99834 | 173 | . 86579 | 25,0 | . 1550 | 3,3 |
| . 317 | . 73214 | 200 | 2.00007 | 173 | . 86604 | 25,0 | . 1547 | 3,3 |
| . 318 | .73414 | 200 | .0018I | 173 | . 86629 | 25,0 | . 1544 | 3,3 |
| . 319 | .73614 | 200 | . 00354 | 174 | . 86653 | 24,9 | . I540 | 3,3 |
| 1.320 | 1.73814 | 201 | 2.00528 | 174 | 0.85578 | 24,9 | I. 1537 | 3,3 |
| . 321 | . 74015 | 201 | . 00702 | 174 | . 85703 | 24,8 | . I534 | 3,3 |
| . 322 | . 74216 | 201 | . 00876 | 174 | . 85728 | 24,8 | . 1530 | 3,3 |
| . 323 | . 74417 | 201 | . 01050 | 174 | . 85753 | 24,7 | . 1527 | 3,3 |
| . 324 | . 74618 | 201 | . 01225 | 175 | . 85778 | 24,7 | . 1524 | 3,3 |
| 1.325 | I.74819 | 201 | 2.01399 | 175 | 0.85802 | 24,7 | 1. 1520 | 3,3 |
| . 326 | . 75021 | 202 | . 01574 | 175 | . 85827 | 24,6 | . 1517 | 3,3 |
| . 327 | . 75222 | 202 | . O1749 | 175 | .85851 | 24,6 | . 1514 | 3,3 |
| . 328 | . 75424 | 202 | . 01925 | 175 | . 86876 | 24,5 | . I5II | 3,2 |
| . 329 | . 75626 | 202 | .02100 | 176 | . 86900 | 24,5 | . 1507 | 3,2 |
| 1.330 | 1. 75828 | 202 | 2.02276 | 176 | 0.86925 | 24,4 | 1. 1504 | 3,2 |
| . 33 I | . 76031 | 202 | . 02452 | 176 | . 86949 | 24,4 | . 1501 | 3,2 |
| . 332 | . 76233 | 203 | . 02628 | 175 | . 86974 | 24,4 | . I498 | 3,2 |
| . 333 | . 76436 | 203 | . 02804 | 175 | . 86998 | 24,3 | . I495 | 3,2 |
| . 334 | . 76639 | 203 | .0298I | I77 | . 87022 | 24,3 | . I49I | 3,2 |
| I. 335 | 1.76842 | 203 | 2.03158 | 177 | 0.87047 | 24,2 | I. I488 | 3,2 |
| . 336 | . 77045 | 203 | . 03335 | 177 | . 87071 | 24,2 | . I485 | 3,2 |
| . 337 | . 77249 | 204 | .03512 | 177 | . 87095 | 24, I | . I482 | 3,2 |
| . 338 | . 77452 | 204 | . 03689 | 177 | .87II9 | 24, I | . 1479 | 3,2 |
| . 339 | . 77656 | 204 | . 03867 | 178 | . 87143 | 24, I | . 1475 | 3,2 |
| I. 340 | I. 77860 | 204 | 2.04044 | 178 | 0.87167 | 24,0 | I. 1472 | 3,2 |
| . 341 | . 78064 | 204 | . 04222 | 178 | . 87191 | 24,0 | . 1469 | 3,2 |
| . 342 | . 78268 | 204 | . 04401 | 178 | . 87215 | 23,9 | . 1466 | 3 3, |
| . 343 | . 78473 | 205 | . 04579 | 178 | . 87239 | 23,9 | . I463 | 3 , 1 |
| . 344 | . 78677 | 205 | . 04758 | 179 | . 87263 | 23,9 | . 1460 | 3, I |
|  | 1. 78882 | 205 | 2.04936 | 179 | 0.87287 | 23,8 | I. 1456 | 3, I |
| . 346 | . 79087 | 205 | .05115 | 179 | . 8731 I | 23,8 | . I453 | 3 , 1 |
| . 347 | . 7929.3 | 205 | . 05294 | 179 | . 87334 | 23,7 | . I450 | 3, I |
| . 348 | . 79498 | 205 | . 05474 | 179 | . 87358 | 23,7 | . 1447 | 3,1 |
| - 349 | . 79704 | 206 | . 05653 | 180 | . 87382 | 23,6 | . I444 | 3,1 |
| I. 350 | I. 79909 | 206 | 2.05833 | 180 | 0.87405 | 23,6 | I. 1441 | 3, 1 |
| u | $\tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 350 | 1. 79909 | 206 | 2.05833 | 180 | 0.87405 | 23,6 | I. 1441 | 3, I |
| . 351 | . 80115 | 206 | .06013 | 180 | . 87429 | 23,6 | . 1438 | 3,1 |
| . 352 | . 8032 I | 206 | . 06194 | 180 | . 87452 | 23,5 | . I435 | 3, I |
| . 353 | . 80528 | 206 | . 06374 | 18 I | . 87476 | 23,5 | . I432 | 3,I |
| . 354 | . 80734 | 207 | . 06555 | I8I | . 87499 | 23,4 | . I429 | 3,I |
| I. 355 | I. 80941 | 207 | 2.06735 | 181 | 0.87523 | 23,4 | I. 1426 | 3,1 |
| . 356 | .81148 | 207 | . 06916 | I8I | . 87546 | 23,4 | . 1423 | 3,0 |
| . 357 | .81355 | 207 | . 07098 | 18 I | . 87570 | 23,3 | .1419 | 3,0 |
| . 358 | . 81562 | 207 | . 07279 | 182 | . 87593 | 23,3 | .1416 | 3,0 |
| . 359 | .81769 | 207 | . 0746 I | 182 | . 87616 | 23,2 | . I4I3 | 3,0 |
| I. 360 | 1.81977 | 208 | 2.07643 | 182 | 0.87639 | 23,2 | 1. 1410 | 3,0 |
| . 361 | . 82184 | 208 | . 07825 | 182 | . 87662 | 23,2 | . 1407 | 3,0 |
| . 362 | . 82392 | 208 | . 08007 | 182 | . 87686 | 23, I | . I404 | 3,0 |
| . 363 | . 82600 | 208 | .08190 | 183 | . 87709 | 23,1 | . I40I | 3,0 |
| .364 | . 82809 | 208 | . 08372 | 183 | . 87732 | 23,0 | . 1398 | 3,0 |
| 1. 365 | 1.83017 | 209 | 2.08555 | 183 | 0.87755 | 23,0 | I. I395 | 3,0 |
| . 366 | . 83226 | 209 | . 08738 | 183 | . 87778 | 23,0 | . 1392 | 3,0 |
| . 367 | . 83435 | 209 | . 08922 | 183 | . 87801 | 22,9 | . I389 | 3,0 |
| . 368 | . 83644 | 209 | . 09105 | 184 | . 87824 | 22,9 | . 1386 | 3,0 |
| .369 | . 83853 | 209 | . 09289 | 184 | . 87846 | 22,8 | . I384 | 3,0 |
| 1.370 | 1. 84062 | 209 | 2.09473 | 184 | 0.87869 | 22,8 | I. 1381 | 3,0 |
| . 371 | . 84272 | 210 | . 09657 | 184 | . 87892 | 22,7 | . 1378 | 2,9 |
| . 372 | . 84482 | 210 | . 09841 | 184 | . 87915 | 22,7 | . I375 | 2,9 |
| . 373 | . 84691 | 210 | . 10026 | 185 | . 87937 | 22,7 | . I372 | 2,9 |
| . 374 | . 84902 | 210 | . 102 I I | 185 | . 87960 | 22,6 | . I369 | 2,0 |
| 1.375 | 1.85112 | 210 | 2. 10396 | 185 | 0.87983 | 22,6 | 1. 1366 | 2,9 |
| . 376 | . 85322 | 211 | . 10581 | 185 | . 88005 | 22,6 | . I363 | 2,9 |
| . 377 | . 85533 | 2 II | . 10766 | 186 | . 88028 | 22,5 | . 1360 | 2,9 |
| . 378 | . 85744 | 2 II | . 10952 | 186 | . 88050 | 22,5 | . I357 | 2,9 |
| . 379 | . 85955 | 2 II | . III38 | 186 | . 88073 | 22,4 | . I354 | 2,9 |
| 1.380 | 1.86166 | 2II | 2. II324 | 186 | 0.88095 | 22,4 | I. I351 | 2,9 |
| . 381 | . 86378 | 212 | . II510 | 186 | .88117 | 22,4 | . I348 | 2,9 |
| . 382 | . 86589 | 212 | . II697 | 187 | .88I40 | 22,3 | . I346 | 2,9 |
| . 383 | . 85801 | 212 | . 11883 | 187 | .88162 | 22,3 | . I343 | 2,9 |
| . 384 | . 87013 | 212 | . 12070 | 187 | .88I84 | 22,2 | . I340 | 2,9 |
| I. 385 | 1.87225 | 212 | 2.12257 | 187 | 0.88207 | 22,2 | I. 1337 | 2,9 |
| . 386 | . 87437 | 212 | . 12445 | 187 | . 88229 | 22,2 | . I334 | 2,8 |
| . 387 | . 87650 | 213 | . 12632 | 188 | . 8825 I | 22, I | . 1331 | 2,8 |
| . 388 | . 87863 | 213 | . 12820 | 188 | . 88273 | 22,I | . I328 | 2,8 |
| . 389 | . 88076 | 213 | . 13008 | 188 | . 88295 | 22,0 | . 1326 | 2,8 |
| 1.390 | 1. 88289 | 213 | 2.13196 | 188 | 0.88317 | 22,0 | I. 1323 | 2,8 |
| . 391 | . 88502 | 213 | . 13385 | 189 | . 88339 | 22,0 | . 1320 | 2,8 |
| . 392 | . 88716 | 214 | . 13573 | 189 | .8836I | 21,9 | .1317 | 2,8 |
| - 393 | . 88929 | 214 | . 13762 | 189 | . 88383 | 21,9 | -I314 | 2,8 |
| - 394 | . 89143 | 214 | . 13951 | 189 | . 88405 | 21,8 | . 1312 | 2,8 |
| I . 395 | 1. 89357 | 214 | 2.14I40 | I89 | 0.88427 | 21,8 | 1. 1309 | 2,8 |
| . 396 | . 89571 | 214 | . 14330 | 190 | . 88448 | 21,8 | . 1306 | 2,8 |
| . 397 | . 89786 | 215 | . I4520 | 190 | . 88470 | 21,7 | . 1303 | 2,8 |
| . 398 | . 90000 | 215 | . 14709 | 190 | . 88492 | 21,7 | . 1300 | 2,8 |
| - 399 | . 90215 | 215 | . 14900 | 190 | . 88513 | 21,7 | . 1298 | 2,8 |
| I. 400 | I. 90430 | 215 | 2.15090 | 190 | 0.88535 | 21,6 | I. 1295 | 2,8 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sin \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{Fo}^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text {o }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.400 | 1.90430 | 215 | 2.15090 | 190 | 0.88535 | 21,6 | I. 1295 | 2,8 |
| . 401 | . 90645 | 215 | . 15280 | 191 | . 88557 | 21,6 | . 1292 | 2,8 |
| . 402 | . 90861 | 215 | . 15471 | 191 | . 88578 | 21,5 | . 1289 | 2,7 |
| . 403 | . 91076 | 216 | . 15662 | 191 | . 88600 | 21,5 | . 1287 | 2,7 |
| . 404 | . 91292 | 216 | . 15853 | 191 | . 8852 I | 21,5 | . 1284 | 2,7 |
| 1. 405 | 1.91508 | 216 | 2.16045 | 192 | 0.88643 | 21,4 | I. 128 I | 2,7 |
| . 406 | . 91724 | 216 | . 16236 | 192 | . 88564 | 21,4 | . 1279 | 2,7 |
| . 407 | . 91940 | 216 | . 16428 | 192 | . 88686 | 21,3 | . 1276 | 2,7 |
| . 408 | . 92157 | 217 | . 16620 | 192 | . 88707 | 21,3 | . 1273 | 2,7 |
| . 409 | . 92374 | 217 | . 16812 | 192 | . 88728 | 21,3 | . 1270 | 2,7 |
| I.410 | 1.92591 | 217 | 2.17005 | 193 | 0.88749 | 21,2 | 1. 1268 | 2,7 |
| . 411 | . 92808 | 217 | . 17198 | 193 | . 88771 | 21,2 | . 1265 | 2,7 |
| .412 | . 93025 | 217 | . 17391 | 193 | . 88792 | 21,2 | . 1262 | 2,7 |
| . 413 | . 93242 | 218 | . 17584 | 193 | . 88813 | 21,1 | . 1260 | 2,7 |
| . 414 | . 93460 | 218 | . 17777 | 193 | . 88834 | 21,1 | . 1257 | 2,7 |
| I.415 | 1.93678 | 218 | 2.17971 | 194 | 0.88855 | 21,0 | 1.1254 | 2,7 |
| . 416 | . 93896 | 218 | . 18164 | 194 | . 88876 | 21,0 | . 1252 | 2,7 |
| . 417 | . 94114 | 218 | . 18358 | 194 | . 88897 | 21,0 | . 1249 | 2,7 |
| . 418 | . 94333 | 219 | . 18553 | 194 | . 88918 | 20,9 | . 1246 | 2,6 |
| . 419 | .94551 | 219 | . 18747 | 195 | . 88939 | 20,9 | . 1244 | 2,6 |
| 1. 420 | 1.94770 | 219 | 2. 18942 | 195 | 0.88960 | 20,9 | 1. 1241 | 2,6 |
| . 421 | . 94989 | 219 | . 19137 | 195 | . 88981 | 20,8 | .1238 | 2,6 |
| . 422 | . 95209 | 219 | . 19332 | 195 | . 89002 | 20,8 | . 1236 | 2,6 |
| 423 | . 95428 | 220 | - 19527 | 195 | . 89022 | 20,8 | . 1233 | 2,6 |
| . 424 | . 95648 | 220 | . 19723 | 196 | . 89043 | 20,7 | . 1231 | 2,6 |
| 1.425 | 1.95867 | 220 | 2. 19918 | 196 | 0.89064 | 20,7 | 1. 1228 | 2,6 |
| . 426 | . 96087 | 220 | . 20114 | 196 | . 89084 | 20,6 | . 1225 | 2,6 |
| . 427 | . 96308 | 220 | . 20310 | 196 | . 89105 | 20,6 | . 1223 | 2,6 |
| . 428 | . 96528 | 221 | . 20507 | 197 | . 89126 | 20,6 | . 1220 | 2,6 |
| . 429 | . 96749 | 221 | . 20704 | 197 | . 89146 | 20,5 | . 1218 | 2,6 |
| I. 430 | 1.96970 | 221 | 2.20900 | 197 | 0.89167 | 20,5 | 1.1215 | 2,6 |
| .431 | .97191 | 221 | . 21097 | 197 | . 89187 | 20,5 | .1212 | 2,6 |
| . 432 | . 97412 | 221 | . 21295 | 197 | . 89208 | 20,4 | . 1210 | 2,6 |
| . 433 | . 97633 | 221 | . 21492 | 198 | . 89228 | 20,4 | . 1207 | 2,6 |
| - 434 | . 97855 | 222 | . 21690 | 198 | . 89248 | 20,3 | . 1205 | 2,6 |
|  | 1.98076 | 222 | 2.21888 | 198 | 0.89269 | 20,3 | I. 1202 | 2,5 |
| . 436 | . 98298 | - 222 | . 22086 | 198 | . 89289 | 20,3 | . 1200 | 2,5 |
| . 437 | . 9852 I | 222 | . 22285 | 199 | . 89309 | 20,2 | . 1197 | 2,5 |
| . 438 | . 98743 | 222 | . 22483 | 199 | . 89329 | 20,2 | . 1195 | 2,5 |
| -439 | . 98966 | 223 | . 22682 | 199 | . 89350 | 20,2 | . 1192 | 2,5 |
| I. 440 | I. 99188 | 223 | 2.2288 I | 199 | 0.89370 | 20, I | 1. 1189 | 2,5 |
| .44I | . 9941 I | 223 | . 23080 | 199 | . 89390 | 20,1 | . 1187 | 2,5 |
| . 442 | . 99635 | 223 | . 23280 | 200 | . 89410 | 20,1 | . 1184 | 2,5 |
| . 443 | . 99858 | 223 | . 23480 | 200 | . 89430 | 20,0 | . 1182 | 2,5 |
| . 444 | 2.00082 | 224 | . 23680 | 200 | . 89450 | 20,0 | . 1179 | 2,5 |
| I. 445 | 2.00305 | 224 | 2.23880 | 200 | 0.89470 | 20,0 | I. 1177 | 2,5 |
| . 446 | . 00529 | 224 | . 24080 | 201 | . 89490 | 19,9 | . 1174 | 2,5 |
| . 447 | . 00753 | 224 | . 2428I | 201 | . 89510 | 19,9 | . 1172 | 2,5 |
| . 448 | . 00978 | 224 | . 24482 | 201 | . 89530 | 19,8 | . 1169 | 2,5 |
| . 449 | . 01202 | 225 | . 24683 | 201 | . 89550 | 19,8 | . 1167 | 2,5 |
| I. 450 | 2.01427 | 225 | 2.24884 | 201 | 0.89569 | 19,8 | 1.1165 | 2,5 |
| u | $\boldsymbol{t a n ~ g d ~ u ~}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{s i n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.450 | 2.01427 | 225 | 2.24884 | 201 | 0.89569 | 19,8 | 1. 1165 | 2,5 |
| .451 | . 01652 | 225 | . 25086 | 202 | . 89589 | 19,7 | . 1162 | 2,5 |
| . 452 | . 01877 | 225 | . 25288 | 202 | . 89609 | 19,7 | . 1160 | 2,5 |
| . 453 | . 02103 | 225 | . 25490 | 202 | . 89628 | 19,7 | . 1157 | 2,4 |
| . 454 | . 02328 | 226 | . 25692 | 202 | . 89648 | 19,6 | . 1155 | 2,4 |
| I. 455 | 2.02554 | 226 | 2.25894 | 203 | 0.89668 | 19,6 | I. II52 | 2,4 |
| . 456 | . 02780 | 226 | . 26097 | 203 | . 89687 | 19,6 | . 1150 | 2,4 |
| . 457 | . 03006 | 226 | . 26300 | 203 | . 89707 | 19,5 | . 1147 | 2,4 |
| . 458 | . 03233 | 227 | . 26503 | 203 | . 89726 | 19,5 | . II45 | 2,4 |
| . 459 | . 03459 | 227 | . 26706 | 203 | . 89746 | 19,5 | . II43 | 2,4 |
| 1. 460 | 2.03686 | 227 | 2.26910 | 204 | 0.89765 | 19,4 | I. 1140 | 2,4 |
| . 461 | . 03913 | 227 | .27114 | 204 | . 89785 | 19,4 | . 1138 | 2,4 |
| . 462 | . 04140 | 227 | . 27318 | 204 | . 89804 | 19,4 | . II35 | 2,4 |
| .463 | . 04368 | 228 | . 27522 | 204 | . 89823 | 19,3 | . II33 | 2,4 |
| . 464 | . 04595 | 228 | . 27726 | 205 | . 89843 | 19,3 | . II3 I | 2,4 |
| 1.465 | 2.04823 | 228 | 2.27931 | 205 | 0.89862 | 19,2 | I. 1128 | 2,4 |
| . 466 | .05051 | 228 | . 28136 | 205 | . 8988 I | 19,2 | . 1126 | 2,4 |
| . 467 | . 05280 | 228 | . 28341 | 205 | . 89900 | 19,2 | . II23 | 2,4 |
| . 468 | . 05508 | 229 | . 28547 | 206 | . 89920 | 19, I | . I121 | 2,4 |
| . 469 | . 05737 | 229 | . 28752 | 206 | . 89939 | 19, I | . III9 | 2,4 |
| 1.470 | 2.05965 | 229 | 2.28958 | 206 | 0.89958 | 19, 1 | I. 1116 | 2,4 |
| . 471 | . 06195 | 229 | . 29164 | 206 | . 89977 | 19,0 | . III4 | 2,4 |
| . 472 | . 06424 | 229 | . 29370 | 206 | . 89996 | 19,0 | . 11112 | 2,3 |
| . 473 | . 06653 | 230 | . 29577 | 207 | . 90015 | 19,0 | . 1109 | 2,3 |
| . 474 | . 06883 | 230 | . 29784 | 207 | . 90034 | 18,9 | . 1107 | 2,3 |
| 1.475 | 2.07113 | 230 | 2.29991 | 207 | 0.90053 | 18,9 | I. 1105 | 2,3 |
| . 476 | . 07343 | 230 | . 30198 | 207 | . 90072 | 18,9 | . 1102 | 2,3 |
| . 477 | . 07573 | 230 | . 30405 | 208 | . 90090 | 18,8 | . 1100 | 2,3 |
| . 478 | . 07804 | 231 | . 30613 | 208 | .90109 | 18,8 | . 1098 | 2,3 |
| . 479 | . 08034 | 231 | . 3082 I | 208 | . 90128 | 18,8 | . 1095 | 2,3 |
| 1.480 | 2.08265 | 231 | 2.31029 | 208 | 0.90147 | 18,7 | 1.1093 | 2,3 |
| .481 | . 08497 | 231 | . 31238 | 208 | . 90166 | 18,7 | . 1091 | 2,3 |
| . 482 | . 08728 | 231 | . 31446 | 209 | . 90184 | 18,7 | . 1088 | 2,3 |
| .483 | . 08959 | 232 | . 31655 | 209 | . 90203 | 18,6 | . 1086 | 2,3 |
| . 484 | .09191 | 232 | -.31864 | 209 | . 9022 I | 18,6 | . 1084 | 2,3 |
| 1. 485 | 2.09423 | 232 | 2.32073 | 209 | 0.90240 | 18,6 | 1. 1082 | 2,3 |
| . 486 | . 09655 | 232 | . 32283 | 210 | . 90259 | 18,5 | . 1079 | 2,3 |
| . 487 | . 09888 | 232 | . 32493 | 210 | . 90277 | 18,5 | . 1077 | 2,3 |
| . 488 | . 10120 | 233 | . 32703 | 210 | . 90296 | 18,5 | . 1075 | 2,3 |
| . 489 | . 10353 | 233 | . 32913 | 210 | . 90314 | 18,4 | .1072 | 2,3 |
| I. 490 | 2. 10586 | 233 | 2.33123 | 2 II | 0.90332 | 18,4 | 1.1070 | 2,3 |
| . 491 | . 10819 | 233 | . 33334 | 2 II | . 90351 | 18,4 | . 1068 | 2,2 |
| . 492 | . 11053 | 234 | - 33545 | 211 | . 90369 | 18,3 | . 1056 | 2,2 |
| . 493 | . 11286 | 234 | . 33756 | 2 II | . 90388 | 18,3 | . 1063 | 2,2 |
| . 494 | . 11520 | 234 | . 33968 | 212 | . 90406 | 18,3 | . 1061 | 2,2 |
| I. 495 | 2. II754 | 234 | 2.34179 | 212 | 0.90424 | 18,2 | 1. 1059 | 2,2 |
| . 496 | . 11989 | 234 | . 34391 | 212 | . 90442 | 18,2 | . 1057 | 2,2 |
| . 497 | . 12223 | 235 | . 34603 | 212 | . 90460 | 18,2 | . 1055 | 2,2 |
| . 498 | . 12458 | 235 | . 34816 | 212 | . 90479 | 18,I | . 1052 | 2,2 |
| . 499 | . 12693 | 235 | -35028 | 213 | . 90497 | 18, 1 | . 1050 | 2,2 |
| 1.500 | 2.12928 | 235 | 2.35241 | 213 | 0.90515 | 18,1 | I. 1048 | 2,2 |
| u | $\tan \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.500 | 2.12928 | 235 | 2.35241 | 213 | 0.90515 | 18,1 | 1. 1048 | 2,2 |
| . 501 | . 13163 | 235 | - 35454 | 213 | . 90533 | 18,0 | . 1046 | 2,2 |
| . 502 | . I3399 | 236 | . 35667 | 213 | . 9055 I | 18,0 | . 1044 | 2,2 |
| . 503 | . I3635 | 236 | .3588I | 214 | . 90569 | 18,0 | . 1041 | 2,2 |
| . 504 | . 13871 | 236 | . 36095 | 214 | . 90587 | 17,9 | . 1039 | 2,2 |
| 1.505 | 2.14107 | 236 | 2.36309 | 214 | 0.90605 | 17,9 | I. 1037 | 2,2 |
| . 506 | . 14343 | 237 | . 36523 | 214 | . 90623 | 17,9 | . 1035 | 2,2 |
| . 507 | . 14580 | 237 | . 36737 | 215 | .9064I | 17,8 | . 1033 | 2,2 |
| . 508 | . 14817 | 237 | . 36952 | 215 | . 90658 | 17,8 | . 1030 | 2,2 |
| . 509 | . 15054 | 237 | . 37167 | 215 | . 90676 | 17,8 | . 1028 | 2,2 |
| 1.510 | 2. I 5291 | 237 | 2.37382 | 215 | 0.90694 | 17,7 | 1. 1026 | 2,2 |
| .5II | . 15529 | 238 | . 37597 | 216 | . 90712 | 17,7 | . 1024 | 2,2 |
| . 512 | . 15766 | 238 | .37813 | 216 | . 90729 | 17,7 | . 1022 | 2,I |
| . 513 | . 16004 | 238 | . 38029 | 216 | . 90747 | 17,6 | . 1020 | 2,I |
| . 514 | . 16242 | 238 | . 38245 | 216 | . 90765 | 17,6 | . 1018 | 2,1 |
| 1.515 | 2.1648I | 238 | 2.3846 I | 216 | 0.90782 | 17,6 | I. 1015 | 2,I |
| . 516 | . 16719 | 239 | . 38678 | 217 | . 90800 | 17,6 | . 1013 | 2,1 |
| . 517 | . 16958 | 239 | . 38895 | 217 | .90817 | 17,5 | . IOII | 2,I |
| . 518 | . 17197 | 239 | -39112 | 217 | . 90835 | 17,5 | . 1009 | 2,I |
| . 519 | . 17436 | 239 | . 39329 | 217 | . 90852 | 17,5 | . 1007 | 2,1 |
| 1.520 | 2.17676 | 240 | 2.39547 | 218 | 0.90870 | 17,4 | 1. 1005 | 2,1 |
| . 52 I | .17915 | 240 | . 39765 | 218 | . 90887 | 17,4 | . 1003 | 2,I |
| . 522 | . 18155 | 240 | . 39983 | 218 | . 90905 | 17,4 | . 1001 | 2, I |
| . 523 | . 18395 | 240 | . 40201 | 218 | . 90922 | 17,3 | . 0998 | 2,I |
| . 524 | . 18636 | 240 | . 40419 | 219 | . 90939 | 17,3 | . 0996 | 2,I |
| 1.525 | 2. 18876 | 24 I | 2.40638 | 219 | 0.90957 | 17,3 | 1.0994 | 2,I |
| . 526 | . 19117 | 24 I | . 40857 | 219 | . 90974 | 17,2 | . 0992 | 2,I |
| . 527 | . 19358 | 24 I | . 41076 | 219 | . 90991 | 17,2 | . 0990 | 2,I |
| . 528 | . 19599 | 24 I | . 41296 | 220 | . 91008 | 17,2 | . 0988 | 2,I |
| . 529 | . 19840 | 242 | .41516 | 220 | . 91025 | 17,I | . 0986 | 2,I |
| 1.530 | 2.20082 | 242 | 2.41736 | 220 | 0.91042 | 17,I | I. 0984 | 2,I |
| . 531 | . 20324 | 242 | . 41956 | 220 | . 91060 | 17,I | . 0982 | 2,I |
| . 532 | . 20566 | 242 | . 42176 | 221 | . 91077 | 17, I | . 0980 | 2,I |
| . 533 | . 20808 | 242 | . 42397 | 221 | .91094 | 17,0 | . 0978 | 2,I |
| . 534 | .2105I | 243 | . 42618 | 221 | .9IIII | 17,0 | . 0976 | 2,0 |
| 1.535 | 2.21293 | 243 | 2.42839 | 22I | 0.91128 | 17,0 | 1.0974 | 2,0 |
| . 536 | . 21536 | 243 | . 43060 | 222 | .91I45 | 16,9 | . 0972 | 2,0 |
| . 537 | . 21780 | 243 | . 43282 | 222 | .9116I | 16,9 | . 0970 | 2,0 |
| . 538 | . 22023 | 244 | . 43504 | 222 | .91178 | 16,9 | . 0968 | 2,0 |
| . 539 | . 22267 | 244 | . 43726 | 222 | .91195 | 16,8 | . 0965 | 2,0 |
| 1.540 | 2.22510 | 244 | 2.43949 | 223 | 0.91212 | 16,8 | 1.0963 | 2,0 |
| . 541 | . 22755 | 244 | . 44171 | 223 | . 91229 | 16,8 | .0961 | 2,0 |
| . 542 | . 22999 | 244 | . 44394 | 223 | . 91246 | 16,7 | . 0959 | 2,0 |
| . 543 | . 23243 | 245 | . 44617 | 223 | . 91262 | 16,7 | . 0957 | 2,0 |
| . 544 | . 23488 | 245 | . 4484 I | 223 | .91279 | 16,7 | . 0955 | 2,0 |
| I. 545 | 2.23733 | 245 | 2.45064 | 224 | 0.91296 | 16,7 | 1. 0953 | 2,0 |
| . 546 | . 23978 | 245 | . 45288 | 224 | . 91312 | 16,6 | .0951 | 2,0 |
| . 547 | . 24224 | 246 | . 45512 | 224 | . 91329 | 16,6 | . 0949 | 2,0 |
| . 548 | . 24469 | 246 | . 45736 | 224 | . 91345 | 16,6 | . 0947 | 2,0 |
| . 549 | . 24715 | 246 | . 4596 I | 225 | .91362 | 16,5 | . 0945 | 2,0 |
| 1.550 | 2.24961 | 246 | 2.46186 | 225 | 0.91379 | 16,5 | I. 0943 | 2,0 |
| 4 | $\boldsymbol{t a n} \mathbf{g d} \mathbf{u}$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |


| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\tanh u$ | $\omega F_{0}{ }^{\circ}$ | $\operatorname{coth} u$ | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 550 | 2.24961 | 246 | 2.46186 | 225 | 0.91379 | 16,5 | 1.0943 | 2,0 |
| . 551 | . 25207 | 246 | . 46411 | 225 | . 91395 | 16,5 | . 0942 | 2,0 |
| . 552 | . 25454 | 247 | . 46636 | 225 | .914II | 16,4 | . 0940 | 2,0 |
| . 553 | . 25701 | 247 | . 46868 | 226 | .91428 | 16,4 | . 0938 | 2,0 |
| . 554 | . 25948 | 247 | . 47088 | 226 | .91444 | 16,4 | . 0936 | 2,0 |
| I. 555 | 2.26195 | 247 | 2.47314 | 226 | 0.91461 | 16,3 | 1.0934 | 2,0 |
| . 556 | . 26442 | 248 | . 47540 | 226 | . 91477 | 16,3 | . 0932 | 2,0 |
| . 557 | . 26690 | 248 | . 47767 | 227 | . 91493 | 16,3 | . 0930 | I,9 |
| . 558 | . 26938 | 248 | . 47993 | 227 | .91510 | 16,3 | . 0928 | I,9 |
| . 559 | . 27186 | 248 | . 4822 I | 227 | .91526 | 16,2 | . 0926 | 1,9 |
| 1.560 | 2.27434 | 248 | 2.48448 | 227 | 0.91542 | 16,2 | 1.0924 | 1,9 |
| . 561 | . 27683 | 249 | . 48675 | 228 | .91558 | 16,2 | . 0922 | 1,9 |
| . 562 | . 27932 | 249 | . 48903 | 228 | .91574 | 16,1 | . 0920 | 1,9 |
| . 563 | .28I8I | 249 | . 49131 | 228 | .91591 | 16, I | . 0918 | I,9 |
| . 564 | . 28430 | 249 | . 49360 | 228 | .91607 | 16,1 | . 0916 | I,9 |
| I. 565 | 2.28679 | 250 | 12.49588 | 229 | 0.91623 | 16, I | 1.0914 | 1,9 |
| . 566 | . 28929 | 250 | . 49817 | 229 | . 91639 | 16,0 | .0912 | 1,9 |
| . 567 | . 29179 | 250 | . 50046 | 229 | . 91655 | 16,0 | .09II | I,9 |
| . 568 | . 29429 | 250 | . 50275 | 229 | .91671 | I6,0 | . 0909 | 1,9 |
| . 569 | . 29680 | 251 | . 50505 | 230 | .91687 | 15,9 | . 0907 | 1,9 |
| 1.570 | 2.29930 | 251 | 2.50735 | 230 | 0.91703 | 15,9 | 1.0905 | 1,9 |
| . 571 | . 30181 | 251 | . 50965 | 230 | .91718 | 15,9 | . 0903 | 1,9 |
| . 572 | . 30432 | 251 | . 51195 | 230 | . 91734 | I 5,8 | . 0901 | 1,9 |
| . 573 | . 30583 | 251 | . 51426 | 23 I | .91750 | I5,8 | . 0899 | 1,9 |
| . 574 | - 30935 | 252 | . 51656 | 231 | .91766 | 15,8 | . 0897 | 1,9 |
| 1. 575 | 2.31187 | 252 | 2.51887 | 231 | 0.91782 | 15,8 | 1.0895 | 1,9 |
| . 576 | . 31439 | 252 | . 52119 | 231 | .91797 | 15,7 | . 0894 | 1,9 |
| . 577 | .31691 | 252 | . 52350 | 232 | .918I3 | 15,7 | . 0892 | 1,9 |
| . 578 | . 31943 | 253 | . 52582 | 232 | .91829 | 15,7 | . 0890 | 1,9 |
| . 579 | . 32196 | 253 | . 52814 | 232 | .91845 | 15,6 | . 0888 | 1,9 |
| 1.580 | 2.32449 | 253 | 2.53047 | 232 | 0.91860 | 15,6 | 1.0886 | 1,9 |
| . 581 | . 32702 | 253 | . 53279 | 233 | .91876 | 15,6 | . 0884 | 1,8 |
| . 582 | - 32956 | 254 | . 53512 | 233 | .91891 | I5,6 | . 0882 | I,8 |
| . 583 | . 33209 | 254 | . 53745 | 233 | . 91907 | 15,5 | .088I | I,8 |
| . 584 | . 33463 | 254 | . 53978 | 233 | . 91922 | 15,5 | . 0879 | I,8 |
| 1. 585 | 2.33717 | 254 | 2.54212 | 234 | 0.91938 | 15,5 | 1.0877 | I,8 |
| . 586 | . 33972 | 254 | . 54446 | 234 | . 91953 | 15,4 | . 0875 | I,8 |
| . 587 | - 34226 | 255 | . 54680 | 234 | .91969 | 15,4 | . 0873 | I,8 |
| . 588 | -34481 | 255 | . 54914 | 234 | . 91984 | 15,4 | . 0871 | 1,8 |
| . 589 | . 34736 | 255 | . 55149 | 235 | . 92000 | 15,4 | . 0870 | 1,8 |
| I. 590 | 2.34991 | 255 | 2.55384 | 235 | 0.92015 | 15,3 | 1.0868 | I,8 |
| . 591 | . 35247 | 256 | . 55619 | 235 | . 92030 | 15,3 | . 0866 | I,8 |
| . 592 | . 35502 | 256 | . 55854 | 236 | . 92046 | I5,3 | . 0864 | I,8 |
| . 593 | - 35758 | 256 | . 56090 | 236 | .9206I | 15,2 | . 0862 | I,8 |
| . 594 | . 36015 | 256 | . 56326 | 236 | . 92076 | 15,2 | .086I | I,8 |
| I. 595 | 2.36271 | 257 | 2.56562 | 236 | 0.92091 | 15,2 | I. 0859 | I,8 |
| . 596 | . 36528 | 257 | . 56798 | 237 | . 92106 | 15,2 | . 0857 | I,8 |
| . 597 | - 36785 | 257 | . 57035 | 237 | . 92122 | 15,I | . 0855 | I,8 |
| . 598 | - 37042 | 257 | . 57272 | 237 | . 92137 | 15, I | . 0853 | I,8 |
| . 599 | . 37299 | 258 | . 57509 | 237 | .92152 | 15,1 | . 0852 | 1,8 |
| 1.600 | 2.37557 | 258 | 2.57746 | 238 | 0.92167 | I5, I | 1. 0850 | I,8 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{g} \mathrm{d} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{Fo}^{\prime}$ | $\cosh u$ | $\omega \mathrm{Fo}^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.600 | 2.37557 | 258 | 2.57746 | 238 | 0.9216\% | 15, I | 1. 0850 | 1,8 |
| . 601 | . 37815 | 258 | . 57984 | 238 | . 92182 | 15,0 | . 0848 | 1,8 |
| . 602 | . 38073 | 258 | . 58222 | 238 | . 92197 | 15,0 | . 0846 | 1,8 |
| . 603 | .3833I | 258 | . 58460 | 238 | . 92212 | 15,0 | . 0845 | I,8 |
| . 604 | . 38590 | 259 | . 58699 | 239 | . 92227 | I4,9 | . 0843 | I,8 |
| 1. 605 | 2.38849 | 259 | 2.58937 | 239 | 0.92242 | 14,9 | 1.0841 | 1,8 |
| . 605 | . 39108 | 259 | . 59176 | 239 | . 92257 | 14,9 | . 0839 | 1,7 |
| . 607 | . 39367 | 259 | . 59416 | 239 | . 92272 | 14,9 | . 0838 | I,7 |
| . 608 | . 39626 | 260 | . 59655 | 240 | - 92286 | 14,8 | . 0836 | 1,7 |
| . 609 | - 39886 | 260 | - 59895 | 240 | . 92301 | 14,8 | . 0834 | I,7 |
| 1.610 | 2.40146 | 260 | 2.60135 | 240 | 0.92316 | 14,8 | 1.0832 | 1,7 |
| .6II | . 40406 | 260 | . 60375 | 240 | . 92331 | 14,8 | . 0831 | 1,7 |
| . 612 | . 40567 | 261 | . 60616 | 24 I | . 92346 | 14,7 | . 0829 | 1,7 |
| . 613 | . 40928 | 261 | . 60857 | 24 I | . 92360 | 14,7 | . 0827 | 1,7 |
| . 614 | .41189 | 261 | . 61098 | 24 I | . 92375 | 14,7 | . 0825 | 1,7 |
| 1.615 | 2.41450 | 261 | 2.61339 | 241 | 0.92390 | 14,6 | 1.0824 | 1,7 |
| . 616 | . 41711 | 262 | . 61581 | 242 | . 92404 | 14,6 | . 0822 | 1,7 |
| . 617 | . 41973 | 262 | . 61822 | 242 | . 92419 | 14,6 | . 0820 | I,7 |
| . 618 | . 42235 | 262 | . 62064 | 242 | . 92433 | 14,6 | . 0819 | 1,7 |
| . 619 | . 42497 | 262 | . 62307 | 242 | . 92448 | 14,5 | .0817 | 1,7 |
| 1.620 | 2.42760 | 263 | 2.62549 | 243 | 0.92462 | 14,5 | 1.0815 | 1,7 |
| .621 | . 43022 | 263 | . 62792 | 243 | . 92477 | 14,5 | . 0814 | 1,7 |
| . 622 | . 43285 | 263 | . 63035 | 243 | . 92491 | 14,5 | . 0812 | 1,7 |
| . 623 | . 43548 | 263 | . 63279 | 244 | . 92506 | 14,4 | . 0810 | 1,7 |
| . 624 | -43812 | 264 | . 63522 | 244 | . 92520 | 14,4 | . 0808 | 1,7 |
| 1. 625 | 2.44075 | 264 | 2.63767 | 244 | 0.92535 | 14,4 | 1.0807 | 1,7 |
| . 626 | . 44339 | 264 | . 64011 | 244 | . 92549 | 14,3 | . 0805 | 1,7 |
| . 627 | . 44603 | 264 | . 64255 | 245 | . 92563 | 14,3 | . 0803 | I,7 |
| . 628 | . 44868 | 264 | . 64500 | 245 | . 92578 | 14,3 | . 0802 | 1,7 |
| . 629 | . 45132 | 265 | . 64745 | 245 | . 92592 | 14,3 | . 0800 | 1,7 |
| 1.630 | 2.45397 | 265 | 2.64990 |  | 0.92606 | 14,2 | 1.0798 | 1,7 |
| .631 | . 45662 | 265 | . 65236 | 246 | . 92620 | 14,2 | . 0797 | 1,7 |
| . 632 | . 45928 | 265 | . 65482 | 246 | . 92635 | 14,2 | . 0795 | 1,7 |
| . 633 | . 46193 | 266 | - . 65728 | 246 | . 92649 | 14,2 | . 0793 | 1,6 |
| . 634 | . 46459 | 266 | . 65974 | 246 | . 92663 | 14,1 | . 0792 | 1,6 |
| 1. 635 | 2.46725 | 266 | 2.66221 | 247 | 0.92677 | 14, I | 1.0790 | 1,6 |
| . 636 | . 46992 | 266 | . 66467 | 247 | . 92691 | I4, I | .0789 | I,6 |
| . 637 | . 47258 | 267 | . 66715 | 247 | . 92705 | 14, 1 | . 0787 | I,6 |
| . 638 | . 47525 | 267 | . 66962 | 248 | . 92719 | 14,0 | . 0785 | 1,6 |
| . 639 | . 47792 | 267 | . 67210 | 248 | . 92733 | 14,0 | . 0784 | 1,6 |
| 1. 640 | 2.48059 | 267 | 2.67457 | 248 | 0.92747 | 14,0 | 1. 0782 | 1,6 |
| .641 | . 48327 | 268 | . 67706 | 248 | . 92761 | I4,0 | . 0780 | 1,6 |
| . 642 | . 48595 | 268 | . 67954 | 249 | . 92775 | I3,9 | . 0779 | I,6 |
| . 643 | . 48853 | 268 | . 68203 | 249 | . 92789 | 12.9 | . 0777 | 1,6 |
| . 644 | .49131 | 268 | . 68452 | 249 | . 92803 | 13,9 | . 0776 | 1,6 |
| 1. 645 | 2.49400 | 269 | 2.68701 | 249 | 0.92817 | 13,9 | 1.0774 | 1,6 |
| . 646 | . 49669 | 269 | . 68951 | 250 | . 92831 | $\begin{array}{r}13,8 \\ \text { 13 } \\ \hline\end{array}$ | . 0772 | 1,6 I,6 |
| . 647 | . 49938 | 269 | . 69200 | 250 | . 92884 | 13,8 13 | . 0771 | 1,6 r,6 |
| .648 .649 | .50207 .50477 | 269 270 | . 69451 | 250 250 | . 92858 | 13,8 13,7 | . 0769 | 1,6 1,6 |
| 1. 650 | 2.50746 | 270 | 2.69951 | 251 | 0.92886 | 13,7 | 1.0766 | 1,6 |
| u | $\tan \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec $\mathrm{gd}^{\text {u }}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} u$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.650 | 2.50746 | 270 | 2.69951 | 251 | 0.92885 | 13,7 | 1.0766 | 1,6 |
| . 651 | . 51017 | 270 | . 70202 | 251 | . 92899 | I3,7 | . 0764 | I,6 |
| . 652 | . 51287 | 270 | . 70454 | 251 | .92913 | 13,7 | . 0763 | I,6 |
| . 653 | . 51557 | 271 | . 70705 | 252 | . 92927 | I3,6 | . 0761 | I,6 |
| . 654 | . 51828 | 271 | . 70957 | 252 | . 92940 | I3,6 | . 0760 | I,6 |
| 1. 655 | 2.52099 | 271 | 2.71209 | 252 | 0.92954 | 13,6 | I. 0758 | I,6 |
| . 656 | . 52371 | 271 | .7146I | 252 | . 92968 | 13,6 | . 0756 | I,6 |
| . 657 | . 52642 | 272 | . 71713 | 253 | .9298I | 13,5 | . 0755 | I,6 |
| . 658 | . 52914 | 272 | . 71966 | 253 | . 92995 | 13,5 | . 0753 | I,6 |
| . 659 | . 53186 | 272 | . 72219 | 253 | . 93008 | I 3,5 | . 0752 | I,6 |
| 1.660 | 2.53459 | 272 | 2.72472 | 253 | 0.93022 | I 3,5 | 1.0750 | - 1,6 |
| . 661 | . 5373 I | 273 | . 72726 | 254 | . 93035 | 13,4 | . 0749 | I,6 |
| . 662 | . 54004 | 273 | . 72980 | 254 | . 93049 | 13,4 | . 0747 | I,5 |
| . 663 | . 54277 | 273 | . 73234 | 254 | . 93062 | I 3,4 | . 0746 | I,5 |
| . 664 | . 5455 I | 273 | . 73489 | 255 | . 93075 | I3,4 | . 0744 | I,5 |
| 1. 665 | 2.54824 | 274 | 2.73743 | 255 | 0.93089 | 13,3 | 1.0742 | I,5 |
| . 666 | . 55098 | 274 | . 73998 | 255 | . 93102 | I3,3 | .074I | I,5 |
| . 667 | . 55372 | 274 | . 74253 | 255 | .93II5 | I3,3 | . 0739 | I,5 |
| . 668 | . 55647 | 275 | . 74509 | 256 | .93I29 | I3,3 | . 0738 | I,5 |
| . 669 | . 55921 | 275 | . 74765 | 256 | .93I42 | I3,2 | . 0736 | I,5 |
| 1.670 | 2.56196 | 275 | 2.7502 I | 256 | 0.93155 | 13,2 | I. 0735 | I,5 |
| . 671 | . 56471 | 275 | . 75277 | 256 | .93168 | 13,2 | . 0733 | I,5 |
| . 672 | . 56747 | 276 | . 75534 | 257 | . 93182 | 13,2 | . 0732 | I,5 |
| . 673 | . 57022 | 276 | . 75791 | 257 | .93195 | I3,I | . 0730 | I,5 |
| . 674 | . 57298 | 276 | . 76048 | 257 | . 93208 | I3, I | . 0729 | I,5 |
| 1.675 | 2.57574 | 276 | 2.76305 | 258 | 0.9322 I | I3,I | 1.0727 | I,5 |
| . 676 | . 5785 I | 277 | . 76563 | 258 | :93234 | I3,I | . 0725 | I,5 |
| . 677 | . 58127 | 277 | .7682I | 258 | . 93247 | I3,0 | . 0724 | I,5 |
| . 678 | . 58404 | 277 | . 77079 | 258 | . 93260 | I3,0 | . 0723 | I,5 |
| . 679 | . 58682 | 277 | . 77338 | 259 | . 93273 | 13,0 | . 0721 | I,5 |
| 1.680 | 2.58959 | 278 | 2.77596 | 259 | 0.93286 | I3,0 | 1.0720 | I,5 |
| .681 | . 59237 | 278 | . 77856 | 259 | . 93299 | I3,0 | . 0718 | I,5 |
| . 682 | . 59515 | 278 | .78115 | 260 | . 93312 | 12,9 | . 0717 | I,5 |
| . 683 | . 59793 | 278 | . 78375 | 250 | . 93325 | 12,9 | . 0715 | I,5 |
| . 684 | . 60072 | 279 | . 78635 | 260 | . 93338 | 12,9 | . 0714 | I,5 |
| 1. 685 | 2.60350 | 279 | 2.78895 | 260 | 0.9335 I | 12,9 | 1.0712 | I,5 |
| . 686 | . 60629 | 279 | .79155 | 26 I | . 93364 | 12,8 | . 0711 | 1,5 |
| . 687 | . 60909 | 279 | . 79416 | 251 | . 93376 | 12,8 | . 0709 | I,5 |
| . 688 | .61 188 | 280 | . 79677 | 26I | . 93389 | 12,8 | . 0708 | I,5 |
| . 689 | .61468 | 280 | . 79938 | 26 I | . 93402 | 12,8 | . 0706 | I,5 |
| 1.690 | 2.61748 | 280 | 2.80200 | 262 | 0.93415 | 12,7 | 1.0705 | I,5 |
| . 691 | . 62028 | 280 | . 80462 | 262 | . 93427 | 12,7 | . 0703 | I,5 |
| . 692 | . 62309 | 28I | . 80724 | 262 | . 93440 | 12,7 | . 0702 | I,5 |
| . 693 | . 62590 | 28I | . 80987 | 263 | . 93453 | 12,7 | . 0701 | I,5 |
| . 694 | . 62871 | 281 | .81249 | 263 | . 93465 | 12,6 | . 0699 | I,4 |
| 1.695 | 2.63152 | 282 | 2.81512 | 263 | 0.93478 | 12,6 | 1.0698 | I,4 |
| . 696 | . 63434 | 282 | .81776 | 263 | . 93491 | 12,6 | . 0696 | I, 4 |
| . 697 | . 63716 | 282 | . 82039 | 264 | . 93503 | 12,6 | . 0695 | I,4 |
| . 698 | . 63998 | 282 | . 82303 | 264 | . 93516 | 12,5 | . 0693 | I,4 |
| . 699 | . 64280 | 283 | . 82567 | 264 | . 93528 | 12,5 | . 0692 | I,4 |
| 1.700 | 2.64563 | 283 | 2.82832 | 265 | 0.93541 | 12,5 | 1.069I | I.,4 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.700 | 2.64563 | 283 | 2.82832 | 265 | 0.93541 | 12,5 | 1.0591 | I,4 |
| . 701 | . 64846 | 283 | . 83096 | 265 | . 93553 | 12,5 | . 0689 | I, 4 |
| . 702 | . 65129 | 283 | . 83361 | 265 | . 93566 | 12,5 | . 0688 | I, 4 |
| . 703 | . 65413 | 284 | . 83627 | 265 | . 93578 | 12,4 | . 0586 | I, 4 |
| . 704 | . 65697 | 384 | . 83892 | 266 | .93591 | 12,4 | . 0685 | I, 4 |
| 1.705 | 2.65981 | 284 | 2.84158 | 266 | 0.93603 | 12,4 | 1. 0683 | I,4 |
| . 706 | . 66265 | 284 | . 84424 | 266 | . 93615 | 12,4 | . 0682 | I,4 |
| . 707 | . 66550 | 285 | . 84690 | 267 | . 93628 | 12,3 | .0681 | I, 4 |
| . 708 | . 66834 | 285 | . 84957 | 267 | . 93640 | 12,3 | . 0679 | I, 4 |
| . 709 | . 67119 | 285 | . 85224 | 267 | . 93652 | 12,3 | . 0678 | I, 4 |
| I.710 | 2.67405 | 285 | 2.85491 | 267 | 0.93665 | 12,3 | 1.0676 | I,4 |
| . 711 | . 67690 | 286 | . 85759 | 268 | . 93677 | 12,2 | . 0675 | I,4 |
| . 712 | . 67976 | 286 | . 86027 | 268 | . 93689 | 12,2 | . 0674 | I,4 |
| .713 | . 68262 | 286 | . 86295 | 268 | .93701 | 12,2 | . 0672 | I,4 |
| . 714 | . 68549 | 287 | . 86563 | 269 | .93714 | 12,2 | . 0671 | I,4 |
| 1.715 | 2.68836 | 287 | 2.86832 | 269 | 0.93726 | 12,2 | 1. 0669 | I, 4 |
| . 716 | . 69123 | 287 | .87101 | 269 | . 93738 | 12, I | . 0668 | I, 4 |
| . 717 | . 69410 | 287 | . 87370 | 269 | . 93750 | 12, I | . 0667 | I, 4 |
| . 718 | . 69697 | 288 | . 87640 | 270 | . 93762 | 12, I | . 0665 | I,4 |
| . 719 | . 69985 | 288 | . 87910 | 270 | . 93774 | 12,1 | . 0664 | I,4 |
| 1.720 | 2.70273 | 288 | 2.88180 | 270 | 0.93786 | 12,0 | 1.0663 | I,4 |
| . 721 | . 70561 | 288 | . 88450 | 271 | . 93798 | 12,0 | . 0661 | I,4 |
| . 722 | . 70850 | 289 | .88721 | 271 | .93810 | 12,0 | . 0660 | I, 4 |
| . 723 | .71139 | 289 | . 88992 | 271 | . 93822 | 12,0 | . 0658 | I,4 |
| . 724 | . 71428 | 289 | . 89263 | 271 | . 93834 | 12,0 | . 0657 | I,4 |
| 1.725 | 2.71717 | 290 | 2.89535 | 272 | 0.93846 | I 1,9 | 1.0656 | I,4 |
| . 726 | . 72007 | 290 | . 89807 | 272 | . 93858 | II,9 | . 0654 | I,4 |
| . 727 | . 72297 | 290 | . 90079 | 272 | . 93870 | II,9 | . 0653 | I,3 |
| . 728 | . 72587 | 290 | . 9035 I | 273 | . 93882 | I 1,9 | . 0652 | I,3 |
| . 729 | . 72878 | 291 | . 90624 | 273 | . 93894 | I I, 8 | . 0650 | I,3 |
| 1.730 | 2.73168 | 291 | 2.90897 | 273 | 0.93905 | II,8 | 1. 0649 | I,3 |
| . 731 | . 73460 | 291 | .91170 | 273 | . 93917 | II,8 | . 0648 | I,3 |
| . 732 | . 73751 | 291 | .91444 | 274 | . 93929 | I I, 8 | . 0646 | I,3 |
| . 733 | . 74042 | 292 | .91718 | 274 | .9394I | II, 8 | . 0645 | I,3 |
| . 734 | . 74334 | 292 | . 91992 | 274 | . 93953 | II,7 | . 0644 | I,3 |
| I. 735 | 2.74626 | 292 | 2.92266 | 275 | 0.93964 | 11,7 | 1.0642 | I,3 |
| . 736 | . 74919 | 293 | . 92541 | 275 | . 93976 | I I,7 | . 0641 | I,3 |
| . 737 | . 75211 | 293 | . 92816 | 275 | . 93988 | I I,7 | . 0640 | I,3 |
| . 738 | . 75504 | 293 | . 93092 | 276 | -93999 | 11,6 | .0638 | I,3 |
| . 739 | . 75798 | 293 | . 93367 | 276 | .940I I | I 1,6 | . 0537 | 1,3 |
| 1.740 | 2.76091 | 294 | 2.93643 | 276 | 0.94023 | II,6 | 1.0536 | I,3 |
| .741 | . 76385 | 294 | . 93919 | 276 | . 94034 | II, 6 | . 0634 | I,3 |
| . 742 | . 76579 | 294 | . 94196 | 277 | . 94046 | I I, 6 | . 0633 | I,3 |
| . 743 | . 76973 | 294 | . 94473 | 277 | . 94057 | II,5 | . 0632 | I, 3 |
| . 744 | . 77268 | 295 | . 94750 | 277 | . 94069 | II,5 | .053I | I,3 |
| 1.745 | 2.77563 | 295 | 2.95027 | 278 | 0.94080 | II,5 | 1.0629 | 1,3 |
| . 746 | . 77858 | 295 | . 95305 | 278 | . 94092 | II,5 | . 0528 | I,3 |
| . 747 | . 78153 | 296 | . 95583 | 278 | . 94103 | II,4 | . 0627 | I,3 |
| .748 | . 78449 | 296 | .9586I | 278 | .94115 | II, 4 | . 0625 | I,3 I,3 |
| . 749 | . 78745 | 296 | . 90140 | 279 | -94126 | II,4 | . 0624 | 1,3 |
| 1.750 | 2.7904 I | 296 | 2.96419 | 279 | 0.94138 | II,4 | 1.0623 | I,3 |
| u | $\tan \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | sec od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n g d u}$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

## Smithsonian Tables

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\text {a }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.750 | 2.79041 | 296 | 2.96419 | 279 | 0.94138 | II,4 | 1.0623 | 1,3 |
| . 751 | . 79338 | 297 | . 96698 | 279 | .94149 | II,4 | .062 I | I,3 |
| . 752 | . 79635 | 297 | . 96978 | 280 | .94160 | II,3 | . 0620 | I,3 |
| . 753 | . 79932 | 297 | . 97257 | 280 | . 94172 | II,3 | . 0619 | I,3 |
| . 754 | . 80229 | 298 | . 97537 | 280 | .94183 | II,3 | .06I8 | I,3 |
| I. 755 | 2.80527 | 298 | 2.97818 | 28I | 0.94194 | II,3 | 1.0616 | I,3 |
| . 756 | . 80825 | 298 | . 98098 | 28I | . 94205 | II,3 | .0615 | I,3 |
| . 757 | .81123 | 298 | . 98379 | 28 I | . 94217 | 11,2 | .06I4 | I,3 |
| . 758 | .81422 | 299 | . 98661 | 28 I | -. 94228 | 11,2 | .06I3 | I,3 |
| . 759 | .81721 | 299 | . 98942 | 282 | . 94239 | II,2 | .06II | 1,3 |
| 1.760 | 2.82020 | 299 | 2.99224 | 282 | 0.94250 | II,2 | 1.0610 | I,3 |
| . 761 | . 82319 | 300 | . 99506 | 282 | . 94261 | II, I | . 0609 | I,3 |
| . 762 | .82619 | 300 | . 99789 | 283 | . 94273 | II,I | . 0608 | I,3 |
| . 763 | . 82919 | 300 | 3.00072 | 283 | . 94284 | II, I | . 0606 | I,2 |
| . 764 | . 83219 | 300 | . 00355 | 283 | . 94295 | II, I | . 0605 | I,2 |
| 1.765 | 2.83519 | 301 | 3.00638 | 284 | 0.94306 | II, I | 1.0604 | I,2 |
| . 766 | . 83820 | 301 | . 00922 | 284 | . 94317 | II,O | . 0603 | I,2 |
| . 767 | . 84121 | 301 | . 01205 | 284 | . 94328 | II,0 | .0601 | I,2 |
| . 768 | . 84422 | 301 | . 01490 | 284 | . 94339 | II,O | . 0600 | I,2 |
| .769 | . 84724 | 302 | . 01774 | 285 | . 94350 | II,0 | . 0599 | I,2 |
| 1.770 | 2.85026 | 302 | 3.02059 | 285 | 0.94361 | 11,0 | I. 0598 | 1,2 |
| . 771 | . 85328 | 302 | . 02344 | 285 | . 94372 | 10,9 | . 0596 | 1,2 |
| . 772 | . 85631 | 303 | . 02630 | 286 | . 94383 | 10,9 | . 0595 | I,2 |
| . 773 | . 85933 | 303 | . 02916 | 286 | . 94394 | 10,9 | . 0594 | 1,2 |
| . 774 | . 86237 | 303 | . 03202 | 286 | . 94405 | 10,9 | . 0593 | I,2 |
| 1.775 | 2.86540 | 303 | 3.03488 | 287 | 0.94416 | 10,9 | I.059I | 1,2 |
| . 776 | . 85844 | 304 | . 03775 | 287 | . 94426 | 10,8 | . 0590 | I,2 |
| . 777 | . 87147 | 304 | . 04052 | 287 | . 94437 | 10,8 | . 0589 | I,2 |
| . 778 | . 87452 | 304 | . 04349 | 287 | . 94448 | 10,8 | . 0588 | 1,2 |
| . 779 | . 87756 | 305 | . 04637 | 288 | . 94459 | 10,8 | . 0587 | I,2 |
| 1.780 | 2.88061 | 305 | 3.04925 | 288 | 0.94470 | 10,8 | 1.0585 | 1,2 |
| .781 | . 88366 | 305 | . 05213 | 288 | . 94480 | 10,7 | . 0584 | 1,2 |
| . 782 | . 88671 | 306 | . 05501 | 289 | .9449I | 10,7 | . 0583 | 1,2 |
| . 783 | . 88977 | 306 | . 05790 | 289 | . 94502 | 10,7 | . 0582 | 1,2 |
| . 784 | .89283 | 306 | . 06079 | 289 | . 94513 | 10,7 | .0581 | 1,2 |
| 1.785 | 2.89589 | 306 | 3.06369 | 290 | 0.94523 | 10,7 | I. 0579 | 1,2 |
| . 786 | . 89896 | 307 | . 06659 | 290 | . 94534 | 10,6 | . 0578 | 1,2 |
| . 787 | . 90202 | 307 | . 05949 | 290 | . 94544 | 10,6 | . 0577 | I,2 |
| . 788 | . 90510 | 307 | . 07239 | 291 | . 94555 | 10,6 | . 0576 | 1,2 |
| .789 | .90817 | 308 | . 07530 | 291 | . 94565 | 10,6 | . 0575 | I,2 |
| 1.790 | 2.91125 | 308 | 3.07821 | 291 | 0.94576 | 10,6 | 1.0574 | 1,2 |
| .791 | .91433 | 308 | .08112 | 291 | . 94587 | 10,5 | . 0572 | 1,2 |
| . 792 | .91741 | 308 | . 08403 | 292 | . 94597 | 10,5 | . 0571 | 1,2 |
| . 793 | . 92049 | 309 | . 08695 | 292 | . 94608 | 10,5 | . 0570 | 1,2 |
| . 794 | . 92358 | 309 | . 08988 | 292 | .94618 | 10,5 | . 0569 | I,2 |
| 1.795 | 2.92667 | 309 | 3.09280 | 293 | 0.94629 | 10,5 | 1.0568 | 1,2 |
| . 796 | . 92977 | 310 | . 09573 | 293 | . 94639 | 10,4 | . 0566 | 1,2 |
| . 797 | . 93287 | 310 | . 09856 | 293 | . 94649 | IO,4 | . 0565 | 1,2 |
| . 798 | . 93597 | 310 | . 10160 | 294 | . 94660 | 10,4 | . 0564 | 1,2 |
| . 799 | . 93907 | 310 | . 10453 | 294 | . 94670 | 10,4 | . 0563 | 1,2 |
| 1.800 | 2.94217 | 3 II | 3.10747 | 294 | 0.94681 | 10,4 | 1. 0562 | 1,2 |
| u | $\boldsymbol{t a n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{g}$ d u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}$ | $\operatorname{coth} u$ | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.800 | 2.94217 | 311 | 3.10747 | 294 | 0.9468I | 10,4 | 1. 0562 | 1,2 |
| . 801 | . 94528 | 3 II | . I 1042 | 295 | .9469I | 10,3 | .056I | I,2 |
| . 802 | . 94840 | 3 II | . 11336 | 295 | . 94701 | 10,3 | . 0560 | I,2 |
| . 803 | .95151 | 312 | . 11631 | 295 | . 94712 | 10,3 | . 0558 | I, I |
| . 804 | . 95463 | 312 | . 11927 | 295 | . 94722 | 10,3 | . 0557 | I, I |
| 1.805 | 2.95775 | 312 | 3.12222 | 296 | 0.94732 | 10,3 | 1.0556 | I, I |
| . 806 | . 96087 | 313 | . 12518 | 296 | . 94742 | 10,2 | . 0555 | I, I |
| . 807 | . 96400 | 3 I 3 | . 12814 | 296 | . 94753 | 10,2 | . 0554 | I, I |
| . 808 | . 96713 | 313 | . 13 III | 297 | . 94763 | 10,2 | . 0553 | I, I |
| . 809 | . 97026 | 313 | . 13408 | 297 | . 94773 | 10,2 | . 0552 | I, I |
| 1.8 IO | 2.97340 | 314 | 3.13705 | 297 | 0.94783 | 10,2 | I. 0550 | I, I |
| .8II | . 97654 | 314 | . 14003 | 298 | . 94793 | 10, I | . 0549 | I, I |
| .812 | . 97968 | 314 | . 14300 | 298 | . 94803 | 10, I | . 0548 | I, I |
| . 813 | . 98282 | 315 | . 14599 | 298 | .94814 | 10,1 | . 0547 | I, I |
| .814 | . 98597 | 315 | . 14897 | 299 | . 94824 | 10, 1 | . 0546 | I, I |
| 1.815 | 2.98912 | 3 I 5 | 3.15196 | 299 | 0.94834 | 10,I | I. 0545 | I, I |
| .816 | . 99227 | 315 | . 15495 | 299 | . 94844 | 10,0 | . 0544 | I, I |
| .817 | . 99543 | 316 | . 15794 | 300 | . 94854 | 10,0 | . 0543 | I, I |
| . 818 | . 99859 | 316 | . 16094 | 300 | . 94864 | 10,0 | .054I | I, I |
| . 819 | 3.00175 | 316 | . 16394 | 300 | . 94874 | 10,0 | . 0540 | I, I |
| 1.820 | 3.00492 | 317 | 3. 16694 | 300 | 0.94884 | 10,0 | 1.0539 | I, I |
| . 821 | . 00808 | 3 I 7 | . 16995 | 301 | . 94894 | 10,0 | . 0538 | I, I |
| . 822 | . 01126 | 317 | . I7296 | 301 | . 94904 | 9,9 | . 0537 | I, I |
| . 823 | . 01443 | 318 | . I7597 | 301 | . 94914 | 9,9 | . 0536 | I, I |
| . 824 | . 01761 | 318 | . 17899 | 302 | . 94924 | 9,9 | . 0535 | I, I |
| 1. 825 | 3.02079 | 318 | 3. 18201 | 302 | 0.94933 | 9,9 | 1.0534 | I, I |
| . 826 | . 02397 | 319 | . 18503 | 302 | . 94943 | 9,9 | . 0533 | I, I |
| . 827 | . 02716 | 319 | . 18805 | 303 | . 94953 | 9,8 | . 0532 | I, I |
| . 828 | . 03035 | 319 | . 19108 | 303 | . 94963 | 9,8 | . 0530 | I, I |
| . 829 | . 03354 | 319 | . 194 II | 303 | . 94973 | 9,8 | . 0529 | I, I |
| 1.830 | 3.03674 | 320 | 3.19715 | 304 | 0.94983 | 9,8 | 1.0528 | I, I |
| . 831 | . 03994 | 320 | . 20019 | 304 | . 94992 | 9,8 | . 0527 | I, I |
| . 832 | . 04314 | 320 | . 20323 | 304 | . 95002 | 9,7 | . 0526 | I, I |
| . 833 | . 04634 | 321 | . 20627 | 305 | . 95012 | 9,7 | . 0525 | I, I |
| . 834 | . 04955 | 321 | . 20932 | 305 | . 95022 | 9,7 | . 0524 | I, I |
| 1.835 | 3.05276 | 321 | 3.21237 | 305 | 0.95031 | 9,7 | 1.0523 | I, I |
| . 836 | . 05597 | 322 | . 21543 | 306 | . 9504 I | 9,7 | . 0522 | I, I |
| . 837 | . 05919 | 322 | . 21849 | 306 | . 95051 | 9,7 | . 0521 | I, I |
| . 838 | .05241 | 322 | . 22155 | 306 | . 95060 | 9,6 | . 0520 | I, I |
| . 839 | . 05563 | 322 | . 22461 | 307 | . 95070 | 9,6 | . 0519 | I, I |
| I. 840 | 3.06886 | 323 | 3.22768 | 307 | 0.95080 | 9,6 | 1.0518 | I, I |
| .84I | . 07209 | 323 | . 23075 | 307 | . 95089 | 9,6 | .05I6 | I, I |
| . 842 | . 07532 | 323 | . 23382 | 308 | . 95099 | 9,6 | .0515 | I, I |
| . 843 | . 07856 | 324 | . 23690 | 308 | .95108 | 9,5 | .0514 | I, I |
| . 844 | .08180 | 324 | . 23998 | 308 | .951 18 | 9,5 | . 0513 | I, I |
| I. 845 | 3.08504 | 324 | 3.24306 | 309 | 0.95127 | 9,5 | 1.0512 | I, I |
| - .846 | . 08828 | 325 | . 24615 | 309 | .95137 | 9,5 | .0511 | 1,0 |
| . 847 | . 09153 | 325 | . 24924 | 309 | . 95146 | 9,5 | . 0510 | 1,0 |
| .848 | . 09478 | 325 | . 25233 | 309 | .95156 | 9,5 | . 0509 | 1,0 |
| . 849 | . 09803 | 326 | . 25543 | 310 | .95165 | 9,4 | . 0508 | 1,0 |
| 1.850 | 3.10129 | 326 | 3.25853 | 310 | 0.95175 | 9,4 | 1.0507 | I,O |
| u | $\boldsymbol{t a n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.850 | 3. 10129 | 326 | 3.25853 | 310 | 0.95175 | 9,4 | 1.0507 | 1,0 |
| . 851 | . 10455 | 326 | . 26163 | 310 | . 95184 | 9,4 | . 0506 | I, 0 |
| . 852 | . 1078 I | 326 | . 26474 | 311 | . 95193 | 9,4 | . 0505 | 1,0 |
| . 853 | . 11108 | 327 | . 26785 | 3 II | . 95203 | 9,4 | . 0504 | 1,0 |
| . 854 | . 11435 | 327 | . 27096 | 3 II | .95212 | 9,3 | . 0503 | 1,0 |
| 1. 855 | 3.11762 | 327 | 3.27408 | 312 | 0.95221 | 9,3 | 1.0502 | 1,0 |
| . 856 | . 12090 | 328 | . 27719 | 312 | .9523I | 9,3 | .0501 | 1,0 |
| . 857 | . 12418 | 328 | . 28032 | 312 | . 95240 | 9,3 | . 0500 | 1,0 |
| . 858 | . 12746 | 328 | . 28344 | 313 | -95249 | 9,3 | . 0499 | 1,0 |
| . 859 | . 13074 | 329 | . 28657 | 313 | -95259 | 9,3 | . 0498 | 1,0 |
| 1.860 | 3.13403 | 329 | 3.28970 | 313 | 0.95268 | 9,2 | 1.0497 | 1,0 |
| . 861 | . 13732 | 329 | . 29284 | 314 | . 95277 | 9,2 | . 0496 | 1,0 |
| . 862 | . 14062 | 330 | . 29598 | 314 | . 95286 | 9,2 | . 0495 | 1,0 |
| . 863 | - 14392 | 330 | . 29912 | 314 | . 95296 | 9,2 | . 0494 | 1,0 |
| . 864 | . 14722 | 330 | -30227 | 315 | . 95305 | 9,2 | . 0493 | 1,0 |
| 1.865 | 3.15052 | 33 I | 3.30542 | 315 | 0.95314 | 9,2 | 1.0492 | 1,0 |
| . 866 | . 15383 | 331 | . 30857 | 315 | . 95323 | 9, I | .0491 | 1,0 |
| . 867 | . 15714 | 33I | . 31172 | 316 | . 95332 | 9,I | . 0490 | 1,0 |
| . 868 | . 16045 | 331 | . 31488 | 316 | .95341 | 9, I | . 0489 | 1,O |
| . 869 | . 16377 | 332 | -31804 | 316 | -95350 | 9,I | . 0488 | I, 0 |
| 1.870 | 3. 16709 | 332 | 3.32121 | 317 | 0.95359 | 9,I | 1.0487 | I,O |
| . 871 | .17041 | 332 | . 32438 | 317 | . 95368 | 9,0 | . 0486 | 1,0 |
| . 872 | . 17374 | 333 | - 32755 | 317 | - 95378 | 9,0 | . 0485 | 1,0 |
| . 873 | - 17706 | 333 | - 33073 | 318 | -95387 | 9,0 | . 0484 | 1,0 |
| . 874 | . 18040 | 333 | . 33390 | 318 | . 95396 | 9,0 | . 0483 | 1,0 |
| I. 875 | 3. 18373 | 344 | 3.33709 | 318 | 0.95405 | 9,0 | 1.0482 | 1,0 |
| . 876 | . 18707 | 334 | - 34027 | 319 | . 95414 | 9,0 | .048I | 1,0 |
| . 877 | . 19041 | 334 | - 34346 | 319 | . 95422 | 8,9 | . 0480 | I,O |
| . 878 | . 19376 | 335 | . 34665 | 319 | .9543I | 8,9 | . 0479 | 1,0 |
| . 879 | . 197 II | 335 | . 34985 | 320 | . 95440 | 8,9 | . 0478 | I,O |
| 1.880 | 3.20046 | 335 | 3.35305 | 320 | 0.95449 | 8,9 | 1.0477 | 1,0 |
| . 88 I | .20381 | 336 | . 35625 | 320 | . 95458 | 8,9 | . 0476 | I,O |
| . 882 | . 20717 | 336 | . 35946 | 321 | . 95467 | 8,9 | . 0475 | 1,0 |
| . 883 | . 21053 | 336 | - 36266 | 321 | - 95476 | 8,8 | . 0474 | 1,0 |
| . 884 | . 21390 | 337 | -36588 | 32 I | - 95485 | 8,8 | . 0473 | 1,0 |
| 1.885 | 3.21726 | 337 | 3.36909 | 322 | 0.95493 | 8,8 | 1.0472 | I, 0 |
| . 886 | . 22063 | 337 | . 37231 | 322 | . 95502 | 8,8 | . 0471 | 1,0 |
| . 887 | . 22401 | 338 | - 37553 | 322 | -95511 | 8,8 | . 0470 | 1,0 |
| . 888 | . 22738 | 338 | - 37876 | 323 | - 95520 | 8,8 | . 0469 | I, 0 |
| . 889 | . 23076 | 338 | -38199 | 323 | -95529 | 8,7 | . 0468 | I,O |
| 1.890 | 3.23415 | 339 | 3.38522 | 323 | 0.95537 | 8,7 | 1.0467 | I,O |
| . 891 | . 23753 | 339 | . 38846 | 324 | . 95546 | 8,7 | . 0466 | I,O |
| . 892 | . 24093 | 339 | - 39170 | 324 | . 95555 | 8,7 | . 0465 | I,O |
| . 893 | . 24432 | 339 | - 39494 | 324 | - 95563 | 8,7 | . 0464 | I,O |
| . 894 | . 24772 | 340 | - 39818 | 325 | . 95572 | 8,7 | . 0463 | 0,9 |
| 1. 895 | 3.25112 | 340 | 3.40143 | 325 | 0.9558 I | 8,6 | 1.0462 | 0,9 |
| . 896 | . 25452 | 340 | . 40469 | 325 | . 95588 | 8,6 | . 0461 | 0,9 |
| . 897 | . 25792 | 341 | . 40794 | 326 | . 95598 | 8,6 | . 0460 | 0,9 |
| . 898 | . 26133 | 341 | .41120 | 326 | -95607 | 8,6 | . 0460 | 0,9 |
| . 899 | . 26475 | 341 | .41447 | 326 | -95615 | 8,6 | . 0459 | 0,9 |
| 1.900 | 3.26816 | 342 | 3.41773 | 327 | 0.95624 | 8,6 | 1.0458 | 0,9 |
| u | $\boldsymbol{t a n} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { c o s h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{c o t h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.900 | 3.26816 | 342 | 3.41773 | 327 | 0.95624 | 8,6 | 1.0458 | 0,9 |
| .90I | .27158 | 342 | . 42100 | 327 | . 95632 | 8,5 | . 0457 | 0,9 |
| . 902 | . 27500 | 342 | . 42427 | 328 | .9564I | 8,5 | . 0456 | 0,9 |
| . 903 | . 27843 | 343 | . 42755 | 328 | . 95649 | 8,5 | . 0455 | 0,9 |
| . 904 | . 28186 | 343 | . 43083 | 328 | . 95658 | 8,5 | . 0454 | 0,9 |
| 1.905 | 3.28529 | 343 | 3.43412 | 329 | 0.95666 | 8,5 | I. 0453 | 0,9 |
| . 906 | . 28873 | 344 | . 43740 | 329 | . 95675 | 8,5 | . 0452 | 0,9 |
| . 907 | . 29217 | 344 | . 44069 | 329 | . 95683 | 8,4 | .045I | 0,9 |
| . 908 | . 2956I | 344 | . 44399 | 330 | . 95692 | 8,4 | . 0450 | 0,9 |
| . 909 | . 29906 | 345 | . 44728 | 330 | . 95700 | 8,4 | . 0449 | 0,9 |
| 1.910 | $3 \cdot 30250$ | 345 | 3.45058 | 330 | 0.95709 | 8,4 | 1.0448 | 0,9 |
| .91I | . 30596 | 345 | . 45389 | 33 I | . 95717 | 8,4 | . 0447 | 0,9 |
| . 912 | . 3094 I | 346 | . 45720 | 33 I | . 95725 | 8,4 | . 0447 | 0,9 |
| . 913 | . 31287 | 346 | . 46051 | 331 | . 95734 | 8,4 | . 0446 | 0,9 |
| .914 | . 31633 | 346 | . 46382 | 332 | . 95742 | 8,3 | . 0445 | 0,9 |
| 1.915 | 3.31980 | 347 | 3.46714 | 332 | 0.95750 | 8,3 | 1.0444 | 0,9 |
| . 916 | . 32327 | 347 | . 47046 | 332 | . 95759 | 8,3 | . 0443 | 0,9 |
| .917 | . 32674 | 347 | . 47379 | 333 | . 95767 | 8,3 | . 0442 | 0,9 |
| .918 | . 33021 | 348 | . 47712 | 333 | . 95775 | 8,3 | .044I | 0,9 |
| . 919 | . 33369 | 348 | . 48045 | 333 | . 95783 | 8,3 | . 0440 | 0,9 |
| 1.920 | 3.33718 | 348 | 3.48378 | 334 | 0.95792 | 8,2 | 1.0439 | 0,9 |
| . 921 | . 34066 | 349 | . 48712 | 334 | . 95800 | 8,2 | . 0438 | 0,9 |
| . 922 | . 34415 | 349 | . 49046 | 334 | .95808 | 8,2 | . 0438 | 0,9 |
| . 923 | . 34764 | 349 | .4938I | 335 | .95816 | 8,2 | . 0437 | 0,9 |
| . 924 | .35II4 | 350 | . 49716 | 335 | .95825 | 8,2 | . 0436 | 0,9 |
| 1.925 | 3.35464 | 350 | $3 \cdot 50051$ | 335 | 0.95833 | 8,2 | 1. 0435 | 0,9 |
| . 926 | . 35814 | 350 | . 50387 | 336 | .9584I | 8,1 | . 0434 | 0,9 |
| . 927 | . 36164 | 351 | . 50723 | 336 | . 95849 | 8, I | . 0433 | 0,9 |
| . 928 | . 36515 | 351 | . 51059 | 337 | . 95857 | 8, I | . 0432 | 0,9 |
| . 929 | . 36867 | 351 | . 51396 | 337 | . 95865 | 8,1 | .043I | 0,9 |
| 1.930 | 3.37218 | 352 | 3.51733 | 337 | 0.95873 | 8, I | 1. 0430 | 0,9 |
| .93I | . 37570 | 352 | . 52070 | 338 | .9588I | 8, I | . 0430 | 0,9 |
| . 932 | . 37922 | 352 | . 52408 | 338 | . 95890 | 8, I | . 0429 | 0,9 |
| . 933 | . 38275 | 353 | . 52746 | 338 | . 95898 | 8,0 | . 0428 | 0,9 |
| . 934 | . 38628 | 353 | . 53085 | 339 | . 95906 | 8,0 | . 0427 | 0,9 |
| I. 935 | $3 \cdot 3898 \mathrm{I}$ | 353 | $3 \cdot 53423$ | 339 | 0.95914 | 8,0 | 1. 0426 | 0,9 |
| . 936 | . 39335 | 354 | . 53763 | 339 | . 95922 | 8,0 | . 0.425 | 0,9 |
| . 937 | . 39689 | 354 | . 54102 | . 340 | . 95930 | 8,0 | . 0424 | 0,9 |
| . 938 | . 40043 | 354 | . 54442 | 340 | . 95938 | 8,0 | . 0423 | 0,9 |
| . 939 | . 40397 | 355 | . 54782 | 340 | . 95945 | 7,9 | . 0423 | 0,9 |
| 1.940 | 3.40752 | 355 | 3.55123 | 341 | - 0.95953 | 7,9 | 1.0422 | 0,9 |
| .94I | . 41108 | 355 | . 55464 | 341 | .9596I | 7,9 | .0421 | 0,9 |
| . 942 | . 41463 | 356 | . 55805 | 341 | . 95969 | 7,9 | . 0420 | 0,9 |
| . 943 | .41819 | 356 | . 56147 | 342 | . 95977 | 7,9 | .0419 | 0,9 |
| . 944 | . 42176 | 356 | . 56489 | 342 | . 95985 | 7,9 | .0418 | 0,9 |
| 1.945 | 3.42532 | 357 | 3.56831 | 343 | 0.95993 | 7,9 | 1.0417 | 0,9 |
| . 946 | . 42889 | 357 | . 57174 | 343 | . 96001 | 7,8 | .0417 | 0,9 |
| . 947 | . 43247 | 358 | . 57517 | 343 | . 96009 | 7,8 | .0416 | 0,9 |
| . 948 | . 43604 | 358 | . 57860 | 344 | .96016 | 7,8 | .0415 | 0,9 |
| . 949 | . 43962 | 358 | . 58204 | 344 | .96024 | 7,8 | .04I4 | 0,9 |
| 1.950 | 3.4432 I | 359 | 3.58548 | 344 | 0.96032 | 7,8 | 1.0413 | 0,8 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | sec gd u | ${ }_{0}{ }^{\text {F }}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| 4 | $\sinh u$ | $\omega F^{\prime}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.950 | 3.14321 | 359 | $3 \cdot 58548$ | 344 | 0.96032 | 7,8 | 1.0413 | 0,8 |
| . 951 | . 44679 | 359 | . 58893 | 345 | . 96040 | 7,8 | . 0412 |  |
| . 952 | . 45038 | 359 | . 59237 | 345 | . 96047 | 7,7 | . 0412 |  |
| . 953 | . 45398 | 360 | . 59583 | 345 | . 96055 | 7,7 | .04II |  |
| . 954 | . 45758 | 360 | - 59928 | 346 | . 96053 | 7,7 | . 0410 |  |
| 1.955 | 3.46118 | 360 | 3.60274 | 346 | 0.95071 | 7,7 | 1.0409 | 0,8 |
| . 956 | . 46478 | 361 | . 60620 | 346 | . 96078 | 7,7 | . 0408 |  |
| . 957 | . 46839 | 261 | . 60967 | 347 | .96086 | 7,7 | . 0407 |  |
| . 958 | . 47200 | 361 | .6I3I4 | 347 | . 96094 | 7,7 | . 0407 |  |
| . 959 | . 47562 | 362 | . 61662 | 348 | .96101 | 7,6 | . 0406 |  |
| 1.950 | 3.47923 | 362 | 3.62009 | 348 | 0.96109 | 7,6 | 1.0405 | 0,8 |
| -961 | . 48286 | 362 | . 62357 | 348 | .96117 | 7,6 | . 0404 |  |
| . 952 | . 48648 | 363 | . 62706 | 349 | .96124 | 7,6 | . 0403 |  |
| . 963 | . 4901 I | 363 | . 63055 | 349 | .96132 | 7,6 | . 0402 |  |
| . 964 | . 49374 | 363 | . 63404 | 349 | . 96139 | 7,6 | . 0402 |  |
| 1.965 | 3.49738 | 364 | 3.63753 | 350 | 0.96147 | 7,6 | I. 0401 | 0,8 |
| . 966 | . 50102 | 364 | . 64103 | 350 | . 96155 | 7,5 | . 0400 |  |
| . 957 | . 50466 | 364 | . 64454 | 350 | .96162 | 7,5 | . 0399 |  |
| . 968 | . 50831 | 365 | . 64804 | 35 I | .96I70 | 7,5 | . 0398 |  |
| . 969 | . 51196 | 365 | . 65155 | 35 I | .95177 | 7,5 | . 0397 |  |
| 1.970 | 3.51561 | 366 | 3.65507 | 352 | 0.96185 | 7,5 | 1.0397 | 0,8 |
| . 971 | . 51927 | 366 | . 65858 | 352 | .96192 | 7,5 | . 0396 |  |
| . 972 | . 52293 | 366 | . 662 I I | 352 | .96199 | 7,5 | . 0395 |  |
| . 973 | . 52659 | 367 | . 66563 | 353 | .96207 | 7,4 | . 0394 |  |
| . 974 | . 53026 | 367 | -. 66916 | 353 | .96214 | 7,4 | . 0393 |  |
| 1.975 | $3 \cdot 53393$ | 367 | 3.67269 | 353 | 0.96222 | 7,4 | 1.0393 | 0,8 |
| . 976 | . 53760 | 368 | . 67623 | 354 | . 96229 | 7,4 | . 0392 |  |
| . 977 | . 54128 | 368 | . 67977 | 354 | . 96237 | 7,4 | .0391 |  |
| . 978 | . 54495 | 368 | . 68331 | 354 | .96244 | 7,4 | . 0390 |  |
| . 979 | . 54855 | 369 | . 68686 | 355 | .9525I | 7,4 | . 0389 |  |
| 1.980 | $3.55234{ }^{\text { }}$ | 369 | 3.69041 | 355 | 0.96259 | 7,3 | I. 0389 | 0,8 |
| .98I | . 55603 | 369 | . 69395 | 356 | .96255 | 7,3 | . 0388 |  |
| . 982 | . 55972 | 370 | . 69752 | 356 | . 96273 | 7,3 | . 0387 |  |
| . 983 | . 56342 | 370 | . 70108 | 356 | .9528I | 7,3 | . 0386 |  |
| . 984 | . 56713 | 370 | . 70465 | 357 | . 96288 | 7,3 | . 0386 |  |
| 1.985 | 3.57083 | 371 | 3.70821 | 357 | 0.96295 | 7,3 | 1. 0385 | 0,8 |
| . 985 | . 57454 | 371 | . 71179 | 357 | . 96302 | 7,3 | . 0384 |  |
| . 987 | . 57826 | 372 | . 71536 | 358 | .96310 | 7,2 | . 0383 |  |
| . 988 | . 58197 | 372 | . 71894 | 358 | .963I7 | 7,2 | . 0382 |  |
| .989 | . 58569 | 372 | . 72253 | 359 | .95324 | 7,2 | . 0382 |  |
| 1.990 | $3 \cdot 58942$ | 373 | 3.726 II | 359 | 0.9633 I | 7,2 | I. 038 I | 0,8 |
| .99I | . 59315 | 373 | . 72971 | 359 | . 96339 | 7,2 | . 0380 |  |
| . .992 | . 59588 | 373 | . 73330 | 360 | . $96346^{\circ}$ | 7,2 | . 0379 |  |
| . 993 | . 60061 | 374 | .73690 | 350 | . 96353 | 7,2 | . 0379 |  |
| . 994 | . 60435 | 374 | . 74050 | 350 | . 96360 | 7,1 | . 0378 |  |
| 1.995 | 3.60809 | 374 | 3.744 II | 361 | 0.96367 | 7,I | 1.0377 | 0,8 |
| . 996 | .6I I84 | 375 | . 74772 | 361 | . 95374 | 7,1 | . 0376 |  |
| . 997 | . 61559 | 375 | . 75133 | 362 | . 96382 | 7,I | . 0375 |  |
| . 998 | . 61934 | 375 | . 75495 | 362 | . 96389 | 7, I | . 0375 |  |
| . 999 | . 62310 | 376 | . 75857 | 362 | . 96396 | 7,I | . 0374 |  |
| 2.000 | 3.62686 | 376 | 3.76220 | 363 | 0.95403 | 7,I | 1.0373 | 0,8 |
| $u$ | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} u$ | $\omega F_{0}{ }^{\text {, }}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} 4$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\circ}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.000 | 3.62686 | 376 | 3.76220 | 363 | 0.96403 | 7,1 | 1. 0373 | 0,8 |
| . 01 | . 63062 | 377 | . 76582 | 363 | .95410 | 7,1 | . 0372 |  |
| . 002 | . 63439 | 377 | . 76946 | 363 | . 96417 | 7,0 | . 0372 |  |
| . 003 | . 63816 | 377 | . 77309 | 364 | . 96424 | 7,0 | . 0371 |  |
| . 004 | . 64194 | 378 | . 77673 | 364 | . 9643 I | 7,0 | . 0370 |  |
| 2.005 | 3.64572 | 378 | 3.78038 | 365 | 0.96438 | 7,0 | 1.0369 | 0,8 |
| . 006 | . 64950 | 378 | . 78402 | 365 | . 96445 | 7,0 | . 0369 | 0,8 |
| . 007 | . 65328 | 379 | . 78768 | 365 | . 96452 | 7,0 | . 0368 | 0,7 |
| . 008 | . 65707 | 379 | . 79133 | 366 | . 96459 | 7,0 | . 0367 |  |
| . 009 | . 66087 | 379 | . 79499 | 366 | . 96466 | 6,9 | . 3366 |  |
| 2.010 | 3.66466 | 380 | 3.79865 | 366 | 0.96473 | 6,9 | 1.0366 | 0,7 |
| . OII | . 66846 | 380 | . 80232 | 367 | . 96480 | 6,9 | . 0365 | 0, |
| . 012 | . 67227 | 38 I | . 80599 | 367 | . 95487 | 6,9 | . 0364 |  |
| . 013 | . 67608 | 381 | . 80966 | 368 | . 96493 | 6,9 | . 0363 |  |
| . 014 | . 67989 | 38I | .81334 | 368 | . 96500 | 6,9 | . 0363 |  |
| 2.015 | 3.68370 | 382 | 3.81702 | 368 | 0.96507 | 6,9 | 1.0362 | 0,7 |
| . 016 | . 68752 | 382 | . 82071 | 369 | . 96514 | 6,9 | .0361 |  |
| . 017 | . 69134 | 382 | . 82440 | 369 | . 9652 I | 6,8 | . 0360 |  |
| .oı8 | . 69517 | 383 | . 82809 | 370 | . 96528 | 6,8 | . 0360 |  |
| . 019 | . 69900 | 383 | . 83179 | 370 | . 96535 | 6,8 | . 0359 |  |
| 2.020 | 3.70283 | 384 | 3.83549 | 370 | 0.96541 | 6,8 | 1.0358 | 0,7 |
| . 021 | . 70667 | 384 | . 83919 | 37 I | . 96548 | 6,8 | . 0358 |  |
| . 022 | . 71051 | 384 | . 84290 | 37 I | . 96555 | 6,8 | . 0357 |  |
| . 023 | . 71436 | 385 | . 84662 | 371 | . 96562 | 6,8 | . 0356 |  |
| . 024 | . 71821 | 385 | . 85033 | 372 | . 96568 | 6,7 | . 0355 |  |
| 2.025 | 3.72206 | 385 | 3.85405 | 372 | 0.96575 | 6,7 | 1.0355 | 0,7 |
| . 025 | . 72591 | 386 | . 85778 | 373 | . 96582 | 6,7 | . 0354 |  |
| . 027 | . 72977 | 386 | . 86150 | 373 | . 96589 | 6,7 | . 0353 |  |
| . 028 | . 73364 | 387 | . 86524 | 373 | . 96595 | 6,7 | . 0352 |  |
| . 029 | . 73750 | 387 | . 86897 | 374 | . 96602 | 6,7 | . 0352 |  |
| 2.030 | 3.74138 | 387 | 3.87271 | 374 | 0.96609 | 6,7 | 1.0351 | 0,7 |
| .031 | . 74525 | 388 | . 87645 | 375 | .96515 | 6,7 | . 0350 |  |
| . 032 | . 74913 | 388 | . 88020 | 375 | . 96622 | 6,6 | . 0350 |  |
| . 033 | . 75301 | 388 | . 88395 | 375 | . 96629 | 6,6 | . 0349 |  |
| . 034 | . 75690 | 389 | . 8877 I | 376 | .96635 | 6,6 | . 0348 |  |
| 2.035 | 3.76079 | 389 | 3.89147 | 376 | 0.96642 | 6,6 |  | 0,7 |
| . 036 | . 76468 | 390 | . 89523 | 376 | . 96648 | 6,6 | . 0347 |  |
| . 037 | . 76858 | 390 | . 89900 | 377 | . 96655 | 6,6 | . 0346 |  |
| . 038 | . 77248 | 390 | . 90277 | 377 | . 96662 | 6,6 | . 0345 |  |
| . 039 | . 77638 | 391 | . 90654 | 378 | . 96668 | 6,6 | . 0345 |  |
| 2.040 | 3.78029 | 391 | 3.91032 | 378 | 0.96675 | 6,5 | I. 0344 | 0,7 |
| . 041 | . 78120 | 391 | . 91410 | 378 | . 9668 I | 6,5 | . 0343 |  |
| . 042 | . 78812 | 392 | . 91789 | 379 | . 96688 | 6,5 | . 0343 |  |
| . 043 | . 79204 | 392 | . 92168 | 379 | . 96694 | 6,5 | . 0342 |  |
| . 044 | . 79596 | 393 | . 92547 | 380 | .96701 | 6,5 | .034I |  |
| 2.045 | 3.79989 | 393 | 3.92927 | 380 | 0.96707 | 6,5 | 1.0340 | 0,7 |
| . 046 | . 80382 | 393 | . 93307 | 380 | . 95714 | 6,5 | . 0340 |  |
| . 047 | . 80776 | 394 | . 93688 | 38 I | . 96720 | 6,5 | . 0339 |  |
| . 048 | . 81169 | 394 | . 94069 | 381 | . 96727 | 6,4 | . 0338 |  |
| . 049 | .81564 | 394 | . 94450 | 382 | . 96733 | 6,4 | . 0338 |  |
| 2.050 | 3.81958 | 395 | 3.94832 | 382 | 0.96740 | 6,4 | 1.0337 | 0,7 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { s i n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.050 | 3.81958 | 395 | 3.94832 | 382 | 0.96740 | 6,4 | 1.0337 | 0,7 |
| . 051 | . 82353 | 395 | . 95214 | 382 | . 96746 | 6,4 | . 0336 |  |
| . 052 | . 82749 | 396 | . 95597 | 383 | . 96752 | 6,4 | . 0336 |  |
| . 053 | . 83145 | 396 | . 95979 | 383 | . 96759 | 6,4 | . 0335 |  |
| . 054 | . 8354 I | 396 | . 96363 | 384 | . 96765 | 6,4 | . 0334 |  |
| 2.055 | 3.83937 | 397 | 3.96747 | 384 | 0.96771 | - 6,4 | 1.0334 | 0,7 |
| . 056 | . 84334 | 397 | .97131 | 384 | . 96778 | 6,3 | . 0333 |  |
| . 057 | . 84732 | 398 | . 97515 | 385 | . 96784 | 6,3 | . 0332 |  |
| . 058 | . 85129 | 398 | -97900 | 385 | . 96790 | 6,3 | . 0332 |  |
| . 059 | . 85527 | 398 | . 98285 | 386 | . 95797 | 6,3 | .033I |  |
| 2.060 | 3.85926 | 399 | 3.98571 | 386 | 0.96803 | 6,3 | 1.0330 | 0,7 |
| . 061 | . 85325 | 399 | . 99057 | 386 | . 96809 | 6,3 | . 0330 |  |
| . 062 | . 86724 | 399 | . 99444 | 387 | . 96816 | 6,3 | . 0329 |  |
| . 063 | . $87124^{\circ}$ | 400 | . 99831 | 387 | . 96822 | 6,3 | . 0328 |  |
| . 064 | . 87524 | 400 | 4.00218 | 388 | . 96828 | 6,2 | . 0328 |  |
| 2.065 | 3.87924 | 401 | 4.00606 | 388 | 0.96834 | 6,2 | 1.0327 | 0,7 |
| . 066 | . 88325 | 401 | . 00994 | 388 | . 9684 | 6,2 | . 0326 |  |
| . 067 | . 88726 | 401 | . 01382 | 389 | . 96847 | 6,2 | . 0326 |  |
| . 068 | . 89128 | 402 | . 01771 | 389 | . 96853 | 6,2 | . 0325 |  |
| . 069 | . 89530 | 402 | .02161 | 390 | . 96859 | 6,2 | . 0324 |  |
| 2.070 | 3.89932 | 403 | 4.02550 | 390 | 0.96865 | 6,2. | 1.0324 | 0,7 |
| . 071 | . 90335 | 403 | . 02941 | 390 | . 96872 | 6,2 | . 0323 |  |
| . 072 | . 90738 | 403 | .03331 | 391 | . 96878 | 6,1 | . 0322 |  |
| . 073 | .91141 | 404 | . 03722 | 391 | . 96884 | 6,1 | . 0322 |  |
| :074 | .91545 | 404 | .04113 | 392 | . 96890 | 6, I | . 0321 |  |
| 2.075 | 3.91950 | 405 | 4.04505 | 392 | 0.96896 | 6, 1 | 1.0320 | 0,7 |
| . 076 | . 92354 | 405 | . 04897 | 392 | . 96902 | 6,1 | . 0320 | 0,6 |
| . 077 | . 92759 | 405 | . 05290 | 393 | . 96908 | 6, I | . 0319 |  |
| . 078 | . 93165 | 406 | . 05683 | 393 | . 96914 | 6, I | .0318 |  |
| . 079 | .9357I | 406 | . 06076 | 394 | . 96920 | 6, I | . 0318 |  |
| 2.080 | 3.93977 | 406 | 4.06470 | 394 | 0.96926 |  |  | 0,6 |
| . 081 | . 94384 | 407 | . 06864 | 394 | . 96933 | 6,0 | . 0316 |  |
| . 082 | . 94791 | 407 | . 07259 | 395 | . 96939 | 6,0 | . 0316 |  |
| . 083 | . 95198 | 408 | . 07654 | 395 | . 96945 | 6,0 | . 0315 |  |
| . 084 | . 95606 | 408 | . 08049 | 396 | . 96951 | 6,0 | . 0315 |  |
| 2.085 | 3.96014 | 408 | 4.08445 | 396 | 0.96957 | 6,0 | 1.0314 | 0,6 |
| . 086 | . 96423 | 409 | .0884I | 396 | . 96963 | 6,0 | . 0313 |  |
| . 087 | . 96832 | 409 | . 09238 | 397 | . 96969 | 6,0 | . 0313 |  |
| . 088 | . 9724 I | 410 | . 09635 | 397 | . 96975 | 6,0 | .0312 |  |
| . 089 | .9765I | 410 | . 10032 | 398 | . 96980 | 5,9 | .03II |  |
| 2.090 | 3.98061 | 410 | 4. 10430 | 398 | 0.96986 | 5,9 | 1.0311 | o,6 |
| . 091 | . 98472 | 411 | . 10828 | 398 | . 95992 | 5,9 | .0310 |  |
| . 092 | . 98883 | 4 II | . 11227 | 399 | . 96998 | 5,9 | . 0309 |  |
| . 093 | -99294 | 412 | . 11626 | 399 | . 97004 | 5,9 | . 0309 |  |
| . 094 | -99706 | 412 | . 12026 | 400 | . 97010 | 5.9 | . 0308 |  |
| 2.095 | 4.00119 | 412 | 4. 12426 | 400 | 0.97016 | 5,9 | 1.0308 | 0,6 |
| . 096 | .00531 | 413 | . 12826 | 401 | . 97022 | 5,9 | . 0307 |  |
| . 097 | . 00944 | 413 | . 13227 | 401 | . 97028 | 5,9 | . 0306 |  |
| . 098 | . 01358 | 414 | . 13628 | 401 | . 97034 | 5,8 | . 0306 |  |
| . 099 | .01771 | 414 | - 14029 | 402 | . 97039 | 5,8 | . 0305 |  |
| 2. 100 | 4.02186 | 414 | 4.14431 | 402 | 0.97045 | 5,8 | 1.0304 | 0,6 |
| $u$ | $\boldsymbol{t a n}$ od $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec$ gd $u$ | $\omega \mathrm{Fo}^{\prime}$ | $\boldsymbol{s i n g d u}$. | $\omega \mathrm{Fo}^{\prime}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

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Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{Fo}^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.100 | 4.02186 | 414 | 4.1443I | 402 | 0.97045 | 5,8 | 1.0304 | 0,6 |
| . 101 | . 02600 | 415 | . 14834 | 403 | .9705I | 5,8 | . 0304 |  |
| . 102 | .03015 | 415 | . 15237 | 403 | . 97057 | 5,8 | . 0303 |  |
| . 103 | .0343I | 416 | . 15640 | 403 | . 97063 | 5,8 | . 0303 |  |
| . 104 | . 03847 | 416 | . 16043 | 404 | . 97068 | 5,8 | . 0302 |  |
| 2.105 | 4.04263 | 416 | 4.16447 | 404 | 0.97074 | 5,8 | 1.0301 | 0,6 |
| . 106 | . 04680 | 417 | . 16852 | 405 | . 97080 | 5,8 | .0301 |  |
| . 107 | . 05097 | 417 | . 17257 | 405 | . 97086 | 5,7 | . 0300 |  |
| . 108 | .05514 | 418 | . 17662 | 406 | .97091 | 5,7 | . 0300 |  |
| .109 | . 05932 | 418 | . 18068 | 406 | . 97097 | 5,7 | . 0299 |  |
| 2.110 | 4.06350 | 418 | 4. 18474 | 406 | 0.97103 | 5,7 | 1. 0298 | 0,6 |
| . III | . 06769 | 419 | . 1888 I | 407 | .97109 | 5,7 | . 0298 |  |
| . 112 | . 07188 | 419 | . 19288 | 407 | .97114 | 5,7 | . 0297 |  |
| . II3 | . 07607 | 420 | . 19695 | 408 | . 97120 | 5,7 | . 0297 |  |
| . 114 | . 08027 | 420 | . 20103 | 408 | . 97126 | 5,7 | . 0296 |  |
| 2.II5 | 4.08448 | 42 I | 4.205 II | 408 | 0.97131 | 5,7 | 1.0295 | 0,6 |
| . i16 | . 08868 | 42 I | . 20920 | 409 | .97137 | 5,6 | . 0295 |  |
| . 117 | . 09289 | 421 | . 21329 | 409 | .97143 | 5,6 | . 0294 |  |
| . 118 | .097II | 422 | . 21738 | 410 | .97148 | 5,6 | . 0294 |  |
| . 119 | . 10133 | 422 | . 22148 | 410 | . 97154 | 5,6 | . 0293 |  |
| 2.120 | 4. 10555 | 423 | 4.22558 | 411 | 0.97159 | 5,6 | I. 0292 | 0,6 |
| . 121 | . 10978 | 423 | . 22969 | 4II | .97165 | 5,6 | . 0292 |  |
| . 122 | . II40I | 423 | . 23380 | 4 II | .97171 | 5,6 | .0291 |  |
| . 123 | . II825 | 424 | . 23792 | 412 | .97176 | 5,6 | .0291 |  |
| . 124 | . 12249 | 424 | . 24204 | 412 | . 97182 | 5,6 | . 0290 |  |
| 2.125 | 4. 12673 | 425 | 4.24617 | 413 | 0.97187 | 5,5 | 1.0289 | 0,6 |
| . 126 | . I3098 | 425 | . 25029 | 413 | . 97193 | 5,5 | . 0289 |  |
| . 127 | . I3523 | 425 | . 25443 | 414 | . 97198 | 5,5 | . 0288 |  |
| . 128 | . 13949 | 426 | . 25856 | 414 | . 97204 | 5,5 | . 0288 |  |
| . 129 | . 14375 | 426 | . 2627 I | 414 | . 97209 | 5,5 | . 0287 |  |
| 2.130 | 4.14801 | 427 | 4.26685 | 415 | 0.97215 | 5,5 | 1.0286 | 0,6 |
| . 131 | . 15228 | 427 | . 27100 | 415 | . 97220 | 5,5 | . 0286 |  |
| . 132 | . I 5656 | 428 | . 27516 | 416 | . 97226 | 5,5 | . 0285 |  |
| . I33 | . 16083 | 428 | . 27932 | 416 | .9723I | 5,5 | . 0285 |  |
| . 134 | . 16512 | 428 | . 28348 | 417 | . 97237 | 5,4 | . 0284 |  |
| 2.135 | 4. 16940 | 429 | 4.28765 | 417 | 0.97242 | 5,4 | 1.0284 | 0,6 |
| . 136 | . 17369 | 429 | . 29182 | 417 | . 97248 | 5,4 | . 0283 |  |
| . 137 | . 17798 | 430 | . 29599 | 418 | . 97253 | 5,4 | . 0282 |  |
| . 138 | . 18228 | 430 | . 30017 | 418 | . 97258 | 5,4 | . 0282 |  |
| . 139 | . 18558 | 430 | . 30436 | 419 | . 97264 | 5,4 | .028I |  |
| 2.140 | 4.19089 | 431 | 4.30855 | 419 | 0.97269 | 5,4 | I. 028 I | 0,6 |
| . 141 | . 19520 | 431 | . 31274 | 420 | . 97275 | 5,4 | . 0280 |  |
| . 142 | . 19952 | 432 | . 31694 - | 420 | . 97280 | 5,4 | . 0280 |  |
| . 143 | . 20384 | 432 | . 32 II4 | 420 | . 97285 | 5,4 | . 0279 |  |
| . 144 | . 20816 | 433 | . 32534 | 42 I | .97291 | 5,3 | . 0278 |  |
| 2. 145 | 4.21249 | 433 | 4.32955 | 42 I | 0.97296 | 5,3 | 1.0278 | 0,6 |
| . 146 | . 21682 | 433 | - 33377 | 422 | .97301 | 5,3 | . 0277 |  |
| . 147 | . 22115 | 434 | - 33799 | 422 | . 97307 | 5,3 | . 0277 |  |
| . 148 | . 22549 | 434 | -3422I | 423 | .97312 | 5,3 | . 0276 |  |
| . 149 | . 22984 | 435 | . 34644 | 423 | .97317 | 5,3 | . 0276 |  |
| 2.150 | 4.23419 | 435 | 4.35067 | 423 | 0.97323 | 5,3 | 1.0275 | 0,6 |
| $u$ | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc g d \mathrm{u}$ | $\omega \mathrm{F}^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathbf{F}^{\prime}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}$ | coth u | $\omega \mathbf{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.150 | 4.23419 | 435 | 4.35067 | 423 | 0.97323 | 5,3 | 1. 0275 | 0,6 |
| . 151 | . 23854 | 435 | . 35491 | 424 | . 97328 | 5,3 | . 0275 |  |
| . 152 | . 24290 | 436 | . 35915 | 424 | . 97333 | 5,3 | . 0274 |  |
| . 153 | . 24726 | 436 | -36339 | 425 | . 97338 | 5,3 | . 0273 |  |
| . 154 | . 25162 | 437 | . 36764 | 425 | . 97344 | 5,2 | . 0273 |  |
| 2. 155 | 4.25599 | 437 | $4 \cdot 37190$ | 426 | 0.97349 | 5,2 | I. 0272 | 0,6 |
| . 156 | . 26037 | 438 | .376I5 | 426 | . 97354 | 5,2 | . 0272 | 0,6 |
| . 157 | . 26475 | 438 | . 38042 | 426 | . 97359 | 5,2 | . 0271 | 0,5 |
| . 158 | . 26913 | 438 | . 38468 | 427 | . 97365 | 5,2 | . 0271 | 0,5 |
| . 159 | . 27352 | 439 | . 38896 | 427 | . 97370 | 5,2 | . 0270 | 0,5 |
| 2.160 | 4.27791 | 439 | $4 \cdot 39323$ | 428 | 0.97375 | 5,2 | 1.0270 | 0,5 |
| .16I | . 28230 | 440 | . 39751 | 428 | . 97380 | 5,2 | . 0269 |  |
| . 162 | . 28570 | 440 | . 40180 | 429 | . 97385 | 5,2 | . 0268 |  |
| . 163 | .29III | 44 I | . 40608 | 429 | . 97390 | 5,2 | . 0268 |  |
| . 164 | . 2955 I | 44 I | . 41038 | 430 | . 97396 | 5, I | . 0267 |  |
| 2.165 | 4.29993 | 44 I | 4.41468 | 430 | 0.97401 | 5, I | 1. 0267 | 0,5 |
| . 166 | . 30434 | 442 | . 41898 | 430 | . 97406 | 5,1 | . 0266 |  |
| . 167 | . 30876 | 442 | . 42328 | 431 | . 9741 I | 5,I | . 0266 |  |
| . 168 | .31319 | 443 | . 42760 | 43 I | . 97416 | 5, I | . 0265 |  |
| . 169 | . 31762 . | 443 | .43191 | 432 | .9742I | 5, I | . 0265 |  |
| 2.170 | $4 \cdot 32205$ | 444 | 4.43623 | 432 | 0.97426 | 5, I | 1. 0264 | 0,5 |
| .171 | . 32649 | 444 | . 44056 | 433 | .9743I | 5, I | . 0264 |  |
| . 172 | . 33093 | 444 | . 44488 | 433 | . 97436 | 5, I | . 0263 |  |
| . 173 | . 33538 | 445 | . 44922 | 434 | . 9744 I | 5, I | . 0263 |  |
| $\because 174$ | . 33983 | 445 | . 45355 | 434 | . 97446 | 5,0 | . 0262 |  |
| 2.175 | 4.34429 | 446 | 4.45790 | 434 | 0.97452 | 5,0 | 1.0262 | 0,5 |
| . 175 | . 34875 | 446 | . 46224 | 435 | . 97457 | 5,0 | .026I |  |
| . 177 | . 3532 I | 447 | . 46659 | 435 | . 97462 | 5,0 | . 0260 |  |
| . 178 | . 35768 | 447 | . 47095 | 436 | . 97467 | 5,0 | . 0260 |  |
| . 179 | . 362 I 5 | 448 | . 4753 I | 436 | . 97472 | 5,0 | . 0259 |  |
| 2.180 | $4 \cdot 36663$ | 448 | 4.47967 | 437 | 0.97477 | 5,0 | I. 0259 | 0,5 |
| . 181 | . 3711 I | 448 | . 48404 | 437 | . 97482 | 5,0 | . 0258 |  |
| . 182 | . 37560 | 449 | . 48842 | 438 | . 97487 | 5,0 | . 0258 |  |
| . 183 | . 38009 | 449 | . 49279 | 438 | .9749I | 5,0 | . 0257 |  |
| . 184 | .38459 | 450 | . 49718 | 438 | . 97496 | 4,9 | . 0257 |  |
| 2.185 | $4 \cdot 38909$ | 450 | 4.50156 | 439 | 0.97501 | 4,9 | 1.0256 | 0,5 |
| . 185 | . 39359 | 451 | . 50595 | 439 | . 97506 | 4,9 | . 0256 |  |
| .187 | . 39810 | 451 | . 51035 | 440 | .9751 1 | 4,9 | . 0255 |  |
| . 188 | . 4026 I | 451 | . 51475 | 440 | .97516 | 4,9 | . 0255 |  |
| . I89 | . 40713 | 452 | . 51916 | 441 | .9752I | 4,9 | . 0254 |  |
| 2. 190 | 4.41165 | 452 | 4.52356 | 441 | 0.97526 | 4,9 | I. 0254 | 0,5 |
| . 191 | . 41617 | 453 | . 52798 | 442 | .9753I | 4,9 | . 0253 |  |
| . 192 | . 42070 | 453 | . 53240 | 442 | . 97536 | 4,9 | . 0253 |  |
| . 193 | . 42524 | 454 | . 53682 | 443 | .9754I | 4,9 | . 0252 |  |
| . 194 | . 42978 | 454 | . 54125 | 443 | . 97545 | 4,8 | . 0252 |  |
| 2. 195 | 4.43432 | 455 | 4.54568 | 443 | 0.97550 | 4,8 | 1.0251 | 0,5 |
| . 196 | . 43887 | 455 | . 55012 | 444 | . 97555 | 4,8 | .0251 |  |
| . 197 | . 44342 | 455 | . 55456 | 444 | . 97560 | 4,8 | . 0250 |  |
| . 198 | . 44798 | 456 | . 55900 | 445 | . 97565 | 4,8 | . 0250 |  |
| . 199 | . 45254 | 456 | . 56345 | 445 | . 97570 | 4,8 | . 0249 |  |
| 2.200 | 4.457 II | 457 | 4.56791 | 446 | 0.97574 | 4,8 | 1.0249 | 0,5 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

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| u | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.200 | 4.457 I I | 457 | 4.56791 | 446 | 0.97574 | 4,8 | 1.0249 | 0,5 |
| . 201 | . 46168 | 457 | . 57237 | 446 | -97579 | 4,8 | . 0248 |  |
| . 202 | . 46625 | 458 | . 57683 | 447 | . 97584 | 4,8 | . 0248 |  |
| . 203 | . 47083 | 458 | . 58130 | 447 | . 97589 | 4,8 | . 0247 |  |
| . 204 | . 4754 I | 459 | . 58577 | 448 | . 97593 | 4,8 | . 0247 |  |
| 2.205 | 4.48000 | 459 | 4.59025 | 448 | 0.97598 | 4,7 | 1.0246 | 0,5 |
| . 206 | . 48459 | 459 | . 59473 | 448 | . 97603 | 4,7 | . 0246 | 0,5 |
| . 207 | . 48919 | 460 | . 59922 | 449 | . 97608 | 4,7 | . 0245 |  |
| . 208 | . 49379 | 460 | . 60371 | 449 | . 97612 | 4,7 | . 0245 |  |
| . 209 | . 49840 | 461 | . 6082 I | 450 | .976I7 | 4,7 | . 0244 |  |
| 2.210 | $4 \cdot 5030 \mathrm{I}$ | 461 | 4.61271 | 450 | 0.97622 | 4,7 | 1.0244 | 0,5 |
| . 211 | . 50762 | 462 | . 61721 | 45 I | . 97626 | 4,7 | . 0243 |  |
| . 212 | . 51224 | 462 | . 62172 | 451 | .9763I | 4,7 | . 0243 |  |
| . 213 | . 51687 | 463 | . 62624 | 452 | . 97636 | 4,7 | . 0242 |  |
| . 214 | . 52149 | 463 | . 63076 | 452 | . 97640 | 4,7 | . 0242 |  |
| 2.215 | 4.52613 | 464 | 4.63528 | 453 | 0.97645 | 4,7 | 1.024 I | 0,5 |
| . 216 | . 53077 | 464 | . 6398 I | 453 | . 97650 | 4,6 | .024I |  |
| .217 | . 5354 I | 464 | . 64434 | 454 | . 97654 | 4,6 | . 0240 |  |
| . 218 | . 54005 | 465 | . 64888 | 454 | . 97659 | 4,6 | . 0240 |  |
| . 219 | . 5447 I | 465 | . 65342 | 454 | . 97664 | 4,6 | . 0239 |  |
| 2.220 | 4.54936 | 466 | 4.65797 | 455 | 0.97668 | 4,6 | 1.0239 | 0,5 |
| . 221 | . 55402 | 466 | . 66252 | 455 | . 97673 | 4,6 | . 0238 |  |
| . 222 | . 55869 | 467 | . 66708 | 456 | . 97678 | 4,6 | . 0238 |  |
| . 223 | . 56336 | 467 | . 67164 | 456 | . 97682 | 4,6 | . 0237 |  |
| . 224 | . 56803 | 468 | . 67620 | 457 | . 97687 | 4,6 | . 0237 |  |
| 2.225 | 4.57271 | 468 | 4.68078 | 457 | 0.97691 | 4,6 | 1. 0236 | 0,5 |
| . 226 | . 57739 | 469 | . 68535 | 458 | . 97696 | 4,6 | . 0236 |  |
| . 227 | . 58208 | 469 | . 68993 | 458 | . 97700 | 4,5 | . 0235 |  |
| . 228 | . 58677 | 469 | . 69451 | 459 | . 97705 | 4,5 | . 0235 |  |
| . 229 | . 59147 | 470 | . 69910 | 459 | . 97709 | 4,5 | . 0234 |  |
| 2.230 | $4 \cdot 59617$ | 470 | 4.70370 | 460 | 0.97714 | 4,5 | 1.0234 | 0,5 |
| . 231 | . 60087 | 471 | . 70830 | 460 | . 97718 | 4,5 | . 0233 |  |
| . 232 | . 60559 | 471 | . 71290 | 461 | . 97723 | 4,5 | . 0233 |  |
| . 233 | . 61030 | 472 | . 71751 | 461 | . 97727 | 4,5 | . 0233 |  |
| . 234 | .61502 | 472 | . 72212 | 462 | . 97732 | 4,5 | . 0232 |  |
| 2.235 | 4.61974 | 473 | 4.72674 | 462 | 0.97736 | 4,5 | 1.0232 | 0,5 |
| . 236 | . 62447 | 473 | .73136 | 462 | . 97741 | 4,5 | .023I |  |
| . 237 | .6292I | 474 | . 73599 | 463 | . 97745 | 4,5 | . 023 I |  |
| . 238 | . 63395 | 474 | . 74062 | 463 | . 97750 | 4,4 | . 0230 |  |
| . 239 | . 63869 | 475 | . 74525 | 464 | . 97754 | 4,4 | . 0230 |  |
| 2.240 | 4.64344 | 475 | 4.74989 | 464 | 0.97759 | 4,4 | 1.0229 | 0,5 |
| . 241 | . 64819 | 475 | . 75454 | 465 | . 97763 | 4,4 | . 0229 |  |
| . 242 | . 65295 | 476 | . 75919 | 465 | . 97768 | 4,4 | . 0228 |  |
| . 243 | . 65771 | 476 | . 76385 | 466 | . 97772 | 4,4 | . 0228 |  |
| . 244 | . 66247 | 477 | . 7685 I | 466 | . 97776 | 4,4 | . 0227 |  |
| 2.245 | 4.66724 |  | 4.77317 | 467 | 0.97781 | 4,4 | 1.0227 | 0,5 |
| . 246 | . 67202 | 478 | . 77784 | 467 | . 97785 | 4,4 | . 0227 |  |
| . 247 | . 67680 | 478 | . 78252 | 468 | . 97790 | 4,4 | . 0226 |  |
| . 248 | .68158 | 479 | .78719 | 468 | . 97794 | 4,4 | . 0226 |  |
| . 249 | . 68637 | 479 | .79188 | 469 | . 97798 | 4,4 | . 0225 |  |
| 2.250 | 4.69117 | 480 | 4.79657 | 469 | 0.97803 | 4,3 | I. 0225 | 0,5 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | coth u | $\omega \mathbf{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.250 | 4.69117 | 480 | 4.79657 | 469 | 0.97803 | 4,3 | I. 0225 | 0,5 |
| .25I | . 69597 | 480 | . 80126 | 470 | . 97807 | 4,3 | . 0224 |  |
| . 252 | . 70077 | 48 I | . 80596 | 470 | .978II | 4,3 | . 0224 |  |
| . 253 | . 70558 | 48I | . 81066 | 471 | .978I6 | 4,3 | . 0223 |  |
| . 254 | . 71039 | 482 | .81537 | 471 | . 97820 | 4,3 | . 0223 | 0,5 |
| 2.255 | 4.71521 | 482 | 4.82008 | 472 | 0.97824 | 4,3 | 1.0222 | 0,4 |
| . 256 | . 72003 | 482 | . 82480 | 472 | . 97829 | 4,3 | . 0222 |  |
| . 257 | . 72486 | 483 | . 82952 | 472 | . 97833 | 4,3 | . 0222 |  |
| . 258 | . 72969 | 483 | . 83425 | 473 | . 97837 | 4,3 | .022I |  |
| . 259 | . 73453 | 484 | . 83898 | 473 | . 9784 I | 4,3 | .022I |  |
| 2.260 | 4.73937 | 484 | 4.84372 | 474 | 0.97846 | 4,3 | 1.0220 | 0,4 |
| . 261 | . 74422 | 485 | . 84846 | 474 | . 97850 | 4,3 | . 0220 |  |
| . 262 | . 74907 | 485 | . 85321 | 475 | . 97854 | 4,2 | . 0219 |  |
| . 263 | . 75392 | 486 | . 85796 | 475 | . 97858 | 4,2 | . 0219 |  |
| . 264 | . 75878 | 486 | . 86272 | 476 | . 97863 | 4,2 | .0218 |  |
| 2.265 | 4.76365 | 487 | 4.86748 | 476 | 0.97867 | 4,2 | 1.0218 | 0,4 |
| . 266 | . 76852 | 487 | . 87224 | 477 | . 97871 | 4,2 | . 0218 |  |
| . 267 | . 77339 | 488 | . 87701 | 477 | . 97875 | 4;2 | . 0217 |  |
| . 268 | . 77827 | 488 | .88179 | 478 | . 97879 | 4,2 | . 0217 |  |
| . 269 | . 783 I 6 | 489 | . 88657 | 478 | . 97884 | 4,2 | . 0216 |  |
| 2.270 | 4.78804 | 489 | 4.89136 | 479 | 0.97888 | 4,2 | 1.0216 | 0,4 |
| .27I | . 79294 | 490 | . 89615 | 479 | . 97892 | 4,2 | .0215 |  |
| . 272 | . 79784 | 490 | . 90094 | 480 | . 97896 | 4,2 | .0215 |  |
| . 273 | . 80274 | 491 | . 90574 | 480 | . 97900 | 4,2 | .0214 |  |
| : 274 | . 80765 | 491 | . 91055 | 48I | . 97905 | 4, I | .0214 |  |
| 2.275 | 4.81256 | 492 | 4.91536 | 48 I | 0.97909 | 4,I | 1.0214 | 0,4 |
| . 276 | . 8 I 748 | 492 | . 92017 | 482 | .97913 | 4,I | . 0213 |  |
| . 277 | . 82240 | 492 | . 92499 | 482 | . 97917 | 4,1 | .0213 |  |
| . 278 | . 82733 | 493 | . 92982 | 483 | . 97921 | 4,I | .0212 |  |
| . 279 | . 83226 | 493 | .93465 | 483 | . 97925 | 4,I | . 0212 |  |
| 2.280 | 4.83720 | 494 | 4.93948 | 484 | 0.97929 | 4,I | I.02II | 0,4 |
| .28I | . 84214 | 494 | . 94432 | 484 | . 97933 | 4, I | .02II |  |
| . 282 | . 84709 | 495 | . 94917 | 485 | . 97937 | 4,1 | .02II |  |
| .283 | . 85204 | 495 | . 95402 | 485 | -. 97942 | 4, I | . 0210 |  |
| . 284 | . 85699 | 496 | . 95887 | 486 | -. 97946 | 4,I | .0210 |  |
| 2.285 | 4.86196 | 496 | 4.96373 | 486 | 0.97950 | 4,I | 1.0209 | 0,4 |
| . 286 | . 86692 | 497 | . 96859 | 487 | . 97954 | 4,I | . 0209 |  |
| .287 | . 87189 | 497 | . 97346 | 487 | . 97958 | 4,0 | . 0208 |  |
| . 288 | . 87687 | 498 | . 97834 | 488 | . 97962 | 4,0 | . 0208 |  |
| . 289 | . 88185 | 498 | . 98322 | 488 | . 97966 | 4,0 | . 0208 |  |
| 2.290 | 4.88684 | 499 | 4.98810 | 489 | 0.97970 | 4,0 | 1.0207 | 0,4 |
| . 291 | .89183 | 499 | . 99299 | 489 | . 97974 | 4,0 | . 0207 |  |
| . 292 | . 89682 | 500 | . 99789 | 490 | . 97978 | 4,0 | . 0206 |  |
| . 293 | . 90182 | 500 | 5.00279 | 490 | . 97982 | 4,0 | . 0206 |  |
| . 294 | . 90683 | 501 | .00769 | 491 | . 97986 | 4,0 | . 0206 |  |
| 2.295 | 4.91184 | 501 | 5.01260 | 49I | 0.97990 | 4,0 | 1.0205 | 0,4 |
| . 296 | .91685 | 502 | . 01751 | 492 | . 97994 | 4,0 | . 0205 |  |
| . 297 | . 92187 | 502 | . 02243 | 492 | . 97998 | 4,0 | . 0204 |  |
| . 298 | . 92690 | 503 | .02736 | 493 | . 98002 | 4,0 | . 0204 |  |
| . 299 | .93193 | 503 | . 03229 | 493 | . 98006 | 3,9 | . 0203 |  |
| 2.300 | 4.93696 | 504 | 5.03722 | 494 | 0.98010 | 3,9 | 1.0203 | 0,4 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

[^13]Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.300 | 4.93696 | 504 | 5.03722 | 494 | 0.98010 | 3,9 | 1.0203 | 0,4 |
| . 301 | . 94200 | 504 | . 04216 | 494 | .98014 | 3,9 | . 0203 |  |
| . 302 | . 94705 | 505 | . 04710 | 495 | .98018 | 3,9 | . 0202 |  |
| . 303 | . 95210 | 505 | . 05205 | 495 | .98021 | 3,9 | . 0202 |  |
| . 304 | . 95715 | 506 | .05701 | 496 | . 98025 | 3,9 | .0201 |  |
| 2.305 | 4.96221 | 506 | 5.06197 | 496 | 0.98029 | 3,9 | 1.0201 | 0,4 |
| . 306 | . 96727 | 507 | . 06693 | 497 | . 98033 | 3,9 | . 0201 |  |
| . 307 | . 97234 | 507 | . 07190 | 497 | . 98037 | 3,9 | . 0200 |  |
| . 308 | . 97742 | 508 | . 07688 | 498 | .9804I | 3,9 | . 0200 |  |
| . 309 | . 98250 | 508 | .08186 | 498 | . 98045 | 3,9 | . 0199 |  |
| 2.310 | 4.98758 | 509 | 5.08684 | 499 | 0.98049 | 3,9 | 1.0199 | 0,4 |
| . 311 | . 99267 | 509 | . 09183 | 499 | . 98053 | 3,9 | . 0199 |  |
| . 312 | . 99777 | 510 | . 09683 | 500 | . 98056 | 3,8 | . 0198 |  |
| . 313 | 5.00286 | 510 | . 10183 | 500 | . 98060 | 3,8 | . 0198 |  |
| . 314 | . 00797 | 511 | . 10683 | 501 | . 98064 | 3,8 | . 0197 |  |
| 2.315 | 5.01308 | 511 | 5.11184 | 501 | 0.98068 | 3,8 | 1.0197 | 0,4 |
| . 316 | . 01819 | 512 | . 11686 | 502 | . 98072 | 3,8 | . 0197 |  |
| . 317 | .0233I | 512 | . 12188 | 502 | . 98076 | 3,8 | . 0196 |  |
| . 318 | . 02844 | 513 | . I2691 | 503 | . 98079 | 3,8 | . 0196 |  |
| . 319 | . 03357 | 513 | . 13194 | 503 | . 98083 | 3,8 | . 0195 |  |
| 2.320 | 5.03870 | 514 | 5.13697 | 504 | 0.98087 | 3,8 | 1.0195 | 0,4 |
| . 321 | . 04384 | 514 | . 14202 | 504 | .98091 | 3,8 | . 0195 |  |
| . 322 | . 04898 | 515 | . 14706 | 505 | . 98095 | 3,8 | . 0194 |  |
| . 323 | .05413 | 515 | . 15211 | 505 | .98098 | 3,8 | . 0194 |  |
| . 324 | . 05929 | 516 | . 15717 | 506 | .98102 | 3,8 | . 0193 |  |
| 2.325 | 5.06445 | 516 | 5.16223 | 506 | 0.98106 | 3,8 | 1. 0193 | 0,4 |
| . 326 | . 06961 | 517 | . 16730 | 507 | .98i 10 | 3,7 | . 0193 |  |
| . 327 | . 07478 | 517 | . 17237 | 507 | .98is3 | 3,7 | . 0192 |  |
| . 328 | . 07996 | 518 | . 17745 | 508 | .98ir | 3,7 | . 0192 |  |
| . 329 | .08514 | 518 | . 1825.3 | 509 | .98121 | 3,7 | . 0192 |  |
| 2.330 | 5.09032 | 519 | 5.18762 | 509 | 0.98124 | 3,7 | 1.0191 | 0,4 |
| .33I | . 09551 | 519 | . 19271 | 510 | .98ı28 | 3,7 | . 0191 |  |
| . 332 | . 10071 | 520 | . 19781 | 510 | .98132 | 3,7 | . 0190 |  |
| . 333 | . I059I | 520 | . 20291 | 5 II | .98136 | 3,7 | . 0190 |  |
| . 334 | . IIIII | 521 | . 20802 | 5 II | .98139 | 3,7 | . 0190 |  |
| 2.335 | 5.11632 | 52 I | 5.21314 | 512 | 0.98143 | 3,7 | I. 0189 | 0,4 |
| . 336 | . 12154 | 522 | . 21825 | 512 | .98I47 | 3,7 | . 0189 |  |
| . 337 | . 12676 | 522 | . 22338 | 513 | .98I50 | 3,7 | . 0188 |  |
| . 338 | . 13199 | 523 | . 22851 | 513 | .98154 | 3,7 | . 0188 |  |
| . 339 | . 13722 | 523 | . 23364 | 514 | .98I58 | 3,7 | . 0188 |  |
| 2.340 | 5.14245 | 524 | 5.23878 | 514 | 0.98161 | 3,6 | 1.0187 | 0,4 |
| . 341 | . 14770 | 524 | . 24393 | 515 | .98i65 | 3,6 | . 0187 |  |
| - 342 | . 15294 | 525 | . 24908 | 515 | .98169 | 3,6 | . 0187 |  |
| . 343 | . 15819 | 525 | . 25423 | 516 | .98172 | 3,6 | . 0186 |  |
| - 344 | . 16345 | 526 | . 25939 | 516 | .98176 | 3,6 | . 0186 |  |
| 2.345 | 5.16871 | 526 | 5.26456 | 517 | 0.98179 | 3,6 | 1.0185 | 0,4 |
| . 346 | . 17398 | 527 | . 26973 | 517 | .98183 | 3,6 | . 0185 |  |
| - 347 | . 17925 | 527 | . 27491 | 518 | .98187 | 3,6 | . 0185 |  |
| . 348 | .18453 .18981 | 528 529 | .28009 .28528 | 518 519 | .98190 | 3,6 3,6 | . 010184 | - |
| -349 | . 18981 | 529 | . 28528 | 519 | -98194 | 3,6 | . 0184 |  |
| 2.350 | 5.19510 | 529 | 5.29047 | 520 | 0.98197 | 3,6 | 1.0184 | 0,4 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\circ}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.350 | 5.19510 | 529 | 5.29047 | 520 | 0.98197 | 3,6 | I. 0184 | 0,4 |
| . 351 | . 20039 | 530 | . 29567 | 520 | . 98201 | 3,6 | . 0183 |  |
| . 352 | . 20569 | 530 | . 30087 | 52 I | . 98204 | 3,6 | . 0183 |  |
| . 353 | . 21100 | 531 | . 30608 | 52 I | . 98208 | 3,6 | . 0182 |  |
| . 354 | . 21630 | 531 | .31129 | 522 | . 98212 | 3,5 | . 0182 |  |
| 2.355 | 5.22162 | 532 | 5.31651 | 522 | 0.98215 | 3,5 | 1.0182 | 0,4 |
| . 356 | . 22694 | 532 | . 32174 | 523 | . 98219 | 3,5 | .018I |  |
| . 357 | . 23226 | 533 | . 32697 | 523 | . 98222 | 3,5 | .018I |  |
| . 358 | .23759 | 533 | . 33220 | 524 | . 98226 | 3,5 | . 0181 |  |
| . 359 | . 24293 | 534 | - 33744 | 524 | . 98229 | 3,5 | . 0180 |  |
| 2.360 | 5.24827 | 534 | 5.34269 | 525 | 0.98233 | 3,5 | 1.0180 | 0,4 |
| .361 | . 25361 | 535 | . 34794 | 525 | . 98236 | 3,5 | . 0180 |  |
| . 362 | . 25896 | 535 | . 35319 | 526 | . 98240 | 3,5 | . 0179 |  |
| .363 | . 26432 | 536 | . 35845 | 526 | . 98243 | 3,5 | . 0179 |  |
| . 364 | . 26968 | 536 | . 36372 | 527 | . 98247 | 3,5 | . 0178 |  |
| 2.365 | 5.27504 | 537 | 5.36899 | 528 | 0.98250 | 3,5 | 1.0178 | 0,4 |
| . 366 | . 28042 | 537 | . 37427 | 528 | . 98254 | 3.5 | . 0178 |  |
| . 367 | . 28579 | 538 | . 37955 | 529 | . 98257 | 3,5 | . 0177 |  |
| . 368 | . 29118 | 538 | . 38484 | 529 | .98261 | 3,4 | . 0177 |  |
| .369 | . 29656 | 539 | . 39014 | 530 | . 98264 | 3,4 | . 0177 |  |
| 2.370 | 5.30196 | 540 | 5.39544 | 530 | 0.98267 | 3,4 | 1.0176 | 0,4 |
| . 371 | . 30735 | 540 | . 40074 | 531 | . 98271 | 3,4 | . 0176 |  |
| . 372 | . 31276 | 54 I | . 40605 | 531 | . 98274 | 3,4 | . 0176 |  |
| . 373 | . 31817 | 541 | . 41137 | 532 | . 98278 | 3,4 | . 0175 |  |
| . 374 | . 32358 | 542 | .41669 | 532 | .9828I | 3,4 | . 0175 |  |
| 2.375 | 5.32900 | 542 | 5.42201 | 533 | 0.98285 | 3,4 | 1. 0175 | 0,4 |
| . 376 | . 33442 | 543 | . 42735 | 533 | . 98288 | 3,4 | . 0174 | 0,4 |
| . 377 | . 33985 | 543 | . 43268 | 534 | .98291 | 3,4 | . 0174 | 0,4 |
| . 378 | - 34529 | 544 | . 43803 | 535 | . 98295 | 3,4 | . 0173 | 0,3 |
| . 379 | . 35073 | 544 | . 44337 | 535 | . 98298 | 3,4 | . 0173 | 0,3 |
| 2.380 | $5 \cdot 35618$ | 545 | 5.44873 | 536 | 0.98301 | 3,4 | 1.0173 | 0,3 |
| . 381 | . 36163 | 545 | . 45409 | 536 | . 98305 | 3,4 | . 0172 |  |
| .382 | . 36708 | 546 | . 45945 | 537 | . 98308 | 3,4 | . 0172 |  |
| . 383 | . 37255 | 546 | . 46482 | 537 | .983I I | 3,3 | . 0172 |  |
| . 384 | . 37801 | 547 | . 47020 | 538 | .98315 | 3,3 | . 0171 |  |
| 2.385 | 5.38349 | 548 | 5.47558 | 538 | 0.98318 | 3,3 | 1.0171 | - 0,3 |
| . 386 | . 38897 | 548 | . 48096 | 539 | . 98322 | 3,3 | . 0171 |  |
| . 387 | - 39445 | 549 | . 48635 | 539 | . 98325 | 3,3 | . 0170 |  |
| . 388 | . 39994 | 549 | . 49175 | 540 | . 98328 | 3,3 | . 0170 |  |
| . 389 | . 40543 | 550 | . 49715 | 541 | . 98331 | 3,3 | . 0170 |  |
| 2.390 | 5.41093 | 550 | 5.50256 | 541 | 0.98335 | 3,3 | 1.0169 | 0,3 |
| . 391 | . 41644 | 55 I | . 50798 | 542 | . 98338 | 3,3 | . 0169 |  |
| . 392 | - 42195 | 551 | . 51339 | 542 | . 93341 | 3,3 | . 0169 |  |
| . 393 | . 42746 | 552 | . 51882 | 543 | . 98345 | 3,3 | . 0168 |  |
| - 394 | . 43299 | 552 | . 52425 | 543 | . 98348 | 3,3 | . 0168 |  |
| 2.395 | 5.43851 | 553 | 5.52969 | 544 | 0.98351 | 3,3 | 1. 0168 | 0,3 |
| . 396 | . 44405 | 554 | . 53513 | 544 | . 98354 | 3,3 | . 0167 |  |
| - 397 | . 44958 | 554 | - 54057 | 545 | . 98358 | 3,3 | . 0167 |  |
| . 398 | . 45513 | 555 | . 54603 | 546 | . 98361 | 3,3 | . 0167 |  |
| - 399 | . 46068 | 555 | . 55148 | 546 | .98364 | 3,2 | . 0166 |  |
| 2.400 | 5.46623 | 556 | 5.55695 | 547 | 0.98367 | 3,2 | 1.0166 | 0,3 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{sing} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.400 | 5.46623 | 556 | 5.55695 | 547 | 0.98367 | 3,2 | 1.0166 | 0,3 |
| . 401 | . 47179 | 556 | . 56242 | 547 | .9837I | 3,2 | . 0166 |  |
| . 402 | . 47735 | 557 | . 56789 | 548 | . 98374 | 3,2 | . 0165 |  |
| . 403 | . 48292 | 557 | . 57337 | 548 | . 98377 | 3,2 | . 0165 |  |
| . 404 | . 48850 | 558 | . 57886 | 549 | . 98380 | 3,2 | .0165 |  |
| 2.405 | 5.49408 | 558 | 5.58435 | 549 | 0.98384 | 3,2 | 1.0164 | 0,3 |
| . 406 | . 49967 | 559 | . 58984 | 550 | . 98387 | 3,2 | . 0164 |  |
| . 407 | . 50526 | 560 | . 59535 | 55 I | . 98390 | 3,2 | . 0164 |  |
| . 408 | . 51086 | 560 | . 60085 | 551 | . 98393 | 3,2 | . 0163 |  |
| . 409 | . 51646 | 561 | . 60637 | 552 | . 98396 | 3,2 | . 0163 | - |
| 2.410 | $5 \cdot 52207$ | 56 I | 5.61189 | 552 | 0.98400 | 3,2 | 1.0163 | 0,3 |
| .41I | . 52769 | 562 | . 61741 | 553 | .98403 | 3,2 | . 0162 |  |
| . 412 | . 53331 | 562 | . 62294 | 553 | . 98406 | 3,2 | . 0162 |  |
| . 413 | . 53893 | 563 | . 62848 | 554 | . 98409 | 3,2 | . 0162 |  |
| . 414 | . 54456 | 563 | . 63402 | 554 | . 98412 | 3,2 | .0161 |  |
| 2.415 | 5.55020 | 564 | 5.63957 | 555 | 0.98415 | 3,1 | 1.016I | 0,3 |
| . 416 | . 55584 | 565 | . 64512 | 556 | .98418 | 3, I | . 0161 |  |
| . 417 | .56149 | 565 | . 65068 | 556 | . 98422 | 3,1 | . 0160 |  |
| . 418 | . 567 I5 | 566 | . 65624 | 557 | . 98425 | 3, I | . 0160 |  |
| .419 | . 57280 | 566 | .66I8I | 557 | . 98428 | 3, I | . 0160 |  |
| 2.420 | 5.57847 | 567 | 5.66739 | 558 | 0.98431 | 3,I | 1.OI59 | 0,3 |
| . 42 I | . 58414 | 567 | . 67297 | 558 | . 98434 | 3,I | . 0159 |  |
| . 422 | . 58981 | 568 | . 67856 | 559 | . 98437 | 3, I | . 0159 |  |
| . 423 | . 59550 | 568 | . 68415 | 560 | . 98440 | 3, I | . 0158 |  |
| . 424 | . 60118 | 569 | . 68975 | 560 | . 98443 | 3, I | . 0158 |  |
| 2.425 | 5.60688 | 570 | 5.69535 | 561 | 0.98446 | 3,I | 1.0158 | 0,3 |
| . 426 | .61257 | 570 | . 70096 | 561 | .98450 | 3, I | . 0157 |  |
| . 427 | . 61828 | 571 | . 70658 | 562 | . 98453 | 3, I | . 0157 |  |
| . 428 | . 62399 | 571 | . 71220 | 562 | . 98456 | 3, I | . 0157 |  |
| . 429 | . 62970 | 572 | . 71783 | 563 | . 98459 | 3, I | . 0157 |  |
| 2.430 | 5.63542 | 572 | 5.72346 | 564 | 0.98462 | 3,I | 1.0156 | 0,3 |
| . 431 | .64115 | 573 | . 72910 | 564 | . 98465 | 3,0 | . 0156 |  |
| . 432 | . 64688 | 573 | . 73474 | 565 | .98468 | 3,0 | . 0156 |  |
| . 433 | . 65262 | 574 | . 74039 | 565 | . 98471 | 3,0 | . 0155 |  |
| . 434 | . 65836 | 575 | .74605 | 566 | . 98474 | 3,c | . 0155 |  |
| 2.435 | 5.66411 | 575 | 5.75171 | 566 | 0.98477 | 3,0 | 1.OI 55 | 0,3 |
| . 436 | . 66986 | 576 | . 75738 | 567 | .98480 | 3,0 | . 0154 |  |
| . 437 | . 67563 | 576 | . 76305 | 568 | .98483 | 3,0 | . 0154 |  |
| . 438 | .68139 | 577 | . 76873 | 568 | .98485 | 3,0 | . 0154 |  |
| . 439 | . 68716 | 577 | . 77441 | 569 | .98489 | 3,0 | . 0153 |  |
| 2.440 | 5.69294 | 578 | 5.78010 | 569 | 0.98492 | 3,0 | 1.0153 | 0,3 |
| . 441 | . 69872 | 579 | . 78580 | 570 | . 98495 | 3,0 | . 0153 |  |
| . 442 | . 7045 I | 579 | . 79150 | 570 | . 98498 | 3,0 | . 0152 |  |
| . 443 | . 7103 I | 580 | . 79721 | 571 | . 98501 | 3,0 | . 0152 |  |
| . 444 | .716II | 580 | . 80292 | 572 | . 98504 | 3,0 | . 0152 |  |
| 2.445 | 5.72191 | 58 I | 5.80864 | 572 | 0.98507 | 3,0 | 1.0152 | 0,3 |
| . 446 | . 72772 | 58I | . 81436 | 573 | . 98510 | 3,0 | . 0151 |  |
| . 447 | . 73354 | 582 | . 82009 | 573 | . 98513 | 3,0 | . 0151 |  |
| . 448 | . 73936 | 583 | . 82583 | 574 | . 98516 | 2,9 | . 0151 |  |
| . 449 | .74519 | 583 | . 83157 | 575 | .98519 | 2,9 | . 0150 |  |
| 2.450 | 5.75103 | 584 | 5.83732 | 575 | 0.98522 | 2,9 | 1.0150 | 0,3 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.450 | 5.75103 | 584 | 5.83732 | 575 | 0.98522 | 2,9 | I.OI50 | 0,3 |
| . 45 I | . 75687 | 584 | . 84307 | 576 | . 98525 | 2,9 | . 0150 |  |
| . 452 | . 76271 | 585 | . 84883 | 576 | . 98528 | 2,9 | . OI49 |  |
| . 453 | . 76856 | 585 | . 85460 | 577 | . 98530 | 2,9 | . 0149 |  |
| . 454 | . 77442 | 586 | . 86037 | 577 | . 98533 | 2,9 | . 0149 |  |
| 2.455 | 5.78029 | 587 | 5.85615 | 578 | 0.98536 | 2,9 | 1.0149 | 0,3 |
| . 456 | . 78615 | 587 | . 87193 | 579 | . 98539 | 2,9 | . 0148 |  |
| . 457 | . 79203 | 588 | . 87772 | 579 | . 98542 | 2,9 | . 0148 |  |
| . 458 | . 79791 | 588 | . 88352 | 580 | . 98545 | 2,9 | . 0148 |  |
| . 459 | . 80380 | 589 | . 88932 | 580 | . 98548 | 2,9 | . 0147 |  |
| 2.460 | 5.80969 | 590 | 5.89512 | 58 I | 0.98551 | 2,9 | I.OI47 | 0,3 |
| . 461 | . 81559 | 590 | . 90094 | 582 | . 98554 | 2,9 | . 0147 |  |
| . 462 | . 82149 | 591 | . 90675 | 582 | . 98556 | 2,9 | .0146 |  |
| . 463 | . 82740 | 591 | .9I258 | 583 | . 98559 | 2,9 | . 0146 |  |
| . 464 | . 83332 | 592 | .9184I | 583 | . 98562 | 2,9 | . 0146 |  |
| 2.465 | 5.83924 | 592 | 5.92425 | 58. | 0.98565 | 2,8 | I. 0146 | 0,3 |
| . 466 | . 84516 | 593 | . 93009 | 585 | . 98568 | 2,8 | . 0145 |  |
| .467 | .85110 | 594 | . 93594 | 585 | . 9857 I | 2,8 | . 0145 |  |
| . 468 | . 85704 | 594 | .94179 | 586 | . 98574 | 2,8 | . 0145 |  |
| . 469 | . 86298 | 595 | . 94765 | 586 | . 98576 | 2,8 | . 0144 |  |
| 2.470 | 5.86893 | 595 | 5.95352 | 587 | 0.98579 | 2,8 | I.OI44 | 0,3 |
| .47I | . 87489 | 596 | . 95939 | 587 | . 98582 | 2,8 | . 0144 |  |
| . 472 | . 88085 | 597 | . 96527 | 588 | . 98585 | 2,8 | . 0144 |  |
| . 473 | . 88682 | 597 | .97115 | 583 | . 98588 | 2,8 | . OI43 |  |
| . 474 | . 89279 | 498 | . 97704 | 589 | . 98590 | 2,8 | .OI43 |  |
| 2.475 | 5.89877 | 598 | 5.98294 | 590 | 0.98593 | 2,8 | I.OI43 | 0,3 |
| . 476 | . 90476 | 599 | . 98884 | 591 | . 98596 | 2,8 | . 0142 |  |
| . 477 | . 91075 | 599 | . 99474 | 591 | . 98599 | 2,8 | . 0142 |  |
| . 478 | . 91675 | 600 | 6.00066 | 592 | . 98602 | 2,8 | .0142 |  |
| . 479 | . 92275 | 601 | . 00658 | 592 | . 98604 | 2,8 | . 0142 |  |
| 2.480 | 5.92876 | 601 | 6.01250 | 593 | 0.98607 | 2,8 | I.OI4I | 0,3 |
| . 48 I | . 93478 | 602 | . 01844 | 593 | .98610 | 2,8 | .0141 |  |
| . 482 | . 94080 | 602 | . 02437 | 594 | . 98613 | 2,8 | . 0141 |  |
| . 483 | . 94682 | 603 | . 03032 | 595 | .985I5 | 2,7 | .0140 |  |
| . 484 | . 95286 | 604 | . 03627 | 595 | .98618 | 2,7 | . 0140 |  |
| 2.485 | 5.95890 | 604 | 6.04222 | 596 | 0.9852 I | 2,7 | 1.OI40 | 0,3 |
| . 486 | . 96494 | 605 | .04818 | 596 | . 98524 | 2,7 | . 0140 |  |
| .487 | . 97099 | 605 | .05415 | 597 | . 98526 | 2,7 | . OI39 |  |
| . 488 | . 97705 | 606 | . 06013 | 598 | . 98629 | 2,7 | .OI39 |  |
| . 489 | .983II | 607 | .066I I | 598 | .98632 | 2,7 | .OI39 |  |
| 2.490 | 5.98918 | 607 | 6.07209 | 599 | 0.98535 | 2,7 | I. 0138 | 0,3 |
| . 491 | . 99526 | 608 | . 07809 | 600 | . 98537 | 2,7 | . 0138 |  |
| . 492 | 6.00134 | 608 | . 08408 | 600 | . 98540 | 2,7 | . 0138 |  |
| . 493 | . 00743 | 609 | . 09009 | 601 | . 98643 | 2,7 | . 0138 |  |
| . 494 | . 01352 | 610 | .09610 | 601 | . 98645 | 2,7 | . 0137 |  |
| 2.495 | 6.01952 | 610 | 6.10211 | 602 | 0.98548 | 2,7 | I. 0137 | 0,3 |
| . 496 | . 02572 | 611 | .10814 | 603 | . 9865 I | 2,7 | . 0137 |  |
| . 497 | .03183 | 6 II | . II4I7 | 603 | . 98653 | 2,7 | .0136 |  |
| . 498 | . 03795 | 612 | . 12020 | 604 | . 98556 | 2,7 | .0136 |  |
| . 499 | . 04408 | 613 | . 12624 | 604 | . 98559 | 2,7 | .0136 |  |
| 2.500 | 6.05020 | 613 | 6.13229 | 605 | 0.g856I | 2,7 | I. 0136 | 0,3 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\propto \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.500 | 6.05020 | 613 | 6.13229 | 605 | 0.98661 | 2,7 | 1.0136 | 0,3 |
| . 501 | . 05634 | 614 | . I3834 | 606 | . 98664 | 2,7 | . 0135 |  |
| . 502 | . 06248 | 614 | . 14440 | 606 | . 98667 | 2,6 | . 0135 |  |
| . 503 | . 06863 | 615 | . 15047 | 607 | . 98669 | 2,6 | .OI35 |  |
| . 504 | . 07478 | 616 | . 15654 | 607 | . 98672 | 2,6 | . 0135 |  |
| 2.505 | 6.08094 | 616 | 6.16262 | 608 | 0.98675 | 2,6 | I.OI34 | 0,3 |
| . 506 | . 08711 | 617 | . 16870 | 609 | . 98677 | 2,6 | . 0134 |  |
| . 507 | . 09328 | 617 | . 17479 | 609 | . 98680 | 2,6 | . 0134 |  |
| . 508 | . 09946 | 618 | . 18089 | 610 | .98683 | 2,6 | . 0134 |  |
| . 509 | . 10564 | 619 | . 18699 | 6i I | .98685 | 2,6 | . OI33 |  |
| 2.510 | 6. 11183 | 619 | 6. 19310 | 611 | 0.98688 | 2,6 | I. 0133 | 0,3 |
| . 511 | . I.1803 | 620 | . 19921 | 612 | . 98590 | 2,6 | . 1133 | 0,3 |
| . 512 | . 12423 | 621 | . 20534 | 612 | . 98693 | 2,6 | . 0132 |  |
| . 513 | . 13044 | 621 | . 21 146 | 613 | . 98596 | 2,6 | . 0132 |  |
| . 514 | . 13665 | 622 | . 21760 | 6I4 | . 98698 | 2,6 | . 0132 |  |
| 2.515 | 6.14287 | 622 | 6.22374 | 614 | 0.98701 | 2,6 | 1.0132 | 0,3 |
| . 516 | . 14910 | 623 | . 22988 | 615 | .c8703 | 2,6 | .0131 |  |
| . 517 | . 15533 | 624 | . 23603 | 616 | . 98706 | 2,6 | .OI3I |  |
| . 518 | . 16157 | 624 | . 24219 | 616 | . 98708 | 2,6 | .OI3I |  |
| . 519 | . 16782 | 625 | . 24836 | 617 | .987II | 2,6 | .OI3I |  |
| 2.520 | 6.17407 | 625 | 6.25453 | 617 | 0.98714 | 2,6 | 1.0130 | 0,3 |
| . 52 I | . 18033 | 626 | . 26071 | 618 | .98716 | 2,6 | . 0130 |  |
| . 522 | . 18659 | 627 | . 26689 | 619 | . 98719 | 2,5 | .0130 |  |
| . 523 | . 19286 | 627 | . 27308 | 619 | .9872I | 2,5 | . 0130 |  |
| . 524 | . 19914 | 628 | . 27927 | 620 | . 98724 | 2,5 | . 0129 |  |
| 2.525 | 6.20542 | 629 | 6.28548 | 621 | 0.98726 | 2,5 | 1.0129 | 0,3 |
| . 526 | . 21171 | 629 | .29169 | 621 | . 98729 | 2,5 | . 0129 |  |
| . 527 | . 21800 | 630 | . 29790 | 622 | .9873I | 2,5 | . 0128 |  |
| . 528 | . 22430 | 630 | . 30412 | 622 | . 98734 | 2,5 | . 0128 |  |
| . 529 | .2306I | 631 | . 31035 | 623 | . 98736 | 2,5 | . 0128 |  |
| 2.530 | 6.23692 | 632 | 6.31658 | 624 | 0.98739 | 2,5 | 1.0128 | 0,3 |
| . 531 | . 24324 | 632 | . 32282 | 624 | .9874I | 2,5 | . 0127 |  |
| . 532 | . 24957 | 633 | . 32907 | 625 | . 98744 | 2,5 | . 0127 |  |
| . 533 | . 25590 | 634 | . 33532 | 626 | . 98746 | 2,5 | . 0127 |  |
| . 534 | . 26224 | 634 | . 34158 | 626 | . 98749 | 2,5 | . 0127 |  |
| 2.535 | 6.26858 | 635 | 6.34785 | 627 | 0.98751 | 2,5 | 1.0126 | 0,3 |
| . 536 | . 27494 | 635 | . 35412 | 627 | .98754 | 2,5 | . 0126 |  |
| . 537 | . 28129 | 636 | . 36040 | 628 | . 98756 | 2,5 | . 0126 |  |
| . 538 | . 28766 | 637 | . 36668 | 629 | . 98759 | 2,5 | .0126 |  |
| . 539 | . 29403 | 637 | . 37297 | 629 | .9876I | 2,5 | . 0125 |  |
| 2.540 | 6.30040 | 638 | 6.37927 | 630 | 0.98764 | 2,5 | 1.0125 | 0,3 |
| . 541 | . 30678 | 639 | . 38557 | 631 | . 98766 | 2,5 | . 0125 | 0,3 |
| . 542 | -31317 | 639 | . 39188 | 631 | . 98769 | 2,4 | . 0125 | 0,3 |
| . 543 | . 31957 | 640 | - 39820 | 632 | .98771 | 2,4 | . 0124 | 0,3 |
| . 544 | - 32597 | $640{ }^{\circ}$ | . 40452 | 633 | . 98773 | 2,4 | . 0124 | 0,2 |
| 2.545 | 6.33238 | 641 | 6.41085 | 633 | 0.98776 | 2,4 | I.OI24 | 0,2 |
| . 546 | . 33879 | 642 | .41719 | 634 | . 98778 | 2,4 | .OI24 |  |
| . 547 | -3452I | 642 | . 42353 | 635 | .98781 | 2,4 | . 0123 |  |
| . 548 | . 35164 | 643 | . 42988 | 635 | .98783 | 2,4 | . 0123 |  |
| . 549 | . 35807 | 644 | . 43623 | 636 | .98785 | 2,4 | . 0123 |  |
| 2.550 | 6.36451 | 644 | 6.44259 | 636 | 0.98788 | 2,4 | 1.0123 | 0.2 |
| u | $\boldsymbol{t a n g d} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.550 | 6.36451 | 644 | 6.44259 | 636 | 0.98788 | 2,4 | 1.0123 | 0,2 |
| . 551 | . 37096 | 645 | . 44896 | 637 | . 98790 | 2,4 | . 0122 |  |
| . 552 | . 37741 | 646 | . 45533 | 638 | . 98793 | 2,4 | . 0122 |  |
| . 553 | . 38387 | 646 | . 46172 | 638 | . 98795 | 2,4 | . 0122 |  |
| . 554 | . 39033 | 647 | . 46810 | 639 | . 98798 | 2,4 | . 0122 |  |
| 2.555 | 6.39680 | 647 | 6.47450 | 640 | 0.98800 | 2,4 | 1.0121 | 0,2 |
| . 556 | . 40328 | 648 | . 48090 | 640 | . 98802 | 2,4 | . 0121 |  |
| . 557 | . 40977 | 649 | . 48730 | 641 | . 98805 | 2,4 | . 0121 |  |
| . 558 | . 41626 | 649 | . 49372 | 642 | .98807 | 2,4 | . 0121 |  |
| . 559 | . 42275 | 650 | . 50014 | 642 | .98810 | 2,4 | . 0120 |  |
| 2.560 | 6.42926 | 651 | 6.50656 | 643 | 0.98812 | 2,4 | 1.0120 | 0,2 |
| . 561 | . 43577 | 651 | . 51299 | 644 | .988I4 | 2,4 | . 0120 |  |
| . 562 | . 44228 | 652 | . 51943 | 644 | .98817 | 2,4 | . 0120 |  |
| . 563 | . 44880 | 653 | . 52588 | 645 | .98819 | 2,3 | . 0120 |  |
| . 564 | . 45533 | 653 | . 53233 | 646 | .9882I | 2,3 | . 0119 |  |
| 2.565 | 6.46187 | 654 | 6.53879 | 646 | 0.98824 | 2,3 | I.OII9 | 0,2 |
| . 566 | .4684I | 655 | . 54525 | 647 | . 98826 | 2,3 | . OII9 |  |
| . 567 | . 47496 | 655 | . 55173 | 647 | .98828 | 2,3 | . OI 19 |  |
| . 568 | .48152 | 656 | . 55820 | 648 | .9883I | 2,3 | . 0118 |  |
| .569 | . 48808 | 656 | . 56469 | 649 | . 98833 | 2,3 | . 0118 |  |
| 2.570 | 6.49464 | 657 | 6.57118 | 649 | 0.98835 | 2,3 | 1. 0118 | 0,2 |
| . 571 | . 50122 | 658 | . 57768 | 650 | . 98838 | 2,3 | . 0118 |  |
| . 572 | . 50780 | 658 | . 58418 | 65 I | . 98840 | 2,3 | . OII7 |  |
| . 573 | . 51439 | 659 | . 59069 | 651 | . 98842 | 2,3 | . 0117 |  |
| . 574 | . 52098 | 660 | . 5972 I | 652 | . 98845 | 2,3 | . 0117 |  |
| 2.575 | 6.52758 | 660 | 6.60374 | 653 | 0.98847 | 2,3 | 1.0117 | 0,2 |
| . 576 | . 53419 | 66 I | .61027 | 653 | . 98849 | 2,3 | . 0116 |  |
| . 577 | . 54080 | 662 | . 61680 | 654 | . 9885 I | 2,3 | . 0116 |  |
| . 578 | . 54742 | 662 | . 62335 | 655 | . 98854 | 2,3 | .OII6 |  |
| . 579 | . 55405 | 663 | . 62990 | 655 | . 98856 | 2,3 | . 0116 |  |
| 2.580 | 6.56068 | 664 | 6.63646 | 656 | 0.98858 | 2,3 | 1.OII5 | 0,2 |
| . 58 I | . 56732 | 664 | . 64302 | 657 | . 98860 | 2,3 | . OII5 |  |
| . 582 | . 57397 | 665 | . 64959 | 657 | . 98853 | 2,3 | .OII5 |  |
| . 583 | . 58062 | 666 | -. 65617 | 658 | . 98865 | 2,3 | .OII5 |  |
| . 584 | . 58728 | 666 | . 66275 | 659 | . 98867 | 2,3 | . OII5 |  |
| 2.585 | 6.59395 | 667 | 6.66934 | 659 | 0.98870 | 2,2 | I. OII 4 | 0,2 |
| . 586 | . 60062 | 668 | . 67594 | 660 | . 98872 | 2,2 | . 0114 |  |
| . 587 | . 60730 | 668 | . 68254 | 66 I | . 98874 | 2,2 | . OII4 |  |
| . 588 | .6I358 | 669 | . 68915 | 661 | . 98876 | 2,2 | . 0114 |  |
| . 589 | . 62068 | 670 | . 69577 | 662 | . 98878 | 2,2 | . OII3 |  |
| 2.590 | 6.62738 | 670 | 6.70240 | 663 | 0.98881 | 2,2 | 1.0113 | 0,2 |
| . 591 | . 63.408 | 671 | . 70903 | 663 | .98883 | 2,2 | . OII 13 |  |
| . 592 | . 64079 | 672 | . 71566 | 664 | . 98885 | 2,2 | . 0113 |  |
| . 593 | . 64751 | 672 | .7223I | 665 | . 98887 | 2,2 | . OII3 |  |
| . 594 | . 65424 | 673 | . 72835 | 665 | . 98890 | 2,2 | . 0112 |  |
| 2.595 | 6.66097 | 674 | 6.73562 | 656 | 0.98892 | 2,2 | 1.0112 | 0,2 |
| . 596 | . 66771 | 674 | . 74228 | 667 | . 98894 | 2,2 | . OI 12 |  |
| . 597 | . 67446 | 675 | . 74895 | 667 | . 98896 | 2,2 | . OII 2 |  |
| . 598 | .68121 | 676 | . 75563 | 668 | . 98898 | 2,2 | . OIII |  |
| . 599 | . 68797 | 676 | . 7623 I | 669 | .98901 | 2,2 | .OIII |  |
| 2.600 | 6.69473 | 677 | 6.76901 | 669 | 0.98503 | 2,2 | I.OIII | 0,2 |
| 4 | $\tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \Gamma^{\prime}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.600 | 6.69473 | 677 | 6.76901 | 669 | 0.98903 | 2,2 | I.OIII | 0,2 |
| . 601 | . 70150 | 678 | . 77570 | 670 | . 98905 | 2,2 | . 0111 |  |
| . 602 | . 70828 | 678 | . 78241 | 671 | . 98907 | 2,2 | . OIIO |  |
| . 603 | . 71507 | 679 | . 78912 | 672 | . 98909 | 2,2 | . O1IO |  |
| . 604 | . 72186 | 680 | . 79584 | 672 | .9891 I | 2,2 | . 0110 |  |
| 2.605 | 6.72866 | 680 | 6.80256 | 673 | 0.98914 | 2,2 | 1.0110 | 0,2 |
| . 606 | . 73547 | 681 | . 80930 | 674 | .98916 | 2,2 | . 0110 |  |
| . 607 | . 74228 | 682 | .81604 | 674 | . 98918 | 2,2 | . 0109 |  |
| . 608 | . 74910 | 682 | . 82278 | 675 | . 98920 | 2,1 | . 0109 |  |
| . 609 | . 75593 | 683 | . 82953 | 675 | . 98922 | 2,I | . 0109 |  |
| 2.610 | 6.76276 | 684 | 6.83629 | 675 | 0.98924 | 2,I | 1.0109 | 0,2 |
| .6II | . 76960 | 684 | . 84306 | 677 | . 98926 | 2,I | . 0109 |  |
| .612 | . 77644 | 685 | . 84983 | 678 | . 98929 | 2,I | . 0108 |  |
| . 613 | . 78330 | 686 | .8566I | 678 | . 88931 | 2,I | . 0108 |  |
| . 614 | . 79016 | 686 | . 86340 | 679 | . 98933 | 2,I | . 0108 |  |
| 2.615 | 6.79702 | 687 | 6.87019 | 680 | 0.98935 | 2,I | 1.0108 | 0,2 |
| .616 | . 80390 | 688 | . 87699 | 680 | . 98937 | 2,1 | . 0107 |  |
| . 617 | .81078 | 688 | . 88380 | 68I | . 98939 | 2,I | . 0107 |  |
| . 618 | .81767 | 689 | .8905I | 682 | .9894I | 2,I | . 0107 |  |
| . 619 | . 82456 | 690 | . 89744 | 682 | .98943 | 2,I | . 0107 |  |
| 2.620 | 6.83146 | 690 | 6.90426 | 683 | 0.98946 | 2,I | 1.0107 | 0,2 |
| . 621 | . 83837 | 691 | .91IIO | 684 | . 98948 | 2,I | . 0106 |  |
| . 622 | . 84528 | 692 | .91794 | 685 | . 98950 | 2,1 | . 0106 |  |
| . 623 | . 85220 | 692 | . 92479 | 685 | . 98952 | 2,I | . 0106 |  |
| . 624 | . 85913 | 693 | .93164 | 686 | . 98954 | 2,I | . 0106 |  |
| 2.625 | 6.86607 | 694 | 6.93851 | 687 | 0.98956 | 2,I | 1.0106 | 0,2 |
| . 626 | . 87301 | 695 | . 94538 | 687 | . 98958 | 2,1 | . 0105 |  |
| . 627 | . 87996 | 695 | . 95225 | 688 | . 98960 | 2,I | . 0105 |  |
| . 628 | . 88691 | 696 | . 95914 | 689 | . 98962 | 2,I | . 0105 |  |
| . 629 | . 89388 | 697 | . 96603 | 689 | . 98964 | 2,I | .0105 | 1 |
| 2.630 | 6.90085 | 697 | 6.97292 | 690 | 0.98966 | 2,I | 1.0104 | 0,2 |
| . 631 | . 90782 | 698 | . 97983 | 691 | . 98968 | 2,1 | . 0104 |  |
| . 632 | .91481 | 699 | . 98674 | 691 | . 98970 |  | . 0104 |  |
| . 633 | . 92180 | 699 | . 99366 | 692 | .98972 | - 2,0 | . 0104 |  |
| . 634 | . 92879 | 700 | 7.00058 | 693 | . 98974 | 2,0 | . 0104 |  |
| 2.635 | 6.93580 | 701 | 7.00752 | 694 | 0.98977 | 2,0 | 1.0103 | 0,2 |
| . 636 | .9428I | 701 | . 01446 | 694 | . 98979 | 2,0 | . 0103 |  |
| . 637 | . 94983 | 702 | . 02140 | 695 | .98981 | 2,0 | . 0103 |  |
| . 638 | . 95685 | 703 | . 02835 | 696 | . 98983 | 2,0 | . 0103 |  |
| . 639 | . 96388 | 704 | . 03532 | 696 | . 98985 | 2,0 | . 0103 |  |
| 2.640 | 6.97092 | 704 | 7.04228 | 697 | 0.98987 | 2,0 | 1.0102 | 0,2 |
| .64I | . 97797 | 705 | . 04926 | 698 | . 98989 | 2,0 | . 0102 |  |
| . 642 | . 98502 | 706 | . 05624 | 699 | .98991 | 2,0 | . 0102 |  |
| . 643 | . 99208 | 706 | . 06323 | 699 | . 98993 | 2,0 | . 0102 |  |
| . 644 | . 99915 | 707 | . 07022 | 700 | . 98995 | 2,0 | . 0102 |  |
| 2.645 | 7.00622 | 708 | 7.07723 | 701 | 0.98997 | 2,0 | 1.0101 | 0,2 |
| . 646 | . 01330 | 708 | . 08423 | 701 | . 98999 | 2,0 | . 0101 |  |
| . 647 | . 02039 | 709 | .09125 | 702 | . 99001 | 2,0 | . OIOI |  |
| . 648 | . 02748 | 710 | . 09828 | 703 | . 99003 | 2,0 | . 0101 |  |
| . 649 | . 03458 | 711 | . 10531 | 703 | . 99005 | 2,0 | . 0101 |  |
| 2.650 | 7.04169 | 711 | 7.11234 | 704 | 0.99007 | 2,0 | 1.0100 | 0,2 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { c o s h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\text {. }}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.650 | 7.04169 | 7 II | 7. II234 | 704 | 0.99007 | 2,0 | 1.0100 | 0,2 |
| . 651 | .0488I | 712 | . II939 | 705 | . 99009 | 2,0 | . 0100 |  |
| . 652 | . 05593 | 713 | . 12544 | 706 | . 9901 I | 2,0 | . 0100 |  |
| . 653 | . 05306 | 713 | . 13350 | 706 | . 99013 | 2,0 | . 0100 |  |
| . 654 | . 07020 | 714 | . 14057 | 707 | . 99015 | 2,0 | . 0100 |  |
| 2.655 | 7.07734 | 715 | 7.14764 | 708 | 0.95016 | 2,0 | I. 0099 | 0,2 |
| . 656 | . 08449 | 715 | . 15472 | 708 | . 99018 | 2,0 | . 0099 |  |
| . 657 | . 09165 | 716 | . 1618 I | 709 | . 99020 | I,9 | . 0099 |  |
| . 658 | . 09882 | 717 | . 1689 I | 710 | . 99022 | I,9 | . 0099 |  |
| . 659 | . 10599 | 718 | . 17601 | 711 | . 99024 | 1,9 | . 0099 |  |
| 2.660 | 7.11317 | 718 | 7.18312 | 711 | 0.99026 | I,9 | I. 0098 | 0,2 |
| . 66 I | . 12036 | 719 | . 19024 | 712 | . 99028 | I,9 | . 0098 |  |
| . 662 | . 12755 | 720 | . 19736 | 713 | . 99030 | I,9 | . 0098 |  |
| . 663 | . 13475 | 720 | . 20449 | 713 | . 99032 | I,9 | . 00098 |  |
| . 664 | . 14196 | 721 | . 21163 | 714 | . 99034 | 1,9 | . 0098 |  |
| 2.665 | 7. 14918 | 722 | 7.21877 | 715 | 0.99036 | 1,9 | I. 0097 | 0,2 |
| . 666 | . 15640 | 723 | . 22593 | 716 | . 99038 | I,9 | . 0097 |  |
| . 667 | . 16363 | 723 | . 23309 | 716 | . 99040 | I,9 | . 0097 |  |
| . 668 | . 17086 | 724 | . 24025 | 717 | . 99042 | I,9 | . 0097 |  |
| . 669 | . 1781 I | 725 | . 24743 | 718 | . 99044 | I,9 | . 0097 |  |
| 2.670 | 7.18536 | 725 | 7.25461 | 719 | 0.99045 | I,9 | 1.0096 | 0,2 |
| . 671 | . 19262 | 726 | . 26180 | 719 | . 99047 | 1,9 | . 00096 |  |
| . 672 | . 19988 | 727 | . 26900 | 720 | . $99049^{\circ}$ | I,9 | . 00096 |  |
| . 673 | . 20715 | 728 | . 27620 | 721 | . 99051 | 1,9 | . 0096 |  |
| . 6.74 | . 21443 | 728 | . 28341 | 721 | . 99053 | I,9 | . 0096 |  |
| 2.675 | 7.22172 | 729 | 7.29063 | 722 | 0,99055 | 1,9 | I. 0095 | 0,2 |
| . 676 | . 22902 | 730 | . 29785 | 723 | . 99057 | 1,9 | . 0095 |  |
| . 677 | . 23632 | 731 | . 30509 | 724 | . 99059 | I,9 | . 0095 |  |
| . 678 | . 24363 | 731 | - 31233 | 724 | . 9906 | I,9 | . 0095 |  |
| . 679 | . 25094 | 732 | . 31957 | 725 | . 99062 | 1,9 | . 0095 |  |
| 2.680 | 7.25827 | 733 | 7.32683 | 726 | 0.99064 | 1,9 | 1.0094 | 0,2 |
| .681 | . 26560 | 733 | . 33409 | 727 | . 99066 | I,9 | . 00094 |  |
| . 682 | . 27293 | 734 | . 34136 | 727 | . 95058 | 1,9 | . 0094 |  |
| . 683 | . 28028 | 735 | - 34864 | 728 | . 99070 | I,9 | . 0094 |  |
| . 684 | . 28763 | 736 | - 35592 | 729 | . 99072 | I,8 | . 0094 |  |
| 2.685 | 7.29499 | 736 | $7 \cdot 36321$ | 729 | 0.99073 | I,8 | 1.0094 | 0,2 |
| . 685 | . 30236 | 737 | . 37051 | 730 | . 99075 | 1,8 | . 0093 |  |
| . 687 | . 30973 | 738 | . 37782 | 731 | . 99077 | I,8 | . 0093 |  |
| . 688 | .3171 | 739 | . 38513 | 732 | . 99079 | I,8 | . 0093 |  |
| . 689 | . 32450 | 739 | - 39245 | 732 | .9908I | I,8 | . 0093 |  |
| 2.690 | 7.33190 | 740 | 7.39978 | 733 | 0.99083 | 1,8 | I. 0093 | 0,2 |
| . 691 | . 33930 | 741 | . 4071 I | 734 | . 99084 | I,8 | . 0092 |  |
| . 692 | . 3467 I | 741 | . 41446 | 735 | . 93085 | I,8 | . 0092 |  |
| . 693 | . 35413 | 742 | . 42 I8I | 735 | . 99088 | I, 8 | . 0092 |  |
| . 694 | . 36156 | 743 | . 42917 | 736 | -99050 | I,8 | . 0092 |  |
| 2.695 | 7.36899 | 744 | 7.43653 | 737 | 0.95092 | 1,8 | 1.0092 | 0,2 |
| . 696 | . 37643 | 744 | . 44390 | 738 | . 95094 | I,8 | . 0001 |  |
| . 697 | . 38388 | 745 | . 45128 | 738 | . 99095 | I,8 | .009I |  |
| . 698 | . 39133 | 746 | . 45867 | 739 | . 99097 | I,8 | .009I |  |
| . 699 | . 39879 | 747 | . 46607 | 740 | . 99099 | I,8 | .0091 |  |
| 2.700 | 7.40626 | 747 | 7.47347 | 741 | 0.99101 | I,8 | 1.0091 | 0,2 |
| $u$ | $\tan \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{g} \mathrm{d} u$ | $\omega \mathrm{F}_{0}{ }^{\text {d }}$ | $\csc g d \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\tanh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{c o t h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.700 | 7.40626 | 747 | 7.47347 | 741 | 0.99101 | I,8 | 1.0091 | 0,2 |
| .701 | . 41374 | 748 | . 48088 | 741 | .99103 | I,8 | .009I |  |
| . 702 | . 42 I 22 | 749 | . 48830 | 742 | . 99104 | I,8 | . 0090 | - |
| . 703 | . 42872 | 750 | . 49572 | 743 | . 99105 | I,8 | . 0090 |  |
| . 704 | . 43622 | 750 | . 50315 | 744 | .99108 | I,8 | . 0090 |  |
| 2.705 | 7.44372 | 751 | 7.51059 | 744 | 0.99110 | I,8 | 1.0090 | 0,2 |
| . 706 | . 45124 | 752 | . 51804 | 745 | .99III | I,8 | . 0090 |  |
| . 707 | . 45876 | 753 | . 52550 | 746 | .99113 | I,8 | . 0089 |  |
| . 708 | . 46629 | 753 | . 53296 | 747 | .99115 | I,8 | .0089 |  |
| . 709 | . 47383 | 754 | . 54043 | 747 | .99117 | I,8 | . 0089 |  |
| 2.710 | 7.48137 | 755 | $7 \cdot 54791$ | 748 | 0.99118 | 1,8 | 1.0089 | 0,2 |
| . 711 | . 48892 | 756 | . 55539 | 749 | . 99120 | 1,8 | . 0089 |  |
| . 712 | . 49648 | 756 | . 56288 | 750 | . 99122 | 1,7 | . 0089 |  |
| . 713 | . 50405 | 757 | . 57038 | 750 | . 99124 | I,7 | . 0088 |  |
| . 714 | . 51162 | 758 | . 57789 | 751 | .99125 | 1,7 | . 0088 |  |
| 2.715 | 7.51920 | 759 | 7.58541 | 752 | 0.99127 | 1,7 | 1. 0088 | 0,2 |
| . 716 | . 52679 | 759 | . 59293 | 753 | .99129 | I,7 | . 0088 |  |
| . 717 | . 53439 | 760 | . 60046 | 753 | .9913I | 1,7 | . 0088 |  |
| . 718 | . 54199 | 761 | . 60800 | 754 | . 99132 | 1,7 | . 0088 |  |
| . 719 | . 54960 | 762 | . 61555 | 755 | .99134 | I,7 | . 0087 |  |
| 2.720 | 7.55722 | 762 | 7.62310 | 756 | 0.99136 | I,7 | 1.0087 | 0,2 |
| .721 | . 56485 | 763 | . 63066 | 756 | . 99138 | 1,7 | . 0087 |  |
| . 722 | . 57249 | 764 | . 63823 | 757 | .99139 | 1,7 | . 0087 |  |
| . 723 | . 58013 | 765 | . 64580 | 758 | .99141 | 1,7 | . 0087 |  |
| . 724 | . 58778 | 765 | . 65339 | 759 | . 99143 | I,7 | . 0086 |  |
| 2.725 | 7.59543 | 766 | 7.66098 | 760 | 0.99144 | 1,7 | 1.0086 | 0,2 |
| . 726 | . 60310 | 767 | . 66858 | 760 | .99146 | 1,7 | . 0086 |  |
| . 727 | .61077 | 768 | .67619 | 751 | .99148 | 1,7 | . 0086 |  |
| . 728 | . 61845 | 768 | . 68380 | 762 | .99150 | 1,7 | . 0086 |  |
| .729 | .62614 | 769 | . 69142 | 763 | .9915I | 1,7 | . 0086 |  |
| 2.730 | 7.63383 | 770 | 7.69905 | 763 | 0.99153 | 1,7 | 1. 0085 | 0,2 |
| .731 | .64154 | 77.1 | . 70669 | 764 | .99I55 | 1,7 | . 0085 |  |
| . 732 | . 64925 | 771 | . 71434 | 765 | . 99156 | 1,7 | . 0085 |  |
| . 733 | . 65697 | 772 | . 72199 | 766 | .99158 | 1,7 | . 0085 |  |
| . 734 | . 66469 | 773 | . 72955 | 766 | .99160 | 1,7 | . 0085 |  |
| 2.735 | 7.67242 | 774 | 7.73732 | 767 | 0.99161 | 1,7 | 1. 0085 | 0,2 |
| . 736 | . 68017 | 774 | . 74500 | 768 | . 99163 | I,7 | . 0084 |  |
| . 737 | .68791 | 775 | . 75268 | 769 | . 99165 | 1,7 | . 0084 |  |
| . 738 | . 69567 | 776 | . 76037 | 770 | .99165 | 1,7 | . 0084 |  |
| . 739 | . 70344 | 777 | . 76807 | 770 | .99168 | 1,7 | . 0084 |  |
| 2.740 | 7.71121 | 778 | 7.77578 | 771 | 0.99170 | 1,7 | 1.0084 | 0,2 |
| .741 | . 71899 | 778 | . 78349 | 772 | .99171 | 1,7 | . 0084 |  |
| . 742 | . 72577 | 779 | . 79122 | 773 | .99173 | 1,6 | .0083 |  |
| . 743 | . 73457 | 780 | . 79895 | 773 | .99175 | I,6 | . 0083 |  |
| . 744 | . 74237 | 78 I | . 80668 | 774 | -99176 | 1,6 | . 0083 |  |
| 2.745 | 7.75018 | 781 | 7.81443 | 775 | 0.99178 | 1,6 | 1.0083 | 0,2 |
| . 746 | . 75800 | 782 | . 82219 | 776 | . 99179 | 1,6 | . 0083 |  |
| .747 | . 76583 | 783 | . 82995 | 777 | .99181 | 1,6 | . 0083 |  |
| . 748 | . 77365 | 784 785 | .83772 .84549 | 777 778 | . 99183 | 1,6 I,6 | . 0082 | - |
| . 749 | -78150 | 785 | . 84549 | 778 | -99184 | 1,6 | . 0082 | - |
| 2.750 | 7.78935 | 785 | 7.85328 | 779 | 0.99186 | 1,6 | 1.0082 | 0,2 |
| $u$ | $\boldsymbol{t a n g} \mathrm{g} u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathbf{u}$ | $\omega F_{0}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.750 | 7.78935 | 785 | 7.85328 | 779 | 0.99186 | 1,6 | 1.0082 | 0,2 |
| . 751 | . 79721 | 786 | . 86107 | 780 | . 99188 | 1,6 | .0082 |  |
| . 752 | . 80507 | 787 | . 86887 | 781 | .99189 | 1,6 | . 0082 |  |
| . 753 | .81295 | 788 | . 87668 | 781 | .99191 | 1,6 | . 0082 |  |
| . 754 | . 82083 | 788 | . 88450 | 782 | .99192 | I,6 | .008I |  |
| 2.755 | 7.82872 | 789 | 7.89232 | 783 | 0.99194 | 1,6 | 1.0081 | 0,2 |
| . 756 | .8366I | 790 | . 90016 | 784 | .99196 | 1,6 | .008I |  |
| . 757 | . 84452 | 791 | . 90800 | 784 | .99197 | 1,6 | .008I |  |
| . 758 | . 85243 | 792 | . 91585 | 785 | . 99199 | 1,6 | .008I |  |
| . 759 | . 85035 | 792 | . 92370 | 785 | . 99200 | 1,6 | .008I |  |
| 2.760 | 7.85828 | 793 | 7.93157 | 787 | 0.99202 | 1,6 | 1.0080 | 0,2 |
| . 761 | . 87621 | 794 | . 93944 | 788 | . 99204 | I,6 | .0080 |  |
| . 762 | . 88415 | 795 | . 94732 | 788 | . 99205 | I,6 | .0080 |  |
| .763 | . 8921 I | 796 | . 95521 | 789 | . 99207 | 1,6 | . 0080 |  |
| . 764 | . 90006 | 796 | . 96310 | 790 | . 99208 | 1,6 | . 0080 |  |
| 2.765 | 7.90803 | 797 | 7.97101 | 791 | 0.99210 | 1,6 ${ }^{\circ}$ | 1.0080 | 0,2 |
| . 766 | .91601 | 798 | . 97892 | 792 | . 99212 | 1,6 | . 0079 |  |
| . 767 | . 92399 | 799 | . 98684 | 792 | . 99213 | 1,6 | . 0079 |  |
| . 768 | .93198 | 799 | . 99477 | 793 | . 99215 | I,6 | . 0079 |  |
| .769 | . 93998 | 800 | 8.00270 | 794 | . 99216 | 1,6 | . 0079 |  |
| 2.770 | 7.94799 | 801 | 8.01065 | 795 | 0.99218 | 1,6 | 1.0079 | 0,2 |
| . 771 | . 95600 | 802 | . 01860 | 796 | . 99219 | I,6 | . 0079 |  |
| . 772 | .96402 | 803 | . 02656 | 796 | . 99221 | 1,6 | . 0079 |  |
| . 773 | . 97205 | 803 | . 03453 | 797 | . 99222 | 1,5 | . 0078 |  |
| . 774 | . 98009 | 804 | . 04250 | 798 | . 99224 | 1,5 | . 0078 |  |
| 2.775 | 7.98814 | 805 | 8.05049 | 799 | 0.99226 | 1,5 | 1.0078 | 0,2 |
| . 776 | . 99619 | 806 | . 05848 | 800 | . 99227 | 1,5 | . 0078 |  |
| . 777 | 8.00426 | 807 | . 06648 | 800 | . 99229 | 1,5 | . 0078 |  |
| . 778 | . 01233 | 807 | . 07449 | 801 | . 99230 | 1,5 | . 0078 |  |
| . 779 | . 02040 | 808 | .0825I | 802 | . 99232 | I,5 | . 0077 |  |
| 2.780 | 8.02849 | 809 | 8.09053 | 803 | 0.99233 | 1,5 | 1.0077 | 0,2 |
| .781 | . 03659 | 810 | . 09856 | 804 | . 99235 | I,5 | . 0077 |  |
| . 782 | . 04469 | 8II | . 10660 | 804 | . 99236 | I,5 | . 0077 |  |
| . 783 | . 05280 | 8II | . 11465 | 805 | . 99238 | I,5 | . 0077 |  |
| . 784 | . 06092 | 8I2 | . I227I | 806 | . 99239 | I,5 | . 0077 |  |
| 2.785 | 8.06904 | 813 | 8. 13077 | 807 | 0.9924 I | 1,5 | 1.0077 | 0,2 |
| . 786 | . 07718 | 8 I 4 | . 13885 | 808 | . 99242 | I,5 | . 0076 |  |
| . 787 | . 08532 | 8 I 5 | . 14693 | 809 | . 99244 | I,5 | . 0076 |  |
| . 788 | . 09347 | 8 I 6 | . 15502 | 809 | . 99245 | I,5 | . 0076 |  |
| . 789 | . 10163 | 8i6 | .163II | 810 | . 99247 | I,5 | . 0076 |  |
| 2.790 | 8. 10980 | 817 | 8.17122 | 8 II | 0.99248 | 1,5 | 1.0076 | 0,2 |
| . 791 | . II797 | 8 I 8 | . I7933 | 812 | . 99250 | I,5 | . 0076 |  |
| . 792 | . 12616 | 819 | . 18746 | 8 I 3 | . 9925 I | 1,5 | . 0075 |  |
| . 793 | . I3435 | 820 | . 19559 | 8 I 3 | . 99253 | I,5 | . 0075 |  |
| . 794 | . 14255 | 820 | . 20373 | 8I4 | . 99254 | I,5 | . 0075 |  |
| 2.795 | 8.15076 | 821 | 8.21187 | 815 | 0.99256 | 1,5 | 1.0075 | 0,2 |
| . 796 | . 15897 | 822 | . 22003 | 8 I 6 | . 99257 | I,5 | . 0075 | 0,2 |
| . 797 | . 16720 | 823 | . 22819 | 817 | . 99259 | I,5 | . 0075 | 0,2 |
| . 798 | . 17543 | 824 | .23636 | 8 I 8 | . 99260 | 1,5 | . 0075 | 0,2 |
| . 799 | . 18367 | 824 | . 24454 | 8 I 8 | . 99262 | I,5 | . 0074 | 0,1 |
| 2.800 | 8. 19192 | 825 | 8.25273 | 819 | 0.99263 | I,5 | 1.0074 | O,I |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\csc \mathrm{cd}^{\text {u }}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.800 | 8.19192 | 825 | 8.25273 | 819 | 0.99263 | 1,5 | 1.0074 | O,I |
| . 801 | . 20018 | 826 | . 26092 | 820 | . 99265 | 1,5 | . 0074 |  |
| . 802 | . 20844 | 827 | . 26913 | 82 I | . 99266 | I,5 | . 0074 |  |
| . 803 | . 21671 | 828 | . 27734 | 822 | . 99268 | 1,5 | . 0074 |  |
| . 804 | . 22499 | 829 | . 28556 | 822 | . 99269 | I,5 | .,0074 |  |
| 2.805 | 8.23328 | 829 | 8.29379 | 823 | 0.99270 | 1,5 | 1.0073 | O,I |
| . 806 | . 24158 | 830 | . 30203 | 824 | . 99272 | I,5 | . 0073 |  |
| . 807 | . 24989 | 831 | - 31027 | 825 | . 99273 | 1,4 | . 0073 |  |
| . 808 | . 25820 | 832 | . 31853 | 826 | . 99275 | I,4 | . 0073 |  |
| . 809 | . 26653 | 833 | . 32679 | 827 | . 99276 | I,4 | . 0073 |  |
| 2.810 | 8.27486 | 834 | 8.33506 | 827 | 0.99278 | 1,4 | 1.0073 | 0,1 |
| .81I | . 28320 | 834 | . 34334 | 828 | . 99279 | I,4 | . 0073 |  |
| .812 | . 29154 | 835 | . 35163 | 829 | .9928I | I,4 | . 0072 |  |
| .813 | . 29990 | 836 | . 35992 | 830 | . 99282 | I,4 | . 0072 |  |
| .814 | . 30826 | 837 | . 36823 | 83 I | . 99283 | 1,4 | . 0072 |  |
| 2.815 | 8.31664 | 838 | 8.37654 | 832 | 0.99285 | I,4 | 1.0072 | 0, I |
| .816 | . 32502 | 838 | . 38486 | 833 | . 99286 | I,4 | . 0072 |  |
| .817 | . 33341 | 839 | . 39319 | 833 | . 99288 | I,4 | . 0072 |  |
| . 818 | . 34180 | 840 | . 40153 | 834 | . 99289 | I,4 | . 0072 |  |
| .819 | . 3502 I | 841 | . 40987 | 835 | . 99291 | I,4 | . 0071 |  |
| 2.820 | 8.35862 | 842 | 8.41823 | 836 | 0.99292 | 1,4 | 1.0071 | 0,1 |
| .821 | . 36704 | 843 | . 42659 | 837 | . 99293 | I,4 | . 007 I |  |
| . 822 | . 37548 | 843 | . 43496 | 838 | . 99295 | I, 4 | . 007 I |  |
| . 823 | .38391 | 844 | . 44334 | 838 | . 99296 | I,4 | . 007 I |  |
| . 824 | . 39236 | 845 | . 45173 | 839 | . 99298 | I,4 | . 0071 |  |
| 2.825 | 8.40082 | 846 | 8.46013 | 840 | 0.99299 | 1,4 | 1.0071 | O,I |
| . 826 | . 40928 | 847 | . 46853 | 841 | . 99300 | I,4 | . 0070 |  |
| . 827 | .41776 | 848 | . 47695 | 842 | . 99302 | I,4 | . 0070 |  |
| . 828 | . 42624 | 849 | . 485.37 | 843 | . 99303 | I, 4 | .0070 |  |
| . 829 | . 43473 | 849 | . 49380 | 843 | . 99305 | I,4 | .0070 |  |
| 2.830 | 8.44322 | 850 | 8.50224 | 844 | 0.99306 | I,4 | 1.0070 | 0,1 |
| . 831 | . 45173 | 851 | . 51068 | 845 | . 99307 | I,4 | . 0070 |  |
| . 832 | . 46025 | 852 | . 51914 | 846 | -99309 | I,4 | . 0070 |  |
| . 833 | . 46877 | 853 | . 52760 | 847 | . 99310 | I,4 | . 0069 |  |
| . 834 | . 47730 | 854 | . 53608 | 848 | .993 I I | I,4 | . 0069 |  |
| 2.835 | 8.48584 | 854 | 8.54456 | 849 | 0.99313 | I,4 | 1.0059 | O,I |
| . 836 | . 49439 | 855 | . 55305 | 849 | . 99314 | I, 4 | . 0069 |  |
| . 837 | . 50295 | 856 | . 56155 | 8=0 | . 99316 | I, 4 | . 0069 |  |
| . 838 | .5115I | 857 | . 57006 | 851 | . 99317 | I,4 | . 0069 |  |
| . 839 | . 52009 | 858 | . 57857 | 852 | . 99318 | I,4 | . 0069 |  |
| 2.840 | 8.52867 | 859 | 8.58710 | 853 | 0.99320 | I,4 | 1.0069 | O,I |
| .84I | . 53726 | 860 | . 59563 | 854 | . 9932 I | I,4 | . 0068 |  |
| . 842 | . 54586 | 860 | . 60417 | 855 | . 99322 | I, 4 | . 0068 |  |
| . 843 | . 55447 | 861 | .61272 | 855 | . 99324 | I,3 | . 0068 |  |
| . 844 | . 56309 | 852 | .62128 | 856 | .99325 | 1,3 | . 0068 |  |
| 2.845 | 8.57171 | 863 | 8.62985 | 857 | 0.99326 | I,3 | 1.0068 | 0,I |
| . 846 | . 58035 | 864 | . 63842 | 858 | . 99328 | 1,3 | . 0068 |  |
| . 847 | . 58899 | 865 | . 64701 | 859 | . 99329 | 1,3 | . 0068 |  |
| . 848 | . 59764 | 866 | . 65560 | 860 | . 99330 | I,3 | . 0067 |  |
| . 849 | . 60630 | 866 | . 66420 | 86 I | . 993332 | I,3 | . 0067 |  |
| 2.850 | 8.61497 | 867 | 8.6728I | 861 | 0.99333 | 1,3 | 1.0067 | 0,I |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin g d u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.850 | 8.61497 | 867 | 8.6728I | 861 | 0.99333 | 1,3 | 1.0067 | 0,I |
| . 851 | . 62365 | 868 | . 68143 | 862 | . 99334 | I,3 | . 0067 |  |
| . 852 | . 63233 | 869 | . 69006 | 863 | . 99336 | I,3 | . 0067 |  |
| . 853 | . 64103 | 870 | . 69870 | 864 | . 99337 | I,3 | . 0067 |  |
| . 854 | . 64973 | 871 | . 70734 | 865 | . 99338 | I,3 | . 0067 |  |
| 2.855 | 8.65844 | 872 | 8.71600 | 866 | 0.99340 | I,3 | 1. 0066 | O,I |
| . 856 | . 66716 | 872 | . 72466 | 867 | . 99341 | I,3 | . 0066 |  |
| . 857 | . 67589 | 873 | . 73333 | 868 | . 99342 | I,3 | . 0066 |  |
| . 858 | . 68463 | 874 | . 74201 | 868 | . 99344 | I,3 | . 0066 |  |
| . 859 | . 69337 | 875 | . 75070 | 869 | . 99345 | I,3 | . 0066 |  |
| 2.860 | 8.70213 | 876 | 8.75940 | 870 | 0.99346 | I,3 | 1.0066 | O,I |
| . 861 | . 71089 | 877 | . 76810 | 871 | . 99348 | I,3 | . 0066 |  |
| . 862 | . 71967 | 878 | . 77682 | 872 | . 99349 | I,3 | . 0066 |  |
| . 863 | . 72845 | 879 | . 78554 | 873 | . 99350 | I, 3 | . 0065 |  |
| . 864 | . 73724 | 879 | . 79428 | 874 | .9935 I | I,3 | . 0065 |  |
| 2.865 | 8.74604 | 880 | 8.80302 | 875 | 0.99353 | I,3 | 1.0065 | 0,1 |
| . 85 | . 75484 | 88 I | .81177 | 875 | . 99354 | I,3 | . 0065 |  |
| . 867 | . 76366 | 882 | . 82053 | 876 | . 99355 | I,3 | . 0065 |  |
| . 868 | . 77248 | 883 | . 82930 | 877 | . 99357 | I,3 | . 0065 |  |
| . 859 | .78132 | 884 | . 83807 | 878 | . 99358 | I,3 | . 0065 |  |
| 2.870 | 8.79016 | 885 | 8.84686 | 879 | 0.99359 | I,3 | 1. 0065 | O,I |
| . 871 | . 79901 | 886 | .85.565 | 880 | . 99360 | I,3 | . 0064 |  |
| . 872 | . 80787 | 886 | . 86446 | 88 I | . 99362 | I,3 | . 0064 |  |
| . 873 | . 81674 | 887 | . 87327 | 882 | . 99363 | I,3 | . 0064 |  |
| . 874 | . 82562 | 888 | . 88209 | 883 | . 09364 | 1,3 | . 0064 |  |
| 2.875 | 8.83450 | 889 | 8.89092 | 883 | 0.99365 | I,3 | 1.0064 | O, I |
| . 876 | . 84340 | 890 | . 89976 | 884 | . 99367 | I,3 | . 0064 |  |
| . 877 | . 85230 | 891 | . 90861 | 885 | . 99368 | 1,3 | . 00064 |  |
| . 878 | . 86122 | 892 | . 91746 | 886 | . 99369 | I,3 | . 0063 |  |
| . 879 | . 87014 | 893 | .92633 | 887 | .9937I | I,3 | . 0063 |  |
| 2.880 | 8.87907 | 894 | 8.93520 | 888 | 0.99372 | 1,3 | 1.0063 | O, I |
| .88I | . 88801 | 894 | . 94409 | 889 | . 99373 | I,3 | . 0063 |  |
| . 882 | . 89696 | 895 | . 95298 | 890 | . 99374 | I,2 | . 0063 |  |
| . 883 | .90591 | 896 | .96188 | 891 | . 99376 | I,2 | . 0063 |  |
| . 884 | .91488 | 897 | . 97079 | 891 | . 99377 | 1,2 | . 0063 |  |
| 2.885 | 8.92386 | 898 | 8.97971 | 892 | 0.99378 | 1,2 | 1.0053 | O, I |
| . 886 | . 93284 | 899 | . 98864 | 893 | . 99379 | 1,2 | . 0062 |  |
| . 887 | . 94183 | 900 | . 99758 | 894 | . 99380 | I,2 | . 0062 | . |
| . 888 | . 95084 | 901 | 9.00652 | 895 | . 99382 | 1,2 | . 0062 |  |
| . 889 | . 95985 | 902 | . 01548 | 896 | . 99383 | 1,2 | . 0062 |  |
| 2.890 | 8.96887 | 902 | 9.02444 | 897 | 0.99384 | 1,2 | 1.0062 | O,I |
| . 891 | . 97790 | 903 | . 03342 | 898 | . 99385 | 1,2 | . 0062 |  |
| . 892 | . 98693 | 904 | . 04240 | 899 | . 99387 | I,2 | . 0062 |  |
| . 893 | . 99598 | 905 | . 05139 | 900 | . 99388 | 1,2 | . 0062 |  |
| . 894 | 9.00504 | 906 | . 06039 | 901 | . 99389 | 1,2 | .006I |  |
| 2.895 | 9.01410 | 907 | 9.06940 | 901 | 0.99390 | I,2 | 1.006I | O,I |
| . 896 | . 02318 | 908 | . 07842 | 902 | . 9939 I | I,2 | . 0061 |  |
| . 897 | . 03226 | 909 | . 08745 | 903 | . 99393 | I,2 | . 0061 |  |
| . 898 | .04135 | 910 | . 09648 | 904 | . 99394 | I, 2 | . 0061 |  |
| . 899 | . 05045 | 911 | . 10553 | 905 | . 99395 | I,2 | .006I |  |
| 2.900 | 9.05956 | 911 | 9.11458 | 906 | 0.99396 | 1,2 | 1.006 1 | O, I |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| u | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { t a n h }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\text {b }}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.900 | 9.05956 | 911 | 9.11458 | 906 | 0.99396 | 1,2 | 1.006I | 0,I |
| .901 | . 06868 | 912 | . 12365 | 907 | . 99398 | I,2 | .006I |  |
| . 902 | .0778I | 913 | . 13272 | co8 | . 99399 | I,2 | .0060 |  |
| . 903 | . 08695 | 914 | . 14180 | 909 | . 99400 | 1,2 | . 0060 |  |
| . 904 | . 09609 | 915 | . 15090 | 910 | .9940I | I,2 | . 0060 |  |
| 2.905 | 9. 10525 | 916 | 9.16000 | 9II | 0.99402 | 1,2 | 1.0060 | O,I |
| . 906 | . I I44I | 917 | . 16911 | 91I | . 99403 | I,2 | . 0060 |  |
| . 907 | . I2359 | 918 | . 17823 | 912 | . 99405 | I,2 | . 0060 |  |
| . 908 | . 13277 | 919 | . 18735 | 913 | . 99406 | I,2 | . 0060 |  |
| . 909 | . 14196 | 920 | . 19649 | 914 | . 99407 | I,2 | . 0060 |  |
| 2.910 | 9.15116 | 921 | 9.20564 | 915 | 0.99408 | I,2 | 1.0060 | 0,1 |
| .91I | . 16037 | 921 | . 21479 | 916 | . 99409 | I,2 | . 0059 |  |
| . 912 | . 16959 | 922 | . 22396 | 917 | .994II | I,2 | . . 0059 |  |
| . 913 | . 17882 | 923 | . 23313 | 918 | . 99412 | I,2 | . .0059 |  |
| . 914 | . 18806 | 924 | . 24232 | 919 | . 99413 | 1,2 | . 0059 |  |
| 2.915 | 9. 19730 | 925 | 9.25151 | 920 | 0.99414 | 1,2 | 1. 0059 | O,I |
| .916 | . 20656 | 926 | . 26071 | 921 | . 99415 | I,2 | . 0059 |  |
| .917 | . 21583 | 927 | . 26992 | 922 | . 99416 | I,2 | . 0059 |  |
| . 918 | . 22510 | 928 | . 27914 | 923 | . 99418 | I,2 | . 0059 |  |
| . 919 | . 23438 | 929 | . 28837 | 923 | . 99419 | 1,2 | . 0058 |  |
| 2.920 | 9.24368 | 930 | 9.29751 | 924 | 0.99420 | 1,2 | I. 0058 | O,I |
| .92I | . 25298 | 931 | . 30686 | 925 | . 9942 I | 1,2 | . 0058 |  |
| . 922 | . 26229 | 932 | . 31612 | 926 | . 99422 | I,2 | . 0058 |  |
| . 923 | .2716I | 933 | . 32538 | 927 | . 99423 | I, I | . 0058 |  |
| . 924 | . 28094 | 933 | . 33466 | 928 | . 99425 | I, I | . 0058 |  |
| 2.925 | 9.29028 | 934 | 9.34395 | 929 | 0.99426 | I, I | 1.0058 | 0,1 |
| . 926 | . 29963 | 935 | . 35324 | 930 | . 99427 | I, I | . 0058 |  |
| .927 | . 30899 | 936 | . 36254 | 931 | . 99428 | I, I | . 0058 |  |
| . 928 | . 31835 | 937 | . 37186 | 932 | . 99429 | I, I | . 0057 |  |
| .929 | . 32773 | 938 | .38i 18 | 933 | . 99430 | I, I | . 0057 |  |
| 2.930 | 9.33712 | 939 | 9.39051 | 934 | 0.9953 I | I, I | 1.0057 | O,I |
| .93I | . 3465 I | 940 | - 39986 | 935 | . 99433 | I, I | . 0057 |  |
| . 932 | - 35592 | 941 | .40921 | 936 | . 99434 | I, I | . 0057 |  |
| . 933 | - 36533 | 942 | . 41857 | 937 | . 99435 | I, I | . 0057 |  |
| . 934 | - 37475 | 943 | . 42794 | 937 | . 99436 | I, I | . 0057 |  |
| 2.935 | 9.38419 | 944 | 9.43732 | 938 | 0.99437 | I, I | 1.0057 | 0,I |
| . 936 | . 39363 | 945 | . 44671 | 939 | . 99438 | I, I | . 0057 |  |
| . 937 | . 40308 | 946 | . 45610 | 940 | . 99439 | I, I | . 0056 |  |
| . 938 | . 41254 | 947 | . 4655 I | 941 | . 99440 | I, I | . 0056 |  |
| . 939 | . 42201 | 947 | . 47493 | 942 | . 9944 I | I, I | . 0056 |  |
| 2.940 | 9.43149 | 948 | 9.48436 | 943 | 0.99443 | I, I | 1.0056 | 0,1 |
| .94I | . 44098 | 949 | . 49379 | 944 | . 99444 | I, I | . 0056 |  |
| . 942 | . 45048 | 950 | . 50324 | 945 | . 99445 | I, I | . 0056 |  |
| . 943 | . 45999 | 951 | . 51269 | 946 | . 99446 | I, I | . 0056 |  |
| . 944 | . 46950 | 952 | . 52216 | 947 | . 99447 | I, I | . 0056 |  |
| 2.945 | 9.47903 | 953 | 9.53163 | 948 | 0.99448 | I, I | 1.0055 | 0,1 |
| . 946 | . 48857 | 954 | . 54112 | 949 | . 99449 | I, I | . 0055 |  |
| . 947 | . 4981 I | 955 | . 55061 | 950 | . 99450 | I, I | . 0055 |  |
| . 948 | . 50767 | 956 | . 56011 | 951 | . 99451 | I, I | . 0055 |  |
| . 949 | . 51723 | 957 | . 56962 | 952 | . 99453 | I, I | . 0055 |  |
| 2.950 | 9.5268I | 958 | 9.57915 | 953 | 0.99454 | I, I | 1.0055 | O,I |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\csc \boldsymbol{g d} \mathbf{u}$ | $\omega \mathrm{Fo}^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.950 | 9.5268I | 958 | 9.57915 | 953 | 0.99454 | I, I | I. 0055 | O, I |
| .951 | . 53639 | 959 | . 58868 | 954 | . 99455 | I, I | . 0055 |  |
| . 952 | . 54598 | 960 | . $5 ¢ 822$ | 955 | . 99456 | I, I | . 0055 |  |
| . 953 | . 55559 | 961 | . 60777 | 956 | . 99457 | I, I | . 0055 |  |
| . 954 | . 56520 | 962 | .61733 | 957 | . 99458 | I, I | . 0055 |  |
| 2.955 | 9.57482 | 963 | 9.62690 | 957 | 0.99459 | I, I | I. 0054 | O,I |
| . 956 | . 58445 | 964 | . 63648 | 958 | . 99460 | I, I | . 0054 |  |
| . 957 | . 59410 | 965 | . 64607 | 959 | . 9946 I | I, I | . 0054 |  |
| . 958 | . 60375 | 966 | . 65567 | 950 | . 99462 | I, I | . 0054 |  |
| . 959 | . 61341 | 967 | . 66528 | 961 | . 99463 | I, I | . 0054 |  |
| 2.960 | 9.62308 | 967 | 9.67490 | 962 | 0.99464 | I, I | I. 0054 | O,I |
| . 961 | . 63276 | 968 | . 68452 | 963 | . 99465 | I, I | . 0054 |  |
| . 962 | . 64245 | 969 | . 69416 | 954 | . 99467 | I, I | . 0054 |  |
| . 963 | .65214 | 970 | . 70381 | 965 | . 99468 | I, I | . 0054 |  |
| . 964 | . 66185 | 971 | .71347 | 956 | . 99469 | I, I | . 0053 |  |
| 2.965 | 9.67157 | 972 | 9.72313 | 957 | 0.99470 | I, I | 1.0053 | O,I |
| . 966 | .68130 | 973 | . 7328 I | 968 | . 9947 I | I, I | . 0053 |  |
| . 967 | . 69104 | 974 | . 74249 | 969 | . 99472 | I, I | . 0053 |  |
| . 968 | . 70078 | 975 | . 75219 | 970 | . 99473 | I, I | . 0053 |  |
| . 969 | . 71054 | 976 | .76190 | 971 | . 99474 | 1,0 | . 0053 |  |
| 2.970 | 9.72031 | 977 | 9.77161 | 972 | 0.99475 | 1,0 | 1.0053 | O,I |
| .971 | . 73008 | 978 | .78134 | 973 | . 99476 | I,O | . 0053 |  |
| . 972 | . 73987 | 979 | . 79107 | 974 | . 99477 | I, 0 | . 0053 |  |
| . 973 | . 74967 | 980 | . 80082 | 975 | . 99478 | 1,0 | . 0052 |  |
| . 974 | . 75947 | 981 | . 81057 | 975 | . 99479 | 1,0 | . 0052 |  |
| 2.975 | 9.76929 | 982 | 9.82034 | 977 | 0.99480 | 1,0 | 1.0052 | O,I |
| . 976 | . 77911 | 983 | . 83011 | 978 | . 9948 I | 1,0 | . 0052 |  |
| . 977 | . 78895 | 984 | . 83989 | 979 | . 99482 | I, 0 | . 0052 |  |
| . 978 | . 79879 | 985 | . 84969 | 980 | . 99483 | 1,0 | . 0052 |  |
| . 979 | . 8085 | 986 | . 85949 | c8i | . 99484 | 1,0 | . 0052 |  |
| 2.980 | 9.81851 | 987 | 9.86930 | 982 | 0.99485 | 1,0 | 1.0052 | O,I |
| .98I | . 82839 | 988 | . 87913 | 983 | . 99486 | 1,0 | . 0052 |  |
| . 982 | . 83827 | 989 | . 88896 | 984 | . 99487 | I, 0 | . 0052 |  |
| . 983 | . 848 I 6 | 990 | . 89880 | 985 | . 99488 | I, 0 | . 0051 |  |
| . 984 | . 85807 | 991 | . 90866 | 986 | . 99489 | I, 0 | . 0051 |  |
| 2.985 | 9.86798 | 992 | 9.91852 | 987 | 0.99490 | 1,0 | I. 0051 | 0,1 |
| -.985 | . 87790 | 993 | . 92839 | 988 | . 9949 I | 1,0 | . 0051 |  |
| . 987 | . 88784 | 994 | . 93828 | 989 | . 99492 | 1,0 | . 0051 |  |
| . 988 | . 89778 | 995 | .94817 | 990 | . 99493 | 1,0 | . 005 I |  |
| . 989 | . 90773 | 996 | .95807 | 991 | .99495 | I, 0 | . 0051 |  |
| 2.990 | 9.91770 |  | 9.96798 | 992 | 0.99496 | 1,0 | 1.0051 | O, I |
| .991 | . 92767 | 998 | .97791 | 993 | . 99497 | I, 0 | . 005 I |  |
| . 992 | . 93765 | 999 | . 98784 | 994 | . 99498 | 1,0 | . 0051 |  |
| . 993 | . 94765 | 1000 | . 99778 | 995 | . 99499 | 1,0 | . 0050 |  |
| . 994 | . 95765 | 1001 | 10.00774 | 996 | . 99500 | 1,0 | . 0050 |  |
| 2.995 | 9.96766 | 1002 | 10.01770 | 997 | 0.99501 | 1,0 | 1.0050 | O, I |
| . 996 | . 97768 | 1003 | . 02767 | 958 | . 99502 | 1,0 | . 0050 |  |
| . 997 | . 98772 | 1004 | . 03765 | 999 | . 99503 | I, 0 | . 0050 |  |
| . 998 | . 99776 | 1005 | . 04765 | 1000 | . 99504 | I, 0 | . 0050 |  |
| . 999 | 10.00781 | 1006 | . 05765 | 1001 | . 99504 | 1,O | . 0050 |  |
| 3.000 | 10.01787 | 1007. | 10.06766 | 1002 | 0.99505 | 1,0 | 1.0050 | O, I |
| u | $\boldsymbol{t a n g d} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Smithsonian Tables

Natural Hyperbolic Functions.

| $u$ | $\sinh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.00 | 10.0179 | 1007 | 10.0677 | 1002 | 0.99505 | 9,9 | 1.0050 | I,O |
| . OI | 10.1191 | 1017 | 10.1683 | 1012 | .99515 | 9,7 | . 0049 | 1,0 |
| . 02 | 10.2212 | 1027 | 10.2700 | 1022 | . 99525 | 9,5 | . 0048 | 1,0 |
| . 03 | 10.3245 | 1037 | 10.3728 | 1032 | . 99534 | 9,3 | . 0047 | 0,9 |
| . 04 | 10.4287 | 1048 | 10.4765 | 1043 | . 99543 | 9,I | . 0046 | 0,9 |
| 3.05 | 10.5340 | 1058 | 10.5814 | 1053 | 0.99552 | 8,9 | I. 0045 | 0,9 |
| . 06 | 10.6403 | 1069 | 10.6872 | 1064 | .9956I | 8,8 | . 0044 | 0,9 |
| . 07 | 10.7477 | 1079 | 10.7942 | 1075 | . 99570 | 8,6 | . 0043 | 0,9 |
| . 08 | 10.8562 | 1090 | 10.9022 | 1086 | . 99578 | 8,4 | . 0042 | 0,8 |
| . 09 | 10.9658 | IIOI | II.OII3 | 1097 | . 99587 | 8,2 | .004I | 0,8 |
| 3.10 | II . 0765 | III2 | II.1215 | 1108 | 0.99595 | 8,1 | I. 004 I | 0,8 |
| . II | 11.1882 | 1123 | II. 2328 | 1119 | . 99603 | 7,9 | . 0040 | 0,8 |
| . 12 | II. 3011 | I 135 | II . 3453 | II30 | .996I I | 7,8 | . 0039 | 0,8 |
| . 13 | 11.4151 | 1146 | II. 4588 | II 42 | .99618 | 7,6 | . 0038 | 0,8 |
| . 14 | II. 5303 | 1157 | II. 5736 | I 153 | . 99626 | 7,5 | . 0038 | 0,8 |
| 3.15 | II. 6466 | 1169 | I 1 : 6895 | I 165 | 0.99633 | 7,3 | I. 0037 | 0,7 |
| . 16 | 11.764I | I18I | 11.8065 | 1176 | .9964I | 7,2 | . 0036 | 0,7 |
| . 17 | II .8827 | 1192 | II .9247 | 1188 | . 99648 | 7,0 | . 0035 | 0,7 |
| . 18 | 12.0025 | 1204 | 12.0442 | 1200 | . 99655 | 6,9 | . 0035 | 0,7 |
| . 19 | 12.1236 | 1216 | 12.1648 | 1212 | . 99662 | 6,8 | . 0034 | 0,7 |
| 3.20 | 12.2459 | 1229 | 12.2866 | 1225 | 0.99568 | 6,6 | 1.0033 | 0,7 |
| . 21 | 12.3694 | 1241 | 12.4097 | 1237 | . 99675 | 6,5 | . 0033 | 0,7 |
| . 22 | 12.494I | 1253 | 12.5340 | 1249 | .9968I | 6,4 | . 0032 | 0,6 |
| . 23 | 12.6200 | 1266 | 12.6595 | 1262 | . 99688 | 6,2 | .003I | 0,6 |
| . 24 | 12.7473 | 1279 | 12.7854 | 1275 | . 99694 | 6, 1 | .003I | 0,6 |
| 3.25 | 12.8758 | 1291 | 12.9146 | 1288 | 0.99700 | 6,0 | 1.0030 | 0,6 |
| . 26 | 13.0056 | 1304 | 13.0440 | 1301 | . 99706 | 5,9 | . 0030 | 0,6 |
| . 27 | 13.1367 | 1317 | 13.1747 | 1314 | . 99712 | 5,8 | . 0029 | 0,6 |
| . 28 | 13.2691 | 1331 | 13.3067 | 1327 | . 99717 | 5,6 | . 0028 | 0,6 |
| . 29 | 13.4028 | 1344 | 13.4401 | 1340 | . 99723 | 5,5 | . 0028 | 0,6 |
| $3 \cdot 30$ | 13.5379 | 1357 | 13.5748 | 1354 | 0.99728 | 5,4 | 1.0027 | 0,5 |
| . 31 | 13.6743 | 1371. | 13.7108 | 1367 | . 99734 | 5,3 | . 0027 | 0,5 |
| . 32 | 13.8121 | 1385 | 13.8483 | I38I | . 99739 | 5,2 | . 0026 | 0,5 |
| . 33 | 13.9513 | 1399 | 13.9871 | 1395 | . 99744 | 5,I | . 0026 | 0,5 |
| . 34 | 14.0918 | 1413 | 14.1273 | 1409 | . 99749 | 5,0 | . 0025 | 0,5 |
| 3.35 | 14.2338 | 1427 | 14.2689 |  | 0.99754 |  | 1.0025 | 0,5 |
| . 36 | 14.3772 | 1441 | 14.4120 | 1438 | . 99759 | 4,8 | . 0024 | 0,5 |
| . 37 | I4.522I | 1456 | 14.5565 | 1452 | . 99764 | 4,7 | . 0024 | 0,5 |
| . 38 | 14.6684 | 1470 | 14.7024 | 1467 | . 99768 | 4,6 | . 0023 | 0,5 |
| - 39 | 14.8161 | I485 | 14.8498 | 1482 | . 99773 | 4,5 | . 0023 | 0,5 |
| 3.40 | 14.9654 | 1500 | 14.9987 | 1497 | 0.99777 | 4,4 | I. 0022 | 0,4 |
| . 41 | 15.1161 | 1515 | 15.1491 | 1512 | . 99782 | 4,4 | . 0022 | 0,4 |
| . 42 | 15.2584 | 1530 | 15.3011 | 1527 | . 99786 | 4,3 | . 002 I | 0,4 |
| . 43 | I5.422I | 1545 | 15.4545 | 1542 | . 99790 | 4,2 | .002I | 0,4 |
| . 44 | 15. $-\cdots$ : | 1561 | 15.6095 | 1558 | . 99795 | 4, I | .002I | 0,4 |
| 3.45 | 15.734 | 1577 | I5.7661 | 1573 | 0.99799 | 4,0 | 1.0020 | 0,4 |
| . 46 | 15.8928 | I 592 | 15.9242 | 1589 | . 99803 | 3,9 | . 0020 | 0,4 |
| . 47 | 16.0528 | 1608 | 16.0839 | 1605 | . 99807 | 3,9 | . 0019 | 0,4 |
| . 48 | 16.2145 | 1625 | 16.2453 | 1621 | .99810 | 3,8 | . 0019 | 0,4 |
| . 49 | 16.3777 | 1641 | 16.4082 | 1638 | .99814 | 3,7 | .0019 | 0,4 |
| $3 \cdot 50$ | 16.5426 | . 1657 | 16.5728 | 1654 | 0.99818 | 3,6 | 1.0018 | 0,4 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c} \mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.50 | 16.5426 | 1657 | 16.5728 | 1654 | 0.99818 | 3,6 | 1.0018 | 0,4 |
| . 51 | 16.7092 | 1674 | 16.7391 | 1671 | .99821 | 3,6 | .0018 | 0,4 |
| . 52 | 16.8774 | 1691 | 16.9070 | 1688 | . 99825 | 3,5 | .0018 | 0,4 |
| . 53 | 17.0473 | 1708 | 17.0766 | 1705 | . 99828 | 3,4 | .0017 | 0,3 |
| . 54 | 17.2190 | 1725 | 17.2480 | 1722 | . 99832 | 3,4 | .0017 | 0,3 |
| $3 \cdot 55$ | 17.3923 | 1742 | 17.4210 | 1739 | 0.99835 | 3,3 | 1.0017 | 0,3 |
| . 56 | I7.5674 | 1760 | 17.5958 | 1757 | . 99838 | 3,2 | .0016 | 0,3 |
| . 57 | 17.7442 | 1777 | 17.7724 | 1774 | . 99842 | 3,2 | .0016 | 0,3 |
| . 58 | 17.9228 | 1795 | 17.9507 | 1792 | . 99845 | 3,I | .0016 | 0,3 |
| . 59 | 18.1032 | I8I3 | 18. 1308 | 1810 | . 99848 | 3,0 | . OOI5 | 0,3 |
| 3.60 | 18.2855 | 1831 | 18.3128 | 1829 | 0.99851 | 3,0 | 1.0015 | 0,3 |
| . 61 | 18.4695 | 1850 | 18.4966 | 1847 | . 99854 | 2,9 | . 0015 | 0,3 |
| . 62 | 18.6554 | 1868 | 18.6822 | 1866 | . 99857 | 2,9 | .0014 | 0,3 |
| . 63 | 18.8432 | 1887 | 18.8697 | 1884 | . 99859 | 2,8 | .0014 | 0,3 |
| . 64 | 19.0328 | 1906 | 19.0590 | 1903 | .99862 | 2,8 | .0014 | 0,3 |
| 3.65 | 19.2243 | 1925 | 19.2503 | 1922 | 0.99865 | 2,7 | 1.0014 | 0,3 |
| . 66 | 19.4178 | 1944 | 19.4435 | 1942 | . 99868 | 2,6 | . 0013 | 0,3 |
| . 67 | 19.6132 | 1964 | 19.6387 | 1961 | . 99870 | 2,6 | .0013 | 0,3 |
| . 68 | 19.8106 | 1984 | 19.8358 | I98I | . 99873 | 2,5 | .0013 | 0,3 |
| . 69 | 20.0099 | 2003 | 20.0349 | 2001 | .99875 | 2,5 | . 0012 | 0,2 |
| 3.70 | 20.2113 | 2024 | 20.2360 | 2021 | 0.99878 | 2,4 | 1.0012 | 0,2 |
| . 71 | 20.4147 | 2044 | 20.4391 | 2041 | . 99880 | 2,4 | .0012 | 0,2 |
| . 72 | 20.6201 | 2064 | 20.6443 | 2052 | . 99883 | 2,3 | . 0012 | 0,2 |
| . 73 | 20.8276 | 2085 | 20.8516 | 2083 | . 99885 | 2,3 | .0012 | 0,2 |
| . 74 | 21.0371 | 2106 | 21.0609 | 2104 | . 99887 | 2,3 | . 001 I | 0,2 |
| 3.75 | 21. 2488 | 2127 | 21.2723 | 2125 | 0.99889 | 2,2 | I.0011 | 0,2 |
| . 76 | 21.4626 | 2149 | 21. 4859 | 2146 | . 99892 | 2,2 | .00II | 0,2 |
| . 77 | 21. 6785 | 2170 | 21.7016 | 2168 | . 99894 | 2,I | .00II | 0,2 |
| . 78 | 21. 8966 | 2192 | 21.9194 | 2190 | .99836 | 2,I | .0010 | 0,2 |
| . 79 | 22. 1169 | 2214 | 22.1395 | 2212 | . 99898 | 2,0 | .0010 | 0,2 |
| 3.80 | 22.3394 | 2236 | 22.3618 | 2234 | 0.99900 | 2,0 | 1.0010 | 0,2 |
| .8I | 22.5641 | 2259 | 22.5863 | 2256 | . 99902 | 2,0 | . 0010 | 0,2 |
| . 82 | 22.7911 | 2281 | 22.8131 | 2279 | . 99904 | I,9 | .0010 | 0,2 |
| . 83 | 23.0204 | 2304 | 23.0421 | 2302 | . 99906 | I,9 | . 0009 | 0,2 |
| . 84 | 23.2520 | 2327 | 23.2735 | 2325 | . 99908 | I,8 | . 0009 | 0,2 |
| 3.85 | 23.4859 | 2351 | 23.5072 | 2349 | 0.99909 | I,8 | 1. 00009 | 0,2 |
| . 86 | 23.7221 | 2374 | 23.7432 | 2372 | . 9991 I | I,8 | . 0009 | 0,2 |
| . 87 | 23.9608 | 2398 | 23.9816 | 2396 | . 99913 | 1,7 | . 0009 | 0,2 |
| . 88 | 24.2018 | 2422 | 24.2224 | 2420 | . 99915 | I,7 | . 0009 | 0,2 |
| . 89 | 24.4452 | 2447 | 24.4657 | 2445 | .99916 | I,7 | . 0008 | 0,2 |
| 3.90 | 24.69 II | 2471 | 24.7113 | 2469 | 0.99918 | 1,6 | I. 0008 | 0,2 |
| . 91 | 24.9395 | 2496 | 24.9595 | 2494 | . 99920 | I,6 | . 0008 | 0,2 |
| . 92 | 25.1903 | 2521 | 25.2101 | 2519 | . 9992 I | 1,6 | . 0008 | 0,2 |
| . 93 | 25.4437 | 2546 | 25.4633 | 2544 | . 99923 | I,5 | . 0008 | 0,2 |
| . 94 | 25.6996 | 2572 | 25.7190 | 2570 | . 99924 | I,5 | . 0008 | 0,2 |
| 3.95 | 25.958I | 2598 | 25.9773 | 2596 | 0.99926 | I,5 | 1.0007 | O,I |
| . 96 | 26.2191 | 2624 | 26.2382 | 2622 | . 99927 | I,5 | . 0007 | O,I |
| . 97 | 26.4828 | 2650 | 26.5017 | 2648 | . 99929 | I,4 | . 0007 | O,I |
| . 98 | 26.7492 | 2677 | 26.7679 | 2575 | . 99930 | I, 4 | .0007 | O,I |
| . 99 | 27.0182 | 2704 | 27.0367 | 2702 | . 99932 | I, 4 | . 0007 | 0, I |
| 4.00 | 27.2899 | 2731 | $27 \cdot 3082$ | 2729 | 0.99933 | I,3 | 1.0007 | O, I |
| u | $\boldsymbol{\operatorname { t a n }} \mathbf{g d} \mathbf{u}$ | $\omega F_{0}{ }^{\prime}$ | sec gd u | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{s i n} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{s i n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | tanh u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.00 | 27.2899 | 2731 | 27.3082 | 2729 | 0.99933 | 1,3 | 1.0007 | 0,1 |
| . 1 | 27.5644 | 2758 | 27.5825 | 2756 | . 99934 | 1,3 | . 0007 |  |
| . 02 | 27.8416 | 2786 | 27.8595 | 2784 | . 99936 | I,3 | . 0006 |  |
| . 03 | 28.1216 | 2814 | 28.1393 | 2812 | - 99937 | 1,3 | . 0006 |  |
| . 04 | 28.4044 | 2842 | 28.4220 | 2840 | . 99938 | 1,2 | . 0006 |  |
| 4.05 | 28.6900 | 2871 | 28.7074 | 2859 | 0.99939 | 1,2 | 1.0006 | 0,I |
| . 06 | 28.9785 | 2900 | 28.9958 | 2898 | . 9994 I | 1,2 | . 0006 |  |
| . 07 | 29.2699 | 2929 | 29.2870 | 2927 | . 99942 | 1,2 | . 0006 |  |
| . 08 | 29.5643 | 2958 | 29.5812 | 2956 | . 99943 | I, I | . 0006 |  |
| . 09 | 29.8616 | 2988 | 29.8783 | 2986 | . 99944 | I, I | . 0006 |  |
| 4.10 | 30.1619 | 3018 | 30.1784 | 3016 | 0.99945 | I, I | 1.0005 | 0,1 |
| . 11 | 30.4652 | 3048 | 30.4816 | 3047 | . 99946 | I, I | . 0005 |  |
| .12 | 30.7715 | 3079 | 30.7877 | 3077 | . 99947 | 1,I | . 0005 |  |
| . 13 | 31.0809 | 3110 | 31.0970 | 3108 | . 99948 | 1,0 | . 0005 |  |
| . 14 | 31.3934. | 3141 | 31.4094 | 3139 | -99949 | 1,0 | . 0005 |  |
| 4.15 | 31.7091 | 3172 | 31.7249 | 3171 | 0.99950 | 1,0 | 1.0005 | 0,1 |
| . 16 | 32.0280 | 3204 | 32.0436 | 3203 | . 99951 | 1,0 | . 0005 |  |
| $\cdot 17$ | 32.3500 | 3237 | 32.3655 | 3235 | - 99952 | 1,0 | . 0005 |  |
| . 18 | 32.6753 | 3269 | 32.6906 | 3268 | -99953 | 0,9 | . 0005 |  |
| . 19 | 33.0038 | 3302 | 33.0150 | 3300 | - 99954 | 0,9 | . 0005 |  |
| 4.20 | 33.3357 | 3335 | 33.3507 | 3334 | 0.99955 | 0,9 | 1.0004 | 0,1 |
| . 21 | 33.6708 | 3369 | 33.6857 | 3367 | . 99956 | 0,9 | . 0004 |  |
| . 22 | 34.0094 | 3402 | 34.024 I | 3401 | - 99957 | 0,9 | . 0004 |  |
| .23 | 34.3513 | 3437 | 34.3659 | 3435 | - 99958 | 0,8 | . 0004 |  |
| . 24 | 34.6967 | 3471 | 34.71 II | 3470 | -99958 | 0,8 | . 0004 |  |
| 4.25 | 35.0456 | 3506 | 35.0598 | 3505 | 0.99959 | 0,8 | 1.0004 | 0, I |
| . 26 | 35.3979 | 3541 | 35.4121 | 3540 | . 99960 | o,8 | . 0004 |  |
| . 27 | 35.7538 | 3577 | 35.7678 | 3575 | . 99961 | 0,8 | . 0004 |  |
| . 28 | 36. 1133 | 3613 | 36.1271 | 3611 | . 99962 | 0,8 | . 0004 |  |
| . 29 | 36.4764 | 3649 | 36.4501 | 3648 | - 99962 | 0,8 | . 0004 |  |
| 4.30 | 36.843I | 3686 | 36.8567 | 3684 | 0.99963 | 0,7 | 1.0004 | 0, I |
| . 31 | 37.2135 | 3723 | 37.2270 | 3721 | . 99964 | 0,7 | . 0004 |  |
| . 32 | 37.5877 | 3760 | 37.6010 | 3759 | . 99965 | 0,7 | . 0004 |  |
| . 33 | 37.9656 | 3798 | 37.9787 | 3797 | . 99965 | 0,7 | . 0003 |  |
| . 34 | 38.3473 | 3836 | 38.3603 | 3835 | . 99966 | 0,7 | . 0003 |  |
| 4.35 | 38.7328 | 3875 | 38.7457 | 3873 | 0.99967 | 0,7 | 1.0003 | 0,I |
| . 36 | 39.1222 | 3913 | 39.1350 | 3912 | . 99967 | 0,7 | . 0003 |  |
| . 37 | 39.5155 | 3953 | 39.528 I | 3952 | . 99968 | 0,6 | . 0003 |  |
| . 38 | 39.9128 | 3993 | 39.9253 | 3991 | - 99969 | 0,6 | . 0003 |  |
| - 39 | 40.3140 | 4033 | 40.3264 | 403I | . 99969 | 0,6 | . 0003 |  |
| 4.40 | 40.7193 | 4073 | 40.7316 | 4072 | 0.99970 | 0,6 | 1.0003 | 0,1 |
| . 41 | 41.1287 | 4114 | 41.1408 | 4113 | . 99970 | 0,6 | . 0003 |  |
| . 42 | 41.5421 | 4155 | 41.5542 | 4154 | . 99971 | 0,6 | . 0003 |  |
| . 43 | 41.9598 | 4197 | 41.9717 | 4156 | . 99972 | 0,6 | . 0003 |  |
| . 44 | 42.3816 | 4239 | 42.3934 | 4238 | . 99972 | 0,6 | . 0003 |  |
| 4.45 | 42.8076 | 4282 | 42.8193 | 428 I | 0.95973 | 0,5 | 1.0003 | 0, I |
| . 46 | 43.2380 | 4325 | 43.2495 | 4324 | . 99973 | 0,5 | . 0003 |  |
| . 47 | 43.6726 | 4368 | 43.6841 | 4367 | . 99974 | 0,5 | . 0003 |  |
| . 48 | 44.1117 | 4412 | 44.1230 | 44 II | -99974 | 0,5 | . 0003 |  |
| . 49 | 44.5551 | 4457 | 44.5663 | 4456 | . 99975 | 0,5 | . 0003 |  |
| 4.50 | 45.0030 | 4501 | 45.0141 | 4500 | 0.99975 | 0,5 | 1.0002 | 0, 0 |
| u | $\boldsymbol{t a n g d u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s e c}$ gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{s i n}$ gd $u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega F_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega F_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $4 \cdot 50$ | 45.0030 | 4501 | 45.0141 | 4500 | 0.99975 | 0,5 | I. 0002 | 0,0 |
| . 51 | 45.4554 | 4547 | 45.4664 | 4546 | . 99976 | 0,5 | . 0002 |  |
| . 52 | 45.9124 | 4592 | 45.9232 | 4591 | . 99976 | 0,5 | . 0002 |  |
| . 53 | 46.3739 | 4638 | 46.3847 | 4637 | . 99977 | 0,5 | . 0002 |  |
| . 54 | 46.8401 | 4685 | 46.8507 | 4684 | . 99977 | 0,5 | . 0002 |  |
| 4.55 | 47.3109 | 4732 | 47.3215 | 4731 | 0.99978 | 0,4 | I. 0002 | 0,0 |
| . 56 | 47.7865 | 4780 | 47.7970 | 4779 | . 99978 | 0,4 | . 0002 |  |
| . 57 | 48.2669 | 4828 | 48.2772 | 4827 | . 99979 | 0,4 | . 0002 |  |
| . 58 | 48.752 I | 4876 | 48.7623 | 4875 | . 99979 | 0,4 | . 0002 |  |
| - 59 | 49.242 I | 4925 | 49.2523 | 4924 | . 99979 | 0,4 | . 0002 |  |
| 4.60 | 49.737 I | 4975 | 49.7472 | 4974 | 0.99980 | 0,4 | I. 0002 | 0,0 |
| .6I | 50.2371 | 5025 | 50.2471 | 5024 | . 99980 | 0,4 | . 0002 |  |
| . 62 | 50.742 I | 5075 | 50.7519 | 5074 | .9998I | 0,4 | . 0002 |  |
| . 63 | 51.2522 | 5126 | 51.2619 | 5125 | .9998I | 0,4 | . 0002 |  |
| . 64 | 51.7673 | 5178 | 51.7770 | 5177 | .9998I | 0,4 | . 0002 |  |
| 4.65 | 52.2877 | 5230 | 52.2973 | 5229 | 0.99982 | 0,4 | 1.0002 | 0,0 |
| . 66 | 52.8133 | 5282 | 52.8228 | 528I | . 99982 | 0,4 | . 0002 |  |
| . 67 | 53.3442 | 5335 | 53.3536 | 5334 | . 99982 | 0,4 | . 0002 |  |
| . 68 | 53.8804 | 5389 | 53.8897 | 5388 | . 99983 | 0,3 | . 0002 |  |
| . 69 | 54.4220 | 5443 | 54.43 I 2 | 5442 | . 99983 | 0,3 | . 0002 |  |
| 4.70 | 54.9690 | 5498 | 54.9781 | 5497 | 0.99983 | 0,3 | I. 0002 | 0,0 |
| . 71 | 55.5216 | 5553 | 55.5306 | 5552 | . 99984 | 0,3 | . 0002 |  |
| .72 | 56.0797 | 5609 | 56.0886 | 5608 | . 99984 | 0,3 | . 0002 |  |
| . 73 | 56.6434 | 5665 | 56.6522 | 5664 | . 99984 | 0,3 | . 0002 |  |
| . 74 | 57.2127 | 5722 | 57.2215 | 5721 | . 99985 | 0,3 | . 0002 |  |
| 4.75 | 57.7878 | 5780 | 57.7965 | 5779 | 0.99985 | 0,3 | I.000I | 0,0 |
| . 76 | 58.3687 | 5838 | 58.3772 | 5837 | . 99985 | 0,3 | .000I |  |
| . 77 | 58.9554 | 5896 | 58.9639 | 5896 | . 99985 | 0,3 | . 0001 |  |
| .78 | 59.5480 | 5956 | 59.5564 | 5955 | . 99986 | 0,3 | . 0001 |  |
| . 79 | 60.1465 | 6015 | 60.1548 | 6015 | . 99986 | 0,3 | . 0001 |  |
| 4.80 | 60.7511 | 6076 | 60.7593 | 6075 | 0.99986 | 0,3 | r.000I | 0,0 |
| . 81 | 61.3617 | 6137 | 61.3699 | 6136 | . 99987 | 0,3 | . 0001 |  |
| . 82 | 61.9785 | 6199 | 61.9866 | 6198 | . 99987 | 0,3 | . 0001 |  |
| . 83 | 62.6015 | 6261 | 62.6095 | 6260 | . 99987 | 0,3 | . 0001 |  |
| . 84 | 63.2307 | 6324 | 63.2386 | 6323 | . 99987 | 0,3 | . 0001 |  |
| 4.85 | 63.8663 | 6387 | 63.8741 | 6387 | 0.99988 | 0,2 | I. 0001 | 0,0 |
| . 86 | 64.5082 | 6452 | 64.5160 | 645 I | . 99988 | 0,2 | .0001 |  |
| . 87 | 65.1566 | 6516 | 65.1643 | 6516 | . 99988 | 0,2 | . 0001 |  |
| . 88 | 65.8 II 5 | 6582 | 65.8191 | 6581 | . 99988 | 0,2 | . 0001 |  |
| . 89 | 66.4730 | 6648 | 66.4805 | 6647 | . 99989 | 0,2 | .000I |  |
| 4.90 | 67.1412 | 6715 | 67.1486 | 6714 | 0.99989 | 0,2 | I.000I | 0,0 |
| .91 | 67.8160 | 6782 | 67.8234 | 6782 | . 99989 | 0,2 | .0001 |  |
| . 92 | 68.4977 | 6850 | 68.5050 | 6850 | . 99989 | 0,2 | . 0001 |  |
| . 93 | 69.186I | 6919 | -69.1934 | 6919 | . 99990 | 0,2 | . 0001 |  |
| . 94 | 69.8815 | 6989 | 69.8887 | 6988 | . 99990 | 0,2 | . 0001 |  |
| 4.95 | 70.5839 | 7059 | 70.5910 | 7058 | 0.99990 | 0,2 | I.000I | 0,0 |
| . 96 | 71.2934 | 7130 | 71.3004 | 7129 | . 99990 | 0,2 | .0001 |  |
| . 97 | 72.0100 | 7202 | 72.0169 | 7201 | . 99990 | 0,2 | .0001 |  |
| . 98 | 72.7338 | 7274 | 72.7406 | 7273 | . 99991 | 0,2 | . 0001 |  |
| . 99 | 73.4648 | 7347 | 73.4716 | 7346 | . 9999 I | 0,2 | .0001 |  |
| 5.00 | 74.2032 | 7421 | 74.2099 | 7420 | 0.99991 | 0,2 | I. 0001 | 0,0 |
| u | $\boldsymbol{t a n} \mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| u | $\boldsymbol{\operatorname { s i n h }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | coth u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.00 | 74.2032 | 7421 | 74.2099 | 7420 | 0.99991 | 0,2 | I. 0001 | 0,0 |
| . 01 | 74.9490 | 7496 | 74.9557 | 7495 | . 9999 I | 0,2 | .0001 |  |
| . 02 | 75.7023 | 7571 | 75.7090 | 7570 | .9999I | 0,2 | . 0001 |  |
| . 03 | 76.4632 | 7647 | 76.4698 | 7646 | .9999I | 0,2 | . 0001 |  |
| . 04 | 77.2318 | 7724 | 77.2382 | 7723 | . 99992 | 0,2 | . 0001 |  |
| 5.05 | 78.0080 | 7801 | 78.0144 | 7801 | 0.99992 | 0,2 | I. 0001 | 0,0 |
| . 06 | 78.7921 | 7880 | 78.7984 | 7879 | . 99992 | 0,2 | . 0001 |  |
| . 07 | 79.5840 | 7959 | 79.5903 | 7958 | . 99992 | 0,2 | . 0001 |  |
| . 08 | 80.3839 | 8039 | 80.3901 | 8038 | . 99992 | 0,2 | .000I |  |
| . 09 | 81.1918 | 8120 | 81.1980 | 8i 19 | . 99992 | 0,2 | . 0001 |  |
| 5.10 | 82.0079 | 8201 | 82.0140 | 8201 | 0.99993 | O,I | I.000I | 0,0 |
| . II | 82.8322 | 8284 | 82.8382 | 8283 | . 99993 | O,I | .0001 |  |
| . 12 | 83.6647 | 8367 | 83.6707 | 8366 | . 99993 | O, I | . 0001 |  |
| . I3 | 84.5056 | 845 I | 84.5115 | 845 I | . 99993 | O,I | .000I |  |
| . I4 | 85.3550 | 8536 | 85.3608 | 8535 | . 99993 | O,I | . 0001 |  |
| 5.15 | 86.2128 | 8622 | 86.2186 | 8621 | 0.99993 | O,I | I.000I | 0,0 |
| . 16 | 87.0794 | 8709 | 87.0851 | 8708 | . 99993 | O,I | . 0001 |  |
| . 17 | 87.9546 | 8796 | 87.9603 | 8795 | . 99994 | O, I | .000I |  |
| . 18 | 88.8386 | 8884 | 88.8442 | 8884 | . 99994 | O, I | .000I |  |
| . 19 | 89.7315 | 8974 | 89.7371 | 8973 | . 99994 | O,I | .000I |  |
| 5.20 | 90.6334 | 9064 | 90.6389 | 9063 | 0.99994 | O,I | I.000I | 0,0 |
| . 21 | 91.5443 | 9155 | 91.5498 | 9154 | . 99994 | O,I | .000I |  |
| . 22 | 92.4644 | 9247 | 92.4698 | 9246 | . 99994 | O,I | . 0001 |  |
| . 23 | 93.3937 | 9340 | 93.3991 | 9339 | . 99994 | O,I | . 0001 |  |
| . 24 | 94.3324 | 9434 | 94.3377 | 9433 | -99994 | O,I | .000I |  |
| 5.25 | 95.2805 | 9529 | 95.2858 | 9528 | 0.99994 | O,I | 1.000I | 0,0 |
| . 26 | 96.238 I | 9624 | 96.2433 | 9624 | . 99995 | O,I | . 0001 |  |
| . 27 | 97.2054 | 9721 | 97.2106 | 9721 | . 99995 | O,I | . 0001 |  |
| . 28 | 98.1824 | 9819 | 98.1875 | 9818 | . 99995 | O,I | . 0001 |  |
| . 29 | 99.1692 | 9917 | 99.1742 | 9917 | . 99995 | O,I | . 0001 |  |
| 5.30 | 100. 1659 | 10017 | 100.1709 | 10017 | 0.99995 | O,I | 1.0000 | 0,0 |
| . 31 | 101. 1726 | 10118 | IOI. 1776 | 10117 | . 99995 | O, I | . 0000 |  |
| . 32 | 102.1895 | 10219 | 102. 1944 | 10219 | . 99995 | O,I | . 0000 |  |
| . 33 | 103.2166 | 10322 | 103.2214 | 10322 | . 99995 | O,I | . 0000 |  |
| . 34 | 104.2540 | 10426 | 104.2588 | 10425 | . 99995 | O,I | . 0000 |  |
| 5.35 | 105.3018 | 10531 | 105.3065 | 10530 | 0.99995 | O, I | 1.0000 | 0,0 |
| . 36 | 106.3601 | 10636 | 106.3648 | 10636 | . 99996 | O,I | . 0000 |  |
| . 37 | 107.4291 | 10743 | 107.4338 | 10743 | . 99996 | O,I | . 0000 |  |
| . 38 | 108.5088 | 10851 | 108.5134 | 10851 | . 99996 | O,I | . 0000 |  |
| - 39 | 109.5994 | 10960 | 109.6040 | 10960 | . 99996 | O,I | . 0000 |  |
| 5.40 | 110.7009 | 11071 | 110.7055 | 11070 | 0.99996 | O,I | 1.0000 | 0,0 |
| . 41 | III.8136 | III82 | III.8180 | III8I | . 99996 | O,I | . 0000 |  |
| . 42 | 112.9375 | 11294 | 112.9418 | 11294 | . 99996 | O,I | . 0000 |  |
| . 43 | I14.0724 | 11408 | 114.0768 | 11407 | . 99996 | O,I | . 0000 |  |
| . 44 | 115.2189 | II 522 | I 15.2233 | II522 | . 99996 | O,I | . 0000 |  |
| 5.45 | 116.3769 | 11638 | I16.3812 | 11638 | 0.99996 | O,I | I. 0000 | 0,0 |
| . 46 | 117.5466 | 11755 | 117.5508 | 11755 | . 99996 | O,I | . 0000 |  |
| . 47 | 118.7280 | 11873 | 118.7322 | 11873 | . 99996 | O,I | . 0000 |  |
| . 48 | 119.9213 | 11993 | 119.9254 | 11992 | . 99997 | O,I | . 0000 |  |
| . 49 | 121.1265 | 12113 | 121.1307 | 12113 | . 99997 | O,I | . 0000 |  |
| 5.50 | 122.3439 | 12235 | 122.3480 | 12234 | 0.99997 | O,I | 1.0000 | 0,0 |
| u | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sec \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

Natural Hyperbolic Functions.

| $u$ | $\boldsymbol{\operatorname { s i n h }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cosh u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{t a n h} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\operatorname{coth} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $5 \cdot 50$ | 122.3439 | 12235 | 122.3480 | 12234 | 0.99997 | O,I | 1.0000 | 0,0 |
| . 51 | 123.5735 | 12358 | 123.5776 | 12357 | . 99997 | 0,1 | . 0000 |  |
| . 52 | I24.8155 | 12482 | I24.8195 | 12482 | . 99997 | 0,1 | . 0000 |  |
| . 53 | 126.0700 | 12607 | 126.0739 | 12607 | . 99997 | O,I | . 0000 |  |
| . 54 | 127.3370 | 12734 | 127.3410 | 12734 | .99997 | O,I | . 0000 |  |
| 5.55 | I28.6i68 | 12862 | 128.6207 | 12862 | 0.99997 | 0,I | 1.0000 | 0,0 |
| . 56 | 129.9095 | 12991 | 129.9133 | 12991 | . 99997 | O,I | . 0000 |  |
| . 57 | I3I.215I | 13122 | 131.2190 | 13122 | -99997 | 0,I | . 0000 |  |
| . 58 | 132.5339 | 13254 | 132.5377 | 13253 | . 99997 | 0,I | . 0000 |  |
| . 59 | I 33.8659 | 13387 | 133.8697 | 13387 | . 99997 | O,I | . 0000 |  |
| 5.60 | 135.2114 | 13522 | 135.2150 | 13521 | 0.99997 | 0,1 | 1.0000 | 0,0 |
| .61 | 136.5703 | I3657 | I36.5739 | I 3657 | . 99997 | O,I | . 0000 |  |
| . 62 | 137.9429 | 13795 | 137.9465 | 13794 | . 99997 | 0,I | . 0000 |  |
| . 63 | 139.3293 | 13933 | 139.3329 | I 3933 | . 99997 | O,I | . 0000 |  |
| . 64 | 140.7296 | 14073 | I40.733 | 14073 | -99997 | 0,I | . 0000 |  |
| 5.65 | 142.1440 | 14215 | 142.1475 | 14214 | 0.99998 | 0,0 | 1.0000 | 0,0 |
| . 66 | 143.5726 | 14358 | 143.5761 | 14357 | . 99998 | 0,0 | . 0000 |  |
| . 67 | 145.0155 | 14502 | 145.0190 | 14502 | . 99998 | 0,0 | . 0000 |  |
| . 68 | 146.4730 | 14648 | 146.4764 | 14647 | . 99998 | 0,0 | . 0000 |  |
| . 69 | 147.9451 | 14795 | $147 \cdot 9485$ | 14795 | . 99998 | 0,0 | . 0000 |  |
| 5.70 | 149.4320 | 14944 | 149.4354 | 14943 | 0.99998 | 0,0 | 1.0000 | 0,0 |
| . 71 | 150.9339 | 15094 | 150.9372 | 15093 | . 99998 | 0,0 | . 0000 |  |
| .72 | 152.4508 | 15245 | 152.4541 | I 5245 | . 99998 | 0,0 | . 0000 |  |
| . 73 | 153.9830 | I $5399{ }^{\circ}$ | 153.9863 | 15398 | . 99998 | 0,0 | . 0000 |  |
| . 74 | 155.5306 | I 5553 | 155.5338 | I 5553 | . 99998 | 0,0 | . 0000 |  |
| 5.75 | 157.0938 | 15710 | 157.0969 | 15709 | 0.99998 | 0,0 | 1.0000 | 0,0 |
| . 76 | 158.6726 | 15868 | r'58.6757 | 15867 | . 99998 | 0,0 | . 0000 |  |
| . 77 | 160.2673 | 16027 | 160.2704 | 16027 | . 99998 | 0,0 | . 0000 |  |
| . 78 | 161.8781 | 16188 | 16I.88II | 16188 | . 99998 | 0,0 | . 0000 |  |
| . 79 | 163.5050 | 16351 | 163.5080 | 16350 | . 99998 | 0,0 | . 0000 |  |
| 5.80 | 165.1483 | 16515 | 165.1513 | 16515 | 0.99998 | 0,0 | 1. 0000 | 0,0 |
| . 81 | 166.808 I | 1668I | 166.8III | 1668I | . 99998 | 0,0 | . 0000 |  |
| . 82 | 168.4845 | 16849 | 168.4875 | 16848 | . 99998 | 0,0 | . 0000 |  |
| . 83 | 170.1779 | 17018 | 170.1808 | 17018 | . 99998 | 0,0 | . 0000 |  |
| . 84 | 171.8882 | I7189 | 171.89II | I7I89 | . 99998 | 0,0 | . 0000 | . |
| 5.85 | 173.6158 | 17362 | 173.6186 | 17362 | 0.99998 | 0,0 | 1.0000 | 0,0 |
| . 86 | 175.3606 | 17536 | 175.3635 | 17536 | . 99998 | 0,0 | . 0000 |  |
| . 87 | 177.1231 | 17713 | 177.1259 | 17712 | . 99998 | 0,0 | . 0000 |  |
| . 88 | 178.9032 | 17891 | 178.9060 | 17890 | -99998 | 0,0 | . 0000 |  |
| . 89 | 180.7013 | 18070 | 180.7040 | 18070 | . 99998 | 0,0 | . 0000 |  |
| 5.90 | 182.5174 | 18252 | 182.5201 | I8252 | 0.99998 | 0,0 | 1.0000 | 0,0 |
| .91 | 184.3517 | '18435 | 184.3544 | I8435 | . 99999 | 0,0 | . 0000 |  |
| . 92 | 186.2045 | 18621 | 186.2072 | 18620 | . 99999 | 0,0 | . 0000 |  |
| . 93 | 188.0759 | 18808 | 188.0786 | 18808 | . 99999 | 0,0 | . 0000 |  |
| . 94 | 189.966I | 18997 | 189.9688 | 18997 | . 99999 | 0,0 | . 0000 |  |
| 5.95 | 191.8754 | 19188 | 191.8780 | 19188 | 0.99999 | 0,0 | 1.0000 | 0,0 |
| . 96 | 193.8038 | 1938I | 193.8064 | 19380 | . 99999 | 0,0 | . 0000 |  |
| . .97 | 195.7516 | 19575 | 195.7541 | 19575 | . 99999 | 0,0 | . 0000 |  |
| . 98 | 197.7189 | 19772 | 197.7214 | 19772 | . 99999 | 0,0 | . 0000 |  |
| . 99 | 199.7061 | 19971 | 199.7086 | 19971 | . 99999 | 0,0 | . 0000 |  |
| 6.00 | 201.7132 | 20172 | 201.7156 | 20171 | 0.99999 | 0,0 | 1.0000 | 0,0 |
| $u$ | $\boldsymbol{\operatorname { t a n }} \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | sec gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\sin \mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | csc gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |

## TABLE III

## NaTURAL AND LOGARITHMIC CIRCULAR FUNCTIONS

Circular Functions.

| $u$ | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0000 | 0.00000 | 10,0 | 1.00000 | . 0,0 | - $-\infty$ | $+\infty$ | 0.00000 | 0,0 | $0^{\circ} 000000000$ |
| .0001 | . 00010 |  | . 00000 |  | 6.00000 | 43429,4 | . 00000 |  | 00020.63 |
| . 0002 | . 00020 |  | . 00000 |  | . 30103 | 21714,7 | . 00000 |  | 00041.25 |
| . 0003 | . 00030 |  | . 00000 |  | . 47712 | 14476,5 | . 00000 |  | 0 O1 01. 88 |
| . 0004 | . 00040 |  | . 00000 |  | . 60206 | 10857,4 | . 00000 |  | O OI 22.51 |
| 0.0005 | 0.00050 | 10,0 | 1.00000 | 0,0 | 6.69897 | 8685,9 | 0.00000 | 0,0 | O OI 43.13 |
| . 0006 | . 00060 |  | . 00000 |  | . 778 I 5 | 7238,2 | . 00000 |  | 00203.76 |
| . 0007 | .00070 |  | . 00000 |  | . 84510 | 6204,2 | . 00000 |  | 00224.39 |
| . 0008 | . 00080 |  | . 00000 |  | . 90309 | 5428,7 | . 00000 |  | 00245.01 |
| . 0009 | . 00090 |  | . 00000 |  | . 95424 | 4825,5 | . 00000 |  | 00305.64 |
| 0.0010 | 0.00100 | 10,0 | 1.00000 | 0,0 | 7.00000 | 4342,9 | 0.00000 | 0,0 | 00326.26 |
| .0011 | .001 10 |  | . 00000 |  | . 04139 | 3948, | . 00000 |  | 00346.89 |
| . 0012 | . 00120 |  | . 00000 |  | .07918 | 3619, 1 | . 00000 |  | 00407.52 |
| .0013 | .00130 |  | . 00000 |  | . I I394 | 3340,7 | . 00000 |  | 00428.14 |
| . 0014 | .00140 |  | . 00000 |  | . 14613 | 3102,1 | . 00000 |  | 00448.77 |
| 0.0015 | 0.00150 | 10,0 | 1.00000 | 0,0 | 7.17609 | 2895,3 | 0.00000 | 0,0 | 00509.40 |
| .0016 | . 00160 |  | . 00000 |  | . 20412 | 2714,3 | . 00000 |  | 00530.02 |
| . 0017 | . 00170 |  | . 00000 |  | . 23045 | 2554,7 | . 00000 |  | 00550.65 |
| . 0018 | .00180 |  | . 00000 |  | . 25527 | 2412,7 | . 00000 |  | 006 II. 28 |
| .0019 | .00190 |  | . 00000 |  | . 27875 | 2285,8 | . 00000 |  | 00631.90 |
| 0.0020 | 0.00200 | 10,0 | 1.00000 | 0,0 | 7.30103 | 2171,5 | 0.00000 | 0,0 | 0 0652.53 |
| . 0021 | . 00210 |  | . 00000 |  | . 32222 | 2068, I | . 00000 |  | 00713.16 |
| . 0022 | . 00220 |  | . 00000 |  | - 34242 | 1974, 1 | . 00000 |  | 00733.78 |
| . 0023 | . 00230 |  | . 00000 |  | . 36173 | 1888,2 | . 00000 |  | 00754.41 |
| . 0024 | . 00240 |  | . 00000 |  | .38021 | 1809,6 | . 00000 |  | 00815.04 |
| 0.0025 | 0.00250 | 10,0 | 1.00000 | 0,0 | $7 \cdot 39794$ | 1737,2 | 0.00000 | 0,0 | 00835.66 |
| . 0026 | . 00260 |  | . 00000 |  | .41497 | 1670,4 | . 00000 |  | 00856.29 |
| . 0027 | . 00270 |  | . 00000 |  | . 43136 | 1608,5 | . 00000 |  | 00916.91 |
| . 0028 | . 00280 |  | . 00000 |  | . 44716 | 1551,0 | . 00000 |  | 00937.54 |
| . 0029 | . 00290 |  | . 00000 |  | . 46240 | 1497,6 | . 00000 |  | 00958.17 |
| 0.0030 | 0.00300 | 10,0 | 1.00000 | 0,0 | 7.47712 | 1447,6 | 0.00000 | 0,0 | 0 10 18.79 |
| .0031 | .00310 |  | . 00000 |  | . 49136 | 1400,9 | . 00000 |  | 0 10 39.42 |
| . 0032 | . 00320 |  | 0.99999 |  | . 50515 | 1357,2 | . 00000 |  | 0 II 00.05 |
| . 0033 | . 00330 |  | . 99999 |  | . 51851 | 1316,0 | . 00000 |  | 0 II 20.67 |
| . 0034 | . 00340 |  | -99999 |  | -53148 | 1277,3 | . 00000 |  | 0 II 41.30 |
| 0.0035 | 0.00350 | 10,0 | 0.99999 | 0,0 | 7.54407 | 1240,8 | 0.00000 | 0,0 | 0 12 or. 93 |
| . 0036 | . 00360 |  | . 99999 |  | . 55630 | 1206,4 | . 00000 |  | 0 1222.55 |
| . 0037 | . 00370 |  | . 99999 |  | . 56820 | 1173,8 | . 00000 |  | 01243.18 |
| . 0038 | .00380 |  | . 99999 |  | - 57978 | I 142,9 | . 00000 |  | 0 13 03.81 |
| . 0039 | . 00390 |  | . 99999 |  | . 59106 | I I 13,6 | . 00000 |  | 0 I3 24.43 |
| 0.0040 | 0.00400 | 10,0 | 0.99999 | 0,0 | 7.60206 | 1085,7 | 0.00000 | 0,0 | 01345.06 |
| . 0041 | . 00410 |  | . 99999 |  | .61278 | 1059,2 | . 00000 |  | 0 1 1405.69 |
| . 0042 | . 00420 |  | . 99999 |  | . 62325 | 1034,0 | . 00000 |  | 0 1426.31 |
| . 0043 | . 00430 |  | . 99999 |  | . 63347 | 1010,0 | . 00000 |  | 0 O 1446.94 |
| . 0044 | . 00440 |  | . 99999 |  | . 64345 | 987,0 | . 00000 |  | 01507.57 |
| 0.0045 | 0.00450 | 10,0 | 0.99999 | 0,0 | 7.65321 | 965, 1 | 0.00000 | 0,0 | $\begin{array}{llll}0 & 15 & 28.19\end{array}$ |
| . 0046 | . 00460 |  | . 99999 |  | . 66276 | 944, I | . 00000 |  | 0 0 15 48.82 |
| . 0047 | . 00470 |  | . 99999 |  | . 67210 | 924,0 | . 00000 |  | 0 l 1609.44 |
| . 0048 | . 00480 |  | . 99999 |  | . 68124 | 904,8 | . 00000 |  | 01630.07 |
| . 0049 | . 00490 |  | . 99999 |  | . 69019 | 886,3 | 9.99999 |  | 01650.70 |
| 0.0050 | 0.00500 | 10,0 | 0.99999 | 0,0 | 7.69897 | 868,6 | 9.99999 | 0,0 | 01711.32 |
| u | -isinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} 4$ | $\omega F_{0}^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\circ}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0050 | 0.00500 | 10,0 | 0.99999 | 0,0 | 7.69897 | 868,6 | 9.99999 | 0,0 | $0^{\circ} 17^{\circ} \mathrm{II} 1.32$ |
| .005I | . 00510 |  | - 99999 | 0,1 | . 70757 | 851,6 | -99999 |  | 0 17 31.95 |
| . 0052 | . 00520 |  | . 99999 |  | . 71600 | 835,2 | . 99999 |  | 01752.58 |
| . 0053 | . 00530 |  | . 99999 |  | . 72427 | 819,4 | .99999 |  | 0 I8 13.20 |
| . 0054 | . 00540 |  | . 99999 |  | -73239 | 804,2 | . 99999 |  | 01833.83 |
| 0.0055 | 0.00550 | 10,0 | 0.99998 | 0,I | 7.74036 | 789,6 | 9.99999 | 0,0 | 0 18 54.46 |
| . 0056 | . 00560 |  | . 99998 |  | . 74819 | 775,5 | . 99999 |  | 0 I9 15.08 |
| . 0057 | . 00570 |  | . 99998 |  | . 75588 | 761,9 | . 99999 |  | 0 O 1935.71 |
| . 0058 | . 00580 |  | . 99998 |  | . 76343 | 748,8 | . 99999 |  | O 1956.34 |
| . 0059 | . 00590 |  | . 99998 |  | . 77085 | 736,1 | . 99999 |  | 02016.96 |
| 0.0060 | 0.00600 | 10,0 | 0.99998 | O,I | 7.77815 | 723,8 | 9.99999 | 0,0 | 02037.59 |
| .006I | . 00610 |  | . 99998 |  | . 78533 | 711,9 | . 99999 |  | 0 2058.22 |
| . 0062 | . 00620 |  | . 99998 |  | . 79239 | 700;5 | . 99999 |  | 0 21 18.84 |
| . 0063 | . 00630 |  | . 99998 |  | -79934 | 689,3 | . 99999 |  | 02139.47 |
| . 0064 | . 00640 |  | . 99998 |  | . 80618 | 678,6 | . 99999 |  | 02200.09 |
| 0.0065 | 0.00650 | 10,0 | 0.99998 | 0,I | 7.81291 | 668, I | 9.99999 | 0,0 | 02220.72 |
| . 0066 | . 00660 |  | . 99998 |  | . 81954 | 658,0 | . 99999 |  | 02241.35 |
| . 0067 | . 00670 |  | . 99998 |  | . 82607 | 648,2 | . 99999 |  | 02301.97 |
| . 0068 | . 00680 |  | . 99998 |  | . 83251 | 638,7 | . 99999 |  | 0 2322.60 |
| . 0069 | . 00690 |  | . 99998 |  | . 83885 | 629,4 | . 99999 |  | 02343.23 |
| 0.0070 | 0.00700 | 10,0 | 0.99998 | O,I | 7.84509 | 620,4 | 9.99999 | 0,0 | 02403.85 |
| . 0071 | . 00710 |  | . 99997 |  | . 85125 | $6 \mathrm{II}, 7$ | . 99999 |  | 0 2424.48 |
| . 0072 | . 00720 |  | . 99997 |  | . 85733 | 603,2 | . 99999 |  | 02445.11 |
| . 0073 | . 00730 |  | . 99997 |  | . 86332 | 594,9 | . 99999 |  | 02505.73 |
| . 0074 | . 00740 |  | . 99997 |  | . 86923 | 586,9 | . 99999 |  | 02526.36 |
| 0.0075 | 0.00750 | 10,0 | 0.99997 | 0,I | 7.87506 | 579,0 | 9.99999 | 0,0 | 02546.99 |
| . 0076 | . 00760 |  | . 99997 |  | . 8808 I | 571,4 | . 99999 |  | 0 2607.61 |
| . 0077 | . 00770 |  | . 99997 |  | . 88649 | 564,0 | . 99999 |  | 02628.24 |
| . 0078 | . 00780 |  | . 99997 |  | . 89209 | 556,8 | . 99999 |  | - 2648.87 |
| . 0079 | . 00790 |  | . 99997 |  | . 89762 | 549,7 | . 99999 |  | 02709.49 |
| 0.0080 | 0.00800 | 10,0 | 0.99997 | 0,1 | 7.90309 | 542,9 | 9.99999 | 0,0 | 02730.12 |
| .008I | .00810 |  | . 99997 |  | . 90848 | 536,2 | . 99999 |  | 02750.74 |
| . 0082 | . 00820 |  | . 99997 |  | .91381 | 529,6 | . 99999 |  | 028 II. 37 |
| . 0083 | . 00830 |  | . 99997 |  | . 91907 | 523,2 | . 99999 |  | 02832.00 |
| . 0084 | . 00840 |  | . 99996 |  | . 92427 | 517,0 | . 99998 |  | 0 2852.62 |
| 0.0085 | 0.00850 | 10,0 | 0.99996 | 0,I | 7.92941 | 510,9 | 9.99998 | 0,0 | $\begin{array}{llll}0 & 29 & 13.25\end{array}$ |
| . 0086 | . 00860 |  | . 99996 |  | . 93449 | 505,0 | . 99998 |  | - 2933.88 |
| . 0087 | . 00870 |  | . 99996 |  | .9395I | 499, 1 | . 99998 |  | o 2954.50 |
| . 0088 | . 00880 |  | . 99996 |  | . 94448 | 493,5 | . 99998 |  | - 30 15.13 |
| . 0089 | . 00890 |  | . 99996 |  | . 94938 | 488,0 | . 99998 |  | - 3035.76 |
| 0.0090 | 0.00900 | 10,0 | 0.99996 | O,I | 7.95424 | 482,5 | 9.99998 | 0,0 | - 3056.38 |
| .0091 | .00910 |  | . 99996 |  | . 95904 | 477,2 | . 99998 |  | 03117.01 |
| . 0092 | . 00920 |  | . 99996 |  | . 96378 | 472,0 | . 99998 |  | - 31 37.64 |
| . 0093 | . 00930 |  | . 99996 |  | . 96848 | 467,0 | . 99998 |  | 03158.26 |
| . 0094 | . 00940 |  | . 99996 |  | . 97312 | 462,0 | . 99998 |  | - 32 18.89 |
| 0.0095 | 0.00950 | 10,0 | 0.99995 | 0,1 | 7.97772 | 457, 1 | 9.99998 | 0,0 | - 3239.52 |
| . 0096 | . 00960 |  | . 99995 |  | . 98226 | 452,4 | . 99998 |  | - 3300.14 |
| . 0097 | . 00970 |  | . 99995 |  | . 98676 | 447,7 | . 99998 |  | 03320.77 |
| . 0098 | . 00980 |  | . 99995 |  | .99122 | 443, I | . 99998 |  | o 33. 41.40 |
| . 0099 | . 00990 |  | . 99995 |  | . 99563 | 438,7 | -99998 |  | 03402.02 |
| 0.0100 | 0.01000 | 10,0 | 0.99995 | O,I | 7.99999 | 434,3 | 9.99998 | 0,0 | - 3422.65 |
| u | -isinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | Og cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| $u$ | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0100 | 0.01000 | 10,0 | 0.99995 | 0,1 | 7.99999 | 434,3 | 9.99998 | 0,0 | $0^{\circ} 344^{\prime} 22^{\prime \prime} 65$ |
| . 0101 | . 01010 |  | . 99995 |  | 8.0043 I | 430,0 | . 99998 |  | 03443.27 |
| . 0102 | . 01020 |  | . 99995 |  | . 00859 | 425,8 | . 99998 |  | 03503.90 |
| . 0103 | . 01030 |  | . 99995 |  | . 01283 | 421,6 | . 99998 |  | - 3524.53 |
| . 0104 | . 01040 |  | . 99995 |  | . 01703 | 417,6 | . 99998 |  | - 3545.15 |
| 0.0105 | 0.01050 | 10,0 | 0.99994 | O,I | 8.02118 | 413,6 | 9.99938 | 0,0 | - 3605.78 |
| . 0106 | . 01060 |  | . 99994 |  | . 02530 | 409,7 | . 99998 |  | 0 3626.41 |
| . 0107 | . 01070 |  | . 99994 |  | . 02938 | 405,9 | . 99958 |  | 二 5647.03 |
| . 0108 | . 01080 |  | . 99994 |  | . 03342 | 402, I | . 99997 |  | - 3707.66 |
| . 0109 | . 01090 |  | . 99994 |  | .03742 | 398,4 | . 99997 |  | - 3728.29 |
| 0.0110 | 0.01100 | 10,0 | 0.99994 | 0,1 | 8.04138 | 394,8 | 9.99997 | 0,0 | - 3748.91 |
| . OIII | . OIIIO |  | . 99994 |  | .0453I | 391,2 | . 99997 |  | - 3809.54 |
| . OII2 | . 01120 |  | . 99994 |  | .0492I | 387,7 | . 99997 |  | - 3830.17 |
| . OII3 | . O1I30 |  | . 99994 |  | . 05307 | 384,3 | . 99997 |  | - 3850.79 |
| .OII4 | . OI I 40 |  | -99994 |  | . 05690 | 380,9 | . 99997 |  | 0 39 II. 42 |
| 0.0115 | 0.01150 | 10,0 | 0.99993 | O,I | 8.06069 | 377,6 | 9.99997 | 0,0 | 03932.05 |
| .OII6 | . 01160 |  | . 99993 |  | . 06445 | 374,4 | . 99997 | O,I | - 3952.67 |
| . 0117 | . O1770 |  | . 99993 |  | .058I8 | 371,2 | . 99997 |  | - 40 I3.30 |
| . 0118 | . 01180 |  | . 99993 |  | . 07187 | 368,0 | . 99997 |  | 0 4033.92 |
| . OII9 | . 01190 |  | . 99993 |  | . 07554 | 364,9 | . 99997 |  | - 4054.55 |
| 0.0120 | 0.01200 | 10,0 | 0.99993 | O,I | 8.07917 | 361,9 | 9.99997 | O,I | $\begin{array}{lll}\text { o } 41 & 15.18\end{array}$ |
| .OI2I | . 01210 |  | . 99993 |  | . 08277 | 358,9 | . 99997 |  | 0 41 35.80 |
| . 0122 | . 01220 |  | . 99993 |  | .086,35 | 356,0 | . 99997 |  | o 4156.43 |
| . 0123 | . 01230 |  | . 99992 |  | . 08989 | 353, 1 | . 99997 |  | 04217.06 |
| . 0124 | . 01240 |  | . 99992 |  | .0934I | 350,2 | . 99997 |  | - 4237.68 |
| 0.0125 | 0.01250 | 10,0 | 0.99992 | O,I | 8.09690 | 347,4 | 9.99997 | O, I | 0 4258.3 I |
| . 0126 | .01260 |  | . 99992 |  | . 10036 | 344,7 | . 99997 |  | 04318.94 |
| . 0127 | . 01270 |  | . 99992 |  | . 10379 | 342,0 | . 99995 |  | o 4339.56 |
| . 0128 | . 01280 |  | . 99992 |  | . 10720 | 339,3 | -99996 |  | 04400.19 |
| . 0129 | . 01290 |  | . 99992 |  | . I 1058 | 335,6 | . 99996 |  | 04420.82 |
| 0.0130 | 0.01300 | 10,0 | 0.99992 | 0,1 | 8. II 393 | 334, I | 9.99996 | O,I | 0 44 41.44 |
| . O131 | .01310 |  | . 99991 |  | . II726 | 331,5 | . 99996 |  | 04502.07 |
| . 0132 | . O1320 |  | . 99991 |  | . I2056 | 329,0 | . 99996 |  | 04522.70 |
| . O133 | .OI330 |  | .9999I | . | . 12384 | 326,5 | . 99996 |  | 0 4543.32 |
| . 0134 | . OI 340 |  | .9999I |  | . 12709 | 324, I | . 99996 |  | 04603.95 |
| 0.0135 | 0.01350 | 10,0 | 0.99991 | O,I | 8.13032 | 321,7 | 9.99996 | O,I | - 4624.57 |
| .0136 | . 01360 |  | .9999I |  | . I3353 | 319,3 | . 99996 |  | 0 4645.20 |
| . 0137 | . 01370 |  | .9999I |  | . I3571 | 317,0 | . 99996 |  | 0 4705.83 |
| . 0138 | . 01380 |  | . 99990 |  | . 13987 | 314,7 | . 99996 |  | 0 0 7726.45 |
| . 0139 | . 01390 |  | . 99990 |  | . 14300 | 312,4 | . 99996 |  | 04747.08 |
| 0.0140 | 0.01400 | 10,0 | 0.99990 | O,I | 8. I46II | 310,2 | 9.99996 | 0,I | 04807.71 |
| . 0141 | . 01410 |  | . 99990 |  | . 14920 | 308,0 | . 99996 |  | 04828.33 |
| . 0142 | . O1420 |  | . 99990 |  | . 15227 | 305,8 | . 99996 |  | - 4848.96 |
| . OI43 | .01430 |  | . 99990 |  | . 15532 | 303,7 | . 99996 |  | - 4909.59 |
| . 0144 | . 01440 |  | . 99990 |  | . 15835 | 301,6 | - 99995 |  | 04930.21 |
| 0.0145 | 0.01450 | 10,0 | 0.99989 | O,I | 8. 16I35 | 299,5 | 9.99995 | O,I | - 4950.84 |
| . 0146 | . 01460 |  | . 99989 |  | . 16434 | 297,4 | . 99995 |  | O 50 II. 47 |
| . 0147 | . 01470 |  | . 99989 |  | . 16730 | 295,4 | . 99995 |  | 0 5032.09 |
| . 0148 | . 01480 |  | . 99989 |  | . 17025 | 293,4 | . 99995 |  | 05052.72 |
| . 0149 | . 01490 |  | . 99989 |  | . 17317 | 291,5 | . 99995 |  | 0 51 13.35 |
| 0.0150 | 0.01500 | 10,0 | 0.99989 | O,I | 8.17608 | 289,5 | 9.99995 | 0,I | 0 51 33.97 |
| 4 | -isinh iu | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| $u$ | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { c o s }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0150 | 0.01500 | 10,0 | 0.99989 | O,I | 8.17608 | 289,5 | 9.99995 | O,I | $0^{\circ} 51 \times 33.97$ |
| . OI5 1 | .OI510 |  | . 99989 | 0,2 | . 17895 | 287,6 | . 99995 |  | 05154.60 |
| . 0152 | . OI 520 |  | . 99988 |  | . 18183 | 285,7 | . 99995 |  | - 5215.23 |
| . 0153 | . 01530 |  | . 99988 |  | . 18467 | 283,8 | . 99995 |  | - 5235.85 |
| . 0154 | . OI 540 |  | . 99988 |  | . 18750 | 282,0 | . 99995 |  | - 5256.48 |
| 0.0155 | 0.01550 | 10,0 | 0.99988 | 0,2 | 8.1903I | 280,2 | 9.99995 | O,I | 05317.10 |
| .0156 | . OI 560 |  | . 99988 |  | . 193II | 278,4 | . 99995 |  | - 5337.73 |
| . 0157 | . OI 570 |  | . 99988 |  | . 19588 | 276,6 | . 99995 |  | - 5358.36 |
| . 0158 | . 01580 |  | . 99988 |  | . 19864 | 274,9 | . 99995 |  | - 5418.98 |
| . OI'59 | . OI 590 |  | . 99987 |  | . 20138 | 273, I | . 99995 |  | 05439.6 I |
| 0.0160 | 0.01600 | 10,0 | 0.99987 | 0,2 | 8.20410 | 271,4 | 9.99994 | 0,I | 05500.24 |
| . 0161 | . 01610 |  | . 99987 |  | . 2068I | 269,7 | . 99994 |  | 0 5520.86 |
| . 0162 | . 01620 |  | . 99987 |  | . 20950 | 268, I | . 99994 |  | O 55 4I. 49 |
| . 0163 | . 01630 |  | . 99987 |  | .21217 | 266,4 | . 99994 |  | 0 5602.12 |
| . 0164 | . 01640 |  | . 99987 |  | . 21482 | 264,8 | . 99994 |  | - 5622.74 |
| 0.0165 | 0.01650 | 10,0 | 0.99985 | 0,2 | 8.21746 | 263,2 | 9.99994 | O,I | - $5643 \cdot 37$ |
| . 0166 | . 01660 |  | . 99986 |  | . 22009 | 26I,6 | . 99994 |  | - 5704.00 |
| . 0167 | . 01670 |  | . 99986 |  | . 22270 | 260,0 | . 99994 |  | - 5724.62 |
| . 0168 | . 01680 |  | . 99985 |  | . 22529 | 258,5 | . 99994 |  | O 5745.25 |
| . 0169 | . 01690 |  | . 99986 |  | . 22787 | 257,0 | . 99994 |  | - 5805.88 |
| 0.0170 | 0.01700 | 10,0 | 0.99986 | 0,2 | 8.23043 | 255,4 | 9.99994 | 0,I | 0 5826.50 |
| . 0171 | . 01710 |  | . 99985 |  | . 23298 | 253,9 | . 99994 |  | 05847.13 |
| . 0172 | . 01720 |  | . 99985 |  | . 23551 | 252,5 | . 99994 |  | 0 5907.75 |
| . 0173 | . 01730 |  | . 99985 |  | . 23802 | 251,0 | . 99994 |  | - 5928.38 |
| . 0174 | . 01740 |  | . 99985 |  | . 24053 | 249,6 | . 99993 |  | - 5949.01 |
| 0.0175 | 0.01750 | 10,0 | 0.99985 | 0,2 | 8.24302 | 248, I | 9.99993 | O,I | $1 \begin{array}{llll}1 & 00 & 09.63\end{array}$ |
| . 0176 | . 01760 |  | . 99985 |  | . 24549 | 246,7 | . 99993 |  | 1 l 0030.26 |
| . 0177 | . 01770 |  | . 99984 |  | . 24795 | 2.45,3 | . 99993 |  | 10050.89 |
| . 0178 | . 01780 |  | . 99984 |  | . 25040 | 244,0 | . 99993 |  | 1 OI II.5I |
| .0179 | . 01790 |  | . 99384 |  | .25283 | 242,6 | . 99993 |  | I OI 32.14 |
| 0.0180 | 0.01800 | 10,0 | 0.99984 | 0,2 | 8.25525 | 241,2 | 9.99993 | O,I | I OI 52.77 |
| . 018 l | . 01810 |  | . 99984 |  | . 25766 | 239,9 | . 99993 |  | 10213.39 |
| . 0182 | . 01820 |  | . 99983 |  | . 26005 | 238,6 | . 99993 |  | 10234.02 |
| . 0183 | . 01830 |  | . 99983 |  | . 26243 | 237,3 | . 99993 |  | 1 l 0254.65 |
| . 0184 | . 01840 |  | . 99983 |  | . 26479 | 236,0 | . 99993 |  | 10315.27 |
| 0.0185 | 0.01850 | 10,0 | 0.99983 | 0,2 | 8.26715 | 234,7 | 9.99993 | O, I |  |
| . 0186 | . 01860 |  | . 99983 |  | . 26949 | 233,5 | . 99992 |  | $\begin{array}{llll}\text { I } 0356.53 \\ \text { I } & 04 \\ \text { I }\end{array}$ |
| . 0187 | . 01870 |  | . 99983 |  | . 27182 | 232,2 | -99992 |  | I 0417.15 |
| . 0188 | . 01880 |  | . 99982 |  | . 27413 | 231,0 | . 99992 |  | $\begin{array}{lll}1 & 04 & 37.78 \\ \text { I } & 04 & 58.40\end{array}$ |
| . 0189 | . 01890 |  | . 99982 |  | . 27644 | 229,8 | -99992 |  | I 0458.40 |
| 0.0190 | 0.01900 | 10,0 | 0.99982 | 0,2 | 8.27873 | 228,5 | 9.99992 | 0,1 | I 0519.03 |
| . 0191 | . 01910 |  | . 99982 |  | . 28101 | 227,4 | . 99992 |  | $\begin{array}{llll}\text { I } & 05 & 39.06 \\ \text { I } & 06 & 00.28\end{array}$ |
| . 0192 | . 01920 |  | . 99982 |  | . 28327 | 226,2 225,0 | . 99992 |  | $\begin{array}{lll}1 & 06 & 00.28 \\ \text { I } & 06 & 20.91\end{array}$ |
| . 0193 | . 01930 |  | .9998I |  | . 288573 | 225,0 223,8 | . 99992 |  | $\begin{array}{llll}1 & 06 & 20.91 \\ 1 & 06 & 41.54\end{array}$ |
| . 0194 | . 01940 |  | . 99981 |  | . 28777 | 223,0 | -99992 |  | 10641.54 |
| 0.0195 | 0.01950 | 10,0 | 0.99981 | 0,2 | 8.29001 | 222,7 | 9.99992 | O,I | 10702.16 |
| . 0196 | . 01960 |  | .9998I |  | . 29223 | 22 I, 6 | . 99992 |  | I 0722.79 |
| . 0197 | . 01970 |  | . 99981 |  | . 29444 | 220,4 | . 99992 |  | I 0743.42 |
| . 0198 | . 01980 |  | . 99980 |  | . 29664 | 219,3 | . 9999 I |  | $\begin{array}{lll}\text { I } & 08 & 04.04\end{array}$ |
| . 0199 | . 01990 |  | . 99980 |  | . 29882 | 218,2 | .9999I |  | I 0824.67 |
| 0.0200 | 0.02000 | 10,0 | 0.99980 | 0,2 | 8.30100 | 217,1 | 9.99991 | 0, I | I 0845.30 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh \mathrm{iu}}{i}$ | $\omega F_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0200 | 0.02000 | 10,0 | 0.99980 | 0,2 | 8.30100 | 217,1 | 9.99991 | O,I | $\mathrm{I}^{\circ} 08^{\prime} 45^{\prime \prime} .30$ |
| . 0201 | . 02010 |  | .99980 |  | -30317 | 216,0 | -9999I |  | 10905.92 |
| . 0202 | . 02020 |  | . 99980 |  | . 30532 | 215,0 | .9999I |  | 10926.55 |
| . 0203 | . 02030 |  | -99979 |  | - 30747 | 213,9 | . 99991 |  | 10947.18 |
| . 0204 | . 02040 |  | . 99979 |  | . 30960 | 212,9 | . 99991 |  | 11007.80 |
| 0.0205 | 0.02050 | 10,0 | 0.99979 | 0,2 | 8.31172 | 211,8 | 9.99991 | O,I | I 1028.43 |
| . 0206 | . 02060 |  | . 99979 |  | -31384 | 210,8 | . 99991 |  | I 1049.06 |
| . 0207 | .02070 |  | . 99979 |  | -31594 | 209,8 | . 99991 |  | 1 II 09.68 |
| . 0208 | . 02080 |  | . 99978 |  | - 31803 | 208,8 | . 99991 |  | 1 II 30.31 |
| . 0209 | . 02090 |  | . 99978 |  | -32012 | 207,8 | . 99991 |  | 1 II 50.93 |
| 0.0210 | 0.02100 | 10,0 | 0.99978 | 0,2 | 8.32219 | 206,8 | 9.99990 | O,I | 11211.56 |
| . 0211 | .02110 |  | . 99978 |  | . 32425 | 205,8 | . 99990 |  | 11232.19 |
| . 0212 | .02120 |  | . 99978 |  | . 32630 | 204,8 | . 99990 |  | 11252.81 |
| . 0213 | . 02130 |  | . 99977 |  | - 32835 | 203,9 | . 99990 |  | $1 \begin{array}{lll}13 & 13.44\end{array}$ |
| . 0214 | .02140 |  | . 99977 |  | . 33038 | 202,9 | . 99990 |  | 1 I 334.07 |
| 0.0215 | 0.02150 | 10,0 | 0.99977 | 0,2 | 8.3324I | 202,0 | 9.99990 | O,I | $1 \begin{array}{lll}13 & 54.69\end{array}$ |
| . 0216 | . 02160 |  | . 99977 |  | . 33442 | 201,0 | . 99990 |  | $1 \begin{array}{lll}14 & 15.32\end{array}$ |
| .0217 | . 02170 |  | -99976 |  | - 33643 | 200, I | . 99990 |  | 1 I4 35.95 |
| . 0218 | . 02180 |  | . 99976 |  | . 33842 | 199,2 | . 99990 |  | 11456.57 |
| . 0219 | . 02190 |  | . 99976 |  | . 3404 I | 198,3 | . 99990 |  | 1 I5 17.20 |
| 0.0220 | 0.02200 | 10,0 | 0.99976 | 0,2 | 8.34239 | 197,4 | 9.99989 | O, I | $1 \begin{array}{llll}1 & 15 & 37.83\end{array}$ |
| .022I | . 02210 |  | . 99976 |  | . 34436 | 196,5 | - 99989 |  | 11558.45 |
| . 0222 | . 02220 |  | . 99975 |  | - 34632 | 195,6 | -99989 |  | 11619.08 |
| . 0223 | . 02230 |  | . 99975 |  | . 34827 | 194,7 | . 99989 |  | 11639.71 |
| . 0224 | . 02240 |  | . 99975 |  | . 35021 | 193,8 | -99989 |  | 11700.33 |
| 0.0225 | 0.02250 | 10,0 | 0.99975 | 0,2 | 8.35215 | 193,0 | 9.99989 | 0,1 | I 1720.96 |
| . 0226 | . 02260 |  | . 99974 |  | . 35407 | 192,I | . 99989 |  | 1 I 74 4 .58 |
| . 0227 | . 02270 |  | . 99974 |  | - 35599 | 191,3 | . 99989 |  | 11802.21 |
| . 0228 | . 02280 |  | . 99974 |  | - 35790 | 190,4 | . 99989 |  | 11822.84 |
| . 0229 | . 02290 |  | . 99974 |  | - 35980 | 189,6 | . 99989 |  | I 1843.46 |
| 0.0230 | 0.02300 | 10,0 | 0.99974 | 0,2 | 8.36169 | 188,8 | 9.99989 | O,I | I 1904.09 |
| . 0231 | . 02310 |  | . 99973 |  | . 36357 | 188,0 | . 99988 |  | I 19 24.72 |
| . 0232 | . 02320 |  | . 99973 |  | . 36545 | 187,2 | . 99988 |  | I 1945.34 |
| . 0233 | . 02330 |  | . 99973 |  | . 36732 | 186,4 | . 99988 |  | 12005.97 |
| . 0234 | . 02340 |  | . 99973 |  | . 36918 | 185,6 | . 99988 |  | 12026.60 |
| 0.0235 | 0.02350 | 10,0 | 0.99972 | 0,2 | 8.37103 | 184,8 | 9.99988 | O,I | I 2047.22 |
| . 0236 | . 02360 |  | . 99972 |  | . 37287 | 184,0 | . 99988 |  | 12107.85 |
| . 0237 | . 02370 |  | . 99972 |  | . 3747 I | 183,2 | . 99988 |  | 12128.48 |
| . 0238 | . 02380 |  | . 99972 |  | . 37654 | 182,4 | . 99988 |  | 12149.10 |
| . 0239 | . 02390 |  | . 9997 I |  | . 37836 | 181,7 | . 99988 |  | 12209.73 |
| 0.0240 | 0.02400 | 10,0 | 0.9997 I | 0,2 | 8.38017 | 180,9 | 9.99987 | 0,1 | 12230.36 |
| . 0241 | . 02410 |  | . 9997 I |  | .38198 | 180,2 | . 99987 |  | 12250.98 |
| . 0242 | . 02420 |  | . 9997 I |  | . 38377 | 179,4 | . 99987 |  | 12311.61 |
| . 0243 | . 02430 |  | . 99970 |  | . 38556 | 178,7 | . 99987 |  | 12332.23 |
| . 0244 | . 02440 |  | . 99970 |  | . 38735 | 178,0 | . 99987 |  | 12352.86 |
| 0.0245 | 0.02450 | 10,0 | 0.99970 | 0,2 | 8.38912 | 177,2 | 9.99987 | O,I | I 2413.49 |
| . 0246 | . 02460 |  | . 99970 |  | . 39089 | 176,5 | . 99987 |  | 12434.11 |
| . 0247 | . 02470 |  | . 99969 |  | - 39265 | 175,8 | . 99987 |  | I 2454.74 |
| . 0248 | . 02480 |  | . 99969 |  | . 3944 I | I75, I | . 99987 |  | $\begin{array}{lll}1 & 25 & 15.37\end{array}$ |
| . 0249 | . 02490 |  | . 99969 |  | . 39615 | 174,4 | . 99987 |  | 1 2535.99 |
| 0.0250 | 0.02500 | 10,0 | 0.99969 | 0,2 | 8.39789 | 173,7 | 9.99986 | 0,I | I 2556.62 |
| u | -I sinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh \mathrm{iu}}{i}$ | ${ }^{\circ} \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| U | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0250 | 0.02500 | 10,0 | 0.59969 | 0,2 | 8.39789 | 173,7 | 9.99986 | O,I | $1{ }^{\circ} 25^{\prime} 56^{\prime \prime} .62$ |
| . 0251 | . 02510 |  | . 99969 | 0,3 | . 39963 | 173,0 | . 99986 |  | I 2617.25 |
| . 0252 | . 02520 |  | . 99968 |  | . 40135 | 172,3 | . 99986 |  | I 2637.87 |
| . 0253 | . 02530 |  | . 99968 |  | . 40307 | 171,6 | . 99986 |  | I 2658.50 |
| . 0254 | . 02540 |  | . 99968 |  | . 40479 | 170,9 | . 99986 |  | 12719.13 |
| 0.0255 | 0.02550 | 10,0 | 0.99967 | 0,3 | 8.40649 | 170,3 | 9.99986 | O,I | I 2739.75 |
| . 0256 | . 02560 |  | . 99967 |  | .40819 | 169,6 | . 99986 |  | I 2800.38 |
| . 0257 | . 02570 |  | . 99967 |  | . 40989 | 168,9 | . 99986 |  | I 282 I .01 |
| . 0258 | . 02580 |  | . 99967 |  | .41157 | 168,3 | . 99986 |  | I 2841.63 |
| . 0259 | . 02590 |  | . 99966 |  | . 41325 | 167,6 | . 99985 |  | I 2902.26 |
| 0.0260 | 0.02600 | 10,0 | 0.99966 | 0,3 | 8.41492 | 167,0 | 9.99985 | O,I | I 2922.88 |
| .0261 | .02610 |  | . 99966 |  | . 41659 | 166,4 | . 99985 |  | I 2943.51 |
| . 0262 | . 02620 |  | . 99966 |  | . 41825 | 165,7 | . 99985 |  | I 3004.14 |
| . 0263 | . 02630 |  | . 99965 |  | . 41991 | 165, I | . 99985 |  | I 3024.76 |
| . 0264 | . 02640 |  | . 99965 |  | . 42155 | 164,5 | . 99985 |  | I 3045.39 |
| 0.0265 | 0.02650 | 10,0 | 0.99965 | 0,3 | 8.42320 | 163,8 | 9.99985 | O,I | 13106.02 |
| . 0266 | . 02660 |  | . 99965 |  | . 42483 | 163,2 | . 99985 |  | 13126.64 |
| . 0267 | . 02670 |  | . 99964 |  | . 42646 | 162,6 | . 99985 |  | I 31 47.27 |
| . 0268 | . 02680 |  | . 99964 |  | . 42808 | 162,0 | . 99984 |  | 13207.90 |
| . 0269 | . 02690 |  | . 99964 |  | . 42970 | 161,4 | . 99984 |  | I 3228.52 |
| 0.0270 | 0.02700 | 10,0 | 0.99964 | 0,3 | 8.43131 | 160,8 | 9.99984 | O,I | I 3249.15 |
| . 0271 | . 02710 |  | . 99963 |  | . 43292 | 160,2 | . 99984 |  | I 3309.78 |
| . 0272 | . 02720 |  | . 99953 |  | . 43452 | I 59,6 | . 99984 |  | I 3330.40 |
| . 0273 | . 02730 |  | . 99963 |  | . 4361 I | 159,0 | . 99984 |  | 13351.03 |
| . 0274 | . 02740 |  | -99962 |  | . 43770 | 158,5 | . 99984 |  | I 34 II. 66 |
| 0.0275 | 0.02750 | 10,0 | 0.99962 | 0,3 | 8.43928 | 157,9 | 9.99984 | O,I | $\begin{array}{llll}\text { I } & 34 & 32.28\end{array}$ |
| . 0276 | . 02760 |  | . 99962 |  | . 44085 | 157,3 | . 99983 |  | 13452.91 |
| . 0277 | . 02770 |  | . 99962 |  | . 44242 | 156,7 | . 99983 |  | 1 ll 13.54 |
| . 0278 | . 02780 |  | .9996I |  | . 44399 | I'56,2 | . 99983 |  | I 3534.16 |
| . 0279 | . 02790 |  | .9996I |  | . 44555 | 155,6 | - 99983 |  | I 3554.79 |
| 0.0280 | 0.02800 | 10,0 | 0.99961 | 0,3 | 8.44710 | 155, 1 | 9.99983 | 0,I | $1{ }_{1} 3615.41$ |
| .0281 | . 02810 |  | . 99961 |  | . 44865 | I 54,5 | . 99983 |  | 13636.04 |
| . 0282 | . 02820 |  | . 99960 |  | . 45019 | I54,0 | . 99983 |  | I 3656.67 |
| . 0283 | . 02830 |  | . 99960 |  | . 45173 | I 53,4 | . 99983 |  | 13717.29 |
| . 0284 | . 02840 |  | . 99960 |  | . 45326 | I 52,9 | . 99982 |  | I 3737.92 |
| 0.0285 | 0.02850 | 10,0 | 0.99959 | 0,3 | 8.45479 | 152,3 | 9.99982 | 0,I | 13758.55 |
| . 0286 | . 02860 |  | . 99959 |  | . 45631 | 151,8 | . 99982 |  | $\begin{array}{llll}1 & 38 & 19.17\end{array}$ |
| . 0287 | . 02870 |  | . 99959 |  | . 45782 | 151,3 | . 99982 |  | 138839.80 |
| . 0288 | . 02880 |  | . 99959 |  | . 45933 | 150,8 | . 99982 |  | I 3900.43 |
| .0289 | . 02890 |  | . 99958 |  | . 46084 | 150,2 | . 99982 |  | I 3921.05 |
| 0.0290 | 0.02900 | 10,0 | 0.99958 | 0,3 | 8.46234 | 149,7 | 9.99982 | O,I | I 3941.68 |
| . 0291 | . 02910 |  | . 99958 |  | .46383 | 149,2 | . 99982 |  | $1{ }^{1} 4002.31$ |
| . 0292 | . 02920 |  | . 99957 |  | .46532 | 148,7 | . 99981 |  | I 4022.93 |
| . 0293 | . 02930 |  | . 99957 |  | . 4668 I | 148,2 | . 99981 |  | I 4043.50 |
| . 0294 | . 02940 |  | . 99957 |  | . 46828 | 147,7 | -0998I |  | I 4104.19 |
| 0.0295 | 0.02950 | 10,0 | 0.99956 | 0,3 | 8.46976 | 147,2 | 9.9998I | 0,I | $1{ }_{1} 4124.8 \mathrm{I}$ |
| . 0296 | . 02960 |  | . 99956 |  | . 47123 | 146,7 | .9998I |  | I 4145.44 |
| .0297 | . 02970 |  | . 99956 |  | . 47269 | 146,2 1457 | . 99981 |  | I 4206.06 I 4226.60 |
| . 0298 | . 02980 |  | . 99956 |  | .47415 | 145,7 145,2 | .9998I |  | $\begin{array}{llll}\text { I } 42 & 26.69 \\ \text { I } 4247.32\end{array}$ |
| . 0299 | . 02990 |  | -99955 |  | . 47561 | 145,2 | . 99981 |  | $14247 \cdot 32$ |
| 0.0300 | 0.03000 | 10,0 | 0.99955 | 0,3 | 8.47706 | 144,7 | 9.99980 | O, I | I 4307.94 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0300 | 0.03000 | 10,0 | 0.99955 | 0,3 | 8.47706 | 144,7 | 9.99980 | O,I |  |
| . 0301 | .03010 |  | . 99955 |  | . 47850 | 144,2 | . 99980 |  | I 4328.57 |
| . 0302 | . 03020 |  | . 99954 |  | . 47994 | 143.8 | . 99980 |  | I 4349.20 |
| . 0303 | . 03030 |  | . 99954 |  | . 48 I 38 | 143,3 | . 99980 |  | I 4409.82 |
| . 0304 | . 03040 |  | . 99954 |  | .4828I | I42,8 | . 99980 |  | I 4430.45 |
| 0.0305 | 0.03050 | 10,0 | 0.99953 | 0,3 | 8.48423 | 142,3 | 9.99980 | O,I | I 4451.08 |
| . 0306 | . 03060 |  | . 99953 |  | . 48565 | 141,9 | . 99980 |  | I 4511.70 |
| . 0307 | . 03070 |  | . 99953 |  | . 48707 | I4I,4 | . 99980 |  | I 4532.33 |
| . 0308 | .03080 |  | . 99953 |  | . 48848 | I41,0 | . 99979 |  | I 4552.96 |
| . 0309 | . 03090 |  | . 99952 |  | . 48989 | 140,5 | . 99979 |  | I 4613.58 |
| 0.0310 | 0.03100 | IO,0 | 0.99952 | 0,3 | 8.49129 | I40, I | 9.99979 | O,I | I 4634.21 |
| .03II | .03109 |  | . 99952 |  | . 49269 | I 39,6 | . 99979 |  | I 4654.84 |
| .0312 | .03119 |  | . 99951 |  | . 49408 | I 39,2 | -99979 |  | I 47 I5.46 |
| .0313 | .03129 |  | .9995I |  | . 49547 | 138,7 | . 99979 |  | I 4736.09 |
| .03I4 | .03I39 |  | . 99951 |  | . 49686 | 138,3 | . 99979 |  | I 4756.71 |
| 0.0315 | 0.03149 | 10,0 | 0.99950 | 0,3 | 3.49824 | 137,8 | 9.99978 | O,I | I 48 17.34 |
| . 0316 | .03159 |  | . 99950 |  | . 49961 | 137,4 | . 99978 |  | I 4837.97 |
| .0317 | .03169 |  | . 99950 |  | . 50099 | 137,0 | . 99978 |  | I 4858.59 |
| . 0318 | .03179 |  | . 99949 |  | . 50235 | 136,5 | . 99978 |  | 14919.22 |
| .0319 | .03189 |  | . 99949 |  | . 50372 | I36, I | .99978 |  | I 4939.85 |
| 0.0320 | 0.03199 | 10,0 | 0.99949 | 0,3 | 8.50508 | 135,7 | 9.99978 | O,I | I 5000.47 |
| . 0321 | . 03209 |  | . 99948 |  | . 50643 | 135,2 | . 99978 |  | I 502 I .10 |
| . 0322 | .03219 |  | . 99948 |  | . 50778 | 134,8 | . 99977 |  | I 504 I .73 |
| . 0323 | . 03229 |  | . 99948 |  | . 50913 | 134,4 | . 99977 |  | I 5102.35 |
| . 0324 | . 03239 |  | . 99948 |  | . 51047 | I34,0 | . 99977 |  | I 5I 22.98 |
| 0.0325 | 0.03249 | 10,0 | 0.99947 | 0,3 | 8.51181 | 133,6 | 9.99977 | 0,1 | I 5143.6 I |
| . 0326 | . 03259 |  | . 99947 |  | .51314 | 133,2 | . 99977 |  | I 5204.23 |
| . 0327 | . 03269 |  | . 99947 |  | . 51447 | 132,8 | . 99977 |  | I 5224.86 |
| . 0328 | . 03279 |  | . 99946 |  | . 51580 | I 32,4 | . 99977 |  | I 5245.49 |
| . 0329 | . 03289 |  | . 99946 |  | . 51712 | 132,0 | . 99976 |  | I 5306.11 |
| 0.0330 | 0.03299 | 10,0 | 0.99946 | 0,3 | 8.51844 | 131,6 | 9.99976 | O,I | I 5326.74 |
| . 033 I | . 03309 |  | . 99945 |  | . 51975 | 131,2 | . 99976 |  | I 5347.37 |
| . 0332 | . 03319 |  | . 99945 |  | . 52106 | I 30,8 | . 99976 |  | I 5407.99 |
| . 0333 | . 03329 |  | . 99945 |  | . 52236 | I30,4 | . 99976 |  | I 5428.62 |
| . 0334 | . 03339 |  | . 99944 |  | . 52367 | 130,0 | . 99976 |  | I 5449.24 |
| 0.0335 | 0.03349 | 10,0 | 0.99944 | 0,3 | 8.52496 | 129,6 | 9.99976 | O,I | I 5509.87 |
| . 0336 | . 03359 |  | . 99944 |  | . 52626 | 129,2 | . 99975 |  | 15530.50 |
| . 0337 | . 03369 |  | . 99943 | - | . 52755 | 128,8 | . 99975 |  | I 555 I .12 |
| . 0338 | . 03379 |  | . 99943 |  | . 52883 | 128,4 | . 99975 |  | $\begin{array}{llll}\text { I } & 56 & 11.75\end{array}$ |
| . 0339 | . 03389 |  | . 99943 |  | . 53012 | 128, I | . 99975 |  | I 5632.38 |
| 0.0340 | 0.03399 | 10,0 | 0.99942 | 0,3 | 8.53:140 | 127,7 | 9.99975 | O,I | I 5653.00 |
| . 0341 | . 03409 |  | . 99942 |  | . 53267 | 127,3 | . 99975 |  | 15713.63 |
| . 0342 | .03419 |  | . 99942 |  | - 53394 | 126,9 | . 99975 |  | I 5734.26 |
| . 0343 | . 03429 |  | . 9994 I |  | . 5352 I | 126,6 | . 99974 |  | I 5754.88 |
| . 0344 | . 03439 |  | . 9994 I |  | . 53647 | 126,2 | . 99974 |  | I 58 I5.51 |
| 0.0345 | 0.03449 | 10,0 | 0.99940 | 0,3 | 8.53773 | 125,8 | 9.99974 | 0,1 | I 5836.14 |
| . 0346 | . 03459 |  | . 99940 |  | . 53899 | 125,5 | . 99974 | 0,2 | I 5856.76 |
| . 0347 | . 03469 |  | . 99940 |  | . 54024 | I25, I | . 99974 |  | I 5917.39 |
| . 0348 | . 03479 |  | . 99939 |  | . 54149 | 124,7 | . 99974 |  | I 5938.02 |
| . 0349 | .03489 |  | . 99939 |  | . 54274 | 124,4 | . 99974 |  | I 5958.64 |
| 0.0350 | 0.03499 | 10,0 | 0.99939 | 0,3 | 8.54398 | 124,0 | 9.99973 | 0,2 | 20019.27 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0350 | 0.03499 | 10,0 | 0.99939 | 0,3 | 8.54398 | 124,0 | 9.99973 | 0,2 | $20^{\circ} 00^{\prime} 19.127$ |
| . 0351 | . 03509 |  | . 99938 | 0,4 | . 54522 | 123,7 | . 99973 |  | 20039.89 |
| . 0352 | . 03519 |  | . 99938 |  | . 54645 | 123,3 | . 99973 |  | 2 OI 00.52 |
| . 0353 | . 03529 |  | . 99938 |  | . 54768 | I23,0 | . 99973 |  | 2 OI 2I.15 |
| . 0354 | . 03539 |  | . 99937 |  | . 5489 I | I22,6 | . 99973 |  | 2 O1 41.77 |
| 0.0355 | 0.03549 | 10,0 | 0.99937 | 0,4 | 8.55014 | 122,3 | 9.99973 | 0,2 | 20202.40 |
| . 0355 | . 03559 |  | . 99937 |  | . 55136 | 121,9 | . 99972 |  | 20223.03 |
| . 0357 | . 03569 |  | . 99936 |  | - 55258 | 121,6 | . 99972 |  | 20243.65 |
| . 0358 | . 03579 |  | - 99936 |  | . 55379 | 121,3 | -99972 |  | 20304.28 |
| . 0359 | . 03589 |  | . 99936 |  | . 55500 | 120,9 | . 99972 |  | 20324.91 |
| 0.0360 | 0.03599 | 10,0 | 0.99935 | 0,4 | 8.55621 | 120,6 | 9.99972 | 0,2 | 20345.53 |
| . 0361 | . 03609 |  | . 99935 |  | -5574I | I20,3 | . 99972 |  | 20406.16 |
| . 0362 | .03619 |  | . 99934 |  | . 5586 I | I 19,9 | . 99972 |  | 20426.79 |
| . 0363 | . 03629 |  | . 99934 |  | . 55981 | I 19,6 | . 9997 I |  | 204 47.41 |
| . 0364 | . 03639 |  | . 99934 |  | .56101 | 119,3 | . 9997 I |  | 20508.04 |
| 0.0365 | 0.03649 | 10,0 | 0.99933 | 0,4 | 8.56220 | I 18,9 | 9.99971 | 0,2 | 20528.67 |
| . 0366 | . 03659 |  | . 99933 |  | . 56338 | I 18,6 | . 9997 I |  | 20549.29 |
| . 0367 | . 03669 |  | . 99933 |  | . 56457 | I 18,3 | . 9997 I |  | 20609.92 |
| . 0368 | . 03679 |  | . 99932 |  | . 56575 | 118,0 | . 9997 I |  | 20630.54 |
| . 0369 | . 03689 |  | . 99932 |  | . 56693 | 117,6 | . 99970 |  | 20651.17 |
| 0.0370 | 0.03699 | 10,0 | 0.99932 | 0,4 | 8.56810 | II7,3 | 9.99970 | 0,2 | 2,07 11.80 |
| . 0371 | . 03709 |  | . 9993 I |  | . 56927 | I 17,0 | . 99970 |  | 20732.42 |
| . 0372 | . 03719 |  | . 9993 I |  | . 57044 | 116,7 | . 99970 |  | 20753.05 |
| . 0373 | . 03729 |  | . 99930 |  | . 57161 | I 16,4 | . 99970 |  | 20813.68 |
| . 0374 | . 03739 |  | . 99930 |  | . 57277 | I 16, 1 | . 99970 |  | 20834.30 |
| 0.0375 | 0.03749 | 10,0 | 0.99930 | 0,4 | 8.57393 | I 15,8 | 9.99969 | 0,2 | 20854.93 |
| . 0376 | . 03759 |  | . 99929 |  | . 57509 | II 5,4 | . 99969 |  | 20915.56 |
| . 0377 | . 03769 |  | . 99929 |  | . 57624 | II5, I | . 99969 |  | 20936.18 |
| . 0378 | . 03779 |  | . 99929 |  | . 57739 | II 4,8 | . 99969 |  | 20956.81 |
| . 0379 | . 03789 |  | . 99928 |  | . 57854 | I I 4,5 | . 99969 |  | 2 IO 17.44 |
| 0.0380 | 0.03799 | 10,0 | 0.99928 | 0,4 | 8.57968 | I 14,2 | 9.99969 | 0,2 | 21038.06 |
| .038I | . 03809 |  | . 99927 |  | . 58082 | I 13,9 | . 99968 |  | 2 IO 58.69 |
| . 0382 | . 03819 |  | . 99927 |  | . 58195 | II3,6 | . 99968 |  | 2 II 19.32 |
| .0383 | . 03829 |  | . 99927 |  | . 58309 | I 13,3 | . 99968 |  | 2 II 39.94 |
| . 0384 | . 03839 |  | . 99926 |  | . 58422 | I 13,0 | . 99968 |  | 21200.57 |
| 0.0385 | 0.03849 | 10,0 | 0.99926 | 0,4 | 8.58535 | 112,7 | 9.99968 | 0,2 |  |
| . 0386 | . 03859 |  | . 99926 |  | . 58548 | 112,5 | . 99968 |  | 2 I2 41.82 |
| . 0387 | . 03869 |  | . 99925 |  | . 58760 | I I 2,2 | . 99967 |  | $2 \begin{array}{llll}2 & 13 & 02.45\end{array}$ |
| . 0388 | . 03879 |  | . 99925 |  | . 58872 | III,9 | . 99967 |  | $2 \begin{array}{llll}2 & 13 & 23.07\end{array}$ |
| . 0389 | . 03889 |  | . 99924 |  | . 58984 | III,6 | . 99967 |  | 21343.70 |
| 0.0390 | 0.03899 | 10,0 | 0.99924 | 0,4 | 8.59095 | III,3 | 9.99967 | 0,2 | $\begin{array}{llll}2 & 14 & 04.33\end{array}$ |
| . 0391 | . 03909 |  | . 99924 |  | . 59207 | I I I, 0 | . 99967 |  | $2 \begin{array}{lll}2 & 14 & 24.95\end{array}$ |
| . 0392 | . 03919 |  | . 99923 |  | . 59317 | 110,7 | . 999067 |  | $\begin{array}{llll}2 & 14 & 45.58\end{array}$ |
| . 0393 | . 03929 |  | . 99923 |  | . 59428 | I 10,5 | . 99966 |  | 2 I5 06.21 |
| . 0394 | . 03939 |  | . 99922 |  | . 59538 | 1 10,2 | - 99966 |  | 21526.83 |
| 0.0395 | 0.03949 | 10,0 | 0.99922 | 0,4 | 8.59648 | 109,9 | 9.99966 | 0,2 | 2 I5 47.46 |
| . 0396 | . 03959 |  | . 99922 |  | . 59758 | 109,6 | . 99966 |  | 21608.09 |
| . 0397 | . 03969 |  | . 9992 I |  | - 59868 | 109,3 | . 99966 |  | 21628.71 |
| . 0398 | . 03979 |  | . 9992 I |  | . 59977 | 109, 1 | . 99966 |  | $\begin{array}{llll}2 & 16 & 49.34\end{array}$ |
| . 0399 | . 03989 |  | . 99920 |  | . 60085 | 108,8 | . 99965 |  | 21709.97 |
| 0.0400 | 0.03999 | 10,0 | 0.99920 | 0,4 | 8.60194 | 108,5 | 9.99965 | 0,2 | 21730.59 |
| $u$ | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0400 | 0.03999 | 10,0 | 0.99920 | 0,4 | 8.60194 | 108,5 | 9.99965 | 0,2 | $2^{\circ} 177^{\prime} 30.159$ |
| . 0401 | . 04009 |  | . 99920 |  | . 60303 | 108,2 | . 99965 |  | 21751.22 |
| . 0402 | .04019 |  | . 99919 |  | . 60411 | 108,0 | . 99965 |  | 218 II. 85 |
| . 0403 | . 04029 |  | .99919 |  | . 60519 | 107,7 | . 99965 |  | 21832.47 |
| . 0404 | . 04039 |  | . 99918 |  | . 60626 | 107,4 | . 99965 |  | 2 I8 53.10 |
| 0.0405 | 0.04049 | 10,0 | 0.99918 | 0,4 | 8.60734 | 107,2 | 9.99964 | 0,2 | 2 I9 13.72 |
| . 0406 | . 04059 |  | . 99918 |  | . 6084 I | 106,9 | . 99964 |  | 2 I9 34.35 |
| .0407 | . 04069 |  | .99917 |  | . 60947 | 106,6 | . 99964 |  | 2 I9 54.98 |
| . 0408 | . 04079 |  | . 99917 |  | . 61054 | 106,4 | . 99964 |  | 22015.60 |
| . 0409 | . 04089 |  | . 99916 |  | .6II60 | 106, I | . 99964 |  | 22036.23 |
| 0.0410 | 0.04099 | 10,0 | 0.99916 | 0,4 | 8.61266 | 105,9 | 9.99963 | 0,2 | 22056.86 |
| .04II | . 04109 |  | . 99916 |  | . 61372 | 105,6 | . 99963 |  | 221517.48 |
| .0412 | .04II9 |  | . 99915 |  | .6I477 | IO5,4 | . 99963 |  | 22138.11 |
| .04I3 | . 04129 |  | . 99915 |  | .61583 | 105, I | . 99963 |  | 2 2158.74 |
| .04II | .04139 |  | .99914 |  | .6I688 | 104,8 | . 99963 |  | 22219.36 |
| 0.0415 | 0.04149 | 10,0 | 0.99914 | 0,4 | 8.61792 | IO4,6 | 9.99963 | 0,2 | 22239.99 |
| . 0416 | .04I59 |  | .99913 |  | . 61897 | 104,3 | . 99962 |  | 22300.62 |
| .0417 | .04169 |  | .99913 |  | . 62001 | 104, I | . 99962 |  | 223 2I.24 |
| .0418 | .04179 |  | .99913 |  | . 62105 | 103,8 | . 99962 |  | 22341.87 |
| .0419 | .04189 |  | . 99912 |  | . 62209 | 103,6 | . 99962 |  | 22402.50 |
| 0.0420 | 0.04199 | 10,0 | 0.99912 | 0,4 | 8.62312 | 103,3 | 9.99962 | 0,2 | 22423.12 |
| . 042 I | . 04209 |  | .999II |  | . 62415 | 103, I | . 99962 |  | 22443.75 |
| . 0422 | .04219 |  | .999II |  | . 62518 | 102,9 | . 99961 |  | $\begin{array}{llll}2 & 25 & 04.37\end{array}$ |
| .0423 | . 04229 |  | .999II |  | . 6262 I | 102,6 | .9996I |  | 22525.00 |
| . 0424 | . 04239 |  | . 99910 |  | . 62724 | 102,4 | . 9996 I |  | 22545.63 |
| 0.0425 | 0.04249 | 10,0 | 0.99910 | 0,4 | 8.62826 | 102, I | 9.9996I | 0,2 | 22606.25 |
| . 0426 | . 04259 |  | . 99909 |  | . 62928 | 101,9 | .9996I |  | 22626.88 |
| . 0427 | . 04269 |  | . 99909 |  | . 63030 | IOI,6 | . 99960 |  | 22647.51 |
| . 0428 | .04279 |  | . 99908 |  | .63I3I | IOI,4 | . 99960 |  | 22708.13 |
| . 0429 | . 04289 |  | . 99908 |  | . 63232 | 101,2 | . 99960 |  | 22728.76 |
| 0.0430 | 0.04299 | 10,0 | 0.99908 | 0,4 | 8.63:333 | 100,9 | 9.99960 | 0,2 | 22749.39 |
| .043I | . 04309 |  | . 99907 |  | . 63434 | 100,7 | . 99960 |  | 228 IO.01 |
| . 0432 | .04319 |  | . 99907 |  | . 63535 | 100,5 | . 99959 |  | 22830.64 |
| . 0433 | . 04329 |  | . 99906 |  | . 63635 | 100,2 | . 99959 |  | 2285 I .27 |
| . 0434 | . 04339 |  | . 99906 |  | . 63735 | 100,0 | . 99959 |  | 22911.89 |
| 0.0435 | 0.04349 | 10,0 | 0.99905 | 0,4 | 8.63835 | 99,8 | 9.99959 | 0,2 | 22932.52 |
| . 0436 | . 04359 |  | . 99905 |  | . 63935 | 99,5 | . 99959 |  | 22953.15 |
| . 0437 | . 04369 |  | . 99905 |  | . 64034 | 99,3 | . 99959 |  | 23013.77 |
| . 0438 | . 04379 |  | . 99904 |  | . 64134 | 99, I | . 99958 |  | 23034.40 |
| . 0439 | . 04389 |  | . 99904 |  | . 64233 | 98,9 | . 99958 |  | 23055.02 |
| 0.0440 | 0.04399 | 10,0 | 0.99903 | 0,4 | 8.6433 I | 98,6 | 9.99958 | 0,2 | 23115.65 |
| . 0441 | . 04409 |  | . 99903 |  | . 64430 | 98,4 | . 99958 |  | 23136.28 |
| . 0442 | .04419 |  | . 99902 |  | . 64528 | 98,2 | . 99958 |  | 23156.90 |
| . 0443 | . 04429 |  | . 99902 |  | .64626 | 98,0 | . 99957 |  | 23217.53 |
| . 0444 | . 04439 |  | .9990I |  | . 64724 | 97,7 | . 99957 |  | 23238.16 |
| 0.0445 | 0.04449 | 10,0 | 0.99901 | 0,4 | 8.64822 | 97,5 | 9.99957 | 0,2 | $2 \begin{array}{lll}2 & 32 & 58.78\end{array}$ |
| . 0446 | . 04459 |  | . 99901 |  | . 64919 | 97,3 | . 99957 |  | 23319.41 |
| . 0447 | . 04469 | $\square$ | . 99900 |  | .65016 | 97, I | . 99957 |  | 23340.04 |
| . 0448 | . 04479 |  | . 99900 |  | .65113 | 96,9 | . 99956 |  | 23400.66 |
| . 0.449 | . 04488 |  | . 99899 |  | .65210 | 96,7 | . 99956 |  | 23421.29 |
| 0.0450 | 0.04498 | 10,0 | 0.99899 | 0,4 | 8.65307 | 96,4 | 9.99956 | 0,2 | 234 41.92 |
| $u$ | -i sinh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega F_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { c o s }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0450 | 0.04498 | 10,0 | 0.99899 | 0,4 | 8.65307 | 96,4 | 9.99956 | 0,2 | $2^{\circ} 34^{\prime} 4 I^{\prime \prime} .92$ |
| .045 | . 04508 |  | . 99898 | 0,5 | . 65403 | 96,2 | . 99956 |  | 23502.54 |
| . 0452 | . 04518 |  | . 99898 |  | . 65499 | 96,0 | . 99956 |  | 23523.17 |
| . 0453 | . 04528 |  | . 99897 |  | . 65595 | 95,8 | . 99955 |  | 23543.80 |
| . 0454 | . 04538 |  | . 99897 |  | .65691 | 95,6 | . 99955 |  | 23604.42 |
| 0.0455 | 0.04548 | 10,0 | 0.99897 | 0,5 | 8.65786 | 95,4 | 9.99955 | 0,2 | 23625.05 |
| . $04{ }^{\prime} 56$ | . 04558 |  | . 99896 |  | .6588I | 95,2 | . 99955 |  | 23645.68 |
| . 0457 | . 04568 |  | . 99896 |  | . 65976 | 95,0 | . 99955 |  | 23706.30 |
| . 0458 | . 04578 |  | . 99895 |  | . 66071 | 94,8 | . 99954 |  | 23726.93 |
| . 0459 | . 04588 |  | . 99895 |  | . 66166 | 94,6 | . 99954 |  | $23747 \cdot 55$ |
| 0.0460 | 0.04598 | 10,0 | 0.99894 | 0,5 | 8.66260 | 94,3 | 9.99954 | 0,2 | 23808.18 |
| .046I | . 04608 |  | . 99894 |  | . 66355 | 94, I | . 99954 |  | 23828.81 |
| . 0462 | .04618 |  | . 99893 |  | . 66449 | 93,9 | . 99954 |  | 23849.43 |
| . 0463 | . 04628 |  | . 99893 |  | . 66543 | 93,7 | . 99953 |  | 23910.06 |
| . 0464 | .04638 |  | . 99892 |  | . 66636 | 93,5 | . 99953 |  | 23930.69 |
| 0.0465 | 0.04648 | 10,0 | 0.99892 | 0,5 | 8.66730 | 93,3 | 9.99953 | 0,2 | $2395 \mathrm{I} \cdot 3 \mathrm{I}$ |
| . 0466 | . 04658 |  | . 99891 |  | . 66823 | 93, I | . 99953 |  | 240 II. 94 |
| . 0467 | . 04668 |  | . 99891 |  | . 66916 | 92,9 | . 99953 |  | 24032.57 |
| . 0468 | . 04678 |  | . 99891 |  | . 67009 | 92,7 | . 99952 |  | 24053.19 |
| . 0469 | . 04688 |  | . 99890 |  | . 67101 | 92,5 | . 99952 |  | 24113.82 |
| 0.0470 | 0.04698 | 10,0 | 0.99890 | 0,5 | 8.67194 | 92,3 | 9.99952 | 0,2 | 24134.45 |
| . 0471 | . 04708 |  | . 99889 |  | . 67286 | 92, I | . 99952 |  | 24155.07 |
| . 0472 | . 04718 |  | . 99889 |  | . 67378 | 91,9 | . 99952 |  | $\begin{array}{llll}2 & 42 & 15.70\end{array}$ |
| . 0473 | . 04728 |  | . 99888 |  | . 67470 | 91,7 | . 9995 I |  | 24236.33 |
| . 0474 | . 04738 |  | . 99888 |  | . 67562 | 91,6 | . 99951 |  | 24256.95 |
| 0.0475 | 0.04748 | 10,0 | 0.99887 | 0,5 | 8.67653 | 91,4 | 9.99951 | 0,2 | $2 \begin{array}{llll}2 & 43 & 17.58\end{array}$ |
| . 0476 | . 04758 |  | . 99887 |  | . 67744 | 91,2 | . 9995 I |  | $243 \begin{array}{llll}28.20\end{array}$ |
| . 0.477 | . 04768 |  | . 99886 |  | . 67835 | 91,0 | . 99951 |  | 24358.83 |
| . 0478 | . 04778 |  | . 99886 |  | . 67926 | 90,8 | . 99950 |  | 24419.46 |
| . 0479 | . 04788 |  | . 99885 |  | . 68017 | 90,6 | . 99950 |  | 24440.08 |
| 0.0480 | 0.04798 | 10,0 | 0.99885 | 0,5 | 8.68107 | 90,4 | 9.99950 | 0,2 | 24500.71 |
| . 048 I | . 04808 |  | . 99884 |  | .68198 | 90,2 | . 99950 |  | 24521.34 |
| . 0482 | . 04818 |  | . 99884 |  | . 68288 | 90,0 | . 99950 |  | 24541.96 |
| . 0483 | . 04828 |  | . 99883 |  | . 68378 | 89,8 | . 99949 |  | 24602.59 |
| . 0484 | . 04838 |  | . 99883 |  | . 68468 | 89,7 | . 99949 |  | 24623.22 |
| 0.0485 | 0.04848 | 10,0 | 0.99882 | 0,5 | 8.68557 | 89,5 | 9.99949 | 0,2 | $\begin{array}{llll}2 & 46 & 43.84\end{array}$ |
| . 0486 | . 04858 |  | . 99882 |  | . 68647 | 89,3 | . 99949 |  | $2 \begin{array}{llll}2 & 47 & 04.47\end{array}$ |
| . 0487 | . 04868 |  | . 9988 I |  | . 68736 | 89, 1 | . 99948 |  | 247 25.10 |
| . 0488 | . 04878 |  | .9988I |  | . 68825 | 88,9 | . 99948 |  | 24745.72 |
| . 0489 | . 04888 |  | . 99880 |  | .68914 | 88,7 | . 99948 |  | 24806.35 |
| 0.0490 | 0.04898 | 10,0 | 0.99880 | 0,5 | 8.69002 | 88,6 | 9.99948 | 0,2 | $24826.98$ |
| . 0491 | . 04908 |  | . 99879 |  | . 69091 | 88,4 | . 99948 |  | 24847.60 |
| . . 0492 | . 04918 |  | . 99879 |  | .69179 | 88,2 | . 99947 |  | 24908.23 |
| . 0493 | . 04928 |  | . 99879 |  | . 69267 | 88,0 87,8 | . 99947 |  | 2 2 4928.85 |
| . 0494 | . 04938 |  | . 99878 |  | . 69355 | 87,8 | -99947 |  | 24949.48 |
| 0.0495 | 0.04948 | 10,0 | 0.99878 | 0,5 | 8.69443 | 87,7 | 9.99947 | 0,2 | 25010.11 |
| . 0496 | . 04958 |  | . 99877 |  | . 69530 | 87,5 | . 99947 |  | 25030.73 |
| . 0497 | . 04968 |  | . 99877 |  | . 69618 | 87,3 | . 99946 |  | 2505 I .36 |
| . 0498 | . 04978 |  | . 99876 |  | . 69705 | 87,1 870 | . 99946 |  | $\begin{array}{llll}2 & 51 & 11.99 \\ 2 & 51 & 32.61\end{array}$ |
| . 0499 | . 04988 |  | . 99876 |  | . 69792 | 87,0 | . 99946 |  | 2 5I 32.6I |
| 0.0500 | 0.04998 | 10,0 | 0.99875 | 0,5 | 8.69879 | 86,8 | 9.99946 | 0,2 | 25153.24 |
| u | -i sinh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0500 | 0.04998 | 10,0 | 0.99875 | 0,5 | 8.69879 | 85,8 | 9.99946 | 0,2 | $2^{\circ} 51^{\prime} 53.24$ |
| . 0501 | . 05008 |  | . 99875 |  | . 69956 | 86,6 | . 99945 |  | 25213.87 |
| . 0502 | . 05018 |  | . 99874 |  | . 70052 | 85,4 | . 99945 |  | 25234.49 |
| . 0503 | . 05028 |  | . 99874 |  | . 70138 | 86,3 | . 99945 |  | 25255.12 |
| . 0504 | . 05038 |  | . 99873 |  | . 70225 | 86, 1 | . 99945 |  | 25315.75 |
| 0.0505 | 0.05048 | 10,0 | 0.99873 | 0,5 | 8.70311 | 85,9 | 9.99945 | 0,2 | 2.5336 .37 |
| . 0506 | . 05058 |  | . 99872 |  | . 70397 | 85,8 | . 99944 |  | 25357.00 |
| . 0507 | . 05068 |  | . 99872 |  | . 70482 | 85,6 | . 99944 |  | 25417.63 |
| . 0508 | . 05078 |  | . 99871 |  | . 70568 | 85,4 | . 99944 |  | 254.38 .25 |
| . 0509 | . 05088 |  | . 95870 |  | . 70553 | 85,2 | . 99944 |  | 25458.88 |
| 0.0510 | 0.05098 | 10,0 | 0.99870 | 0,5 | 8.70738 | 85, 1 | 9.99943 | 0,2 | 25519.51 |
| .05II | .05108 |  | . 99859 |  | . 70823 | 84,9 | . 99943 |  | 25540.13 |
| . 0512 | . 05118 |  | . 99869 |  | . 70908 | 84,7 | . 99943 |  | 25600.76 |
| .0513 | .05128 |  | . 99868 |  | . 70993 | 84,6 | . 99943 |  | 25621.38 |
| .0514 | .05138 |  | . 99868 |  | . 71077 | 84,4 | . 99943 |  | 25642.01 |
| 0.0515 | 0.05148 | 10,0 | 0.95867 | 0,5 | 8.71162 | 84,3 | 9.99942 | 0,2 | 25702.64 |
| . 0516 | .05158 |  | . 99867 |  | . 712.46 | 84,1 | . 99942 |  | 25723.26 |
| . 0517 | .05168 |  | .95866 |  | . 71330 | 83,9 | . 99942 |  | 25743.89 |
| .0518 | .05178 |  | . 99866 |  | . 71414 | 83,8 | . 99942 |  | 25804.52 |
| .0519 | .05188 |  | . 99855 |  | . 71497 | 83,6 | .9994I |  | 25825.14 |
| 0.0520 | 0.05198 | 10,0 | 0.99855 | 0,5 | 8.71581 | 83,4 | 9.9994I | 0,2 | 25845.77 |
| .052I | . 05208 |  | . 99864 |  | . 71654 | 83,3 | . 9994 I |  | 25906.40 |
| . 0522 | . 05218 |  | . 99864 |  | . 71747 | 83,1 | . 9994 I |  | 25927.02 |
| .0523 | . 05228 |  | . 99863 |  | .71830 | 83,0 | . 9994 I |  | 25947.65 |
| . .0524 | . 05238 |  | . 99863 |  | . 71913 | 82,8 | . 99940 |  | 30008.28 |
| 0.0525 | 0.05248 | 10,0 | 0.99862 | 0,5 | 8.71996 | 82,6 | 9.99940 | 0,2 | 30028.90 |
| . 0526 | . 05258 |  | . 99862 |  | . 72079 | 82,5 | . 99940 |  | 30049.53 |
| . 0527 | . 05268 |  | . 99861 |  | .7216I | 82,3 | . 99940 |  | 3 OI 10.16 |
| . 0528 | . 05278 |  | .9986I |  | . 72243 | 82,2 | . 99939 |  | 3 OI 30.78 |
| . 0529 | . 05288 |  | . 99860 |  | . 72325 | 82,0 | . 99939 |  | 3 OI 5I.4I |
| 0.0530 | 0.05298 | 10,0 | 0.99860 | 0,5 | 8.72407 | 81,9 | 9.99939 | 0,2 | 30212.03 |
| . 0531 | . 05308 |  | . 99859 |  | . 72489 | 81,7 | . 99939 |  | 30232.66 |
| . 0532 | . 05317 |  | . 99859 |  | . 72571 | 81,6 | . 99939 |  |  |
| . 0533 | . 05327 |  | .95858 |  | . 72652 | 8r,4 | . 99938 |  | $\begin{array}{llll}3 & 03 & 13.91\end{array}$ |
| . 0534 | . 05337 |  | . 99857 |  | . 72733 | 81,3 | . 99938 |  | 30334.54 |
| 0.0535 | 0.05347 | 10,0 | 0.99857 | 0,5 | 8.728I5 | 8I, I | 9.99938 | 0,2 | 30355.17 |
| . 0536 | . 05357 |  | . 99856 |  | . 72896 | 80,9 | . 99938 |  | 30415.79 |
| . 0537 | . 05367 |  | . 99856 |  | . 72977 | 80,8 | . 99937 |  | 30436.42 |
| . 0538 | .C5377 |  | . 99855 |  | . 73057 | 80,6 | . 99937 |  | 30457.05 |
| . 0539 | . 05387 |  | . 99855 |  | .73I38 | 80,5 | . 99937 |  | 30517.67 |
| 0.0540 | 0.05397 | 10,0 | 0.99854 | 0,5 | 8.73218 | 80,3 | 9.99937 | 0,2 | 30538.30 |
| . 0541 | . 05407 |  | . 99854 |  | . 73299 | 80,2 | . 99936 |  | 30558.93 |
| . 0542 | . 05417 |  | . 99853 |  | . 73379 | 80,0 | . 99936 |  | $\begin{array}{llll}3 & 06 & 19.55\end{array}$ |
| . 0543 | . 05427 |  | . 99853 |  | . 73459 | 79,9 | . 99936 |  | 30640.18 |
| . 0544 | . 05437 |  | . 99852 |  | . 73538 | 79,8 | . 99936 |  | 30700.81 |
| 0.0545 | 0.05447 | 10,0 | 0.99852 | 0,5 | 8.73618 | 79,6 | 9.99935 | 0,2 | 30721.43 |
| . 0546 | . 05457 |  | . 9985 |  | . 73608 | 79,5 | . 99935 |  | 30742.06 |
| . 0547 | . 05467 |  | . 99850 |  | . 73777 | 79,3 | . 99935 |  | $\begin{array}{llll}3 & 08 & 02.68 \\ 3 & 08 & 23.31\end{array}$ |
| . 0548 | . 05477 |  | . 99850 |  | . 73856 | 79,2 79,0 | . 99935 |  | $\begin{array}{llll}3 & 08 & 23.31 \\ 3 & 08 & 43.94\end{array}$ |
| . 0549 | . 05487 |  | -99849 |  | . 73935 | 79,0 | . 99935 |  | $30843 \cdot 94$ |
| 0.0550 | 0.05497 | 10,0 | 0.99849 | 0,5 | 8.74014 | 78,9 | 9.99934 | 0,2 | 30904.56 |
| ju: | -i sinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh$ iu | $\omega F_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | $\boldsymbol{\operatorname { l o g }} \sin u$ | ${ }_{\sim}^{\omega} \mathrm{F}_{0}{ }^{\prime \prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0550 | 0.05497 | 10,0 | 0.99849 | 0,5 | 8.74014 | 78,9 | 9.99934 | 0,2 | $3^{\circ} 090004.56$ |
| . 0551 | . 051507 |  | . 99848 | 0,6 | . 74093 | 78,7 | . 99934 |  | 30925.19 |
| . 0552 | . 05517 |  | .95848 |  | . 74172 | 78,6 | . 99934 |  | 30945.82 |
| . 0553 | . 05527 |  | . 99847 |  | . 74250 | 78,5 | . 99934 |  | 31006.44 |
| . 0554 | . 05537 |  | .99847 |  | . 74329 | 78,3 | . 99933 |  | 31027.07 |
| 0.0555 | 0.05547 | 10,0 | 0.99846 | 0,6 | 8.74407 | 78,2 | 9.99933 | 0,2 | 31047.70 |
| . 0556 | . 05557 |  | . 99845 |  | . 74485 | 78,0 | . 99933 |  | 3 II 08.32 |
| . 0557 | . 05567 |  | . 99845 |  | . 74563 | 77,9 | . 99933 |  | 3 II 28.95 |
| . 0558 | . 05577 |  | . 99844 |  | . 7464 I | 77,7 | . 99993 |  | 3 II 49.58 |
| . 0.559 | . 05587 |  | . 99844 |  | . 74719 | 77,6 | . 99932 |  | 31210.20 |
| 0.0560 | 0.05597 | 10,0 | 0.99843 | 0,6 | 8.74796 | 77,5 | 9.99932 | 0,2 | $\begin{array}{llll}3 & 12 & 30.83\end{array}$ |
| .0561 | . 05607 |  | . 99843 |  | . 74873 | 77,3 | . 99932 |  | $\begin{array}{lllll}3 & 12 & 51.46\end{array}$ |
| . 0562 | .05617 |  | . 99842 |  | .74951 | 77,2 | . 9993 I |  | $\begin{array}{llll}3 & 13 & 12.08\end{array}$ |
| .0563 | . 05627 |  | . 99842 |  | . 75028 | 77,I | . 9993 I |  | 311332.71 |
| . 0564 | . 05637 |  | . 99841 |  | .75105 | 76,9 | . 99931 |  | $\begin{array}{llllllllllllllllllll}3 & 13 & 53.34\end{array}$ |
| 0.0565 | 0.05647 | 10,0 | 0.99840 | 0,6 | 8.75182 | 76,8 | 9.99931 | 0,2 | 3 I 4 I 3.96 |
| . 0566 | . 05657 |  | . 99840 |  | . 75258 | 76,6 | . 99930 |  | 3 I4 34.59 |
| . 0567 | . 05667 |  | . 99839 |  | . 75335 | 76,5 | . 99930 |  | 31455.21 |
| .0568 | . 05677 |  | . 99839 |  | .754II | 76,4 | . 99930 |  | 3 I |
| . 0569 | . 05687 |  | . 99838 |  | . 75488 | 76,2 | . 99930 |  | 3 I5 36.47 |
| 0.0570 | 0.05697 | 10,0 | 0.99838 | 0,6 | 8.75564 | 76,1 | 9.99929 | 0,2 | 31557.09 |
| . 0571 | .05707 |  | . 99837 |  | . 75640 | 76,0 | . 99929 |  | 31617.72 |
| . 0572 | . 05717 |  | . 99836 |  | . 75716 | 75,8 | . 99929 |  | 3 I6 38.35 |
| . 0573 | . 05727 |  | . 99836 |  | . 75792 | 75,7 | . 99929 |  | 3 I6 58.97 |
| . 0574 | . 05737 |  | . 998315 |  | . 75867 | 75,6 | . 99928 |  | 31719.60 |
| 0.0575 | 0.05747 | 10,0 | 0.9983'5 | 0,6 | 8.75943 | 75,4 | 9.99928 | 0,2 | 31740.23 |
| . 0576 | . 05757 |  | . 99834 |  | . 76018 | 75,3 | . 99928 | 0,3 | 31800.85 |
| . 0577 | . 05767 |  | . 99834 |  | . 76093 | 75,2 | . 99928 |  | 31821.48 |
| . 0578 | . 05777 |  | . 99833 |  | .76169 | 75,1 | . 99927 |  | 3 I8 42.11 |
| . 0579 | . 05787 |  | . 99832 |  | . 76244 | 74,9 | . 99927 |  | 31902.73 |
| 0.0580 | 0.05797 | 10,0 | 0.99832 | 0,6 | 8.76318 | 74,8 | 9.99927 | 0,3 | 31923.36 |
| .0581 | .05807 |  | .9983I |  | . 76393 | 74,7 | . 99927 |  | 3 I9 43.99 |
| . 0582 | .05817 |  | .9983I |  | . 76468 | 74,5 | . 99926 |  | 32004.61 |
| .0583 | . 05827 |  | . 99830 |  | .76542 | 74,4 | . 99926 |  | 32025.24 |
| . 0584 | . 05837 |  | . 99830 |  | . 76617 | 74,3 | . 99926 |  | 32045.86 |
| 0.0585 | 0.05847 | 10,0 | 0.99829 | 0,6 | 8.76691 | 74,2 | 9.99926 | 0,3 | 32106.49 |
| . 0586 | . 05857 |  | . 99828 |  | . 76765 | 74,0 | . 99925 |  | 3 21 27.12 |
| .0587 | . 05867 |  | . 99828 |  | . 76839 | 73,9 | . 99925 |  | 32147.74 |
| . 0588 | . 05877 |  | . 99827 |  | . 76913 | 73,8 | . 99925 |  | 32208.37 |
| . 0589 | . 05887 |  | . 99827 |  | . 76986 | 73,6 | . 99925 |  | 32229.00 |
| 0.0590 | 0.05897 | 10,0 | 0.99826 | 0,6 | 8.77060 | 73,5 | 9.99924 | 0,3 | 32249.62 |
| .0591 | . 05907 |  | . 99825 |  | .77133 | 73,4 | . 99924 |  | 32310.25 |
| . 0592 | . 05917 |  | . 99825 |  | . 77207 | 73,3 | . 99924 |  | $\begin{array}{llll}3 & 23 & 30.88\end{array}$ |
| . 0593 | . 05927 |  | . 99824 |  | . 77280 | 73,2 | . 99924 |  | 323 51.50 |
| . 0594 | . 05937 |  | . 99824 |  | . 77353 | 73,0 | . 99923 |  | 32412.13 |
| 0.0595 | 0.05946 | 10,0 | 0.99823 | 0,6 | 8.77426 | 72,9 | 9.99923 | 0,3 | 32432.76 |
| . 0596 | . 05956 |  | . 99822 |  | . 77499 | 72,8 | . 99923 |  | 32453.38 |
| . 0597 | . 05966 |  | . 99822 |  | . 77572 | 72,7 | . 99923 |  | 32514.01 |
| . 0598 | .05976 |  | . 9982 I |  | .77644 | 72,5 | . 99922 |  | 32534.64 |
| . 0599 | . 05986 |  | .9982I |  | . 77717 | 72,4 | . 99922 |  | 32555.26 |
| 0.0500 | 0.05996 | 10,0 | 0.99820 | 0,6 | 8.77789 | 72,3 | 9.99922 | 0,3 | 32615.89 |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | log cosh iu | $F_{0}{ }^{\prime}$ | $u \div$ |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0600 | 0.05996 | 10,0 | 0.99820 | 0,6 | 8.77789 | 72,3 | 9.99922 | 0,3 | $3^{\circ} 26^{\prime} 15.189$ |
| . 0601 | .06006 |  | . 99819 |  | .77861 | 72,2 | . 99922 |  | 32636.51 |
| . 0602 | . 06016 |  | . 99819 |  | . 77933 | 72,I | . 99921 |  | 32657.14 |
| . 0603 | . 06026 |  | - 99818 |  | . 78005 | 71,9 | . 99921 |  | $\begin{array}{lllll}3 & 27 & 17.77\end{array}$ |
| . 0604 | . 06036 |  | . 9988 |  | . 78077 | 71,8 | . 99921 |  | 3 3 |
| 0.0605 | 0.06046 | 10,0 | 0.99817 | 0,6 | 8.78149 | 71,7 | 9.99920 | 0,3 | 32759.02 |
| . 0606 | . 05056 |  | . 99816 |  | . 7822 I | 71,6 | . 99920 |  | 32819.65 |
| . 0607 | . 06066 |  | . 99816 |  | . 78292 | 71,5 | . 99920 |  | 32840.27 |
| . 0608 | . 05076 |  | . 99815 |  | . 78364 | 71,3 | . 99920 |  | 32900.90 |
| . 0609 | . 06086 |  | . 99815 | , | . 78435 | 71,2 | . 99919 |  | 329 21.53 |
| 0.0610 | 0.06096 | 10,0 | 0.99814 | 0,6 | 8.78506 | 71,1 | 9.99919 | 0,3 | 32942.15 |
| . 06.611 | .06106 |  | .99813 |  | . 78577 | 71,0 | . 99919 |  | 33002.78 |
| .0612 | .06116 |  | . 99813 |  | . 78648 | 70,9 | . 99919 |  | 33023.41 |
| .0613 | .06126 |  | . 99812 |  | . 78719 | 70,8 | . 99918 |  | 33044.03 |
| . 0614 | .06136 |  | . 99812 |  | . 78790 | 70,6 | . 99918 |  | 3 31 04.66 |
| 0.0615 | 0.06146 | 10,0 | 0.998 I I | 0,6 | 8.78860 | 70,5 | 9.99918 | 0,3 | 33125.29 |
| .0616 | . 06156 |  | . 99810 |  | . 78931 | 70,4 | . 99918 |  | 33145.91 |
| . 0617 | . 06166 |  | . 99810 |  | . 79001 | 70,3 | -99917 |  | $\begin{array}{lllll}3 & 32 & 06.54\end{array}$ |
| . 0618 | .06176 |  | . 99809 |  | . 7907 I | 70,2 | . 99917 |  | 33227.17 |
| . 0619 | .06I86 |  | - 99808 |  | .7914I | 70,1 | . 99917 |  | 33247.79 |
| 0.0620 | 0.06196 | 10,0 | 0.99808 | 0,6 | 8.7921 I | 70,0 | 9.99916 | 0,3 | 33308.42 |
| . 0621 | . 06206 |  | . 99807 |  | .7928I | 69,8 | . 99916 |  | 33329.04 |
| . 0622 | . 06216 |  | . 99807 |  | . 7935 I | 69,7 | . 99916 |  | 3 3 |
| . 0623 | . 06226 |  | . 99806 |  | . 7942 I | 69,6 | -99916 |  | 3 <br> 34 |
| . 0624 | . 06236 |  | . 99805 |  | . 79490 | 69,5 | . 99915 |  | 33430.92 |
| 0.0625 | 0.06246 | 10,0 | 0.99805 | 0,6 | 8.79560 | 69,4 | 9.99915 | 0,3 | 3.3451 .55 |
| . 0626 | . 06256 |  | . 99804 |  | . 79629 | 69,3 | . 99915 |  | 33512.18 |
| . 0627 | . 06266 |  | . 99804 |  | . 79698 | 69,2 | . 99915 |  | 33532.80 |
| . 0628 | . 06276 |  | . 99803 |  | . 79767 | 69,1 | -99914 |  | 3 35535.43 |
| . 0629 | . 06286 |  | . 99802 |  | . 79836 | 69,0 | . 99914 |  | 33614.06 |
| 0.0630 | 0.06296 | 10,0 | 0.99802 | 0,6 | 8.79905 | 68,8 | 9.99914 | 0,3 | 33634.68 |
| . 0631 | . 06306 |  | . 99801 |  | . 79974 | 68,7 | . 99913 |  | 33655.31 |
| . 0632 | . 06316 |  | - 99800 |  | . 80043 | 68,6 | - 99913 |  | $\begin{array}{lllll}3 & 37 & 15.94\end{array}$ |
| . 0633 | . 05322 |  | - 99800 |  | . 80111 | 68,5 | -99913 |  | 33736.56 |
| . 0634 | .06336 |  | . 99799 |  | . 80180 | 68,4 | . 99913 |  | 33757.19 |
| 0.0635 | 0.06346 | 10,0 |  | 0,6 | $\begin{array}{r}8.80248 \\ .80316 \\ \hline 8034\end{array}$ |  | 9.99912 .99912 | 0,3 |  |
| .0636 .0637 | .06356 |  | . 99798 |  | . 80316 | 68,2 68,1 | .99912 |  | 3 <br> 3 <br> 3 <br> 388 <br> 38 |
| .0637 | . 06366 |  | . 999797 |  | . 80453 | 68,0 | . 999912 |  | 3 <br> 3 <br> 3 <br> 19 <br> 19.69 |
| . 0639 | . 06386 |  | . 99796 |  | . 80521 | 67,9 | . 9991 I |  | $33940.3^{2}$ |
| 0.0640 | 0.06396 | 10,0 | 0.99795 | 0,6 | 8.80588 | 67,8 | 9.99911 | 0,3 | 34000.95 |
| . 0641 | . 06406 |  | . 99795 |  | . 80056 | 67,7 | . 99911 |  | 34021.57 |
| . 0642 | .06416 |  | . 99794 |  | . 80724 | 67,6 | - 99910 |  | 34042.20 |
| . 0643 | . 06426 |  | - 99793 |  | . 80791 | 67,4 | -99910 |  | $\begin{array}{llll}3 & 41 & 02.83 \\ 3 & 41 & 23.45\end{array}$ |
| . 0644 | . 06436 |  | . 99793 |  | . 80859 | 67,3 | -99910 |  | 34123.45 |
|  | 0.06446 | 10,0 | 0.99792 | 0,6 | 8.80926 | 67,2 | 9.99910 | 0,3 | $\begin{array}{llll}3 & 41 \\ 3\end{array} 4.08$ |
| . 06646 | . 06456 |  | .99791 |  | . 80993 | 67, 1 | - 99909 |  | $\begin{array}{llll}3 & 42 & 04.71\end{array}$ |
| . 0647 | . 06465 |  | . 99791 |  | .81060 | 67,0 | - 99909 |  | $\begin{array}{llll}3 & 42 & 25.33 \\ 3 & 42 & 45.96\end{array}$ |
| . 0648 | . 06475 |  | - 99770 |  | .81127 .8194 | 66,9 66,8 | . 99909 |  | 34245.96 34306.59 |
| . 0649 | . 06485 |  | . 99789 |  | .8II94 | 66,8 | -99908 |  | 34300.59 |
| 0.0650 | 0.06495 | 10,0 | 0.99789 | 0,6 | 8.81261 | 66,7 | 9.99908 | 0,3 | 34327.21 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh \text { iu }}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh$ iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| $u$ | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0650 | 0.06495 | 10,0 | 0.99789 | 0,6 | 8.81261 | 66,7 | 9.99908 | 0,3 | $3^{\circ} 433^{\prime} 27^{\prime \prime} .21$ |
| . 0651 | . 06505 |  | . 99788 | 0,7 | .81327 | 66,6 | . 99908 | 0,3 | $\begin{array}{llll}3 & 43 & 47.84\end{array}$ |
| . 0652 | . 06515 |  | . 99788 |  | .81394 | 66,5 | . 99908 |  | $\begin{array}{llll}3 & 44 & 08.47\end{array}$ |
| . 0653 | . 06525 |  | . 99787 |  | . 81460 | 66,4 | . 99907 |  | 34429.09 |
| . 0654 | . 06535 |  | . 99786 |  | . 81527 | 66,3 | . 99907 |  | 34449.72 |
| 0.0655 | 0.06545 | 10,0 | 0.99786 | 0,7 | 8.81593 | 66,2 | 9.99907 | 0,3 | 345 IO. 34 |
| . 0656 | . 06555 |  | . 99785 |  | . 81659 | 66, | . 99906 |  | 34530.97 |
| . 0657 | . 06565 |  | . 99784 |  | .81725 | 66,0 | . 99906 |  | 34551.60 |
| . 0658 | . 06575 |  | . 99784 |  | . 81791 | 65,9 | . 99906 |  | 34612.22 |
| . 0659 | . 06585 |  | .99783 |  | .81857 | 65,8 | . 99906 |  | 34632.85 |
| 0.0660 | 0.06595 | 10,0 | 0.99782 | 0,7 | 8.81923 | 65,7 | 9.99905 | 0,3 | 34653.48 |
| .0661 | .06605 |  | . 99782 |  | . 81989 | 65,6 | . 99905 |  | 34714.10 |
| . 0662 | . 06615 |  | .9978I |  | . 82054 | 65,5 | . 99905 |  | 34734.73 |
| . 0663 | . 06625 |  | . 99780 |  | . 82120 | 65,4 | . 99904 |  | 34755.36 |
| . 0664 | . 06635 |  | . 99780 |  | . 82185 | 65,3 | . 99904 |  | $3 \quad 48 \quad 15.98$ |
| 0.0665 | 0.06645 | 10,0 | 0.99779 | 0,7 | 8.82250 | 65,2 | 9.99904 | 0,3 | 34836.61 |
| . .0666 | . 06655 |  | . 99778 | , | .82315 | 65, 1 | . 99904 |  | 34857.24 |
| . 0667 | . 06665 |  | . 99778. |  | . 82380 | 65,0 | . 99903 |  | 34917.86 |
| . 0668 | . 06675 |  | . 99777 |  | . 82445 | 64,9 | . 99903 |  | 34938.49 |
| . 0669 | . 06685 |  | . 99776 |  | . 82510 | 64,8 | . 99903 |  | 34959.12 |
| 0.0670 | 0.06695 | 10,0 | 0.99776 | 0,7 | 8.82575 | 64,7 | 9.99902 | 0,3 | 35019.74 |
| . 0671 | . 06705 |  | . 99775 |  | . 82640 | 64,6 | . 99902 |  | 35040.37 |
| . 0672 | . 06715 |  | . 99774 |  | . 82704 | 64,5 | . 99902 |  | 3 51 00.99 |
| . 0673 | . 06725 |  | . 99774 |  | . 82769 | 64,4 | . 99902 |  | 35121.62 |
| . 0674 | . 06735 |  | . 99773 |  | . 82833 | 64,3 | .9990I |  | 35142.25 |
| 0.0675 | 0.06745 | 10,0 | 0.99772 | 0,7 | 8.82897 | 64,2 | 9.99901 | 0,3 | 35202.87 |
| . 0676 | . 067515 |  | . 99772 |  | . 82962 | 64, 1 | . 99901 |  | 35223.50 |
| . 0677 | . 06765 |  | . 99771 |  | . 83026 | 64,1 | . 99900 |  | 35244.13 |
| . 0678 | . 06775 |  | . 99770 |  | . 83090 | 64,0 | . 99900 |  | 35304.75 |
| . 0679 | . 06785 |  | . 99770 |  | .83154 | 63,9 | . 99900 |  | 35325.38 |
| 0.0680 | 0.06795 | 10,0 | 0.99769 | 0,7 | 8.83217 | 63,8 | 9.99900 | 0,3 | 35346.01 |
| .068I | . 06805 |  | . 99768 |  | .8328I | 63,7 | . 99899 |  | 35406.63 |
| . 0682 | .068I5 |  | . 99768 |  | . 83345 | 63,6 | . 99899 |  | 35427.26 |
| . 0683 | . 06825 |  | .99767 |  | . 83408 | 63,5 | . 99899 |  | 35447.89 |
| . 0684 | . 06835 |  | . 99766 |  | . 83472 | 63,4 | . 99898 |  | 35508.5 I |
| 0.0685 | 0.06845 | 10,0 | 0.99765 | 0,7 | 8.83535 | 63,3 | 9.99898 | 0,3 | 35529.14 |
| . 0686 | . 06855 |  | . 99765 |  | . 83598 | 63,2 | . 99898 |  | 35549.77 |
| . 0687 | . 06865 |  | . 99764 |  | . 83662 | 63,1 | -99897 |  | 35610.39 |
| . 0688 | . 06875 |  | . 99763 |  | . 83725 | 63,0 | . 99897 |  | 35631.02 |
| . 0689 | . 06885 |  | . 99763 |  | . 83788 | 62,9 | . 99897 |  | 35651.65 |
| 0.0690 | 0.06895 | 10,0 | 0.99762 | 0,7 | 8.83850 | 62,8 | 9.99897 | 0,3 | 35712.27 |
| . 0691 | . 06905 |  | . 99761 |  | . 83913 | 62,8 | . 99896 |  | 35732.90 |
| . 0692 | . 06914 |  | . 99761 |  | . 83976 | 62,7 | -99896 |  | 35753.52 |
| . 0693 | . 06924 |  | . 99760 |  | . 84039 | 62,6 | -99896 |  | 358 I4.15 |
| . 0694 | . 06934 |  | . 99759 |  | .84101 | 62,5 | . 99895 |  | 35834.78 |
| 0.0695 | 0.06944 | 10,0 | 0.99759 | 0,7 | 8.84164 | 62,4 | 9.99895 | 0,3 | 35855.40 |
| . 0696 | . 06954 |  | . 99758 |  | . 84226 | 62,3 | . 99895 |  | 35916.03 |
| . 0597 | . 06964 |  | . 99757 |  | . 84288 | 62,2 | . 99894 |  | 35936.66 |
| . 0699 | . 06974 |  | . 99756 |  | . 84350 | 62,1 | . 99894 |  | 35957.28 |
| . 0699 | . 06984 |  | . 99756 |  | . 84412 | 62,0 | . 99894 |  | 40017.91 |
| 0.0700 | 0.06994 | 10,0 | 0.99755 | 0,7 | 8.84474 | 61,9 | 9.99894 | 0,3 | 40038.54 |
| u | -isinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\mathrm{F}_{0}{ }^{\prime}$ | u |

## Smithsonian Tables

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0700 | 0.06994 | 10,0 | 0.99755 | 0,7 | 8.84474 | 6I,9 | 9.99894 | 0,3 | $40^{\circ} 00^{\prime} 38^{\prime \prime} .54$ |
| .0701 | . 07004 |  | . 99754 |  | . 84536 | 6I,9 | . 99893 |  | 40059.16 |
| . 0702 | .07014 |  | . 99754 |  | . 84598 | 6I,8 | . 99893 |  | 4 OI 19.79 |
| . 0703 | . 07024 |  | . 99753 |  | . 84660 | 61,7 | . 99893 |  | 4 OI 40.42 |
| . 0704 | . 07034 |  | . 99752 |  | . 84721 | 6I,6 | . 99892 |  | 40201.04 |
| 0.0705 | 0.07044 | 10,0 | 0.99752 | 0,7 | 8.84783 | 61,5 | 9.99892 | 0,3 | 40221.67 |
| . 0706 | . 07054 |  | . 99751 |  | . 84844 | 6I, 4 | . 99892 |  | 40242.30 |
| . 0707 | . 07064 |  | . 99750 |  | . 84906 | 6I,3 | . 9989 I |  | 40302.92 |
| . 0708 | . 07074 |  | . 99749 |  | . 84967 | $6 \mathrm{I}, 2$ | . 9989 I |  | $403 \quad 23.55$ |
| . 0709 | . 07084 |  | . 99749 |  | . 85028 | 6I,2 | . 99891 |  | 40344.17 |
| 0.0710 | 0.07094 | 10,0 | 0.99748 | 0,7 | 8.85089 | 6I, 1 | 9.99890 | 0,3 | 40404.80 |
| . 0711 | . 07104 |  | . 99747 |  | .85150 | $6 \mathrm{I}, 0$ | . 99890 |  | 40425.43 |
| . 0712 | . 07114 |  | . 99747 |  | . 8521 I | 60,9 | . 99890 |  | 40446.05 |
| . 0713 | . 07124 |  | . 99746 |  | . 85272 | 60,8 | . 99890 |  | 40506.68 |
| . 0714 | . 07134 |  | . 99745 |  | . 85333 | 60,7 | . 99889 |  | 40527.3 I |
| 0.0715 | 0.07144 | 10,0 | 0.99744 | 0,7 | 8.85394 | 60,6 | 9.99889 | 0,3 | 40547.93 |
| . 0716 | . 07154 |  | . 99744 |  | . 85454 | 60,6 | . 99889 |  | 40608.56 |
| .0717 | .07164 |  | . 99743 |  | . 85515 | 60,5 | . 99888 |  | 40629.19 |
| . 0718 | . 07174 |  | . 99742 |  | . 85575 | 60,4 | . 99888 |  | 40649.8 I |
| . 0719 | . 07184 |  | . 99742 |  | . 85635 | 60,3 | . 99888 |  | 40710.44 |
| 0.0720 | 0.07194 | 10,0 | 0.99741 | 0,7 | 8.85696 | 60,2 | 9.99887 | 0,3 | 40731.07 |
| .0721 | . 07204 |  | . 99740 |  | . 85756 | 60, I | . 99887 |  | 40751.69 |
| . 0722 | . 07214 |  | . 99739 |  | . 85816 | 60,0 | . 99887 |  | 40812.32 |
| .0723 | . 07224 |  | . 99739 |  | . 85876 | 60,0 | . 99886 |  | 40832.95 |
| . 0724 | . 07234 |  | . 99738 |  | . 85936 | 59,9 | . 99886 |  | 40853.57 |
| 0.0725 | 0.07244 | 10,0 | 0.99737 | 0,7 | 8.85996 | 59,8 | 9.99886 | 0,3 | 40914.20 |
| . 0726 | . 07254 |  | . 99737 |  | . 86056 | 59,7 | . 99885 |  | 40934.82 |
| . 0727 | . 07264 |  | . 99736 |  | .86II5 | 59,6 | . 99885 |  | 40955.45 |
| . 0728 | . 07274 |  | . 99735 |  | . 86175 | 59,6 | . 99885 |  | 4 10 16.08 |
| . 0729 | . 07284 |  | . 99734 |  | . 86234 | 59,5 | . 99884 |  | 4 Io 36.70 |
| 0.0730 | 0.07294 | 10,0 | 0.99734 | 0,7 | 8.86294 | 59,4 | 9.99884 | 0.3 | 41057.33 |
| .0731 | . 07303 |  | . 99733 |  | . 86353 | 59,3 | . 99884 |  | 4 II 17.96 |
| . 0732 | .07313 |  | . 99732 |  | . 86412 | 59,2 | . 99884 |  | 4 II 38.58 |
| . 0733 | . 07323 |  | .9973I |  | . 86472 | 59, I | . 99883 |  | 4 II 59.2 I |
| . 0734 | . 07333 |  | .9973I |  | . 8653 I | 59, I | . 99883 |  | 41219.84 |
| 0.0735 | 0.07343 | 10,0 | 0.99730 | 0,7 | 8.86590 | 59,0 | 9.99883 | 0,3 | 41240.46 |
| . 0736 | . 07353 |  | . 99729 |  | . 86649 | 58,9 | . 99882 |  | 41301.09 |
| . 0737 | . 07363 |  | . 99729 |  | . 86707 | 58,8 | . 99882 |  | 4 I3 21.72 |
| . 0738 | . 07373 |  | . 99728 |  | . 86766 | 58,7 | . 99882 |  | 4 I3 42.34 |
| . 0739 | . 07383 |  | . 99727 |  | . 86825 | 58,7 | .9988I |  | 41402.97 |
| 0.0740 | 0.07393 | 10,0 | 0.99726 | 0,7 | 8.86884 | 58,6 | 9.9988I | 0,3 | 41423.60 |
| . 0741 | . 07403 |  | . 99726 |  | . 86942 | 58,5 | .9988I |  | 41444.22 |
| . 0742 | . 07413 |  | . 99725 |  | . 87001 | 58,4 | . 99880 |  | $4{ }^{4} 1504.85$ |
| . 0743 | . 07423 |  | . 99724 |  | . 87059 | 58,3 | . 99880 |  | $\begin{array}{llll}4 & 15 & 25.48\end{array}$ |
| . 0744 | . 07433 |  | . 99723 |  | .87117 | 58,3 | . 99880 |  | 4 I5 46.10 |
| 0.0745 | 0.07443 | 10,0 | 0.99723 | 0,7 | 8.87175 | 58,2 | 9.99879 | 0,3 | 41606.73 |
| . 0746 | . 07453 |  | . 99722 |  | . 87234 | 58,1 | . 99879 |  | 41627.35 |
| . 0747 | . 07463 |  | . 99721 |  | . 87292 | 58,0 | . 99879 |  | 41647.98 |
| . 0748 | . 07473 |  | . 99720 |  | .87350 .87408 | 58,0 57,9 | . 99878 |  | $\begin{array}{llll}4 & 17 & 08.61 \\ 4 & 17 & 29.23\end{array}$ |
| . 0749 | . 07483 |  | . 99720 |  | . 87408 | 57,9 | -99878 |  | 41729.23 |
| 0.0750 | 0.07493 | 10,0 | 0.99719 | 0,7 | 8.87465 | 57,8 | 9.99878 | 0,3 | 41749.86 |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega F_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| 4 | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cos 4 | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0750 | 0.07493 | 10,0 | 0.99719 | 0,7 | 8.87465 | 57,8 | 9.99878 | 0,3 | $4^{\circ} 17^{\prime} 49.48$ |
| . 0751 | . 07503 |  | . 99718 | 0,8 | . 87523 | 57,7 | . 99877 |  | 41810.49 |
| . 0752 | . 07513 |  | . 99717 |  | .87581 | 57,6 | . 99877 |  | 4183 I .11 |
| . 0753 | . 07523 |  | . 99717 |  | . 87638 | 57,6 | . 99877 |  | 41851.74 |
| . 0754 | . 07533 |  | . 99716 |  | . 87696 | 57,5 | . 99876 |  | 41912.37 |
| 0.0755 | 0.07543 | 10,0 | 0.99715 | - 0,8 | 8.87753 | 57,4 | 9.99876 | 0,3 | 41932.99 |
| . 0756 | . 07553 |  | . 99714 |  | . 87811 | 57,3 | . 99876 |  | 41953.62 |
| . 0757 | . 07563 |  | . 99714 |  | . 87858 | 57,3 | - 99875 |  | 42014.25 |
| . 0758 | . 07573 |  | . 99713 |  | . 87925 | 57,2 | . 99875 |  | 42034.87 |
| . 0759 | . 07583 |  | -99712 |  | . 87982 | 57,I | . 99875 |  | 42055.50 |
| 0.0760 | 0.07593 | 10,0 | 0.99711 | 0,8 | 8.88040 | 57,0 | 9.99874 | 0,3 | 42116.13 |
| . 0761 | . 07603 |  | . 9971 I |  | . 88097 | 57,0 | . 99874 |  | 42136.75 |
| . 0762 | . 07613 |  | . 99710 |  | . 88153 | 56,9 | . 99874 |  | 42157.38 |
| . 0763 | . 07623 |  | . 99709 |  | . 88210 | 56,8 | . 99873 |  | 42218.00 |
| . 0764 | . 07633 |  | -99708 |  | . 88267 | 56,7 | . 99873 |  | 42238.63 |
| 0.0765 | 0.07643 | 10,0 | 0.99708 | 0,8 | 8.88324 | 56,7 | 9.99873 | 0,3 | 42259.26 |
| . 0766 | . 07653 |  | . 99707 |  | . 88380 | 56,6 | . 99872 |  | 42319.88 |
| . 0767 | . 07662 |  | -99706 |  | . 88437 | 56,5 | . 99872 |  | 42340.51 |
| . 0768 | . 07672 |  | . 99705 |  | . 88493 | 56,4 | . 99872 |  | 424 OI. I4 |
| . 0769 | . 07682 |  | . 99704 |  | . 88550 | 56,4 | . 99871 |  | 42421.76 |
| 0.0770 | 0.07692 | 10,0 | 0.99704 | 0,8 | 8.88606 | 56,3 | 9.99871 | 0,3 | 42442.39 |
| . 0771 | . 07702 |  | . 99703 |  | . 88562 | 56,2 | . 99871 |  | 42503.02 |
| . 0772 | . 07712 |  | . 99702 |  | . 88719 | 56,I | . 99870 |  | 42523.64 |
| . 0773 | . 07722 |  | . 99701 |  | . 88775 | 56,I | . 99870 |  | 42544.27 |
| . 0774 | . 07732 |  | .99701 |  | . 8883 I | 56,0 | . 99870 |  | 42604.90 |
| 0.0775 | 0.07742 | 10,0 | 0.99700 | 0,8 | 8.88887 | 55,9 | 9.99869 | 0,3 | 42625.52 |
| . 0776 | . 07752 |  | . 99699 |  | . 88943 | 55,9 | . 99869 |  | 42646.15 |
| . 0777 | . 07762 |  | . 99698 |  | . 88998 | 55,8 | . 99869 |  | 42706.78 |
| . 0778 | . 07772 |  | . 99698 |  | . 89054 | 55,7 | . 99868 |  | 42727.40 |
| . 0779 | . 07782 |  | -99697 |  | . 89110 | 55,6 | . 99858 |  | 42748.03 |
| 0.0780 | 0.07792 | 10,0 | 0.99696 | 0,8 | 8.89165 | 55,6 | 9.99868 | 0,3 | 42808.65 |
| . 0781 | . 07802 |  | . 99695 |  | . 8922 I | 55,5 | . 99867 |  | 42829.28 |
| . 0782 | . 07812 |  | . 99694 |  | . 89276 | 55,4 | . 99867 |  | 42849.91 |
| . 0783 | . 07822 |  | . 99694 |  | . 89332 | 55,4 | . 99867 |  | 429 10. 53 |
| . 0784 | . 07832 |  | . 99693 |  | . 89387 | 55,3 | -99866 |  | 42931.16 |
| 0.0785 | 0.07842 | 10,0 | 0.99692 | 0,8 | 8.89442 | 55,2 | 9.99866 | 0,3 | 42951.79 |
| . 0785 | . 07852 |  | . 99691 |  | . 89498 | 55, I | . 99866 |  | 43012.41 |
| . 0787 | . 07882 |  | . 99690 |  | . 89553 | 55, 1 | . $9986{ }^{\circ}$ |  | 43033.04 |
| . 0788 | . 07872 |  | . 99690 |  | . 89608 | 55,0 | . 99865 |  | 43053.67 |
| . 0789 | . 07882 |  | . 99689 |  | . 89653 | 54,9 | . 99865 |  | 43114.29 |
| 0.0790 | 0.07892 | 10,0 | 0.99688 | 0,8 | 8.89718 | 54,9 | 9.99864 | 0,3 | 43134.92 |
| . 0791 | . 07902 |  | . 99687 |  | . 89772 | 54,8 | . 99864 |  | 43155.55 |
| . 0792 | . 07912 |  | . 99687 |  | . 89827 | 54,7 | . 99864 |  | 432 16.17 |
| . 0793 | . 07922 |  | - 99686 |  | . 89882 | 54,7 | . 99863 |  | 43236.80 |
| . 0794 | . 07932 |  | - 99685 |  | . 89936 | 54,6 | . 99863 |  | 43257.43 |
| 0.0795 | 0.07942 | 10,0 | 0.99684 | 0,8 | 8.89991 | 54,6 | 9.99853 | 0,3 | 43318.05 |
| . 0796 | . 07952 |  | . 99683 |  | . 90045 | 54,4 | . 99862 |  | 43338.68 |
| . 0797 | . 07962 |  | . 99683 |  | . 90100 | 54,4 | . 99862 |  | 433 59.31 |
| . 0798 | . 07972 |  | - 99682 |  | . 90154 | 54,3 | . 99862 | - | 43419.93 |
| . 0799 | . 07982 |  | . 99681 |  | .90208 | 54,2 | . 99861 |  | 43440.56 |
| 0.0800 | 0.07991 | 10,0 | 0.99680 | 0,8 | 8.90263 | 54,2 | 9.9986I | 0,3 | 435 or. 18 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | 100 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} 4$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cos 4 | $\omega \mathrm{F}_{0}{ }^{\circ}$ | $\log \sin u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0800 | 0.07991 | 10,0 | 0.99680 | 0,8 | 8.90263 | 54,2 | 9.99861 | 0,3 | $4^{\circ} 35^{\circ}$ ог". ${ }^{\text {r }}$ |
| . 0801 | . 08001 |  | . 99679 |  | . 90317 | 54, 1 | . 99861 |  | 435 21.81 |
| . 0802 | . 08011 |  | . 99679 |  | . 9037 I | 54,0 | . 99860 |  | 43542.44 |
| . 0803 | . 08021 |  | . 99678 |  | . 90425 | 54,0 | . 99860 |  | 43603.06 |
| . 0804 | . 08031 |  | . 99677 |  | . 90479 | 53,9 | . 99859 |  | 43623.69 |
| 0.0805 | 0.08041 | 10,0 | 0.99676 | 0,8 | 8.90533 | - 53,8 | 9.99859 | 0,4 | 43644.32 |
| . 0806 | . 08051 |  | . 99675 |  | . 90586 | 53,8 | . 99859 |  | 43704.94 |
| . 0807 | . 08061 |  | . 99675 |  | . 90640 | 53,7 | . 99858 |  | 43725.57 |
| . 0808 | . 08071 |  | . 99674 |  | . 90694 | 53,6 | . 99858 |  | 43746.20 |
| . 0809 | .0808I |  | . 99673 |  | . 90747 | 53,6 | . 99858 |  | 43806.82 |
| 0.0810 | 0.08091 | 10,0 | 0.99672 | 0,8 | 8.90801 | 53,5 | 9.99857 | 0,4 | 43827.45 |
| .08II | .08101 |  | . 99671 |  | . 90854 | 53,4 | . 99857 |  | 43848.08 |
| .0812 | .081II |  | . $9967{ }^{\text {- }}$ |  | . 90908 | 53,4 | . 99857 |  | 43908.70 |
| .0813 | .0812I |  | -99970 |  | . 90951 | 53,3 | . 99856 |  | 43929.33 |
| . 0814 | .08131 |  | -99669 |  | .91014 | 53,2 | . 99856 |  | 43949.96 |
| 0.0815 | 0.08141 | 10,0 | 0.99668 | 0,8 | 8.91068 | 53,2 | 9.99856 | 0,4 | 44010.58 |
| . 0816 | .08151 |  | . 99667 |  | .91121 | 53,1 | . 99855 |  | 44031.21 |
| . 0817 | .0816I |  | . 99666 |  | .91174 | 53,0 | - 99855 |  | 44051.83 |
| . 0818 | .08171 |  | . 99666 |  | . 91227 | 53,0 | . 99855 |  | 44112.46 |
| . 0819 | .08181 |  | . 99665 |  | . 91280 | 52,9 | . 99854 |  | 44133.09 |
| 0.0820 | 0.08191 | 10,0 | 0.99664 | 0,8 | 8.91333 | 52,8 | 9.99854 | 0,4 | 44153.71 |
| . 0821 | . 08201 |  | . 99663 |  | . 91386 | 52,8 | . 99853 |  | 44214.34 |
| . 0822 | . 08211 |  | . 99662 |  | .91438 | 52,7 | - 99853 |  | 44234.97 |
| . 0823 | . 08221 |  | -99662 |  | .91491 | 52,7 | - 99853 |  | 44255.59 |
| . 0824 | .0823I |  | -99661 |  | . 91544 | 52,6 | - 99852 |  | 44316.22 |
| 0.0825 | 0.0824 I | 10,0 | 0.99660 | 0,8 | 8.91596 | 52,5 | 9.99852 | 0,4 | 44336.85 |
| . 0826 | . 08251 |  | . 99659 |  | . 91649 | 52,5 | - 99852 |  | 443.57 .47 |
| . 0827 | . 08261 |  | - 99658 |  | -91701 | 52,4 | - 9985 s |  | 444 18.10 |
| . 0828 | . 08271 |  | . 99657 |  | .91753 | 52,3 | . 9985 s |  | 44438.73 |
| . 0829 | .0828I |  | -99657 |  | .91806 | 52,3 | . 9985 I |  | 44459.35 |
| 0.0830 | 0.08290 | 10,0 | 0.99656 | 0,8 | 8.91858 | 52,2 | 9.99850 | 0,4 | 44519.98 |
| . 0831 | . 08300 |  | . 99655 |  | . 91910 | 52,1 | . 99850 |  | 44540.61 |
| . 0832 | . 08310 |  | . 99654 |  | . 91962 | 52,1 | . 99850 |  | 446 or. 23 |
| . 0833 | . 08320 |  | . 99653 |  | . 92014 | 52,0 | . 99849 |  | 446 21.86 |
| . 0834 | . 08330 |  | . 99652 |  | . 92066 | 52,0 | - 99849 |  | 44642.48 |
| 0.0835 | 0.08340 | 10,0 | 0.99652 | 0,8 | 8.92118 | 51,9 | 9.99848 | 0,4 | 44703.11 |
| . 0836 | . 08350 |  | . 99651 |  | . 92170 | 51,8 | . 99848 |  | 44723.74 |
| . 0837 | . 08360 |  | - 99650 |  | .92222 | 51,8 | - 99848 |  | 44744.36 |
| . 0838 | . 08370 |  | . 99649 |  | . 922274 | 51,7 | - 99847 |  | 44804.99 |
| . 0839 | . 08380 |  | . 99648 |  | . 92325 | 51,6 | - 99847 |  | 44825.62 |
| 0.0840 | 0.08390 | 10,0 | 0.99647 | 0,8 | 8.92377 | 51,6 | 9.99847 | 0,4 | 44846.24 |
| . 0841 | . 08400 |  | . 99647 |  | . 92428 | 51,5 | . 99846 |  | 44906.87 |
| . 0842 | . 08410 |  | - 99646 |  | . 92480 | 51,5 | - 99846 |  | 44927.50 |
| . 0843 | . 08420 |  | . 99645 |  | .9253I | 51,4 | . 99846 |  | 449 48. 12 |
| . 0844 | . 08430 |  | . 99644 |  | . 92583 | 51,3 | - 99845 |  | 45008.75 |
| 0.0845 | 0.08440 | 10,0 | 0.99643 | o,8 | 8.92634 | 51,3 | 9.99845 | 0,4 | 45029.38 |
| . 0846 | . 08450 |  | . 99642 |  | . 92685 | 51,2 | . 99844 |  | 45050.00 |
| . 0847 | . 08460 |  | . 99642 |  | . 92736 | 51,2 | - 99844 |  | 45110.63 |
| . 0848 | . 08470 |  | . 99641 |  | . 92788 | 51,1 | - 99844 |  | 45131.26 |
| . 0849 | . 08480 |  | . 99640 |  | . 92839 | 51,0 | . 99843 |  | 45151.88 |
| 0.0850 | 0.08490 | 10,0 | 0.99639 | 0,8 | 8.92890 | 151,0 | 9.99843 | 0,4 | 452 12.51 |
| $u$ | -i sinh iu | $\omega \mathrm{FF}^{\prime}$ | cosh iu | $\omega^{\text {F }}{ }^{\prime}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{Fo}^{\prime}$ | log cosh iu | $\omega \mathrm{Fo}^{\prime}$ | $u$ |

Circular Functions.

| $u$ | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0850 | 0.08490 | 10,0 | 0.99639 | 0,8 | 8.92890 | 51,0 | 9.99843 | 0,4 | $4^{\circ} 52^{\prime} 12.51$ |
| . 0851 | . 08500 |  | . 99638 | 0,8 | .9294I | 50,9 | . 99843 |  | 45233.14 |
| . 0852 | . 08510 |  | . 99637 | 0,9 | .92991 | 50,9 | . 99842 |  | 45253.76 |
| . 0853 | . 08520 |  | . 99636 |  | . 93042 | 50,8 | . 99842 |  | 45314.39 |
| . 0854 | . 08530 |  | . 99636 |  | . 93093 | 50,7 | . 9984 I |  | 45335.01 |
| 0.0855 | 0.08540 | 10,0 | 0.99635 | 0,9 | 8.93144 | 50,7 | 9.9984 I | 0,4 | 45355.64 |
| . 0856 | . 08550 |  | . 99634 |  | .93194 | 50,6 | . 99841 |  | 45416.27 |
| . 0857 | . 08560 |  | . 99633 |  | . 93245 | 50,6 | . 99840 |  | 45436.89 |
| . 0858 | . 08569 |  | . 99632 |  | . 93295 | 50,5 | . 99840 |  | 45457.52 |
| . 0859 | . 08579 |  | .9963I |  | . 93346 | 50,4 | . 99840 |  | 455 18.15 |
| 0.0860 | 0.08589 | 10,0 | 0.99630 | 0,9 | 8.93396 | 50,4 | 9.99839 | 0,4 | 45538.77 |
| .086I | . 08599 |  | . 99630 |  | . 93447 | 50,3 | . 99839 |  | 45559.40 |
| . 0862 | . 08609 |  | . 99629 |  | . 93497 | 50,3 | . 99838 |  | 45620.03 |
| . 0863 | .08619 |  | . 99628 |  | . 93547 | 50,2 | . 99838 |  | 45640.65 |
| . 0864 | . 08629 |  | . 99627 |  | . 93597 | 50, I | . 99838 |  | 457 OI. 28 |
| 0.0865 | 0.08639 | 10,0 | 0.99626 | 0,9 | 8.93647 | 50,1 | 9.99837 | 0,4 | 45721.91 |
| . 0866 | . 08649 |  | . 99625 |  | . 93697 | 50,0 | . 99837 |  | 45742.53 |
| . 0867 | . 08659 |  | . 99624 |  | . 93747 | 50,0 | . 99837 |  | 45803.16 |
| . 0868 | . 08669 |  | . 99624 |  | . 93797 | 49,9 | . 99836 |  | 45823.79 |
| . 0869 | . 08679 |  | . 99623 |  | . 93847 | 49,9 | . 99836 |  | $45844 \cdot 41$ |
| 0.0870 | 0.08689 | 10,0 | 0.99622 | 0,9 | 8.93897 | 49,8 | 9.99835 | 0,4 | 45905.04 |
| . 0871 | . 08699 | , | . 9962 I |  | . 93947 | 49,7 | . 99835 |  | 45925.66 |
| . 0872 | . 08709 |  | . 99620 |  | . 93997 | 49,7 | . 99835 |  | 45946.29 |
| . 0873 | . 08719 |  | .99619 |  | . 94046 | 49,6 | . 99834 |  | 50006.92 |
| . 0874 | . 08729 |  | . 99618 |  | . 94096 | 49,6 | . 99834 |  | 50027.54 |
| 0.0875 | 0.08739 | 10,0 | 0.99617 | 0,9 | 8.94145 | 49,5 | 9.99834 | 0,4 | 50048.17 |
| . 0876 | . 08749 |  | .99617 |  | . 94195 | 49,5 | . 99833 |  | 5 OI 08.80 |
| . 0877 | . 08759 |  | . 99616 |  | . 94244 | 49,4 | . 99833 |  | 5 OI 29.42 |
| . 0878 | . 08769 |  | .996I5 |  | . 94294 | 49,3 | . 99832 |  | 5 OI 50.05 |
| . 0879 | . 08779 |  | .99614 |  | . 94343 | 49,3 | . 99832 |  | 50210.68 |
| 0.0880 | 0.08789 | 10,0 | 0.99613 | 0,9 | 8.94392 | 49,2 | 9.99832 | 0,4 | 50231.30 |
| .088I | . 08799 |  | . 99612 |  | . 9444 | 49,2 | . 99831 |  | 5025 I .93 |
| . 0882 | . 08809 |  | .996II |  | .9449I | 49, I | .9983I |  | $\begin{array}{llll}5 & 03 & 12.56\end{array}$ |
| . 0883 | .08819 |  | .996io |  | . 94540 | 49, I | . 99830 |  | 50333.18 |
| . 0884 | . 08828 |  | .99610 |  | . 94589 | 49,0 | . 99830 |  | 503 53.8I |
| 0.0885 | 0.08838 | 10,0 | 0.99609 | 0,9 | 8.94638 | 48,9 | 9.99830 | 0,4 | 50414.44 |
| . 0886 | . 08848 |  | . 99608 |  | . 94687 | 48,9 | . 99829 |  | 50435.06 |
| . 0887 | . 08858 |  | . 99607 |  | . 94735 | 48,8 | . 99829 |  | 50455.69 |
| . 0888 | . 08868 |  | . 99606 |  | . 94784 | 48,8 | . 99829 |  | 505 16.3I |
| . 0889 | . 08878 |  | . 99605 |  | . 94833 | 48,7 | . 99828 |  | 50536.94 |
| 0.0890 | 0.08888 | 10,0 | 0.99604 | 0,9 | 8.94882 | 48,7 | 9.99828 | 0,4 | $505 \quad 57.57$ |
| .0891 | . 08898 |  | . 99603 |  | . 94930 | 48,6 | . 99827 |  | 50618.19 |
| . 0892 | . 08008 |  | . 99602 |  | . 94979 | 48,6 | . 99827 |  | 50638.82 |
| . 0893 | . 08918 |  | . 99602 |  | . 95027 | 48,5 | . 99827 |  | 50659.45 |
| . 0894 | . 08928 |  | .9960I |  | . 95076 | 48,4 | . 99826 |  | 50720.07 |
| 0.0895 | 0.08938 | 10,0 | 0.99600 | 0,9 | 8.95124 | 48,4 | 9.99826 | 0,4 | 50740.70 |
| . 0896 | . 08948 |  | . 99599 |  | . 95173 | 48,3 | . 99825 |  | 508 OI. 33 |
| . 0897 | . 08958 |  | . 99598 |  | . 9522 I | 48,3 | . 99825 |  | 50821.95 |
| .0898 | . 08968 |  | . 99597 |  | .95269 | 48,2 | . 99825 |  | $\begin{array}{llll}5 & 08 & 42.58 \\ 5 & 00 & 03.21\end{array}$ |
| . 0899 | . 08978 |  | . 99596 |  | .95317 | 48,2 | . 99824 |  | 50903.21 |
| 0.0900 | 0.08988 | 10,0 | 0.99595 | 0,9 | 8.95366 | 48, I | 9.99824 | 0,4 | 50923.83 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 10 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { c o s }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0900 | 0.08988 | 10,0 | 0.99595 | 0,9 | 8.95366 | 48,1 | 9.99824 | 0,4 | $5^{\circ} 099^{\prime} 23.83$ |
| . 0901 | . 08998 |  | . 99594 |  | . 95414 | 48, I | . 99823 |  | 50944.46 |
| . 0902 | . 09008 |  | . 99593 |  | . 95462 | 48,0 | . 99823 |  | 51005.09 |
| . 0903 | .09018 |  | . 99593 |  | .95510 | 48,0 | . 99823 |  | 5 10 25.71 |
| . 0904 | . 09028 |  | . 99592 |  | . 95558 | 47,9 | . 99822 |  | 51046.34 |
| 0.0905 | 0.09038 | 10,0 | 0.99591 | 0,9 | 8.95606 | 47,9 | 9.99822 | 0,4 | 5 II 06.96 |
| . 0906 | . 09048 |  | . 99590 |  | . 95653 | 47,8 | . 99822 |  | 5 II 27.59 |
| . 0907 | . 09058 |  | . 99589 |  | .95701 | 47,8 | . 99821 |  | 5 II 48.22 |
| . 0908 | . 09068 |  | . 99588 |  | . 95749 | 47,7 | . 99821 |  | 51208.84 |
| . 0909 | . 09077 |  | . 99587 |  | . 95797 | 47,6 | . 99820 |  | 51229.47 |
| 0.0910 | 0.09087 | 10,0 | 0.99586 | 0,9 | 8.95844 | 47,6 | 9.99820 | 0,4 | 51250.10 |
| . 0911 | . 09097 |  | . 99585 |  | . 95892 | 47,5 | . 99820 |  | 51310.72 |
| .0912 | .09107 |  | . 99584 |  | . 95939 | 47,5 | .99819 |  | 5 13 3I. 35 |
| .0913 | .09117 |  | . 99584 |  | . 95987 | 47,4 | .99819 |  | 5 I3 51.98 |
| . 0914 | . 09127 |  | . 99583 |  | . 96034 | 47,4 | .998I8 |  | 51412.60 |
| 0.0915 | 0.09137 | 10,0 | 0.99582 | 0,9 | 8.9608I | 47,3 | 9.99818 | 0,4 | 5 I4 33.23 |
| .0916 | . 09147 |  | .99581 |  | .96I29 | 47,3 | .99818 |  | 51453.86 |
| .0917 | . 09157 |  | . 99580 |  | .96176 | 47,2 | .99817 |  |  |
| . 0918 | . 09167 |  | . 99579 |  | .96223 | 47,2 | .99817 |  | 5 I5 35.11 |
| . 0919 | .09177 |  | . 99578 |  | . 96270 | 47, 1 | .99816 |  | 51555.74 |
| 0.0920 | 0.09187 | 10,0 | 0.99577 | 0,9 | 8.96317 | 47,1 | 9.99816 | 0,4 | 516 ı6.36 |
| .0921 | . 09197 |  | . 99576 |  | .96365 | 47,0 | .998i6 |  | $5 \begin{array}{llll}5 & 16 & 36.99\end{array}$ |
| . 0922 | . 09207 |  | . 99575 |  | .96412 | 47,0 | .99815 |  | 51657.62 |
| . 0923 | .09217 |  | . 99574 |  | . 96458 | 46,9 | . 99815 |  | $\begin{array}{lllll}5 & 17 & 18.24\end{array}$ |
| . 0924 | . 09227 |  | . 99573 |  | . 96505 | 46,9 | .998I4 |  | 51738.87 |
| 0.0925 | 0.09237 | 10,0 | 0.99572 | 0,9 | 8.96552 | 46,8 | 9.99814 | 0,4 | 51759.49 |
| . 0926 | . 09247 |  | . 99572 |  | . 96599 | 46,8 | .99814 |  | 51820.12 |
| . 0927 | .09257 |  | .9957I |  | . 96646 | 46,7 | .99813 |  | $5 \quad 1840.75$ |
| . 0928 | . 09267 | , | . 99570 |  | .96602 | 46,7 | .99813 |  | 51901.37 |
| . 0929 | . 09277 |  | . 99569 |  | . 96739 | 46,6 | . 99812 |  | 51922.00 |
| 0.0930 | 0.09287 | 10,0 | 0.99568 | 0,9 | 8.95786 | 46,6 | 9.99812 | 0,4 | 51942.63 |
| . 0931 | .09297 |  | . 99567 |  | . 96832 | 46,5 | .99812 |  | $\begin{array}{llll}5 & 20 & 03.25\end{array}$ |
| . 0932 | .09307 |  | . 99566 |  | . 96879 | 46,5 | .998II |  | 52023.88 |
| . 0933 | .09316 |  | . 99565 |  | . 96925 | 46,4 | .998II |  | 52044.5 I |
| . 0934 | . 09326 |  | . 99564 |  | . 96972 | 46,4 | .99810 |  | 52105.13 |
| 0.0935 | 0.09336 | 10,0 | 0.99563 | 0,9 | 8.97018 | 46,3 | 9.99810 | 0,4 | 52125.76 |
| . 0936 | . 09346 |  | . 99562 |  | . 97064 | 46,3 | .99809 |  | 5 21 46.39 |
| . 0937 | . 09356 |  | .9956I |  | .971 10 | 46,2 | . 99809 |  | 52207.01 |
| . 0938 | . 09366 |  | . 99560 |  | . 97157 | 46,2 | . 99809 |  | 52227.64 |
| . 0939 | . 09376 |  | -99559 |  | .97:203 | 46,1 | . 99808 |  | 52248.27 |
| 0.0940 | 0.09386 | 10,0 | 0.99559 | 0,9 | 8.97249 | 46, I | 9.99808 | 0,4 | $\begin{array}{llll}5 & 23 & 08.89\end{array}$ |
| . 0941 | .09396 |  | . 99558 |  | . 97295 | 46,0 | . 99807 |  | $\begin{array}{llll}5 & 23 & 29.52\end{array}$ |
| . 0942 | . 09406 |  | . 99557 |  | . 5734 I | 46,0 | . 99807 |  | 523 50.14 |
| . 0943 | .09416 |  | . 99556 |  | . 97387 | 45,9 | . 99807 |  |  |
| . 0944 | . 09426 |  | . 99555 |  | . 97433 | 45,9 | . 99806 |  | 52431.40 |
| 0.0945 | 0.09436 | 10,0 | 0.99554 | 0,9 | 8.97479 | 45,8 | 9.99806 | 0,4 |  |
| . 0946 | . 09446 |  | . 99553 |  | . 97524 | 45,8 | . 99805 |  | 52512.65 |
| . 0947 | . 09456 |  | . 99552 |  | . 97570 | 45,7 | .99805 |  | 52533.28 |
| . 0948 | . 09466 |  | . 99551 |  | .97616 | 45,7 | . 99805 |  | 52553.90 |
| . 0949 | .09476 |  | . 99550 |  | .9766I | 45,6 | . 99804 |  | 52614.53 |
| 0.0950 | 0.09486 | 10,0 | 0.99549 | 0,9 | 8.97707 | 45,6 | 9.99804 | 0,4 | 52635.16 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.0950 | 0.09486 | 10,0 | 0.99549 | 0,9 | 8.97707 | 45,6 | 9.99804 | 0,4 | $5^{\circ} 26^{\prime} 355^{\prime \prime} .16$ |
| . 095I | . 09496 |  | . 99548 | 0,9 | . 97753 | 45,5 | . 99803 |  | $\begin{array}{llll}5 & 2655.78\end{array}$ |
| . 0952 | . 09506 |  | . 99547 | 1,0 | . 97798 | 45,5 | . 99803 |  | 527 16.41 |
| . 0953 | .09516 |  | . 99546 |  | . 97844 | 45,4 | . 99802 |  | 52737.04 |
| . 0954 | . 09526 |  | . 99545 |  | . 97889 | 45,4 | .99802 |  | 52757.66 |
| 0.0955 | 0.09535 | 10,0 | 0.99544 | 1,0 | 8.97934 | 45,3 | 9.99802 | 0,4 | 52818.29 |
| . 0956 | . 09545 |  | . 99543 |  | . 97980 | 45,3 | . 99801 |  | 52838.92 |
| . 0957 | . 09555 |  | . 99542 |  | .98025 | 45,2 | . 99801 |  | $5 \begin{array}{llll}5 & 28 & 59.54\end{array}$ |
| . 0958 | . 09565 |  | .9954I |  | . 98070 | 45,2 | . 99800 |  | 529 20.17 |
| . 0959 | . 09575 |  | .9954I |  | 98II5 | 45, I | . 99800 |  | 52940.79 |
| 0.0960 | 0.09585 | 10,0 | 0.99540 | 1,0 | 8.98160 | 45, I | 9.99800 | 0,4 | 530 OI .42 |
| .096I | . 09595 |  | . 99539 |  | . 98205 | 45, I | . 99799 |  | 53022.05 |
| . 0962 | . 09605 |  | . 99538 |  | .9825I | 45,0 | . 99799 |  | 53042.67 |
| . 0963 | . 09615 |  | . 99537 |  | . 98295 | 45,0 | . 99798 |  | 53103.30 |
| . 0964 | . 09625 |  | . 99536 |  | . 98340 | 44,9 | . 99798 |  | 53123.93 |
| 0.0965 | 0.09635 | 10,0 | 0.99535 | 1,0 | 8.98385 | 44,9 | 9.99797 | 0,4 | 5 3I 44.55 |
| . 0966 | . 09645 |  | . 99534 |  | . 98430 | 44,8 | . 99797 |  | 53205.18 |
| . 0967 | . 09655 |  | . 99533 |  | . 98475 | 44,8 | . 99797 |  | 53225.81 |
| . 0968 | . 09665 |  | . 99532 |  | . 98520 | 44,7 | . 99796 |  | 53246.43 |
| . 0969 | . 09675 |  | .9953I |  | . 98564 | 44,7 | . 99796 |  | 53307.06 |
| 0.0970 | 0.09685 | 10,0 | 0.99530 | 1,0 | 8.98609 | 44,6 | 9.99795 | 0,4 | $\begin{array}{lll}5 & 33 & 27.69\end{array}$ |
| . 0971 | . 09695 |  | . 99529 |  | . 98554 | 44,6 | . 99795 |  | 53348.3 I |
| . 0972 | . 09705 |  | . 99528 |  | . 98698 | 44,5 | . 99795 |  | 53408.94 |
| . 0973 | . 09715 |  | . 99527 |  | . 98743 | 44,5 | . 99794 |  | 53429.57 |
| . 0974 | . 09725 |  | . 99526 |  | . 98787 | 44,4 | . 99794 |  | 53450.19 |
| 0.0975 | 0.09735 | 10,0 | 0.99525 | 1,0 | 8.98832 | 44,4 | 9.99793 | 0,4 | 53510.82 |
| . 0976 | . 09745 |  | . 99524 |  | . 98876 | 44,4 | . 99793 |  | 53531.45 |
| . 0977 | . 09754 |  | . 99523 |  | . 98920 | 44,3 | . 99792 |  | 53552.07 |
| . 0978 | .09764 |  | . 99522 |  | . 98965 | 44,3 | . 99792 |  | 53612.70 |
| . 0979 | . 09774 |  | .9952I |  | . 99009 | 44,2 | . 99792 |  | 53633.32 |
| 0.0980 | 0.09784 | 10,0 | 0.99520 | 1,0 | 8.99053 | 44,2 | 9.99791 | 0,4 |  |
| .0981 | . 09794 |  | .99519 |  | . 99097 | 44, I | . 99791 |  | 53714.58 |
| . 0982 | . 09804 |  | .99518 |  | .9914I | 44, I | . 99790 |  | 53735.20 |
| .0983 | .09814 |  | . 99517 |  | . 99185 | 44,0 | . 99790 |  | 53755.83 |
| . 0984 | . 09824 |  | . 99516 |  | . 99229 | 44,0 | . 99789 |  | 53816.46 |
| 0.0985 | 0.09834 | 10,0 | 0.99515 | 1,0 | 8.99273 | 43,9 | 9.99789 | 0,4 |  |
| . 0986 | . 09844 |  | . 99514 |  | . 99317 | 43,9 | . 99789 |  | $\begin{array}{lllllllllll}5 & 38 & 57.71\end{array}$ |
| . 0987 | . 09854 |  | .99513 |  | . 99361 | 43,9 | . 99788 |  | 53918.34 |
| . 0988 | . 09864 |  | . 99512 |  | . 99405 | 43,8 | . 99788 |  | 53938.96 |
| . 0989 | . 09874 |  | .995II |  | -99449 | 43,8 | . 99787 |  | 53959.59 |
| 0.0990 | 0.09884 | 10,0 | 0.99510 | I, 0 | 8.99493 | 43,7 | 9.99787 | 0,4 |  |
| .0991 | . 09894 |  | . 99509 |  | . 99536 | 43,7 | . 99786 |  | 54040.84 |
| . 0992 | . 09904 |  | . 99508 |  | . 99580 | 43,6 | . 99786 |  | 541101.47 |
| . 0993 | . 09914 |  | . 99507 |  | . 99624 | 43,6 | . 99786 |  | 54122.10 |
| . 0994 | . 09924 |  | . 99506 |  | . 99667 | 43,5 | . 99785 |  | 54142.72 |
| 0.0995 | 0.09934 | 10,0 | 0.99505 | I,O | 8.997II | 43,5 | 9.99785 | 0,4 | 54203.35 |
| . 0996 | . 09944 |  | . 99504 |  | . 99754 | 43,5 | . 99784 |  | 54223.97 |
| . 0997 | . 09953 |  | . 99503 |  | . 99798 | 43,4 | . 99784 |  | 54244.60 |
| . 0998 | . 09963 |  | . 99502 |  | .9984 | 43,4 | .99783 |  | $\begin{array}{lll}5 & 43 & 05.23 \\ 5 & 43 & 25.85\end{array}$ |
| . 0999 | . 09973 |  | .99501 |  | . 99884 | 43,3 | . 99783 |  | 54325.85 |
| 0. 1000 | 0.09983 | 10,0 | 0.99500 | 1,0 | 8.99928 | 43,3 | 9.99782 | 0,4 | 54346.48 |
| u | -isinhiu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | © $\mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.100 | 0.09983 | 99,5 | 0.99500 | 10,0 | 8.99928 | 432,8 | 9.99782 | 4,4 | $5^{\circ} 433^{\prime} 46^{\prime \prime} .48$ |
| . IOI | . 10083 | 99,5 | . 99490 | 10,1 | 9.00358 | 428,5 | . 99778 | 4,4 | 54712.75 |
| . 102 | . 10182 | 99,5 | . 99480 | 10,2 | . 00785 | 424,3 | . 99774 | 4,4 | 55039.01 |
| . 103 | . 10282 | 99,5 | . 99470 | 10,3 | . 01207 | 420,2 | . 99769 | 4,5 | 55405.28 |
| . 104 | . 10381 | 99,5 | .99460 | 10,4 | . 01625 | 416,1 | . 99765 | 4,5 | 557 3I. 54 |
| 0.105 | 0.1048I | 99,4 | 0.99449 | 10,5 | 9.02039 | 412,I | 9.99760 | 4,6 | 60057.80 |
| . 106 | . 10580 | 99,4 | . 99439 | 10,6 | . 02449 | 408,2 | . 99756 | 4,6 | 60424.07 |
| . 107 | . 10580 | 99,4 | . 99428 | 10,7 | . 02855 | 404,3 | . 99751 | 4,7 | 60750.33 |
| . 108 | . 10779 | 99,4 | . 99417 | 10,8 | . 03258 | 400,6 | . 99746 | 4,7 | 6 II 16.60 |
| . 109 | . 10878 | 99,4 | . 99407 | 10,9 | . 03657 | 396,9 | .9974I | 4,8 | 6 I4 42.86 |
| O. 110 | 0.10978 | 99,4 | 0.99396 | II,0 | 9.04052 | 393,2 | 9.99737 | 4,8 | 6 18 09.13 |
| . III | . 11077 | 99,4 | . 99385 | II, I | . 04443 | 389,6 | . 99732 | 4,8 | 6 21 35.39 |
| . 112 | . I I I 77 | 99,4 | . 99373 | II,2 | .0483I | 386, 1 | . 99727 | 4,9 | 62501.66 |
| . II3 | . 11276 | 99,4 | . 99362 | I I, 3 | . 05215 | 382,7 | . 99722 | 4,9 | 62827.92 |
| . II4 | . I I375 | 99,4 | .9935I | I I, 4 | . 05596 | 379,3 | . 99717 | 5,0 | 63154.19 |
| 0. 115 | O. II475 | 99,3 | 0.99339 | II,5 | 9.05974 | 376,0 | 9.99712 | 5,0 | 63520.45 |
| . 116 | . II574 | 99,3 | . 99328 | I 1,6 | . 06348 | 372,7 | . 99707 | 5, I | 63846.72 |
| . 117 | . 11673 | 99,3 | . 99316 | II,7 | .06719 | 369,5 | . 99702 | 5, I | 64212.98 |
| . II8 | . II773 | 99,3 | . 99305 | I I, 8 | . 07087 | 366,3 | . 99697 | 5, I | 64539.25 |
| . 119 | . 11872 | 99,3 | . 99293 | II,9 | . 07452 | 363,2 | . 99692 | 5,2 | 649 05.5I |
| 0.120 | O. 11971 | 99,3 | 0.9928 I | 12,0 | 9.07814 | 360,2 | 9.99687 | 5,2 | 6523 I .78 |
| . 121 | . 12070 | 99,3 | . 99269 | 12,I | .08173 | 357,2 | .9968I | 5,3 | 65558.04 |
| . 122 | . 12170 | 99,3 | . 99257 | 12,2 | . 08528 | 354,2 | . 99676 | 5,3 | 659 24.3I |
| . 123 | . 12269 | 99,2 | . 99245 | 12,3 | .0888I | 351,3 | . 99671 | 5,4 | 70250.57 |
| . 124 | . 12368 | 99,2 | . 99232 | 12,4 | .0923I | 348,4 | . 99665 | 5,4 | 70616.84 |
| 0.125 | 0.12467 | 99,2 | 0.99220 | 12,5 | 9.09578 | 345,6 | 9.99660 | 5,5 | 70943.10 |
| . 126 | . 12567 | 99,2 | . 99207 | 12,6 | . 09922 | 342,9 | . 99654 | 5,5 |  |
| . 127 | . I2666 | 99,2 | . 99195 | 12,7 | . 10264 | 340, 1 | . 99649 | 5,5 | $7 \quad 1635.63$ |
| . 128 | . 12765 | 99,2 | .99182 | 12,8 | . 10602 | 337,4 | . 99643 | 5,6 | 72001.90 |
| . 129 | . 12864 | 99,2 | .99169 | 12,9 | . 10938 | 334,8 | . 99638 | 5,6 | 723 28.16 |
| 0.130 | 0.12963 | 99,2 | 0.99156 | 13,0 | 9. 11272 | 332,2 | 9.99632 | 5,7 | 72654.42 |
| . 131 | . 13063 | 99,1 | . 99143 | 13, I | . 11603 | 329,6 | . 99626 | 5,7 | 73020.69 |
| . 132 | . 13162 | 99, I | .99130 | 13,2 | . I 193I | 327,1 | .99621 | 5,8 | 73346.95 |
| . I33 | . 13261 | 99, I | .99117 | 13,3 | . 12257 | 324,6 | .996I5 | 5,8 | 73713.22 |
| . 134 | . 13360 | 99, I | .99104 | I3,4 | . 12580 | 322,2 | . 99609 | 5,9 | 74039.48 |
| 0.135 | 0.13459 | 99, I | 0.99090 | 13,5 | 9.12901 | 319,7 | 9.99603 | 5,9 | 74405.75 |
| . I36 | . 13558 | 99, I | . 99077 | 13,6 | . I3220 | 317,4 | . 99597 | 5,9 | 74732.01 |
| . 137 | . 13657 | 99,1 | . 99063 | 13,7 | . 13536 | $3 \mathrm{I} 5,0$ | . 99591 | 6,0 | 75058.28 |
| . 138 | . 13756 | 99,0 | . 99049 | 13,8 | . 13850 | 312,7 | . 99585 | 6,0 | 75424.54 |
| . 139 | . 13855 | 99,0 | . 99036 | 13,9 | . 14162 | 310,4 | . 99579 | 6,1 | 75750.81 |
| 0.140 | 0.13954 | 99,0 | 0.99022 | 14,0 | 9.1447 I | 308,2 | 9.99573 | 6,1 | 8 O1 17.07 |
| . I4I | . I4053 | 99,0 | . 99008 | I4,I | . 14778 | 306,0 | . 99567 | 6,2 | 80443.34 |
| . 142 | . 14152 | 99,0 | . 98993 | 14,2 | . 15083 | 303,8 | . 99561 | 6,2 | 80809.60 |
| . 143 | . I425I | 99,0 | . 98979 | 14,3 | . 15385 | 301,6 | . 99554 | 6,3 | 8 II 35.87 |
| . 144 | . 14350 | 99,0 | .98965 | 14,4 | . 15686 | 299,5 | . 99548 | 6,3 | 8 I5 02.13 |
|  | 0.14449 | 99,0 | 0.98951 | 14,4 | 9. 15985 | 297,4 | 9.99542 | 6,3 | 81828.40 |
| . 146 | . 14548 | 98,9 | . 98936 | 14,5 | . 1628 I | 295,3 | . 99535 | 6,4 | 82154.66 |
| . 147 | . 14647 | 98,9 | .98921 | 14,6 | . 16575 | 293,3 | . 99529 | 6,4 | 82520.93 |
| . 148 | . 14746 | 98,9 | . 98907 | 14,7 | . 16868 | 291,3 | . 99523 | 6,5 | 82847.19 |
| . 149 | . 14845 | 98,9 | . 98892 | 14,8 | . 17158 | 289,3 | . 99516 | 6,5 | 832 I3.46 |
| 0.150 | 0.14944 | 98,9 | 0.98877 | 14,9 | 9. 17446 | 287,4 | 9.99510 | 6,6 | 83539.72 |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.150 | 0. 14944 | 98,9 | 0.98877 | 14,9 | 9.17446 | 287,4 | 9.99510 | 6,6 | $8^{\circ} 35^{\prime} 39.72$ |
| . 151 | . 15043 | 98,9 | . 98862 | 15,0 | . 17733 | 285,4 | . 99503 | 6,6 | 83905.99 |
| . 152 | . 15142 | 98,8 | . 98847 | J5,1 | . 18017 | 283,5 | . 99496 | 6,7 | 84232.25 |
| . 153 | . 15240 | 98,8 | . 98832 | 15,2 | . 18300 | 28I,6 | . 99490 | 6,7 | 84558.52 |
| . 154 | . 15339 | 98,8 | .988I7 | 15,3 | . 18580 | 279,8 | . 99483 | 6,7 | 84924.78 |
| 0.155 | 0. 15438 | 98,8 | 0.98801 | 15,4 | 9.18859 | 277,9 | 9.99476 | 6,8 | 85251.04 |
| . 156 | . 15537 | 98,8 | . 98786 | 15,5 | -.19136 | 276, 1 | . 99469 | 6,8 | 856 I7.3I |
| . 157 | . 15636 | 98,8 | . 98770 | 15,6 | . 19411 | 274,3 | . 99463 | 6,9 | 85943.57 |
| . 158 | . 15734 | 98,8 | . 98754 | 15,7 | . 19685 | 272,6 | . 99456 | 6,9 | 90309.84 |
| . 159 | . 55833 | 98,7 | . 98739 | I5,8 | . 19957 | 270,8 | . 99449 | 7,0 | 90636.10 |
| 0.160 | 0.15932 | 98,7 | 0.98723 | 15,9 | 9.20227 | 269, 1 | 9.99442 | 7,0 | 91002.37 |
| . 161 | . 1603 I | 98,7 | . 98707 | 16,0 | . 20495 | 267,4 | . 99435 | 7,1 | 91328.63 |
| . 162 | . 16129 | 98,7 | . 98691 | 16, I | . 20761 | 265,7 | . 99428 | 7,1 | 91654.90 |
| . 163 | . 16228 | 98,7 | . 98674 | 16,2 | . 21026 | 264, I | . 99420 | 7,1 | 92021.16 |
| . 164 | . 16327 | 98,7 | . 98658 | 16,3 | .21290 | 262,4 | . 99413 | 7,2 | 92347.43 |
| 0. 165 | 0.16425 | 98,6 | 0.98642 | 16,4 | 9.21551 | 260,8 | 9.99406 | 7,2 | 92713.69 |
| . 166 | . 16524 | 98,6 | . 98625 | 16,5 | .218II | 259,2 | . 99399 | 7,3 | 93039.96 |
| .167 | . 16622 | 98,6 | . 98609 | 16,6 | . 22070 | 257,6 | . 99392 | 7,3 | 93406.22 |
| . 168 | . 16721 | 98,6 | . 98592 | 16,7 | . 22326 | 256,1 | . 99384 | 7,4 | 93732.49 |
| .169 | . 16820 | 98,6 | . 98575 | 16,8 | . 22582 | 254,5 | . 99377 | 7,4 | 94058.75 |
| 0.170 | 0.16918 | 98,6 | 0.98558 | 16,9 | 9.22836 | 253,0 | 9.99369 | 7,5 | 94425.00 |
| . 171 | .17017 | 98,5 | . 98542 | 17,0 | . 23088 | 251,5 | . 99362 | 7,5 | 94751.28 |
| . 172 | . 17115 | 98,5 | . 98524 | 17,1 | . 23338 | 250,0 | . 99354 | 7,5 | 95117.55 |
| . 173 | . 17214 | 98,5 | . 98507 | 17,2 | . 23588 | 248,5 | . 99347 | 7,6 | 95443.81 |
| . 174 | . 17312 | 98,5 | .98490 | 17,3 | . 23836 | 247, I | . 99339 | 7,6 | 95810.08 |
| 0.175 | 0.17411 | 98,5 | 0.98473 | 17,4 | 9.24082 | 245,6 | 9.99332 | 7,7 | 10 or 36.34 |
| . 176 | . 17509 | 98,5 | . 98455 | 17,5 | . 24327 | 244,2 | . 99324 | 7,7 | 100502.61 |
| $\therefore 177$ | . I7608 | 98,4 | . 98438 | 17,6 | . 24570 | 242,8 | .99316 | 7,8 |  |
| . 178 | . 17706 | 98,4 | . 98420 | 17,7 | . 24812 | 241,4 | . 99308 | 7,8 | IO II 55.14 |
| . 179 | . 17805 | 98,4 | . 98402 | 17,8 | . 25053 | 240,0 | . 99300 | 7,9 | IO 1521.40 |
| 0.180 | 0.17903 | 98,4 | 0.98384 | 17,9 | 9.25292 | 238,7 | 9.99293 | 7,9 | 10 $18 \quad 47.67$ |
| . 181 | . 18001 | 98,4 | . 98366 | 18,0 | . 25530 | 237,3 | . 99285 | 7,9 | $\begin{array}{llll}10 & 22 & 13.93\end{array}$ |
| . 182 | . 18100 | 98,3 | . 98348 | 18,1 | . 25767 | 236,0 | . 99277 | 8,0 | 102540.19 |
| . 183 | . 18198 | 98,3 | . 98330 | 18,2 | . 26002 | 234,7 | .99269 | 8,0 | IO 2906.46 |
| . 184 | . 18296 | 98,3 | .98312 | 18,3 | . 26236 | 233,4 | .9926I | 8, I | IO $32 \quad 32.72$ |
| . 0185 | 0. 18395 | 98,3 | 0.98294 | 18,4 | 9.26469 | 232,I | 9.99253 | 8,I | 10 $35 \quad 58.99$ |
| . 186 | . 18493 | 98,3 | . 98275 | 18,5 | . 26701 | 230,8 | . 99244 | 8,2 | 10 3925.25 |
| . 187 | . 18591 | -98,3 | . 98257 | 18,6 | . 26931 | 229,5 | . 99236 | 8,2 | 104251.52 |
| . 188 | . 18689 | 98,2 | . 98238 | 18,7 | . 27160 | 228,3 | . 99228 | 8,3 | 10 4617.78 |
| . 189 | . 18788 | 98,2 | . 98219 | 18,8 | . 27387 | 227,0 | . 99220 | 8,3 | IO 4944.05 |
| 0.190 | 0.18886 | 98,2 | 0.98200 | 18,9 | 9.27614 | 225,8 | 9.992 I | 8,4 | 105310.31 |
| . 191 | . 18984 | 98,2 | .98181 | 19,0 | . 27839 | 224,6 | . 99203 | 8,4 | Io 5636.58 |
| . 192 | . 19082 | 98,2 | .98162 | 19,I | . 28063 | 223,4 | .99195 | 8,4 | II 0002.84 |
| . 193 | . 19180 | 98, 1 | .98143 | 19,2 | . 28286 | 222,2 | .99186 | 8,5 | $\text { II } 0329.1 \mathrm{I}$ |
| . 194 | . 19279 | 98,1 | .98124 | 19,3 | . 28507 | 221,0 | .99178 | 8,5 | II 0655.37 |
| 0.195 | 0.19377 | 98, 1 | 0.98105 | 19,4 | 9.28728 | 219,9 | 9.99169 | 8,6 | II 1021.64 |
| . 196 | . 19475 | 98, 1 | . 98085 | 19,5 | . 28947 | 218,7 | . 99160 | 8,6 | II I I3 47.90 |
| . 197 | . 19573 | 98, 1 | . 98066 | 19,6 | .29165 | 217,6 | .99152 | 8,7 |  |
| . 198 | . 19671 | 98,0 | . 98046 | 19,7 19,8 | . 29382 | 216,5 215,3 | .99143 | 8,7 8,8 | $\begin{array}{lll}\text { II } & 20 & 40.43 \\ \text { II } & 24 & 06.70\end{array}$ |
| . 199 | . 19769 | 98,0 | . 98026 | 19,8 | . 29598 | 215,3 | -99134 | 8,8 | II 2400.70 |
| 0.200 | 0. 19867 | 98,0 | 0.98007 | 19,9 | 9.29813 | 214,2 | 9.99126 | 8,8 | II 2732.96 |
| u | -i sinh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $100 \cosh$ iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega F_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.200 | 0. 19867 | 98,0 | 0.98007 | 19,9 | 9.29813 | 214,2 | 9.99126 | 8,8 | II ${ }^{\circ} 27^{\prime} 32.96$ |
| . 20I | . 19965 | 98,0 | . 97987 | 20,0 | . 30027 | 213, 1 | .99117 | 8,8 | II 3059.23 |
| . 202 | . 20063 | 98,0 | . 97967 | 20,1 | . 30239 | 212, I | .99108 | 8,9 | II 3425.49 |
| . 203 | . 2016I | 97,9 | . 97947 | 20,2 | -3045I | 211,0 | . 99099 | 8,9 | II 3751.76 |
| . 204 | . 20259 | 97,9 | . 97926 | 20,3 | . 3066 I | 209,9 | . 99090 | 9,0 | II 4118.02 |
| 0.205 | 0.20357 | 97,9 | 0.97906 | 20,4 | 9.30871 | 208,9 | 9.99081 | 9,0 | II 4444.29 |
| . 206 | . 20455 | 97,9 | . 97886 | 20,5 | . 31079 | 207,8 | . 99072 | 9,1 | II 4810.55 |
| . 207 | . 20552 | 97,9 | . 97865 | 20,6 | . 31286 | 206,8 | . 99063 | 9, | II 5136.8 i |
| . 208 | . 20650 | 97,8 | . 97845 | 20,7 | . 31493 | 205,8 | . 99054 | 9,2 | II 5503.08 |
| . 209 | . 20748 | 97,8 | . 97824 | 20,7 | . 31698 | 204,8 | . 99044 | 9,2 | II 5829.34 |
| 0.210 | 0.20846 | 97,8 | 0.97803 | 20,8 | 9.31902 | 203,8 | 9.99035 | 9,3 | 12 or 55.6 I |
| . 211 | . 20944 | 97,8 | . 97782 | 20,9 | . 32106 | 202,8 | . 99026 | 9,3 | 1205121.87 |
| . 212 | . 21042 | 97,8 | .9776I | 21,0 | . 32308 | 201,8 | .99017 | 9,3 | 120848.14 |
| . 213 | . 21 139 | 97,7 | . 97740 | 2I, I | - 32509 | 200,8 | . 99007 | 9,4 | $\begin{array}{llll}12 & 12 & 14.40\end{array}$ |
| . 214 | . 21237 | 97,7 | . 97719 | 21,2 | . 32709 | 199,8 | . 98998 | 9,4 | 121540.67 |
| 0.215 | 0.21335 | 97,7 | 0.97698 | 21,3 | 9.32909 | 198,9 | 9.98988 | 9,5 | 121906.93 |
| . 216 | . 21432 | 97,7 | . 97676 | 2I,4 | . 33107 | 197,9 | . 98979 | 9,5 | 122233.20 |
| .217 | . 21530 | 97,7 | . 97655 | 21,5 | . 33305 | 197,0 | . 98969 | 9,6 | 122559.46 |
| . 218 | . 21628 | 97,6 | . 97633 | 21,6 | . 33501 | 196,0 | . 98960 | 9,6 | 122925.73 |
| . 219 | . 21725 | 97,6 | . 97612 | 21,7 | . 33697 | 195, I | . 98950 | 9,7 | 123251.99 |
| 0.220 | 0.21823 | 97,6 | 0.97590 | 21,8 | 9.33891 | 194,2 | 9.98940 | 9,7 | 123618.26 |
| . 221 | .21921 | 97,6 | . 97568 | 21,9 | . 34085 | 193,3 | .9893I | 9,8 | 123944.52 |
| . 222 | . 22018 | 97,5 | . 97546 | 22,0 | - 34278 | 192,4 | .9892I | 9,8 | 124310.79 |
| .223 | .22116 | 97,5 | . 97524 | 22,1 | . 34470 | 191,5 | .9891 I | 9,8 | 124637.05 |
| . 224 | . 22213 | 97,5 | . 97502 | 22,2 | . 34661 | 190,6 | .98901 | 9,9 | $12 \quad 50 \quad 03.32$ |
| 0.225 | 0.223 II | 97,5 | 0.97479 | 22,3 | 9.34851 | 189,8 | 9.98891 | 9,9 | 1253129.58 |
| . 226 | . 22408 | 97,5 | . 97457 | 22,4 | . 3504 I | 188,9 | .9888I | 10,0 | 125655.85 |
| . 227 | . 22506 | 97,4 | . 97435 | 22,5 | . 35229 | 188,0 | .9887I | 10,0 | 130022.11 |
| . 228 | . 22603 | 97,4 | .97412 | 22,6 | -35417 | 187,2 | .9886I | 10,1 | 130348.38 |
| . 229 | . 22700 | 97,4 | . 97389 | 22,7 | . 35603 | 186,3 | . 98851 | 10,1 | I3 0714.64 |
| 0.230 | 0.22798 | 97,4 | 0.97367 | 22,8 | 9.35789 | 185,5 | 9.98841 | 10,2 | 131040.91 |
| . 231 | . 22895 | 97,3 | . 97344 | 22,9 | . 35974 | 184,7 | . 98831 | 10,2 | 131407.17 |
| . 232 | . 22992 | 97,3 | .9732I | 23,0 | -36158 | 183,8 | . 98821 | 10,3 | 13 I7 33.44 |
| . 233 | . 23090 | 97,3 | . 97298 | 23,1 | . 36342 | 183,0 | .98810 | 10,3 | I3 2059.70 |
| . 234 | . 23187 | 97,3 | . 97275 | 23,2 | . 36525 | 182,2 | . 98800 | 10,4 | $13 \quad 2425.96$ |
| 0.235 | 0.23284 | 97,3 | 0.97251 | 23,3 | 9.36706 | 181,4 | 9.98790 | 10,4 | 1312752.23 |
| . 236 | . 23382 | 97,2 | . 97228 | 23,4 | . 36887 | 180,6 | . 98779 | 10,4 | 13 31 18.49 |
| . 237 | . 23479 | 97,2 | . 97205 | 23,5 | - 37068 | 179,8 | . 98769 | 10,5 | I3 3444.76 |
| . 238 | . 23576 | 97,2 | .97181 | 23,6 | - 37247 | I79,0 | . 98758 | 10,5 | 1338 II. 02 |
| . 239 | . 23673 | 97,2 | .97I58 | 23,7 | . 37426 | 178,2 | . 98748 | 10,6 | I3 4137.29. |
| 0.240 | 0.23770 | 97, I | 0.97134 | 23,8 | 9.37603 | 177,5 | 9.98737 | 10,6 | 134503.55 |
| . 241 | . 23867 | 97, I | . 97110 | 23,9 | . 37780 | 176,7 | . 98726 | 10,7 | I3 4829.82 |
| . 242 | . 23964 | 97, 1 | . 97086 | 24,0 | . 37957 | 175,9 | . 98716 | 10,7 | 13 51 56.08 |
| .243 | . 24062 | 97, I | . 97062 | 24,1 | . 38132 | 175,2 | . 98705 | 10,8 | I3 5522.35 |
| . 244 | . 24159 | 97,0 | . 97038 | 24,2 | . 38307 | 174,4 | . 98694 | 10,8 | I3 5848.61 |
| 0.245 | 0.24256 | 97,0 | 0.97014 | 24,3 | 9.3848 I | 173,7 | 9.98683 | 10,9 | $14 \quad 0214.88$ |
| . 246 | . 24353 | 97,0 | . 96989 | 24,4 | . 38655 | 173,0 | . 98672 | 10,9 | 14054 I .14 |
| . 247 | . 24450 | 97,0 | . 96965 | 24,4 | . 38827 | I72,2 | . 98662 | I I,O | 140907.41 |
| . 248 | . 24547 | 96,9 | . 96941 | 24,5 | - 38999 | 171,5 | .9865I | I I, 0 | $\begin{array}{llll}14 & 12 & 33.67\end{array}$ |
| . 249 | . 24643 | 96,9 | .96916 | 24,6 | . 39170 | 170,8 | . 98640 | II,O | 1415159.94 |
| 0.250 | 0.24740 | 96,9 | 0.96891 | 24,7 | 9.3934 I | 170, I | 9.98528 | II, I | $\begin{array}{lll}14 & 19 & 26.20\end{array}$ |
| u | -i sinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | 10 sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh$ iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| 4 | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 008 u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.250 | 0.24740 | 96,9 | 0.96891 | 24,7 | 9.39341 | 170, 1 | 9.98628 | II,I | $14{ }^{\circ} 19 \times 26^{\prime \prime} 20$ |
| .25I | . 24837 | 96,9 | . 96866 | 24,8 | . 39510 | 169,4 | . 98617 | II, I | $14 \quad 22 \quad 52.47$ |
| . 252 | . 24934 | 96,8 | . 96842 | 24,9 | . 39679 | 168,7 | . 98606 | II,2 | $14 \quad 2618.73$ |
| . 253 | . 2503 I | 96,8 | .96817 | 25,0 | - 39848 | 168,0 | . 98595 | II,2 | 142945.00 |
| . 254 | .25128 | 96,8 | . 96792 | 25, I | . 40015 | 167,3 | . 98584 | II,3 | 1433 II. 26 |
| 0.255 | 0.25225 | 96,8 | 0.96766 | 25,2 | 9.40182 | 166,6 | 9.98572 | II,3 | 143637.53 |
| . 256 | . 25321 | 96,7 | .96741 | 25,3 | . 40349 | 165,9 | . 98561 | II,4 | 144003.79 |
| . 257 | . 25418 | 96,7 | . 96716 | 25,4 | . 40514 | 165,2 | . 98550 | II,4 | 144330.06 |
| . 258 | . 25515 | 96,7 | . 96690 | 25,5 | . 40679 | 164,6 | . 98538 | II,5 | 144656.32 |
| . 259 | .256II | 96,7 | .96665 | 25,6 | . 40843 | 163,9 | . 98527 | 11,5 | 145022.58 |
| 0.260 | 0.25708 | 96,6 | 0.96639 | 25,7 | 9.41007 | 163,3 | 9.98515 | II, 6 | $14 \quad 5348.85$ |
| . 261 | . 25805 | 96,6 | . 966I3 | 25,8 | . 41170 | 162,6 | . 98504 | II,6 | 145715.11 |
| . 262 | . 25901 | 96,6 | . 96587 | 25,9 | .41332 | 162,0 | . 98492 | II,6 | 150041.38 |
| . 263 | . 25998 | 96,6 | .96561 | 26,0 | . 41494 | 161,3 | . 98480 | II,7 | 150407.64 |
| . 264 | . 26094 | 96,5 | . 96535 | 26, I | .41655 | 160,7 | .98469 | II,7 | 150733.91 |
| 0.265 | 0.26191 | 96,5 | 0.96509 | 26,2 | 9.41815 | 160,0 | 9.98457 | II, 8 | I5 II 00.17 |
| . 266 | . 26287 | 96,5 | . 96483 | 26,3 | .41975 | 159,4 | . 98445 | II,8 | 151426.44 |
| . 267 | . 26384 | 96,5 | . 96457 | 26,4 | . 42134 | 158,8 | . 98433 | II,9 | 151752.70 |
| . 268 | . 26480 | 96,4 | . 96430 | 26,5 | . 42292 | 158,2 | . 9842 I | I 1,9 | 15 21 18.97 |
| . 269 | . 26577 | 96,4 | . 96404 | 26,6 | . 42450 | 157,5 | . 98409 | 12,0 | $15 \quad 2445.23$ |
| 0.270 | 0.26673 | 96,4 | 0.96377 | 26,7 | 9.42607 | 156,9 | 9.98397 | 12,0 | $15 \quad 28$ II. 50 |
| . 271 | . 26770 | 96,4 | . 96350 | 26,8 | . 42764 | 156,3 | . 98385 | 12,I | 15 31 37.76 |
| . 272 | . 26866 | 96,3 | . 96324 | 26,9 | . 42920 | 155,7 | . 98373 | 12,I | 153504.03 |
| . 273 | . 26962 | 96,3 | . 96297 | 27,0 | . 43075 | I55, I | .9836I | 12,2 | 153830.29 |
| . 274 | . 27058 | 96,3 | . 96270 | 27,1 | . 43230 | 154,5 | . 98349 | 12,2 | I5 4I 56.56 |
| 0.275 | 0.27155 | 96,2 | 0.96243 | 27,2 | 9.43384 | I 53,9 | 9.98337 | 12,3 | $1545 \quad 22.82$ |
| . 276 | . 2725I | 96,2 | . 96215 | 27,3 | . 43538 | 153,3 | . 98324 | 12,3 | I5 4849.09 |
| :277 | . 27347 | 96,2 | .96188 | 27,3 | . 4369 I | 152,8 | .98312 | 12,3 | $15 \quad 5215.35$ |
| . 278 | . 27443 | 96,2 | .9616I | 27,4 | . 43844 | I52,2 | . 98300 | 12,4 | 155541.62 |
| . 279 | . 27539 | 96, 1 | .96I33 | 27,5 | . 43996 | 151,6 | . 98287 | 12,4 | I5 5907.88 |
| 0.280 | 0.27636 | 96, 1 | 0.96106 | 27,6 | 9.44147 | 151,0 | 9.98275 | 12,5 | 160234.15 |
| .281 | . 27732 | 96, I | . 96078 | 27,7 | . 44298 | 150,5 | . 98262 | 12,5 | 160600.41 |
| . 282 | . 27828 | 96, | . 96050 | 27,8 | . 44448 | 149,9 | . 98250 | 12,6 | 160926.68 |
| .283 | . 27924 | 96,0 | . 96022 | 27,9 | . 44597 | 149,3 | . 98237 | 12,6 | 161252.94 |
| . 284 | . 28020 | 96,0 | . 95994 | 28,0 | . 44746 | 148,8 | . 98225 | 12,7 | 16 16 19.20 |
| 0.285 | 0.28116 | 96,0 | 0.95966 | 28,1 | 9.44895 | 148,2 | 9.98212 | 12,7 | 16 19 45.47 |
| . 286 | . 28212 | 95,9 | . 95938 | 28,2 | . 45043 | 147,7 | .98199 | 12,8 | $16 \quad 2311.73$ |
| . 287 | . 28308 | 95,9 | . 95910 | 28,3 | . 45190 | 147, 1 | .98186 | 12,8 | 162638.00 |
| . 288 | . 28404 | 95,9 | .9588I | 28,4 | . 45337 | 146,6 | .98173 | 12,9 | 163004.26 |
| . 289 | . 28499 | 95,9 | . 95853 | 28,5 | . 45484 | 146, 1 | .9816I | 12,9 | I6 3330.53 |
| 0.290 | 0.28595 | 95,8 | 0.95824 | 28,6 | 9.45629 | 145,5 | 9.98148 | 13,0 | 163656.79 |
| . 291 | . 28691 | 95,8 | . 95796 | 28,7 | . 45775 | I45,0 | .98135 | I 3,0 | 164023.06 |
| . 292 | . 28787 | 95,8 | . 95767 | 28,8 | . 45919 | 144,5 | .98122 | 13,1 | 164349.32 |
| . 293 | . 28883 | 95,7 | . 95738 | 28,9 | . 46064 | 144,0 | .98109 | 13,1 | 164715.59 |
| . 294 | . 28978 | 95,7 | . 95709 | 29,0 | . 46207 | 143,4 | . 98095 | 13,1 | 165041.85 |
| 0.295 | 0.29074 | 95,7 | 0.95680 | 29,1 | 9.46350 | 142,9 | 9.98082 | 13,2 | 165408.12 |
| . 296 | . 29170 | 95,7 | .95651 | 29,2 | . 46493 | 142,4 | . 98069 | 13,2 | 165734.38 |
| .297 | . 29265 | 95,6 | . 95622 | 29,3 | $.46635$ | 141,9 | $.98056$ | 13,3 | $\text { I7 OI } 00.65$ |
| . 298 | . 29361 | 95,6 | . 95593 | 29,4 29,5 | . 46777 | 141,4 140,9 | . 98042 | I 3,3 I 3,4 | $\begin{array}{llll}17 & 04 & 26.91 \\ \text { I7 } & 07 & 53.18\end{array}$ |
| . 299 | . 29456 | 95,6 | -95563 | 29,5 | . 46918 | 140,9 | .98029 | 13,4 | I7 0753.18 |
| 0.300 | 0.29552 | 95,5 | 0.95534 | 29,6 | 9.47059 | I40,4 | 9.98016 | 13,4 | I7 II 19.44 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | 10 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \sin \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.300 | 0.29552 | 95,5 | 0.95534 | 29,6 | 9.47059 | 140,4 | 9.98016 | I3,4 | 17 ${ }^{\circ} 11 \times 19.44$ |
| . 301 | . 29648 | 95,5 | . 95504 | 29,6 | . 47199 | 139,9 | . 98002 | 13,5 | 171445.71 |
| - 302 | . 29743 | 95,5 | . 95474 | 29,7 | . 47339 | 139,4 | . 97989 | 13,5 | 171811.97 |
| . 303 | . 29838 | 95,4 | . 95445 | 29,8 | . 47478 | 138,9 | . 97975 | 13,6 | I7 2138.24 |
| . 304 | . 29934 | 95,4 | . 95415 | 29,9 | . 47616 | I 38,4 | . 97962 | 13,6 | 172504.50 |
| 0.305 | 0.30029 | 95,4 | 0.95385 | 30,0 | 9.47755 | 137,9 | 9.97948 | 13,7 | $\begin{array}{llll}17 & 28 & 30.77\end{array}$ |
| . 306 | . 30125 | 95,4 | . 95355 | 30,1 | . 47892 | 1 37,5 | . 97934 | 13,7 | 173157.03 |
| . 307 | . 30220 | 95,3 | -95324 | 30,2 | . 48029 | ${ }^{1} 37,0$ | . 97920 | I3,8 |  |
| . 308 | . 30315 | 95,3 | . 95294 | 30,3 | .48166 | 136,5 | . 97907 | I3,8 | $17 \quad 3849.56$ |
| . 309 | . 304 II | 95,3 | . 95264 | 30,4 | . 48303 | 136,0 | . 97893 | I 3,9 | I7 4215.83 |
| 0.310 | 0.30506 | 95,2 | 0.95233 | 30,5 | 9.48438 | 135,6 | 9.97879 | 13,9 | I7 4542.09 |
| . 3 II | . 30601 | 95,2 | . 95203 | 30,6 | . 48574 | 135, 1 | . 97865 | 14,0 | 174908.35 |
| -312 | . 30696 | 95,2 | .95172 | 30,7 | . 48709 | 134,7 | . 97851 | 14,0 | 175234.62 |
| . 313 | . 30791 | 95, 1 | .9514I | 30,8 | . 48843 | 134,2 | . 97837 | 14,I | 175600.88 |
| . 314 | . 30887 | 95, I | .95III | 30,9 | . 48977 | 133,7 | . 97823 | I4, I | 175927.15 |
| 0.315 | 0.30982 | 95,1 | 0.95080 | 31,0 | 9.49110 | I 33,3 | 9.97809 | 14,2 | 180253.4 I |
| . 316 | . 31077 | 95,0 | . 95049 | 31,1 | . 49244 | 132,8 | . 97795 | 14,2 | 180619.68 |
| . 317 | . 31172 | 95,0 | . 95017 | 3I, 2 | . 49376 | 132,4 | . 97780 | 14,2 | 180945.94 |
| . 318 | . 31267 | 95,0 | . 94986 | 3r,3 | . 49508 | 131,9 | . 97766 | 14,3 | I8 1312.21 |
| . 319 | . 31362 | 95,0 | . 94955 | 31,4 | . 49640 | I3I,5 | . 97752 | I4,3 | I8 I6 38.47 |
| 0.320 | 0.31457 | 94,9 | 0.94924 | 31,5 | 9.49771 | I3I, 1 | 9.97737 | 14,4 | $\begin{array}{llll}18 & 20 & 04.74\end{array}$ |
| . 321 | . 31552 | 94,9 | . 94892 | 31,6 | . 49902 | 130,6 | . 97723 | 14,4 | $18 \quad 23 \quad 31.00$ |
| . 322 | . 31646 | 94,9 | . 94860 | 31,6 | . 50032 | I30,2 | . 97709 | 14.5 | 18 2657.27 |
| . 323 | . 31741 | 94,8 | . 94829 | 31,7 | . 50162 | 129,7 | . 97694 | 14,5 | $18 \quad 3023.53$ |
| . 324 | .31836 | 94,8 | . 94797 | 31,8 | . 50292 | 129,3 | . 97679 | 14,6 | I8 3349.80 |
| 0.325 | 0.31931 | 94,8 | 0.94765 | 31,9 | 9.5042 I | 128,9 | 9.97665 | 14,6 | $18 \quad 37$ 16.06 |
| . 326 | . 32026 | 94,7 | . 94733 | 32,0 | . 50550 | 128,5 | . 97650 | 14,7 | 184042.33 |
| . 327 | . 32120 | 94,7 | . 94701 | 32,I | . 50678 | 128,0 | . 97635 | 14,7 | 184408.59 |
| . 328 | . 32215 | 94,7 | . 94669 | 32,2 | . 50806 | 127,6 | . 97621 | 14,8 | $18 \quad 4734.86$ |
| . 329 | . 32310 | 94,6 | . 94637 | 32,3 | . 50933 | 127,2 | . 97606 | 14,8 | 185 I OI. 12 |
| 0.330 | 0.32404 | 94,6 | 0.94604 | 32,4 | 9.51060 | 126,8 | 9.97591 | I4,9 | $18 \quad 5427.39$ |
| . 331 | . 32499 | 94,6 | . 94572 | 32,5 | . 51187 | 126,4 | . 97576 | I4,9 | $18 \quad 5753.65$ |
| . 332 | . 32593 | 94,5 | . 94539 | 32,6 | . 51313 | 126,0 | . 9756 I | 15,0 | 19 OI 19.92 |
| . 333 | . 32688 | 94,5 | . 94507 | 32,7 | . 51439 | 125,6 | . 97546 | 15,0 | 190446.18 |
| . 334 | . 32782 | 94,5 | . 94474 | 32,8 | . 51564 | 125,2 | . 9753 I | 15, I | 190812.45 |
| 0.335 | 0.32877 | 94,4 | 0.94441 | 32,9 | 9.51689 | 124,8 | 9.97516 | 15,I | 19 II 38.71 |
| . 336 | . 32971 | 94,4 | . 94408 | 33,0 | . 51814 | 124,4 | . 97501 | I5,2 | 19 15 04.97 |
| . 337 | . 33066 | 94,4 | . 94375 | 33,1 | . 51938 | 124,0 | . 97486 | I5,2 | 19 I8 31.24 |
| . 338 | . 33160 | 94,3 | . 94342 | 33,2 | . 52062 | 123,6 | . 97470 | 15,3 | 19 21 57.50 |
| . 339 | . 33254 | 94,3 | . 94309 | 33,3 | . 52185 | 123,2 | . 97455 | 15,3 | 192523.77 |
| 0.340 | 0.33349 | 94,3 | 0.94275 | 33,3 | 9.52308 | 122,8 | 9.97440 | 15,4 | 192850.03 |
| . 34 I | . 33443 | 94,2 | . 94242 | 33,4 | . 52430 | 122,4 | . 97424 | I5,4 | 1932 I 6.30 |
| . 342 | . 33537 | 94,2 | . 94209 | 33,5 | . 52553 | 122,0 | . 97409 | 15,5 | 19 3542.56 |
| - 343 | . 33631 | 94,2 | . 94175 | 33,6 | . 52674 | 121,6 | . 97394 | 15,5 | 193908.83 |
| . 344 | . 33726 | 94, I | .94I4I | 33,7 | . 52796 | 121,2 | . 97378 | 15,6 | 194235.09 |
| 0.345 | 0.33820 | 94, I | 0.94108 | 33,8 | 9.52917 | 120,8 | 9.97362 | 15,6 | 1946 O1. 36 |
| . 346 | . 33914 | 94, I | . 94074 | 33,9 | . 53038 | 120,5 | . 97347 | 15,7 | 194927.62 |
| . 347 | . 34008 | 94,0 | . 94040 | 34,0 | . 53158 | 120, I | . 9733 I | 15,7 | 195253.89 |
| . 348 | . 34102 | 94,0 | . 94006 | 34,1 | . 53278 | II9,7 | . 97315 | 15,8 | 1956 |
| . 349 | . 34196 | 94,0 | . 93972 | 34,2 | . 53397 | 1 19,3 | . 97300 | 15,8 | I9 5946.42 |
| 0.350 | 0.34290 | 93,9 | 0.93937 | 34,3 | 9.53516 | I 19,0 | 9.97284 | I 5,9 | $20 \quad 0312.68$ |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

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Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.350 | 0.34290 | 93,9 | 0.93937 | 34.3 | 9.53516 | I 19,0 | 9.97284 | 15,9 | $20^{\circ} 033^{\prime} 12.06$ |
| . 351 | . 34384 | 93,9 | . 93903 | 34,4 | . 53635 | I 18,6 | . 97268 | I 5,9 | 200638.95 |
| . 352 | . 34478 | 93,9 | . 93869 | 34,5 | . 53754 | 1 18,2 | . 97252 | 16,0 | 201005.21 |
| - 353 | . 34571 | 93,8 | . 93834 | 34,6 | . 53872 | I 17,9 | . 97236 | 16,0 | 20 I3 31.48 |
| - 354 | . 34665 | 93,8 | . 93799 | 34,7 | . 53989 | I 17,5 | . 97220 | 16, 1 | 201657.74 |
| 0.355 | 0.34759 | 93,8 | 0.93765 | 34,8 | 9.54107 | II7,2 | 9.97204 | 16,1 | 202024.01 |
| . 356 | . 34853 | 93,7 | . 93730 | 34,9 | . 54224 | I 16,8 | . 97188 | 16,1 | 202350.27 |
| . 357 | . 34946 | 93,7 | . 93695 | 34,9 | . 54340 | I 16,4 | .97172 | 16,2 | 202716.54 |
| - 358 | . 35040 | 93,7 | . 93660 | 35,0 | . 54457 | II6, I | .97I 55 | 16,2 | 203042.80 |
| - 359 | . 35134 | 93,6 | . 93625 | 35, I | - 54573 | I 15,7 | . 97139 | 16,3 | 203409.07 |
| 0.360 | 0.35227 | 93,6 | 0.93590 | 35,2 | 9.54688 | II 5,4 | 9.97123 | 16,3 | $2037 \quad 35.33$ |
| . 361 | . 3532 I | 93,6 | . 93554 | 35,3 | . 54803 | I I 5,0 | . 97106 | 16,4 | 2041 OI. 60 |
| . 362 | . 35415 | 93,5 | .93519 | 35,4 | . 54918 | II4,7 | . 97090 | 16,4 | 204427.86 |
| . 363 | . 35508 | 93,5 | . 93484 | 35,5 | . 55033 | 114,3 | . 97074 | 16,5 | 204754.12 |
| . 364 | .35601 | 93,4 | . 93448 | 35,6 | . 55147 | II 4,0 | . 97057 | 16,5 | 205120.39 |
| 0.365 | 0.35695 | 93,4 | 0.93412 | 35,7 | 9.5526I | 113,7 | 9.97040 | 16,6 | 205446.65 |
| . 366 | . 35788 | 93,4 | . 93377 | 35,8 | . 55374 | 113,3 | . 97024 | 16,6 | $20 \quad 5812.92$ |
| . 367 | . 35882 | 93,3 | .9334I | 35,9 | - 55487 | 113,0 | . 97007 | 16,7 | 21 OI 39.18 |
| . 368 | . 35975 | 93,3 | . 93305 | 36,0 | . 55600 | II2,6 | . 96990 | 16,7 | 210505.45 |
| . 369 | . 36068 | 93,3 | . 93269 | 36,1 | . 55713 | 112,3 | . 96974 | 16,8 | 210831.71 |
| 0.370 | 0.36162 | 93,2 | 0.93233 | 36,2 | 9.55825 | I 12,0 | 9.96957 | 16,8 | 21 II 57.98 |
| . 371 | . 36255 | 93,2 | . 93197 | 36,3 | . 55937 | II I, 6 | . 96940 | 16,9 | 2 I I5 24.24 |
| . 372 | . 36348 | 93,2 | .93160 | 36,3 | . 56048 | III, 3 | . 96923 | 16,9 | 2 I 18 50.51 |
| . 373 | . 3644 I | 93, 1 | .93124 | 36,4 | . 56159 | I I I, 0 | . 96906 | 17,0 | 212216.77 |
| . 374 | . 36534 | 93, I | . 93087 | 36,5 | . 56270 | I 10,7 | . 96889 | 17,0 | 21 2543.04 |
| 0.375 | 0.36627 | 93,1 | 0.93051 | 36,6 | 9.56380 | 1 10,3 | 9.96872 | 17,I | 212909.30 |
| . 376 | . 36720 | 93,0 | . 93014 | 36,7 | . 56491 | I 10,0 | . 95855 | 17,I | 213235.57 |
| :377 | . 36813 | 93,0 | . 92977 | 36,8 | . 56600 | 109,7 | . 96838 | 17,2 | 21 3601.83 |
| . 378 | . 36906 | 92,9 | . 92940 | 36,9 | . 56710 | 109,4 | . 96820 | 17,2 | 21 3928.10 |
| - 379 | . 36999 | 92,9 | . 92904 | 37,0 | . 56819 | 109,0 | . 96803 | 17,3 | 214254.36 |
| 0.380 | 0.37092 | 92,9 | 0.92866 | 37, I | 9.56928 | 108,7 | 9.96786 | 17,3 | 214620.63 |
| . 381 | . 37185 | 92,8 | . 92829 | 37,2 | . 57037 | 108,4 | . 96769 | I7,4 | 21 4946.89 |
| . 382 | . 37278 | 92,8 | . 92792 | 37,3 | . 57145 | 108, 1 | . 9675 I | 17;4 | 215313.16 |
| .383 | . 37370 | 92,8 | . 92755 | 37,4 | . 57253 | 107,8 | .95734 | 17,5 | 215639.42 |
| . 384 | . 37463 | 92,7 | . 92717 | 37,5 | . 57361 | 107,5 | . 96716 | 17,5 | 220005.69 |
| 0.385 | 0.37556 | 92,7 | 0.92680 | 37,6 | 9.57468 | 107,2 | 9.96699 | 17,6 | $\begin{array}{llll}22 & 03 & 31.95\end{array}$ |
| . 386 | . 37649 | 92,6 | . 92642 | 37,6 | . 57575 | 106,9 | .9668I | 17,6 | 220658.22 |
| . 387 | . 37741 | 92,6 | .92605 | 37,7 | . 57682 | 106,6 | . 96663 | 17,7 | 22 10 24.48 |
| . 388 | . 37834 | 92,6 | . 92567 | 37,8 | . 57788 | 106,3 | . 95646 | 17,8 | 22 13 50.74 |
| . 389 | . 37926 | -92,5 | . 92529 | 37,9 | . 57894 | 106,0 | . 96628 | 17,8 | $2217 \begin{array}{lllllll} & 17\end{array}$ |
| 0.390 | 0.38019 | 92,5 | 0.92491 | 38,0 | 9.58000 | 105,7 | 9.96610 | 17,9 | $\begin{array}{llll}22 & 20 & 43.27\end{array}$ |
| . 391 | .38III | 92,5 | . 92453 | 38,1 | . 58105 | 105,4 | . 96592 | 17,9 | $\begin{array}{lllll}22 & 24 & 09.54\end{array}$ |
| . 392 | . 38204 | 92,4 | . 92415 | 38,2 | . 5821 II | 105, 1 | . 96574 | 18,0 | 222735.80 |
| . 393 | . 38296 | 92,4 | . 92376 | 38,3 | . 58316 | 104,8 | .96556 | 18,0 | 223102.07 |
| - 394 | . 38389 | 92,3 | . 92338 | 38,4 | . 58420 | 104,5 | . 96538 | 18,1 | 223428.33 |
| 0.395 | 0.38481 | 92,3 | 0.92300 | 38,5 | 9.58524 | 104,2 | 9.96520 | 18,1 | $\begin{array}{llll}22 & 3754.60\end{array}$ |
| . 396 | . 38573 | 92,3 | .9226I | 38,6 | . 58628 | 103,9 | . 96502 | 18,2 | 224120.86 |
| . 397 | . 38665 | 92,2 | . 92223 | 38,7 | . 58732 | 103,6 | . 96484 | 18,2 | 2244 47.13 |
| . 398 | . 38758 | 92,2 $92, \mathrm{I}$ | . 92184 | 38,8 38,8 | . 58836 | 103,3 103,0 | .96465 | 18,3 18,3 | $\begin{array}{llll}22 & 48 & 13.39 \\ 22 & 51 & 39.66\end{array}$ |
| - 399 | - 38850 | 92,I | .92145 | 38,8 | -58939 | 103,0 | -96447 | 18,3 | 225139.66 |
| 0.400 | 0.38942 | 92, I | 0.92106 | 38,9 | 9.59042 | 102,7 | 9.96429 | 18,4 | 225505.92 |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 100 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.400 | 0.38942 | 92, I | 0.92106 | 38,9 | 9.59042 | 102,7 | 9.96 .429 | 18,4 | $22^{\circ} 55^{\prime} 05^{\prime \prime} .92$ |
| . 401 | . 39034 | 92, I | . 92067 | 39,0 | . 59144 | 102,4 | .96410 | 18,4 | 225832.19 |
| . 402 | - 39126 | 92,0 | . 92028 | 39, I | . 59247 | 102,2 | . 96392 | 18,5 | 23 OI 58.45 |
| . 403 | - 39218 | 92,0 | .91989 | 39,2 | . 59349 | IOI,9 | . 96374 | 18,5 |  |
| . 404 | . 39310 | 91,9 | . 91950 | 39,3 | . 59450 | 101,6 | . 96355 | 18,6 | 230850.98 |
| 0.405 | 0.39402 | 91,9 | 0.91910 | 39,4 | 9.59552 | 101,3 | 9.96336 | 18,6 | $\begin{array}{lll}23 & 12 & 17.25\end{array}$ |
| . 406 | . 39494 | 91,9 | .9187I | 39,5 | . 59653 | IOI, 0 | . 963 I 8 | 18,7 | 23 I5 43.51 |
| . 407 | . 39586 | 9I,8 | .9183I | 39,6 | . 59754 | 100,7 | . 96299 | 18,7 | $\begin{array}{llllllllllllllllllll}23 & 19 & 09.78\end{array}$ |
| . 408 | - 39677 | 9I,8 | .91792 | 39,7 | . 59854 | 100,5 | . 96280 | I8,8 | $23 \quad 2236.04$ |
| . 409 | . 39769 | 91,8 | .91752 | 39,8 | . 59955 | 100,2 | . 96262 | 18,8 | 232602.31 |
| 0.410 | 0.3986I | 91,7 | 0.91712 | 39,9 | $9.60055^{\prime}$ | 99,9 | 9.96243 | 18,9 | $\begin{array}{lll}23 & 29 & 28.57\end{array}$ |
| . 411 | . 39953 | 91,7 | . 91672 | 40,0 | . 60155 | 99,6 | . 96224 | 18,9 | $\begin{array}{lllll}23 & 32 & 54.84\end{array}$ |
| . 412 | . 40044 | 91,6 | .91632 | 40,0 | . 60254 | 99,4 | . 96205 | 19,0 | 2336 21.10 |
| . 413 | . 40136 | 91,6 | .91592 | 40,1 | . 60353 | 99, I | .96186 | 19,0 | 233947.36 |
| . 414 | . 40227 | 91,6 | .91552 | 40,2 | . 60452 | 98,8 | . 96167 | 19, I | 234313.63 |
| 0.415 | 0.40319 | 91,5 | 0.91512 | 40,3 | 9.60551 | 98,6 | 9.96148 | 19, I | 234639.89 |
| . 416 | . 40410 | 91,5 | .91471 | 40,4 | . 60649 | 98,3 | . 96128 | 19,2 | 235006.16 |
| .417 | . 40502 | 9I,4 | .9143I | 40,5 | . 60748 | 98,0 | . 96109 | 19,2 | 235332.42 |
| . 418 | . 40593 | 9I,4 | .91390 | 40,6 | . 60845 | 97,8 | . 96090 | 19,3 | 235658.69 |
| .419 | . 40685 | 91,3 | . 91350 | 40,7 | . 60943 | 97,5 | .9607I | 19,3 | 240024.95 |
| 0.420 | 0.40776 | 91,3 | 0.91309 | 40,8 | 9.61041 | 97,3 | 9.96051 | 19,4 | 240351.22 |
| . 42 I | . 40867 | 91,3 | .91268 | 40,9 | .61138 | 97,0 | . 96032 | 19,4 | 240717.48 |
| . 422 | . 40959 | 91,2 | . 91227 | 41,0 | . 61234 | 96,7 | . 96012 | 19,5 | 24 IO 43.75 |
| . 423 | . 41050 | 9I,2 | .91186 | 41,0 | .6I33I | 96,5 | . 95993 | 19,6 | 241410.01 |
| . 424 | . 4 II 41 | 9I, 1 | .91145 | 4I, I | .61427 | 96,2 | . 95973 | 19,6 | 241736.28 |
| 0.425 | 0.41232 | 91, I | 0.91104 | 41,2 | 9.61524 | 96,0 | 9.95954 | 19,7 | 242102.54 |
| . 426 | . 41323 | 9I, I | . 91063 | 4I,3 | .61619 | 95,7 | . 95934 | 19,7 | 242428.81 |
| .427 | . 41414 | 91,0 | .9102I | 4I,4 | . 61715 | 95,5 | .95914 | 19,8 | 242755.07 |
| . 428 | . 41505 | 91,0 | . 90980 | 41,5 | .61810 | 95,2 | . 95894 | 19,8 | 24 31 21.34 |
| .429 | . 41596 | 90,9 | . 90938 | 41,6 | . 61905 | 94,9 | . 95875 | 19,9 | 243447.60 |
| 0.430 | 0.41687 | 90,9 | 0.90897 | 41,7 | 9.62000 | 94,7 | 9.95855 | 19,9 | 243813.87 |
| . 431 | . 41778 | 90,9 | . 90855 | 41,8 | . 62095 | 94,4 | . 95835 | 20,0 | 244140.13 |
| . 432 | . 41869 | 90,8 | .908I3 | 41,9 | . 62189 | 94,2 | .95815 | 20,0 | 244506.40 |
| . 433 | . 41960 | 90,8 | . 90771 | 42,0 | . 62283 | 94,0 | . 95795 | 20, I | 244832.66 |
| . 434 | . 42050 | 90,7 | . 90729 | 42, I | . 62377 | 93,7 | . 95775 | 20, I | 245158.93 |
| 0.435 | 0.42141 | 90,7 | 0:90687 | 42, I | 9.62471 | 93,5 | 9.95755 | 20,2 | 2455 25.19 |
| . 436 | . 42232 | 90,6 | . 90645 | 42,2 | . 62564 | 93,2 | . 95734 | 20,2 | 2458 51.46 |
| . 437 | . 42322 | 90,6 | . 90603 | 42,3 | . 62657 | 93,0 | . 95714 | 20,3 | 250217.72 |
| . 438 | . 42413 | 90,6 | . 90560 | 42,4 | . 62750 | 92,8 | . 95694 | 20,3 | $\begin{array}{lllll}25 & 05 & 43.99\end{array}$ |
| . 439 | . 42503 | 90,5 | . 90518 | 42,5 | . 62842 | 92,5 | . 95673 | . 20,4 | 250910.25 |
| 0.440 | 0.42594 | 90,5 | 0.90475 | 42,6 | 9.62935 | 92,2 | 9.95653 | 20,4 | 251236.51 |
| . 44 I | . 42684 | 90,4 | . 90433 | 42,7 | . 63027 | 92,0 | . 95632 | 20,5 | $\begin{array}{lllll}25 & 16 & 02.78\end{array}$ |
| . 442 | .42775 | 90,4 | . 90390 | 42,8 | .63119 | 91,8 | .956I2 | 20,6 | $\begin{array}{llll}25 & 19 & 29.04\end{array}$ |
| . 443 | . 42865 | 90,3 | . 90347 | 42,9 | . 63210 | 91,5 | .95591 | 20,6 | $25 \quad 22 \quad 55.31$ |
| . 444 | . 42956 | 90,3 | . 90304 | 43,0 | . 63302 | 91,3 | .95571 | 20,7 | 252621.57 |
| 0.445 | 0.43046 | 90,3 | 0.90261 | 43,0 | 9.63393 | 91, I | 9.95550 | 20,7 | $25 \quad 2947.84$ |
| .446 | . 43136 | 90,2 | . 90218 | 43, I | . 63484 | 90,8 | . 95529 | 20,8 | $25 \quad 3314.10$ |
| . 447 | . 43226 | 90,2 | . 90175 | 43,2 | . 63575 | 90,6 | . 95509 | 20,8 | 253640.37 |
| . 448 | . 43316 | 90, I | .90132 | 43,3 | . 63665 | 90,4 | . 65488 | 20,9 | $\begin{array}{llll}25 & 40 & 06.63\end{array}$ |
| . 449 | . 43406 | 90, 1 | . 90088 | 43,4 | . 63755 | 90, I | .95467 | 20,9 | 254332.90 |
| 0.450 | 0.43497 | 90,0 | 0.90045 | 43,5 ${ }^{\circ}$ | 9.63845 | 89,9 | 9.95446 | 21,0 | 254659.16 |
| u | -i sinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{s i n} 4$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \cos u$ | $\omega F_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.450 | 0.43497 | 90,0 | 0.90045 | 43,5 | 9.63845 | 89,9 | 9.95446 | 21,0 | $25^{\circ} 46^{\prime} 59.16$ |
| .45I | . 43587 | 90,0 | .9000I | 43,6 | . 63935 | 89,7 | . 95425 | 21,0 | 255025.43 |
| . 452 | . 43677 | 90,0 | . 89958 | 43,7 | . 64025 | 89,4 | . 95404 | 21,1 | 2553 51. 69 |
| . 453 | . 43766 | 89,9 | . 89914 | 43,8 | . 64114 | 89,2 | . 95383 | 21,1 | $25 \quad 5717.96$ |
| . 454 | . 43856 | 89,9 | . 89870 | 43,9 | . 64203 | 89,0 | .95361 | 21,2 | 260044.22 |
| 0.455 | 0.43946 | 89,8 | 0.89826 | 43,9 | 9.64292 | 88,8 | 9.95340 | 21,2 | 260410.49 |
| . 456 | . 44036 | 89,8 | . 89782 | 44,0 | .64381 | 88,5 | .95319 | 21,3 | 260736.75 |
| . 457 | . 44126 | 89,7 | . 89738 | 44, I | .64469 | 88,3 | . 95298 | 21,4 | 26 II 03.02 |
| . 458 | . 44216 | 89,7 | . 89694 | 44,2 | . 64557 | 88, 1 | . 95276 | 21,4 | 261429.28 |
| . 459 | .44305 | 89,6 | . 89650 | 44,3 | . 64645 | 87,9 | . 95255 | 21,5 | 26 I7 55.55 |
| 0.460 | 0.44395 | 89,6 | 0.89605 | 44,4 | 9.64733 | 87,7 | 9.95233 | 21,5 | 26 21 2I.8I |
| . 461 | . 44484 | 89,6 | . 89561 | 44,5 | .64821 | 87,4 | .95212 | 21,6 | 262448.08 |
| . 462 | . 44574 | 89,5 | . 89516 | 44,6 | . 64908 | 87,2 | . 95190 | 21,6 | $26 \quad 2814.34$ |
| . 463 | . 44663 | 89,5 | . 89472 | 44,7 | . 64995 | 87,0 | .95169 | 21,7 | 26 31 40.6I |
| . 464 | . 44753 | 89,4 | . 89427 | 44,8 | . 65082 | 86,8 | .95147 | 21,7 | 263506.87 |
| 0.465 | 0.44842 | 89,4 | 0.89382 | 44,8 | 9.65169 | 86,6 | 9.95125 | 21,8 | 2638 33.13 |
| . 466 | . 44932 | 89,3 | . 89337 | 44,9 | . 652515 | 86,4 | . 95103 | 21,8 | 264159.40 |
| .467 | . 4502 I | 89,3 | . 89292 | 45,0 | .6534I | 86, I | .9508I | 21,9 | 264525.66 |
| . 468 | .451 10 | 89,2 | . 89247 | 45, I | . 65428 | 85,9 | . 95059 | 22,0 | 264851.93 |
| .469 | .45199 | 89,2 | . 89202 | 45,2 | . 65513 | 85,7 | . 95037 | 22,0 | 2652 18.19 |
| 0.470 | 0.45289 | 89,2 | 0.89157 | 45,3 | 9.65599 | 85,5 | 9.95015 | 22,I | 265544.46 |
| . 471 | . 45378 | 89, I | .891 II | 45,4 | . 65684 | 85,3 | . 94993 | 22, I | 265910.72 |
| . 472 | . 45467 | 89, I | . 89066 | 45,5 | . 65769 | 85, 1 | . 9497 I | 22,2 | 270236.99 |
| . 473 | . 45556 | 89,0 | . 8902 I | 45,6 | . 65854 | 84,9 | . 94949 | 22,2 | 270503.25 |
| . 474 | . 45645 | 89,0 | . 88975 | 45,6 | . 65939 | 84,7 | . 94927 | 22,3 | 270929.52 |
| 0.475 | 0.45734 | 88,9 | 0.88929 | 45,7 | 9.66024 | 84,4 | 9.94904 | 22,3 | $27 \quad 12 \quad 55.78$ |
| . 476 | . 45823 | 88,9 | . 88883 | 45,8 | . 66108 | 84,2 | . 94882 | 22,4 | 271622.05 |
| . 477 | . 45912 | 88,8 | . 88838 | 45,9 | . 66192 | 84,0 | . 94850 | 22,4 | 27 19 48.31 |
| . 478 | . 46000 | 88,8 | . 88792 | 46,0 | .66276 | 83,8 | . 94837 | 22,5 | 2723 I4.58 |
| . 479 | . 46089 | 88,7 | . 88746 | 46,1 | . 66360 | 83,6 | .94815 | 22,6 | 272640.84 |
| 0.480 | 0.46178 | 88,7 | 0.88699 | 46,2 | 9.66443 | 83,4 | 9.94792 | 22,6 | 273007.11 |
| .48I | . 46267 | 88,7 | . 88653 | 46,3 | . 66527 | 83,2 | . 94769 | 22,7 | $2733 \quad 33.37$ |
| . 482 | . 46355 | 88,6 | . 88607 | 46,4 | . 66510 | 83,0 | . 94747 | 22,7 | 273659.64 |
| .483 | . 46444 | 88,6 | .8856I | 46,4 | .66693 | 82,8 | . 94724 | 22,8 | 274025.90 |
| . 484 | . 46532 | 88,5 | . 88514 | 46,5 | . 66775 | 82,6 | .94701 | 22,8 | 274352.17 |
| 0.485 | 0.46621 | 88,5 | 0.88467 | 46,6 | 9.66858 | 82,4 | 9.94678 | 22,9 | $27 \quad 47 \quad 18.43$ |
| . 486 | . 46709 | 88,4 | . 8842 I | 46,7 | . 66940 | 82,2 | . 94655 | 22,9 | 275044.70 |
| .487 | . 46798 | 88,4 | . 88374 | 46,8 | . 67022 | 82,0 | . 94633 | 23,0 | 275410.96 |
| . 488 | . 46886 | 88,3 | . 88327 | 46,9 | . 67104 | 81,8 | . 94609 | 23, I | 275737.23 |
| .489 | . 46974 | 88,3 | . 88280 | 47,0 | . 67186 | 8ı,6 | . 94586 | 23, I | 28 O1 03.49 |
| 0.490 | 0.47063 | 88,2 | 0.88233 | 47,I | 9.67268 | 81,4 | 9.94563 | 23,2 | 280429.76 |
| . 491 | .47151 | 88,2 | .88I86 | 47,2 | . 67349 | 81,2 | . 94540 | 23,2 | 280756.02 |
| . 492 | . 47239 | 88, I | .88I 39 | 47,2 | . 67430 | $8 \mathrm{I}, 0$ | . 94517 | 23,3 | 28 II 22.28 |
| . 493 | . 47327 | 88,1 | . 88092 | 47,3 | .675II | 80,8 | . 94493 | 23,3 | 28 I4 48.55 |
| . 494 | . 47415 | 88,0 | . 88044 | 47,4 | . 67592 | 80,6 | . 94470 | 23,4 | 28 I8 I4.8I |
| 0.495 | 0.47503 | 88,0 | 0.87997 | 47,5 | 9.67672 | 80,5 | 9.94447 | 23,4 | 28 21 4 I .08 |
| . 496 | . 47591 | 87,9 | . 87949 | 47,6 | . 67753 | 80,3 | . 94423 | 23,5 | $28 \quad 2507.34$ |
| . 497 | .47679 | 87,9 | . 87902 | 47,7 | . 67833 | 80,1 | . 94400 | 23,6 |  |
| . 498 | . 47767 | 87,9 878 | . 87854 | 47,8 | . 67913 | 79,9 | . 94376 | 23,6 | $\begin{array}{llll}28 & 31 & 59.87\end{array}$ |
| . 499 | . 47855 | 87,8 | . 87806 | 47,9 | . 67993 | 79,7 | . 94352 | 23,7 | $28 \quad 3526.14$ |
| 0.500 | 0.47943 | 87,8 | 0.87758 | 47,9 | 9.68072 | 79,5 | 9.94329 | 23,7 | 283852.40 |
| $u$ | -i sinh iu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.500 | 0.47943 | 87,8 | 0.87758 | 47,9 | 9.68072 | 79,5 | 9.94329 | 23,7 | $28^{\circ} 38^{\prime} 52.40$ |
| . 501 | . 48030 | 87,7 | . 87710 | 48,0 | .68152 | 79,3 | . 94305 | 23,8 | $28 \quad 42$ 18.67 |
| . 502 | .48i 18 | 87,7 | . 87662 | 48, I | .6823I | 79,1 | .9428I | 23,8 | 284544.93 |
| . 503 | . 48206 | 87,6 | . 87614 | 48,2 | . 68310 | 78,9 | . 94257 | 23,9 | 2849 II. 20 |
| . 504 | . 48293 | 87,6 | . 87566 | 48,3 | . 68389 | 78,7 | . 94233 | 24,0 | $285237 \cdot 46$ |
| 0.505 | 0.4838 I | 87,5 | 0.87517 | 48,4 | 9.68467 | 78,6 | 9.94209 | 24,0 | 285603.73 |
| . 506 | . 48.468 | 87,5 | . 87469 | 48,5 | . 68546 | 78,4 | . 94185 | 24, I | 285929.99 |
| . 507 | . 48556 | 87,4 | . 8742 I | 48,6 | . 68624 | 78,2 | . 94161 | 24, I | 290256.26 |
| . 508 | . 48643 | 87,4 | . 87372 | 48,6 | . 68702 | 78,0 | .94I37 | 24,2 | 290622.52 |
| . 509 | . 48730 | 87,3 | . 87323 | 48,7 | . 68780 | 77,8 | .94II3 | 24,2 | 290948.79 |
| 0.510 | 0.488 I 8 | 87,3 | 0.87274 | 48,8 | 9.68858 | 77,6 | 9.94089 | 24,3 | 29 I3 15.05 |
| . 511 | . 48905 | 87,2 | . 87226 | 48,9 | . 68935 | 77,5 | . 94064 | 24,3 | 291641.32 |
| . 512 | . 48992 | 87,2 | . 87177 | 49,0 | . 69013 | 77,3 | . 94040 | 24,4 | 292007.58 |
| . 513 | . 49079 | 87, | . 87128 | 49, I | . 69090 | 77, 1 | . 94016 | 24,5 | 292333.85 |
| . 514 | . 49166 | 87, 1 | . 87078 | 49,2 | . 69167 | 76,9 | . 9399 I | 24,5 | 2927 00. II |
| 0.515 | 0.49253 | 87,0 | 0.87029 | 49,3 | 9.69244 | 76,7 | 9.93967 | 24,6 | $2930 \quad 26.38$ |
| . 516 | . 49340 | 87,0 | . 86980 | 49,3 | . 69320 | 76,6 | . 93942 | 24,6 | 293352.64 |
| . 517 | . 49427 | 86,9 | . 86931 | 49,4 | . 69397 | 76,4 | . 93917 | 24,7 | 293718.90 |
| . 518 | . 49514 | 86,9 | .8688I | 49,5 | . 69473 | 76,2 | . 93893 | 24,8 | 294045.17 |
| . 519 | . 49601 | 86,8 | . 86832 | 49,6 | . 69549 | 76,0 | . 93858 | 24,8 | 2944 II. 43 |
| 0.520 | 0.49688 | 86,8 | 0.86782 | 49,7 | 9.69625 | 75,9 | 9.93843 | 24,9 | 294737.70 |
| . 521 | . 49775 | 86,7 | . 86732 | 49,8 | . 69701 | 75,7 | . 93818 | 24,9 | 29 51 03.96 |
| . 522 | . 4986 I | 86,7 | . 86682 | 49,9 | . 69777 | 75,5 | . 93793 | 25,0 | 295430.23 |
| . 523 | . 49948 | 86,6 | . 86632 | 49,9 | . 69852 | 75,3 | . 93768 | 25,0 | 295756.49 |
| . 524 | . 50035 | 86,6 | . 86582 | 50,0 | . 69927 | 75,2 | . 93743 | 25, I | 30 OI 22.76 |
| 0.525 | 0.50121 | 86,5 | 0.86532 | 50, I | 9.70002 | 75,0 | 9.93718 | 25,2 | 300449.02 |
| . 526 | . 50208 | 86,5 | . 86482 | 50,2 | . 70077 | 74,8 | . 93693 | 25,2 | $30 \quad 0815.29$ |
| . 527 | . 50294 | 86,4 | . 86432 | 50,3 | . 70152 | 74,6 | . 93667 | 25,3 | 30 II 41.55 |
| . 528 | . 5038 I | 86,4 | . 86382 | 50,4 | . 70226 | 74,5 | . 93642 | 25,3 | 301507.82 |
| . 529 | . 50467 | 86,3 | . 86331 | 50,5 | . 70301 | 74,3 | .936I7 | 25,4 | $30 \quad 18 \quad 34.08$ |
| 0.530 | 0.50553 | 86,3 | 0.8628I | 50,6 | 9.70375 | 74,I | 9.93:591 | 25,4 | 302200.35 |
| . 531 | . 50640 | 86,2 | . 86230 | 50,6 | . 70449 | 74,0 | . 93566 | 25,5 | $30 \quad 25 \quad 26.6 \mathrm{I}$ |
| . 532 | . 50726 | 86,2 | . 86179 | 50,7 | . 70523 | 73,8 | . 93540 | 25,6 | $30 \quad 2852.88$ |
| . 533 | . 50812 | 86, I | . 86129 | 50,8 | . 70597 | 73,6 | .93515 | 25,6 | $3032 \begin{array}{llll}30 & 19\end{array}$ |
| . 533 | . 50898 | 86, I | . 86078 | 50,9 | . 70670 | 73,4 | . 93489 | 25,7 | 303545.41 |
| 0.535 | 0.50984 | 86,0 | 0.86027 | 51,0 | 9.70743 | 73,3 | 9.93463 | 25,7 | $30 \quad 39$ II. 67 |
| . 536 | . 51070 | 86,0 | . 85976 | 5I, I | . 70817 | 73, 1 | . 93438 | 25,8 | 304237.94 |
| . 537 | . 51156 | 85,9 | . 85925 | 51,2 | . 70890 | 72,9 | . 93412 | 25,9 | $30 \quad 4604.20$ |
| . 538 | . 51242 | 85,9 | . 85874 | 51,2 | . 70963 | 72,8 | . 93386 | 25,9 | $30 \quad 4930.47$ |
| . 539 | . 51328 | 85,8 | . 85822 | 51,3 | . 71035 | 72,6 | . 93360 | 26,0 | 305256.73 |
| 0.540 | 0.51414 | 85,8 | 0.85771 | 51,4 | 9.71108 | 72,5 | 9.93334 | 26,0 | 305623.00 |
| . 541 | . 51499 | 85,7 | . 85719 | 51,5 | . 71180 | 72,3 | . 93308 | 26, 1 | 305949.26 |
| . 542 | . 51585 | 85,7 | . 85668 | 51,6 | . 71252 | 72,1 | . 93282 | 26,2 | 3103 I 5.52 |
| . 543 | . 51671 | 85,6 | . 85616 | 51,7 | . 71324 | 72,0 | . 93256 | 26,2 | 3 I of 41.79 |
| . 544 | . 51756 | 85,6 | . 85565 | 51,8 | . 71396 | 71,8 | . 93229 | 26,3 | 311008.05 |
| 0.545 | 0.51842 | 85,5 | 0.85513 | 51,8 | 9.71468 | 71,6 | 9.93203 | 26,3 | 3 I I3 $34 \cdot 32$ |
| . 546 | . 51927 | 85,5 | . 85461 | 51,9 | . 71540 | 71,5 | .93177 | 26,4 | 3117700.58 |
| . 547 | . 52013 | 85,4 | . 85409 | 52,0 | .71611 | 71,3 | .93150 | 26,4 | $\begin{array}{llll}31 & 20 & 26.85\end{array}$ |
| . 548 | . 52098 | 85,4 | . 85357 | 52,1 | . 71682 | 71,2 | .93124 | 26,5 | $\begin{array}{llll}31 & 23 & 53.11 \\ 31 & 27 & 19.38\end{array}$ |
| . 549 | . 52183 | 85,3 | . 85305 | 52,2 | .71753 | 71,0 | . 93097 | 26,6 | 312719.38 |
| 0.550 | 0.52269 | 85,3 | 0.85252 | 52,3 | 9.71824 | 70,8 | 9.93071 | 26,6 | 313045.64 |
| $u$ | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega F_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.550 | 0.52269 | 85,3 | 0.85252 | 52,3 | 9.71824 | 70,8 | 9.93071 | 26,6 | $31^{\circ} 30^{\prime} 45.64$ |
| . 551 | . 52354 | 85,2 | . 85200 | 52,4 | . 71895 | 70,7 | . 93044 | 26,7 | 313411.91 |
| . 552 | . 52439 | 85, I | . 85148 | 52,4 | . 71966 | 70,5 | . 93017 | 26,7 | 313738.17 |
| . 553 | . 52524 | 85,1 | . 85095 | 52,5 | . 72036 | 70,4 | . 92991 | 26,8 | 3 I 4 I 04.44 |
| . 554 | . 52609 | 85,0 | . 85043 | 52,6 | . 72106 | 70,2 | . 92964 | 26,9 | 3I 4430.70 |
| 0.555 | 0.52694 | 85,0 | 0.84990 | 52,7 | 9.72176 | 70,0 | 9.92937 | 26,9 | 314756.97 |
| . 556 | . 52779 | 84,9 | . 84937 | 52,8 | . 72246 | 69,9 | . 92910 | 27,0 | 315123.23 |
| . 557 | . 52864 | 84,9 | . 84884 | 52,9 | . 72316 | 69,7 | . 92883 | 27,0 | 315449.50 |
| . 558 | . 52949 | 84,8 | .84832 | 52,9 | . 72386 | 69,6 | . 92856 | 27, I | 315815.76 |
| . 559 | . 53034 | 84,8 | . 84779 | 53,0 | . 72455 | 69,4 | . 92829 | 27,2 | 32 O1 42.03 |
| 0.560 | O.53II9 | 84,7 | 0.84726 | 53, I | 9.72525 | 69,3 | 9.92801 | 27,2 | 320508.29 |
| . 56 I | . 53203 | 84,7 | . 84672 | 53,2 | . 72594 | 69,1 | . 92774 | 27,3 |  |
| . 562 | . 53288 | 84,6 | .846I9 | 53,3 | . 72663 | 69,0 | . 92747 | 27,3 | 321200.82 |
| . 563 | . 53373 | 84,6 | . 84566 | 53,4 | . 72732 | 68,8 | . 92719 | 27,4 | $\begin{array}{lllll}32 & 15 & 27.09\end{array}$ |
| . 564 | . 53457 | 84,5 | . 84512 | 53,5 | . 72801 | 68,7 | .92692 | 27,5 | 32 I8 53.35 |
| 0.565 | 0.53542 | 84,5 | 0.84459 | 53,5 | 9.72869 | 68,5 | 9.92665 | 27,5 | $\begin{array}{llll}32 & 22 & 19.62\end{array}$ |
| . 566 | . 53626 | 84,4 | . 84405 | 53,6 | . 72938 | 68,4 | . 92637 | 27,6 | 322545.88 |
| . 567 | . 53710 | 84,4 | . 84352 | 53,7 | . 73006 | 68,2 | . 92609 | 27,7 | 322912.15 |
| . 568 | . 53795 | 84,3 | . 84298 | 53,8 | . 73074 | 68, 1 | . 92582 | 27,7 | $3232 \begin{array}{llll}38.41\end{array}$ |
| .569 | . 53879 | 84,2 | . 84244 | 53,9 | .73142 | 67,9 | . 92554 | 27,8 | $\begin{array}{llll}32 & 36 & 04.67\end{array}$ |
| 0.570 | 0.53963 | 84,2 | 0.84190 | 54,0 | 9.73210 | 67,8 | 9.92526 | 27,8 | 323930.94 |
| . 571 | . 54047 | 84, I | . 84136 | 54,0 | . 73277 | 67,6 | . 92498 | 27,9 | 324257.20 |
| . 572 | .5413I | 84, I | . 84082 | 54,1 | . 73345 | 67,5 | . 92470 | 28,0 | $\begin{array}{lllll}32 & 46 & 23.47\end{array}$ |
| . 573 | . 54216 | 84,0 | . 84028 | 54,2 | . 73412 | 67,3 | . 92442 | 28,0 | 324949.73 |
| . 574 | . 54300 | 84,0 | . 83974 | 54,3 | . 73480 | 67,2 | .924I4 | 28, 1 | 325316.00 |
| 0.575 | 0.54383 | 83,9 | 0.83919 | 54,4 | 9.73547 | 67,0 | 9.92386 | 28, I | $\begin{array}{llll}32 & 56 & 42.26\end{array}$ |
| . 576 | . 54467 | 83,9 | . 83865 | 54,5 | . 73614 | 66,9 | . 92358 | 28,2 | 330008.53 |
| . 577 | . 5455 I | 83,8 | .83810 | 54,6 | . 73680 | 66,7 | . 92330 | 28,3 |  |
| . 578 | . 54635 | 83,8 | . 83756 | 54,6 | . 73747 | 66,6 | . 92301 | 28,3 | 330701.06 |
| . 579 | . 54719 | 83,7 | . 83701 | 54,7 | .73814 | 66,4 | . 92273 | 28,4 | 33 Io 27.32 |
| 0.580 | 0.54802 | 83,6 | 0.83646 | 54,8 | 9.73880 | 66,3 | 9.92245 | 28,5 | 33 I3 53.59 |
| . 58 I | . 54886 | 83,6 | . 83591 | 54,9 | . 73946 | 66,2 | . 92216 | 28,5 | $\begin{array}{lllll}33 & 17 & 19.85\end{array}$ |
| . 582 | . 54970 | 83,5 | . 83536 | 55,0 | . 74012 | 66,0 | . 922188 | 28,6 | 332046.12 |
| . 583 | . 55053 | 83,5 | . 8348 I | 55, I | . 74078 | 65,9 | .92I 59 | 28,6 | $\begin{array}{llll}33 & 24 & 12.38\end{array}$ |
| . 584 | . 55137 | 83,4 | . 83426 | 55, I | .74144 | 65,7 | .92130 | 28,7 | 332738.65 |
| 0.585 | 0.55220 | 83,4 | 0.83371 | 55,2 | 9.74210 | 65,6 | 9.92102 | 28,8 | 333104.91 |
| . 586 | . 55303 | 83,3 | . 83316 | 55,3 | . 74275 | 65,4 | .92073 | 28,8 | 3334 3I.18 |
| . 587 | . 55387 | 83,3 | . 8326 I | 55,4 | . 74340 | 65,3 | . 92044 | 28,9 | 333757.44 |
| . 588 | . 55470 | 83,2 | . 83205 | 55,5 | . 74406 | 65,1 | . 92015 | 29,0 | 334123.71 |
| . 589 | . 55553 | 83,1 | . 83150 | 55,6 | . 74471 | 65,0 | .91986 | 29,0 | 334449.97 |
| 0.590 | 0.55636 | 83,1 | 0.83094 | 55,6 | 9.74536 | 64,9 | 9.91957 | 29, I | 334816.24 |
| . 591 | . 55719 | 83,0 | . 83038 | 55,7 | . 74600 | 64,7 | . 91928 | 29, I | 33 51 42.50 |
| . 592 | . 55802 | 83,0 | . 82983 | 55,8 | .74665 | 64,6 | . 91899 | 29,2 | 335508.77 |
| . 593 | . 55885 | 82,9 | . 82927 | 55,9 | . 74730 | 64,4 | .91869 | 29,3 | 335835.03 |
| . 594 | - 55968 | 82,9 | . 82871 | 56,0 | . 74794 | 64,3 | .91840 | 29,3 | 3402 OI. 29 |
| 0.595 | 0.56051 | 82,8 | 0.828 I5 | 56, I | 9.74858 | 64,2 | 9.91811 | 29,4 | 340527.56 |
| . 596 | . 56134 | 82,8 | . 82759 | 56, I | . 74922 | 64,0 | .91781 | 29,5 | $\begin{array}{llll}34 & 08 & 53.82\end{array}$ |
| . 597 | . 56216 | 82,7 | . 82703 | 56,2 | . 74986 | 63,9 | .91752 | 29,5 | 341220.09 |
| . 598 | . 56299 | 82,6 | . 82646 | 56,3 | . 75050 | 63,8 | -91722 | 29,6 | $\begin{array}{llll}34 & \text { I5 } & 46.35 \\ 34 & \text { I9 } & \text { I2.62 }\end{array}$ |
| . 599 | . 56382 | 82,6 | . 82590 | 56,4 | .75II4 | 63,6 | .91693 | 29,6 | 3419 I 2.62 |
| 0.600 | 0.56464 | 82,5 | 0.82534 | 56,5 | 9.75177 | 63,5 | 9.91663 | 29,7 | 342238.88 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega F_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.600 | 0.56464 | 82,5 | 0.82534 | 56,5 | 9.75177 | 63,5 | 9.91663 | 29,7 | $34^{\circ} 222^{\prime} 38^{\prime \prime} .88$ |
| . 601 | . 56547 | 82,5 | . 82477 | 56,5 | . 7524 I | 63,3 | . 91633 | 29,8 | 342605.15 |
| . 602 | . 56629 | 82,4 | . 82420 | 56,6 | . 75304 | 63,2 | . 91604 | 29,8 | 3429 31.4I |
| . 603 | . 56712 | 82,4 | . 82364 | 56,7 | . 75367 | 63,1 | .91574 | 29,9 | $3432 \quad 57.68$ |
| . 604 | . 56794 | 82,3 | . 82307 | 56,8 | . 75430 | 62,9 | .91544 | 30,0 | 343623.94 |
| 0.605 | 0.56876 | 82,3 | 0.82250 | 56,9 | 9.75493 | 62,8 | 9.91514 | 30,0 | 343950.2 I |
| . 606 | . 56958 | 82,2 | . 82193 | 57,0 | . 75556 | 62,7 | .91484 | 30,1 | 344316.47 |
| . 607 | . 57041 | 82,I | . 82136 | 57,0 | . 75618 | 62,5 | . 91454 | 30,2 | 344642.74 |
| . 608 | . 57123 | 82,I | . 82079 | 57, I | . 7568 I | 62,4 | . 91423 | 30,2 | 345009.00 |
| . 609 | . 57205 | 82,0 | . 82022 | 57,2 | . 75743 | 62,3 | .91393 | 30,3. | 345335.27 |
| 0.610 | 0.57287 | 82,0 | 0.81965 | 57,3 | 9.75805 | 62, 1 | 9.91363 | 30,4 | 3457 OI. 53 |
| .6II | . 57369 | 81,9 | .81907 | 57,4 | . 75867 | 62,0 | . 91332 | 30,4 | 350027.80 |
| . 612 | . 5745 I | 81,9 | . 81850 | 57,5 | . 75929 | 6I,9 | . 91302 | 30,5 | 350354.05 |
| . 613 | . 57532 | 8r,8 | .81793 | 57,5 | . 75991 | 6I,7 | .9127I | 30,5 | 350720.33 |
| .614 | . 57614 | 8r,7 | .81735 | 57,6 | .76053 | 61,6 | .9124I | 30,6 | 35 IO 46.59 |
| 0.615 | 0.57696 | 81,7 | 0.81677 | 57,7 | 9.76II4 | 6I,5 | 9.91210 | 30,7 | $\begin{array}{llll}35 & 14 & 12.86\end{array}$ |
| . 616 | . 57778 | 81,6 | . 81620 | 57,8 | . 76176 | 6I,4 | .91179 | 30,7 | 35 I7 39.12 |
| .6I7 | . 57859 | 81,6 | .81562 | 57,9 | . 76237 | 6I,2 | .91149 | 30,8 | 35 21 05.39 |
| . 618 | . 57941 | 8I,5 | .81504 | 57,9 | . 76298 | 6I, | -91II8 | 30,9 | 352431.65 |
| . 619 | . 58022 | 8I, 4 | . 81446 | 58,0 | . 763159 | 6I,0 | . 91087 | 30,9 | $35 \quad 2757.92$ |
| 0.620 | 0.58104 | 8r,4 | 0.81388 | 58, I | 9.76420 | 60,8 | 9.91056 | 31,0 | 353124.18 |
| . 62 I | . 58185 | 8r,3 | .81330 | 58,2 | . 7648 I | 60,7 | .91025 | 3I, I | 353450.44 |
| . 622 | . 58266 | 81,3 | .8127I | 58,3 | . 76542 | 60,6 | . 90994 | 31,I | 3538 16.71 |
| . 623 | . 58347 | 81,2 | .812I3 | 58,3 | . 76602 | 60,4 | . 90963 | 31,2 | 354142.97 |
| . 624 | . 58429 | 8I,2 | . 81155 | 58,4 | . 76663 | 60,3 | .9093I | 31,3 | 354509.24 |
| 0.625 | 0.58510 | $8 \mathrm{r}, \mathrm{I}$ | 0.81096 | 58,5 | 9.76723 | 60,2 | 0.90900 | 3I,3 | $\begin{array}{llll}35 & 48 & 35.50\end{array}$ |
| . 626 | . 58591 | 81,0 | .81038 | 58,6 | . 76783 | 60, I | . 90869 | 3I,4 | 3552 OI. 77 |
| . 627 | . 58672 | 81,0 | . 80979 | 58,7 | . 76843 | 59,9 | . 90837 | 31,5 | 355528.03 |
| . 628 | . 58753 | 80,9 | . 80920 | 58,8 | . 76903 | 59,8 | . 90806 | 31,5 | $35 \quad 58 \quad 54.30$ |
| . 629 | . 58834 | 80,9 | . 80862 | 58,8 | . 76963 | 59,7 | . 90774 | 31,6 | 360220.56 |
| 0.630 | 0.58914 | 80,8 | 0.80803 | 58,9 | 9.77022 | 59,6 | 9.90743 | 31,7 | 360546.83 |
| . 631 | . 58995 | 80,7 | . 80744 | 59,0 | . 77082 | 59,4 | . 90711 | $3 \mathrm{I}, 7$ | $36 \quad 0913.09$ |
| . 632 | . 59076 | 80,7 | . 80685 | 59, I | . 77141 | 59,3 | . 90679 | 31,8 | 361239.36 |
| . 633 | . 59157 | 80,6 | . 80626 | 59,2 | . 77200 | 59,2 | . 90647 | 31,9 | $36 \quad 1605.62$ |
| . 634 | . 59237 | 80,6 | . 80566 | 59,2 | . 77259 | 59, I | .906I5 | 31,9 | 36 19 31.89 |
| 0.635 | 0.59318 | 80,5 | 0.80507 | 59,3 | 9.77318 | 58,9 | 9.90583 | 32,0 | 362258.15 |
| . 636 | . 59398 | 80,4 | . $80+48$ | 59,4 | . 77377 | 58,8 | .9055I | 32,I | $3626 \quad 24.42$ |
| . 637 | . 59479 | 80,4 | . 80388 | 59,5 | . 77436 | 58,7 | . 90519 | 32, I | 362950.68 |
| . 638 | . 59559 | 80,3 | . 80329 | 59,6 | . 77495 | 58,6 | . 90487 | 32,2 | 36 33. 16.95 |
| . 639 | . 59639 | 80,3 | . 80269 | 59,6 | . 77553 | 58,5 | . 90455 | 32,3 | 363643.21 |
| 0.640 | 0.59720 | 80,2 | 0.80210 | 59,7 | 9.77612 | 58,3 | 9.90423 | 32,3 | 364009.48 |
| . 641 | . 59800 | 80, 1 | . 80150 | 59,8 | . 77670 | 58,2 | . 90390 | 32,4 | $3643 \quad 35.74$ |
| . 642 | . 59880 | 80, 1 | . 80090 | 59,9 | . 77728 | 58, I | . 90358 | 32,5 | 364702.01 |
| . 643 | . 59960 | 80,0 | . 80030 | 60,0 | . 77786 | 58,0 | . 90325 | 32,5 | 365028.27 |
| . 644 | . 60040 | 80,0 | . 79970 | 60,0 | . 77844 | 57,8 | . 90293 | 32,6 | $365354 \cdot 54$ |
| 0.645 | 0.60120 | 79,9 | 0.79910 | 60, 1 | 9.77902 | 57,7 | 9.90260 | 32,7 | 365720.80 |
| . 646 | . 60200 | 79,8 | . 79850 | 60,2 | . 77959 | '57,6 | . 90227 | 32,7 | 370047.06 |
| . 647 | . 60280 | 79,8 | . 79790 | 60,3 | . 78017 | 57,5 | .90195 | 32,8 | 370413.33 |
| . 648 | . 60359 | 79,7 | . 79729 | 60,4 | . 78074 | 57,4 | . 90162 | 32,9 | $3707 \begin{array}{llll}39 & 39 & 59\end{array}$ |
| . 649 | . 60439 | 79,7 | . 79669 | 60,4. | . 78132 | 57,2 | . 90129 | 32,9 | 37 II 05.86 |
| 0.650 | 0.60519 | 79,6 | 0.79608 | 60,5 | 9.78189 | 57, I | 9.90096 | 33,0 | 37 I4 32.12 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh$ iu | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.650 | 0.60519 | 79,6 | 0. 79608 | 60,5 | 9.78189 | 57,I | 9.90096 | 33,0 | $37^{\circ} 144^{\prime} 32^{\prime \prime} .12$ |
| . 651 | . 60598 | 79,5 | . 79548 | 60,6 | . 78246 | 57,0 | . 90063 | 33,1 | 371758.39 |
| . 652 | . 60678 | 79,5 | . 79487 | 60,7 | . 78303 | 56,9 | . 90030 | 33,2 | 372124.65 |
| . 653 | . 60757 | 79,4 | . 79426 | 60,8 | . 78360 | 56,8 | . 89997 | 33,2 | 372450.92 |
| . 654 | . 60837 | 79,4 | . 79366 | 60,8 | . 78416 | 56,7 | . 89963 | 33,3 | $37 \quad 28$ 17.18 |
| 0.655 | 0.60916 | 79,3 | 0.79305 | 60,9 | 9.78473 | 56,5 | 9.89930 | 33,4 | 373143.45 |
| . 656 | . 60995 | 79,2 | . 79244 | 61,0 | . 78530 | 56,4 | . 89897 | 33,4 | 373509.71 |
| . 657 | . 61074 | 79,2 | . 79183 | 61,1 | . 78586 | 56,3 | . 89853 | 33,5 | 373835.98 |
| . 658 | . 61154 | 79,1 | . 79122 | 61,2 | . 78642 | 56,2 | . 89830 | 33,6 | $3742 \quad 02.24$ |
| . 659 | .61233 | 79,1 | . 79060 | 61,2 | . 78698 | 56, I | . 89796 | 33,6 | 3745 28,51 |
| 0.660 | 0.61312 | 79,0 | 0.78999 | 61,3 | 9.78754 | 56,0 | 9.89762 | 33,7 | 374854.77 |
| . 661 | .61391 | 78,9 | . 78938 | 61,4 | . 78810 | 55,8 | . 89729 | 33,8 | 375221.04 |
| . 662 | . 61470 | 78,9 | . 78876 | 61,5 | . 78866 | 55,7 | . 89695 | 33,8 | $375547 \cdot 30$ |
| . 663 | . 61548 | 78,8 | . 78815 | 61,5 | . 78922 | 55,6 | . 89661 | 33,9 | $37 \quad 5913.57$ |
| . 664 | . 61627 | 78,8 | . 78753 | 61,6 | . 78977 | 55,5 | . 89627 | 34,0 | 380239.83 |
| 0.665 | 0.61706 | 78,7 | 0.78692 | 61,7 | 9.79033 | 55,4 | 9.89593 | 34, 1 | 380606.10 |
| . 666 | . 61785 | 78,6 | . 78630 | 61,8 | . 79088 | 55,3 | . 89559 | 34, | 380932.36 |
| . 667 | . 61853 | 78,6 | . 78568 | 61,9 | . 79143 | 55,2 | . 89525 | 34,2 | 381258.63 |
| . 668 | .61942 | 78,5 | . 78506 | 61,9 | - 79198 | 55,0 | . 89490 | 34, | 381624.89 |
| . 669 | . 62020 | 78,4 | . 78444 | 62,0 | . 79253 | 54,9 | . 89456 | 34,3 | 3819 51.16 |
| 0.670 | 0.62099 | 78,4 | 0.78382 | 62,1 | 9.79308 | 54,8 | 9.89422 | 34,4 | $38 \quad 2317.42$ |
| . 671 | . 62177 | 78,3 | . 78320 | 62,2 | . 79363 | 54,7 | . 89387 | 34,5 | $38 \quad 2643.68$ |
| . 672 | . 62255 | 78,3 | . 78258 | 62,3 | . 79418 | 54,6 | . 89353 | 34, | 383009.95 |
| . 673 | . 62333 | 78,2 | . 78196 | 62,3 | . 79472 | 54,5 | . 89318 | 34,6 | 3833 36.21 |
| . 674 | . 62412 | 78, 1 | . 78133 | 62,4 | . 79527 | 54,4 | . 89284 | 34,7 | 383702.48 |
| 0.675 | 0.6249 | 78,1 | 0.78071 | 62,5 | 9.79581 | 54,3 | 9.89249 | 34,8 | 384028.74 |
| . 676 | . 62568 | 78,0 | . 78008 | 62,6 | . 79635 | 54, I | . 89214 | 34,8 | 3843 55.01 |
| . 677 | . 62646 | 77,9 | . 77946 | 62,6 | . 79689 | 54,0 | . 89179 | 34,9 | 3847 21.27 |
| . 678 | . 62724 | 77,9 | . 77883 | 62,7 | . 79743 | 53,9 | . 89144 | 35,0 | 385047.54 |
| . 679 | . 62802 | 77,8 | . 77820 | 62,8 | . 79797 | 53,8 | . 89109 | 35,0 | 3854 I3.80 |
| 0.680 | 0.62879 | 77,8 | 0.77757 | 62,9 | 9.79851 | 53,7 | 9.89074 | 35,1 | 385740.07 |
| .681 | . 62957 | 77,7 | . 77694 | 63,0 | . 79904 | 53,6 | . 89039 | 35,2 | 39 or 06.33 |
| . 682 | . 63035 | 77,6 | .77631 | 63,0 | . 79958 | 53,5 | . 89004 | 35,3 | 390432.60 |
| . 683 | . 63112 | 77,6 | . 77568 | 63,1 | . 80011 | 53,4 | . 88968 | 35,3 | 390758.86 |
| . 684 | . 63190 | 77,5 | . 77505 | 63,2 | . 80065 | 53,3 | . 88933 | 35,4 | 39 II 25.13 |
| 0.685 | 0.63267 | 77,4 | 0.77442 | 63,3 | 9.80118 | 53,2 | 9.88898 | 35,5 | 39 I4 51.39 |
| . 686 | . 63345 | 77,4 | . 77379 | 63,3 | . 80171 | 53,1 | . 88852 | 35,6 | 391817.66 |
| . 687 | . 63422 | 77,3 | . 77315 | 63,4 | . 80224 | 52,9 | . 88826 | 35,6 | 392143.92 |
| . 688 | . 63499 | 77,3 | . 77252 | 63,5 | . 80277 | 52,8 | .88791 | 35,7 | 3925 10.19 |
| . 689 | . 63577 | 77,2 | . 77188 | 63,6 | . 80330 | 52,7 | . 88755 | 35,8 | 392836.45 |
| 0.690 | 0.63654 | 77,I | 0.77125 | 63,7 | 9.80382 | 52,6 | 9.83719 | 35,8 | 393202.72 |
| . 691 | . 63731 | 77,1 | . 77061 | 63,7 | . 80435 | 52,5 | . 88683 | 35,9 | 393528.98 |
| . 692 | . 63808 | 77,0 | . 76997 | 63,8 | . 80487 | 52,4 | . 88547 | 36,0 | 393855.25 |
| . 693 | . 63885 | 76,9 | . 76933 | 63,9 | . 80540 | 52,3 | .885ir | 36,1 | 3942 21.51 |
| . 694 | . 63962 | 76,9 | . 76869 | 64,0 | . 80592 | 52,2 | . 88575 | 36, 1 | 394547.78 |
| 0.695 | 0.64039 | 76,8 | 0.76805 | 64,0 | 9.80644 | 52, I | 9.88539 | 36,2 | 394914.04 |
| . 696 | . 64115 | 76,7 | . 76741 | 64, 1 | . 80695 | 52,0 | . 88503 | 36,3 | 395240.31 |
| . 697 | . 64192 | 76,7 | . 76677 | 64,2 | . 80748 | 51,9 | . 88467 | 36,4 | 395606.57 |
| . 698 | . 64269 | 76,6 | . 76613 | 64,3 | . 80800 | 51,8 | . 88430 | 36,4 | 395932.83 |
| . 699 | . 64345 | 76,5 | . 76549 | 64,3 | . 80852 | 51,7 | . 88394 | 36,5 | 400259.10 |
| 0.700 | 0.64422 | 76,5 | 0.76484 | 64,4 | 9.80903 | 51,6 | 9.88357 | 36,6 | 400625.36 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | 4 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.700 | 0.64422 | 76,5 | 0.76484 | 64,4 | 9.80903 | 51,6 | 9.88357 | 36,6 | $40^{\circ} 06^{\prime} 25^{\prime \prime} 36$ |
| . 701 | . 64498 | 76,4 | . 76420 | 64,5 | . 80955 | 51,5 | .88321 | 36,7 | 400951.63 |
| . 702 | . 64575 | 76,4 | . 76355 | 64,6 | .81006 | 5II,4 | . 88284 | 36,7 | 401317.89 |
| . 703 | . 64651 | 76,3 | . 76291 | 64,7 | .81057 | 51,2 | . 88247 | 36,8 | 401644.16 |
| . 704 | . 64727 | 76,2 | . 76226 | 64,7 | .8i 109 | 51, 1 | . 88210 | 36,9 | 402010.42 |
| 0.705 | 0.64803 | 76,2 | 0.76161 | 64,8 | 9.81160 | 51,0 | 9.88 I 73 | 37,0 | $\begin{array}{llll}40 & 23 & 36.69\end{array}$ |
| . 706 | . 64880 | 76,1 | . 76096 | 64,9 | .8I2II | 50,9 | .88ı36 | 37,0 | 402702.95 |
| . 707 | . 64956 | 76,0 | . 76031 | 65,0 | .81262 | 50,8 | . 88099 | 37, I | $40 \quad 30 \quad 29.22$ |
| . 708 | . 65032 | 76,0 | . 75966 | 65,0 | .81312 | 50,7 | . 88352 | 37,2 | $40 \quad 33 \quad 55.48$ |
| . 709 | . 65108 | 75,9 | . 75901 | 65, 1 | .81363 | 50,6 | . 88025 | 37,3 | 403721.75 |
| 0.710 | 0.65183 | 75,8 | 0.75836 | 65,2 | 9.81414 | 50,5 | 9.87988 | 37,3 | 404048.01 |
| .711 | . 65259 | 75,8 | . 75771 | 65,3 | .81464 | 50,4 | . 87950 | 37,4 | $40 \quad 4414.28$ |
| . 712 | . 65335 | 75,7 | . 75706 | 65,3 | .81515 | 50,3 | . 87913 | 37,5 | 404740.54 |
| . 713 | . 654 II | 75,6 | . 75640 | 65,4 | .8I565 | 50,2 | . 87875 | 37,6 | 40 51 06.8r |
| .714 | .65486 | 75,6 | . 75575 | 65,5 | .8I6I5 | 50, I | . 87838 | 37,6 | 40.5433 .07 |
| 0.715 | 0.65562 | 75,5 | 0.75509 | 65,6 | 9.81665 | 50,0 | 9.87800 | 37,7 | $40 \quad 5759.34$ |
| . 716 | . 65637 | 75,4 | . 75444 | 65,6 | .81715 | 49,9 | . 87762 | 37,8 | 41 OI 25.60 |
| . 717 | . 65713 | 75,4 | . 75378 | 65,7 | .81765 | 49,8 | . 87724 | 37,9 | $4 \mathrm{l} 045 \mathrm{5I} .87$ |
| . 718 | . 65788 | 75,3 | . 75312 | 65,8 | .81815 | 49,7 | . 87687 | 37,9 | 410818.13 |
| . 719 | . 65863 | 75,2 | . 75246 | 65,9 | .8I864 | 49,6 | . 87649 | 38,0 | 4I II 44.40 |
| 0.720 | 0.65938 | 75,2 | 0.7518 r | 65,9 | 9.81914 | 49,5 | 9.8761 I | 38,1 | 4 I I5 10.66 |
| . 721 | . 66014 | 75, 1 | .75115 | 66,0 | . 81963 | 49,4 | . 87572 | 38,2 | 4 I I8 36.93 |
| . 722 | . 66089 | 75,0 | . 75049 | 66, r | . 82013 | 49,3 | . 87534 | 38,2 | 412203.19 |
| . 723 | . 66164 | 75,0 | . 74982 | 66,2 | . 82052 | 49,2 | . 87496 | 38,3 | $4125 \quad 29.45$ |
| .724 | . 66239 | 74,9 | . 74916 | 66,2 | .82III | 49, I | . 87458 | 38,4 | 412855.72 |
| 0.725 | 0.66314 | 74,8 | 0.74850 | 66,3 | 9.82160 | 49,0 | 9.87419 | 38,5 | 413221.98 |
| . 726 | . 66388 | 74,8 | . 74784 | 66,4 | . 82209 | 48,9 | .87381 | 38,6 | 4 I 3548.25 |
| . 727 | . 66463 | 74,7 | . 74717 | 66,5 | . 82258 | 48,8 | . 87342 | 38,6 | 4 I 3914.51 |
| . 728 | . 66538 | 74,7 | . 74651 | 66,5 | . 82307 | 48,7 | . 87303 | 38,7 | 41 4240.78 |
| .729 | . 66612 | 74,6 | . 74584 | 66,6 | . 82356 | 48,6 | . 87265 | 38,8 | 41 4607.04 |
| 0.730 | 0.66687 | 74,5 | 0.74517 | 66,7 | 9.82404 | 48,5 | 9.87226 | 38,9 | $414933 \cdot 31$ |
| . 731 | .6676I | 74,5 | . 7445 I | 66,8 | . 82453 | 48,4 | . 87187 | 38,9 | 415259.57 |
| . 732 | . 66836 | 74,4 | . 74384 | 66,8 | . 82501 | 48,3 | . 87148 | 39,0 | 415625.84 |
| . 733 | . 66910 | 74,3 | . 74317 | 66,9 | . 82549 | 48,2 | . 87109 | 39, I | 4 I 5952.10 |
| . 734 | . 66984 | 74,3 | . .74250 | 67,0 | . 82597 | 48, I | . 87070 | 39,2 | 420318.37 |
| $0.735^{\circ}$ | 0.67059 | 74,2 | 0.74183 | 67, r | 9.82646 | 48,0 | 9.87030 | 39,3 | $42 \quad 0644.63$ |
| . 736 | . 67133 | 74,1 | . 74116 | 67, 1 | . 82694 | 47,9 | . 86991 | 39,3 | 42 10 10.90 |
| . 737 | . 67207 | 74,0 | . 74049 | 67,2 | . 82741 | 47,9 | . 86952 | 39,4 | 42 I3 37.16 |
| . 738 | . 67281 | 74,0 | . 73982 | 67,3 | . 82789 | 47,8 | . 86912 | 39,5 | $\begin{array}{llllll}42 & 17 & 03.43\end{array}$ |
| . 739 | . 67355 | 73,9 | . 73914 | 67,4 | . 82837 | 47,7 | .85873 | 39,6 | $42 \quad 20 \quad 29.69$ |
| 0.740 | 0.67429 | 73,8 | 0.73847 | 67,4 | 9.82885 | 47,6 | 9.86833 | 39,7 | $42 \quad 23 \quad 55.96$ |
| . 741 | . 67503 | 73,8 | . 73779 | 67,5 | . 82932 | 47,5 | . 86794 | 39,7 | 422722.22 |
| . 742 | . 67576 | 73,7 | . 73712 | 67,6 | . 82979 | 47,4 | . 85754 | 39,8 | 423048.49 |
| .743 | . 67650 | 73,6 | . 73644 | 67,7 | . 83027 | 47,3 | . 86714 | 39,9 | 423414.75 |
| . 744 | . 67724 | 73,6 | . 73577 | 67,7 | . 83074 | 47,2 | . 86674 | 40,0 | 423741.02 |
| 0.745 | 0.67797 | 73,5 | 0.73509 | 67,8 | 9.831211 | 47, I | 9.86634 | 40,0 | 424107.28 |
| . 746 | . 6787 I | 73,4 | . 7344 I | 67,9 | . 83168 | 47,0 | . 86594 | 40, I | $424433 \cdot 55$ |
| . 747 | . 67944 | 73,4 | . 73373 | 67,9 | . 83215 | 46,9 | . 86554 | 40,2 | 4247 59.81 |
| -748 | . 68017 | 73,3 | . 73305 | 68,0 | . 83262 | 46,8 | . 86513 | 40,3 | 425126.08 |
| . 749 | .68091 | 73,2 | . 73237 | 68,1 | .83309 | 46,7 | . 86473 | 40,4 | 425452.34 |
| 0.750 | 0.68164 | 73,2 | 0.73169 | 68,2 | 9.83355 | 46,6 | 9.86433 | 40,5 | $42 \quad 58 \quad 18.60$ |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $100 \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\boldsymbol{\operatorname { l o g }} \boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.750 | 0.68164 | 73,2 | 0.73169 | 68,2 | 9.83355 | 46,6 | 9.86433 | 40,5 | $42 \quad 58 \quad 18.60$ |
| .751 | . 68237 | 73, 1 | . 73101 | 68,2 | . 83402 | 46,5 | . 86392 | 40,5 | 43 O1 44.87 |
| . 752 | .68310 | 73,0 | . 73032 | 68,3 | . 83448 | 46,4 | . 86352 | 40,6 | 4305 II. 13 |
| . 753 | . 68383 | 73,0 | . 72964 | 68,4 | . 83495 | 46,3 | . 86311 | 40,7 | 430837.40 |
| . 754 | . 68456 | 72,9 | . 72896 | 68,5 | . 8354 I | 46,2 | . 86270 | 40,8 | 431203.66 |
| 0.755 | 0.68529 | 72,8 | 0.72827 | 68,5 | 9.83587 | 46,2 | 9.86229 | 40,9 | 431529.93 |
| . 756 | . 68602 | 72,8 | . 72759 | 68,6 | . 83633 | 46, I | .86I88 | 40,9 | 4318 56.19 |
| . 757 | . 68674 | 72,7 | . 72690 | 68,7 | .83679 | 46,0 | . 86147 | 41,0 | 432222.46 |
| . 758 | . 68747 | 72,6 | . 72621 | 68,7 | . 83725 | 45,9 | . 86106 | 4I, I | 432548.72 |
| . 759 | . 68820 | 72,6 | . 73552 | 68,8 | . 83771 | 45,8 | . 86065 | 41,2 | $43 \quad 2914.99$ |
| 0.760 | 0.68892 | 72,5 | 0.72484 | 68,9 | 9.83817 | 45,7 | 9.86024 | 41,3 | 433241.25 |
| . 761 | . 68965 | 72,4 | . 72415 | 69,0 | . 83863 | 45,6 | . 85983 | 4I,4 | $43 \quad 3607.52$ |
| . 762 | . 69037 | 72,3 | . 72346 | 69,0 | . 83908 | 45,5 | . 8594 I | 41,4 | $43 \quad 3933.78$ |
| . 763 | . 69109 | 72,3 | . 72277 | 69,1 | . 83954 | 45,4 | . 85900 | 41,5 | 434300.05 |
| . 764 | . 69182 | 72,2 | . 72207 | 69,2 | . 83999 | 45,3 | . 85858 | 41,6 | 434626.3 l |
| 0.765 | 0.69254 | 72, I | 0.72138 | 69,3 | 9.84044 | 45,2 | 9.85817 | 41,7 | 434952.58 |
| . 766 | . 69326 | 72, 1 | . 72069 | 69,3 | . 84089 | 45, I | . 85775 | 41,8 | $43 \quad 5318.84$ |
| .767 | . 69398 | 72,0 | . 72000 | 69,4 | . 84135 | 45, I | . 85733 | 41,9 | 435645.11 |
| . 768 | . 69470 | 71,9 | . 71930 | 69,5 | . 84180 | 45,0 | .85691 | $4 \mathrm{I}, 9$ | 440011.37 |
| . 769 | . 69542 | 71,9 | . 7186 I | 69,5 | . 84225 | 44,9 | . 85649 | 42,0 | $44 \quad 37.64$ |
| 0.770 | 0.69614 | 71,8 | 0.71791 | 69,6 | 9.84269 | 44,8 | 9.85607 | 42, I | 440703.90 |
| . 771 | . 69685 | 71,7 | . 71721 | 69,7 | . 84314 | 44,7 | . 85565 | 42,2 | 44 10 30.17 |
| . 772 | . 69757 | 71,7 | . 71652 | 69,8 | . 84359 | 44,6 | . 85523 | 42,3 | 44 I3 56.43 |
| . 773 | . 69829 | 71,6 | . 71582 | 69,8 | . 84403 | 44,5 | . 85480 | 42,4 | 441722.70 |
| . 774 | . 69900 | 71,5 | . 71512 | 69,9 | . 84448 | 44,4 | . 85438 | 42,5 | 442048.96 |
| 0.775 | 0.69972 | 71,4 | 0.71442 | 70,0 | 9.84492 | 44,3 | 9.85395 | 42,5 | 442415.22 |
| . 776 | . 70043 | 71,4 | . 71372 | 70,0 | . 845336 | 44,3 | . 85353 | 42,6 | 442741.49 |
| . 777 | . 70114 | 71,3 | . 71302 | 70,1 | .8458I | 44,2 | .85310 | 42,7 | 44 31 07.75 |
| . 778 | . 70186 | 71,2 | . 71232 | 70,2 | . 84625 | 44, I | . 85267 | 42,8 | 443434.02 |
| . 779 | . 70257 | 71,2 | . 71162 | 70,3 | . 84669 | 44,0 | . 85225 | 42,9 | 443800.28 |
| 0.780 | 0.70328 | 71,1 | 0.71091 | 70,3 | 9.84713 | 43,9 | 9.85182 | 43,0 | 444126.55 |
| .781 | . 70399 | 71,0 | . 71021 | 70,4 | . 84757 | 43,8 | . 85139 | 43,0 | 4444 52.81 |
| . 782 | . 70470 | 71,0 | . 70951 | 70,5 | . 84800 | 43,7 | . 85096 | 43, I | 444819.08 |
| . 783 | . 70541 | 70,9 | . 70880 | 70,5 | . 84844 | 43,6 | . 85052 | 43,2 | 445145.34 |
| . 784 | . 70612 | 70,8 | . 70809 | 70,6 | . 84888 | 43,6 | . 85009 | 43,3 | 4455 II.6I |
| 0.785 | 0.70683 | 70,7 | 0.70739 | 70,7 | 9.84931 | 43,5 | 9.84966 | 43,4 | $44 \quad 5837.87$ |
| . 786 | . 70753 | 70,7 | . 70668 | 70,8 | . 84975 | 43,4 | . 84922 | 43,5 | 450204.14 |
| .787 | . 70824 | 70,6 | . 70597 | 70,8 | . 85018 | 43,3 | . 84879 | 43,6 | 450530.40 |
| . 788 | . 70894 | 70,5 | . 70526 | 70,9 | .8506I | 43,2 | . 84835 | 43,7 | 450856.67 |
| . 789 | . 70965 | 70,5 | . 70456 | 71,0 | . 85104 | 43, I | . 84792 | 43,7 | $45 \quad 1222.93$ |
| 0.790 | 0.71035 | 70,4 | 0.70385 | 71,0 | 9.85147 | 43,0 | 9.84748 | 43,8 | 451549.20 |
| . 791 | . 71106 | 70,3 | . 70313 | 71, 1 | . 85190 | 42,9 | . 84704 | 43,9 | $45 \quad 1915.46$ |
| . 792 | . 71176 | 70,2 | . 70242 | 71,2 | . 85233 | 42,9 | . 84660 | 44,0 | 452241.73 |
| . 793 | . 71246 | 70,2 | . 70171 | 71,2 | . 85276 | 42,8 | . 84616 | 44, I | $45 \quad 26 \quad 07.99$ |
| . 794 | . 71316 | 70,1 | . 70100 | 71,3 | .85319 | 42,7 | . 84572 | 44,2 | $45 \quad 2934.26$ |
| 0.795 | 0.71386 | 70,0 | 0.70028 | 71,4 | 9.85362 | 42,6 | 9.84527 | 44,3 | 453300.52 |
| . 796 | . 71456 | 70,0 | . 69957 | 71,5 | . 85404 | 42,5 | . 84483 | 44,4 | $45 \quad 3626.79$ |
| . 797 | . 71526 | 69,9 | . 69886 | 71,5 | . 85447 | 42,4 | . 84439 | 44,4 | 453953.05 |
| . 798 | . 71596 | 69,8 | . 69814 | 71,6 | . 85489 | 42,3 | . 84394 | 44,5 | $\begin{array}{lllllllllll}45 & 43 & 19.32\end{array}$ |
| . 799 | . 71656 | 69,7 | . 69742 | 71,7 | .8553I | 42,3 | . 84350 | 44,6 | $454645 \cdot 58$ |
| 0.800 | 0.71736 | 69,7 | 0.69671 | 71,7 | 9.85573 | 42,2 | 9.84305 | 44,7 | $45 \quad 50 \quad 11.84$ |
| u | -isinhiu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$. | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| u | $\boldsymbol{s i n} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}^{\prime}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.800 | 0.71736 | 69,7 | 0.69671 | 71,7 | 9.85573 | 42,2 | 9.84305 | 44,7 | $45^{\circ} 50^{\prime} 11.1 .84$ |
| . 801 | . 71805 | 69,6 | . 69599 | 71,8 | . 85616 | 42,1 | . 84260 | 44,8 | 4553 38.11 |
| . 802 | . 71875 | 69,5 | . 69527 | 71,9 | . 85658 | 42,0 | . 84215 | 44,9 | $45 \quad 57 \quad 04.37$ |
| . 803 | . 71944 | 69,5 | . 69455 | 71,9 | . 85700 | 41,9 | . 84170 | 45,0 | 460030.64 |
| . 804 | . 72014 | 69,4 | . 69383 | 72,0 | . 85742 | 41,8 | . 84125 | 45, 1 | 460356.90 |
| 0.805 | 0.72083 | 69,3 | 0.69311 | 72, 1 | 9.85783 | 41,8 | 9.84080 | 45,2 | 460723.17 |
| . 806 | . 72152 | 69,2 | . 69239 | 72,2 | . 85825 | 41,7 | . 84035 | 45,3 | 46 10 49.43 |
| . 807 | . 72222 | 69,2 | . 69167 | 72,2 | . 85867 | 41,6 | . 83990 | 45,3 | $46 \quad 1415.70$ |
| . 808 | . 72291 | 69, 1 | . 69095 | 72,3 | . 85908 | 41,5 | . 83944 | 45,4 | 46 I7 41.96 |
| . 809 | . 72360 | 69,0 | . 69022 | 72,4 | . 85950 | 4'I,4 | . 83899 | 45,5 | 462108.23 |
| 0.810 | 0.72429 | 68,9 | 0.68950 | 72,4 | 9.85991 | 41,3 | 9.83853 | 45,6 | $46 \quad 2434.49$ |
| .8II | . 72498 | 68,9 | . 68877 | 72,5 | . 86032 | 4I,3 | . 83808 | 45,7 | $4628 \quad 00.76$ |
| . 8 I 2 | . 72566 | 68,8 | . 68805 | 72,6 | . 86074 | 4I,2 | . 83762 | 45,8 | 463127.02 |
| . 813 | . 72635 | 68,7 | . 68732 | 72,6 | .86II5 | 41, I | . 83716 | 45,9 | 463453.29 |
| .814 | .72704 | 68,7 | . 68660 | 72,7 | .85ı56 | 41,0 | . 83670 | 46,0 | 4638 19.55 |
| 0.815 | 0.72773 | 68,6 | 0.68587 | 72,8 | 9.86197 | 40,9 | 9.83624 | 46, 1 | 464145.82 |
| .816 | . 72841 | 68,5 | . 68514 | 72,8 | . 86238 | 40,8 | . 83578 | 46,2 | $46 \quad 45 \quad 12.08$ |
| . 817 | . 72910 | 68,4 | . 68441 | 72,9 | . 86278 | 40,8 | . 83532 | 46,3 | 464838.35 |
| . 818 | . 72978 | 68,4 | . 68368 | 73,0 | . 85319 | 40,7 | . 83485 | 46,4 | 465204.61 |
| . 819 | . 73046 | 68,3 | . 68295 | 73,0 | . 86360 | 40,6 | . 83439 | 46,5 | 465530.88 |
| 0.820 | $0.73 \mathrm{I} 5^{5}$ | 68,2 | 0.68222 | 73, 1 | 9.86400 | 40,5 | 9.83393 | 46,5 | 465857.14 |
| . 821 | . 73183 | 68, 1 | .68149 | 73,2 | . 86441 | 40,4 | . 83346 | 46,6 | $47 \quad 0223.41$ |
| . 822 | . 7325 I | 68, I | . 68076 | 73,3 | .8648I | 40,4 | . 83299 | 46,7 | 470549.67 |
| . 823 | . 73319 | 68,0 | . 68002 | 73,3 | . 86522 | 40,3 | . 83252 | 46,8 | $47 \quad 09 \quad 15.94$ |
| . 824 | . 73387 | 67,9 | . 67929 | 73,4 | . 86562 | 40,2 | . 83206 | 46,9 | 47 I2 42.20 |
| 0.825 | 0.73455 | 67,9 | 0.67856 | 73,5 | 9.86602 | 40, I | 9.83159 | 47,0 | $47 \quad 16 \quad 08.47$ |
| . 826 | . 73523 | 67,8 | . 67782 | 73,5 | . 86642 | 40,0 | .83112 | 47, 1 | 47 I9 34.73 |
| . 827 | . 73590 | 67,7 | . 67709 | 73,6 | . 86682 | 40,0 | . 83064 | 47,2 | $47 \quad 2300.99$ |
| . 828 | . 73658 | 67,6 | . 67635 | 73,7 | . 86722 | 39,9 | . 83017 | 47,3 | $47 \quad 26 \quad 27.26$ |
| . 829 | . 73726 | 67,6 | . 67561 | 73,7 | . 86762 | 39,8 | . 82970 | 47,4 | 472953.52 |
| 0.830 | 0.73793 | 67,5 | 0.67488 | 73,8 | 9.86802 | 39,7 | 9.82922 | 47,5 | 473319.79 |
| . 83 I | . 7386 r | 67,4 | . 67414 | 73,9 | . 8684 I | 39,6 | . 82875 | 47,6 | 473646.05 |
| . 832 | . 73928 | 67,3 | . 67340 | 73,9 | .8588I | 39,6 | . 82827 | 47,7 | $47 \quad 40$ 12.32 |
| . 833 | . 73995 | 67,3 | . 67266 | 74,0 | . 85920 | 39,5 | . 82779 | 47,8 | 474338.58 |
| . 834 | . 74062 | 67,2 | . 67192 | 74, 1 | . 86960 | 39,4 | . 82732 | 47,9 | $47 \quad 4704.85$ |
| 0.835 | 0.74130 | 67, 1 | 0.67118 | 74, I | 9.86999 | 39,3 | 9.82684 | 48,0 | 47503 I .11 |
| . 836 | . 74197 | 67,0 | . 67044 | 74,2 | . 87038 | 39,2 | . 82636 | 48,1 | 475357.38 |
| . 837 | . 74264 | 67,0 | . 66969 | 74,3 | . 87078 | 39,2 | . 82588 | 48,2 | 4757523.64 |
| . 838 | . 74331 | 66,9 | . 66895 | 74,3 | . 87117 | 39, 1 | . 82539 | 48,3 | 480049.91 |
| . 839 | . 74398 | 66,8 | . 6682 I | 74,4 | . 87156 | 39,0 | .82491 | 48,4 | 4804 I6.17 |
| 0.840 | 0.74464 | 66,7 | 0.66746 | 74,5 | 9.87195 | 38,9 | 9.82443 | 48,5 | $48 \quad 0742.44$ |
| . 841 | . 74531 | 66,7 | . 66672 | 74,5 | . 87234 | 38,8 | . 82394 | 48,5 | 48 II 08.70 |
| . 842 | . 74598 | 66,6 | . 66597 | 74,6 | . 87273 | 38,8 | . 82346 | 48,6 | 48 I4 34.97 |
| . 843 | . 74664 | 66,5 | . 66523 | 74,7 | .873II | 38,7 | . 82297 | 48,7 | 48 I8 or. 23 |
| . 844 | . 74731 | 66,4 | . 66448 | 74,7 | . 87350 | 38,6 | . 82248 | 48,8 | 482127.50 |
| 0.845 | 0.74797 | 66,4 | 0.66373 | 74,8 | 9.87388 | 38,5 | 9.82199 | 48,9 | 482453.76 |
| . 8.46 | . 74863 | 66,3 | . 66298 | 74,9 | . 87427 | 38,5 | . 82150 | 49,0 | $4828 \quad 20.03$ |
| . 847 | . 74930 | 66,2 | . 66223 | 74,9 | . 87465 | 38,4 | . 82 IOI | 49,1 | 48 31 46.29 |
| . 848 | .74996 | 66, 1 | . 66148 | 75,0 | . 87504 | 38,4 | . 82052 | 49,2 | $48 \quad 35 \quad 12.56$ |
| . 849 | . 75062 | 66, I | .66073 | 75, 1 | . 87542 | 38,2 | . 82003 | 49,3 | $48 \quad 38 \quad 38.82$ |
| 0.850 | 0.75128 | 66,o | 0.65998 | 75, I | 9.87580 | 38,2 | 9.81953 | 49,4 | 484205.09 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\boldsymbol{s i n} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.850 | 0.75128 | 66,0 | 0.65998 | 75,I | 9.87580 | 38,2 | 9.81953 | 49,4 | $48^{\circ} 42^{\prime} 05^{\prime \prime} .09$ |
| . 851 | . 75194 | 65,9 | . 65923 | 75,2 | . 87618 | 38, 1 | . 81904 | 49,5 | 484531.35 |
| . 852 | . 75260 | 65,8 | . 65848 | 75,3 | . 87656 | 38,0 | . 81854 | 49,6 | 484857.61 |
| . 853 | . 75326 | 65,8 | . 65773 | 75,3 | . 87694 | 37,9 | . 81805 | 49,7 | 485223.88 |
| . 854 | .75391 | 65,7 | . 65697 | 75,4 | . 87732 | 37,8 | . 81755 | 49,8 | 4855 50.14 |
| 0.855 | 0.75457 | 65,6 | 0.65622 | 75,5 | 9.87770 | 37,8 | 9.81705 | 49,9 | 4859 16.41 |
| . 856 | . 75523 | 65,5 | . 65546 | 75,5 | . 87808 | 37,7 | . 81655 | 50,0 | 490242.67 |
| . 857 | . 75588 | 65,5 | . 65471 | 75,6 | . 87845 | 37,6 | . 81605 | 50, I | 490608.94 |
| . 858 | . 75654 | 65,4 | . 65395 | 75,7 | . 87883 | 37,5 | . 81555 | 50,2 | 490935.20 |
| . 859 | . 75719 | 65,3 | . 65320 | 75,7 | . 87920 | 37,5 | . 81504 | 50,3 | 49 I3 or. 47 |
| 0.860 | 0.75784 | 65,2 | 0.65244 | 75,8 | 9.87958 | 37,4 | 9.81454 | 50,4 | 491627.73 |
| .86I | . 75849 | 65,2 | . 65168 | 75,8 | . 87995 | 37,3 | . 81403 | 50,5 | 49 19 54.00 |
| . 862 | . 75915 | 65,1 | . 65092 | 75,9 | . 88033 | 37,2 | . 81353 | 50,7 | 492320.26 |
| . 863 | . 75980 | 65,0 | . 65016 | 76,0 | . 88070 | 37,2 | . 81302 | 50,8 | 492646.53 |
| . 864 | . 76045 | 64,9 | . 64940 | 76,0 | .88107 | 37, I | .8125I | 50,9 | 493012.79 |
| 0.865 | 0.76110 | 64,9 | 0.64864 | 76,1 | 9.88144 | 37,0 | 9.81200 | 51,0 | 493339.06 |
| . 866 | . 76174 | 64,8 | . 64788 | 76,2 | . 8818 I | 36,9 | .81149 | 51, I | 493705.32 |
| . 867 | . 76239 | 64,7 | . 64712 | 76,2 | . 88218 | 36,9 | . 81098 | 51,2 | 494031.59 |
| . 868 | . 76304 | 64,6 | . 64635 | 76,3 | . 88255 | 36,8 | . 81047 | 51,3 | 494357.85 |
| . 869 | . 76368 | 64,6 | . 64559 | 76,4 | . 88291 | 36,7 | . 80996 | 51,4 | 4947 24.12 |
| 0.870 | 0.76433 | 64,5 | 0.64483 | 76,4 | 9.88328 | 36,6 | 9.80944 | 51,5 | 495050.38 |
| . 87 I | . 76497 | 64,4 | . 64406 | 76,5 | . 88365 | 36,6 | . 80893 | 51,6 | 4954 16.65 |
| . 872 | . 76562 | 64,3 | . 64330 | 76,6 | . 8840 II | 36,5 | . 8084 I | 51,7 | 495742.91 |
| . 873 | . 76626 | 64,3 | . 64253 | 76,6 | . 88438 | 36,4 | . 80789 | 51,8 | 50 or 09.18 |
| . 874 | . 76690 | 64,2 | . 64176 | 76,7 | . 88474 | 36,3 | . 80738 | 51,9 | $500435 \cdot 44$ |
| 0.875 | 0.76754 | -64,1 | 0.64100 | 76,8 | 9.88510 | 36,3 | 9.80686 | 52,0 | 5008 or. 71 |
| . 876 | . 76818 | 64,0 | . 64023 | 76,8 | . 88547 | 36,2 | . 80634 | 52, I | 50 II 27.97 |
| . 877 | . 76882 | 63,9 | . 63946 | 76,9 | . 88583 | 36,1 | .80581 | 52,2 | 50 $14 \begin{array}{ll}54.24 \\ 50\end{array}$ |
| . 878 | . 76946 | 63,9 | . 63869 | 76,9 | . 88519 | 36,0 | . 80529 | 52,3 | $5018 \quad 20.50$ |
| . 879 | . 77010 | 63,8 | . 63792 | 77,0 | . 88655 | 36,0 | . 80477 | 52,4 | 50 21 46.76 |
| 0.880 | 0.77074 | 63,7 | 0.63715 | 77,1 | 9.88691 | 35,9 | 9.80424 | 52,5 | 502513.03 |
| . 881 | . 77138 | 63,6 | . 63638 | 77, I | . 88727 | 35,8 | . 80372 | 52,6 | 502839.29 |
| . 882 | . 77201 | 63,6 | . 63561 | 77,2 | . 88762 | 35,8 | . 80319 | 52,7 | 503205.56 |
| . 883 | . 77265 | 63,5 | . 63484 | 77,3 | . 88798 | 35,7 | . 80266 | 52,9 | 503531.82 |
| . 884 | . 77328 | 63,4 | . 63406 | 77,3 | . 88834 | 35,6 | . 80213 | 53,0 | 503858.09 |
| 0.885 | 0.77391 | 63,3 | 0.63329 | 77,4 | 9.88869 | 35,5 | 9.80160 | 53, I |  |
| . 886 | . 77455 | 63,3 | . 63252 | 77,5 | . 88905 | 35,5 | . 80107 | 53,2 | 504550.62 |
| . 887 | . 77518 | 63,2 | . 63174 | 77,5 | . 88940 | 35,4 | . 80054 | 53,3 | 5049 16.88 |
| . 888 | .77581 | 63,1 | . 63096 | 77,6 | . 88976 | 35,3 | . 80001 | 53,4 | 505243.15 |
| . 889 | . 77644 | 63,0 | . 63019 | 77,6 | .8901 I | 35,2 | . 79947 | 53,5 | 505609.41 |
| 0.890 | 0.77707 | 62,9 | 0.62941 | 77,7 | 9.89046 | 35,2 | 9.79894 | 53,6 | 50. 5935.68 |
| . 891 | . 77770 | 62,9 | . 62863 | 77,8 | .89081 | 35, 1 | . 79840 | 53,7 | 510301.94 |
| . 892 | . 77833 | 62,8 | . 62786 | 77,8 | . 89116 | 35,0 | . 79786 | 53,8 | 5 I 0628.21 |
| . 893 | . 77896 | 62,7 | . 62708 | 77,9 | . 89151 | 35,0 | . 79732 | 53,9 | 5 I 0954.47 |
| . 894 | . 77958 | 62,6 | . 62630 | 78,0 | . 89186 | 34,9 | . 79678 | 54, 1 | 511320.74 |
| 0.895 | 0.78021 | 62,6 | 0.62552 | 78,0 | 9.80221 | 34,8 | 9.79624 | 54,2 | 511647.00 |
| . 896 | . 78083 | 62,5 | . 62474 | 78,1 | . 89256 | 34,7 | . 79570 | 54,3 | 512013.27 |
| . 897 | . 78146 | 62,4 | . 62396 | 78, 1 | . 89291 | 34,7 | . 79515 | 54,4 | 512339.53 |
| . 898 | . 78208 | 62,3 | . 62318 | 78,2 | . 89325 | 34,6 | . 79461 | 54,5 | $\begin{array}{lllll}51 & 27 & 05.80 \\ 51 & 30 & 32.06\end{array}$ |
| . 899 | . 78270 | 62,2 | . 62239 | 78,3 | . 89360 | 34,5 | . 79406 | 54,6 | 51 3032.06 |
| 0.900 | 0.78333 | 62,2 | 0.62161 | 78,3 | 9.89394 | 34,5 | 9.79352 | 54,7 | 51 3358.33 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega^{(1)} \mathrm{F}^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.900 | 0.78333 | 62,2 | 0.62161 | 78,3 | 9.89394 | 34,5 | 9.79352 | 54,7 | 51 ${ }^{\circ} 33$ ' 58.133 |
| . 901 | . 78395 | 62, I | . 62083 | 78,4 | . 89429 | 34,4 | . 79297 | 54,8 | $\begin{array}{lllllllllllllll}51 & 37 & 24.59\end{array}$ |
| . 902 | . 78457 | 62,0 | . 62004 | 78,5 | . 89463 | 34,3 | . 79242 | 55,0 | 514050.86 |
| . 903 | . 78519 | 61,9 | .61926 | 78,5 | . 89497 | 34,3 | . 79187 | 55, I | 5144 I7.12 |
| . 904 | .78581 | 6I,8 | . 61847 | 78,6 | . 89532 | 34,2 | .79132 | 55,2 | 514743.38 |
| 0.905 | 0.78643 | 6I,8 | 0.61769 | 78,6 | 9.89566 | 34, I | 9.79077 | 55,3 | 5I 51 09.65 |
| . 906 | . 78704 | 61,7 | . 61690 | 78,7 | . 89600 | 34,0 | . 79021 | 55,4 | 5 I 5435.9 I |
| . 907 | . 78766 | 6I,6 | .616i I | 78,8 | . 89634 | 34,0 | . 78966 | 55,5 | 51 58 02.18 |
| . 908 | . 78827 | 6I,5 | . 61532 | 78,8 | . 89668 | 33,9 | . 78910 | 55,6 | 52 OI 28.44 |
| . 909 | .78889 | 61,5 | . 61453 | 78,9 | .89702 | 33,8 | .78855 | 55,8 | 520454.71 |
| 0.910 | 0.78950 | 6I,4 | 0.61375 | 79,0 | 9.89735 | 33,8 | 9.78799 | 55,9 | $\begin{array}{llll}52 & 08 & 20.97\end{array}$ |
| .9II | . 79012 | 6I,3 | . 61296 | 79,0 | . 89769 | 33,7 | . 78743 | 56,0 | 52 II 47.24 |
| . 912 | . 79073 | 61,2 | .61217 | 79, 1 | . 89803 | 33,6 | . 78687 | 56, I | $\begin{array}{llll}52 & 15 & 13.50\end{array}$ |
| .913 | . 79134 | 61, 1 | .61137 | 79,1 | . 89836 | 33,6 | . 7863 I | 56,2 | $\begin{array}{llllllllllllllllllllll}52 & 18 & 39.77\end{array}$ |
| .914 | . 79195 | 61, I | . 61058 | 79,2 | . 89870 | 33,5 | . 78574 | 56,3 | 522206.03 |
| 0.915 | 0.79256 | 61,0 | 0.60979 | 79,3 | 9.89903 | 33,4 | 9.78518 | 56,4 | $\begin{array}{lll}52 & 25 & 32.30\end{array}$ |
| .916 | . 79317 | 60,9 | . 60900 | 79,3 | . 89937 | 33,3 | . 78462 | 56,6 | 522858.56 |
| .917 | . 79378 | 60,8 | . 60820 | 79,4 | .89970 | 33,3 | . 78405 | 56,7 | 523224.83 |
| . 918 | . 79439 | 60,7 | . 60741 | 79,4 | . 90003 | 33,2 | . 78348 | 56,8 | 5235151.09 |
| . 919 | . 79500 | 60,7 | . 60662 | 79,5 | . 90036 | 33, I | . 7829 I | 56,9 | 523917.36 |
| 0.920 | 0.79560 | 60,6 | 0.60582 | 79̊,6 | 9.90070 | 33, 1 | 9.78234 | 57,0 | 524243.62 |
| .92I | . 7962 I | 60,5 | . 60502 | 79,6 | . 90103 | 33,0 | .78177 | 57,2 | $5246 \quad 09.89$ |
| . 922 | . 7968 I | 60,4 | . 60423 | 79,7 | .90136 | 32,9 | .78120 | 57,3 | 524936.15 |
| . 923 | . 79742 | 60,3 | . 60343 | 79,7 | .90168 | 32,9 | .78063 | 57,4 | 525302.42 |
| . 924 | . 79802 | 60,3 | . 60263 | 79,8 | .90201 | 32,8 | . 78005 | 57,5 | $\begin{array}{lllll}52 & 56 & 28.68\end{array}$ |
| 0.925 | 0.79862 | 60,2 | 0.60183 | 79,9 | 9.90234 | 32,7 | 9.77948 | 57,6 | 525954.95 |
| . 926 | . 79922 | 60,1 | . 60104 | 79,9 | . 90267 | 32,7 | . 77800 | 57,7 | 530321.21 |
| .927 | . 79982 | 60,0 | . 60024 | 80,0 | . 90299 | 32,6 | . 77832 | 57,9 |  |
| . 928 | . 80042 | 59,9 | . 59944 | 80,0 | . 90332 | 32,5 | . 77774 | 58,0 | 53 10 13.74 |
| . 929 | . 80102 | 59,9 | . 59864 | 80, 1 | . 90364 | 32,5 | . 77716 | 58, I | 53 I3 40.01 |
| 0.930 | 0.80162 | 59,8 | 0.59783 | 80,2 | 9.90397 | 32,4 | 9.77658 | 58,2 | $\begin{array}{llll}53 & 17 & 06.27\end{array}$ |
| .93I | . 80222 | 59,7 | . 59703 | 80,2 | . 90429 | 32,3 | . 77600 | 58,4 | $\begin{array}{llll}53 & 20 & 32.53\end{array}$ |
| . 932 | . 8028 I | 59,6 | . 59623 | 80,3 | .9046I | 32,3 | . 77541 | 58,5 | 532358.80 |
| . 933 | . 80341 | 59,5 | . 59543 | 80,3 | . 90494 | 32,2 | . 77483 | 58,6 | 532725.06 |
| . 934 | . 80400 | 59,5 | . 59462 | 80,4 | . 90526 | 32, I | . 77424 | 58,7 | 533051.33 |
| 0.935 | 0.80460 | 59,4 | 0.59382 | 80,5 | 9.90558 | 32, I | 9.77365 | 58,8 | $\begin{array}{llll}53 & 34 & 17.59\end{array}$ |
| . 936 | . 80519 | 59,3 | . 5930I | 80,5 | . 90590 | 32,0 | . 77306 | 59,0 | $53 \quad 3743.86$ |
| . 937 | . 80579 | 59,2 | . 5922 I | 80,6 | . 90622 | $3 \mathrm{I}, 9$ | . 77247 | 59, I | 5341 10.12 |
| . 938 | . 80638 | 59, I | . 59140 | 80,6 | . 90654 | $3 \mathrm{I}, 9$ | . 77188 | 59,2 | 534436.39 |
| . 939 | . 80697 | 59,1 | . 59060 | 80,7 | . 90686 | 31,8 | . 77129 | 59,3 | 534802.65 |
| 0.940 | 0.80756 | 59,0 | 0.58979 | 80,8 | 9.90717 | 31,7 | 9.77070 | 59,5 | 535128.92 |
| . 941 | . 808I5 | 58,9 | . 58898 | 80,8 | . 90749 | 31,7 | . 77010 | 59,6 | 535455.18 |
| . 942 | . 80874 | 58,8 | . 588 I 7 | 80,9 | .9078I | 31,6 | . 76950 | 59,7 | 5358121.45 |
| . 943 | . 80932 | 58,7 | . 58736 | 80,9 | .90812 | 31,5 | . 7689 I | 59,8 | 54 O1 47.71 |
| . 944 | . 80991 | 58,7 | . 58655 | 81,0 | . 90844 | 31,5 | . 76831 | 60,0 | 540513.98 |
|  | 0.81050 | 58,6 | 0.58574 | $8 \mathrm{I}, 0$ | 9.90875 | 31,4 | 9.76771 | 60, I | 540840.24 |
| . 946 | .8iro8 | 58,5 | . 58493 | $8 \mathrm{I}, \mathrm{I}$ | . 90906 | 3I,3 | . 76711 | 60,2 | 541206.51 |
| . 947 | .81167 | 58,4 | . 58412 | 81,2 | . 90938 | 31,3 | . 76650 | 60,3 | 541532.77 |
| . 948 | .8I225 | 58,3 | . 58331 | 81,2 | . 90969 | 31,2 | . 76590 | 60,5 | 541859.04 |
| . 949 | . 81283 | 58,2 | . 58250 | 81,3 | . 91000 | 31, I | . 76529 | 60,6 | 542225.30 |
| 0.950 | 0.81342 | 58,2 | 0.58 I 68 | 8I,3 | 9.91031 | 31, I | 9.76469 | 60,7 | 542551.57 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | og cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

## Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.950 | 0.81342 | 58,2 | 0.58168 | 81,3 | 9.91031 | 3I, I | 9.76469 | 60,7 | $54^{\circ} 25^{\prime} 51.4 .57$ |
| . 951 | .81400 | 58,I | . 58087 | 81,4 | . 91062 | 31,0 | . 76408 | 60,9 | $54 \quad 2917.83$ |
| . 952 | .81458 | 58,0 | . 58006 | 81,5 | .91093 | 30,9 | . 76347 | 61,0 | 543244.10 |
| . 953 | .81516 | 57,9 | . 57924 | 81,5 | .91124 | 30,9 | . 76286 | 6I, 1 | $\begin{array}{lllllllllllllllll}54 & 36 & 10.36\end{array}$ |
| . 954 | .81574 | 57,8 | . 57842 | 81,6 | .91155 | 30,8 | . 76225 | 6r,2 | 543936.63 |
| 0.955 | 0.81631 | 57,8 | 0.57761 | 8r,6 | 9.91186 | 30,7 | 9.76163 | 61,4 | 544302.89 |
| . 956 | . 81689 | 57,7 | . 57679 | 81,7 | . 91216 | 30,7 | . 76102 | 61,5 | 5446 29.15 |
| . 957 | . 81747 | - 57,6 | . 57597 | 81,7 | .91247 | 30,6 | . 76040 | 6I,6 | 544955.42 |
| . 958 | .81804 | 57,5 | . 57516 | 8r,8 | .91278 | 30,5 | . 75979 | 61,8 | 545321.68 |
| . 959 | . 81862 | 57,4 | . 57434 | 8I,9 | .91308 | 30,5 | .75917 | 61,9 | 545647.95 |
| 0.960 | 0.81919 | 57,4 | 0.57352 | 81,9 | 9.91339 | 30,4 | 9.75855 | 62,0 | $5500 \cdot 14.21$ |
| . 961 | 0.81976 | 57,3 | . 57270 | 82,0 | .91369 | 30,3 | . 75793 | 62,2 | 550340.48 |
| . 962 | . 82034 | 57,2 | . 57188 | 82,0 | .91399 | 30,3 | . 75731 | 62,3 |  |
| . 963 | . 82091 | 57,1 | . 57106 | 82,1 | . 91429 | 30,2 | . 75668 | 62,4 | 55 10 33.01 |
| . 964 | . 82148 | 57,0 | . 57024 | 82,I | .91460 | 30,1 | . 75606 | 62,6 | $\begin{array}{lllllllllllll}55 & 13 & 59.27\end{array}$ |
| 0.965 | 0.82205 | 56,9 | 0.56942 | 82,2 | 9.91490 | 30,1 | 9.75543 | 62,7 | $\begin{array}{llll}55 & 17 & 25.54\end{array}$ |
| . 966 | . 82262 | 56,9 | . 56859 | 82,3 | .91520 | 30,0 | . 75480 | 62,8 | 552051.80 |
| . 967 | . 82319 | 56,8 | . 56777 | 82,3 | .91550 | 29,9 | . 75417 | 63,0 | $\begin{array}{llll}55 & 24 & 18.07\end{array}$ |
| . 968 | . 82375 | 56,7 | . 56695 | 82,4 | .91580 | 29,9 | . 75354 | 63,1 | 552744.33 |
| . 969 | . 82432 | 56,6 | . 566 I 2 | 82,4 | .91610 | 29,8 | .75291 | 63,2 | 553110.60 |
| 0.970 | 0.82489 | 56,5 | 0.56530 | 82,5 | 9.91639 | 29,8 | 9.75228 | 63,4 | $\begin{array}{llll}55 & 34 & 36.86\end{array}$ |
| . 971 | . 82545 | 56,4 | . 56447 | 82,5 | . 91669 | 29,7 | . 75164 | 63,5 | 5538 03.13 |
| . 972 | . 82601 | 56,4 | . 56365 | 82,6 | . 91699 | 29,6 | .75101 | 63,6 | 554129.39 |
| . 973 | . 82658 | 56,3 | . 56282 | 82,7 | .91728 | 29,6 | . 75037 | 63,8 | 554455.66 |
| . 974 | . 82714 | 56,2 | . 56200 | 82,7 | .91758 | 29,5 | . 74973 | 63,9 | 5548 21.92 |
| 0.975 | 0.82770 | 56,1 | 0.56117 | 82,8 | 9.91787 | 29,4 | 9.74909 | 64,1 | 55 51 48.19 |
| . 976 | . 82826 | 56,0 | . 56034 | 82,8 | .91817 | 29,4 | . 74845 | 64,2 | 555514.45 |
| . 977 | . 82882 | 56,0 | . 55951 | 82,9 | .91846 | 29,3 | . 74781 | 64,3 | 555840.72 |
| . 978 | . 82938 | 55,9 | . 55868 | 82,9 | .91875 | 29,2 | . 74717 | 64,5 | 560206.98 |
| . 979 | . 82994 | 55,8 | . 55785 | 83,0 | . 91905 | 29,2 | . 74652 | 64,6 | $56 \quad 533.25$ |
| 0.980 | 0.83050 | 55,7 | 0.55702 | 83,0 | 9.91934 | 29, I | 9.74587 | 64,8 | 560859.51 |
| .981 | . 83105 | 55,6 | . 55619 | 83,1 | . 91963 | 29, I | . 74522 | 64,9 | 56 I2 25.77 |
| . 982 | .83161 | 55,5 | . 55536 | 83,2 | .91992 | 29,0 | . 74457 | 65,0 | 56 I5 52.04 |
| . 983 | . 83216 | 55,5 | . 55453 | 83;2 | .92021 | 28,9 | . 74392 | 65,2 | $\begin{array}{llll}56 & 19 & 18.30\end{array}$ |
| . 984 | . 83272 | 55,4 | . 55370 | 83,3 | . 92050 | 28,9 | . 74327 | 65,3 | $56 \quad 2244.57$ |
| 0.985 | 0.83327 | 55,3 | 0.55286 | 83,3 | 9.92079 | 28,8 | 9.74262 | 65,5 | $\begin{array}{llll}56 & 2610.83\end{array}$ |
| . 986 | . 83382 | 55,2 | . 55203 | 83,4 | . 92107 | 28,8 | . 74196 | 65,6 | 5629 37.10 |
| . 987 | . 83438 | 55,1 | . 55120 | 83,4 | .92136 | 28,7 | . 7413 I | 65,7 | $5633 \quad 03.36$ |
| . 988 | . 83493 | 55,0 | . 55036 | 83,5 | . 92165 | 28,6 | . 74065 | 65,9 | 563629.63 |
| . 989 | . 83548 | 55,0 | . 54953 | 83,5 | . 92193 | 28,6 | . 73999 | 66,0 | 563955.89 |
| 0.990 | 0.83603 | 54,9 | 0.54869 | 83,6 | 9.92222 | 28,5 | 9.73933 | 66,2 | 564322.16 |
| . 991 | . 83657 | 54,8 | . 54785 | 83,7 | . 92250 | 28,4 | . 73866 | 66,3 | 564648.42 |
| . 992 | . 83712 | 54,7 | . 54702 | 83,7 | . 92279 | 28,4 | . 73800 | 66,5 | 565014.69 |
| . 993 | . 83767 | 54,6 | . 54618 | 83,8 | . 92307 | 28,3 | . 73734 | 66,6 | 565340.95 |
| . 994 | . 83821 | 54,5 | . 54534 | 83,8 | . 92335 | 28,3 | . 73667 | 66,8 | $56 \quad 5707.22$ |
|  | 0.83876 | 54,5 | 0.54450 | 83,9 | 9.92364 | 28,2 | 9.73600 | 66,9 | $57 \quad 0033.48$ |
| . 996 | . 83930 | 54,4 | . 54366 | 83,9 | . 92392 | 28, 1 | . 73533 | 67,0 | $\begin{array}{llllll}57 & 03 & 59.75\end{array}$ |
| . 997 | . 83985 | 54,3 | . 54282 | 84,0 | . 92420 | 28, 1 | . 73466 | 67,2 | 570726.01 |
| . 998 | . 84039 | 54,2 | . 54198 | 84,0 | . 92448 | 28,0 | . 73399 | 67,3 | 571052.28 |
| . 999 | . 84093 | 54, I | .54114 | 84,1 | . 92476 | 27,9 | .7333I | 67,5 | $\begin{array}{lllll}57 & 14 & 18.54\end{array}$ |
| 1.000 | 0.84147 | 54,0 | 0.54030 | 84, 1 | 9.92504 | 27,9 | 9.73264 | 67,6 | 57 I7 44.8I |
| u | -i sinh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.84147 | 54,0 | 0.54030 | 84,I | 9.92504 | 27,9 | 9.73264 | 67,6 | $57^{\circ} 17^{\prime} 44.81$ |
| . 001 | . 84201 | 53,9 | . 53946 | 84,2 | . 92532 | 27,8 | -.73196 | 67,8 | 572111.07 |
| . 002 | . 84255 | 53,9 | . 53862 | 84,3 | . 92560 | 27,8 | . 73128 | 67,9 | 572437.34 |
| . 003 | . 84309 | 53,8 | . 53778 | 84,3 | . 92587 | 27,7 | . 73060 | 68,1 | $57 \quad 2803.60$ |
| . 004 | . 84363 | 53,7 | . 53693 | 84,4 | .92615 | 27,6 | . 72992 | 68,2 | 573129.87 |
| 1.005 | 0.84416 | 53,6 | 0.53609 | 84,4 | 9.92643 | 27,6 | 9.72924 | 68,4 | 573456.13 |
| . 006 | . 84470 | 53,5 | . 53524 | 84,5 | . 92670 | 27,5 | . 72855 | 68,5 | $57 \quad 3822.40$ |
| . 007 | . 84523 | 53,4 | . 53440 | 84,5 | . 92698 | 27,5 | . 72787 | - 68,7 | 574148.66 |
| . 008 | . 84577 | 53.4 | . 53355 | 84,6 | . 92725 | 27,4 | . 72718 | 68,8 | $5745 \quad 14.92$ |
| . 009 | . 84630 | 53,3 | . 5327 I | 84,6 | . 92752 | 27,3 | . 72649 | 69,0 | 57484 I .19 |
| 1.010 | 0.84683 | 53,2 | 0.53186 | 84,7 | 9.92780 | 27,3 | 9.72580 | 69,1 | 575207.45 |
| . 011 | . 84736 | 53, 1 | . 53101 | 84,7 | . 92807 | 27,2 | .72511 | 69,3 | 575533.72 |
| . 012 | . 84789 | 53,0 | . 53017 | 84,8 | . 92834 | 27,2 | . 7244 I | 69,5 | 575859.98 |
| .013 | . 84842 | 52,9 | . 52932 | 84,8 | . 92851 | 27, I | . 72372 | 69,6 | $\begin{array}{llll}58 & 02 & 26.25\end{array}$ |
| . 014 | . 84895 | 52,8 | . 52847 | 84,9 | . 92888 | 27,0 | . 72302 | 69,8 | 5805 52.51 |
| 1.015 | 0.84948 | 52,8 | 0.52762 | 85,0 | 9.92915 | 27,0 | 9.72232 | 69,9 | $58 \quad 0918.78$ |
| . 016 | . 85001 | 52,7 | . 52677 | 85,0 | . 92942 | 26,9 | . 72162 | 70, 1 | 58 12 45.04 |
| . 017 | . 85053 | 52,6 | . 52592 | $85, \mathrm{I}$ | . 92969 | 26,9 | . 72092 | 70,2 | 58 I6 II. 31 |
| . 018 | .85106 | 52,5 | . 52507 | 85, I | . 92996 | 26,8 | . 72022 | 70,4 | $\begin{array}{llll}58 & 19 & 37.57\end{array}$ |
| . 019 | .85158 | 52,4 | . 52422 | 85,2 | . 93023 | 26,7 | . 71951 | 70,6 | $\begin{array}{llll}58 & 23 & 03.84\end{array}$ |
| 1.020 | 0.852 II | 52,3 | 0.52337 | 85,2 | 9.93049 | 26,7 | 9.7188 I | 70,7 | $58 \quad 26$ 30.10 |
| . 021 | . 85263 | 52,3 | . 52251 | 85,3 | . 93076 | 26,6 | . 71810 | 70,9 | 582956.37 |
| . 022 | . 85315 | 52,2 | . 52166 | 85,3 | .93103 | 26,6 | . 71739 | 71,0 | 583322.63 |
| . 023 | . 85367 | 52,1 | . 5208I | 85,4 | .93I29 | 26,5 | . 71668 | 71,2 | 583648.90 |
| . 024 | . 85419 | 52,0 | . 51995 | 85,4 | .93156 | 26,4 | . 71596 | 71,3 | 584015.16 |
| 1.025 | 0.8547 I | 51,9 | 0.51910 | 85,5 | 9.93182 | 26,4 | 9.71525 | 71,5 | 58434 I .43 |
| . 026 | . 85523 | 5I,8 | . 51824 | 85,5 | .93208 | 26,3 | . 71453 | 71,7 | 584707.69 |
| . 027 | . 85575 | 51,7 | . 51739 | 85,6 | . 93235 | 26,3 | . 71382 | 71,8 | 585033.96 |
| . 028 | . 85627 | 51,7 | . 51653 | 85,6 | .9326I | 26,2 | . 71310 | 72,0 | 585400.22 |
| . 029 | . 85678 | 51,6 | . 51568 | 85,7 | . 93287 | 26, 1 | . 71238 | 72,2 | 585726.49 |
| 1.030 | 0.85730 | 5I,5 | 0.51482 | 85,7 | 9.93313 | 26,1 | 9.71165 | 72,3 | 590052.75 |
| .031 | .85781 | 5I,4 | . 51396 | 85,8 | . 93339 | 26,0 | . 71093 | 72,5 | 590419.02 |
| . 032 | . 85833 | 51,3 | . 51310 | 85,8 | . 93365 | 25,0 | . 71020 | 72,6 | 590745.28 |
| . 033 | . 85884 | 51,2 | . 51224 | 85,9 | .9339I | 25,9 | . 70948 | 72,8 | 59 II II. 54 |
| . 034 | . 85935 | 5I,I | . 51139 | 85,9 | .934I7 | 25,8 | . 70875 | 73,0 | 59 I4 37.8I |
| 1.035 | 0.85986 | 5I, I | 0.51053 | 86,0 | 9.93443 | 25,8 | 9.70802 | 73,1 | $\begin{array}{llll}59 & 18 & 04.07\end{array}$ |
| . 036 | . 86037 | 51,0 | . 50967 | 86,0 | . 93469 | 25,7 | . 70729 | 73,3 | 592130.34 |
| . 037 | . 86088 | 50,9 | . 5088 I | 86, I | . 93494 | 25,7 | . 70655 | 73,5 | 592456.60 |
| . 038 | . 86139 | 50,8 | . 50794 | 86, | . 93520 | 25,6 | . 70582 | 73,6 | 592822.87 |
| . 039 | . 86190 | 50,7 | . 50708 | 86,2 | . 93546 | 25,6 | . 70508 | 73,8 | 59 31 49.13 |
| 1.040 | 0.86240 | 50,6 | 0.50622 | 85,2 | 9.93571 | 25,5 | 9.70434 | 74,0 | 5935 I5.40 |
| . 041 | . 86291 | 50,5 | . 50536 | 85,3 | . 93597 | 25,4 | . 70360 | 74,2 | 593841.66 |
| . 042 | . 8634 I | 50,4 | . 50449 | 8Ј,3 | . 93622 | 25,4 | . 70286 | 74,3 | 594207.93 |
| . 043 | . 86392 | 50,4 | . 50363 | 86,4 | . 93647 | 25,3 | .7021 I | 74,5 | 5945 34.19 |
| . 044 | . 86442 | 50,3 | . 50277 | 86,4 | . 93673 | 25,3 | . 70137 | 74,7 | 594900.46 |
| 1.045 | 0.86492 | 50,2 | 0.50190 | 86,5 | 9.93698 | 25,2 | 9.70062 | 74,8 | $59 \quad 52 \quad 26.72$ |
| . 046 | . 85543 | 50, I | . 50104 | 85,5 | . 93723 | 25, I | . 69987 | 75,0 | 595552.99 |
| . 047 | . 86593 | 50,0 | . 50017 | 86,6 | . 93748 | 25,1 | . 69912 | 75,2 | 595919.25 |
| . 048 | . 86643 | 49,9 498 | . 49930 | 86,6 86,7 | . 93773 | 25,0 | . 69837 | 75,4 | $\begin{array}{llll}60 & 02 & 45.52 \\ 60 & 06 & 11.78\end{array}$ |
| . 049 | .86693 | 49,8 | . 49844 | 86,7 | . 93798 | 25,0 | .6975I | 75,5 | 6006 II. 78 |
| 1.050 | 0.86742 | 49,8 | 0.49757 | 86,7 | 9.93823 | 24,9 | 9.69686 | 75,7 | 600938.05 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| 4 | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.050 | 0.86742 | 49,8 | 0.49757 | 86,7 | 9.93823 | 24,9 | 9.69686 | 75,7 | $60^{\circ} 09{ }^{\prime} 38^{\prime \prime} .05$ |
| .05I | . 86792 | 49,7 | . 49670 | 86,8 | . 93848 | 24,9 | . 69610 | 75,9 | 60 I3 04.31 |
| . 052 | . 86842 | 49,6 | . 49584 | 86,8 | . 93873 | 24,8 | . 69534 | 76, 1 | $60 \quad 1630.58$ |
| . 053 | . 86891 | 49,5 | . 49497 | 86,9 | . 93898 | 24,7 | . 69458 | 76,2 | $60 \quad 1956.84$ |
| . 054 | . 8694 I | 49,4 | .49410 | 86,9 | . 93922 | 24,7 | .6938I | 76,4 | 6023 23.1I |
| 1.055 | 0.86990 | 49,3 | 0.49323 | 87,0 | 9.93947 | 24,6 | 9.69305 | 76,6 | $60 \quad 2649.37$ |
| . 056 | . 87039 | 49,2 | . 49236 | 87,0 | . 93972 | 24,6 | . 69228 | 76,8 | 603015.64 |
| . 057 | . 87088 | 49, I | . 49149 | 87, 1 | . 93996 | 24,5 | . 69151 | 77,0 | 6033 41.90 |
| . 058 | . 87138 | 49, 1 | . 49062 | 87,1 | .9402I | 24,5 | . 69074 | 77, I | 603708.17 |
| . 059 | . 87187 | 49,0 | . 48974 | 87,2 | . 94045 | 24,4 | . 68997 | 77,3 | 604034.43 |
| 1.060 | 0.87236 | 48,9 | 0.48887 | 87,2 | 9.94069 | 24,3 | 9.68920 | 77,5 | 604400.69 |
| .06I | . 87284 | 48,8 | . 48800 | 87,3 | . 94094 | 24,3 | . 68842 | 77,7 | 604726.96 |
| . 062 | . 87333 | 48,7 | . 48713 | 87,3 | -94118 | 24,2 | .68764 | 77,9 | 605053.22 |
| . 063 | . 87382 | 48,6 | . 48625 | 87,4 | .94142 | 24,2 | . 68686 | 78,0 | 605419.49 |
| . 064 | . 87430 | 48,5 | . 48538 | 87,4 | .94166 | 24, I | . 68608 | 78,2 | 605745.75 |
| 1.065 | 0.87479 | 48,5 | 0.48450 | 87,5 | 9.94190 | 24, I | 9.68530 | 78,4 | 6r or 12.02 |
| . 066 | . 87527 | 48,4 | . 48363 | 87,5 | . 94214 | 24,0 | . 68451 | 78,6 | 6I 0438.28 |
| . 067 | . 87576 | 48,3 | . 48275 | 87,6 | . 94238 | 23,9 | . 68373 | 78,8 | 6 l 0804.55 |
| . 068 | . 87624 | 48,2 | .48188 | 87,6 | . 94262 | 23,9 | . 68294 | 79,0 | 6I II 30.8I |
| . 069 | . 87672 | 48,1 | .48100 | 87,7 | . 944286 | 23,8 | . 68215 | 79,2 | 6 I I4 57.08 |
| 1.070 | 0.87720 | 48,0 | 0.48012 | 87,7 | 9.94310 | 23,8 | 9.68135 | 79,3 | 61 1823.34 |
| . 071 | . 87768 | 47,9 | . 47925 | 87,8 | . 94334 | 23,7 | . 68056 | 79,5 | 612149.61 |
| . 072 | .87816 | 47,8 | . 47837 | 87,8 | . 943157 | 23,7 | . 67976 | 79,7 | 612515.87 |
| . 073 | . 87864 | 47,7 | . 47749 | 87,9 | . 94381 | 23,6 | .67896 | 79,9 | 612842.14 |
| . 074 | . 8791 I | 47,7 | .47661 | 87,9 | . 94405 | 23,6 | . 67816 | 80, I | 6I 3208.40 |
| 1.075 | 0.87959 | 47,6 | 0.47573 | 88,0 | 9.94428 | 23,5 | 9.67736 | 80,3 | 6 l 3534.67 |
| . 076 | . 88007 | 47,5 | . 47485 | 88,0 | .9445I | 23,4 | . 67656 | 80,5 | 613900.93 |
| . 077 | . 88054 | 47,4 | . 47397 | 88, 1 | . 94475 | 23,4 | . 67575 | 80,7 | 61 4227.20 |
| . 078 | . 88 IOI | 47,3 | . 47309 | 88, I | . 94498 | 23,3 | . 67494 | 80,9 | 6I 4553.46 |
| . 079 | . 88149 | 47,2 | .4722I | 88, 1 | . 94522 | 23,3 | . 67414 | 81, 1 | 6149 19.73 |
| 1.080 | 0.88196 | 47, I | 0.47133 | 88,2 | 9.94545 | 23,2 | 9.67332 | 8r,3 | 6I 5245.99 |
| .08I | . 88243 | 47,0 | . 47045 | 88,2 | . 94568 | 23,2 | . 67251 | 8I,5 | 615612.26 |
| . 082 | . 88290 | 47,0 | . 46956 | 88,3 | .9459I | 23, 1 | . 67169 | $8 \mathrm{I}, 7$ | 615938.52 |
| . 083 | . 88337 | 46,9 | . 46868 | 88,3 | .94614 | 23,0 | . 67088 | 81,9 | 620304.79 |
| . 084 | . 88384 | 46,8 | . 46780 | 88,4 | . 94637 | 23,0 | . 67006 | 82,I | 620631.05 |
| 1.085 | 0.88430 | 46,7 | 0.46691 | 88,4 | 9.94660 | 22,9 | 9.66924 | 82,3 | 620957.31 |
| . 086 | . 88477 | 46,6 | . 46603 | 88,5 | . 94683 | 22,9 | . 66841 | 82,5 | 62 I3 23.58 |
| . 087 | . 88524 | 46,5 | . 46514 | 88,5 | . 94706 | 22,8 | . 66759 | 82,7 | 621649.84 |
| . 088 | . 88570 | 46,4 | . 46426 | 88,6 | . 947729 | 22,8 | . 66676 | 82,9 | 6220 I6.11 |
| . 089 | . 88616 | 46,3 | . 46337 | 88,6 | .9475I | 22,7 | . 66593 | 83, 1 | $62 \quad 2342.37$ |
| 1.090 | 0.88663 | 46,2 | 0.46249 | 88,7 | 9.94774 | 22,7 | 9.66510 | 83,3 | $62 \quad 27 \quad 08.64$ |
| .091 | . 88709 | 46,2 | . 46160 | 88,7 | . 94797 | 22,6 | . 66426 | 83,5 | 623034.90 |
| . 092 | . 88755 | 46, I | . 46071 | 88,8 | .94819 | 22,5 | . 66343 | 83,7 | 6234 OI. 17 |
| . 093 | . 88801 | 46,0 | . 45982 | 88,8 | . 94842 | 22,5 | . 66259 | 83,9 | $6237 \quad 27.43$ |
| . 094 | . 88847 | 45,9 | . 45894 | 88,8 | . 94864 | 22,4 | .66I75 | 84, 1 | 624053.70 |
| 1.095 | 0.88893 | 45,8 | 0.45805 | 88,9 | 9.94887 | 22,4 | 9.66091 | 84,3 | 624419.96 |
| . 096 | . 88939 | 45,7 | . 45716 | 88,9 | . 94909 | 22,3 | . 66007 | 84,5 | 624746.23 |
| . 097 | . 88984 | 45,6 | . 45627 | 89,0 | .9493' | 22,3 | . 65922 | 84,7 | $62 \quad 51 \quad 12.49$ |
| . 098 | . 89030 | 45,5 | . 45538 | 80,0 | -94954 | 22,2 | . 65837 | 84,9 | 625438.76 |
| . 099 | . 89075 | 45,4 | . 45449 | 89,I | . 94976 | 22,2 | . 65752 | 85, 1 | 625805.02 |
| 1. 100 | 0.8912 I | 45,4 | 0.45360 | 89, 1 | 9.94998 | 22, I | 9.65667 | 85,3 | 63 or 31.29 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh \mathrm{iu}}{i}$ | $\omega F_{0}{ }^{\prime}$ | 100 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| $u$ | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\circ}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 100 | 0.89121 | 45,4 | 0.45360 | 89, I | 9.94998 | 22,I | 9.65667 | 85,3 | $63^{\circ}$ O1' 31.1 .29 |
| . 101 | . 89166 | 45,3 | . 45270 | 89,2 | . 95020 | 22,0 | . 6558 I | 85,5 | 630457.55 |
| . 102 | . 8921 I | 45,2 | .4518I | 89,2 | . 95042 | 22,0 | . 65496 | 85,8 | 630823.82 |
| . 103 | . 89256 | 45, I | . 45092 | 89,3 | . 95054 | 21,9 | . 65410 | 86,0 | 63 II 50.08 |
| . 104 | . 89301 | 45,0 | . 45003 | 89,3 | . 95086 | 21,9 | . 65324 | 86,2 | 631516.35 |
| I. 105 | 0.89346 | 44,9 | 0.44913 | 89,3 | 9.95108 | 21,8 | 9.65238 | 86,4 | 631842.61 |
| . 106 | .89391 | 44,8 | . 44824 | 89,4 | .95130 | 21,8 | .65151 | 86,6 | $63 \quad 2208.88$ |
| . 107 | . 89436 | 44,7 | . 44735 | 89,4 | .95151 | 21,7 | . 65064 | 86,8 | 6325 35.14 |
| . 108 | . 89481 | 44,6 | . 44645 | 89,5 | .95173 | 21,7 | . 64977 | 87,0 | 6329 OI. 4 I |
| . 109 | . 89525 | 44,6 | . 44556 | 89,5 | .95195 | 21,6 | . 64890 | 87,3 | 633227.67 |
| I. 110 | 0.89570 | 44,5 | 0.44466 | 89,6 | 9.95216 | 21,6 | 9.64803 | 87,5 | $63 \quad 3553.93$ |
| . III | . 89614 | 44,4 | . 44377 | 89,6 | . 95238 | 21,5 | . 64715 | 87,7 | 633920.20 |
| . II 2 | . 89559 | 44,3 | . 44287 | 89,7 | . 95259 | 21,5 | .64628 | 87,9 | 634246.46 |
| . II3 | . 89703 | 44,2 | . 44197 | 89,7 | .95281 | 21,4 | . 64540 | 88, 1 | 6346 1.2.73 |
| . 114 | . 89747 | 44, I | . 44108 | 89,7 | . 95302 | 21,3 | .6445 1 | 88,4 | 634938.99 |
| I.II5 | 0.89791 | 44,0 | 0.44018 | 89,8 | 9.95323 | 2I,3 | 9.64363 | 88,6 | 635305.26 |
| . 116 | . 89835 | 43,9 | . 43928 | 89,8 | . 95345 | 21,2 | . 64274 | 88,8 | 635631.52 |
| . 117 | . 89879 | 43,8 | . 43838 | 89,9 | . 95366 | 21,2 | .64185 | 89,0 | 635957.79 |
| . 118 | . 89923 | 43,7 | . 43748 | 89,9 | . 95387 | 21,1 | . 64096 | 89,3 | 640324.05 |
| . 119 | . 89966 | 43.7 | . 43658 | 90,0 | . 95408 | 21,1 | . 64007 | 89,5 | 640650.32 |
| I. 120 | 0.90010 | 43,6 | 0.43568 | 90,0 | 9.95429 | 21,0 | 9.63917 | 89,7 | 641016.58 |
| . 121 | . 90054 | 43,5 | . 43478 | 90, 1 | . 95450 | 21,0 | . 63827 | 90,0 | 641342.85 |
| . 122 | . 90097 | 43,4 | . 43388 | 90, I | .95471 | 20,9 | . 63737 | 90,2 | 641700.11 |
| . 123 | .90140 | 43,3 | . 43298 | 90,1 | . 95492 | 20,9 | . 63647 | 90,4 | 642035.38 |
| . 124 | . 90184 | 43,2 | . 43208 | 90,2 | . 95513 | 20,8 | . 63556 | 90,6 | 642401.64 |
| 1. 125 | 0.90227 | 43, I | 0.43118 | 90,2 | 9.95534 | 20,8 | 9.63466 | 90,9 | $64 \quad 27 \quad 27.91$ |
| . 126 | . 90270 | 43,0 | . 43027 | 90,3 | . 95554 | 20,7 | . 63375 | 91, I | 643054.17 |
| . 127 | . 90313 | 42,9 | . 42937 | 90,3 | . 95575 | 20,6 | . 63283 | 91,3 | 643420.44 |
| . 128 | . 90356 | 42,8 | . 42847 | 90,4 | . 95596 | 20,6 | . 63192 | 91,6 | 643746.70 |
| . 129 | . 90398 | 42,8 | . 42756 | 90,4 | . 95616 | 20,5 | . 63100 | 91,8 | 64 41 12.97 |
| 1. 130 | 0.9044 I | 42,7 | 0.42666 | 90,4 | 9.95637 | 20,5 | 9.63008 | 92,I | 644439.23 |
| . 131 | . 90484 | 42,6 | . 42576 | 90,5 | . 95657 | 20,4 | . 62916 | 92,3 | 644805.50 |
| . 132 | . 90526 | 42,5 | . 42485 | 90,5 | . 95678 | 20,4 | . 62824 | 92,5 | 645131.76 |
| . I33 | . 90569 | 42,4 | . 42394 | 90,6 | . 95698 | 20,3 | .6273I | 92,8 | 645458.03 |
| . 134 | . 906 II | 42,3 | . 42304 | 90,6 | .95718 | 20,3 | . 62638 | 93,0 | 645824.29 |
| 1.135 | 0.90653 | 42,2 | 0.42213 | 90,7 | 9.95738 | 20,2 | 9.62545 | 93,3 | 65 or 50.56 |
| . 136 | . 90696 | 42,1 | . 42123 | 90,7 | . 95759 | 20,2 | .62451 | 93,5 | 650516.82 |
| . 137 | . 90738 | 42,0 | . 42032 | 90,7 | . 95779 | 20,1 | . 62358 | 93,8 | 650843.08 |
| . 138 | . 90780 | 41,9 | . 41941 | 90,8 | . 95799 | 20, I | . 62264 | 94,0 | 65 I2 09.35 |
| . 139 | . 90822 | 41,9 | .41850 | 90,8 | .95819 | 20,0 | . 62170 | 94,2 | 65 15 35.61 |
| I. 140 | 0.90863 | 41,8 | 0.41759 | 90,9 | 9.95839 | 20,0 | 9.62075 | 94,5 | 65 19 oi. 88 |
| . 141 | . 90905 | 41,7 | . 41669 | 90,9 | . 95859 | 19,9 | . 61981 | 94,7 | $65 \quad 22 \quad 28.14$ |
| . 142 | . 90947 | 41,6 | .41578 | 90,9 | . 95879 | 19,9 | . 61886 | 95,0 | 652554.41 |
| . 143 | . 90988 | 41,5 | . 41487 | 91,0 | . 95899 | 19,8 | .61791 | 95,2 | $65 \quad 2920.67$ |
| . 144 | .91030 | 41,4 | .41396 | 91,0 | . 95918 | 19,7 | .61695 | 95,5 | 653246.94 |
| I. I45 | 0.91071 | 4I,3 | 0.41305 | 91, I | 9.95938 | 19,7 | 9.61600 | 95,8 | $65 \quad 3613.20$ |
| . 146 | .91112 | 41,2 | . 41214 | 91, I | . 95958 | 19,6 | . 61504 | 96,0 | 653939.47 |
| . 147 | .91153 | 4I, I | .41122 | 91,2 | . 95977 | 19,6 | .61408 | 96,3 | 654305.73 |
| . 148 | .91195 | 41,0 | . 41031 | 91,2 | . 95997 | 19,5 | .613II | 96,5 | 654632.00 |
| . 149 | . 91235 | 40,9 | . 40940 | 91,2 | .96016 | 19,5 | . 61215 | 96,8 | 654958.26 |
| 1.150 | 0.91276 | 40,8 | 0.40849 | 91,3 | 9.96036 | 19,4 | 9.61118 | 97,0 | $65 \quad 53 \quad 24.53$ |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh$ iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| $u$ | $\boldsymbol{\operatorname { s i n }} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 150 | 0.91 .276 | 40,8 | 0.40849 | 91,3 | 9.96036 | 19,4 | 9.6III8 | 97,0 | $65^{\circ} 53 \cdot 24^{\prime \prime} 53$ |
| .15I | .91317 | 40,8 | . 40757 | 91,3 | . 96055 | 19,4 | .61021 | 97,3 | $65 \quad 5650.79$ |
| . 152 | .91358 | 40,7 | . 40566 | 9I,4 | . 96075 | 19,3 | . 60923 | 97,6 | 660017.06 |
| . 153 | . 91399 | 40,6 | . 40575 | 91,4 | . 96094 | 19,3 | . 60826 | 97,8 | $660343 \cdot 32$ |
| . 154 | . 91439 | 40,5 | . 40483 | 91,4 | . 96113 | 19,2 | . 60728 | 98, 1 | 660709.59 |
| I. 155 | 0.91479 | 40,4 | 0.40392 | 91,5 | 9.96132 | 19,2 | 9.60629 | 98,4 | 66 10 35.85 |
| . 156 | . 91520 | 40,3 | . 40300 | 91;5 | . 96152 | 19,I | . 60531 | 98,6 | 66 14 02.12 |
| . 157 | . 91560 | 40,2 | . 40209 | 91,6 | .96I7I | I9, I | . 60432 | 98,9 | 6617128.38 |
| . 158 | . 91600 | 40,1 | . 40117 | 91,6 | . 96190 | 19,0 | . 60333 | 99,2 | $66 \quad 2054.65$ |
| . 159 | .91640 | 40,0 | . 40026 | 91,6 | . 96209 | 19,0 | . 60234 | 99,4 | 662420.91 |
| 1. 160 | 0.91680 | 39,9 | 0.39934 | 91,7 | 9.96228 | 18,9 | 9.60134 | 99,7 | 662747.18 |
| . 161 | .91720 | 39,8 | . 39842 | 91,7 | . 96246 | 18,9 | . 60034 | 100,0 | 663113.44 |
| . 162 | . 91760 | 39,8 | -3975I | 91,8 | . 96265 | 18,8 | . 59934 | 100,3 | 663439.70 |
| .163 | . 91800 | 39,7 | . 39659 | 91,8 | . 96284 | I8,8 | . 59834 | 100,5 | $6638 \quad 05.97$ |
| . 164 | .91839 | 39,6 | . 39567 | 91,8 | .96303 | 18,7 | - 59733 | 100,8 | 664132.23 |
| I. 165 | 0.91879 | 39,5 | 0.39475 | 91,9 | 9.96322 | 18,7 | 9.59632 | IOI, 1 | 664458.50 |
| . 166 | . 91918 | 39,4 | . 39383 | 91,9 | . 96340 | 18,6 | . 5953 I | IOI, 4 | 664824.76 |
| . 167 | . 91958 | 39,3 | . 39291 | 92,0 | . 96359 | 18,6 | . 59430 | 101,6 | 66 51 51.03 |
| . 168 | . 91997 | 39,2 | . 39199 | 92,0 | . 96377 | 18,5 | . 59328 | 101,9 | 665517.29 |
| . 169 | .92036 | 39, I | . 39107 | 92,0 | . 96396 | 18,5 | . 59226 | 102,2 | $665843 \cdot 56$ |
| I. 170 | 0.92075 | 39,0 | 0.39015 | 92,1 | 9.96414 | 18,4 | 9.59123 | 102,5 | $\begin{array}{llll}67 & 02 & 09.82\end{array}$ |
| . 171 | .92II4 | 38,9 | . 38923 | 92,1 | . 96433 | 18,4 | . 59021 | 102,8 | $6705 \quad 36.09$ |
| . 172 | . 92153 | 38,8 | .3883I | 92,2 | .9645I | 18,3 | - 58918 | 103, I | 670902.35 |
| .173 | . 92192 | 38,7 | . 38739 | 92,2 | .96469 | 18,2 | . 588 I 5 | 103,4 | 67 I2 28.62 |
| . 174 | .92230 | 38,6 | . 38647 | 92,2 | .96487 | 18,2 | . 587 II | 103,6 | 67 I5 54.88 |
| 1.175 | 0.92269 | 38,6 | 0. 38554 | 92,3 | 9.96506 | 18, 1 | 9.58607 | 103,9 | 671921.15 |
| . I'76 | .92307 | 38,5 | . 38462 | 92,3 | . 96524 | 18, I | . 58503 | 104,2 | 672247.41 |
| .177 | .92346 | 38,4 | . 38370 | 92,3 | . 96542 | 18,0 | . 58399 | 104,5 | 672613.68 |
| . 178 | .92384 | 38,3 | . 38277 | 92,4 | . 96560 | 18,0 | . 58294 | IO4,8 | 672939.94 |
| . I79 | .92422 | 38,2 | . 38185 | 92,4 | . 96578 | 17,9 | . 58189 | 105, I | 673306.21 |
| 1. 180 | 0.9246 I | 38, I | 0.38092 | 92,5 | 9.96596 | 17,9 | 9.58084 | 105,4 | 673632.47 |
| . 18 I | . 92499 | 38,0 | . 38000 | 92,5 | . 95614 | 17,8 | . 57978 | 105,7 | 673958.74 |
| . 182 | . 92537 | 37,9 | - 37907 | 92,5 | . 9663 I | 17,8 | . 57872 | 106,0 | 674325.00 |
| .183 | . 92574 | 37,8 | . 37815 | 92,6 | .96649 | 17,7 | . 57766 | 106,3 | 6746 5.1.27 |
| . 184 | .92612 | 37,7 | - 37722 | 92,6 | . 96667 | 17,7 | . 57660 | 106,6 | 6750 I7.53 |
| I. 185 | 0.92650 | 37,6 | 0.37630 | 92,6 | 9.96684 | 17,6 | 9.57553 | 106,9 | 675343.80 |
| . 186 | . 92687 | 37,5 | . 37537 | 92,7 | . 96702 | 17,6 | . 57446 | 107,2 | 675710.06 |
| . 187 | . 92725 | 37,4 | - 37444 | 92,7 | . 96720 | 17,5 | - 57339 | 107,5 | $68 \quad 0036.33$ |
| . 188 | .92762 | 37,4 | - 37352 | 92,8 | . 96737 | 17,5 | . 5723 I | 107,9 | $\begin{array}{llll}68 & 04 & 02.59\end{array}$ |
| . 189 | . 92800 | 37,3 | . 37259 | 92,8 | . 9675 | 17,4 | . 57123 | 108,2 | $68 \quad 07 \quad 28.85$ |
| I. 190 | 0.92837 | 37,2 | 0.37166 | 92,8 | 9.96772 | 17,4 | 9.57015 | 108,5 | 68 10 55.12 |
| . 191 | . 92874 | 37, 1 | . 37073 | 92,9 | . 96789 | 17,3 | . 56906 | 108,8 | $68 \quad 14121.38$ |
| . 192 | .929I'I | 37,0 | . 36980 | 92,9 | . 96807 | 17,3 | . 56797 | I09, I | 681747.65 |
| . 193 | . 92948 | 36,9 | . 36887 | 92,9 | . 96824 | 17,2 | . 56688 | 109,4 | 68 21 13.91 |
| . 194 | .92985 | 36,8 | . 36794 | 93,0 | . 9684 I | 17,2 | . 56578 | 109,8 | 682440.18 |
| I. 195 | 0.93022 | 36,7 | 0.36701 | 93,0 | 9.96858 | 17,I | 9. 56468 | IIO, I | $68 \quad 2806.44$ |
| . 196 | . 93058 | 36,6 | . 36608 | 93,I | . 96875 | 17,1 | . 56358 | 110,4 | 683132.71 |
| . 197 | . 93095 | 36,5 | . 36515 | 93, I | . 96893 | 17,0 | . 56247 | I 10,7 | 683458.97 |
| . 198 | .93131 | 36,4 | . 36422 | 93, I | . 96910 | 17,0 | . 56137 | III, 0 | $68 \quad 38 \quad 25.24$ |
| . 199 | .93168 | 36,3 | . 36329 | 93,2 | .96927 | 16,9 | . 56025 | I I I, 4 | 68 4I 5I. 50 |
| 1.200 | 0.93204 | 36,2 | 0.36236 | 93,2 | 9.96943 | 16,9 | $9 \cdot 55914$ | II I,7 | $68 \quad 45 \quad 17.77$ |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log $\frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| 4 | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.200 | 0.93204 | 36,2 | 0.36236 | 93,2 | 9.96943 | 16,9 | 9.55914 | I I I,7 | $68^{\circ} 45^{\prime} 177^{\prime \prime} .77$ |
| . 201 | . 93240 | 36, I | . 36143 | 93,2 | . 96960 | 16,8 | . 558802 | I 12,0 | 684844.03 |
| . 202 | . 93276 | 36,0 | . 36049 | 93,3 | . 96977 | 16,8 | . 55690 | I 12,4 | 6852 10.30 |
| . 203 | .933I2 | 36,0 | . 35956 | 93,3 | . 96994 | 16,7 | . 55577 | I 12,7 | 685536.56 |
| . 204 | . 93348 | 35,9 | . 35863 | 93,3 | .9701 1 | 16,7 | . 55464 | I 13,0 | 685902.83 |
| I. 205 | 0.93384 | 35,8 | 0.35769 | 93,4 | 9.97027 | 16,6 | 9.55351 | I I 3,4 | 690229.09 |
| . 206 | . 93420 | 35,7 | . 35676 | 93,4 | . 97044 | 16,6 | . 553237 | I 1 3,7 | 690555.36 |
| . 207 | . 93455 | 35,6 | - 35582 | 93,5 | . 97060 | 16,5 | . 55124 | II4, 1 | 690921.62 |
| . 208 | .93491 | 35,5 | - 35489 | 93,5 | . 97077 | 16,5 | . 55009 | I I 4,4 | 691247.89 |
| . 209 | . 93526 | 35,4 | - 35395 | 93,5 | . 97093 | 16,4 | . 54895 | I I 4,8 | 69 I6 14.15 |
| 1.210 | 0.93562 | 35,3 | 0.35302 | 93,6 | 9.97110 | 16,4 | 9.54780 | I I5, I | 691940.42 |
| . 211 | . 93597 | 35,2 | -35208 | 93,6 | .97126 | 16,3 | . 54665 | I 15,5 | 692306.68 |
| . 212 | . 93632 | 35, I | -35II5 | 93,6 | .97142 | 16,3 | . 54549 | I 1 5,8 | 692632.95 |
| . 213 | . 93667 | 35,0 | . 35021 | 93,7 | . 97159 | 16,2 | . 54433 | I 16,2 | 692959.21 |
| . 214 | . 93702 | 34,9 | . 34927 | 93,7 | .97175 | 16,2 | . 54317 | 1 16,5 | 693325.47 |
| I. 215 | 0.93737 | 34,8 | 0.34834 | 93,7 | 9.9719 I | 16,I | 9.54200 | I I 6,9 | 693651.74 |
| . 216 | .93772 | 34,7 | . 34740 | 93,8 | . 97207 | 16, 1 | . 54083 | 117,2 | 694018.00 |
| .217 | . 93806 | 34,6 | . 34646 | 93,8 | . 97223 | 16,0 | . 53965 | 117,6 | 694344.27 |
| . 218 | . 9384 I | 34,6 | - 34552 | 93,8 | . 97239 | 16,0 | . 53848 | I 18,0 | 6947 10.53 |
| . 219 | .93876 | 34,5 | . 34458 | 93,9 | .97255 | 15,9 | . 53730 | I 18,3 | 695036.80 |
| 1.220 | 0.93910 | 34,4 | 0.34365 | 93,9 | 9.9727 I | 15,9 | 9.5361 I | 118,7 | 695403.06 |
| . 221 | . 93944 | 34,3 | . 3427 I | 93,9 | . 97287 | I5,8 | . 53492 | I19, 1 | $6957 \quad 29.33$ |
| . 222 | . 93978 | 34,2 | -34177 | 94,0 | . 97303 | I5,8 | . 53373 | I I9,4 | $70 \quad 0055.59$ |
| . 223 | .94013 | 34, I | - 34083 | 94,0 | .97319 | 15,7 | . 53253 | II9,8 | 700421.86 |
| . 224 | . 94047 | 34,0 | . 33989 | 94,0 | . 97334 | 15,7 | . 53133 | 120,2 | 700748.12 |
| 1.225 | 0.94081 | 33,9 | 0.33895 | 94, I | 9.97350 | 15,6 | 9.53013 | 120,5 | 70 II 14.39 |
| .226 | .94II4 | 33,8 | . 33800 | 94, I | . 97366 | I 5,6 | . 52892 | 120,9 | 70 I4 40.65 |
| . 227 | .94148 | 33,7 | . 33706 | 94, I | .9738I | 15,5 | . 52771 | 121,3 | $70.18 \quad 06.92$ |
| . 228 | . 94182 | 33,6 | .336r2 | 94,2 | . 97397 | 15,5 | . 52650 | 121,7 | 70 21 33.18 |
| . 229 | . 94215 | 33,5 | . 33518 | 94,2 | . 97412 | 15,5 | . 52528 | 122,1 | $70 \quad 2459.44$ |
| 1.230 | 0.94249 | 33,4 | 0.33424 | 94,2 | 9.97428 | 15,4 | 9.52406 | 122,5 | $\begin{array}{lllll}70 & 28 & 25.71\end{array}$ |
| . 231 | . 94282 | 33,3 | . 33330 | 94,3 | . 97443 | 15,4 | . 52283 | 122,9 | 703151.98 |
| . 232 | . 94316 | 33,2 | . 333235 | 94,3 | . 97458 | 15,3 | . 52160 | 123,2 | $\begin{array}{llll}70 & 35 & 18.24\end{array}$ |
| . 233 | . 94349 | 33, I | -3314I | 94,3 | . 97474 | I 5,3 | . 52036 | 123,6 | $70 \quad 38 \quad 44 \cdot 5 \mathrm{I}$ |
| . 234 | . 94382 | 33,0 | . 33047 | 94,4 | . 97489 | 15,2 | . 51913 | 124,0 | 704210.77 |
| 1.235 | 0.94415 | 33,0 | 0.32952 | 94,4 | 9.97504 | 15,2 | 9.51788 | 124,4 | $70 \quad 45 \quad 37.04$ |
| . 236 | . 94448 | 32,9 | . 32858 | 94,4 | . 97519 | I5,I | . 51664 | 124,8 | $70 \quad 49 \quad 03.30$ |
| . 237 | . 9448 I | 32,8 | . 32763 | 94,5 | . 97534 | I5, I | -51539 | 125,2 | $70 \quad 52 \quad 29.57$ |
| . 238 | .94513 | 32,7 | . 32669 | 94,5 | . 97549 | 15,0 | . 51413 | 125,6 | $70 \quad 55 \quad 55.83$ |
| . 239 | . 94546 | 32,6 | . 32574 | 94,5 | . 97564 | 15,0 | . 51287 | 126,1 | 705922.09 |
| I. 240 | 0.94578 | 32,5 | 0. 32480 | 94,6 | 9.97579 | 14,9 | 9.5116 I | 126,5 | 710248.36 |
| . 241 | . 94611 I | 32,4 | . 32385 | 94,6 | . 97594 | 14,9 | . 51034 | 126,9 | 710614.62 |
| . 242 | . 94643 | 32,3 | - 32290 | 94,6 | . 97609 | 14,8 | . 50907 | 127,3 | 710940.89 |
| . 243 | . 94675 | 32,2 | . 32196 | 94,7 | . 97624 | I4,8 | . 50780 | 127,7 | 711307.15 |
| . 244 | . 947708 | 32, I | . 32 IOI | 94,7 | . 97638 | 14,7 | . 50652 | 128, 1 | $71 \quad 1633.42$ |
| 1.245 | 0.94740 | 32,0 | 0.32006 | 94,7 | 9.97653 | 14,7 | 9.50524 | 128,6 | 711959.68 |
| . 246 | . 94772 | 31,9 | . 31912 | 94,8 | . 97668 | 14,6 | . 50395 | 129,0 | 712325.95 |
| . 247 | . 94803 | 31,8 | .31817 | 94,8 | . 97682 | 14,6 | . 50266 | 129,4 | 712652.21 |
| . 248 | . 94835 | 31,7 | . 31722 | 94,8 | . 97697 | 14,5 | . 50136 | 129,8 | 713018.48 |
| . 249 | . 94867 | 31,6 | . 31627 | 94,9 | .977II | 14,5 | . 50006 | I30,3 | 7 I 3344.74 |
| I. 250 | 0.94898 | 31,5 | 0.31532 | 94,9 | 9.97726 | I4,4 | 9.49875 | 130,7 | 7I 37 II.OI |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.250 | 0.94898 | 31,5 | 0.31532 | 94,9 | 9.97726 | 14,4 | 9.49875 | I30,7 | 71 $37^{\circ} \mathrm{II} 1.01$ |
| . 251 | . 94930 | 3I,4 | .31437 | 94,9 | . 97740 | 14,4 | . 49745 | I3I, I | 714037.27 |
| . 252 | .94961 | 3I,3 | . 31342 | 95,0 | . 97755 | 14,3 | . 49613 | I31,6 | 714403.54 |
| . 253 | . 94993 | 31,2 | . 31247 | 95,0 | . 97769 | 14,3 | . 4948 I | 132,0 | 714729.80 |
| . 254 | . 95024 | 31,2 | -3II52 | 95,0 | . 97783 | I4,2 | . 49349 | I 32,5 | 715056.07 |
| I. 255 | 0.95055 | 31,1 | 0.31057 | 95, I | 9.97797 | 14,2 | 9.49216 | 132,9 | 715422.33 |
| . 256 | . 95086 | 31,0 | . 30962 | 95, I | .978I2 | 14, I | . 49083 | 133,4 | 715748.60 |
| . 257 | .95117 | 30,9 | . 30867 | 95, I | . 97826 | I4, I | . 48950 | I 33, 8 | 72 OI 14.86 |
| . 258 | . 95148 | 30,8 | . 30772 | 95, I | . 97840 | 14,0 | . 48816 | 134,3 | 720441.13 |
| . 259 | .95178 | 30,7 | . 30677 | 95,2 | . 97854 | 14,0 | .4868I | I 34,7 | $\begin{array}{lllll}72 & 08 & 07.39\end{array}$ |
| 1.260 | 0.95209 | 30,6 | 0.30582 | 95,2 | 9.97868 | 13,9 | 9.48546 | I 35,2 | 72 II 33.66 |
| . 261 | . 95240 | 30,5 | . 30486 | 95,2 | . 97882 | 13,9 | . 484 II | I 35,7 | 72 I4 59.92 |
| . 262 | . 95270 | 30,4 | . 30391 | 95,3 | . 978195 | 13,9 | . 48275 | 136,1 | 72 18 26.19 |
| . 263 | . 95300 | 30,3 | . 30296 | 95,3 | . 97909 | 13,8 | .48138 | 136,6 | 72 21 52.45 |
| . 264 | .9533I | 30,2 | .30201 | 95,3 | . 97923 | 13,7 | . 48002 | I37, I | 722518.72 |
| 1. 265 | 0.9536 I | 30,1 | 0.30105 | 95,4 | 9.97937 | 13,7 | 9.47864 | I37,6 | $72 \quad 2844.98$ |
| . 266 | . 9539 I | 30,0 | . 30010 | 95,4 | .9795I | 13,7 | . 47726 | I38,0 | 723211.24 |
| . 267 | .9542I | 29,9 | . 29914 | 95,4 | . 97964 | 13,6 | . 47588 | I 38,5 | 723537.51 |
| . 268 | . 95451 | 29,8 | . 29819 | 95,5 | . 97978 | 13,6 | . 47449 | I 39,0 | $72 \quad 3903.77$ |
| . 269 | . 95480 | 29,7 | . 29724 | 95,5 | .97991 | 13,5 | . 47310 | I 39,5 | 724230.04 |
| 1.270 | 0.95510 | 29,6 | 0.29628 | 95,5 | 9.98005 | 13,5 | 9.47170 | 140,0 | $7245 \quad 56.30$ |
| . 271 | . 95540 | 29,5 | . 29533 | 95,5 | . 98018 | I'3,4 | . 47030 | 140,5 | 724922.57 |
| . 272 | . 95569 | 29,4 | . 29437 | 95,6 | . 98032 | I 3,4 | . 46889 | 141,0 | $72 \quad 5248.83$ |
| . 273 | . 95599 | 29,3 | . 2934 I | 95,6 | . 98045 | I3,3 | . 46748 | 141,5 | 7256 I5.10 |
| . 274 | . 95628 | 29,2 | . 29246 | 95,6 | . 98058 | I3,3 | . 46606 | 142,0 | 725941.36 |
| I. 275 | 0.95657 | 29,2 | 0.29150 | 95,7 | 9.98072 | I3,2 | 9.46464 | I42,5 | $\begin{array}{llll}73 & 03 & 07.63\end{array}$ |
| . 276 | . 95686 | 29,1 | . 29054 | 95,7 | . 98085 | 13,2 | .46321 | 143,0 | 730633.89 |
| .277 | . 95715 | 29,0 | . 28959 | 95,7 | .98098 | I3,1 | .46178 | 143,5 | 731000.16 |
| . 278 | . 95744 | 28,9 | . 28863 | 95,7 | .98III | I3, I | . 46034 | I44, 1 | 73 I3 26.42 |
| . 279 | . 95773 | 28,8 | . 28767 | 95,8 | .98124 | I3,0 | . 45890 | 144,6 | 73 I6 52.69 |
| I. 280 | 0.95802 | 28,7 | 0. 28672 | 95,8 | 9.98137 | 13,0 | 9.45745 | I45, I | $73 \quad 2018.95$ |
| . 281 | . 95830 | 28,6 | . 28576 | 95,8 | . 98150 | 13,0 | . 45600 | 145,6 | $\begin{array}{llll}73 & 23 & 45.22\end{array}$ |
| . 282 | . 95859 | 28,5 | . 28480 | 95,9 | .98163 | 12,9 | . 45454 | 146,2 | 7327 II. 48 |
| .283 | . 95887 | 28,4 | . 28384 | 95,9 | .98176 | 12,9 | . 45307 | 146,7 | $\begin{array}{lllll}73 & 30 & 37.75\end{array}$ |
| . 284 | . 95916 | 28,3 | . 28288 | 95,9 | .98189 | 12,8 | . 45160 | 147,3 | 7334 04.01 |
| I. 285 | 0.95944 | 28,2 | 0.28192 | 95,9 | 9.98202 | 12,8 | 9.45013 | 147,8 | $73 \quad 37 \quad 30.28$ |
| . 286 | . 95972 | 28,1 | . 28096 | 96,0 | . 98214 | 12,7 | . 44865 | 148,3 | 734056.54 |
| . 287 | . 96000 | 28,0 | . 28000 | 96,0 | . 98227 | 12,7 | . 44716 | 148,9 | 734422.81 |
| .288. | . 96028 | 27,9 | . 27904 | 96,0 | . 98240 | 12,6 | . 44567 | 149,5 | 734749.07 |
| . 289 | . 96056 | 27,8 | . 27808 | 96, I | .98252 | 12,6 | . 44417 | I 50, 0 | 7351515.34 |
| I. 290 | 0.96084 | 27,7 | 0.27712 | 96, I | 9.98265 | 12,5 | 9.44267 | 150,6 | 73 54 41.60 |
| .291 | .96III | 27,6 | . 27616 | 96, 1 | . 98277 | 12,5 | . 44116 | I5I, 1 | $73 \quad 5807.86$ |
| . 292 | . 96139 | 27,5 | . 27520 | 96, I | . 98290 | 12,4 | .43965 | 151,7 | 74 O1 34.13 |
| . 293 | .96166 | 27,4 | . 27424 | 96,2 | .98302 | I2,4 | . 43813 | 152,3 | 740500.39 |
| . 294 | .96194 | 27,3 | . 27328 | 96,2 | .98315 | 12,3 | . 43660 | 152,9 | $74 \quad 0826.66$ |
| I. 295 | 0.96221 | 27,2 | 0.2723 I | 96,2 | 9.98327 | 12,3 | 9.43507 | I 53,5 | 74 II 52.92 |
| . 296 | . 96248 | 27,1 | . 27135 | 96,2 | . 98339 | 12,2 | . 43353 | 154,0 | 74 15 19.19 |
| . 297 | . 96275 | 27,0 | . 27039 | 96,3 | .9835I | I2,2 | . 43199 | I'54,6 | 74 18 45.45 |
| . 298 | . 96302 | 26,9 | . 26943 | 96,3 | . 98364 | 12,2 | . 43044 | 1 55,2 | 7422 II. 72 |
| . 299 | . 96329 | 26,8 | . 26846 | 96,3 | . 98376 | 12,I | . 42888 | I 55,8 | 742537.98 |
| 1.300 | 0.96356 | 26,7 | 0.26750 | 96,4 | 9.98388 | 12,I | 9.42732 | 156,4 | $74 \quad 2904.25$ |
| u | -isinhiu | $\omega F_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 300 | 0.96356 | 25,7 | 0.26750 | 96,4 | 9.98388 | I2,I | 9.42732 | I 56,4 |  |
| . 301 | . 95383 | 26,7 | . 26654 | 96,4 | . 98400 | 12,0 | . 42575 | 157,0 | $7432 \begin{array}{llll}73 & 30.51\end{array}$ |
| . 302 | . 96409 | 26,6 | . 26557 | 96,4 | . 98412 | 12,0 | . 42418 | 157,7 | $\begin{array}{lllllllllllllllll}74 & 35 & 56.78\end{array}$ |
| . 303 | . 96436 | 26,5 | . 26461 | 96,4 | . 98424 | II,9 | . 42260 | 158,3 | 743923.04 |
| . 304 | . 96462 | 26,4 | . 26364 | 96,5 | . 98436 | I 1,9 | . 42102 | 158,9 | 744249.31 |
| I. 305 | 0.96488 | 26,3 | 0.26268 | 96,5 | 9.98447 | I I, 8 | 9.41942 | 159,5 | $\begin{array}{lllllllllllll}74 & 46 & 15.57\end{array}$ |
| . 306 | . 96515 | 26,2 | . 26171 | 96,5 | . 98459 | I 1 , 8 | . 41782 | 160,2 | 744941.84 |
| . 307 | . 9654 I | 26,1 | . 26075 | 96,5 | . 98471 | II,7 | . 41622 | 160,8 | 745308.10 |
| . 308 | . 96567 | 26,0 | . 25978 | 96,6 | . 98483 | I I,7 | .4146I | 161,4 | $74 \quad 5634 \cdot 37$ |
| . 309 | . 96593 | 25,9 | . 25882 | 96,6 | . 98494 | I 1,6 | . 41299 | 162,I | 750000.63 |
| 1.3IO | 0.966 I 8 | 25,8 | 0. 25785 | 96,6 | 9.98506 | 11,6 | 9.41137 | 162,7 | $\begin{array}{llll}75 & 03 & 26.90\end{array}$ |
| .311 | . 96644 | 25,7 | . 25688 | 96,6 | .98518 | I 1,5 | . 40974 | 163,4 | 750653.16 |
| . 312 | . 96670 | 25,6 | . 25592 | 96,7 | . 98529 | II,5 | . 40810 | 164,0 | 75 10 19.43 |
| . 313 | . 96695 | 25,5 | . 25495 | 96,7 | . 98541 | I I,5 | . 40646 | 164,7 | $\begin{array}{lllllllllll}75 & 13 & 45.69\end{array}$ |
| . 314 | . 96721 | 25,4 | . 25398 | 96,7 | . 98552 | I I,4 | . 4048 I | 165,4 | 75 I7 II.95 |
| I.3I5 | 0.96746 | 25,3 | 0.25302 | 96,7 | 9.98563 | II,4 | 9.40315 | 166, 1 | $\begin{array}{llll}75 & 20 & 38.22\end{array}$ |
| . 3116 | . 96771 | 25,2 | . 25205 | 96,8 | . 98575 | II,3 | . 40148 | 166,7 | $75 \quad 24 \quad 04.49$ |
| . 317 | . 96797 | 25, I | . 25108 | 96,8 | . 98586 | I I, 3 | . 3998 I | 167,4 | $75 \quad 2730.75$ |
| . 318 | . 96822 | 25,0 | . 2501 I | 96,8 | . 98597 | II,2 | -39814 | 168, 1 | $75 \quad 3057.01$ |
| . 319 | . 96847 | 24,9 | . 24914 | 96,8 | . 98608 | II,2 | . 39645 | 168,8 | 753423.28 |
| 1.320 | 0.96872 | 24,8 | 0.24818 | 96,9 | 9.98620 | II, I | 9.39476 | 169,5 | 753749.54 |
| . 321 | . 96896 | 24,7 | . 24721 | 96,9 | .9863I | II, I | - 39306 | 170,2 | 75 4I 15.8I |
| . 322 | . 9692 I | 24,6 | . 24624 | 96,9 | . 98542 | II,O | . 39135 | 170,9 | 754442.07 |
| . 323 | . 96946 | 24,5 | . 24527 | 96,9 | . 98653 | I I, 0 | . 38964 | I71,7 | 754808.34 |
| . 324 | . 96970 | 24,4 | . 24430 | 97,0 | . 98664 | 10,9 | . 38792 | 172,4 | 755134.60 |
| I. 325 | 0.96994 | 24,3 | 0.24333 | 97,0 | 9.98675 | 10,9 | 9.38619 | I73,1 |  |
| . 326 | .97019 | 24,2 | . 242336 | 97,0 | . 98686 | 10,8 | . 38446 | 173,9 | 755827.13 |
| . 327 | . 97043 | 24, I | . 24 I'39 | 97,0 | .98696 | 10,8 | -38272 | 174,6 | 76 or 53.40 |
| . 328 | . 97067 | 24,0 | . 24042 | 97, I | .98707 | 10,8 | -38097 | I75,3 | 760519.66 |
| . 329 | .9709I | 23,9 | . 23945 | 97, I | .98718 | 10,7 | . 3792 I | 176,1 | 760845.93 |
| I. 330 | 0.97115 | 23,8 | 0. 23848 | 97, I | 9.98729 | 10,7 | 9.37744 | 176,9 | 76 12 12.19 |
| . 331 | . 97139 | 23,8 | . 23750 | 97, I | . 98739 | 10,6 | . 37567 | 177,6 | 76 I5 38.46 |
| . 332 | . 97162 | 23,7 | . 23653 | 97,2 | . 98750 | 10,6 | -37389 | 178,4 | $76 \quad 1904.72$ |
| . 333 | .97186 | 23,6 | . 23556 | 97,2 | . 98760 | 10,5 | - 37210 | 179,2 | 762230.99 |
| . 334 | . 97209 | 123,5 | . 23459 | 97,2 | .98771 | 10,5 | .3703I | 180,0 | 762557.25 |
| I. 335 | 0.97233 | 23,4 | 0.23362 | 97,2 | 9.9878r | 10,4 | 9.36851 | 180,8 | 762923.52 |
| . 336 | . 97256 | 23,3 | . 23264 | 97,3 | . 98792 | 10,4 | . 36669 | 181,6 | 763249.78 |
| . 337 | . 97279 | 23,2 | .23167 | 97,3 | . 98802 | 10,3 | . 36487 | 182,4 | 763616.05 |
| . 338 | . 97303 | 23,1 | .23070 | 97,3 | . 98812 | 10,3 IO,3 | . 36305 | 183,2 184,0 | $\begin{array}{llll}76 & 39 & 42.31 \\ 76 & 43 & 08.58\end{array}$ |
| . 339 | . 97326 | 23,0 | . 22973 | 97,3 | . 98823 | 10,3 | .3612I | 184,0 | 764308.58 |
| I. 340 | 0.97348 | 22,9 | 0.22875 | 97,3 | 9.98833 | 10,2 | 9.35937 | 184,8 | 764634.84 |
| . 341 | . 97371 | 22,8 | . 22778 | 97,4 | . 98843 | 10,2 | - 3575 I | 185,7 | 7650 O1. 11 |
| . 342 | . 97394 | 22,7 | .2268I | 97,4 | . 98853 | 10, I | -35565 | 186,5 | 765327.37 |
| . 343 | . 97417 | 22,6 | . 212583 | 97,4 | . 98863 | 10,1 | - 35378 | 187,3 | 765653.63 |
| . 344 | . 97439 | 22,5 | . 22486 | 97,4 | . 98873 | 10,0 | .35191 | 188,2 | 770019.90 |
| I. 345 | 0.97462 | 22,4 | 0.22388 | 97,5 | 9.98883 | 10,0 | 9.35002 | 189,1 | $\begin{array}{llll}77 & 03 & 46.16\end{array}$ |
| . 346 | . 97484 | 22,3 | . 22291 | 97,5 | . 98893 | 9,9 | -34813 | 189,9 | 770712.43 |
| . 347 | . 97506 | 22,2 | . 22193 | 97,5 | . 98903 | 9,9 | . 34622 | 190,8 | 77 10 38.69 |
| . 348 | . 97528 | 22,1 | . 22096 | 97,5 | . 98913 | 9,8 | . 34431 | 191,7 | $\begin{array}{llll}77 & 14 & 04.96\end{array}$ |
| . 349 | . 97550 | '22,0 | . 21998 | 97,6 | . 98923 | 9,8 | - 34239 | 192,6 | 77 I7 3I. 22 |
| 1.350 | 0.97572 | 21,9 | 0.21901 | 97,6 | 9.98933 | 9,7 | 9.34046 | 193,5 | $77 \quad 2057.49$ |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 10 cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |

Circular Functions.

| $u$ | $\sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 350 | 0.97572 | 21,9 | 0.21901 | 97,6 | 9.98933 | 9,7 | 9.34046 | 193,5 | $77^{\circ} 20^{\prime} 57.49$ |
| . 351 | . 97594 | 21,8 | . 21803 | 97,6 | . 98942 | 9,7 | . 33852 | 194,4 | $77 \quad 2423.75$ |
| - 352 | . 97616 | 21,7 | . 21705 | 97,6 | . 98952 | 9,7 | . 33657 | 195,3 | 772750.02 |
| . 353 | . 97638 | 21,6 | . 21608 | 97,6 | . 98962 | 9,6 | . 3346 I | 196,2 | $77 \begin{array}{lll}71 & 16.28\end{array}$ |
| . 354 | . 97659 | 2I,5 | . 21510 | 97,7 | . 9897 I | 9,6 | . 33264 | 197,2 | 773442.55 |
| I. 355 | 0.97681 | 2I,4 | 0.21413 | 97,7 | 9.9858I | 9,5 | 9.33067 | 198, I | $77 \quad 3808.81$ |
| . 356 | . 97702 | 2I,3 | . 2I315 | 97,7 | . 98990 | 9,5 | . 32868 | 199, I | 774135.08 |
| - 357 | . 97723 | 21,2 | . 21217 | 97,7 | . 99000 | 9,4 | - 32669 | 200,0 | 7745 OI .34 |
| . 358 | . 97744 | 2I, I | . 21119 | 97,7 | . 99009 | 9,4 | . 32468 | 201,0 | 77. 48 27.6I |
| - 359 | . 97765 | 21,0 | . 21022 | 97,8 | .99019 | 9,3 | . 32267 | 202,0 | 775153.87 |
| - 1.360 | 0.97786 | 20,9 | 0.20924 | 97,8 | 9.99028 | 9,3 | 9.32064 | 203,0 | 775520.14 |
| . 361 | . 97807 | 20,8 | . 20826 | 97,8 | . 99037 | 9,2 | . 31861 | 204,0 | 775846.40 |
| . 362 | . 97828 | 20,7 | . 20728 | 97,8 | . 99046 | 9,2 | . 31656 | 205,0 | $\begin{array}{llll}78 & 02 & 12.67\end{array}$ |
| . 363 | . 97849 | '20,6 | . 20630 | 97,8 | . 99056 | 9,2 | -3145I | 206,0 | $\begin{array}{llllll}78 & 05 & 38.93\end{array}$ |
| . 364 | . 97859 | 20,5 | . 20533 | 97,9 | . 99065 | 9, I | . 31244 | 207,0 | 780905.20 |
| 1. 365 | 0.97890 | 20,4 | 0.20435 | 97,9 | 9.99074 | 9,1 | 9.31037 | 208,0 | 78 12 31.46 |
| . 366 | . 97910 | 20,3 | . 20337 | 97,9 | . 99083 | 9,0 | . 30828 | 209, I | 78 15 57.73 |
| . 367 | . 97931 | 20,2 | . 20239 | 97,9 | . 99092 | 9,0 | . 30619 | 210, I | 78 19 23.99 |
| . 368 | .9795I | 20,1 | . 20141 | 98,0 | .9910I | 8,9 | . 30408 | 211,2 | $78 \quad 2250.25$ |
| . 369 | . 9797 I | 20,0 | . 20043 | 98,0 | . 99110 | 8,9 | . 30196 | 212,3 | $78 \quad 2616.52$ |
| 1.370 | 0.97991 | 19,9 | 0. 19945 | 98,0 | 9.99119 | 8,8 | 9.29983 | 213,4 | $78 \quad 2942.78$ |
| . 371 | . 9801 I | 19,8 | . 19847 | 98,0 | . 99127 | 8,8 | . 29769 | 214,5 | $78 \quad 3309.05$ |
| . 372 | . 98031 | 19,7 | . 19749 | 98.0 | .99136 | 8,7 | . 29554 | 215,6 | $78 \quad 3635 \cdot 31$ |
| . 373 | . 98050 | 19,7 | . 19651 | 98, I | .99145 | 8,7 | . 29338 | 216,7 | 7840 OI. 58 |
| . 374 | . 98070 | 19,6 | . 19553 | 98, 1 | . 99154 | 8,7 | . 29121 | 217,8 | $78 \quad 43 \quad 27.84$ |
| 1.375 | 0.98089 | 19,5 | 0. 19455 | -8, 1 | 9.99162 | 8,6 | 9.28903 | 219,0 | 7846 54.II |
| . 376 | . 98109 | 19,4 | . 19357 | 98, I | .9917I | 8,6 | . 28683 | 220,1 | 785020.37 |
| . 377 | .98128 | 19,3 | . 19259 | 9S, I | .99179 | 8,5 | . 28462 | 221,3 | 785346.64 |
| . 378 | .98147 | 19,2 | . 19160 | 98, 1 | . 99188 | 8,5 | . 28240 | 222,5 | $78 \quad 5712.90$ |
| . 379 | .98I66 | 19,I | . 19062 | 98,2 | .99196 | 8,4 | . 28017 | 223,7 | 790039.17 |
| 1.380 | 0.98185 | 19,0 | 0. 18964 | 98,2 | 9.99205 | 8,4 | 9.27793 | 224,9 |  |
| . 38 I | . 98204 | 18,9 | . 18856 | 98,2 | . 99213 | 8,3 | . 27568 | 226, 1 | 790731.70 |
| . 382 | . 98223 | I8,8 | . 18768 | 98,2 | . 99221 | 8,3 | . 27341 | 227,3 | 79 10 57.96 |
| .383 | . 98242 | 18,7 | . 18669 | 98,2 | . 99230 | 8,3 | . 27 I I3 | 228,5 | 79 14 24.23 |
| . 384 | . 98260 | 18,6 | . 1857I | 98,3 | . 99238 | 8,2 | . 26884 | 229,8 | 79 17 50.49 |
| I. 385 | 0.98279 | 18,5 | 0. 18473 | 98,3 | 9.99246 | 8,2 | 9.26654 | 23I, I | 79 21 16.76 |
| . 386 | . 98297 | 18,4 | . 18375 | 98,3 | . 99254 | 8, I | . 26422 | 232,3 | 792443.02 |
| . 387 | .983I6 | 18,3 | . 18276 | 98,3 | . 99262 | 8,I | . 26189 | 233,6 | $\begin{array}{lllllllllll}79 & 28 & 09.29\end{array}$ |
| . 388 | . 98334 | 18,2 | . 18ı78 | 98,3 | . 99270 | 8,0 | . 25955 | 234,9 | 79 3I 35.55 |
| . 389 | . 98352 | 18,1 | . 18080 | 98,4 | . 99278 | 8,0 | . 25719 | 236,3 | 7935 O1. 82 |
| 1.390 | 0.98370 | 18,0 | 0.17981 | 98,4 | 9.99286 | 7,9 | 9.25482 | 237,6 | $79 \quad 38 \quad 28.08$ |
| .391 | . 98388 | 17,9 | . 17883 | 98,4 | . 99294 | 7,9 | . 25244 | 238,9 | 79 41 54.35 |
| . 392 | .98406 | 17,8 | . 17785 | 98,4 | . 99302 | 7,8 | . 25004 | 240,3 | 794520.61 |
| - 393 | . 98424 | 17,7 | . 17686 | 98,4 | .993IO | 7,8 | .24763 | 241,7 | 794846.88 |
| . 394 | .9844' | 17,6 | . 17588 | S8,4 | . 99318 | 7,8 | . 2452 I | 243, I | 7952 I3.14 |
| 1.395 | 0.98459 | 17,5 | 0.17489 | 98,5 | 9.99325 | 7,7 | 9.24277 | 244,5 | 795539.40 |
| - 396 | . 98476 | 17,4 | . 17391 | 98,5 | . 99333 | 7,7 | . 24032 | 245,9 | 795905.67 |
| - 397 | -98494 | 17,3 | . I7292 | 98,5 | .9934 I | 7,6 | . 23785 | 247,4 | $\begin{array}{cccc}80 & 02 & 31.93 \\ 80 & 05 & 58.20\end{array}$ |
| - 398 | . 9851 I | 17,2 | . 17194 | c8,5 | . 99348 | 7,6 | . 23537 | 248,8 | 80 0558.20 |
| . 399 | . 98528 | 17,1 | . 17095 | 98,5 | . 99356 | 7,5 | . 23288 | 250,3 | 800924.46 |
| 1.400 | 0.98545 | 17,0 | 0.16997 | 98,5 | 9.99363 | 7,5 | 9.23036 | 251,8 | 801250.73 |
| u | -isinh $i u$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | $\log$ cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.400 | 0.98545 | 17,0 | 0. 16997 | 98,5 | 9.99363 | 7,5 | 9.23036 | 251,8 | $80^{\circ} 12 \times 50 \prime \prime 73$ |
| . 401 | . 98562 | 16,9 | . 16898 | 98,6 | . 9937 I | 7,4 | . 22784 | 253,3 | 801616.99 |
| . 402 | . 98579 | 16,8 | . 16800 | 98,6 | . 99378 | 7,4 | . 22530 | 254,8 | 80 I9 43.26 |
| . 403 | . 98596 | 16,7 | . 16701 | 98,6 | . 99386 | 7,4 | . 22274 | 256,4 | $80 \quad 2309.52$ |
| . 404 | . 98612 | 16,6 | . 16602 | 98,6 | . 99393 | 7,3 | . 22017 | 258,0 | $80 \quad 2635.79$ |
| 1.405 | 0.98629 | 16,5 | 0. 16504 | 98,6 | 9.99400 | 7,3 | 9.21758 | 259,5 | 803002.05 |
| . 406 | . 98645 | 16,4 | . 16405 | 98,6 | . 99408 | 7,2 | . 21498 | 26I, I | 8033128.32 |
| . 407 | . 98662 | 16,3 | . 16306 | 98,7 | . 99415 | 7,2 | . 21236 | 262,8 | 80 |
| . 408 | . 98678 | 16,2 | . 16208 | 98,7 | . 99422 | 7,1 | . 20972 | 264,4 | 804020.85 |
| . 409 | . 98694 | 16,1 | . 16109 | 98,7 | . 99429 | 7,1 | . 20707 | 266, I | 8043 47.II |
| 1.410 | 0.98710 | 16,0 | 0.16010 | 98,7 | 9.99436 | 7,0 | 9.20440 | 267,8 | $80 \quad 4713.38$ |
| . 411 | . 98726 | 15,9 | . 15912 | 98,7 | . 99443 | 7,0 | . 20172 | 269,5 | 805039.64 |
| . 412 | . 98742 | 15,8 | . 15813 | 98,7 | . 99450 | 7,0 | . I990I | 271,2 | 805405.91 |
| . 413 | . 98758 | 15,7 | . 15714 | 98,8 | . 99457 | 6,9 | . 19629 | 272,9 | 805732.17 |
| . 414 | . 98773 | 15,6 | . 15615 | 98,8 | -99464 | 6,9 | . 19355 | 274,7 | 81 0058.44 |
| 1.415 | 0.98789 | 15,5 | 0.15517 | 98,8 | 9.99471 | 6,8 | 9. 19080 | 276,5 | 8 I 0424.70 |
| . 416 | . 98804 | 15,4 | . 15418 | 98,8 | . 99478 | 6,8 | . 18802 | 278,3 | 81 0750.97 |
| . 417 | . 98820 | 15,3 | . 15319 | 98,8 | . 99484 | 6,7 | . 18523 | 280,2 | 81 II I7.23 |
| . 418 | . 98835 | 15,2 | . 15220 | 98,8 | .99491 | 6,7 | . 18242 | 282,0 | 81 14 43.50 |
| . 419 | . 98850 | I'5, I | . 15121 | 58,9 | . 99498 | 6,6 | . 17959 | 283,9 | 81 1809.76 |
| 1.420 | 0.98865 | 15,0 | 0. 15023 | 98,9 | 9.99504 | 6,6 | 9.17674 | 285,8 | 81 2136.02 |
| . 42 I | . 98880 | 14,9 | . 14924 | 98,9 | .995 I I | 6,6 | . 17388 | 287,8 | 81 2502.29 |
| . 422 | . 98895 | 14,8 | . 14825 | 98,9 | . 99517 | 6,5 | . I7099 | 289,7 | $\begin{array}{llllllllll}81 & 28 \\ 81\end{array}$ |
| . 423 | . 98910 | 14,7 | . 14726 | 88,9 | . 99524 | 6,5 | . 16808 | 291,7 | 81 3154.82 |
| . 424 | . 98924 | 14,6 | . 14627 | 98,9 | . 99530 | 6,4 | . 16515 | 293,7 | 81 3521.08 |
| I. 425 | 0.98939 | 14,5 | 0.14528 | c8,9 | 9.99537 | 6,4 | 9.1622I | 295,8 | 81 3847.35 |
| . 426 | . 98954 | 14,4 | . 14429 | 99,0 | . 99543 | 6,3 | . 15924 | 297,8 | 81 42 I3.6I |
| . 427 | . 98968 | 14,3 | . I4330 | 99,0 | . 99549 | 6,3 | . 15625 | 299,9 | 81 4539.88 |
| . 428 | . 98982 | 14,2 | . 14231 | 99,0 | . 99556 | 6,2 | . 15324 | 302,1 | 81 49006.14 |
| . 429 | . 98996 | 14, 1 | . 14132 | 99,0 | . 99562 | 6,2 | . 1502 I | 304,2 | 81 5232.41 |
| 1.430 | 0.99010 | 14,0 | 0. I4033 | 99,0 | 9.99568 | 6,2 | 9.14716 | 306,4 | 815558.67 |
| . 431 | . 99024 | 13,9 | . 13934 | 99,0 | . 99574 | 6,1 | . 14408 | 308,6 | 81 5924.94 |
| . 432 | . 99038 | 13,8 | . 13835 | 99,0 | . 99580 | 6,1 | . 14098 | 310,9 | 82025 I .20 |
| . 433 | . 99052 | 13,7 | . 13736 | 99, I | . 99586 | 6,0 | . 13786 | 313,2 | 820617.47 |
| . 434 | . 99066 | 13,6 | . I3637 | 99, I | . 99592 | 6,0 | . 13472 | 315,5 | $820943 \cdot 73$ |
| I. 435 | . 99079 | 13,5 | 0. 13538 | 99,1 | 9.99598 | 5,9 | 9.13r55 | 317,8 | 82 I3 10.00 |
| . 436 | . 99093 | I 3,4 | . 13439 | 99, 1 | . 99604 | 5,9 | . 12836 | 320,2 | 82 16 36.26 |
| . 437 | .99106 | I3,3 | . 13340 | 99,1 | .99610 | 5,8 | . 12515 | 322,7 | $82 \quad 2002.53$ |
| . 438 | .99120 | 13,2 | . 13241 | 99, I | .96616 | 5,8 | . 12191 | 325, I | $\begin{array}{lllll}82 & 23 & 28.79\end{array}$ |
| . 439 | .99I33 | 13,I | . 13142 | 99, I | . 99622 | 5,8 | . 11865 | 327,6 | 822655.06 |
| I. 440 | 0.99146 | 13,0 | 0. 13042 | 99, I | 9.99627 | 5,7 | 9.11536 | 330, 1 | 823021.32 |
| . 44 I | . 99159 | 12,9 | . 12943 | 99,2 | . 99633 | 5,7 | . 11204 | 332,7 | 823347.59 |
| . 442 | .99172 | 12,8 | . 12844 | 99,2 | . 99639 | 5,6 | . 10870 | 335,3 | 823713.85 |
| . 443 | . 99185 | 12,7 | . 12745 | 99,2 | . 99644 | 5,6 | . 10534 | 338,0 | $824040.12$ |
| . 444 | . 99197 | 12,6 | . 12646 | 99,2 | . 99650 | 5,5 | . 10194 | 340,7 | 824406.38 |
| 1.445 | 0.99210 | 12,5 | 0. 12546 | 99,2 | 9.99655 | 5,5 | 9.09852 | 343,4 | 824732.65 |
| . 446 | . 99222 | 12,4 | . 12447 | 99,2 | . 99661 | 5,4 | . 09507 | 346,2 | 825058.91 |
| . 447 | . 99235 | 12,3 | . 12348 | 99,2 | . 99666 | 5,4 | . 09160 | 349,0 | 825425.17 |
| . 448 | . 99247 | 12,2 | . 12249 | 99,2 | . 99672 | 5,4 | . 08809 | 351,9 | 825751.44 |
| . 449 | . 99259 | 12,1 | . 12150 | 99,3 | . 99677 | 5,3 | . 08456 | 354,8 | 83 ol 17.70 |
| 1.450 | 0.99271 | 12,1 | 0.12050 | 99,3 | 9.99682 | 5,3 | 9.08100 | 357,8 | $83 \quad 443.97$ |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega F_{0}{ }^{\prime}$ | $\log \frac{\sinh \mathrm{iu}}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | log cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Circular Functions.

| u | $\sin u$ | $\omega F_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega F_{0}^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.450 | 0.99271 | 12,1 | 0.12050 | 99,3 | 9.99682 | 5,3 | 9.08100 | 357,8 | $83 \stackrel{\circ}{04} 43.97$ |
| .451 | . 99283 | 12,0 | . 11951 | 99,3 | . 99588 | 5,2 | . 07740 | 300,8 | 83 OS 10.23 |
| . 452 | . 99295 | I 1,9 | . 11852 | 99,3 | . 99693 | 5,2 | . 07378 | 363,9 | 83 II 36.50 |
| . 453 | . 99307 | I I, 8 | . 11752 | 99,3 | .99598 | 5, I | . 07013 | 367,0 | 831502.76 |
| . 454 | . 993 I9 | I 1,7 | . II653 | 99,3 | . 99703 | 5, I | . 06644 | 370, I | 83 I8 29.03 |
| 1. 455 | 0.99330 | II,6 | 0. II 554 | 99,3 | 9.99708 | 5, I | 9.06272 | 373,4 | 832155.29 |
| . 456 | . 99342 | I I,5 | . I I 454 | 99,3 | . 99713 | 5,0 | . 05877 | 376,7 | $8325 \quad 21.56$ |
| . 457 | . 99353 | II,4 | . II 355 | 99,4 | . 99718 | 5,0 | .05519 | 380,0 | $83 \quad 2847.82$ |
| . 458 | . 99365 | II,3 | . I1256 | 99,4 | . 99723 | 4,9 | .05137 | 383,4 | $83 \quad 32 \quad 14.09$ |
| . 459 | . 99376 | II,2 | . III 56 | 99,4 | . 99728 | 4,9 | . 04752 | 386,8 | 833540.35 |
| 1. 460 | 0.99387 | I I, I | 0. 11057 | 99,4 | 9.99733 | 4,8 | 9.04364 | 390,4 | $83 \quad 3906.62$ |
| . 461 | . 99398 | I I, 0 | . 10958 | 99,4 | . 99738 | 4,8 | . 03971 | 394,0 | 834232.88 |
| . 462 | . 99409 | 10,9 | . 10858 | 99,4 | . 99742 | 4,7 | . 03576 | 397,6 | 834559.15 |
| .463 | . 99420 | 10,8 | . 10759 | 99,4 | . 99747 | 4,7 | . 03176 | 401,3 | 834925.41 |
| . 464 | . 99430 | 10,7 | . 10659 | 99,4 | . 99752 | 4,7 | . 02773 | 405, I | 835251.68 |
| 1.465 | 0.99441 | 10,6 | 0.10560 | 99,4 | 9.99756 | 4,6 | 9.02366 | 409,0 | $83 \quad 5617.94$ |
| . 466 | . 9945 I | 10,5 | . 10460 | 99,5 | . 99761 | 4,6 | . 01955 | 412,9 | 835944.21 |
| . 467 | . 99462 | 10,4 | . 10361 | 99,5 | . 99766 | 4,5 | . 01540 | 416,9 | 840310.47 |
| . 468 | . 99472 | 10,3 | . 10262 | 99,5 | . 99770 | 4,5 | . 01121 | 421,0 | 840636.74 |
| .469 | . 99482 | 10,2 | . 10162 | 99,5 | . 99775 | 4,4 | .00698 | 425,2 | 841003.00 |
| 1.470 | 0.99492 | 10, 1 | 0. 10063 | 99,5 | 9.99779 | 4,4 | 9.00271 | 429,4 | 8413329.27 |
| . 471 | . 99502 | 10,0 | . 09963 | 99,5 | . 99783 | 4,3 | 8.99839 | 433,7 | 841655.53 |
| . 472 | . 99512 | 9,9 | . 09864 | 99,5 | . 99788 | 4,3 | . 99403 | 438,2 | 842021.79 |
| . 473 | . 99522 | 9,8 | . 09764 | 99,5 | . 99792 | 4,3 | . 98963 | 442,7 | 842348.06 |
| . 474 | . 99532 | 9,7 | . 09665 | 99,5 | . 99796 | 4,2 | . 98518 | 447,3 | $8+27$ I4.32 |
| 1.475 | 0.99542 | 9,6 | 0.09565 | 99,5 | 9.99800 | 4,2 | 8.98068 | 452,0 | 843040.59 |
| . 476 | . 9955 I | 9,5 | . 09465 | 99,6 | .99805 | 4,1 | .97614 | 456,8 | 843406.85 |
| . 477 | . 99560 | 9,4 | . 09366 | 99,6 | . 99809 | 4,1 | . 97155 | 461,7 | 843733.12 |
| . 478 | . 99570 | 9,3 | . 09266 | 99,6 | .99813 | 4,0 | .96691 | 466,7 | 844059.38 |
| . 479 | . 99579 | 9,2 | .09167 | 99,6 | .99817 | 4,0 | . 96222 | 471,8 | 844425.65 |
| I. 480 | 0.99588 | 9, I | 0.09067 | 99,6 | 9.99821 | 4,0 | 8.95747 | 477,0 | 844751.91 |
| . 481 | . 99597 | 9,0 | . 08968 | 99,6 | . 99825 | 3,9 | . 95267 | 482,3 | 845 I 18.18 |
| . 482 | . 99606 | 8,9 | . 08858 | 99,6 | . 99829 | 3,9 | . 94782 | 487,8 | 845444.44 |
| . 483 | . 99615 | 8,8 | . 08768 | 99,6 | . 99832 | 3,8 | . 94292 | 493,4 | 845810.71 |
| . 484 | . 99624 | 8,7 | . 08669 | 99,6 | . 99836 | 3,8 | . 93796 | 499, I | 85 or 36.97 |
| I. 485 | 0.99632 | 8,6 | 0.08569 | 99,6 | 9.99840 | 3,7 | 8.93294 | 504,9 | 850503.24 |
| . 485 | . 99641 | 8,5 | . 08.869 | 99,6 | . 99844 | 3,7 | . 92786 | 510,9 | $8508 \quad 29.50$ |
| . 487 | . 99649 | 8,4 | . 08370 | 99,6 | . 99847 | 3,6 | . 92272 | 517, I | 85 II 55.77 |
| . 488 | . 99657 | 8,3 | . 08270 | 99,7 | .9985I | 3,6 | .9175I | 523,3 | 85 |
| . 489 | . 99656 | 8,2 | .08171 | 99,7 | . 99855 | 3,6 | . 91225 | 529,8 | $85 \quad 1848.30$ |
| 1.490 | 0.99674 | 8,1 | 0.08071 | 99,7 | 9.99858 | 3,5 | 8.90692 | 536,3 | 852214.56 |
| . 491 | . 99682 | 8,0 | . 07971 | 99,7 | . 99862 | 3,5 | . 90152 | 543, I | 852540.83 |
| . 492 | . 99690 | 7,9 | . 0787 I | 99,7 | . 99865 | 3,4 | . 89606 | 550,0 | $85 \quad 2907.09$ |
| . 493 | . 99698 | 7,8 | . 07772 | 99,7 | . 99868 | 3,4 | .89052 | 557, 1 | 853233.36 |
| . 494 | . 99705 | 7,7 | . 07672 | 99,7 | .99872 | 3,3 | . 8849 I | 564,4 | 853559.62 |
| 1.495 | 0.99713 | 7,6 | 0.07572 | 99,7 | 9.99875 | 3,3 | 8.87923 | 571,9 | 853925.89 |
| . 496 | . 99720 | 7,5 | . 07473 | 99,7 | . 99878 | 3,3 | . 87348 | 579,6 | 854252.15 |
| . 497 | . 99728 | 7,4 | . 07373 | 99,7 | . 99882 | 3,2 | . 86764 | 587,4 | 854618.41 |
| . 498 | . 99735 | 7,3 | . 07273 | 99,7 | . 99885 | 3,2 | . 86173 | 595,5 | 854944.68 |
| . 499 | . 99742 | 7,2 | . 07173 | 99,7 | . 99888 | 3,I | .85573 | 603,9 | $85 \quad 5310.94$ |
| 1.500 | 0.99749 | 7,1 | 0.07074 | 99,7 | 9.9989 I | 3,1 | 8.84965 | 612,4 | 855637.21 |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

Smithsonian Tables

Circular Fúnctions.

| u | $\boldsymbol{\operatorname { s i n }} 4$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos 4$ | $\omega \mathrm{F}_{0}{ }^{\circ}$ | $\log \sin u$ | $\omega \mathrm{Fo}^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 500 | 0.99749 | 7,I | 0.07074 | 99,7 | 9.99891 | 3,I | 8.84965 | 612,4 | $85^{\circ} 56^{\prime} 37^{\prime \prime} .21$ |
| . 501 | . 99757 | 7,0 | . 06974 | 99,8 | . 99894 | 3,1 | . 84348 | 621,2 | 860003.47 |
| . 502 | . 99763 | 6,9 | . 06874 | 99,8 | -99897 | 3,0 | . 83722 | 630,3 | 860329.74 |
| . 503 | . 99770 | 6,8 | . 06774 | 99,8 | -99900 | 2,9 | . 83087 | 639,6 | 860656.00 |
| . 504 | . 99777 | 6,7 | . 06675 | 99,8 | -99903 | 2,9 | . 82443 | 649,2 | 851022.27 |
| 1.505 | 0.99784 | 6,6 | 0.06575 | 99,8 | 9.99906 | 2,9 | 8.81789 | 659,1 | 86 I3 48.53 |
| . 506 | . 99790 | 6,5 | . 06475 | 99,8 | . 99909 | 2,8 | .81125 | 669,3 | 861714.80 |
| . 507 | . 99797 | 6,4 | . 06375 | 99,8 | . 99912 | 2,8 | . 80450 | 679,8 | 862041.06 |
| . 508 | . 99803 | 6,3 | . 06276 | 99,8 | . 99914 | 2,7 | . 79765 | 690,7 | $86 \quad 24$ 07.33 |
| . 509 | . 99809 | 6,2 | .06176 | 99,8 | . 99917 | 2,7 | . 79069 | 701,9 | $86 \quad 2733.59$ |
| 1.510 | 0.99815 | 6,1 | 0.05076 | 99,8 | 9.99920 | 2,6 | 8.78361 | 713,5 | 863059.86 |
| . 511 | .99821 | 6,0 | . 05976 | 99,8 | . 99922 | 2,6 | . 77642 | 725,4 | 863426.12 |
| . 512 | . 99827 | 5,9 | . 05876 | 99,8 | -99925 | 2,6 | . 76910 | 737,8 | 863752.39 |
| .513 | . 99833 | 5,8 | . 05776 | 99,8 | -99927 | 2,5 | . 76166 | 750,6 | 864118.65 |
| . 514 | .94839 | 5,7 | . 05677 | 99,8 | -99930 | 2,5 | . 75409 | 763,8 | 864444.92 |
| 1.515 | 0.99844 | 5,6 | 0.05577 | 99,8 | 9.99932 | 2,4 | 8.74638 | 777,5 | 8648 II. 18 |
| . 516 | . 99850 | 5,5 | . 05477 | 99,8 | -99935 | 2,4 | . 73853 | 791,8 | 865137.45 |
| . 517 | - 99855 | 5,4 | . 05377 | 99,9 | -99937 | 2,3 | . 73054 | 806,5 | 865503.71 |
| . 518 | . 9986 I | 5,3 | . 05277 | 99,9 | -99939 | 2,3 | . 72240 | 821,8 | 865829.98 |
| . 519 | . 99866 | 5,2 | . 05177 | 99,9 | . 99942 | 2,3 | . 71410 | 837,7 | 87 O1 56.24 |
| 1.520 | 0.99871 | 5,1 | 0.05077 | 99,9 | 9.99944 | 2,2 | 8.70565 | 854,2 | 870522.51 |
| . 521 | . 99876 | 5,0 | . 04978 | 99,9 | . 99946 | 2,2 | . 69702 | 871,4 | 8708.48 .77 |
| . 522 | . 99881 | 4,9 | . 04878 | 99,9 | . 99948 | 2,I | . 68821 | 889,3 | $\begin{array}{lllll}87 & 12 & 15.04 \\ 87 & 15 & 41\end{array}$ |
| . 523 | . 99886 | 4,8 | . 04778 | 99,9 | . 99950 | 2,I | . 67923 | 907,9 | $\begin{array}{llll}87 & 15 & 41.30\end{array}$ |
| . 524 | . 99891 | 4,7 | . 04678 | 99,9 | -99952 | 2,0 | . 67005 | 927,4 | 871907.56 |
| 1.525 | 0.99895 | 4,6 | 0.04578 | 99,9 | 9.99954 | 2,0 | 8.66068 | 947,7 | 872233.83 |
| . 526 | . 99900 | 4,5 | . 04478 | 99,9 | . 99956 | 1,9 | . 65110 | 968,8 | 872600.09 |
| . 527 | . 99904 | 4,4 | . 04378 | 99,9 | . 95958 | 1,9 | . 64130 | 991,0 | 872926.36 |
| . 528 | . 99908 | 4,3 | . 04278 | 99,9 | . 99960 | 1,9 | . 63127 | 1014,2 | 873252.62 |
| . 529 | . 99913 | 4,2 | . 04178 | 99,9 | . 99962 | I,8 | . 62101 | 1038,5 | 873618.89 |
| 1.530 | 0.99917 | 4,1 | 0.04079 | 99,9 | 9.99964 | 1,8 | 8.61050 | 1064,0 | 873945.15 |
| . 531 | . 99921 | 4,0 | . 03979 | 99,9 | . 99966 | I,7 | . 59973 | 1090,7 | 8743 II. 42 |
| . 532 | . 99925 | 3,9 | .03879 | 99,9 | . 99967 | I,7 | . 58868 | I 1 18,9 | 874637.68 |
| . 533 | . 99929 | 3,8 | . 03779 | 99,9 | . 99969 | I,6 | . 57735 | 1148,5 | 875003.95 |
| . 534 | . 99932 | 3,7 | . 03679 | 99,9 | . 9997 I | I,6 | . 56571 | 1179,7 | 875330.21 |
| 1. 535 | 0.99936 | 3,6 | 0.03579 | 99,9 | 9.99972 | 1,6 | 8.55375 | 1212,7 | 875656.48 |
| . 536 | . 99939 | 3,5 | . 03479 | 99,9 | . 99974 | I,5 | . 54145 | 1247,6 | 88 0022.74 |
| . 537 | . 99943 | 3,4 | . 03379 | 99,9 | -99975 | 1,5 | - 52879 | 1284,5 | $8_{88}^{88} 0349.01$ |
| . 538 | . 99946 | 3,3 | . 03279 | 99,9 | -99977 | I,4 | . 51575 | 1323,7 | 88 O7 815.27 |
| - 539 | - 99949 | 3,2 | . 03179 | 99,9 | . 99978 | I,4 | . 50230 | 1365,4 | 88 10 41.54 |
| 1. 540 | 0.99953 | 3,1 | 0.03079 | 100,0 | 9.99979 | I,3 | 8.48843 | I409,8 I457, I |  |
| .541 | . 99956 | 3,0 | . 02979 | 100,0 | -9998I | I,3 | -47410 | 1457,1 | $\begin{array}{llll}88 & 17 & 34.07 \\ 88 & 21 & 00.33\end{array}$ |
| . 542 | - 99959 | 2,9 | . 02879 | 100,0 | -99982 | 1,3 | - 45928 | 1507,7 | 88 212100.33 |
| . 543 | . 99961 | 2,8 | . 02779 | 100,0 | - 95983 | I,2 | - 44393 | 1562,0 | 88 $24 \begin{array}{ll}26.60\end{array}$ |
| - 544 | . 99964 | 2,7 | . 02679 | 100,0 | . 99984 | 1,2 | . 42802 | 1620,3 | $88 \quad 2752.86$ |
| I. 545 | 0.99967 | 2,6 | 0.02579 | 100,0 | 9.99986 | I, I | 8.41151 | 1683,2 | 883119.13 |
| . 546 | . 99969 | 2,5 | . 02479 | 100,0 | . 99987 | I, I | - 39434 | 1751,1 | 88 3445.39 |
| . 547 | . 99972 | 2,4 | . 02379 | 100,0 | - 99988 | 1,0 | -37647 | 1824,7 | 883811.66 |
| - 548 | . 99974 | 2,3 | . 02279 | 100,0 | . 99989 | 1,0 | - 35783 | 1904,8 |  |
| - 549 | . 99976 | 2,2 | . 02179 | 100,0 | . 99990 | 0,9 | . 33835 | 1992,2 | 8845 04.18 |
| 1. 550 | 0.99978 | 2,I | 0.02079 | 100,0 | 9.99991 | 0,9 | 8.31796 | 2088,0 | 884830.45 |
| u | -i sinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 4 |

Circular Functions.

| u | $\boldsymbol{\operatorname { s i n }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\cos u$ | $\omega F_{0}{ }^{\prime}$ | $\log \sin u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cos u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.550 | 0.99978 | 2,I | +0.02079 | 100,0 | 9.99991 | 0,9 | 8.31796 | 2088,0 | $88^{\circ} 48^{\prime} 30^{\prime \prime} .45$ |
| . 551 | . 99980 | 2,0 | . 01980 |  | .9999I | 0,9 | . 29656 | 2193,5 | 885 5 56.7 I |
| . 552 | . 99982 | 1,9 | . 01880 |  | . 99992 | 0,8 | . 27405 | 2310,3 | $8855 \quad 22.98$ |
| . 553 | . 99984 | I,8 | . 01780 |  | . 99993 | 0,8 | . 2503 I | 2440, I | $88 \quad 5849.24$ |
| . 554 | . 99986 | 1,7 | . 01680 |  | . 99994 | 0,7 | . 22519 | 2585,4 | 8902 I5.5I |
| 1.555 | 0.99988 | 1,6 | +0.01580 | 100,0 | 9.99995 | 0,7 | 8. 19854 | 2749, I | 890541.77 |
| . 556 | . 99989 | I,5 | . 01480 |  | . 999995 | 0,6 | . 17014 | 2934,9 | 890908.04 |
| . 557 | . 99990 | I,4 | . 01380 |  | . 99996 | 0,6 | . I3975 | 3147,7 | 89 I2 $34 \cdot 30$ |
| . 558 | . 99992 | I,3 | . 01280 |  | . 99996 | 0,6 | . 10707 | 3393,7 | 891600.57 |
| . 559 | . 99993 | 1,2 | . 01180 |  | . 99997 | 0,5 | .07174 | 3681,4 | 89 19 26.83 |
| 1.560 | 0.99994 | 1,I | +0.01080 | 100,0 | 9.99997 | 0,5 | 8.03327 | 4022,5 | 892253.10 |
| . 561 | . 99995 | 1,0 | .00980 |  | . 99998 | 0,4 | 7.99106 | 4433, 1 | $89 \quad 2619.36$ |
| . 562 | . 99996 | 0,9 | . 00880 |  | . 99998 | 0,4 | . 94430 | 4937, I | 892945.63 |
| . 563 | . 99997 | 0,8 | . 00780 |  | . 99999 | 0,3 | . 89189 | 5570,4 | 8933 II. 89 |
| . 564 | . 99998 | 0,7 | . 00680 |  | . 99999 | 0,3 | . 83227 | 6390,0 | 893638.16 |
| I. 565 | 0.99998 | 0,6 | +0.00580 | 100,0 | 9.99999 | 0,3 | 7.76315 | 7492,5 | 894004.42 |
| . 566 | . 99999 | 0,5 | . 00480 |  | 0.00000 | 0,2 | .6809I | 9054,7 | 894330.69 |
| . 567 | . 99999 | 0,4 | .00380 |  | . 00000 | 0,2 | . 57936 | I I 439,8 | 894656.95 |
| . 568 | 1.00000 | 0,3 | . 00280 |  | . 00000 | O, I | . 44659 | 15530,9 | 895023.22 |
| . 569 | 1.00000 | 0,2 | .00180 |  | . 00000 | 0,1 | . 25438 | 24176,8 | 895349.48 |
| I. 570 | I. 00000 | 0,I | +0.00080 | İ0,0 | 0.00000 | 0,0 | 6.90109 | 54537,4 | $8957 \quad 15.75$ |
| . 571 | . 00000 | 0,0 | -. 00020 |  | . 00000 | 0,0 | $6.30894 n$ | 213228,5 | 900042.01 |
| . 572 | . 00000 | O,I | . 00120 |  | . 00000 | O, I | 7.08051 | 36080,7 | $90 \quad 0408.28$ |
| . 573 | . 00000 | 0,2 | . 00220 |  | . 00000 | O, I | . 34315 | 19707,7 | $90 \quad 0734.54$ |
| . 574 | 0.99999 | 0,3 | . 00320 |  | . 00000 | O,I | . 50565 | 13556, I | 90 II 00.8 I |
| 1.575 | 0.99999 | 0,4 | -0.00420 | 100,0 | 0.00000 | 0,2 | $7.62363 n$ | 10331,2 | 90 I4 27.07 |
| . 576 | . 99999 | 0,5 | . 00520 |  | 9.99999 | 0,2 | . 7163 I | 8345,8 | $9017 \quad 53.33$ |
| . 577 | . 99998 | 0,6 | . 00620 |  | . 99999 | 0,3 | . 79255 | 7000,5 | 902119.60 |
| . 578 | . 99997 | 0,7 | . 00720 |  | . 99999 | 0,3 | . 85755 | 6028,6 | 902445.86 |
| . 579 | . 99997 | 0,8 | . 00820 |  | . 99999 | 0,4 | . 91400 | 5293,8 | 9028 I2.I3 |
| 1.580 | 0.99996 | 0,9 | -0.00920 | 100,0 | 9.99998 | 0,4 | $7.96396 n$ | 4718,6 | $90 \begin{array}{llll} & 31 & 38.39\end{array}$ |
| . 581 | . 99995 | I,O | . 01020 |  | . 99998 | 0,4 | 8.00875 | 4256, 1 | 903504.66 |
| . 582 | . 99994 | I, I | . 01120 |  | . 99997 | 0,5 | . 04935 | 3876,2 | 903838.92 |
| . 583 | . 99993 | 1,2 | . 01220 |  | . 99997 | 0,5 | . 08648 | 3558,5 | 904157.19 |
| . 584 | .9999I | I,3 | . 01320 |  | . 99996 | 0,6 | . 12068 | 3289,0 | $9045 \quad 23.45$ |
| I. 585 | 0.99990 | I,4 | -0.01420 | 100,0 | 9.99996 | 0,6 | 8.15239n | 3057,4 | 904849.72 |
| . 586 | . 99988 | 1,5 | . 01520 |  | . 99995 | 0,7 | . 18193 | 2856,3 | $90 \quad 52.15 .98$ |
| . 587 | . 99987 | 1,6 | .01620 |  | . 99994 | 0,7 | . 20959 | 2680,0 | 905542.25 |
| . 588 | . 99985 | 1,7 | . 01720 |  | . 99994 | 0,7 | . 23560 | 2524,2 | 905908.5 I |
| . 589 | . 99983 | 1,8 | . 01820 |  | . 99993 | 0,8 | . 26014 | 2385,5 | 91 0234.78 |
| I. 590 | 0.99982 | 1,9 | -0.01920 | 100,0 | 9.99992 | 0,8 | $8.28336 n$ | 2261,2 | 91 06 or. 04 |
| . 591 | . 99980 | 2,0 | . 02020 |  | . 9999 I | 0,9 | . 30540 | 2149,3 | 91 0927.3 I |
| . 592 | . 99978 | 2,I | . 02120 |  | . 99990 | 0,9 | . 32638 | 2047,9 | 91 $12 \begin{array}{lll}12 & 53.57\end{array}$ |
| . 593 | . 99975 | 2,2 | . 02220 |  | . 99989 | 1,0 | . 34639 | 1955,6 | $91 \quad 16519.84$ |
| . 594 | . 99973 | 2,3 | . 02320 |  | . 99988 | 1,0 | . 36552 | 1871,3 | 911946.10 |
| 1.595 | 0.99971 | 2,4 | -0.02420 | 100,0 | 9.99987 | I, I | $8.38384 n$ | 1794,0 | 912312.37 |
| . 596 | . 99908 | 2,5 | . 02520 |  | . 99986 | I, I | . 40142 | I722,8 | $91 \quad 2638.63$ |
| . 597 | . 99966 | 2,6 | . 02620 |  | . 99985 | I, I | . 4183 I | 1657,0 | 91 3004.90 |
| . 598 | . 99963 | 2,7 | . 02720 |  | . 99984 | 1,2 | . 43457 | 1 595, 1 | 9133 3I.16 |
| - 599 | . 99960 | 2,8 | . 02820 |  | . 99983 | 1,2 | . 45025 | I 539,4 | 913657.43 |
| 1. 600 | 0.99957 | 2,9 | -0.02920 | 100,0 | 9.9998I | I,3 | 8.46538 | 1485,7 | 91 $40 \quad 23.69$ |
| u | -isinh iu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | cosh iu | $\omega \mathrm{F}_{0}{ }^{\text {a }}$ | $\log \frac{\sinh i u}{i}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\log \cosh \mathrm{iu}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u |

## TABLE IV

## THE ASCENDING AND DESCENDING EXPONENTIAL AND $\log _{10}\left(e^{e}\right)$

Note. -In Table IV, for $u$ greater than 2.302, the tabulated values of the ascending exponential may sometimes be erroneous to one unit in the last place.

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{n}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0.0000000 | 1.000000 | 1.000 0000 | 0.050 | 0.0217147 | 1.051271 | 0. |
| . 001 | . 0004343 | . OOI OOI | 0.9990005 | .05I | . 0221490 | . 052323 | . 9502787 |
| . 002 | . 0008686 | . 002002 | . 9980020 | . 052 | .0225833 | . 053376 | . 9493289 |
| . 003 | .001 3029 | . 003005 | . 9970045 | . 053 | . 0230176 | . 054430 | . 9483800 |
| . 004 | .OOI 7372 | . 004008 | . 9960080 | . 054 | . 0234519 | . 055485 | . 9474321 |
| 0.005 | 0.0021715 | 1.005013 | 0.995 OI25 | 0.055 | 0.0238862 | 1.056541 | 0.946485 I |
| . 006 | . 0026058 | . 006018 | . 994 OI80 | . 056 | .0243205 | . 057598 | . 9455391 |
| . 007 | . 003 0401 | .007025 | . 9930244 | . 057 | .0247548 | . 058656 | . 944 5941 |
| . 008 | . 0034744 | .008032 | . 9920319 | . 058 | . 025 I89I | . 059715 | . 9436499 |
| . 009 | .0039087 | . 009041 | .991 0404 | . 059 | .0256234 | . 060775 | .9427068 |
| 0.010 | 0.0043429 | 1.010050 | 0.9900498 | 0.060 | 0.0260577 | 1.061837 | 0.9417645 |
| . OII | . 0047772 | . OII 06I | . 9890603 | .06I | . 0264920 | . 062899 | . 9408232 |
| . 012 | . 0052115 | . 012072 | .9880717 | . 062 | .0269263 | . 063962 | . 9398829 |
| . 013 | .0056458 | . 013085 | .9870841 | . 063 | .0273606 | . 065027 | $\text { . } 9389435$ |
| . 014 | . 006 080I | . 014098 | .9860975 | . 064 | . 0277948 | . 066092 | $.9380050$ |
| 0.015 | 0.0065144 | 1.015 II3 | 0.985 III9 | 0.065 | 0.028229 I | 1.067159 | 0.9370675 |
| . 016 | . 0069487 | . 016129 | . 9841273 | . 066 | . 0286634 | . 068227 | $.9361309$ |
| . 017 | . 0073830 | . 017145 | . 9831437 | . 067 | . 0290977 | . 069295 | . 9351952 |
| . 018 | . 007 8173 | . 018163 | .9821610 | . 068 | . 0295320 | . 070365 | . 9342605 |
| . 019 | . 0082516 | . 019182 | .981 1794 | . 069 | . 0299663 | . 071436 | . 9333267 |
| 0.020 | 0.0086859 | 1.020201 | 0.9801987 | 0.070 | 0.0304006 | 1.072508 | 0.932 .3938 |
| .02I | . 0091202 | .021 222 | . 9792190 | . 071 | . 0308349 | . 073 581 | . 9314619 |
| . 022 | . 0095545 | . 022244 | . 9782402 | . 072 | .031 2692 | . 074655 | . 9305309 |
| . 023 | . 0099888 | .023267 | .9772625 | . 073 | .031 7035 | .075731 | . 9296008 |
| . 024 | . 010423 I | .024290 | . 9762857 | . 074 | .0321378 | . 076807 | . 9286717 |
| 0.025 | 0.010 8574 | 1.025315 | 0.9753099 | 0.075 | 0.0325721 | 1.077884 | 0.9277435 |
| . 026 | . OII 2917 | . 02634 I | . 974335 I | . 076 | . 0330064 | . 078963 | . 9268162 |
| . 027 | . O1I 7260 | .027368 | . 9733612 | . 077 | .0334407 | . 080042 | .9258899 |
| . 028 | . 0121602 | . 028396 | .9723884 | . 078 | .0338750 | .081 123 | . 9249644 |
| . 029 | . 0125945 | .029425 | . 9714165 | . 079 | .0343093 | . 082204 | . 9240399 |
| 0.033 | 0.0130288 | I. 030455 | 0.9704455 | 0.080 | 0.0347436 | 1.083287 | 0.9231163 |
| . 031 | . 0134631 | .031 486 | . 9694756 | .08I | . 0351779 | . 084371 | . 9221937 |
| . 032 | . O13 8974 | .032518 | . 9685066 | . 082 | .035 612I | .085456 | . 9212720 |
| . 033 | . 0143317 | . 033551 | . 9675386 | . 083 | .0360464 | . 086542 | . 920 3511 |
| . 034 | .0147660 | . 034585 | . 9665715 | . 084 | .0364807 | . 087629 | . 9194313 |
| 0.035 | 0.0152003 | 1.035620 | 0.9656054 | 0.085 | 0.0369150 | 1.088717 | 0.9185123 |
| . 036 | . O15 6346 | . 036656 | . 9646403 | . 086 | . 0373493 | . 089806 | . 9175942 |
| . 037 | . 0160689 | . 037693 | . 9636761 | . 087 | .0377836 | . 090897 | .916 6771 |
| . 038 | . 0165032 | . 038731 | . 9627129 | . 088 | . 0382179 | . 091988 | .915 7609 |
| . 039 | . 0169375 | . 039770 | .961 7507 | . 089 | . 0386522 | . 093 08I | .914 8456 |
| 0.040 | 0.0173718 | I. 040 8II | 0.9607894 | 0.090 | 0.0390865 | 1.094174 |  |
| . 041 | . 01788061 | .041852 | . 9598291 | .091 | . 0395208 | . 095269 | .913 0177 |
| . 042 | . 0182404 | . 042894 | . 9588698 | . 092 | . 039 955I | . 096365 | . 9121051 |
| . 043 | . 0186747 | .043938 | . 957 9114 | . 093 | . 0403894 | $.097462$ | $\text { .9II } 1935$ |
| . 044 | . 0191090 | . 044982 | . 9569540 | . 094 | . 0408237 | . 098560 | .910 2828 |
| 0.045 | 0.0195433 | 1.046028 | 0.9559975 | 0.095 | 0.0412580 | 1.099659 | 0.9093729 |
| . 046 | . 0199775 | . 047074 | . 9550420 | . 096 | .041 6923 | . 100759 | . 9084640 |
| . 047 | . 0204118 | . 048122 | . 9540874 | . 097 | . 0421266 | . IOI 860 | . 9075560 |
| . 048 | . 0208461 | . 049 171 | . 9531338 | . 098 | .0425609 | . 102963 | . 9066489 |
| . 049 | .021 2804 | . 050220 | . 952 I8II | . 099 | . 0429952 | . 104066 | . 9057427 |
| 0.050 | 0.0217147 | 1.051271 | 0.95I 2294 | 0.100 | 0.0434294 | 1. 105 I 71 | 0.9048374 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $\mathrm{e}^{-}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\text {u }}\right.$ ) | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-0}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\mathrm{e}^{\mathrm{u}}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.100 | 0.0434294 | I. 105 I7I | 0.9048374 | 0.150 | 0.0651442 | I. 161 834 | 0.8607080 |
| . IOI | . 0438637 | . 106277 | . 9039330 | . 151 | . 0655785 | . 162997 | . 8598477 |
| . 102 | . 0442980 | . 107383 | .9030296 | . 152 | . 0660128 | . 164160 | . 8589883 |
| . 103 | . 0447323 | . 10849 I | . 9021270 | . I53 | . 0664471 | . 165325 | .8581297 |
| . 104 | . 0451666 | . 109600 | . 9012253 | . 154 | . 0668814 | . 166491 | . 8572720 |
| 0.105 | 0.0456009 | I.IIO 711 | 0.9003245 | 0.155 | 0.0673156 | 1.167658 | 0.8564152 |
| . 105 | . 0460352 | . III 822 | . 8994246 | . 156 | . 0677499 | . 168826 | . 8555592 |
| . 107 | . 0464695 | . II2 934 | . 8985257 | . 157 | . 068 1842 | . 169996 | . 8547041 |
| . 108 | . 0469038 | . II4 048 | .8976276 | . 158 | . 068 6185 | . 171166 | . 8538498 |
| . 109 | . 047 3381 | . 115162 | .8967304 | . 159 | . 0690528 | . 172338 | . 8529964 |
| 0.110 | 0.0477724 | I.II6 278 | 0.8958341 | 0.160 | 0.069487 I | 1.173511 | 0.8521438 |
| . III | . 0482067 | . II7 395 | . 8949387 | . 161 | . 0699214 | . 174685 | . 8512921 |
| . II2 | . 048 6410 | . 118513 | . 8940443 | . 162 | .0703557 | . 175860 | .8504412 |
| . II3 | . 0490753 | . II9 632 | . 8931507 | . 163 | .0707900 | -. 177037 | .8495912 |
| . II4 | . 0495096 | . 120752 | . 8922580 | . 164 | . 0712243 | .178 214 | .8487420 |
| 0.115 | 0.0499439 | I. 121873 | 0.8913661 | 0. 165 | 0.071 6586 | 1. I79 393 | 0.8478937 |
| . 116 | . 0503782 | . 122996 | . 8904752 | . 166 | . 0720929 | .180 573 | . 8470462 |
| . 117 | . 050 8125 | . 124119 | . 8895852 | . 167 | . 0725272 | . 181 754 | . 8461996 |
| . II8 | .051 2467 | . 125244 | . 888 6961 | : 168 | . 0729615 | . 182937 | .8453538 |
| . 119 | .051 6810 | . 126370 | .8878078 | . 169 | .0733958 | . 184120 | . 8445089 |
| 0. 120 | 0.052 II53 | 1.127497 | 0.8869204 | 0.170 | 0.0738301 | I. 185305 | 0.8436648 |
| . 121 | .0525496 | . 128625 | . 8860340 | . 171 | . 074 2644' | . 186491 | . 8428216 |
| . 122 | .0529839 | . 129754 | . 8851484 | . 172 | .0746987 | .187678 | . 8419792 |
| .123 | .0534182 | . 130884 | . 8842637 | .173 | .0751329 | . 188866 | .841 1376 |
| . 124 | . 0538525 | . 132 OI6 | .8833798 | . 174 | .0755672 | . 190056 | . 8402969 |
| 0.125 | 0.0542868 | I. 133148 | 0.8824969 | 0.175 | 0.0760015 | I.I91 246 | 0.8394570 |
| . 126 | . 054 7211 | . I34 282 | .88I 6148 | . 176 | . 0764358 | . 192438 | . 838 6180 |
| . 127 | . 0551554 | . 135417 | . 8807337 | . 177 | . 0768701 | . 193631 | . 8377798 |
| . 128 | . 0555897 | . 136 553 | . 8798534 | . 178 | . 0773044 | . 194825 | . 8369424 |
| . 129 | .0560240 | . 137690 | .8789740 | . 179 | .0777387 | . 19602 I | .8361059 |
| 0.130 | 0.0564583 | I. 138828 | 0.8780954 | 0. 180 | 0.0781730 | I. 197217 | 0.8352702 |
| . I3 I | . 0568926 | - I39 968 | . 8772178 | . 181 | . 0786073 | . 1984 r 5 | . 8344354 |
| . 132 | .0573269 | . 141108 | . 8763410 | . 182 | .0790416 | . 199614 | . 8336013 |
| . I33 | .0577612 | . I42 250 | . 8754651 | . 183 | . 0794759 | . 200 8I4 | . 8327682 |
| . 134 | . 0581955 | . 143393 | . 8745901 | . 184 | .0799102 | . 202016 | . 8319358 |
| 0.135 | 0.0586298 | 1.144 537 | 0.8737159 | 0. 185 | 0.0803445 | 1.203218 | 0.8311043 |
| . 136 | . 0590640 | .145 682 | . 8728426 | . 186 | . 0807788 | . 204422 | . 8302736 |
| . 137 | .0594983 | . 146828 | . 8719702 | . 187 | .08I 213 I | . 205627 | . 8294437 |
| . 138 | . 0599326 | . 147976 | . 8710987 | . 188 | .081 6474 | .206834 | .8286147 |
| . 139 | . 0603669 | . 149124 | . 8702280 | . 189 | . 0820817 | .208041 | .8277865 |
| 0.140 | 0.0608012 | I. 150274 | 0.8693582 | D. 190 | 0.0825160 | I. 209250 | 0.8269591 |
| . 141 | .061 2355 | . 151425 | . 8684893 | . 191 | .0829502 | . 210459 | . 8261326 |
| . 142 | .06I 6698 | . 152577 | .8576213 | . 192 | . 0833845 | .211 671 | .8253069 |
| . I43 | .0621041 | . 153730 | . 8667541 | . 193 | .0838188 | . 212883 | . 8244820 |
| . I44 | . 0625384 | . 154884 | .8658877 | . 194 | . 084253 I | .214096 | .8236579 |
| 0.145 | 0.0629727 | I. 156040 | 0.8650223 | 0.195 | 0.0846874 |  | 0.8228347 |
| . I46 | . 0634070 | . 157196 | . 8641577 | . 195 | .085 1217 | . 216527 | . 8220122 |
| . 147 | .0638413 | . 158354 | .8632940 | . 197 | .0855560 | . 217744 | .821 1905 |
| . 148 | . 0642756 | . 159513 | . 8624311 | . 198 | .0859903 | .218962 | .8203699 |
| . 149 | . 0647099 | . 160673 | . 8615691 | . 199 | . 0864246 | . 220182 | .819 5499 |
| 0.150 | 0.0651442 | I.161 834 | 0.8607080 | 0.200 | 0.0868589 | 1.221403 | 0.8187308 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{u}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-a}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.200 | 0.0868589 | 1.221403 | 0.818 7308 | 0.250 | 0.108 5736 | 1.284025 | 0.7788008 |
| . 20 | . 0872932 | . 222625 | .817 9124 | . 251 | . 1090079 | . 285310 | . 7780224 |
| . 20 | . 0877275 | . 223848 | . 8170949 | . 252 | . 1094422 | . 286596 | . 7772447 |
| . 203 | . 088 1618 | . 225072 | . 8162782 | . 253 | . 1098765 | . 287883 | . 7764679 |
| . 204 | . 088 5961 | . 226298 | .815 4624 | . 254 | . 1103108 | . 289172 | . 7756918 |
| 0.205 | 0.0890304 | 1.227525 | 0.8146473 | 0.255 | 0. 1107451 | 1.290462 | 0.7749165 |
| . 206 | . 0894647 | . 228753 | . 8138331 | . 256 | . 1111794 | . 291753 | . 7741420 |
| . 207 | . 0898990 | . 229983 | . 8130196 | . 257 | . 11116137 | . 293045 | . 7733682 |
| . 208 | . 0903333 | . 231213 | . 8122070 | . 258 | . 1120480 | . 294339 | . 7725952. |
| . 209 | . 0907675 | . 232445 | .8II 3952 | . 259 | . 1124823 | . 295634 | . 7718230 |
| 0.210 | 0.0912018 | 1.233678 | $0.810{ }^{5842}$ | 0.260 | 0.1129166 | 1. 296930 | 0.7710516 |
| . 2 | . 0916361 | . 234912 | . 8097741 | . 261 | . 1133509 | . 298228 | . 7702809 |
| . 21 | . 0920704 | . 236148 | . 8089647 | . 262 | . 1137852 | . 299527 | . 7635110 |
| . 213 | . 0925047 | . 237385 | . 8081561 | . 263 | . 1142194 | . 300827 | . 7687419 |
| . 214 | . 0929390 | . 2338.623 | . 8073484 | . 264 | . 1146537 | -302 128 | . 7679735 |
| 0.215 | 0.0933733 | 1.239862 | 0.8065414 | 0.265 | 0.115 0880 | 1.303 431 | 0.767 2059 |
| . 216 | . 0938076 | . 241102 | . 8057353 | . 266 | . 1155223 | . 304735 | . 7664391 |
| . 217 | . 0942419 | . 242344 | . 8049300 | . 267 | . II5 9566 | . 306040 | . 7656731 |
| . 218 | . 0946762 | . 243587 | . 8041254 | . 268 | . 1163909 | . 307347 | . 7649078 |
| . 219 | . 0951105 | . 244831 | . 8033217 | . 269 | . 1168252 | . 308655 | . 7641433 |
| 0.2 | 0.0955448 | 1.246077 | 0.8025188 | 0.270 | 0.117 2595 | I. 309964 | 0.7633795 |
| . | . 0959791 | . 247323 | . 8017167 | . 271 | .117 6938 | -3II 275 | . 7626165 |
| . 222 | . 0964134 | . 248571 | . 8009154 | . 272 | . 118 1281 | . 312587 | . 7618543 |
| . 223 | . 0968477 | . 249821 | . 8001148 | . 273 | . 1185624 | . 313900 | . 761 0928 |
| . 224 | . 0972820 | . 251071 | . 799 3151 | . 274 | . 1189967 | . 315215 | . 7603321 |
| 0.225 | 0.0977163 | 1.252323 | 0.7985162 |  | 0.119 4310 | 1.316 531 | 0.7595721 |
| . 226 | . 0981506 | . 253576 | . 7977181 | . 276 | . 1198653 | - 317848 | -.758 8129 |
| . | . 0985848 | . 254830 | . 7969208 | . 277 | . 1222996 | . 319166 | . 7580545 |
| . 228 | . 099 о191 | . 256085 | . 7961243 | . 278 | . 1207339 | . 320486 | . 7572968 |
| . 229 | . 0994534 | . 257342 | . 7953285 | . 279 | . 1211682 | . 321807 | .7565399 |
| 0.230 | 0.0998877 | 1.258600 | $0.794{ }^{\prime} 5336$ | 0.280 | 0.121 6025 | 1.323130 | 0.7557837 |
| . 231 | . 1003220 | . 259859 | . 7937395 | . 281 | . 1220367 | -. 324454 | . 7550283 |
| . 232 | . 1007563 | . 261120 | . 7929461 | . 282 | . 1224710 | . 325779 | . 7542737 |
| . 233 | . 1011906 | . 262381 | . 7921536 | .283 | . 1229053 | . 327105 | . 7535198 |
| . 234 | . 1016249 | . 263644 | .791 3618 | . 284 | . 1233396 | . 328433 | . 7527656 |
| 0.235 | 0. 1020592 | 1. 264909 | 0.790 5708 | 0.285 | 0.1237739 | 1. 329762 | 0.7520143 |
| . 236 | . 1024935 | . 266174 | . 7897807 | . 286 | . 1242082 | . 331092 | . 7512626 |
| . 237 | . 1029278 | . 267441 | . 788 9913 | . 287 | .124 6425 | - 332424 | . 7505117 |
| . 238 | . 1033621 | . 268709 | . 7882027 | . 288 | . 1250768 | - 333757 | - 7497616 |
| . 239 | . 1037964 | . 269979 | . 7874149 | . 289 | . 1255111 | -335 092 | . 749 O122 |
| 0.240 | 0.104 2307 | 1.271 249 | 0.7866279 | 0.290 | 0.125. 9454 | 1.336427 | 0.7482636 |
| . 241 | . 1046650 | . 272521 | . 7858416 | . 291 | . 1263797 | . 337765 | . 7475157 |
| . 242 | . 1050993 | . 273794 | . 7850562 | . 292 | . 1268140 | . 339103 | . 7467685 |
| . 243 | . 1055336 | . 275069 | . 7842715 | . 293 | . 1272483 | - 340443 | . 7460221 |
| . 244 | . 1059679 | . 276344 | .7834876 | . 294 | . 1276826 | -341 784 | . 7452765 |
|  | 0. 1064021 | 1.277621 | 0.7827045 | 0.295 | 0.1281169 | 1.343126 | 0.7445316 |
| . 246 | . 1068364 | . 278900 | . 7819222 | . 296 | . 1285512 | . 344470 | . 7437874 |
| . 247 | . 1072707 | . 280179 | . 7811407 | . 297 | . 1289855 | . 345815 | . 7430440 |
| . 248 | . 1077050 | .281 460 | . 7803599 | . 298 | . 1294198 | -347 162 | . 7423013 |
| . 249 | . 1081393 | . 282742 | . 7795800 | . 299 | . 129854 I | - 348510 | .741 5594 |
| 0.250 | 0.108 5736 | 1.284025 | 0.7788008 | 0.300 | 0.1302883 | 1. 349859 | 0.7408182 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ |  | $\log _{\mathrm{e}}\left(\mathrm{e}^{\text {u }}\right.$ ) | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.300 | 0.130 2883 | I. 349859 | 0.7408182 | 0.350 | 0.1520031 | 1. 419068 | 0.704 688I |
| . 301 | .130 7226 | .351 209 | . 7400778 | -35I | . I52 4374 | . 420487 | . 7039838 |
| . 302 | . I3I I569 | . 352 561 | . 739 3381 | . 352 | . 1528717 | . 421909 | . 7032801 |
| . 303 | . 1315912 | . 353914 | . 7385991 | - 353 | . 1533060 | . 423 33I | . 7025772 |
| . 304 | . 1320255 | . 355269 | . 7378609 | . 354 | . 1537402 | . 424755 | .701 8,50 |
| 0.305 | -. 132 4598 | 1. 356625 | 0.7371234 | 0.355 | 0.154 1745 | r. 426 181 | 0.7011734 |
| . 306 | . 1328941 | . 357982 | . 7363866 | . 356 | . I54 6088 | . 427608 | . 7004726 |
| . 307 | . I33 3284 | . 35934 I | . 7356506 | - 357 | . 155 043'I | . 429036 | . 6997725 |
| . 308 | . I33 7627 | . 360701 | .7349153 | . 358 | . I55 4774 | . 430466 | . 6990731 |
| . 309 | . I34 1970 | . 362062 | . 7341808 | - 359 | . I55 91I7 | . 43 I 897 | .6983744 |
| 0.310 | 0.134 6313 | 1. 363425 | 0.7334470 | 0.360 | 0.1563460 | 1.433329 | 0.6976763 |
| .311 | . 1350656 | . 364789 | . 7327139 | . 361 | . 1567803 | . 434763 | . 6969790 |
| . 312 | . 1354999 | . 366155 | .731 98I5 | . 362 | . 1572146 | . 436199 | . 6962824 |
| . 313 | . 1359342 | . 367522 | .731 2499 | . 363 | . 1576489 | . 437636 | . 6955864 |
| . 314 | . 1363685 | . 368890 | . 7305190 | . 364 | . 1580832 | . 439074 | . 6948912 |
| 0.315 | 0.1368028 | 1.370259 | 0.7297889 | 0.365 | -. 1585175 | 1.440514 | 0.6941967 |
| . 316 | . 1372371 | . 371630 | . 7290595 | . 366 | . 1589518 | . 441955 | . 6935028 |
| . 317 | . 1376714 | . 373003 | . 7283308 | . 367 | . I59 386I | . 443398 | . 6928096 |
| . 318 | . 1381056 | . 374376 | .7276028 | . 368 | . 1598204 | . 444842 | . 692 II72 |
| . 319 | . 1385399 | . 37575 I | .7268755 | . 369 | . 1602547 | . 446288 | . 6914254 |
| 0.320 | 0.138 9742 | 1.377 128 | 0.7261490 | 0.370 | 0. 1606890 | I. 447735 | 0.6907343 |
| . 321 | . 1394085 | . 378506 | . 7254233 | . 371 | . 161 1233 | . 449183 | . 6900439 |
| . 322 | . 1398428 | . 379885 | . 7246982 | . 372 | . 1615575 | . 450633 | . 6893542 |
| . 323 | . 1402771 | -381 265 | . 7239739 | . 373 | . 1619918 | . 452084 | . 688 6652 |
| . 324 | . 1407114 | . 382647 | . 7232502 | . 374 | . 1624261 | . 453537 | . 6879769 |
| 0.325 | 0.14I 1457 | I. 38403 I | 0.7225274 | 0.375 | 0. 1628604 | r. 454 991 | 0.6872893 |
| . 326 | . 1415800 | .385415 | . 7218052 | - 376 | . I63 2947 | . 456447 | . 6866023 |
| . 327 | . 1420143 | . 38680 l | . 7210837 | - 377 | . 1637290 | . 457904 | . 685 9161 |
| . 328 | . I42 4486 | . 388 189 | . 7203630 | . 378 | . 1641633 | . 459363 | .6852305 |
| . 329 | . I42 8829 | .389578 | . 7196430 | . 379 | . 1645976 | . 460823 | . 6845456 |
| 0.330 | 0.143 3172 | 1. 390968 | 0.7189237 | 0.380 | 0.1650319 | 1.462 285 | 0.6838614 |
| . 331 | . 1437515 | . 392360 | . 7182052 | -381 | . 1654662 | . 463748 | . 6831779 |
| . 332 | . 1441858 | . 393753 | . 7174873 | - 382 | . 1659005 | . 465212 | . 682495 I |
| . 333 | . 1446201 | . 395147 | .7167702 | . 383 | . 1663348 | .466678 | .68i 8iz9 |
| . 334 | . 1450544 | . 396543 | .7160538 | . 384 | . 1667691 | . 468 I45 | .681 13I4 |
| 0.335 | 0.1454887 | I. 397940 | 0.7153381 | 0.385 | 0. 1672034 | 1.469614 | 0.6804506 |
| . 336 | . I45 9229 | . 399339 | . 7146231 | . 386 | . 1676377 | . 471085 | . 6797705 |
| -337 | . 1463572 | . 400739 | . 7139088 | . 387 | . 1680720 | . 472556 | . 67909 II |
| . 338 | . 1467915 | . 402 I4I | . 7131953 | . 388 | . 1685063 | . 474030 | . 6784123 |
| . 339 | . 1472258 | . 403543 | . 7124824 | . 389 | . 1689406 | . 475505 | . 6777343 |
| 0.340 | D. 1476601 | I. 404948 | 0.7117703 | 0. 390 | 0.169 3748 | I. 47698 I | 0.6770569 |
| . 341 | . 1480944 | . 406353 | . 7110589 | -39I | . 1698091 | . 478459 | . 6763802 |
| . 342 | . 1485287 | . 407760 | . 7103482 | . 392 | . I70 2434 | . 479938 | . 6757041 |
| - 343 | . 1489630 | . 409169 | . 7096382 | - 393 | . 170 6777 | .48I 418 | . 6750287 |
| . 344 | . 1493973 | . 410579 | .7089289 | . 394 | . 171 I 120 | . 482901 | . 674 354I |
| 0.345 | -. 1498316 | 1.4II 990 | 0.7082204 | 0.395 | 0.171 5463 | I. 484384 | 0.6736800 |
| . 346 | . 1502659 | .413 403 | . 7075125 | . 396 | . 1719806 | . 485869 | . 6730067 |
| - 347 | . 1507002 | . 414 817 | . 7068053 | . 397 | . I72 4149 | . 487356 | . 6723340 |
| -348 | . I5.1 1345 | .416232 | . 7060989 | . 398 | . I72 8492 | . 488844 | . 6716620 |
| . 349 | . 1515688 | .417 649 | . 705 393I | - 399 | . 1732835 | . 490334 | . 6709907 |
| 0.350 | D. 1520031 | 1.419068 | 0.704 688I | 0.400 | 0.173 7178 | 1.49I 825 | 0.6703200 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{3}\right)$ | $\log _{10}\left(e^{u}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{n}}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{a}}$ | $e^{-a}$ | 4 | $\log _{10}\left(\mathrm{e}^{\text {u }}\right.$ ) | $\mathrm{e}^{\text {a }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.400 | 0.173 7178 | 1.491825 | 0.6703200 | 0.450 | 0.195 4325 | 1.568312 | 0.6376282 |
| . 401 | . 1741521 | -493 317 | . 669 6501 | .45I | . 1958668 | . 56988 I | . 6369908 |
| -402 | . 1745864 | . 494 81I | . 66898807 | -452 | . 1963011 | -571 452 | . 6363542 |
| -403 | -1750207 | . 496307 | . 6683121 | -453 | . 1967354 | . 573024 | . 635181 |
| -404 | . 1754550 | . 497804 | . 6676441 | -454 | . 1971697 | . 574598 | . 635 082j |
| 0.405 | 0.1758893 | 1.499303 | 0.6669768 | 0.455 | 0.1976040 | 1.576173 | 0.6344480 |
| - 406 | . 1763236 | . 500803 | . 6663102 | . 456 | . 1980383 | . 577750 | . 6338138 |
| . 407 | . 1767579 | . 502304 | . 6666442 | . 457 | - 1984726 | . 579329 | . 6331803 |
| -408 | . 1771921 | . 503807 | . 6649789 | . 458 | . 1989069 | . 580909 | . 6325475 |
| . 409 | . 1776264 | . 505312 | . 6643142 | . 459 | . 1993412 | . 582491 | .631 9152 |
| 0.410 | 0. 1780607 | 1. 506818 | 0.6636503 | 0.460 | 0. 1997755 | 1.584074 | $0.631 \quad 2836$ |
| . 411 | . 1784950 | . 508325 | . 6629869 | . 461 | . 2002098 | . 585659 | . 6306527 |
| . 412 | - 1789293 | . 509834 | . 6623243 | . 462 | . 2006441 | . 587245 | . 6300223 |
| .413 | - 1793636 | . 511345 | . 6616623 | . 463 | :201 0783 | . 588833 | . 6293926 |
| .414 | . 1797979 | . 512857 | . 6610010 | . 464 | . 2015126 | . 590423 | . 6287636 |
| 0.415 | 0.180 2322 | 1.514371 | 0.6603403 | 0.465 | 0.2019469 | 1.592014 | 0.6281351 |
| . 416 | . 1806665 | . 515886 | . 6596803 | . 466 | . 2023812 | . 593607 | . 6275073 |
| -417 | . 1811008 | . 517403 | . 6590209 | . 467 | . 202 8155 | . 595201 | . 6268801 |
| -418 | . 1815351 | . 518921 | . 6583622 | . 468 | . 2032498 | . 596797 | . 6262535 |
| .419 | . 181 9694 | . 520440 | . 6577042 | -4,9 | . 2036841 | . 598395 | . 6256276 |
| 0.420 | 0.182 4037 | 1.521 962 | 0.6570468 | 0.470 | $0.204 \mathrm{T184}$ | 1. 599994 | 0.6250023 |
| . 421 | . 1828380 | . 523484 | . 6563901 | . 471 | . 2045527 | . 601595 | . 6243776 |
| . 422 | . 1832723 | . 525009 | . 6557340 | . 472 | . 2049870 | . 603197 | . 6237535 |
| . 423 | . 1837066 | . 526534 | . 6550786 | .473' | . 2054213 | . 60480 l | .623 I301 |
| . 424 | . 1841409 | . 528062 | . 6544239 | . 474 | . 2058556 | . 606407 | . 6225073 |
| 0.425 | 0. 1845752 | 1.529590 | 0.6537698 | 0.475 | 0.2062899 | 1.608014 | 0.621 8851 |
| . 426 | . 1850094 | . 531121 | . 6531163 | . 476 | . 2067242 | . 609623 | . 6212635 |
| . 427 | . 1854437 | . 532653 | . 6524636 | -477 | . 2071585 | .6i1 233 | . 6206425 |
| . 428 | . 1858780 | . 534187 | . 651 8114 | -478 | . 2075928 | . 612845 | . 6200222 |
| . 429 | . 1863123 | . 535721 | .651 1599 | . 479 | . 2080271 | . 614459 | 619 4025 |
| 0.430 | o. 1867466 | 1.537258 |  | 0.480 |  |  | 0.6187834 |
| . 431 | . 1871809 | . 538796 | . 6498589 | .481 | . 2088956 | . 617691 | . 6181649 |
| . 432 | . 1876152 | . 540335 | . 6492094 | . 482 | . 2093299 | . 619310 | . 6175471 |
| . 433 | . 1880495 | . 541876 | . 6485605 | . 483 | . 2097642 | . 620930 | . 6169298 |
| . 434 | . 1884838 | . 543419 | . 6479123 | . 484 | . 2101985 | . 622552 | 6163132 |
| 0.435 | o. 188 918I | 1. 544963 | 0.6472647 | 0.485 | 0.2106328 | 1.624175 | 0.615 6972 |
| . 436 | . 1893524 | . 546509 | . 6466177 | . 486 | .211 0671 | . 625800 | . 6150818 |
| . 437 | . 1897867 | . 548056 | . 6459714 | . 487 | .211 5014 | . 627427 | . 6144670 |
| . 438 | . 1902210 | . 549605 | . 6453258 | -488 | .211 9357 | . 629055 | 613 8529 |
| -439 | . 1906553 | .551 155 | . 6446808 | . 489 | .2123700 | . 630685 | .613 2393 |
| 0.440 | -.1910896 | 1.552 707 | 0.6440364 | 0.490 | 0.2128043 | 1.632316 | 0.6126264 |
| .441 | . 1915239 | . 554261 | . 6433927 | .491 | . 2132386 | . 633949 | . 6120141 |
| . 442 | . 191 9582 | . 555816 | . 6427496 | . 492 | .213 6729 | . 635584 | .611 4024 |
| . 443 | . 1923925 | . 557372 | . 6421072 | . 493 | . 2141072 | . 637221 | 610 7913 |
| . 444 | . 1928267 | . 558930 | . 6414654 | -494 | . 2145415 | . 638859 | .610 I808 |
| 0.445 | 0. 1932610 | 1. 560490 | 0.640824 .3 | 0.495 | 0.2149758 | 1.640498 | 0.6095709 |
| . 446 | . 1936953 | . 562051 | . 6401838 | . 496 | . 2154101 | . 642140 | . 6089616 |
| . 447 | . 1941296 | . 563614 | . 6395439 | -497 | . 2158444 | . 643783 | . 6083530 |
| . 448 | . 1945639 | . 565179 | . 6389047 | -498 | . 2162787 | . 645427 | . 6077449 |
| . 449 | . 1949982 | . 566745 | . 6382661 | . 499 | . 2167129 | . 647073 | . 6071275 |
| 0.450 | 0. 1954325 | 1.568312 | 0.6376282 | 0.500 | 0.2171472 | 1. 648721 | 0.6065307 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{a}}$ | $\mathrm{e}^{-\mathrm{u}}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$. | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.500 | 0.2171472 | 1. 648721 | 0.6065307 | 0.550 | 0.2388520 | 1.733253 | 0.5769498 |
| . 501 | . 217 58I5 | . 650 371 | . 6059244 | . 551 | . 2392963 | . 734987 | . 576 3731 |
| . 502 | . 2180158 | . 652022 | . 6053188 | . 552 | . 2397306 | . 736723 | . 5757971 |
| . 503 | . 2184501 | . 653675 | . 6047138 | . 553 | . 2401648 | . 738461 | . 5752216 |
| . 504 | . 2188844 | .655329 | . 6041094 | - 554 | . 240 5991 | . 740200 | . 5746466 |
| 0.505 | 0.2193187 | 1. 656986 | 0.6035056 | 0.555 | 0.2410334 | 1.741941 | 0.5740723 |
| . 506 | . 2197530 | . 658643 | . 6029024 | . 556 | . 2414677 | . 743684 | . 5734985 |
| . 507 | . 2201873 | . 660303 | . 6022998 | . 557 | . 2419020 | . 745428 | . 5729253 |
| . 508 | .2206216 | .661 964 | . 6016978 | . 558 | .2423363 | . 747175 | . 5723526 |
| . 509 | .22I 0559 | .663627 | . 6010964 | . 559 | . 2427706 | . 748923 | . 5717806 |
| 0.510 | 0.2214902 | 1.665291 | 0.6004956 | 0.560 | 0.2432049 | 1.750673 | 0.5712091 |
| . 511 | . 221 9245 | . 666957 | . 5998954 | . 561 | . 2436392 | . 752424 | . 5706381 |
| . 512 | . 2223588 | . 668625 | . 5992958 | . 562 | .2440735 | . 754177 | . 5700678 |
| . 513 | .222793 I | . 670295 | . 5986968 | . 563 | .2445078 | . 755932 | . 5694980 |
| . 514 | .2232274 | . 671966 | . 5980984 | . 564 | . 244942 I | . 757689 | . 5689288 |
| 0.515 | 0.2236617 | 1.673639 | 0.5975006 | 0.565 | 0.2453764 | 1. 759448 | 0. 568360 I |
| . 516 | . 2240960 | . 675 313 | . 5969034 | . 566 | .2458107 | .761 208 | . 5677921 |
| . 517 | . 2245302 | . 676989 | . 5963068 | . 567 | . 2462450 | . 762970 | . 5672246 |
| . 518 | .2249645 | .678667 | . 5957108 | . 568 | .2466793 | . 764734 | . 5666576 |
| . 519 | . 2253988 | .680346 | . 595 II54 | . 569 | . 247 II36 | . 766500 | . 5660912 |
| 0.520 | 0.225833 I | 1.682028 | 0.5945205 | 0.570 | 0.2475479 | I. 768267 | 0. 5655254 |
| . 521 | . 2262674 | . 6837 II | . 5939263 | . 571 | . 2479821 | . 770036 | . 5649602 |
| . 522 | .2267017 | . 685395 | . 5933327 | . 572 | .2484164 | .771 807 | . 5643955 |
| . 523 | .2271360 | . 687 081 | . 5927397 | . 573 | . 2488507 | .773580 | . 5638314 |
| . 524 | .2275703 | . 688769 | . 5921472 | . 574 | . 2492850 | . 775354 | . 5632679 |
| 0.525 | 0.2280046 | 1.690459 | 0.5915554 | 0.575 | 0.2497193 | 1.777 131 | 0.5627049 |
| . 526 | .2284389 | . 692150 | . 590, 9641 | . 576 | . 2501536 | . 778909 | . 5621424 |
| . 527 | .2288732 | . 693843 | . 5903734 | . 577 | . 2505879 | . 780688 | . 5615806 |
| . 528 | . 2293075 | . 695538 | . 5897834 | . 578 | . 2510222 | .782470 | . 561 0193 |
| . 529 | .2297418 | . 697234 | . 5891939 | . 579 | . 2514565 | . 784253 | . 5604585 |
| 0.530 | 0.2301761 | 1. 698932 | 0.5886050 | 0.580 | 0.2518908 | 1.786038 | 0. 5598984 |
| . 531 | . 2306104 | . 700632 | . 5880167 | . 581 | . 2523251 | . 787825 | . 559 338 ${ }^{\text {¢ }}$ |
| . 532 | . 2310447 | . 702334 | . 5874289 | . 582 | . 2527594 | . 789614 | . 5587797 |
| . 533 | .231 4790 | . 704037 | . 5868418 | . 583 | . 2531937 | .791 405 | . 5582212 |
| . 534 | . 2319133 | . 705742 | . 5862553 | . 584 | . 2536280 | . 793197 | . 5576632 |
| 0.535 | 0.2323475 | 1.707448 | 0.5856693 | 0.585 | 0.2540623 | 1.794 991 | 0.5571059 |
| . 536 | . 2327818 | .709157 | . 5850839 | . 586 | . 2544966 | . 796787 | . 5565490 |
| . 537 | . 233 2161 | .710 867 | . 5844991 | . 587 | . 2549309 | . 798585 | . 5559928 |
| . 538 | . 233 6504 | . 712578 | . 5839149 | . 588 | . 2553652 | .800384 | . 5554370 |
| . 539 | . 2340847 | . 714292 | . 583 33I3 | . 589 | . 2557994 | . 802185 | . 554 8819 |
| 0.540 | 0.2345190 | 1.716007 | 0.5827483 | 0.590 | 0.2562337 | 1.803988 | 0.5543273 |
| . 54 I | . 2349533 | . 717724 | . 5821658 | . 591 | . 2566680 | . 805793 | . 5537732 |
| . 542 | .2353876 | . 719442 | -581 5839 | . 592 | .2571023 | .807600 | . 5532197 |
| . 543 | .2358219 | .721 163 | . 5810026 | . 593 | .2575366 | .809409 | . 5526668 |
| . 544 | . 2362562 | . 722885 | . 5804219 | . 594 | . 2579709 | .81 1 219 | . 552 II44 |
| 0.545 | 0.2366905 | 1.724608 | 0.5798418 | 0.595 | 0.2584052 | 1.8 I 303 I | 0.5515626 |
| . 546 | . 237 I 248 | . 726334 | . 5792622 | . 596 | . 2588395 | .814 845 | . 551 0113 |
| - 17 | . 237 5591 | .728051 | . 5786833 | . 597 | . 2592738 | .816 661 | . 5504605 |
| - 34 | $.2379934^{\circ}$ | . 729790 | . 5781049 | . 598 | .2597081 | . 818478 | . 5499104 |
| . 549 | .2384277 | .731 521 | . 5775270 | . 599 | . 2611424 | . 820298 | . 5443607 |
| 0.550 | 0.2388620 | 1.733253 | 0.5769498 | 0.600 | 0.2605767 | 1.822 I19 | 0.548 8ı16 |
| $\log _{e}\left(\mathrm{e}^{\text {u }}\right.$ ) | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ |  | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(e^{u}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.600 | 0.2605767 | 1.822119 | 0.548 8ıı6 | 0.650 | 0.2822914 | 1.915541 | 0.5220458 |
| . 601 | . 2610110 | . 823942 | . 5482631 | . 651 | . 2827257 | .917457 | .5215240 .521 |
| . 602 | . 2614453 | . 825767 | . 547 7151 | . 652 | .2831600 | . 919376 | . 5210027 |
| . 603 | . 2618796 | .827593 | . 5471677 | . 653 | .2835943 | . 921296 | . 5204820 |
| . 604 | . 2623139 | . 829422 | . 5466208 | . 654 | . 2840286 | .923218 | $\text { . } 5199618$ |
| 0.605 | 0.2627482 | 1.831 252 | 0.5460744 | 0.655 | 0.2844629 | 1.925143 | 0.5194421 |
| . 606 | . 2631825 | . 833084 | . 5455286 | . 656 | . 2848972 | . 927069 | $.5189229$ |
| . 607 | .2636168 | . 834918 | . 5449834 | . 657 | .2853315 | . 928997 | $\begin{array}{r} .5184042 \end{array}$ |
| . 608 | .2640510 | . 836754 | . 5444387 | . 658 | .2857658 | . 930927 | . 5178861 |
| . 609 | .2644853 | .838592 | . 5438945 | . 659 | . 2862001 | . 932859 | . 5173684 |
| 0.610 | 0.2649196 | 1.840431 | 0.5433509 | 0.660 | 0.2866344 | 1.934792 | 0.5168513 |
| . 611 | . 2653539 | . 842273 | . 5428078 | . 661 | . 2870687 | . 936728 | . 5163347 |
| . 612 | .2657882 | . 844116 | . 5422653 | . 662 | .2875029 | . 938666 | . 5158187 |
| .613 | . 2662225 | . 845961 | -541 7233 | . 663 | .2879372 | .940605 | $.5153031$ |
| .614 | .2666568 | . 847808 | . 54118 r 8 | . 664 | . 2883715 | . 942547 | $\text { . } 514788 I$ |
| 0.615 | 0.2670911 | 1. 849657 | 0.5406409 | 0.665 | 0.2888058 | 1.944491 | 0.5142735 |
| . 616 | . 2675254 | . 851507 | . 5401005 | . 666 | . 2892401 | . 946436 | . 5137595 |
| . 617 | . 2679597 | . 853360 | . 5395607 | . 667 | . 2896744 | . 948383 | . 5132460 |
| . 618 | . 2683940 | . 855214 | . 5390214 | . 668 | . 2901087 | . 950333 | . 5127330 |
| . 619 | . 2688283 | . 857070 | . 5384827 | . 669 | .2905430 | . 952284 | . 5122205 |
| 0.620 | 0.2692626 | 1.858928 | 0.5379444 | 0.670 | 0.2909773 | 1.954237 | 0.5117086 |
| . 621 | . 2696969 | . 860788 | . 5374068 | . 671 | . 2914116 | . 956193 | . 5111971 |
| . 622 | . 2701312 | . 862650 | . 5368696 | . 672 | . 2918459 | . 958150 | . 5106862 |
| . 623 | .2705655 | .864513 | . 5363330 | . 673 | . 2922802 | . 960109 | $.510 \quad 1758$ |
| . 624 | .2709998 | .866379 | . 5357970 | . 674 | .2927145 | . 962070 | $.5096658$ |
| 0.625 | 0.271434 I | 1.868246 | 0.5352614 | 0.675 | 0.2931488 | 1.964 033 | 0.5091564 |
| . 626 | . 2718583 | . 870115 | . 5347264 | . 676 | . 293 '5831 | . 965998 | . 5086475 |
| . 627 | .2723026 | . 871986 | . 5341920 | . 677 | . 294 0174 | . 967965 | . 5081391 |
| . 628 | .2727369 | . 873859 | . 5336581 | . 678 | . 2944517 | . 969934 | .5076312 |
| . 629 | .2731712 | . 875734 | . 5331247 | . 679 | . 2948860 | . 971905 | . 5071239 |
| 0.630 | 0.2736055 | 1.877 6II | 0.5325918 | 0.680 | 0.2953202 | 1.973878 | 0.506 6170 |
| . 631 | . 2740398 | . 879489 | . 5320595 | .681 | . 2957545 | . 975853 | . 5061106 |
| .632 | . 2744741 | . 881370 | . 5315277 | . 682 | . 2961888 | . 977829 | . 5056048 |
| . 633 | . 2749084 | . 883252 | . 5309964 | . 683 | .296623 I | . 979808 | . 5050994 |
| . 634 | .2753427 | . 885136 | . 5304657 | . 684 | . 2970574 | .981 789 | . 5045946 |
| 0.635 | 0.2757770 | 1.887022 | 0.5299355 | 0.685 | 0.2974917 | 1.983772 | 0.5040902 |
| . 636 | . 2762113 | . 888910 | . 5294058 | . 686 | . 2979260 | . 985757 | . 5035864 |
| . 637 | . 2766456 | . 800800 | . 5288767 | . 687 | .2983603 | . 987743 | . 5030831 |
| . 638 | .2770799 | .892692 | . 528348 I | . 688 | . 2987946 | . 989732 | . 5025802 |
| . 639 | .2775142 | .894585 | . 5278200 | . 689 | . 2992289 | .991 723 | . 5020779 |
| 0.640 | 0.2779485 | 1. 89648 I | 0.5272924 | 0.690 | 0.2996632 | 1.993716 | 0.501 5761 |
| . 641 | . 2783828 | . 898378 | . 5267654 | . 691 | . 3000975 | . 995710 | . 5010747 |
| . 642 | . 278 8171 | . 900278 | . 5262389 | . 692 | -300 5318 | . 997707 | . 5005739 |
| . 643 | . 2792514 | .902179 | . 5257129 | . 693 | . 3009661 | .999706 | $.5000736$ |
| . 644 | .2796856 | . 904082 | . 5251875 | . 694 | . 3014004 | 2.001706 | . 4995738 |
| 0.645 | 0.2801199 | 1.905987 | 0.5246625 | 0.695 | 0.301 8347 | 2.003709 | 0.4990744 |
| . 646 | . 2805542 | . 907894 | . 524138 I | . 696 | . 3022690 | . 005714 | . 4985756 |
| . 647 | . 2809885 | . 909803 | . 523 6r43 | . 697 | . 3027033 | . 007720 | . 498.0773 |
| . 648 | . 2814228 | .911 714 | . 5230909 | . 698 | . 3031375 | . 009729 | . 4975795 |
| . 649 | .28I 8571 | .913 626 | . 5225681 | . 699 | - 3035718 | .OII 740 | . 497 0821 |
| 0.650 | 0.2822914 | 1.915541 | 0.5220458 | 0.700 | 0.3040061 | 2.013753 | 0.4955853 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathbf{u}}$ | $e^{-}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{u}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.700 | 0.3040061 | 2.013753 | 0.4965853 | 0.750 | 0.3257209 | 2.117000 | 0.4723666 |
| . 701 | . 3044404 | . 015767 | . 496 0850 | .751 | . 3261552 | . 119118 | . 4718944 |
| . 702 | - 3048747 | . 017784 | . 495 5931 | . 752 | . 3265895 | . 121238 | -471 4228 |
| . 703 | - 3053090 | . 019803 | -495 0978 | . 753 | -3270237 | . 123361 | . 4709516 |
| .70'4 | . 3057433 | .021 824 | . 4946029 | . 754 | . 3274580 | . 125485 | -470 4809 |
| 0.705 | 0.3061776 | 2.023847 | 0.4941086 | 0.755 | 0.3278923 | 2.127612 | 0.470 oro6 |
| . 705 | . 3066119 | ${ }^{\prime} .025872$ | . 4936147 | . 756 | . 3283266 | . 129740 | . 4695408 |
| . 707 | - 3070462 | . 027898 | -493 1213 | . 757 | . 3287609 | . 131871 | . 4690715 |
| . 708 | -3074805 | . 029927 | . 4926285 | -7.78 | . 3291952 | . 134004 | . 4686027 |
| . 709 | - 3079148 | .031 958 | . 492 I 36 I | . 759 | . 3296295 | . 136139 | . 468 I343 |
| 0.710 | 0.3083491 | 2.033991 | 0.491 6442 | 0.760 | 0.3300638 | 2.1381276 | 0.4676664 |
| . 711 | . 3087834 | . 036026 | .491 1528 | . 761 | -330 4981 | . 140416 | . 4671990 |
| . 712 | -309 2177 | . 038063 | .4906619 | . 762 | -330 9324 | . I42 557 | . 4667320 |
| . 713 | - 3096520 | . 040102 | . 4901715 | . 763 | -331 3667 | . 1447801 | . 4662655 |
| . 714 | . 310085 | . 042144 | . 4896815 | . 764 | . 33180 | . 146846 | . 4657995 |
| 0.715 | 0.3105206 | 2.044187 | 0.489 1921 | 0.765 | 0.3322353 | 2. 148994 | 0.4653339 |
| . 716 | -310 9548 | . 046232 | . 4887032 | . 766 | - 3326696 | .151 144 | . 4648588 |
| . 717 | -311 3891 | . 048279 | . 4882147 | . 767 | . 3331039 | . 153297 | . 4644042 |
| . 718 | -3II 8234 | . 050328 | -487 7267 | . 768 | -333 5382 | . 155451 | . 4639400 |
| . 719 | . 3122577 | . 052380 | . 4872393 | . 769 | . 3339725 | . 157608 | . 4634763 |
| 0.720 | 0.3126920 | 2.054433 | 0.4867523 | 0.770 | 0.3344068 | 2. 159766 | 0.4630131 |
| .721 | .313 1263 | . 056489 | . 4852657 | .771 | - 334 8410 | .16I 927 | . 4625503 |
| . 72 | .313 5606 | . 058546 | . 4857797 | . 77 | -335 2753 | . 164090 | . 4620880 |
| . 723 | . 3139949 | . 060606 | . 4852942 | . 773 | - 3357096 | . 166255 | . 4616261 |
| . 724 | . 3144292 | . 062667 | :484 809r | . 774 | . 3361439 | . 168423 | . 4611647 |
| 0.725 | 0.3148635 | 2.054 731 | 0.4843246 | 0.775 | 0.3365782 | 2.170592 | 0.4607038 |
| . 726 | -315 2978 | . 066797 | . 4838405 | . 776 | . 3370125 | . 172764 | . 4602433 |
| -7 | . 3157321 | . 068865 | . 4833569 | . 777 | . 3374468 | . 174938 | . 4597833 |
| . 728 | .316 1664 | . 070935 | . 4828738 | . 778 | -337. 8811 | . 177114 | -459 3237 |
| . 729 | .316 6007 | . 073007 | . 482 3911 | . 779 | . 3383154 | . 179292 | . 4588646 |
| 0.730 | 0.3170350 | 2.07508 I | 0.4819090 | 0.780 | 0.3387497 | 2.181 472 | 0.4584060 |
| . 731 | . 3174693 | . 077157 | .481 4273 | .781 | . 3391840 | .183 655 | . 4579478 |
| . 73 | -3179036 | . 079235 | . 480 9461 | . 782 | -339 6183 | . 185840 | -457 4901 |
| . 733 | . 3183379 | .081 315 | . 4804654 | . 783 | -340 0526 | . 188027 | . 4570329 |
| . 734 | . 3187721 | . 083398 | . 4799852 | . 784 | . 3404869 | . 190216 | . 4565760 |
| 0.735 | 0.3192064 | 2.085482 | 0.4795055 | 0.785 | 0.3409212 | 2. 192407 | 0.4561197 |
| . 736 | . 3196407 | . 087569 | . 4790262 | . 786 | . 3413555 | . 194600 | . 4556638 |
| . 737 | - 3200750 | . 089657 | -4785474 | . 787 | -341 7898 | . 196796 | -455 2084 |
| . 738 | - 3205093 | .091 748 | .478 0691 |  | - 3422241 | . 198994 | -454 7534 |
| . 739 | -3209436 | . 093841 | . 4775913 | . 789 | -3426583 | . 201194 | -454 2989 |
| 0.740 | 0.3213779 | 2.095936 | 0.4771139 | 0.790 | 0.3430926 | 2.203396 | 0. 4538448 |
| .741 | -3218122 | . 098032 | . 4766370 | .791 | -343 5269 | . 205601 | -453 3912 |
| . 742 | - 3222465 | . 100132 | . 4761686 | . 792 | - 3439612 | . 207808 | -4529380 |
| . 743 | . 3226808 | . 102233 | . 4756847 | . 793 | - 3443955 | .210 017 | . 4524853 |
| . 744 | -323 I151 | . 104336 | .475 2093 | . 794 | - 3448298 | . 212228 | . 4520330 |
| 0.745 | 0.3235494 | 2.106 44I | 0.4747343 | 0.795 | 0.3452641 | 2.214441 | 0.4515812 |
| . 746 | . 3239837 | . 108549 | . 4742598 | . 796 | - 3456984 | . 216657 | .451 1299 |
| . 747 | - 3244180 | . 110659 | . 4737858 | . 797 | -346 1327 | . 218874 |  |
| 2. 748 | - 3248523 | . 112770 | . 4733122 | . 798 | - 3465670 | .221 094 | . 4502285 |
| . 749 | . 3252856 | . 114884 | . 4728392 | . 799 | -347 0013 | . 223 316 | . 4497785 |
| 0.750 | 0.3257209 | 2.117000 | 0.4723656 | 0.800 | 0.3474356 | 2.225541 | 0.4493290 |
| $\log _{\text {e }}\left({ }^{\text {u }}\right.$ ) | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-u}$ |

The Exponential.

| a | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{u}}$ | $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {a }}$ | $\mathrm{e}^{-\mathrm{u}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.800 | 0.3474356 | 2.225 541 | 0.4493290 | 0.850 | 0.3691503 | 2.339647 | 0.4274149 |
| . 8 | . 3478699 | . 2227768 | . 4488799 | . 851 | . 3695846 | . 341988 | . 4269877 |
| . 802 | - 3483042 | . 229996 | . 4484312 | . 852 | -370 0189 | - 344 331 | . 4265610 |
| . 803 | . 3487385 | . 232228 | -4479830 | . 853 | - 3704532 | . 346676 | . 426 I346 |
|  | -349 1728 | . 234461 | . 4475352 | . 854 | - 3708875 | - 349024 | . 4257087 |
| 0.805 | 0.3496071 | 2.236696 | 0.4470879 | 0.855 | 0.3713218 | 2.351374 | 0.425 2832 |
| . | . 3500414 | . 238934 | . 4466411 | . 856 | . 371 7561 | . 353727 | . 424858 I |
| . 8 | - 3504756 | . 241174 | . 4461946 | . 857 | . 3721904 | . 356082 | . 4244335 |
|  | -350 9099 | . 243417 | . 4457487 | . 858 | - 3726247 | . 358439 | . 4240093 |
| . 809 | -351 3442 | . 245661 | . 4453031 | . 859 | - 3730590 | . 360799 | . 4235855 |
| 0.8 io | 0.3517785 | 2.247908 | 0.444858 I | 0.860 | 0.3734933 | 2.363 16I | 0.4231621 |
| .8II | . 3522128 | . 250157 | -444 4I34 | . 861 | . 3739275 | . 365525 | . 4227391 |
| .812 | - 352647 I | .252408 | . 4439592 | . 862 | - 374 3618 | . 367892 | . 42231006 |
| .813 .814 | -353 0814 | . 254662 | . 4435255 | . 863 | - 374.7961 | . 370261 | . 4218945 |
|  | .353 5157 | . 256918 | . 4430822 | . 864 | - $375{ }^{\circ} 2304$ | . 372632 | . 4214728 |
| 0.815 | 0.3539500 | 2.259176 | 0.4426393 | 0.865 | 0.3756647 | 2.375006 | 0.4210516 |
| .816 | . 3543843 | . 261436 | . 4421969 | . 866 | . 3760990 | . 377382 | . 4206307 |
| .817 <br> .818 <br> 81 | - 3548185 | . 263699 | -441 7549 | . 867 | - 3765333 | . 379761 | . 4202103 |
|  | - 3552529 | . 265963 | .441 3134 | . 868 | - 3769676 | . 382142 | . 4197903 |
| 19 | -355 6872 | . 268230 | . 4408723 | . 869 | -3774019 | -384 525 | .4193707 |
| 0.820 | 0.3561215 | 2.270500 | 0.4404317 | 0.870 | 0.3778362 | 2.386911 | 0.4189515 |
| . 821 | . 3565558 | . 272771 | . 4399914 | . 87 I | . 3782705 | . 389299 | . 4185328 |
| . 822 | -356 9901 | . 275045 | . 4395517 | . 872 | . 3787048 | -391 689 | . 4181145 |
| . 823 | .3574244 .3578587 | .277322 .279600 | . $433 \mathrm{II23}$ | . 873 | . 3791391 | - 394082 | . 4176966 |
|  | -357.8587 | . 279600 | .438 6734 | . 874 | -379 5734 | -396478 | .417 2791 |
| 0.825 | 0.3582929 | 2.28188 I | 0.4382350 |  | 0.3800077 | 2.398875 | 0.4168620 |
| . 826 | . 3587272 | . 284164 | . 4377970 | . 875 | . 3804420 | . 401275 | . 4164454 |
| .827 .828 | .3591615 <br> .3595958 | . 285449 | . 4373594 | . 877 | - 3808763 | . 403678 | . 4160291 |
| .828 .829 | .3595958 .3600301 | .288737 .291027 | . .4369223 | . 878 | .381 .381 .3106 7448 | . 406083 | . 4156133 |
|  |  | . 291027 |  |  | -381 7448 | . 408490 | .415 1979 |
| 0.830 | 0.3604644 | 2.293319 | 0.4360493 | 0.880 | 0.382 I 791 | 2.410900 | 0.4147829 |
| . 831 | . 3608987 | . 295613 | . 4356135 | . 881 | . 382 6134 | .413 312 | . 4143683 |
| . 832 | -361 3330 | . 297910 | . 435 1781 | . 882 | . 3830477 | . 415726 | . 4139542 |
| . 833 | . 3617673 | . 300209 | . 4347431 | . 883 | - 3834820 | . 418143 | .413 5404 |
| . 834 | . 3622016 | . 302510 | -434 3086 | . 884 | . 3839163 | . 420563 | .413 1271 |
| 0.835 | 0.3626359 | 2.304814 |  | 0.885 | 0.3843506 | 2.422984 | 0.4127142 |
| . 836 | . 3630702 | . 307120 | . 4334408 | . 885 | . 3847849 | .425409 | . 4123017 |
| . 837 | . 3635045 | - 309428 | . 4330076 | . 887 | . 3852192 | . 427835 | .41I 8896 |
| .838 .839 | .3639388 .3643731 | $\begin{array}{r}\text {.311 } 739 \\ .314 \\ \hline 142\end{array}$ | .4325748 .4321424 | . 888 | -3856535 | . 430264 | .411 4779 |
| . 839 | -364 3731 | . 314052 | .432 1424 | . 889 | - 3860878 | . 432696 | -4II 0666 |
| 0.840 | 0.3648074 | 2.316367 | 0.4317105 | 0.890 | 0.3865221 | 2.435130 | 0.410 6558 |
| . 841 | . 3652417 | . 318685 | .431 2790 | . 891 | -3869564 | . 437566 | . 4102453 |
| . 842 | . 3656760 | -321 004 | . 4308480 | . 892 | . 3873907 | . 440005 | -4098353 |
| . 843 | - 3661102 | . 323327 | . 4304173 | . 893 | - 3878250 | . 442446 | -409 4256 |
| . $8+4$ | -3565445 | . 325651 | . 4299871 | . 894 | . 3882593 | . 444890 | -409 or64 |
| 0.845 | 0.3669788 | 2.327978 | 0.4295574 | 0.895 |  |  |  |
| . 846 | . 3674131 | . 330307 | . 429 I 280 | . 896 | . 3891279 | . 449784 | $.408 \text { I992 }$ |
| . 847 | - 3678474 | - 332638 | . 4286991 | . 897 | -389 5622 | . 452235 | $.407742$ |
| . 848 | .3682817 .3687160 | $\begin{array}{r}.334972 \\ .337 \\ \hline\end{array}$ | .4282706 .4278426 | .898 .899 | .3899964 .3904307 | . 454689 | - 40738836 |
| . 849 | -3687160 | -337308 | . 4278426 | . 899 | -390 4307 | -457 145 | -4069764 |
| 0.850 | 0.3691503 | 2.339647 | 0.4274149 | 0.900 | 0.3908650 | 2.459603 | 0.4065697 |
| $\log _{\text {c }}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-0}$ | $\log _{\text {e }}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\log _{10}\left(e^{\text {a }}\right.$ ) | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.900 | 0.3908650 | 2.459603 | 0.4065697 | 0.950 | 0.4125798 | 2.585710 | 0.3867410 |
| . 901 | . 3912993 | .462064 | . 4061633 | .95I | . 413 OI4I | . 588297 | . 3863545 |
| . 902 | . 3917336 | . 464527 | . 4057573 | . 952 | . 4134483 | . 590886 | . 3859683 |
| . 903 | . 3921679 | . 466993 | . 4053518 | . 953 | . 4138826 | . 593478 | . 3855825 |
| . 904 | . 3926022 | . 469 46I | . 4049466 | . 954 | . 4143169 | . 595073 | . 385 I97I |
| 0.905 | 0.3930365 | 2.471 932 | 0.4045419 | 0.955 | 0.4147512 | 2.598671 | 0.384 8121 |
| . 905 | .3934708 | . 474405 | . 4041375 | . 956 | .415 1855 | .601 271 | . 3844275 |
| . 907 | . 393 905I | . 476 881 | . 4037336 | . 957 | .415 6198 | .603873 | . 3840433 |
| . 908 | - 3943394 | . 479359 | . 4033301 | . 958 | . 416054 I | . 606478 | . 3836594 |
| .909 | . 3947737 | .481 839 | . 4029269 | . 959 | .4164884 | . 609086 | . 3832760 |
| 0.910 | 0.3952080 | 2.484323 | 0.4025242 | 0.960 | 0.4169227 | 2.6II 696 | 0.3828929 |
| .9II | . 3956423 | . 486808 | . 4021219 | .95I | . 4173570 | . 614309 | . 3825102 |
| .912 | . 3960766 | . 489295 | . 4017200 | . 962 | . 4177913 | .616 925 | . 3821279 |
| .913 | - 3965109 | . 491787 | . 4013185 | .963 | . 4182256 | . 619543 | -38I 7459 |
| . 914 | - 3969452 | . 494280 | . 4009173 | . 964 | .418 6599 | .622164 | . 3813644 |
| 0.915 | 0.3973795 | 2.496775 | 0.4005166 | 0.965 | 0.4190942 | 2.624788 | 0.3809832 |
| . 916 | . 397 8137 | . 499273 | . 400 I 163 | . 966 | . 4195285 | . 627 414 | . 3806024 |
| .917 | - 3982480 | . 501774 | - 3997164 | . 967 | . 4199628 | .630042 | . 3802220 |
| .918 | - 3986823 | . 504277 | - 3993169 | .958 | . 4203971 | .632674 | . 3798420 |
| . 919 | . 399 II66 | . 506782 | - 398 9178 | . 969 | . 4208314 | .635308 | . 379.4623 |
| 0.920 | 0.3995509 | '2.509 290 | 0.3985190 | 0.970 | 0.4212656 | 2.637944 | 0.3790830 |
| . 921 | . 3999852 | .5II 801 | . 3981207 | .971 | . 4216999 | . 640584 | . 3787041 |
| . 922 | . 4004195 | .514 314 | - 3977228 | . 972 | . 4221342 | .643225 | - 3783256 |
| . 923 | . 4008538 | . 516830 | . 3973253 | . 973 | . 4225685 | .645870 | - 3779475 |
| . 924 | . 401 288I | . 519348 | - 396 9281 | . 974 | . 4230028 | .648517 | - 3775697 |
| 0.925 | 0.401 7224 | 2.521868 | 0.3965314 | 0.975 | 0.4234371 | 2.651167 | 0.3771924 |
| . 926 | . 4021567 | . 524391 | . 396 I35I | . 976 | . 4238714 | . 653820 | . 376 8153 |
| . 927 | .4025910 | . 526917 | - 3957391 | . 977 | . 4243057 | -. 656475 | - 3764387 |
| . 928 | . 4030253 | . 529445 | . 3953436 | . 978 | . 4247400 | .659 I33 | $.3760525$ |
| . 929 | .4034596 | . 531976 | . 3949485 | . 979 | . 425 I743 | .661 793 | . 3756866 |
| 0.930 | 0.4038939 | 2.534509 | 0.3945537 | 0.980 | 0.4256086 | 2.664456 | 0.375 3III |
| .93I | . 4043282 | . 537045 | . 3941594 | .98I | . 4260429 | . 667122 | . 3749360 |
| . 932 | . 4047625 | . 539583 | . 3937654 | . 982 | . 4264772 | . 669790 | . 3745612 |
| . 933 | . 405 I968 | . 542124 | - 3933718 | . 983 | . 426 9115 | .672462 | . 374 I869 |
| . 934 | .4056310 | . 544668 | . 3929786 | . 984 | .4273458 | . 675135 | . 373 8129 |
| 0.935 | 0.4060653 | 2.547213 | 0.3925859 | 0.985 | 0.427 7801 | 2.677 812 | 0.3734392 |
| . 936 | . 4064996 | . 549762 | . 3921935 | . 986 | . 4282144 | . 68049 I | . 3730660 |
| . 937 | . 4069339 | . 552313 | -391 8015 | . 987 | . 4286487 | . 683 I73 | . 3726931 |
| . 938 | . 4073682 | . 554867 | . 3914099 | . 988 | . 4290829 | .685857 | . 3723206 |
| . 939 | . 4078025 | . 557433 | .391 0187 | . 989 | .4295172 | . 688545 | . 3719485 |
| 0.940 | 0.4082368 | 2.559 981 | 0.3906278 | 0.990 | 0.4299515 | 2.691234 | 0.3715767 |
| .94I | . 4086711 | . 562543 | . 3902374 | .99I | . 4303858 | . 693927 | . 3712053 |
| . 942 | . 4091054 | . 565107 | . 3898474 | . 992 | . 4308201 | . 696622 | . 3708343 |
| . 943 | . 4095397 | .567673 | . 3894577 | . 993 | . 43 I 2544 | .699320 | - 3704635 |
| . 944 | . 4099740 | . 570242 | . 3890684 | . 994 | . 43 I 6887 | . 702021 | . 3700934 |
| 0.945 | 0.4104083 | 2.572813 | 0.3886796 | 0.995 | 0.432 I 230 |  | $0.3697234$ |
| . 946 | . 4108426 | . 575387 | . 3882911 | . 996 | . 4325573 | . 707430 | $\text { . } 3693539$ |
| . 947 | .4II 2769 | . 577964 | .3879030 | -. 997 | . 4329916 | . 710139 | $\text { . } 3689847$ |
| .948 | -411 7II2 | . 580543 | -3875153 | . 998 | - 4334259 | . 712851 | . 368 6I59 |
| . 949 | .4121455 | . 583 I 25 | . 387 I280 | . 999 | . 4338502 | .715 565 | . 3682475 |
| 0.950 | 0.4125798 | 2.585710 | 0.3867410 | I . 000 | 0.4342945 | 2.718282 | 0.3678794 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-}$ | $\log _{\mathrm{e}}\left(\theta^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-0}$ | $u$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.000 | 0.4342945 | 2.718282 | 0.3678794 | 1.050 | 0.4560092 | 2.857651 |  |
| . 001 | . 4347288 | . 721001 | . 3675117 | . 051 | . 4564435 | . 860 510 | $.3495880$ |
| . 002 | . 4351631 | .723724 | . 3671444 | . 052 | . 4568778 | . 863372 | . 3492386 |
| . 003 | . 4355974 | .726449 | . 3667775 | . 053 | . 457 3121 | . 866237 | . 3488895 |
| . 004 | . 4360317 | . 729 I77 | .3664109 | . 054 | . 4577464 | . 869105 | $\text { . } 3485408$ |
| 1.005 | 0.4364660 | 2.731907 | 0.3660446 | 1.055 | 0.4581807 | 2.871975 | 0.3481924 |
| . 006 | . 4369002 | . 734641 | . 3656788 | . 056 | . 458 6150 | . 874849 | . 3478444 |
| .007 | . 4373345 | . 737377 | . 365 3133 | . 057 | . 4590493 | . 877725 | . 3474967 |
| . 008 | . 4377688 | . 740 II5 | . 364 9481 | . 058 | . 4594836 | . 880604 | $.347 \quad 1494$ |
| . 009 | . 4382031 | . 742857 | . 3645834 | . 059 | . 459 9179 | . 883486 | $\cdot 3468024$ |
| 1.010 | 0.4386374 | 2.745601 | 0.3642190 | 1.060 | 0.4603522 | 2.886371 | 0.3464558 |
| . 011 | . 4390717 | . 7483848 | . 3638549 | .06I | . 4607854 | . 889259 | $.3461095$ |
| . 012 | . 4395050 | .751 098 | .3634913 | . 062 | .461 2207 | . 892150 | -3457636 |
| . 013 | . 4399403 | . 753850 | . 3631280 | . 063 | . 4616550 | . 895043 | . 3454180 |
| . 014 | . 4403746 | . 756605 | . 3627650 | . 064 | .4620893 | . 897940 | . 3450728 |
| 1.015 | 0.4408089 | 2.759363 | 0.3624024 | 1.065 | 0.4625236 | 2.900839 | 0.3447279 |
| . 016 | -441 2432 | . 762124 | . 3620402 | . 066 | . 4629579 | .903741 | . 3443833 |
| . 017 | .441 6775 | . 764888 | .361 6783 | . 067 | . 4633922 | . 906646 | . 344 0391 |
| . 018 | . 442 III8 | . 767654 | .36i 3169 | . 068 | . 4638265 | . 909555 | . 3436952 |
| . 019 | . 442 546I | . 770423 | . 3609557 | . 069 | . 4642608 | . 912466 | - 343 35I7 |
| 1.020 | 0.4429804 | 2.773 I95 | 0.3605949 | - 1.070 | 0.4646951 | 2.915379 | 0.3430085 |
| . 021 | . 4434147 | . 775969 | - 3602345 | . 071 | .4651294 | . 918296 | . 3426657 |
| . 022 | . 4438890 | . 778747 | - 3598745 | . 072 | .4655637 | .921 216 | - 3423232 |
| . 023 | . 4442833 | .781 527 | . 3595148 | . 073 | . 4659980 | . 924139 | . 3419810 |
| . 024 | . 4447175 | . 784310 | - 359 I554 | . 074 | . 4664323 | . 927064 | .341 6392 |
| 1.025 | 0.4451518 | 2.787095 | 0.3587965 | 1.075 | 0.4668666 | 2.929993 | 0.3412978 |
| . 026 | . 445 5861 | . 789884 | . 3584378 | . 076 | . 4673009 | . 932924 | . 3409566 |
| . 027 | .4460204 | . 792675 | . 3580796 | . 077 | . 4677352 | .935859 | -340 6158 |
| . 028 | . 4464547 | .795469 | . 3577217 | . 078 | . 468 I695 | . 938796 | . 3402754 |
| . 029 | . 4468890 | . 798266 | . 3573641 | . 079 | .4686037 | .941 736 | . 3399353 |
| 1.030 | 0.4473233 | 2.801066 | 0.3570070 | 1.080 | 0.4690380 | 2.944680 | 0.3395955 |
| .03I | . 4477576 | . 803868 | . 356 6501 | .08I | . 4694723 | . 947626 | . 339 2561 |
| . 032 | . 4481919 | . 806674 | . 3562937 | . 082 | . 4699066 | . 950575 | . 3389170 |
| . 033 | . 4486262 | . 809482 | . 3559375 | . 083 | . 4703409 | . 953527 | . 3385783 |
| . 034 | . 4490605 | .8I2 293 | - 355 5818 | . 084 | . 4707752 | . 956482 | . 3382399 |
| 1.035 | 0.4494948 | 2.8 I 5106 | 0.3552264 | 1.085 | 0.4712095 | 2.959440 | 0.3379018 |
| . 036 | . 4499291 | .817 923 | . 3548713 | . 086 | . 4716438 | . 962401 | . 3375641 |
| . 037 | . 4503634 | .820742 | . 3545166 | . 087 | . 472078 I | . 965365 | . 3372267 |
| . 038 | . 4507977 | . 823564 | . 354 1623 | . 088 | . 4725124 | . 96833 I | . 3368896 |
| . 039 | . 4512320 | . 826389 | . 3538083 | . 089 | . 4729467 | .971 301 | . 3365529 |
| 1.040 | 0.4516663 | 2.829217 | 0.3534547 | 1.090 | 0.473 3810 | 2.974274 | 0.3362165 |
| . 041 | . 4521006 | . 832048 | . 353 IOI4 | .091 | . 473 8153 | . 977250 | . 3358804 |
| . 042 | . 4525349 | . 834 881 | - 3527485 | . 092 | . 4742495 | . 980229 | . 3355447 |
| . 043 | . 4529691 | . 837717 | . 3523959 | . 093 | . 4746839 | .983210 | . 3352094 |
| . 044 | . 4534034 | . 840557 | - 3520437 | . 094 | . 475 I I82 | . 986195 | . 3348743 |
| 1.045 | 0.4538377 | 2.843399 | 0.351 6918 | 1.095 | 0.4755525 | 2.989 I83 | 0.3345396 |
| . 046 | . 4542720 | . 846243 | -351 3403 | . 096 | . 4759868 | . 992 I73 | . 3342052 |
| . 047 | . 4547063 | . 849091 | . 3509891 | . 097 | . 4764210 | . 995167 | - 3338712 |
| . 048 | . 4551406 | . 851942 | . 3506383 | . 098 | . 4768553 | . 998164 | . 3335375 |
| . 049 | . 4555749 | . 854795 | - 3502879 | . 099 | . 4772896 | 3.001163 | . 333 2041 |
| 1.050 | 0.4560092 | 2.85765 I | 0.3499377 | I. 100 | 0.4777239 | 3.004166 | 0.3328711 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-a}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

Smithsonian Tables

The Exponential.


The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right.$ ) | $\epsilon^{u}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.200 | 0.5211534 | 3.320 I17 | 0.301 1942 | 1.250 | 0.542868 r | 3.490343 | 0.2865048 |
| . 201 | . 5215877 | . 323439 | . 3008932 | .25I | . 5433024 | . 493835 | . 2862184 |
| . 202 | . 5220220 | . 326764 | - 3005924 | . 252 | . 5437367 | . 49733 I | . 2859324 |
| . 203 | . 5224563 | -330 092 | - 3002920 | . 253 | . 5441710 | . 500830 | . 2856466 |
| . 204 | . 5228906 | . 333424 | . 2999918 | . 254 | . 5446053 | . 504332 | . 285 3611 |
| 1.205 | 0.5233249 | $3 \cdot 336759$ | 0.2996920 | I. 255 | 0.5450396 | 3.507838 | 0.2850758 |
| . 206 | . 5237591 | . 340098 | . 2993925 | . 256 | . 5454739 | . 5 II 348 | . 2847909 |
| .207 | . 5241934 | - 343439 | . 2990932 | . 257 | . 5459082 | . 514851 | .2845063 |
| . 208 | . 5246277 | . 346784 | . 2987943 | . 258 | . 5463425 | . 518378 | . 2842219 |
| . 209 | . 5250620 | . 350133 | .2984956 | . 259 | . 5467768 | . 521898 | . 2839378 |
| 1.210 | 0.5254963 | 3.353485 | 0.2981973 | 1.260 | 0.5472110 | 3.52542 I | 0.2836540 |
| . 211 | . 5259306 | . 356840 | . 2978992 | . 261 | . 5476453 | . 528949 | . 2833705 |
| . 212 | . 5253649 | . 360198 | . 2976015 | . 262 | . 5480796 | . 532479 | . 2830873 |
| . 213 | . 5267992 | . 363560 | . 2973040 | . 263 | . 548 5I39 | . 536 OI4 | . 2828043 |
| . 214 | . 5272335 | . 366925 | . 2970059 | . 264 | . 5489482 | . 539 551 | .2825217 |
| 1.215 | 0.5276678 | 3.370294 | 0.2967100 | I. 265 | 0.5493825 | 3.543093 | 0.2822393 |
| . 216 | . 528 1021 | . 373666 | .2964135 | . 266 | - 549 8168 | . 546638 | . 281 9572 |
| . 217 | . 5285354 | . 377041 | . 2961772 | . 267 | . 55025 II | . 550186 | .28I 6754 |
| . 218 | . 5289707 | . 380420 | . 2958212 | . 268 | . 5506854 | . 553738 | .281 3938 |
| . 219 | . 5294050 | . 383802 | . 2955255 | . 269 | .551 1197 | . 557293 | .281 II26 |
| 1.220 | 0.5298393 | 3.387188 | 0.2952302 | 1.270 | O.551 5540 | 3.560853 | 0.280 8316 |
| . 22 I | . 5302736 | . 390577 | . 2949351 | . 271 | . 5519883 | . 564415 | . 2805509 |
| . 222 | . 5307079 | . 393969 | . 2946403 | . 272 | . 5524226 | . 56798 I | . 2802705 |
| . 223 | . 5311422 | . 397365 | . 2943458 | . 273 | . 5528569 | . 571551 | . 2799904 |
| . 224 | . 5315764 | . 400764 | . 2940516 | . 274 | . 5532912 | . 575124 | . 2797105 |
| 1.225 | 0.5320107 | 3.404166 | 0.2937577 | I. 275 | 0.5537255 | 3.578701 | 0.2794310 |
| . 226 | . 5324450 | . 407572 | . 2934641 | . 276 | . 5541598 | . 582282 | . 2791517 |
| . 227 | . 5328793 | . 410 981 | . 2931708 | . 277 | . 554594 I | . 585866 | . 2788727 |
| . 228 | . 533 3I36 | . 414394 | . 2928777 | . 278 | . 5550283 | . 589454 | . 2785939 |
| . 229 | . 5337479 | . 417810 | . 2925850 | . 279 | . 5554626 | . 593045 | . 2783155 |
| I. 230 | 0.5341822 | 3.421230 | 0.2922926 | 1.280 | 0.5558969 | 3.596640 | 0.2780373 |
| .23I | . 5346165 | . 424652 | . 2920004 | . 281 | . 5563312 | . 600238 | . 2777594 |
| . 232 | . 5350508 | . 428079 | . 2917086 | . 282 | . 5567655 | . 603840 | . 2774818 |
| . 233 | . 535485 I | . 431509 | . 2914170 | . 283 | . 5571998 | . 607446 | . 2772044 |
| . 234 | . 5359194 | . 434942 | . 2911257 | . 284 | . 557634 I | .6II 055 | .2769274 |
| 1.235 | 0.5363537 | 3.438379 | 0. 2908348 | I. 285 | 0.5580684 | 3.614668 | 0.2766506 |
| . 236 | . 5367880 | . 441819 | . 290544 I | . 286 | . 5585027 | . 618284 | . 2763741 |
| . 237 | . 5372223 | . 445262 | . 2902537 | . 287 | . 5589370 | . 621905 | . 2760978 |
| . 238 | . 5376566 | . 448709 | .2899636 | . 288 | . 5593713 | . 625528 | . 2758219 |
| . 239 | . 5380909 | .452160 | .2896737 | . 289 | . 5598056 | . 629156 | .2755462 |
| I. 240 | 0.5385252 | 3.455613 | 0.2893842 | I. 290 | 0.5602399 | 3.632787 | 0.2752708 |
| . 241 | . 5389595 | . 459071 | . 2890950 | . 291 | . 5606742 | . 636421 | . 2749956 |
| . 242 | . 5393937 | . 462532 | . 2888060 | 292 | . 5611085 | . 640059 | . $27+7208$ |
| . 243 | . 5398280 | . 465996 | . 288 5174 | 293 | . 5615428 | . 643701 | .2744462 |
| . 244 | . 5402623 | . 469464 | .2882290 | . 294 | . 5619771 | . 647347 | . 274 I719 |
| 1.245 | 0.5406966 | 3.472935 | 0.2879409 | 1.295 | 0.5624114 | 3.650996 | 0.2738979 |
| . 246 | . 5411309 | . 476409 | . 2876531 | . 296 | . 5628456 | . 654649 | . 2736241 |
| . 247 | . 5415652 | . 479888 | .2873656 | . 297 | . 5632799 | . 658305 | . 2733506 |
| . 248 | . 5419995 | .483369 | .2870784 | . 298 | . 5637142 | . 661965 | . 2730774 |
| . 249 | . 5424338 | . 486854 | .2867914 | . 299 | . 5641485 | .665629 | . 2728045 |
| I. 250 | 0.542868 r | 3.490343 | 0.2865048 | 1.300 | 0.5645828 | 3.659297 | 0.2725318 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-a}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.300 | 0.5645828 | 3.669297 | 0.2725318 | 1.350 | 0.5862976 | 3.857426 | 0.2592403 |
| . 301 | . 5650171 | . 672968 | . 2722594 | . 351 | . 5867318 | . 861285 | . 258 9811 |
| - 302 | - 5654514 | . 676643 | . 271 | - 352 | . 5871661 | . 865148 | . 2587223 |
| - 303 | - 5658857 | . 680321 | . 2717154 | - 353 | . 5876004 | . 869 ol5 | . 2584637 |
| -304 | . 5663200 | . 684003 | . 2714438 | - 354 | . 5880347 | . 872886 | . 2582054 |
| 1.305 | 0.5667543 | 3.687689 | 0.2711725 | 1.355 | 0.5884690 | 3.876761 | 0.2579473 |
| . 306 | . 567 I886 | .691 379 | . 2709015 | . 356 | . 5889033 | . 880640 | . 2576895 |
| . 307 | . 5676229 | . 695072 | . 2706307 | . 357 | . 5893376 | . 884522 | . 2574319 |
| . 308 | . 5680572 | . 698769 | . 2703602 | - 358 | . 5897719 | . 888409 | .2571746 |
| -309 | . 5684915 | . 702469 | . 2700900 | -359 | - 5902062 | . 892299 | . 2569176 |
| 1.310 | 0.5689258 | 3.706174 | 0.2698201 | 1. 360 | 0.5906405 | 3.896193 | 0.2566608 |
| .311 | . 5693601 | . 709882 | . 2695504 | -361 | . 5910748 | . 900091 | . 2564042 |
| -312 | - 5697944 | . 713593 | . 2692810 | - 362 | . 591 5091 | . 903993 | . 2561480 |
| -313 | . 5702287 | . 717309 | . 259 O118 | - 363 | .591 9434 | . 907899 | . 2558919 |
| -314 | -570 6629 | .721 028 | . 2687429 | - 364 | . 5923777 | .911 809 | .2556362 |
| 1.315 | 0.5710972 | 3.724751 | 0.2684743 | 1. 365 | 0. 5928120 | 3.915723 | 0.2553807 |
| -316 | . 5715315 | . 728478 | . 2682060 | - 366 | . 5932463 | . 91964 I | . 2551254 |
| -317 | -571 9658 | . 732208 | . 2679379 | - 367 | - 5936806 | . 923562 | . 2548704 |
| -318 | . 5724001 | . 735942 | .2676701 | . 368 | . 5941149 | . 927488 | . 2546157 |
| .319 | . 5728344 | . 739680 | . 2674026 | - 369 | . 594 5491 | .931 417 | .254 3612 |
| 1.320 | 0.5732687 | 3.743421 | 0.2671353 | 1. 370 | 0. 5949834 | 3.935351 | 0.2541070 |
| . 321 | . 5737030 | . 747167 | . 2668683 | -371 | . 5954177 | . 939288 | . 2538530 |
| - 322 | . 5741373 | . 750916 | . 2666016 | - 372 | . 5958520 | . 943229 | . 2535993 |
| - 323 | . 5745716 | . 754669 | .2663351 | - 373 | . 5962863 | . 947174 | . 2533458 |
| -324 | . 5750059 | . 758425 | . 2660689 | - 374 | . 5967206 | .951 124 | .2530926 |
| 1.325 | 0.5754402 | 3.762185 | 0.2658030 | 1.375 | 0.5971549 | 3.955077 | 0.2528396 |
| . 326 | . 5758745 | . 765949 | . 2655373 | - 376 | . 5975892 | . 959034 | . 2525869 |
| - 327 | - 5763088 | . 769717 | . 2652719 | - 377 | . 5980235 | . 962995 | . 2523344 |
| - 328 | -576 7431 | . 773489 | . 2650067 | - 378 | - 5984578 | . 966960 | . 2520822 |
| . 329 | . 5771774 | . 777264 | . 2647419 | - 379 | -5988921 | . 970929 | .2518303 |
| 1.330 | 0.5776117 | 3.781043 | 0.2644773 | I. 380 | 0.5993264 | 3.974 902 | 0.2515786 |
| .331 | . 5780460 | . 784826 | . 2642129 | -381 | . 5997607 | . 978879 | ..251 3271 |
| -332 | - 5784802 | . 788613 | . 2639488 | - 382 | . 6001950 | . 982859 | . 2510759 |
| -333 | . 5789145 | . 792404 | . 2636850 | - 383 | . 6006293 | . 986844 | . 2508249 |
| -334 | - 5793488 | . 795198 | . 2634215 | -384 | . 6010636 | . 990833 | . 2505742 |
| 1. 335 | 0.5797831 | 3.799995 | 0.2631582 | I. 385 | 0.601 4979 | 3.994826 | 0.25032 .38 |
| . 336 | -580 2174 | . 803798 | . 2628951 | -386 | . 6019322 | . 998823 | . 2500736 |
| - 337 | -580 6517 | . 807604 | . 2626324 | - 387 | . 6023664 | 4.002824 | . 2498237 |
| - 338 | -581 0860 | .8II 413 | . 2523699 | - 388 | . 6028007 | . 006828 | . 2495740 |
| -339 | .581 5203 | .815 226 | . 2621076 | - 389 | . 6032350 | . 010837 | . 2493245 |
| 1.340 | 0.5819546 | 3.819044 | 0.26I 8457 | I. 390 | 0.6036693 | 4.014850 | 0.2490753 |
| -341 | . 5823889 | . 822864 | . 2615840 | . 391 | . 6041036 | . 018867 | . 2488264 |
| -34 | . 5828232 | . 826689 | . 2613225 | - 392 | . 6045379 | . 022888 | . 2485777 |
| -343 | . 5832575 | . 830518 | . 2610613 | - 393 | . 6049722 | . 026913 | . 2483292 |
| -344 | . 5836918 | . 834350 | . 2608004 | -394 | . 6054065 | . 030942 | . 248 0810 |
| I. 345 | 0.5841261 |  | 0.2605397 | I. 395 | 0.6058408 | 4.034975 | 0.2478330 |
| -346 | . 5845604 | . 842027 | . 2602793 | - 396 | . 6052751 | . 039 OI2 | . 2475853 |
| - 347 | -5849947 | . 845871 | . 2600191 | - 397 | . 6067094 | . 043053 | . 2473379 |
| -348 | . 5854290 | . 849718 | .2597593 | - 398 | . 6071437 | . 047098 | . 2470907 |
| -349 | -585 8633 | . 853570 | . 2594996 | - 399 | . 6075780 | .051 147 | . 2468437 |
| 1.350 | 0.5862976 | 3.857426 | 0.2592403 | 1. 400 | 0.6080123 | 4.055200 | 0.2465970 |
| $\log _{\mathrm{e}}\left(\mathrm{e}{ }^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ |  | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{u}}$ |

Smithsonian Tables

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{a}}\right)$ | $\mathrm{e}^{\text {a }}$ | $e^{-0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.400 | 0.6080123 | 4.055200 | 0.2465970 | 1.450 | 0.6297270 | 4.263115 | 0.2345703 |
| .401 | . 6084466 | . 059257 | . 2463505 | .451 | . 630 1613 | . 267380 | . 2343358 |
| . 402 | . 6088809 | . 063318 | . 2461043 | . 452 | . 6305956 | .271 649 | . 234 Io16 |
| . 403 | . 6093152 | . 067384 | . 2458583 | . 453 | . 6310299 | . 275923 | . 2338676 |
| . 404 | . 6097495 | .071 453 | . 2456125 | . 454 | . 6314642 | . 280201 | . 2336339 |
| 1. 405 | 0.6101837 | 4.075527 | 0.2453671 | 1.455 | 0.6318985 | 4.284483 | 0.2334004 |
| . 406 | . 6106180 | . 079604 | . 2451218 | . 456 | . 6323328 | .288770 | . 2331671 |
| . 407 | .6II 0523 | .083 686 | . 2448768 | . 457 | . 6327571 | . 293061 | . 2329340 |
| . 408 | .6II 4866 | . 087772 | . 2446321 | . 458 | . 6332014 | . 297356 | . 2327012 |
| . 409 | .611 9209 | .091 861 | . 2443875 | . 459 | . 6336356 | . 301656 | . 2324686 |
| 1.410 | 0.6123552 | 4.095955 | 0.2441433 | 1.460 | 0.6340699 | 4.305960 | 0.2322363 |
| . 411 | . 6127895 | . 100053 | . 2438993 | . 461 | . 6345042 | . 310268 | . 2320042 |
| . 412 | . 6132238 | . 104156 | . 2436555 | . 462 | . 6349385 | . 314580 | . 2317723 |
| .413 | .613 6581 | . 108262 | . 2434120 | .463 | . 6353728 | . 318897 | . 2315406 |
| . 414 | . 6140924 | . 112372 | . 2431687 | . 464 | . 6358071 | . 323218 | . 2313092 |
| 1.415 | 0.6145267 | 4.116486 | 0.2429256 | I. 465 | 0.6362414 | 4.327543 | 0.2310780 |
| .416 | .6I4 9610 | . 120605 | . 2426828 | . 466 | . 6366757 | - 331873 | . 2308470 |
| . 417 | . 6153953 | . 124728 | . 2424402 | . 467 | . 6371100 | . 336207 | . 2306163 |
| . 418 | .6158296 .616263 | . 128854 | . 2421979 | . 468 | . 6375443 | . 340545 | . 2303858 |
| .419 | . 6162639 | . 132985 | .241 9559 | . 469 | . 6379786 | - 344888 | . 2301555 |
| 1.420 | 0.6166982 | 4.137120 | 0.2417140 | 1.470 | 0.6384129 | 4.349235 | 0.2299255 |
| . 421 | . 6171325 | . I41 260 | . 2414724 | . 471 | . 6388472 | . 353587 | . 2296957 |
| . 422 | . 6175668 | . 145403 | . 2412311 | -472 | . 6392815 | . 357942 | . 2294661 |
| . 423 | . 618 0010 | . 149550 | . 2409900 | . 473 | . 6397158 | . 362302 | . 2292367 |
| . 424 | . 6184353 | . 153702 | . 240 7491 | -474 | . 640 1501 | . 366667 | . 2290076 |
| 1.425 | 0.6188696 | 4. 157858 | 0.2405085 | I. 475 | 0.6405844 | 4.371036 | 0.2287787 |
| . 426 | . 6193039 | . 162018 | . 240268 I | . 476 | . 641 or 87 | $\begin{array}{r}\text {. } 375409 \\ \hline\end{array}$ | . 2285501 |
| . 427 | . 6197382 | . 166182 | . 2400279 | . 477 | . 6414529 | . 379787 | . 2283216 |
| . 428 | .6201725 .6206068 | . 170350 | . 2397880 | . 478 | . 6418872 | - 384169 | . 2280934 |
| . 429 | . 6206068 | . 174523 | . 2395484 | . 479 | . 6423215 | -388 555 | . 2278654 |
| 1.430 | 0.6210411 | 4.178 699 | 0.2393089 | 1.480 | 0.6427558 | 4.392946 | 0.2276377 |
| . 431 | . 6214754 | . 182880 | . 2390697 | .481 | . 643 I 901 | . 397341 | . 2274102 |
| . 432 | . 6219097 | . 187065 | . 2388308 | . 482 | . 6436244 | . 401740 | . 2271829 |
| -433 | .6223440 | . 191254 | . 2385921 | . 483 | . 6440587 | . 406144 | . 2269558 |
| -434 | . 6227783 | - 195447 | .238 3536 | . 484 | . 6444930 | . 410553 | . 2267290 |
| 1.435 | 0.6232126 | 4. 199645 | 0.2381154 | 1.485 | 0.6449273 | 4.414965 | 0.2265023 |
| . 436 | . 6236469 | . 203847 | . 2378774 | . 486 | . 6453615 | . 419383 | . 2262760 |
| -437 | . 6240812 | . 208053 | . 2376396 | . 487 | . 6457959 | . 423804 | . 2260498 |
| . 438 | . 6245155 | . 212263 | .2374021 | . 488 | . 6462302 | . 428230 | . 2258239 |
| . 439 | . 6249498 | . 216477 | . 2371648 | . 489 | . 6466645 | . 432 661 | . 225 5981 |
| 1.440 | 0.625384 I | 4.220696 | 0.2369278 | r. 490 | 0.6470988 | 4.437096 | 0.2253727 |
| . 441 | . 6258183 | . 224919 | . 2366909 | -491 | . 6475331 | .44I 535 | . 2251474 |
| . 442 | . 6262526 | . 222146 | . 2364544 | . 492 | . 6479674 | . 445979 | . 2249224 |
| . 443 | . 6266869 | . 233377 | . 2362180 | . 493 | . 6484017 | . 450427 | . 2246976 |
| . 444 | . 6271212 | . 237612 | . 2359819 | . 494 | . 6488360 | . 454879 | . 2244730 |
| 1. 445 | 0.6275555 | 4.241852 | 0.2357461 | I. 495 | 0.6492703 | 4.459337 | 0.2242486 |
| . 446 | . 6279898 | . 246096 | . 2355104 | . 496 | . 6497045 | . 463798 | . 2240245 |
| . 447 | . 6284241 | . 250344 | . 2352751 | . 497 | . 6501388 | . 468254 | . 2238006 |
| -448 | . 6288584 | . 254597 | . 2350399 | - 498 | . 6505731 | . 472735 | . 2235769 |
| . 449 | . 6292927 | . 258854 | . 2348050 | . 499 | . 6510074 | . 477 210 | . 2233534 |
| 1.450 | 0.6297270 | 4.263115 | 0.2345703 | I. 500 | 0.6514417 | 4.481 689 | 0.2231302 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-\square}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{a}}$ | $e^{-n}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 500 | 0.6514417 | 4.481 689 | 0.2231302 | 1.550 | 0.6731564 | 4.711470 | 0.2122480 |
| . 501 | . 6518760 | . 486173 | . 222 9071 | -55I | . 6735907 | . 716184 | . 2120358 |
| . 502 | . 6523103 | . 490661 | . 2226843 | . 552 | . 6740250 | . 720903 | .21I 8239 |
| . 503 | . 6527446 | . 495154 | . 222 46I8 | - 553 | .6744593 | . 725626 | .211 6i22 |
| . 504 | . 6531789 | . 499652 | . 2222394 | . 554 | . 6748936 | . 730354 | . 2114007 |
| 1. 505 | 0.653 6132 | 4.504154 | 0.2220173 | I. 555 | 0.6753279 | 4.735087 | 0.2111894 |
| . 506 | . 6540475 | . 508660 | .221 7954 | . 556 | . 6757522 | . 739824 | . 2109783 |
| . 507 | . 65448 I 8 | . 513171 | . 2215737 | . 557 | . 676 1955 | . 744566 | . 2107674 |
| . 508 | . 654 916ı | .517 686 | . 221 3522 | . 558 | .6766308 | . 749 313 | . 2105568 |
| . 509 | . 6553504 | . 522206 | . 2211310 | . 559 | . 677065 I | . 754065 | . 2103463 |
| 1.510 | 0.6557847 | 4.526731 | 0.2209100 | I. 560 | 0.6774994 | 4.75882 I | 0.2101361 |
| . 511 | . 6562190 | . 531260 | . 2206892 | . 561 | . 6779337 | . 763582 | . 209 9260 |
| . 512 | .6566533 | . 535793 | . 2204686 | . 562 | . 6783680 | . 768348 | .2097162 |
| . 513 | . 6570876 | . 54033 I | . 2202482 | . 563 | . 6788023 | . 773119 | . 2095066 |
| . 514 | .6575218 | . 544874 | . 220 0281 | . 564 | . 6792366 | . 777895 | . 2092972 |
| 1.515 | 0.6579561 | 4.549421 | 0.2198082 | 1.565 | 0.6796709 | 4.782675 | 0.2090880 |
| . 516 | . 6583904 | . 553973 | . 2195885 | . 566 | . 6801052 | . 787460 | . 2088790 |
| . 517 | . 6588247 | . 558529 | . 2193690 | . 567 | . 6805395 | . 792250 | .2086703 |
| . 518 | . 6592590 | . 563090 | .219 I497 | . 568 | . 6809737 | . 797045 | . 2084617 |
| . 519 | .6596933 | . 567655 | . 2189307 | . 569 | .681 4080 | . 801844 | .2082533 |
| 1.520 | 0.6501276 | 4.572225 | 0.2187119 | I. 570 | 0.681 8423 | 4.806648 | 0.2080452 |
| . 52 I | . 6605619 | . 576800 | . 2184933 | . 571 | .682 2766 | .81I 457 | . 2078372 |
| . 522 | . 6609962 | .581 379 | . 2182749 | . 572 | . 6827109 | .816 271 | . 2076295 |
| . 523 | . 6614305 | . 585962 | . 2180567 | . 573 | .6831452 | .821 090 | . 2074220 |
| . 524 | .66ı 8648 | . 590 55I | . 2178388 | . 574 | .6835795 | .825913 | . 2072147 |
| I. 525 | 0.6622991 | $4 \cdot 595$ I44 | 0.2176211 | 1.575 | 0.684 0I38 | 4.830742 | 0.2070076 |
| . 526 | . 6627334 | . 59974 I | .2174035 | . 576 | . 684 448I | . 835575 | . 2068006 |
| . 527 | . 6631677 | . 604343 | . 2171862 | . 577 | . 6848824 | . 8404 I 3 | . 2065940 |
| . 528 | .6636020 | . 608950 | . 2169692 | . 578 | .6853167 | . 845256 | . 2063875 |
| . 529 | .6640363 | .6I3 56ı | .2167523 | . 579 | . 685 7510 | .850103 | . 206 1812 |
| I. 530 | 0.6644706 | 4.618177 | 0.2165357 | 1.580 | 0.686 I853 | 4.854956 | 0.2059751 |
| . 531 | . 6649049 | . 622797 | .2163192 | .581 | . 686 6I96 | . 859 813 | . 2057692 |
| . 532 | . 665 3391 | .627422 | .2161030 | . 582 | .6870539 | . 864675 | . 2055636 |
| . 533 | .6657734 | .632052 | . 2158870 | . 583 | .6874882 | .869543 | . 205 3581 |
| . 534 | . 6662077 | .636687 | . 2156713 | . 584 | . 6879225 | . 874415 | . 2051528 |
| 1.535 | 0.6666420 | 4.641326 | 0.2154557 | 1. 585 | 0.6883568 | 4.879291 | 0.2049478 |
| . 536 | . 6670763 | . 645969 | . 2152403 | . 585 | . 6887910 | . 884173 | . 2047429 |
| . 537 | . 667 5106 | . 650617 | . 2150252 | . 587 | . 6892253 | . 889060 | . 2045383 |
| . 538 | . 6679449 | . 655270 | . 214 8103 | . 588 | .6896596 |  | . 2043339 |
| . 539 | . 6683792 | . 659928 | . 2145956 | . 589 | . 6900939 | . 898848 | . 2041296 |
| 1.540 | 0.668 8135 | 4.664590 | 0.2143811 | I. 590 | 0.6905282 | 4.903749 | 0.2039256 |
| . 541 | . 6692478 | . 669.257 | . 2141668 | . 591 | . 6909625 | .908 655 | . 2037218 |
| . 542 | . 6696821 | . 673929 | . 2139528 | . 592 | . 6913968 | .913 566 | . 2035182 |
| . 543 | . 6701164 | .678605 | . 2137389 | . 593 | . 6918311 | . 918482 | . 2033148 |
| . 544 | . 6705507 | .683286 | . 2135253 | . 594 | . 6922654 | .923403 | . 203 III5 |
| 1.545 | 0.6709850 | 4.687972 | 0.2133119 | I. 595 | 0.6926997 | 4.928329 | 0.2029085 |
| . 546 | . 6714193 | . 692662 | . 2130987 | . 596 | . 6931340 | .933260 | . 2027057 |
| . 547 | . 6718536 | .697357 | . 2128857 | . 597 | . 6935683 | .938 196 | . 202503 I |
| . 548 | .6722879 | . 702057 | . 2126729 | - 598 | $.6940026$ | $.943 \text { I36 }$ | $.2023007$ |
| . 549 | .6727222 | .706761 | . 2124603 | . 599 | . 6944369 | . 948082 | . 2020985 |
| I. 550 | 0.6731564 | 4.7II 470 | 0.2122480 | 1.600 | 0.6948712 | 4.953032 | 0.201 8965 |
| $\log _{e}\left(e^{\text {a }}\right.$ ) | $\log _{10}\left(e^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ |

## Smithsonian Tables

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 600 | 0.6948712 | 4.953032 | 0.201 8965 | 1.650 | 0.7165859 | 5.206980 | 0.1920499 |
| . 601 | . 6953055 | . 957988 | . 2016947 | . 651 | . 7170202 | . 212 I 89 | . 191 8580 |
| . 602 | .6957398 | . 962948 | . 2014931 | . 652 | . 7 I 74545 | . 217404 | . I91 6662 |
| . 603 | . 696174 I | . 967914 | . 2012917 | . 653 | . 7178888 | . 222624 | . I91 4746 |
| . 604 | .6966083 | . 972884 | . 2010905 | . 654 | . 718323 I | .227849 | .191 2832 |
| 1.605 | 0.6970426 | 4.977860 | 0.2008896 | 1.655 | 0.7187574 | 5.233080 | O.191 0921 |
| . 606 | . 6974769 | . 982840 | . 2006888 | . 656 | . 719 1917 | . 238316 | . 1909011 |
| . 607 | . 697 9112 | .987825 | . 2004882 | . 657 | . 7196260 | . 243557 | . 1907103 |
| . 608 | . 6983455 | . 992 816 | . 2002878 | . 658 | . 7200603 | . 248803 | . 1905196 |
| . 609 | . 6987798 | . 997 8II | . 2000876 | . 659 | .7204945 | . 254054 | . 1903292 |
| 1.610 | 0.6992141 | 5.00281 I | 0. 1998876 | I. 660 | 0.7209288 | 5.259 3II | 0.190 1390 |
| .6II | . 6996484 | . 007817 | . 1996878 | . 661 | . 7213631 | . 264573 | . 1899489 |
| .6I2 | .7000827 | . 012827 | . 1994882 | . 662 | . 7217974 | . 269840 | . 1897591 |
| .6I3 | . 7005170 | . 017842 | . 1992888 | . 663 | . 7222317 | . 275112 | . 1895694 |
| . 614 | . 7009513 | . 022863 | . 1990897 | . 664 | .7226660 | . 280390 | . 1893799 |
| 1.615 | 0.701 3856 | 5.027888 | 0. 1988907 | 1. 665 | 0.7231003 | 5.285673 | 0.1891907 |
| .6I6 | . 7018199 | . 032918 | . 1986919 | . 666 | . 7235346 | . 290962 | . 1890016 |
| .6I7 | . 7022542 | .037954 | . 1984933 | . 667 | . 7239689 | . 296255 | . 1888127 |
| . 618 | . 7026885 | . 042994 | . 1982949 | . 668 | .7244032 | . 301554 | . 1886239 |
| . 619 | .7031228 | .048040 | . 1980967 | . 669 | .7248375 | . 306858 | . 1884354 |
| 1.620 | 0.7035571 | 5.053090 | 0. 1978987 | 1.670 | 0.7252718 | 5.312 168 | 0. 188247 I |
| . 62 I | . 7039914 | . 058146 | . 1977009 | . 671 | .7257061 | . 317483 | . 1880589 |
| . 622 | . 7044256 | . 063207 | . 1975033 | . 672 | .7261404 | .322803 | . 1878709 |
| . 623 | . 7048599 | . 068272 | . 1973059 | . 673 | .7265747 | . 328 I28 | . 1876832 |
| . 624 | . 7052942 | .073343 | . 1971087 | . 674 | .7270090 | . 333459 | . 1874956 |
| I. 625 | 0.7057285 | 5.078419 | 0.1969117 | 1. 675 | 0.7274433 | 5.338795 | 0.1873082 |
| . 626 | . 7061628 | . 083500 | . 1967149 | . 676 | . 7278776 | . 344 137 | . 1871210 |
| . 627 | . 7065971 | . 088586 | . 1965182 | . 677 | . 728 3II8 | . 349483 | . I86 9339 |
| . 628 | . 7070314 | . 093677 | . 1963218 | . 678 | .7287461 | . 354836 | . 1867471 |
| . 629 | .7074657 | . 098773 | . 1961256 | . 679 | .729 1804 | . 360193 | . 1865604 |
| 1. 630 | 0.7079000 | 5.103 875 | 0. 1959296 | 1. 680 | 0.7296147 | 5.365556 | 0.1863740 |
| .63I | . 7083343 | . 10898 I | . 1957337 | .68I | . 7300490 | . 370924 | . 1861877 |
| . 632 | . 7087686 | . 114093 | . 195538 I | . 682 | . 7304833 | . 376298 | . 1860016 |
| . 633 | . 7092029 | . II9 209 | . 1953427 | .683 | . 7309176 | .381 677 | . 1858157 |
| . 634 | . 7096372 | . 124 33I | . 1951474 | . 684 | .731 3519 | . 387 06I | .185 6300 |
| 1. 635 | 0.7100715 | 5.129 458 | 0.194 9524 | 1.685 | 0.7317862 | $5 \cdot 392451$ | 0.1854444 |
| . 636 | . 7105058 | . 134590 | . 1947575 | . 686 | . 7322205 | . 397846 | . 1852591 |
| . 637 | . 7109401 | . I39 727 | . 1945629 | . 687 | .7326548 | . 403247 | . 1850739 |
| . 638 | . 7113744 | . 144869 | . 1943684 | . 688 | . 7330891 | . 408653 | . 1848889 |
| . 639 | . 7118087 | . 150 OI7 | . 194 I74I | . 689 | .7335234 | . 414064 | . 1847041 |
| 1. 640 | 0.7122430 | 5.155 170 | 0. 1939800 | 1.690 | 0.7339577 | 5.419 48I | 0.184 5195 |
| . 641 | . 7126772 | . I60 327 | . 1937852 | . 691 | . 7343920 | . 424903 | . 184335 I |
| . 642 | . 7131115 | . 165490 | . 1935925 | . 692 | . 7348263 | . 43033 I | . I84 1509 |
| . 643 | . 7135458 | . I70 658 | . 1933950 | . 693 | . 7352606 | . 435764 | . 1839668 |
| . 644 | .7139801 | . 17583 I | . 1932057 | . 694 | .7356949 | . 441202 | . 1837829 |
| 1. 645 | 0.7144144 | 5.181 010 | 0. 193 O126 | 1. 695 | 0.7361291 | 5.446646 | 0.183 5992 |
| . 646 | . 7148487 | . 186194 | . 1928196 | . 696 | . 7365634 | . 452095 | . 183 4157 |
| . 647 | . 7152830 | . 191382 | . 1926269 | . 697 | . 7369977 | . 457550 | . 183 2324 |
| . 648 | .7157173 | . 196 576 | . 1924344 | . 698 | .7374320 | . 463010 | . 183 0493 |
| . 649 | .7161516 | . 201775 | . 1922421 | . 699 | . 7378663 | . 468476 | . 1828563 |
| 1. 650 | 0.7165859 | 5.206980 | 0. 1920499 | 1.700 | 0.7383006 | 5.473947 | 0.1826835 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $u$ | $\log _{10}\left(e^{u}\right)$ | $e^{u}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.700 | 0.7383006 | 5.473947 | 0.182 6835 | I. 750 | 0.7600153 | 5.754603 | 0.173 7739 |
| . 701 | . 7387349 | . 479424 | . 1825009 | . 751 | . 7604496 | . 760360 | . 1736003 |
| . 702 | . 7391692 | .484906 | . 1823185 | . 752 | . 7608839 | . 766123 | . 1734267 |
| . 703 | .7396035 | . 490394 | . 1821363 | . 753 | .761 3I82 | . 771892 | . I73 2534 |
| . 704 | . 7400378 | . 495887 | .181 9542 | . 754 | .761 7525 | . 777667 | . 1730802 |
| 1.705 | 0.7404721 | 5.501 386 | 0.1817724 | 1.755 | 0.762 I868 | 5.783448 | 0.1729072 |
| . 706 | . 7409064 | . 506890 | . I8I 5907 | . 756 | . 7626211 | . 789234 | . 1727344 |
| . 707 | . 7413407 | . 512399 | .18I 4092 | . 757 | . 7630554 | . 795026 | . I72 5618 |
| . 708 | . 7417750 | .517915 | . I81 2279 | . 758 | .7634897 | . 800824 | . I72 3893 |
| . 709 | . 7422093 | . 523435 | . 1810467 | . 759 | .7639240 | .806628 | . 172 2170 |
| 1.710 | 0.7426436 | 5.528 96I | 0.I80 8658 | 1.760 | 0.7643583 | 5.812 437 | 0.1720449 |
| . 7 II | . 7430779 | . 534493 | . 1806850 | . 761 | . 7647926 | . 818253 | . 1718729 |
| . 712 | . 7435122 | . 540030 | . 1805044 | . 762 | .7652269 | . 824074 | . I7I 7011 |
| .713 | . 7439464 | . 545573 | . 1803240 | . 763 | .7656612 | . 829 901 | .1715295 |
| . 714 | . 7443807 | .551 122 | . 180 I438 | . 764 | .7660955 | .835734 | . I7I 358I |
| 1.715 | 0.744 8I50 | $5 \cdot 556676$ | -.179 9637 | 1.765 | 0.7665298 | 5.84 L 572 | 0.171 1868 |
| . 716 | . 7452493 | . 562235 | . 1797838 | . 766 | . 7669641 | . 847417 | . I7I OI57 |
| . 717 | . 7456836 | . 567800 | . 1796042 | . 767 | . 7673983 | . 853267 | . 1708448 |
| . 718 | . 746 II79 | . 573 371 | . 1794246 | . 768 | . 7678326 | . 859123 | .170 6740 |
| .719 | .7465522 | . 578947 | . 1792453 | .769 | .7682659 | . 864985 | . I70 5034 |
| 1.720 | 0.7469865 | $5 \cdot 584528$ | 0.179 066I | 1.770 | 0.7687012 | 5.870853 | 0.1703330 |
| . 721 | . 7474208 | . 590 I16 | . 1788872 | . 771 | . 7691355 | . 876727 | . 170 1627 |
| . 722 | . 7478855 | . 595709 | . 1787084 | . 772 | . 7695698 | .882607 | . 1699927 |
| . 723 | . 7482894 | . 601307 | . 1785298 | . 773 | .7700041 | .888492 | . 1698228 |
| . 724 | .7487237 | . 606 9II | . 1783513 | . 774 | .7704384 | .894384 | . 1696530 |
| 1.725 | 0.749 I580 | 5.612521 | 0.178 173I | 1.775 | 0.7708727 | 5.90028 I | 0.169 4834 |
| . 726 | . 7495923 | . 618 I36 | . 1779950 | . 776 | . 7713070 | . 906184 | . 1693141 |
| . 727 | . 7500266 | .623757 | . 1778 8171 | . 777 | .771 7413 | . 912094 | . 1691448 |
| . 728 | .7504609 | . 629384 | . 1776393 | . 778 | .7721756 | . 918009 | . 1689758 |
| .729 | .7508952 | . 635016 | . 1774618 | . 779 | .7726099 | . 923930 | . 1688069 |
| I. 730 | 0.7513295 | 5.640654 | 0.177 2844 | 1.780 | 0.7730442 | 5.929856 | 0. 168638 I |
| . 731 | .751 7637 | . 646297 | .1771072 | .781 | . 7734785 | . 935789 | . 1684696 |
| . 732 | . 7521980 | . 651947 | . 1769302 | . 782 | . 7739128 | .941 728 | . 1683012 |
| . 733 | .7526323 | .657601 | . 1767534 | . 783 | . 774347 I | .947673 | . 1681330 |
| . 734 | .7530666 | . 663262 | .176 5767 | . 784 | . 774 7814 | .953623 | . 1679649 |
| 1.735 | 0.7535009 | 5.668928 | 0.1764002 | 1.785 | 0.7752157 | 5.959580 | 0.1677971 |
| . 736 | . 7539352 | . 674600 | . 1762239 | . 785 | . 7756499 | . 965543 | . IU7 6293 |
| . 737 | . 7543695 | . 680277 | . 1760478 | . 787 | . 776108.42 | .971 511 | . 1674618 |
| . 738 | . 7548038 | . 685960 | . 1758718 | . 788 | .7765185 | . 977485 | $.1672944$ |
| . 739 | . 755 2381 | . 691649 | . 1756960 | . 789 | . 7769528 | .983466 | . 167 I272 |
| 1.740 | 0.7556724 | 5.697343 | 0.175 5204 | 1.790 | 0.7773871 | 5.989452 | 0.1669602 |
| . 741 | . 7561057 | . 703044 | . 1753450 | . 791 | . 7778214 | . 995445 | . 1667933 |
| . 742 | . 7565410 | . 708750 | - 1751697 | . 792 | . 7782557 | 6.001443 | . 1666266 |
| . 743 | . 7569753 | . 714461 | . I74 9946 | . 793 | . 7786900 | . 007448 | . 1664600 |
| . 744 | . 7574096 | . 720178 | . 1748197 | . 794 | . 7791243 | . 013458 | . 1662937 |
|  | 0.7578439 | 5.725901 | 0.174 6450 | 1.795 | 0.7795586 | 6.019475 | 0.1661275 |
| . 746 | . 7582782 | .731 630 | . 1744704 | . 796 | . 7799929 | . 025497 | . 1659614 |
| . 747 | . 7587125 | .737365 | . I74 2960 | . 797 | . 7804272 | .031 526 | .1657955 |
| . 748 | . 7591468 | .743105 | . 1741218 | . 798 | .780 86I5 | .037560 | $.1656298$ |
| . 749 | . 7595810 | .74885 I | . 1739478 | . 799 | .781 2958 | . 043601 | . I65 4643 |
| 1.750 | 0.7600153 | 5.754603 | 0.173 7739 | 1.800 | 0.7817301 | 6.049647 | 0.165 2989 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.800 | 0.7817301 | 6.049647 | 0. 1652989 | 1.850 | 0.8034448 | 6.359820 | 0.1572372 |
| . 801 | . 7821644 | . 055700 | . 1651337 | .851 | . 8038791 | . 365183 | $.1570800$ |
| . 802 | . 7825587 | .06I 759 | . I64 9686 | . 852 | . 804 3I34 | - 372552 | . 1569230 |
| . 803 | .7830330 | . 067824 | . 1648037 | . 853 | . 8047477 | . 378928 | $\text { . } 567662$ |
| . 804 | .7834672 | .073895 | . 1646390 | . 854 | . 8051820 | . 385310 | $\begin{array}{r} .1566095 \end{array}$ |
| 1.805 | 0.7839015 | 6.079 97I | 0.164 4745 | 1.855 | 0.8056163 | 6.391698 | 0.1564529 |
| . 806 | . 7843358 | . 086054 | . 1643101 | . 856 | . 8060506 | . 398093 | . 1562966 |
| . 807 | . 7847701 | . 092144 | . 1641458 | . 857 | . 8064849 | . 404494 | . 1561403 |
| . 808 | .7852044 | . 098239 | . 1639818 | . 858 | . 8069191 | . 410902 | $\text { . I55 } 9843$ |
| . 809 | .7856387 | . 104340 | . 163 8179 | . 859 | . 8073534 | . 417316 | $.1558284$ |
| 1.810 | 0.7860730 | 6.110 447 | 0.163 654I | 1.860 | 0.8077877 | 6.423737 | 0. I'55 6726 |
| .8II | . 7865073 | . 116561 | . 1634906 | . 861 | . 8082220 | . 430164 | . 155 5170 |
| . 812 | . 7869416 | . 12268 I | . 1633272 | . 862 | .8086563 | . 436597 | . 1553616 |
| . 813 | . 7873759 | . 128806 | . 1631639 | . 863 | . 8090906 | . 443037 | . 1552063 |
| .814 | .7878102 | . 134938 | . 1630008 | . 864 | . 8095249 | . 449.483 | . 1550512 |
| 1.815 | 0.7882445 | 6.141076 | 0.1628379 | 1.865 | 0.8099592 | 6.455936 | 0.154 8962 |
| .816 | . 7886788 | . 147220 | . 1626752 | . 866 | . 810 3935 | . 462395 | $\text { . I54 } 7414$ |
| .817 | . 789 II3I | . 153371 | . 162 5126 | . 867 | .810 8278 | . 468 86I | . 1545867 |
| . 818 | . 7895474 | . 159527 | . 1623501 | . 858 | .8II 262I | . 475333 | . 1544322 |
| . 819 | .789 98I7 | .165690 | . 1621879 | . 859 | .8II 6964 | . 48 I 8II | . 1542779 |
| 1.820 | 0.7904160 | 6.171858 | 0.1620258 | 1.870 | 0.8121307 | 6.488296 | 0.154 1237 |
| . 821 | . 7908503 | .178 033 | . 1618638 | - . 871 | . 8125650 | . 494788 | $\text { . I53 } 9696$ |
| . 822 | .791 2845 | . 1842.15 | . 161 7020 | . 872 | .8I2 9993 | . 501286 | . 1538157 |
| . 823 | . 791 7188 | . 190402 | . I6I 5404 | . 873 | . 8134336 | . 507791 | . I53 6620 |
| . 824 | .7921531 | . 196595 | . 1613789 | . 874 | .8ı3 8679 | . 514302 | . 1535084 |
| 1.825 | 0.7925874 | 6.202795 | 0.1612176 | 1.875 | 0.8143022 | 6.520 819 | O.I53 3550 |
| . 826 | . 7930217 | . 209 00I | . 1610565 | . 876 | .814 7364 | . 527343 | . 1532017 |
| . 827 | .7934560 | . 215213 | . 1608955 | . 877 | .815 1707 | . 533874 | . 1530486 |
| . 828 | .7938903 | . 221431 | . 1607347 | . 878 | .815 6050 | . 5404 II | . 1528956 |
| . 829 | . 7943246 | .227656 | . 1605741 | . 879 | .816 0393 | . 546955 | . 1527428 |
| 1.830 | 0.7947589 | 6.233887 | 0.1604136 | 1.880 | 0.8164736 | 6.553505 | 0.152 590I |
| . 831 | . 7951932 | . 240124 | . 1602532 | .88I | . 8169079 | . 560062 | . I52 4376 |
| . 832 | .7956275 | .246367 | . 160093 I | . 882 | .817 3422 | . 566625 | . 1522852 |
| . 833 | . 7960618 | .252616 | . 1599330 | . 883 | .817 7765 | . 573195 | . 1521330 |
| . 834 | .796 4961 | .258872 | . I59 7732 | . 884 | .8I8 2108 | . 579771 | . 1519810 |
| 1.835 | 0.7969304 | 6.265134 | 0.159 6I35 | 1.885 | 0.818645 I | 6.586354 | 0.1518291 |
| . 836 | . 7973647 | . 271402 | . 1594540 | . 886 | .819 0794 | . 592944 | .1516775 |
| . 837 | . 7977990 | .277677 | . I59 2946 | . 887 | .819 5I37 | . 599540 | .151 5257 |
| . 838 | . 7982333 | . 283958 | . I59 I354 | . 888 | . 8199480 | . 606143 | .151 3743 |
| . 839 | .7986676 | . 290245 | . 1589763 | . 889 | .8203823 | .6I2 753 | .151 2230 |
| I. 840 | 0.7991018 | 6.296538 | -. 1588174 | 1.890 | 0.820 8166 | 6.619369 | 0.1510718 |
| .841 | . 7995361 | . 302838 | . 1586587 | . 891 | . 8212509 | . 625991 | . 1509208 |
| . 842 | . 7599704 | . 309 I44 | . I58 500I | . 892 | . 8216852 | . 632621 | . 1507700 |
| . 843 | . 8004047 | . 315455 | . 1583417 | . 893 | .8221195 | . 639257 | . 1506193 |
| . 844 | . 8008390 | -321 775 | . 158 I834 | . 894 | .8225537 | . 645899 | . 1504687 |
| . 1.845 | 0.8012733 | 6.328100 | 0. 1580253 | I. 895 | 0.8229880 | 6.652548 | $0.1503183$ |
| $.846$ | $.8017076$ | $.33443 \mathrm{I}$ | . 1578574 | . 896 | . 8234223 | $.659204$ | $.150 \mathrm{I} 68 \mathrm{I}$ |
| . 847 | . 8021419 | - 340769 | . 1577096 | . 897 | .8238566 | . 665867 | . 1500180 |
| . 848 | .8025762 | . 347 II3 | . 1575520 | . 898 | . 8242909 | . 672536 | . I49 868I |
| . 849 | .8030105 | . 353463 | . 1573945 | . 899 | . 8247252 | . 679212 | . 1497183 |
| 1.850 | 0.8034448 | 6.359820 | 0.1572372 | 1.900 | 0.8251595 | 6.685894 | 0.149 5686 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{u}\right)$ | $\log _{10}\left(e^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}{ }^{\text {u }}\right.$ ) | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {a }}$ | $e^{-0}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right.$ ) | $\mathrm{e}^{\text {a }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.900 | 0.8251595 | 6.685894 | 0.149 5686 | 1.950 | 0.8468742 | 7.028688 | 0. 1422741 |
| .901 | . 8255938 | . 692584 | . 1494191 | .95I | . 8473085 | . 035720 | - 1421319 |
| . 902 | . 826 0281 | . 699280 | - 1492698 | . 952 | . 8477428 | . 042759 | - 1419898 |
| . 903 | . 8264624 | . 705982 | . 1491206 | . 953 | . 8481771 | . 049805 | - 141 8479 |
| . 904 | . 8268967 | . 712692 | . 1489715 | . 954 | . 848 6II4 | . 056859 | .141 7061 |
| I. 905 | 0.827 3310' | 6.719408 | 0. 1488226 | I.955 | 0.8490457 | 7.063919 | 0.14I 5645 |
| . 906 | . 8277653 | . 726130 | . 1486739 | . 956 | . 8494800 | . 070985 | - I4I 4230 |
| . 907 | . 8281996 | . 732850 | . 1485253 | . 957 | . 8499143 | . 078061 | . 1412816 |
| . 908 | . 8286339 | . 739596 | . 1483768 | . 958 | . 8503486 | . 085143 | - 1411404 |
| . 909 | . 8290682 | . 746339 | . 1482285 | . 959 | . 8507829 | . 092231 | . 1409993 |
| I.910 | 0.8295025 | 6.753089 | 0. 1480804 | I.960 | 0.8512172 | 7.099327 | 0. 1408584 |
| .91I | . 8299368 | . 759845 | . 1479324 | .961 | . 8516515 | . 106430 | - 1407176 |
| . 9 | . 8303710 | . 766 | . 1477845 | . 962 | . 8520858 | . II3 540 | - 140 5770 |
| . 913 | . 8308053 | . 773378 | . 1476368 | . 963 | . 8525201 | . 120657 | . 1404365 |
| . 914 | .831 2396 | . 780 I55 | . 1474892 | . 964 | . 8529544 | . 127 781 | . 1402961 |
| 1.915 | 0.8316739 | 6.786939 | o. 1473418 | I. 965 | 0.8533887 | 7.134 913 | 0.140 1559 |
| . 916 | . 8321082 | . 793729 | . 1471946 | . 966 | . 8538230 | . 142051 | . 140 O158 |
| . 917 | . 8325425 | . 800526 | . 1470474 | . 967 | . 8542572 | . 149197 | . 1398759 |
| .918 | . 8329768 | . 807330 | . 1469005 | . 968 | . 8546915 | . 156349 | - 1397360 |
| .919 | . 833411 I | . 814 I 4 I | . 1467536 | . 969 | . 8551258 | . 163509 | . 1395964 |
| 1.920 | 0.8338454 | 6.820958 | 0. 1466070 | 1.970 | 0.855 5601 | 7.170676 | 0.139 4569 |
| . 921 | . 8342797 | . 827783 | . 1464604 | .971 | . 8559944 | . 177851 | - 1393175 |
| . 922 | . 8347140 | . 834614 | . 1463140 | . 972 | . 8564287 | . 185032 | - 1391782 |
| . 923 | . 8351483 | . 841452 | . 1461678 | . 973 | . 8568630 | . 192221 | - 1390391 |
| . 924 | . 8355826 | . 848297 | . 1460217 | .974 | . 8572973 | -199417 | . 1389001 |
| I. 925 | 0.8360169 | 6.855149 | o. 1458758 | 1.975 | 0.8577316 | 7.206620 | 0.138 7613 |
| . 926 | . 8364512 | . 862007 | . 1457300 | . 970 | . 8581659 | . 213830 | - 1386226 |
| . 927 | . 8368855 | . 868873 | . 1455843 | . 977 | . 8586002 | . 221047 | . 1384841 |
| . 928 | . 8373198 | . 875745 | . 1454388 | . 978 | . 8590345 | . 228272 | -1383457 |
| . 929 | . 837754 I | . 882624 | . 1452934 | . 979 | . 8594688 | .235504 | . 1382074 |
| I. 930 | 0.8381884 | 6.889510 | 0. 1451482 | 1.980 | 0.8599031 | 7.242743 | 0. 1380692 |
| . 93 | . 8386226 | . 896403 | . 1450031 | .981 | . 8603374 | . 249989 | -1379312 |
| . 932 | . 8390569 | . 903303 | . 1448582 | -982 | . 8607717 | .257243 | - 1377934 |
| . 933 | . 8394912 | -910 210 | . 1447134 | .983 | . 8612060 | . 264504 | . 1376557 |
| . 934 | . 8399255 | .917 123 | . 1445688 | . 984 | .861 6403 | . 271772 | -137 5181 |
| 1.935 | 0.8403598 | 6.924044 | O. 1444243 | 1.985 | 0.8620745 | 7.279047 | 0. 1373806 |
| . 936 | . 8407941 | -930 972 | . 1442799 | .98 | . 8625088 | . 286330 | - 1372433 |
| -937 | . 8412284 | . 937905 | -144 1357 | . 987 | . 8629431 | . 293620 | . 1371061 |
| . 938 | . 8416627 | . 944847 | . 1439916 | . 988 | . 8633774 | -300 917 | - 1369691 |
| -939 | . 8420970 | .951 796 | . 1438477 | . 989 | . 863 8117 | - 308222 | - I368322 |
| 1.940 | 0.8425313 | 6.958751 | 0.1437039 | 1.990 | 0.8642460 | 7.315534 | 0.136 6954 |
| .94I | . 8429656 | .965 713 | . 1435603 | .991 | . 8646803 | - 322853 | - 1365588 |
| . 942 | . 8433999 | . 972682 | . 1434168 | -992 | . 8651146 | . 330179 | . 1364223 |
| . 943 | . 8438342 | . 979659 | . 1432735 | -993 | . 8655489 | -337513 | - 1362860 |
| . 944 | . 8442685 | . 986642 | . 1431303 | -994 | . 8659832 | -344 854 | . 1361497 |
| 1.945 | 0.8447028 | 6.993632 | 0. 1429872 | 1. 995 | 0.8664175 | 7.352203 | 0.136 0137 |
| . 946 | . 8451371 | 7.000629 | . 1428443 | . 996 | . 8668518 | . 359559 | . 1358777 |
| . 947 | . 8455714 | . 007633 | . 1427015 | . 997 | . 8672861 | . 366922 | -1357419 |
| . 948 | . 8460057 | . 014644 | . 1425589 | -998 | . 8677204 | -374 293 | . 1356062 |
| . 949 | . 8464399 | .021 662 | . 1424164 | -999 | . 8681547 | .381 671 | -1354707 |
| I. 950 | 0.8468742 | 7.028688 | 0.1422741 | 2.000 | 0.8685890 | 7.389056 | 0.135 3353 |
| $\log _{\text {e }}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ |  | $\log _{\text {e }}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-0}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.000 | 0.8685890 | 7.389056 | 0.135 3353 | 2.050 | 0.8903037 | 7.767 901 | 0.1287349 |
| .00I | . 8690233 | - 396449 | . I35 2000 | .051 | . 8907380 | . 775673 | . 1286062 |
| . 002 | .8694576 | . 403849 | . I35 0649 | . 052 | . 8911723 | . 783452 | . 1284777 |
| . 003 | .8698918 | .411 257 | . I34 9299 | . 053 | . 8916066 | . 791240 | . 1283493 |
| . 004 | .8703261 | . 418672 | . I34 7950 | . 054 | .8920 .409 | . 799035 | . 1282210 |
| 2.005 | 0.8707604 | 7.426094 | 0.1346603 | 2.055 | 0.8924752 | 7.806838 | 0.1280928 |
| . 006 | .871 1947 | . 433524 | . I34 5257 | . 056 | . 8929095 | .814 649 | . 1279648 |
| . 007 | . 8716290 | . 440961 | . I34 3912 | . 057 | . 8933437 | . 822467 | . 1278369 |
| . 0008 | . 8720633 | . 448406 | . I34 2569 | . 058 | .8937780 | . 830294 | .1277091 |
| . 009 | .8724976 | . 455858 | . 1341227 | . 059 | . 894 2123 | . 838 128 | . 127 5815 |
| 2.010 | 0.8729319 | 7.463317 | -. 1339887 | 2.060 | 0.8946466 | 7.845970 | 0.1274540 |
| .OII | . 8733662 | . 470784 | . 1338548 | .06I | . 8950809 | . 853820 | . 1273266 |
| .OI2 | .8738005 | . 478259 | . 1337210 | . 062 | . 895 5152 | .86I 677 | .1271993 |
| . OI3 | . 8742348 | . 485741 | . I33 5873 | . 063 | .8959495 | . 869543 | . 1270722 |
| . 014 | . 8746691 | . 493230 | . I33 4538 | . 064 | .8963838 | . 877417 | . 1269452 |
| 2.015 | 0.8751034 | 7.500727 | O. 1333204 | 2.065 | 0.896 8ı8I | 7.885298 | 0.126 8183 |
| . 016 | . 8755377 | . 508232 | . 1331871 | . 066 | . 8972524 | . 893187 | . 1266915 |
| . 017 | .8759720 | . 515744 | . 1330540 | . 067 | .8976867 | .901 084 | .1265649 |
| . 018 | .8764063 | . 523263 | . 1329210 | . 068 | . 898 I210 | . 908989 | . 1264384 |
| . 019 | .8768406 | . 530790 | . I32 7882 | . 069 | . .8985553 | . 916902 | . 1263120 |
| 2.020 | 0.8772749 | 7.538325 | 0.132 6555 | 2.070 | 0.8989896 | 7.924823 | 0.126 1858 |
| . 021 | . 877 7091 | . 545867 | . 1325229 | . 071 | . 8994239 | . 932752 | . 1260597 |
| . 022 | . 8781434 | . 553417 | . 1323904 | . 072 | . 8998582 | . 940689 | . 1259337 |
| . 023 | . 8785777 | . 560974 | . 132258 I | . . 073 | . 9002925 | . 948633 | . 1258078 |
| . 024 | . 879 OI20 | . 568539 | . I32 I259 | . 074 | . 9007268 | . 956586 | .1256820 |
| 2.025 | 0.8794463 | 7.576 III | O.I3I 9938 | 2.075 | 0.9011610 | 7.964546 | 0.125 5564 |
| . 026 | . 8798806 | . 583691 | . I3I 8619 | . 076 | .901 5953 | . 972 515 | . 1254309 |
| . 027 | . 8803149 | . 591278 | . 131 7301 | . 077 | .9020296 | . 980491 | . 1253056 |
| . 028 | . 8807492 | .598873 | . I3I 5985 | . 078 | .9024639 | . 988476 | . 1251803 |
| . 029 | .88I 1835 | . 606476 | . I3I 4669 | . 079 | . 9028982 | . 996468 | .1250552 |
| 2.030 | 0.88 I 6ı78 | 7.614086 | O.I3I 3355 | 2.080 | 0.9033325 | 8.004469 | 0.124 9302 |
| .03I | . 8820521 | .621 704 | . I31 2043 | .08I | . 9037668 | . 012477 | . 1248053 |
| . 032 | .8824864 | .629330 | . I3I 073I | . 082 | . 9042011 | . 020494 | . 1246806 |
| . 033 | .8829207 | .636963 | . 130942 I | . 083 | . 9046354 | . 028518 | . 1245560 |
| . 034 | .8833550 | .644604 | - I30 8iI2 | . 084 | .9050697 | . 03655 I | . 124 43I5 |
| 2.035 | 0.8837893 | 7.652252 | 0.130 6805 | 2.085 | 0.9055040 | 8.044591 | 0.1243071 |
| . 036 | . 8842236 | . 659908 | . I30 5499 | . 086 | . 9059383 | . 052640 | . 1241829 |
| . 037 | .8846579 | . 667572 | . I30 4194 | . 087 | . 9063726 | . 050697 | . 1240588 |
| . 038 | .8850922 | .675243 | . I30 2890 | . 088 | . 9068069 | . 068761 | . I239348 |
| . 039 | . 8855264 | .682922 | . 1301588 | . 089 | . 9072412 | . 076834 | . 123 8109 |
| 2.040 | 0.8859607 | 7.690609 | 0.130 0287 | 2.090 | 0.9076755 | 8.084915 | 0.1236871 |
| . 041 | .8863950 | . 698304 | . 1298987 | . 091 | . 9081098 | . 093004 | .1235635 |
| . 042 | . 8868293 | . 706006 | . 1297689 | . 092 | . 908 544I | . IOI IOI | . 1234400 |
| . 043 | .8872636 | .713716 | . 1296392 | . 093 | .9089784 | . 109206 | .1233166 |
| . 044 | . 8876979 | .721 433 | . 1295096 | . 094 | .9094126 | . 117320 | . 1231934 |
| 2.045 | 0.8881322 | 7.729159 | 0.1293802 | 2.095 | 0.9098469 | 8.12544 I | 0.1230702 |
| . 046 | . 8885665 | . 736892 | . 1292509 | . 096 | .910 2812 | . 133570 | . 1229472 |
| . 047 | . 8890008 | . 744632 | . I29 1217 | . 097 | .910 7155 | . 141708 | . 1228243 |
| . 048 | . 8894351 | .752 38I | . I28 9926 | . 098 | .91I 1498 | . 149854 | . 1227016 |
| . 049 | . 8898694 | . 760137 | . 1288637 | . 099 | .911 5841 | . 158008 | . 1225789 |
| 2.050 | 0.8903037 | 7.767901 | 0.1287349 | 2.100 | 0.9120184 | 8.166 I70 | 0.1224564 |
| $\log _{e}\left({ }^{\text {( }}\right.$ ) $)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}{ }^{\mathrm{u}}\right)$ | $\log _{10}\left({ }^{\text {u }}\right.$ ) | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ | u | $\log _{10}\left(e^{u}\right)$ | $e^{\text {n }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.100 | 0.912 OI84 | 8.166 170 | 0. 1224564 | 2.150 | 0.933 733I | 8.584858 | 0.116 4842 |
| . IOI | . 9124527 | . 174340 | . 1223340 | . 151 | . 9341674 | . 593448 | . II6 3677 |
| . 102 | . 9128870 | . 182519 | . 122 2118 | . 152 | . 9346017 | . 602045 | . 1162514 |
| . 103 | . 9133213 | . 190705 | . I22 0896 | . 153 | . 9350360 | . 610652 | . II6 I352 |
| . 104 | -913 7556 | . 198900 | . 1219676 | . 154 | .9354703 | . 619267 | . II6 OI92 |
| 2.105 | 0.9141899 | 8.207103 | O.I2I 8457 | 2.155 | 0.9359046 | 8.627890 | O.II5 9032 |
| . 106 | .914 6242 | .2I5 3I4 | . I2I 7239 | . 156 | . 9363389 | . 636522 | . II5 7873 |
| . 107 | .915 0585 | . 223534 | . I2I 6022 | . 157 | . 9367732 | .645 I63 | . II5 6716 |
| . 108 | . 9154928 | . 231 76I | . I2I 4807 | . 158 | . 9372075 | . 653 813 | . II5 5560 |
| . 109 | . 915927 I | . 239997 | . I2I 3593 | . 159 | . 93764 I 8 | . 662 47I | . II5 4405 |
| 2.110 | 0.9163614 | 8.24824 I | 0.121 2380 | 2. 160 | 0.938 0761 | 8.671 I 38 | O.II5 325I |
| . II | . 9167957 | .256494 | . 1211168 | . 16I | .9385104 | . 679 813 | . II5 2099 |
| . II2 | . 9172299 | . 264754 | . 1209957 | . 162 | . 9389447 | . 688497 | . II5 0947 |
| . II3 | .917 6642 | .273023 | . 1208748 | . 163 | . 9393790 | . 697190 | . II4 9797 |
| . II4 | . 9180985 | .28I 300 | . 1207540 | . 164 | . 939 8I33 | . 705892 | . I I4 8647 |
| 2.115 | 0.9185328 | 8.289586 | 0.1206333 | 2.165 | 0.9402476 | 8.714602 | 0.1147499 |
| . 116 | . 9189671 | . 297879 | . 1205127 | . 166 | . 9406818 | . 72332 I | . II4 6352 |
| . 117 | . 9194014 | . 306182 | . 1203923 | . 167 | .94I II6I | .732049 | . II4 5207 |
| . II8 | . 9198357 | .314 492 | . 1202719 | . 168 | .941 5504 | . 740785 | . II4 4062 |
| . 119 | . 9202700 | . 322 8II | . 1201517 | . 169 | .94I 9847 | . 749530 | . II4 2919 |
| 2.120 | 0.9207043 | 8.331 137 | 0.1200316 | 2. 170 | 0.9424190 | 8.758284 | 0.114 1776 |
| . 121 | .921 I386 | . 339473 | . II9 9117 | . 171 | . 9428533 | . 767047 | . 11400635 |
| . 122 | .921 5729 | -347 816 | . I19 7918 | . 172 | . 9432876 | . 775 818 | . II3 9495 |
| . 123 | . 9220072 | . 356168 | . II9 672I | . 173 | . 9437219 | . 784598 | . II3 8356 |
| . 124 | . 9224415 | . 364529 | . II9 5525 | . 174 | . 944 I562 | . 793387 | . I13 7218 |
| 2.125 | 0.9228758 | 8.372897 | O.II9 4330 | 2.175 | 0.9445905 | 8.802185 | 0.II3 6082 |
| . 126 | . 923 3101 | .381 275 | - II9 3136 | . 176 | . 9450248 | . 810992 | . II3 4946 |
| . 127 | .923. 7444 | . 389660 | . II9 1943 | . 177 | . 9454591 | .819807 | . II3 38I2 |
| . 128 | . 9241787 | . 398054 | . II9 0752 | . 178 | . 9458934 | . 828631 | . II3 2678 |
| . 129 | . 924 6I30 | . 406456 | . 1189562 | . 179 | . 9463277 | .837464 | . II3 1546 |
| 2. I30 | 0.9250472 | 8.414867 | 0.1188373 | 2.180 | 0.9467620 | 8.846306 | O.II3 04I5 |
| .13I | . 925 4815 | . 423286 | . 1187185 | . 181 | . 947 1963 | . 855 I 57 | . 1129285 |
| . 132 | . 925 9158 | . 431713 | . II8 5999 | . 182 | . 9476306 | . 864 O17 | . 1128157 |
| . 133 | . 9263501 | . 440149 | . II8 48I3 | . 183 | . 9480649 | . 872885 | . II2 7029 |
| . I34 | . 9267844 | . 448594 | . II8 3629 | . 184 | . 948 499I | . 881762 | . I 125903 |
| 2. 135 | 0.9272187 | 8.457047 | 0.118 2446 | 2.185 | 0.9489334 | 8.890649 |  |
| . I36 | . 9276530 | .465508 | . II8 1264 | . 186 | . 9493677 | . 899544 | . I12 3653 |
| . 137 | . 9280873 | .473978 | . II8 0083 | . 187 | . 9498020 | . 908448 | . II2 2530 |
| . 138 | . 9285216 | . 482456 | . II7 8904 | . 188 | . 9502363 | .917361 | . II2 I408 |
| . 139 | . 9289559 | . 490942 | . 1177726 | . 189 | . 9506706 | . 926282 | . I 120287 |
| 2. 140 | 0.9293902 | 8.499438 | 0.II7 6548 | 2. 190 | 0.9511049 | 8.935213 | 0.1119167 |
| . 141 | . 9298245 | . 50794 I | . II7 5372 | . 19I | .951 5392 | . 944 I53 | . III 8049 |
| . 142 | . 9302588 | . 516454 | .117 4198 | . 192 | .951 9735 | . 953 IOI | . III 693 I |
| . 143 | . 9306931 | . 524974 | . II7 3024 | - 193 | . 9524078 | . 962059 | . III 58I5 |
| . 144 | .93I I274 | . 533503 | . 1171852 | . 194 | . 952842 I | .971 026 | . III 4700 |
| 2.145 | 0.9315617 |  | $0.1170680$ | 2. 195 | 0.9532764 | 8.980001 | O.III 3586 |
| . 146 | .931 9960 | -550 588 | . 1169510 | . 196 | .9537107 | . 988986 | . III 2473 |
| . 147 | . 9324303 | . 559 I42 | . 1168341 | . 197 | . 9541450 | . 997979 | . III 1361 |
| . 148 | . 9328645 | $\begin{aligned} & .567706 \\ & .576278 \end{aligned}$ | . 1167174 | . 198 | .9545793 | 9.006982 | . III 0250 |
| . 149 | . 9332988 | - 570278 | . 1166007 | . 199 | . 955 OI36 | . 015993 | - IIO 9140 |
| 2.150 | 0.933733 I | 8.584858 | 0.II6 4842 | 2.200 | 0.9554479 | 9.025 OI3 | O.IIO 8032 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{\text {a }}$ | $e^{-}$ | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{\text {u }}$ | $e^{-u}$ |


| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.200 | 0.9554479 | 9.025 O13 | 0.110 8032 | 2.250 | 0.9771626 | 9.487736 | O.IO5 3992 |
| . 201 | . 9558822 | . 034043 | . IIO 6924 | .25I | . 9775969 | . 497228 | . IO5 2939 |
| . 202 | . 9563164 | . 043082 | . IIO 58i8 | . 252 | . 9780312 | . 506730 | . 1051886 |
| . 203 | . 9567507 | .052129 | . IIO 4712 | . 253 | . 9784655 | . 516242 | . 1050835 |
| . 204 | . 957 I850 | .061 186 | . IIO 3608 | . 254 | . 9788998 | . 525763 | . 1049785 |
| 2.205 | 0.9576193 | 9.070252 | 0.1102505 | 2.255 | 0.9793341 | 9.535293 | 0.104 8735 |
| . 206 | . 9580536 | . 079326 | . 1101403 | . 256 | . 9797684 | . 544833 | . 1047687 |
| . 207 | . 9584879 | . 088410 | . 1100302 | . 257 | . 9802026 | . 554383 | . 1046640 |
| . 208 | . 9589222 | .097503 | . 1099203 | . 258 | . 9806369 | . 563942 | . 1045594 |
| . 209 | . 9593565 | . 106605 | . 1098104 | . 259 | .98I 0712 | -573 5II | . 1044549 |
| 2.210 | 0.9597908 | 9.115716 | 0.1097006 | 2.260 | 0.9815055 | 9.583089 | 0.104 3505 |
| . 211 | . 9602251 | . 124837 | . 1095910 | .26I | . 981 9398 | . 592677 | . IO4 2462 |
| . 212 | . 9606594 | . I33966 | . 109 48i5 | . 262 | . 982374 I | . 602275 | . 1041420 |
| . 213 | .96i 0937 | . I43 105 | . 1093720 | . 263 | . 9828084 | .6ıI 882 | . 1040379 |
| . 214 | .96I 5280 | . I52 252 | . 1092627 | . 264 | . 9832427 | . 621498 | . 1039339 |
| 2.215 | 0.9619623 | 9.161 409 | 0.109 1535 | 2.265 | 0.9836770 | 9.63 I 125 | 0.103 8300 |
| . 216 | . 9623966 | . 170575 | . IO9 0444 | . 266 | . 984 III3 | . 640761 | . 1037263 |
| . 217 | . 9628309 | . I79 750 | - I08 9354 | . 267 | . 9845456 | . 650406 | . 1036226 |
| . 218 | . 9632652 | . 188935 | . 1088265 | . 268 | . 9849799 | . 660061 | . 1035190 |
| . 219 | . 9636995 | . 198128 | . 1087178 | . 269 | .9854142 | . 669726 | . 1034155 |
| 2.220 | 0.9641337 | 9.207331 | 0.1086091 | 2.270 | 0.g85 8485 | 9.679401 | 0.103 3122 |
| . 22I | . 9645680 | . 216543 | . 1085006 | . 271 | . 9852828 | . 689085 | . 1032089 |
| . 222 | . 9650023 | . 225764 | . 1083921 | . 272 | . 986 7171 | . 698779 | . 1031058 |
| .223 | .9654366 | . 234994 | . 1082838 | .273 | .9871514 | . 708483 | . 1030027 |
| . 224 | .9658709 | . 244234 | . 1081755 | . 274 | .9875857 | .718 196 | . IO2 8998 |
| 2.225 | 0.9663052 | 9.253483 | 0.1080674 | 2.275 | 0.988 0199 | 9.727919 | 0.102 7969 |
| . 226 | . 9657395 | . 262741 | . 1079594 | . 276 | . 9884542 | . 737652 | . 1026942 |
| . 227 | . 9671738 | .272008 | . 1078515 | . 277 | . 9888885 | . 747394 | . 1025915 |
| . 228 | .967 608I | .28I 285 | . 1077437 | . 278 | .9893228 | . 757147 | . 1024890 |
| . 229 | . 9680424 | . 29057 I | .1076360 | . 279 | . 9897571 | . 766909 | . 1023865 |
| 2.230 | 0.9684767 | 9.299866 | 0.107 5284 | 2.280 | 0.990 I914 | 9.776680 | 0.102 2842 |
| .23I | . 968 9110 | . 309 171 | . 1074210 | .28I | . 9906257 | . 786462 | . 1021820 |
| . 232 | . 9693453 | -318 484 | . 1073136 | .282 | .991 0600 | . 796253 | . 1020798 |
| . 233 | . 9697796 | . 327808 | . 1072063 | . 283 | .991 4943 | . 806054 | . IOI 9778 |
| . 234 | . 970 2139 | . 337140 | . 1070992 | . 284 | .991 9286 | .815 865 | . IOI 8759 |
| 2.235 | 0.9706482 | 9.346482 | 0.106 992I | 2.285 | 0.9923629 | 9.825686 | O.IOI 7741 |
| . 236 | . 9710825 | . 355833 | . 1068852 | . 286 | . 9927972 | . 835517 | . IOI 6723 |
| . 237 | .971 5168 | . 365194 | . 1067784 | .287 | .9932315 | . 845357 | . IOI 5707 |
| . 238 | .971 9511 | . 374563 | . 1066716 | . 288 | . 9936658 | .855208 | . IOI 4692 |
| . 239 | . 9723853 | . 383943 | . 1065650 | . 289 | . 994 IOOI | . 865068 | . IOI 3678 |
| 2.240 | 0.972 8ig6 | 9.393 331 | 0.106 4585 | 2.290 | 0.9945344 | 9.874938 | O.IOI 2665 |
| . 241 | . 9732539 | . 402729 | . 1063521 | . 291 | . 9949687 | . 884818 | . IOI 1652 |
| . 242 | . 9736882 | . 412137 | . 1062458 | . 292 | . 9954030 | .894707 | . IOI 064I |
| . 243 | . 9741225 | . 421554 | . 1061396 | . 293 | . 9958372 | .904607 | . 1009631 |
| . 244 | . 9745568 | . 430980 | . 1060335 | . 294 | . 9962715 | . 914 517 | . 1008622 |
| 2.245 | 0.974 99II | 9.440416 | 0.105 9275 | 2.295 | 0.9967058 | 9.924436 | 0.100 7614 |
| . 246 | . 9754254 | . 449861 | . 1058217 | . 296 | . 997 I401 | . 934365 | . 1006607 |
| . 247 | . 9758597 | . 459315 | $.1057159$ | -. 297 | . 9975744 | -944 305 | $\text { . } 10005601$ |
| . 248 | . 9762940 | . 468779 | . 1056102 | . 298 | . 9980087 | . 954254 | . IOO 4596 |
| . 249 | . 9767283 | . 478253 | . 1055047 | . 299 | . 9984430 | . 964213 | . 1003592 |
| 2.250 | 0.9771626 | 9.487736 | 0.1053992 | $2 \cdot 300$ | 0.9988773 | 9.974 I82 | 0.100 2588 |
| $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $\mathrm{e}^{-}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |


| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.300 | 0.9988773 | 9.974 I82 | 0.100 2588 | 2.350 | 1.0205920 | 10.485570 | 0.0953692 |
| . 301 | . 999 3116 | .984162 | . 1001586 | .351 | .021 0263 | . 496061 | . 0952738 |
| . 302 | . 9997459 | . 994 I5I | . 1000585 | - 352 | .021 4606 | . 506562 | . 0951786 |
| . 303 | 1.000 1802 | 10.004 I 50 | . . 0999585 | - 353 | .02I 8949 | . 517074 | . 0950835 |
| - 304 | . 0006145 | . 014159 | . 0998586 | . 354 | .0223292 | . 527596 | . 0949884 |
| 2.305 | I.001 0488 | 10.024178 | 0.0997588 | 2.355 | 1.0227635 | 10.538129 | 0.0948935 |
| . 306 | . 0014831 | .034207 | . 0996591 | . 356 | . 0231978 | . 548672 | . 0947987 |
| . 307 | .001 9174 | . 044247 | . 0995595 | . 357 | .0236321 | . 559226 | . 0947039 |
| . 308 | .0023517 | .054296 | . 0994600 | . 358 | . 0240564 | . 569791 | . 0946093 |
| . 309 | . 0027860 | . 064355 | . 0993606 | . 359 | .0245007 | . 580366 | . 0945147 |
| 2.310 | 1.0032203 | 10.074425 | 0.0992613 | 2.360 | 1. 0249350 | 10.590951 | 0.0944202 |
| . 311 | .003 6545 | . 084504 | . 0991620 | .36I | .0253693 | . 601548 | . 0943259 |
| . 312 | . 0040888 | .094594 | . 0990629 | . 362 | . 0258036 | . 612155 | . 0942316 |
| .3I3 | . 004523 I | . 104693 | . 0989639 | . 363 | . 0262379 | . 622772 | . 0941374 |
| . 314 | . 0049574 | . II4 803 | . 0988650 | - 364 | . 0266722 | . 633400 | . 0940433 |
| 2.315 | 1.0053917 | 10.124 923 | 0.0987662 | 2.365 | 1.0271064 | 10.644039 | 0.0939493 |
| .316 | . 0058260 | . I35 053 | . 0986675 | . 356 | .0275407 | . 654688 | . 0938554 |
| .317 | . 0062603 | . 145193 | . 0985688 | . 367 | .0279750 | . 665348 | . 0937616 |
| . 318 | .006 6946 | . 155343 | . 0984703 | . 368 | . 0284093 | . 676 O19 | .0936679 |
| . 319 | . 0071289 | . 165504 | . 0983719 | . 369 | .0288436 | . 686700 | . 0935743 |
| $2 \cdot 320$ | 1.0075632 | 10.175 674 | 0.0982736 | 2.370 | 1.0292779 | 10.697392 | 0.0934807 |
| . 321 | . 0079975 | . 185855 | . 0981754 | . 371 | . 0297122 | . 708095 | . 0933873 |
| . 322 | . 0084318 | . 196046 | . 0980772 | . 372 | . 0301465 | . 718808 | . 0932940 |
| . 323 | . 0088861 | . 206247 | . 0979792 | . 373 | . 0305808 | . 729533 | . 0932007 |
| . 324 | . 0093004 | . 216459 | . 097 88I3 | . 374 | .03I OI5I | . 740268 | . 0931076 |
| 2.325 | 1. 0097347 | 10.226680 | 0.0977834 | 2.375 | I.03I 4494 | 10.75I OI3 | 0.0930145 |
| . 326 | . 010 I690 | . 236912 | . 0976857 | . 376 | .031 8837 | .761 770 | . 0929215 |
| . 327. | . 0106033 | . 247 I54 | . 097 588I | . 377 | .0323180 | . 772537 | . 0928286 |
| . 328 | .OII 0376 | . 257406 | . 0974905 | -378 | .0327523 | . 783315 | . 0927359 |
| . 329 | .OII 4718 | .267669 | . 097393 I | . 379 | . 0331866 | . 794103 | . 0926432 |
| 2.330 | I.OII 906I | 10.277942 | 0.0972957 | 2.380 | 1. 0336209 | 10.804903 | 0.0925506 |
| . 33 I | . 0123404 | . 288225 | . 0971985 | . 38 I | . 0340552 | .815 713 | . 092458 I |
| . 332 | . 0127747 | . 2985 I8 | . 097 IOI4 | . 382 | . 0344895 | . 826534 | . 0923657 |
| - 333 | . 0132090 | . 308822 | . 0970043 | . 383 | .0349238 | .837366 | . 0922733 |
| . 334 | .OI3 6433 | . 319 I36 | . 0969073 | . 384 | .0353580 | .848209 | . 092 I8II |
| 2.335 | 1.0140776 | 10.329 460 | 0.0968105 | 2.385 | I. 0357923 | 10.859063 | 0.0920890 |
| . 336 | . 014 5119 | . 339795 | . 0967137 | . 386 | . 0362266 | . 869927 | .091 9959 |
| . 337 | . 0149462 | . 350 I40 | . 0966171 | . 387 | .0366609 | . 880803 | .091 9050 |
| . 338 | . OI5 3805 | . 360495 | . 0965205 | . 388 | .0370952 | . 991689 | .091 8i3I |
| . 339 | . OI 58148 | . 37086 I | . 0964240 | . 389 | . 0375295 | . 902585 | .091 7214 |
| 2.340 | 1.016 2491 | 10.381 237 | 0.0963276 | 2.390 | I. 0379638 | 10.913494 | c.091 6297 |
| .34I | . 0166834 | .391 623 | . 0962314 | . 391 | . 0383981 | . 924 4I3 | .091 538I |
| . 342 | . 0171177 | . 402020 | . 0961352 | . 392 | . 0388324 | . 935343 | .091 4466 |
| - 343 | . O17 5520 | . 412427 | . 0960391 | - 393 | .0392667 | . 946284 | .091 3552 |
| - 344 | . 0179863 | . 422845 | . 095 943I | - 394 | .0397010 | . 957235 | .091 2639 |
| 2.345 | I. 0184206 | 10.433273 | 0.0958472 | 2.395 | 1. 0401353 | 10.968198 |  |
| . 346 | . 0188549 | . 443711 | . 0957514 | . 396 | . 0405696 | . 979 I72 | . 091 08I6 |
| - 347 | . O19 2891 | .454160 | . 0956557 | . 397 | .041 0039 | . 990 I56 | . 0909905 |
| - 348 | . 0197234 | . 464620 | . 0955601 | . 398 | .041 4382 | II.OOI 152 | . 0908996 |
| - 349 | . 0201577 | . 475089 | . 0954646 | . 399 | .041 8725 | . OI 2159 | . 0908087 |
| 2.350 | 1.0205920 | 10.485570 | 0.0953692 | 2.400 | 1.0423068 | 11.023176 | 0.0907180 |
| $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\mathrm{gog}_{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{a}}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {a }}$ | $\mathrm{e}^{-4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.400 | I. 0423068 | 11.023176 | 0.0907180 | 2.450 | 1. 0640215 | II. 588347 | 0.0862936 |
| . 401 | . 0427411 | . 034205 | . 0906273 | .45I | . 0644558 | . 59994 I | . 0862073 |
| . 402 | . 0431753 | . 045245 | . 0905367 | . 452 | . 0648901 | .6II 547 | . 0861212 |
| . 403 | . 0436096 | . 056296 | . 0904462 | -453 | . 0653244 | . 623164 | . 0860351 |
| . 404 | . 0440439 | . 067357 | . 0903558 | -454 | . 0657587 | . 634793 | . 085 9491 |
| 2.405 | 1. 0444782 | 11.078430 | 0.0902655 | 2.455 | 1. 0661930 | II. 646434 | 0.0858632 |
| . 406 | . 0449125 | . 089514 | . 0901753 | . 456 | . 0666272 | . 658086 | . 0857774 |
| . 407 | . 0453468 | . 100609 | . 090085 I | -457 | . 0670615 | . 669750 | . 0856916 |
| . 408 | . 045 7811 | . 111715 | . 0899951 | . 458 | . 0674958 | .681 425 | . 0856060 |
| . 409 | . 0462154 | . 122833 | . 0899052 | -459 | . 067 9301 | . 693 II3 | . 0855204 |
| 2.410 | I. 0466497 | II. 133961 | 0.089 8153 | 2.460 | 1. 0683644 | 11.704812 | 0.0854350 |
| . 411 | . 0470840 | . I45 IOI | . 0897255 | . 461 | . 0687987 | . 716522 | . 0853496 |
| . 41 | . 0475183 | . 156251 | . 0896358 | . 462 | . 0692330 | . 728245 | . 0852643 |
| .413 | . 0479526 | . 167413 | . 0895463 | . 463 | . 0696673 | . 739979 | . 0851790 |
| . 414 | . 0483869 | . 178586 | . 0894568 | -464 | . 070 1016 | .751 725 | . 0850939 |
| 2.415 | 1.048 8212 | II. 189770 | 0.0893673 | 2.465 | 1.0705359 | 11.763482 | 0.0850088 |
| . 416 | . 0492555 | . 200966 | . 0892780 | . 466 | . 0709702 | . 775252 | . 0849239 |
| . 417 | . 0496898 | . 212172 | . 0891888 | . 467 | . 0714045 | . 787033 | . 0848390 |
| . 418 | . 0501241 | . 223390 | . 0890996 | . 468 | . 0718388 | . 798826 | . 0847542 |
| -419 | . 0505584 | . 234619 | . 0890106 | . 469 | . 0722731 | .810 630 | . 0846695 |
| 2.420 | 1. 0509926 | 11.245859 | 0.0889216 | 2.470 | 1.072 7074 | 11.822447 | 0.0845849 |
| . 421 | . 0514269 | . 257 III | . 0888327 | . 471 | . 0731417 | . 834275 | . 0845003 |
| . 422 | . 0518512 | . 268374 | . 0887440 | -472 | . 0735760 | . 846115 | . 0844159 |
| . 423 | . 0522955 | . 279648 | . 0886553 | -473 | . 074 O103 | . 857967 | . 0843315 |
| . 424 | . 0527298 | . 290933 | . 0885666 | -474 | . 0744445 | . 869831 | . 0842472 |
| 2.425 | 1.0531641 | 11.302229 | 0.088 4781 | 2.475 | 1. 0748788 | 11.881707 | 0.0841630 |
| . 426 | . 0535984 | -3I3 537 | . 0883897 | -476 | . 075 3131 | . 893595 | . 0840789 |
| . 427 | . 0540327 | - 324857 | . 0883013 | . 477 | . 0757474 | .905 494 | . 0839948 |
| . 428 | . 0544670 | . 336187 | . 0882131 | -478 | . 0761817 | . 917406 | . 0839109 |
| . 429 | . 054 9013 | -347 529 | . 0881249 | -479 | . 0766160 | . 929329 | . 0838270 |
| 2.430 | I. 0553356 | 11.358882 | 0.0880368 | 2.480 | I. 0770503 | 11.941264 | 0.0837432 |
| .431 | . 0557699 | -370 247 | . 0879488 | . 481 | . 0774846 | . 953212 | . 0836595 |
| -432 | . 0562042 | -381 623 | . 0878609 | -482 | . 0779189 | .965 171 | . 8335759 |
| -433 | . 0566385 | -393 010 | . 0877731 | . 483 | . 0783532 | . 977142 | . 0834924 |
| -434 | . 0570728 | . 404409 | .087 6854 | -484 | . 0787875 | . 989125 | . 0834089 |
| 2.435 | 1.0575071 | 11.415819 | 0.0875977 | 2.485 | 1.0792218 | 12.001120 | 0.0833256 |
| . 436 | . 0579414 | . 427240 | . 0875102 | -486 | . 0796561 | .013 127 | . 0832423 |
| -437 | . 0583757 | . 438673 | . 0874227 | . 487 | . 0800904 | . 025147 | . 0831591 |
| -438 | . 0588099 | -450 118 | .087 3353 | . 488 | . 0805247 | . 037178 | . 0830760 |
| . 439 | . 0592442 | . 461573 | . 087 2481 | . 489 | . 0809590 | . 04922 I | . 0829929 |
| 2.440 | 1. 0596785 | 11.473041 | 0.0871609 | 2.490 | 1.081 3933 | 12.061276 | 0.0829100 |
| . 441 | . 0601128 | . 484520 | .087 0737 | .491 | .081 8276 | . 073343 | . 0828271 |
| -412 | . 060 5471 | -496 10 | . 0869867 | -492 | . 0822618 | . 085423 | . 0827443 |
| . 443 | . 0609814 | . 507512 | . 0868998 | . 493 | . 0826961 | . 097514 | . 0826616 |
| -444 | . 0614157 | .519 025 | . 086 8129 | . 494 | . 0831304 | . 109618 | . 0825790 |
| 2.445 | 1. 0618500 | 11.530550 | 0.0867261 | 2.495 | 1.083 5647 | 12.121 734 |  |
| . 4446 | .0622843 .0627186 | . 542086 | .0866395 .086529 | . 496 | .0839990 .0844333 | . 133861 | .0824140 .0823316 |
| . 4448 | $\begin{array}{r}.0627186 \\ .0631529 \\ \hline 063\end{array}$ | . 553634 | . 08655429 | . 497 | .0844333 .0848676 | .146 001 | .0823316 .0822493 |
| -449 | . 0635872 | . 576764 | . 0863799 | . 499 | . 0853019 | -170 318 | . 082167 I |
| 2.450 | 1. 0640215 | II. 588347 | 0.0862936 | 2.500 | 1.0857362 | 12.182 494 | 0.0820850 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\text {a }}$ | $\mathrm{e}^{-\mathrm{u}}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{u}}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathbf{u}}$ | $e^{-0}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.500 | I. 0857362 | 12.182 494 | 0.0820850 | 2.550 | I. 1074509 | 12.807104 | 0.0780817 |
| . 501 | . 0861705 | . 194683 | . 0820030 | . 551 | . 1078852 | .819 917 | . 0780036 |
| . 502 | . 0866048 | . 206883 | .081 9210 | - 552 | . 1083195 | .832744 | . 0779257 |
| . 503 | .0870391 | . 219006 | .08I 8391 | . 553 | . 1087538 | .845583 | . 0778478 |
| . 504 | . 0874734 | .23I 322 | .08I 7573 | . 554 | . 109 I88I | .858435 | . 0777700 |
| 2.505 | 1.087 9077 | 12.243559 | 0.081 6755 | 2.555 | I. 1096224 | 12.871300 | 0.0776922 |
| . 506 | . 0883420 | .255809 | .08I 5940 | . 556 | . IIO 0567 | . 884 I77 | . 0776146 |
| . 507 | . 0887763 | . 26807 I | .08I 5124 | . 557 | . 1104910 | . 897068 | . 0775370 |
| . 508 | . 0892106 | . 280345 | .08I 4309 | . 558 | . I IO 9253 | . 909972 | . 0774595 |
| . 509 | . 0896449 | . 292 63I | .0SI $3+95$ | . 559 | . III 3596 | . 922888 | . 077 382I |
| 2.510 | I. 0900791 | I2.304 930 | 0.081 2682 | 2.560 | I.III 7939 | 12.935 817 | 0.0773047 |
| . 51 I | . 090 . 5134 | .317 24I | .081 I370 | . 561 | . II2 2282 | . 948760 | . 0772275 |
| . 512 | . 0909477 | . 329565 | .081 1059 | . 562 | . II2 6625 | .96I 715 | . 0771503 |
| . 513 | .091 3820 | .341 900 | .081 0248 | . 563 | . II3 0968 | . 974683 | . 0770732 |
| . 514 | .091 8163 | . 354248 | .0809438 | . 564 | . II3 53II | .987664 | . 076 9961 |
| 2.515 | 1. 0922506 | 12.366609 | 00808629 | 2.565 | I. II3 9653 | 13.000 658 | 0.0769192 |
| . 516 | . 0926849 | . 3781982 | .c80 7821 | . 566 | . II4 3996 | .013 666 | . 0768423 |
| . 517 | . 093 I192 | . 391306 | .080 7013 | . 567 | . II4 8339 | . 026686 | . 0767655 |
| . 518 | . 0935535 | . 403764 | .c80 6207 | . 568 | . II5 2682 | .039719 | . 0766888 |
| . 519 | . 0939878 | . 416 I 14 | . 0805401 | . 569 | . II5 7025 | .052765 | . 076 6I2I |
| 2.520 | I. 094 422I | 12.428597 | 0.0804595 | 2.570 | I. II6 1368 | 13.065 824 | 0.0765355 |
| . 521 | . 0948564 | . 441032 | . 0803792 | . 571 | . II6 57II | . 078897 | . 0764590 |
| . 522 | . 0952907 | . 453 479 | . $086 \cdot 2988$ | . 572 | . II7 0054 | . 091982 | . 0763826 |
| . 523 | . 0957250 | .465938 | . 0802186 | . 573 | . II7 4397 | . 10508 I | . 0763063 |
| . 524 | . 0961593 | . 478 4II | . 080 I384 | . 574 | . 1178740 | . 118192 | . 0762300 |
| 2.525 | 1.096 5936 | 12.490895 | 0.0800583 | 2.575 | I. 1183083 | 13.13I 317 | 0.0761538 |
| . 526 | . 0970279 | . 503392 | .0799783 | . 576 | . 1187426 | . 144455 | . 0760777 |
| . 527 | . 0974622 | . 515902 | . 0798984 | . 577 | . II9 1769 | . 157606 | . 0760017 |
| . 528 | . 0978965 | . 528424 | . 079 8185 | . 578 | . II9 6II2 | .170 770 | . 0759257 |
| . 529 | . 0983307 | . 540959 | .0797387 | . 579 | . 1200455 | . 183948 | . 0758498 |
| 2.530 | 1.098 7650 | 12.553506 | 0.0796590 | 2.580 | I. 1204798 | I3.197 138 | 0.0757740 |
| . 53 I | . 0991993 | . 566066 | . 0795794 | . 581 | . 1209141 | . 210342 | . 0756983 |
| . 532 | .0996336 | . 578638 | . 0794999 | . 582 | .121 3484 | . 223559 | . 0756226 |
| . 533 | . 1000679 | . 591223 | . 0794204 | . 583 | . 1217826 | .236789 | . 0755470 |
| . 534 | . 1005022 | . 60382 I | . 0793410 | . 584 | . 1222169 | .250032 | . 07547 I 5 |
| 2.535 | I. 1009365 | 12.616431 | 0.0792617 | 2.585 | 1. 1226512 | 13.263289 | 0.0753961 |
| . 536 | . IOI 3708 | . 629054 | . 0791825 | . 586 | . 1230855 | . 276559 | . 0753207 |
| . 537 | . IOI 805I | . 641689 | . 0791034 | . 587 | . 1235198 | . 289842 | . 0752454 |
| . 538 | . 1022394 | . 654337 | . 0790243 | . 588 | . 1239541 | . 303139 | . 0751702 |
| . 539 | . 1026737 | . 666998 | . 0789453 | . 589 | . 1243884 | . 316449 | . 0750951 |
| 2.540 | 1. 1031080 | 12.679671 | 0.0788664 | 2.590 | I. 1248227 | I3.329 772 | 0.0750200 |
| . 54 I | . 1035423 | . 692357 | . 0787876 | . 591 | . 1252570 | . 343108 | . 074 9451 |
| . 542 | . 1039766 | . 705056 | . 0787088 | . 592 | . 1256913 | . 356458 | . 074 8701 |
| . 543 | . 1044109 | . 717767 | . 0786302 | - 593 | . 1261256 | -369 821 | . 0747953 |
| . 544 | . 1048452 | . 730491 | . 0785516 | . 594 | . 1265599 | . 383198 | . 0747206 |
| 2.545 | I. 1052795 | 12.743228 | 0.0784731 | 2.595 | I. 1269942 | 13.396 587 | 0.0746459 |
| . 546 | . 1057138 | . 755978 | . 0783946 | . 596 | . 1274285 | . 409 991 | . 0745713 |
| . 547 | . 1061480 | -768 740 | . 0783163 | . 597 | . 1278628 | . 423407 | . 0744967 |
| . 548 | . 1065823 | .781 515 | . 0782380 | . 598 | . 1282971 | .436838 | . 0744223 |
| . 549 | . 1070166 | . 794303 | . 0781598 | . 599 | . 1287314 | . 450 28I | . 0743479 |
| 2.550 | I. 1074509 | 12.807104 | 0.078 0817 | 2.600 | I. 1291657 | 13.463 738 | 0.0742736 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $e^{\text {a }}$ | $e^{-u}$ | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{\text {u }}$ | $e^{-0}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-a}$ | u | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.600 | I. 1291657 | 13.463738 | 0.0742736 | 2.650 | I. 1508804 | I4. I54 039 | 0.0706512 |
| . 601 | . 1295999 | . 477208 | . 0741993 | .651 | . I5I 3147 | . 168200 | $.0705806$ |
| . 602 | . 1300342 | . 490692 | .0741252 | . 652 | - I5I 7490 | . 182375 | . 0705101 |
| . 603 | . I30 4685 | . 504190 | . 074 05II | . 653 | . 1521833 | . 196565 | . 0704396 |
| . 604 | . I30 9028 | . 517701 | . 0739771 | . 654 | . 152 6176 | . 210768 | .0703692 |
| 2.605 | I.I3I 337I | 13.531 225 | 0.0739031 | 2.655 | I. 1530518 | 14.224986 | 0.0702988 |
| . 606 | .131 7714 | . 544763 | . 0738293 | . 656 | . I53 486I | . 239218 | . 0702286 |
| . 607 | . I32 2057 | . 558315 | .0737555 | . 657 | . I53 9204 | . 253464 | .070 1584 |
| . 608 | . I326400 | . 571880 | .07368 I 8 | . 658 | . 1543547 | .267725 | . 0700883 |
| . 609 | . I33 0743 | . 585459 | . 073 608I | . 659 | . I54 7890 | . 282000 | . 0700182 |
| 2.610 | I. I33 5086 | 13.599051 | 0.0735345 | 2.660 | I. 1552233 | 14.296289 | 0.0699482 |
| .6II | . I33 9429 | . 612657 | . 0734610 | . 66 I | . 1556576 | . 310593 | . 0698783 |
| . 612 | . I34 3772 | .626276 | .0733876 | . 662 | . 1560919 | . 324910 | . 0698085 |
| .6I3 | . 1348115 | .639909 | .0733143 | .663 | . I565262 | - 339242 | . 0697387 |
| . 614 | . I35 2458 | . 653556 | . 0732410 | . 664 | . I56 9605 | . 353589 | . 0696690 |
| 2.615 | I. I35 680I | 13.667216 | 0.0731678 | 2.665 | I. 1573948 | 14.367950 | 0.0695994 |
| . 616 | . I36 II44 | . 680890 | . 0730947 | . 666 | . 1578291 | . 382325 | . 0695298 |
| . 617 | . I36 5487 | .694578 | .0730216 | . 667 | . I58 2634 | . 396714 | . 0694603 |
| . 618 | - I36 9830 | . 708280 | .0729486 | . 668 | . 1586977 | . 411118 | .0693909 |
| . 619 | . 1374172 | . 721995 | .0728757 | . 669 | . I59 1320 | . 425536 | . 0693215 |
| 2.620 | r. 1378515 | 13.735724 | 0.0728029 | 2.670 | I. 1595663 | 14.439969 | 0.0692522 |
| . 621 | . 1382858 | . 749466 | . 0727301 | . 671 | . 1600006 | . 454416 | . 0691830 |
| . 622 | . 1387201 | . 763222 | . 0726574 | . 672 | . I60 4349 | . 468878 | . 069 II39 |
| . 623 | . I39 I544 | .776993 | .0725848 | . 673 | . I60 8692 | . 483354 | . 0690448 |
| . 624 | . 1395887 | .790776 | .0725122 | . 674 | . I6I 3034 | . 497845 | . 0689758 |
| 2.625 | I. I40 0230 | 13.804574 | 0.0724398 | 2.675 | ェ.161 7377 | 14.512350 | 0.0689068 |
| . 626 | . I40 4572 | . 818386 | . 0723674 | . 676 | . 1621720 | . 526869 | . 0688380 |
| . 627 | . I40 8916 | . 8322 II | .0722950 | . 677 | . 1626063 | . 541404 | . 0687692 |
| . 628 | - I4I 3259 | .846050 | . 0722228 | . 678 | . I63 0406 | . 555952 | . 0687004 |
| . 629 | .141 7602 | .859903 | . 072 I 506 | . 679 | . I63 4749 | :570 515 | . 0686318 |
| 2.630 | I. I42 1945 | 13.873770 | 0.0720785 | 2.680 | 1. 1639092 | 14.585093 | 0.0685632 |
| . 631 | . I42 6288 | . 887651 | . 0720064 | .68I | . 1643435 | . 599686 | . 0684946 |
| . 632 | . I43 063I | .901 545 | .071 9344 | . 682 | . 1647778 | . 614293 | . 0684262 |
| . 633 | . I43 4974 | .915 454 | .071 8626 | . 683 | . 1652121 | . 628914 | . 0683578 |
| . 634 | . 1439317 | .929376 | .071 7907 | . 684 | . 1656464 | . 643550 | . 0582894 |
| 2.635 | I. I44 3660 | 13.943312 | 0.0717190 | 2.685 | I. 1660807 | 14.658201 | $0.068{ }^{2212}$ |
| . 636 | . I44 8003 | . 957263 | .071 6473 | . 686 | . 166 5150 | . 672867 | . 0681530 |
| . 637 | . I45 2345 | .971 227 | .07I 5757 | . 687 | . I669493 | . 687547 | . 0680849 |
| . 638 | . I45 6688 | . 985205 | . 0715041 | . 688 | . 1673836 | . 702242 | . 0680168 |
| . 639 | . I46 103I | . 999197 | . 0714327 | . 689 | . 167 8179 | . 716952 | . 0679489 |
| 2.640 | I. 1465374 | 14.0I3 204 | 0.07136 I 3 | 2.690 | I. 1682522 | 14.731676 | 0.0678809 |
| . 641 | . 1469717 | .027224 | .071 2899 | . 691 | . 1686865 | . 746415 | . 067 813I |
| . 642 | . 1474060 | .04I 258 | . 0712187 | . 692 | . 169 1207 | . 761169 | . 0677453 |
| . 643 | . 1478403 | .055306 | .071 1475 | . 693 | . 1695550 | . 775937 | .0676776 |
| . 644 | . 1482746 | .069369 | .071 0764 | . 694 | . 1699893 | . 790721 | . 0676100 |
| 2.645 | I. 1487089 | 14.083445 | 0.0710054 | 2.695 | I. 1704236 | 14.805519 | 0.0675424 |
| . 646 | . I49 1432 | .097536 | . 0709344 | . 696 | . I70 8579 | . 820332 | . 0674749 |
| . 647 | . I49 5775 | . III 640 | . 0708635 | . 697 | . 171 2922 | . 835159 | . 0674074 |
| . 648 | . 1500118 | . 125759 | . 0707927 | . 698 | . 1717265 | .850002 | . 0673401 |
| . 649 | . 150446 I | . I39 892 | .0707219 | . 699 | . 1721608 | . 864859 | . 0672728 |
| 2.650 | I. 1508804 | 14.154 039 | 0.0706512 | 2.700 | 1. 1725951 | 14.879732 | 0.0672055 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{\text {u }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.700 | I. I72 595I | 14.879732 | 0.0672055 | 2.750 | I. 1943098 | 15.642632 | 0.0639279 |
| .701 | . 1730294 | . 894 619 | . 0671383 | .751 | . 194 7441 | . 658282 | . 0638540 |
| . 702 | - I73 4637 | . 90952 I | .0670712 | . 752 | . 1951784 | . 673948 | . 0638001 |
| . 703 | . I73 8980 | . 924438 | .0670042 | . 753 | . 1956127 | . 689630 | . 0637364 |
| . 704 | . 1743323 | . 939370 | . 0669372 | . 754 | -196 0470 | . 705328 | . 0636727 |
| 2.705 | I. 1747666 | 14.954317 | 0.0668703 | 2.755 | I. 19648 I 3 | 15.721041 | 0.0636090 |
| . 706 | . 1752009 | . 969278 | . 0668035 | . 756 | . 1969156 | . 736770 | . 0635454 |
| . 707 | . I75 6352 | . 984255 | . 0667367 | . 757 | . 1973499 | . 752514 | . 063 4819 |
| . 708 | . 1760695 | . 999247 | . 0666700 | . 758 | -197 7842 | . 768275 | .0634185 |
| . 709 | . 1765038 | I5.014 254 | . 0666039 | . 759 | . 1982185 | . 784 051 | . 063 355I |
| 2.710 | 1.1769380 | 15.029275 | 0.0665368 | 2.760 | I. 1986528 | 15.799843 | 0.0632918 |
| . 711 | . 1773723 | . 044312 | .0664703 | . 761 | . 1990871 | .815 651 | . 0632285 |
| . 712 | . 1778066 | .059364 | .0664039 | . 762 | . 1995214 | .831 474 | . 0631653 |
| . 713 | . 1782409 | . 07443 I | .0663375 | . 763 | . 1999557 | . 847314 | . 0631022 |
| . 714 | .178 6752 | .089 513 | . 0662712 | . 764 | . 2003899 | .863169 | . 063 039I |
| 2.715 | I.I79 1095 | 15.104610 | 0.0662050 | 2.765 | I. 2008242 | 15.879040 | 0.062 976I |
| . 716 | . . I79 5438 | . 119722 | . 066 I388 | . 766 | . 2012585 | . 894927 | . 0629132 |
| .717 | . I79 978I | . I34 850 | . 0660727 | . 767 | . 2016928 | .910 830 | . 0628503 |
| . 718 | . 1804124 | - I49 992 | . 0660066 | . 768 | .2021271 | .926749 | .062 7875 |
| . 719 | . 1808467 | . 165149 | .0659407 | .769 | . 2025614 | . 942683 | . 0627247 |
| 2.720 | I. 181 2810 | 15.180322 | 0.0658748 | 2.770 | I. 2029957 | 15.958634 | 0.0626620 |
| .721 | . 1817153 | . 195510 | . 0658089 | . 771 | . 2034300 | . 974601 | . 0625994 |
| . 722 | . 1821496 | . 210713 | . 0657431 | . 772 | . 2038643 | .990583 | . 0625368 |
| . 723 | .1825839 | . 225932 | . 0656774 | . 773 | . 2042986 | 16.006582 | . 0624743 |
| . 724 | . 1830182 | . 241165 | . 065 6II8 | . 774 | . 2047329 | . 022596 | .062 4119 |
| 2.725. | I. 183 4525 | I5.256 414 | 0.0655462 | 2.775 | I. 2051672 | 16.038 627 | 0.0623495 |
| . 726 | . 1838868 | . 271678 | . 0654807 | . 776 | . 2056015 | . 054674 | . 0622872 |
| . 727 | . 1843211 | . 286957 | . 0654152 | . 777 | . 2060358 | . 070736 | . 0622249 |
| . 728 | . 1847553 | . 302252 | . 0653499 | . 778 | . 2064701 | . 086 8i5 | . 0621627 |
| . 729 | . 185 I896 | . 317562 | . 0652845 | . 779 | : 2069044 | . 102910 | . 0621006 |
| 2.730 | I. 1856239 | 15.332887 | 0.0652193 | 2.780 | I. 2073387 | 16. 119021 | 0.0620385 |
| . 731 | . 1860582 | - 348228 | . 0651541 | .781 | . 2077730 | . 135148 | .061 9765 |
| . 732 | . I86 4925 | . 363583 | . 0650890 | . 782 | .2082072 | .151 291 | .061 9146 |
| . 733 | . 1869268 | -378955 | . 0650239 | . 783 | . 2086415 | . 167451 | .06I 8527 |
| . 734 | . 1873611 | . 394 34I | . 0649589 | . 784 | . 2090758 | . 183626 | .06I 7908 |
| 2.735 | I. 1877954 | 15.409743 | 0.0648940 | 2.785 | I. 209 5101 | 16.199818 | 0.0617291 |
| . 736 | . 1882297 | . 425 I6I | . 0648291 | . 786 | . 2099444 | . 216026 | .06I 6674 |
| . 737 | . 1886640 | . 440594 | . 0647643 | . 787 | . 2103787 | .232250 | .06I 6058 |
| .738 | . 1890983 | .456 042 | . 0646996 | . 788 | .210 8130 | .248490 | .06I 5442 |
| .739 | . 1895326 | . 471506 | . 0646349 | . 789 | . 2II 2473 | .264747 | .061 4827 |
| 2.740 | I. 1899669 | 15.486 985 | 0.0645703 | 2.790 | 1.211 6816 | 16.281 020 | 0.0614212 |
| . 741 | . 1904012 | . 502480 | . 0645058 | . 791 | . 2121159 | . 297309 | .06I 3598 |
| . 742 | . 1908355 | . 517990 | . 0644413 | . 792 | . 2125502 | -3I3 6I4 | .06I 2985 |
| . 743 | . I91 2698 | . 533516 | . 0643769 | . 793 | . 2129845 | . 329936 | .06I 2372 |
| . 744 | . 1917041 | - 549057 | . 0643126 | . 794 | . 2134188 | . 346274 | .061 1760 |
| 2.745 | I. 1921384 | 15.564614 | 0.0642483 | 2.795 | I. 213853 I | 16.362629 | 0.0611149 |
| . 746 | . 1925726 | . 580 I86 | . 0641841 | . 796 | . 2142874 | . 379000 | .06I 0538 |
| . 747 | . 1930069 | . 595774 | $.064 \text { II99 }$ | . 797 | . 2147217 | . 395387 | . 0609928 |
| . 748 | . 19344 I 2 | .6II 378 | . 0640558 | .798 .799 | .2151560 .2155903 | .411 790 | .0609318 .0608709 |
| . 749 | . 1938755 | . 626997 | . 06399 | . 799 | .215 5903 | . 428210 | . 0608709 |
| 2.750 | I. 1943098 | 15.642632 | 0.0639279 | 2.800 | I. 2160245 | 16.444647 | 0.060 8iot |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{\text {u }}\right.$ ) | $e^{\text {u }}$ | $e^{-u}$ | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(e^{u}\right)$. | $e^{\text {u }}$ | $e^{-0}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.800 | 1. 2160245 | 16.444 647 | 0.0508101 | 2.850 | I. 2377393 | 17.287782 | 0.0578443 |
| . 801 | . 2164588 | .461 100 | .060 7493 | . 851 | .2381736 | . 305078 | . 0577865 |
| . 802 | . 216893 I | . 477569 | . 0506886 | . 852 | .2386079 | . 322392 | . 0577287 |
| . 803 | . 2173274 | . 494055 | . 0606279 | . 853 | .2390422 | . 339723 | . 0576710 |
| . 804 | .217 7617 | . 510557 | . 0605673 | . 854 | .2394765 | . 357 07I | . 0576134 |
| 2.805 | 1.218 1960 | 16.527076 | 0.0605068 | 2.855 | I. 2399107 | 17.374 437 | 0.0575558 |
| . 806 | . 2186303 | . 543 61 I | . 0604463 | . 856 | . 2403450 | -391 820 | . 0574983 |
| . 807 | . 2190646 | . 560 I63 | . 0603859 | . 857 | . 2407793 | . 409221 | . 0574408 |
| . 808 | . 2194989 | . 576732 | . 0603255 | . 858 | . 24I 2136 | . 426639 | .0573834 |
| . 809 | . 2199332 | . 593 317 | . 0602652 | . 859 | .24I 6479 | . 444074 | . 057326 I |
| 2.810 | 1.2203675 | 16.609918 | 0.0602050 | 2.860 | I. 2420822 | 17.46I 527 | 0.0572688 |
| .8II | . 2208018 | . 626536 | . 0601448 | .86I | . 2425165 | . 478997 | . 0572115 |
| . 812 | . 2212361 | . 643 I71 | . 0600847 | . 852 | . 2429508 | . 496485 | .0571543 |
| . 813 | . 2216704 | . 659823 | .0500246 | . 863 | . 243 385I | . 513 990 | . 0570972 |
| . 814 | .2221047 | . 67649 I | .0599647 | . 864 | . 243 8194 | . 53 I 513 | . 057 0401 |
| 2.815 | 1. 2225390 | 16.693176 | 0.0599047 | 2.865 | 1.244 2537 | 17.549053 | 0.0569831 |
| .8i6 | . 2229733 | . 709877 | . 0598448 | . 866 | . 2446880 | . 566611 | . 0569262 |
| .8I7 | .2234076 | . 726595 | . 0597850 | . 857 | .2451223 | . 584 I86 | . 0568693 |
| .818 | .2238418 | . 743 33I | . 0597253 | . 868 | . 2455566 | . 601779 | .056 8124 |
| . 819 | . 224 276I | . 760082 | .0596656 | . 869 | . 2459909 | . 619390 | .0567557 |
| 2.820 | 1.2247104 | 16.776851 | 0.0596059 | 2.870 | I. 2464252 | 17.637 о18 | 0.0566989 |
| . 82 I | . 22251447 | . 793636 | . 0595464 | . 871 | . 2468595 | . 654664 | . 0566423 |
| . 822 | .2255790 | . 810438 | . 0594868 | . 872 | . 2472938 | . 672328 | .0565856 |
| . 823 | . 226 OI33 | . 827257 | .0594274 | . 873 | .2477280 | .690009 | .0565291 |
| . 824 | .2264476 | . 8440092 | . 0593680 | . 874 | .2481623 | . 707708 | . 0564726 |
| 2.825 | I. 2268819 | 16.860 945 | 0.0593087 | 2.875 | 1. 2485966 | 17.725424 | 0.056416 I |
| . 826 | . 2273162 | . 877 814 | . 0592494 | . 876 | . 2490309 | . 743158 | . 0563598 |
| . 827 | . 2277505 | . 894701 | . 0591902 | . 877 | . 2494652 | . 760910 | . 0563034 |
| . 828 | . 228 I848 | .91I 604 | . 0591310 | . 878 | . 2498995 | . 778680 | . 056247 I |
| . 829 | . 228 6191 | .928524 | . 0590719 | . 879 | .2503338 | .796468 | .0561909 |
| 2.830 | I. 2290534 | 16.94546 I | 0.0590129 | 2.880 | 1. 250768 I | 17.814 273 | 0.0561348 |
| . 831 | . 2294877 | . 962415 | . 0589539 | . 88 I | .251 2024 | . 832096 | . 0560787 |
| . 832 | . 2299220 | .979386 | . 0588949 | . 882 | .251 6367 | . 849937 | . 0560226 |
| . 833 | . 2303563 | .996374 | . 0588361 | . 883 | .2520710 | .857795 | . 0559666 |
| . 834 | .2307906 | 17.013378 | .0587773 | . 884 | .2525053 | .885673 | .0559107 |
| 2.835 | 1.231 2249 | 17.030400 | 0.0587185 | 2.885 | 1. 2529396 | 17.903568 | 0.0558548 |
| . 836 | .231 6592 | . 047439 | . 0586598 | . 886 | . 2533739 | .921 480 | . 0557990 |
| . 837 | .2320934 | . 064495 | . 0586012 | . 887 | . 2538082 | . 939 4II | . 0557432 |
| . 838 | . 2325277 | .081 568 | . 0585426 | . 888 | .2542425 | .957359 | $.0556875$ |
| . 839 | .2329620 | .098658 | . 058484 I | . 889 | . 2546768 | . 975325 | . 0556318 |
| 2.840 | 1.2333963 | 17.115 766 | 0.0584257 | 2.890 | I. 255 IIII | 17.993310 | 0.0555762 |
| . 84 I | . 2338306 | . 132890 | . 0583673 | . 891 | . 2555453 | 18.011312 | . 0555207 |
| . 842 | . 2342649 | . 150031 | . 0583089 | . 892 | . 2559796 | . 029332 | . 0554652 |
| . 843 | .2346992 | . 167190 | $.0582507$ | . 893 | .2564139 | . 047371 | . 0554097 |
| . 844 | . 235 I335 | . 184365 | . 0581924 | . 894 | . 2568482 | . 065427 | . 0553544 |
|  | I. 2355678 | 17.201 559 | 0.0581343 | 2.895 | I. 2572825 | 18.083501 |  |
| . 846 | .2360021 | . 218769 | $.0580762$ | . 896 | $.2577168$ | - IOI 594 | $.0552438$ |
| . 847 | .2364364 | .235996 | . 058 0181 | . 897 | . 25815 II | . 119705 | .055 1885 |
| . 848 | .2368707 | .25324 I | . 0579601 | . 898 | .2585854 | . 137833 | $.0551334$ |
| . 849 | .2373050 | .270503 | . 0579022 | . 899 | . 2590197 | . 155980 | . 0550783 |
| 2.850 | I. 2377393 | 17.287 782 | 0.0578443 | 2.900 | I. 2594540 | 18.174 145 | 0.0550232 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\log _{e}\left(e^{u}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-0}$ |

The Exponential.

| $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | u | $\log _{10}\left(e^{u}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.900 | I. 2594540 | 18.174 145 | 0.0550232 | 2.950 | 1.281 1687 | 19. 105954 | 0.0523397 |
| . 901 | . 2598883 | . 192329 | . 0549682 | . 951 | .281 6030 | . 125069 | . 0522874 |
| . 902 | . 2603226 | . 210530 | . 0549133 | .952 | .2820373 | . 144204 | . 0522351 |
| . 903 | . 2607569 | . 228750 | . 0548584 | . 953 | .2824716 | . 163358 | .0521829 |
| . 904 | . 2611912 | . 246988 | .0548036 | . 954 | . 2829059 | . 18253 I | .0521308 |
| 2.905 | 1.261 6255 | 18.265244 | 0.0547488 | 2.955 | 1.2833402 | 19.201723 | 0.0520787 |
| . 906 | . 2620598 | .283518 | . 0546941 | . 956 | .2837745 | . 220934 | . 0520266 |
| . 907 | . 262494 I | . 3018 II | .054 6394 | . 957 | . 2842088 | . 240165 | .051 9746 |
| . 908 | . 2629284 | . 320122 | .0545848 | . 958 | . 284643 I | . 259 414 | .051 9227 |
| . 909 | . 2633626 | . 33845 I | .05I 5302 | -959 | .2850774 | .278683 | .051 8708 |
| 2.910 | 1. 2637969 | 18.356799 | 0.0544757 | 2.960 | 1.2855117 | 19.297972 | 0.05I 8189 |
| . 911 | . 2642312 | . 375165 | . 0544213 | . 961 | .2859460 | . 317279 | .051 7671 |
| . 912 | . 2646655 | . 393549 | . 0543669 | . 962 | . 2863803 | . 336606 | .051 7154 |
| . 913 | . 2650998 | .411 952 | .0543125 | . 963 | . 286 8145 | . 355953 | .05I 6637 |
| . 914 | . 265534 I | . 430373 | . 0542583 | . 954 | . 2872488 | . 375 3I8 | .05I 6121 |
| 2.915 | I. 2659684 | 18.4488 I 2 | 0.0542040 | 2.965 | 1.2876831 | 19.394703 | 0.0515605 |
| . 916 | . 2664027 | .467270 | . 0541499 | . 966 | . 288 1174 | .414 108 | . 0515089 |
| . 917 | . 2668370 | . 485747 | . 0540957 | . 967 | . 2885517 | . 43353 I | .051 4575 |
| . 918 | . 2672713 | . 504242 | .0540417 | . 968 | . 2889860 | . 452975 | .051 4060 |
| . 919 | .2677056 | . 522755 | .0539876 | . 969 | .2894203 | . 472437 | .051 3546 |
| 2.920 | I. 268 I 399 | 18.541 287 | 0.0539337 | 2.970 | 1.289 8546 | 19.491 920 | 0.0513033 |
| . 921 | . 2685742 | . 559838 | . 053 8758 | .97I | . 2902889 | .5II 421 | .05I 2520 |
| . 922 | . 2690085 | . 578407 | . 0538259 | . 972 | . 2907232 | . 530942 | .051 2008 |
| . 923 | .2694428 | . 596995 | . 0537721 | . 973 | .291 1575 | . 550483 | .051 1496 |
| . 924 | . 2698771 | .6I5 60I | .0537184 | . 974 | . 2915918 | -570 043 | .051 0985 |
| 2.925 | 1.2703114 | 18.634226 | 0.0536647 | 2.975 | I. 2920261 | 19.589623 | 0.051 0474 |
| . 926 | . 2707457 | . 652870 | . 053 6III | . 976 | . 2924604 | . 609223 | . 0509964 |
| . 927 | . 2711799 | . 671532 | .0535575 | . 977 | . 2928947 | . 628842 | . 0509454 |
| . 928 | . 2716142 | . 690213 | .0535039 | . 978 | . 2933290 | . 648480 | . 0508945 |
| . 929 | .2720485 | .708912 | . 0534505 | . 979 | . 2937633 | . 668139 | . 0508437 |
| 2.930 | 1.272 4828 | 18.727631 | 0.0533970 | 2.980 | 1. 2941976 | 19.687 8I7 | 0.0507928 |
| .93I | . 272 9171 | . 746368 | . 0533437 | .98I | . 2946319 | . 707514 | . 0507421 |
| . 932 | .2733514 | . 765123 | . 0532904 | . 982 | . 2950661 | . 727232 | .050 6913 |
| . 933 | .2737857 | . 783898 | .0532371 | . 983 | . 2955004 | . 746969 | .050 6407 |
| . 934 | . 2742200 | . 802691 | . 0531839 | . 984 | . 2959347 | .766726 | . 0505901 |
| 2.935 | I. 2746543 | 18.821503 | 0.0531307 | 2.985 | 1. 2963690 | 19.786502 | 0.0505395 |
| . 936 | . 2750886 | . 840334 | . 0530776 | . 986 | . 2968033 | . 806299 | . 0504890 |
| . 937 | . 2755229 | . 859184 | .0530246 | . 987 | . 2972376 | . 826115 | . 0504385 |
| . 938 | .2759572 | . 878052 | .0529716 | . 988 | .2976719 | . 845951 | . 050 3881 |
| . 939 | .2763915 | .896940 | .0529186 | . 989 | . 2981062 | . 865807 | . 0503377 |
| 2.940 | I. 2768258 | 18.915846 | 0.0528657 | 2.990 | 1. 2985405 | 19.885682 | 0.0502874 |
| . 941 | . 2772601 | . 934772 | .052 8i29 | . 991 | . 2989748 | . 905578 | . 0502372 |
| . 942 | .2776944 | . 953716 | .0527601 | . 992 | . 2994091 | . 925494 | . 0501870 |
| . 943 | . 2781287 | . 972679 | .0527074 | . 993 | . 2998434 | . 945429 | . 0501368 |
| . 944 | .2785630 | .991 66I | .0526547 | . 994 | . 3002777 | .965385 | . 0500867 |
| 2.945 | I. 2789972 | 19.010662 | 0.0526021 | 2.995 | 1.300 7120 | 19.985360 | 0.0500366 |
| . 946 | . 2794315 | .029683 | .0525495 | . 996 | . 3011463 | 20.005355 | . 0499866 |
| . 947 | . 2798658 | $.048722$ | .0524970 | . 997 | -301 5806 | .025371 | . 0499367 |
| .948 | .2803001 | . 067780 | .0524445 .0523921 | . 998 | . 3020149 | .045406 | . 0498857 |
| . 949 | . 2807344 | . 086857 | . 052 392I | . 999 | . 3024492 | . 065461 | . 0498369 |
| 2.950 | 1.281 1687 | 19.105 954 | 0.0523397 | 3.000 | 1. 3028834 | 20.085537 | 0.0497871 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{u}\right)$ | $\log _{10}\left(e^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{a}}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-\mathrm{a}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.00 | I. 3028834 | 20.085537 | 0.0497871 | 3.50 | 1.5200307 | 33.115 452 | 0.0301974 |
| . | . 3072264 | . 287400 | . 0492917 | . 51 | . 5243736 | . 448268 | . 0298969 |
| . 02 | -3115693 | -491 292 | . 0488012 | . 52 | . 5287 I 66 | . 784429 | . 0295994 |
| . 03 | -315 9123 | . 697233 | . 0483156 | - 53 | . 5330595 | 34.123968 | . 0293049 |
| . 04 | - 3222552 | . 905243 | . 0478349 | . 54 | . 5374025 | . 466919 | . 029 OI33 |
| 3.05 | 1. 3245982 | 21.115 344 | 0.0473589 | 3.55 | I.541 7454 | 34.813318 | 0.0287246 |
| . 06 | . 32894 II | . 327557 | . 0468877 | . 56 | . 5460884 | 35.163197 | . 0284388 |
| . 07 | - 333284 I | . 541903 | . 0464212 | . 57 | . 5504313 | . 516593 | . 0281559 |
| . 08 | - 3376270 | . 758402 | . 0459593 | . 58 | . 5547742 | . 873541 | . 0278757 |
| . 09 | -3419699 | . 977078 | . 0455020 | . 59 | . 5591172 | 36.234076 | . 0275983 |
| 3.10 | 1. 3463129 | 22.197 951 | 0.0450492 | 3.60 | I. 5634601 | 36.598234 | 0.0273237 |
| . 1 | . 3506558 | . 421044 | . 044 6010 | . 61 | . 5678031 | . 966053 | . 0270518 |
| . 12 | - 3549988 | . 646380 | . 0441572 | . 62 | . 5721460 | 37.337568 | . 0267827 |
| . 13 | - 3593417 | . 873980 | . 0437178 | . 63 | .5764890 .5808319 | .712817 | . 0265162 |
| . 14 | - 3636847 | 23.103 867 | . 0432828 | . 64 | . 5808319 | 38.091837 | . 0262523 |
| 3.15 | 1. 3680276 | 23.336065 | 0.0428521 | 3.65 | 1. 5851749 | 38.474666 | 0.0259911 |
| . 16 | . 3723706 | . 570596 | . 0424257 | . 66 | . 5895178 | . 861343 | . 0257325 |
| . 17 | - 3767135 | . 807484 | . 0420036 | . 67 | - 5938607 | 39.251906 | . 0254765 |
| . 18 | -381 0565 | 24.046754 | .041 5857 | . 68 | - 5982037 | . 646394 | . 0252230 |
| . 19 | -385 3994 | .288427 | .041 1719 | . 69 | . 6025466 | 40.044847 | . 0249720 |
| 3.20 | I. 3897423 | 24.532530 | 0.0407622 | 3.70 | 1. 6068896 | 40.447304 | 0.0247235 |
| , | . 3940853 | . 779086 | . 0403566 | . 71 | . 6112325 | . 853807 | . 0244775 |
| :22 | - 3984282 | 25.028120 | . 039 9551 | . 72 | .615 5755 | 41.264394 | . 0242340 |
| . 23 | - 4027712 | . 279657 | . 0395575 | . 73 | . 6199184 | . 679108 | . 0239928 |
| . 24 | . 407 II4I | . 533722 | . 0391639 | . 74 | . 6242614 | 42.097990 | . 023 7541 |
| 3.25 | I.4II 4571 | 25.790340 | 0.0387742 | 3.75 | 1. 6286043 | 42.521082 | 0.023 5177 |
| . 26 | .4158000 | 26.049537 | . 0383884 | . 76 | . 6329473 | . 948426 | . 0232837 |
| . 27 | . 4201430 | . 3111339 | . 0380064 | . 77 | . 6372902 | 43.380055 | . 023052 I |
| . 28 | . 4244859 | . 575773 | . 0376283 | . 78 | . 641633 I | .816 042 | . 0228227 |
| . 29 | . 4288288 | . 842864 | . 0372538 | . 79 | . 6459761 | 44.256400 | . 0225956 |
| $3 \cdot 30$ | 1.4331718 | 27.112 639 | 0.0368832 | 3.80 | 1.6503190 | 44.701184 | 0.0223708 |
| . 31 | . 4375147 | . 385 125 | . 0365162 | .8I | . 6546620 | 45.150439 | . 0221482 |
| . 32 | -4418577 | . 660351 | . 3361528 | . 82 | . 6590049 | . 604208 | . 0219278 |
| . 33 | . 4462006 | . 938342 | . 0357931 | . 83 | . 6633479 | 46.062538 | . 0217096 |
| - 34 | . 4505436 | 28.219127 | . 0354370 | . 84 | . 6676908 | . 525474 | .021 4936 |
| $3 \cdot 35$ | 1. 4548865 | 28.502734 | 0.0350844 | 3.85 | 1.6720338 | 46.993063 | 0.0212797 |
| . 36 | - 4592295 | . 789 191 | . 0347353 | . 86 | . 6763767 | 47.465351 | . 0210680 |
| . 37 | . 4635724 | 29.078527 | . 0343896 | . 87 | . 6807196 | . 942386 | . 0208584 |
| . 38 | . 4679153 | . 370771 | . 0340475 | . 88 | . 6850626 | 48.424215 | . 0206508 |
| - 39 | - 4722583 | . 665952 | . 0337087 | . 89 | . 6894055 | .910 887 | . 0204453 |
| 3.40 | 1.476 6012 | 29.964100 | 0.0333733 | 3.90 | 1. 6937485 | 49.402449 | 0.0202419 |
| .41 | . 4809442 | 30.265244 | . 0330412 | .91 | . 6980914 | . 898952 | . 0200405 |
| . 42 | - 4852871 | . 569415 | . 0327124 | . 92 | . 7024344 | 50.400445 | .or9 841 |
| -43 | . 4896301 | . 876643 | . 0323869 | -93 | . 7067773 | . 906978 | .or9 6437 |
| - 44 | - 4939730 | 31. 186958 | . 0320647 | . 94 | .711 1203 | 51.418601 | .o19 4482 |
| 3.45 | I. 4983160 | 31.500392 | 0.0317456 | 3.95 | 1. 7154632 | 51.935367 | 0.0192547 |
| . 46 | . 5026589 | .816 977 | .031 4298 | . 96 | . 7198061 | 52.457326 | . 19080631 |
| . 47 | . 5070019 | 32.136 743 | .031 1170 | . 97 | . 7241491 | .984531 53.517034 | $\text { . } 188734$ |
| . 48 | .5113448 .5156877 | .459722 .785948 | .0308074 .0305009 | . 98 | .7284920 .7328350 | 53.517 54.054 889 | $\begin{aligned} & .0186856 \\ & .0184997 \end{aligned}$ |
| .49 3.50 | .5156877 1. 5200307 | .785948 33.115452 | .0305009 0.0301974 | .99 4.00 | .7328350 1. 7371779 | 54.054889 54.598150 | 0.0183156 |
| $\log _{e}\left(e^{\text {u }}\right.$ ) | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | $e^{-a}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{n}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {a }}$ | ${ }^{-}$ |

Smithsonian Tables

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $e^{-u}$ | u | $\log _{10}\left(\mathrm{e}^{\mathbf{u}}\right)$ | $\mathrm{e}^{\mathrm{u}}$ | $\mathrm{e}^{-u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4.00 | 1.7371779 | 54.598150 | 0.0183156 | 4.50 | 1. 9543252 | 90.017131 | 0.011 . 1090 |
| . OI | . 7415209 | 55.146 871 | . 0181334 | . 51 | . 958 6681 | . 921819 | .oio 9985 |
| . 02 | . 7458538 | . 701106 | . 0179530 | . 52 | . 963 O111 | 91.835598 | . 0108890 |
| . 03 | . 7502068 | 56.260911 | . 1777743 | . 53 | . 9673540 | 92.758 561 | . -10 7807 |
| . 04 | . 7545497 | .826343 | . 1775975 | . 54 | .971 6969 | 93.690800 | .oro 6734 |
| 4.05 | 1.758 8927 | 57.397457 | 0.0174224 | 4.55 | 1.9760399 | 94.632408 | 0.010 5672 |
| . 06 | . 7632356 | . 974311 | . 0172490 | . 56 | . 9803828 | 95.583480 | .oio 4621 |
| . 07 | . 7675785 | 58.556963 | . 1770774 | . 57 | . 9847258 | 96.544110 | . 0103580 |
| . 08 | . 7719215 | 59.145 470 | . 10169075 | . 58 | . 9890687 | 97.514394 | . 0102549 |
| . 09 | . 7762644 | . 739892 | .016 7392 | . 59 | . 9934117 | 98.494430 | .oio 1529 |
| 4. 10 | 1. 7806074 | 60.340288 | 0.0165727 | 4.60 | 1.9977546 | 99.484316 | 0.0100518 |
| 11 | . 7849503 | . 9446718 | . 0164078 | . 61 | 2.0020976 | 100.484150 | . 0099518 |
| . 12 | -. 7892933 | 61. 559242 | . 10162445 | . 62 | . 0064405 | IOI. 494032 | . 0098528 |
| . 13 | . 7936362 | 62.177923 | . 10160829 | . 63 | .010 7835 | 102.514064 | .009 7548 |
| . 14 | . 7979792 | . 80282 I | . 0159229 | . 64 | . 0151264 | 103.544348 | - .09) 6577 |
| 4.15 | 1.8023221 | 63.434000 | 0.0157644 | 4.65 | 2.0194693 | 104.584 986 | 0.0095616 |
| . 16 | . 8066650 | 64.071523 | . 0156076 | . 66 | . 0238123 | 105.636082 | . 0094665 |
| . 17 | . 81110080 | . 715452 | .or5 4523 | . 67 | . 0281552 | 106.697743 | . 0093723 |
| . 18 | . 8153509 | 65.365853 | . 1152985 | . 68 | . 0324982 | 107.770073 | . 0092790 |
| . 19 | .819 6939 | 66.022791 | .oI5 I463 | . 69 | . 036841 I | 108.853 I8c | . 0091867 |
| 4.20 | 1.8240368 | 66.686331 | 0.0149956 | 4.70 | 2.041 1841 | 109.947172 | 0.0090953 |
| I | . 8283798 | 67.356540 | . 0148464 | . 71 | . 0455270 | 111.052160 | . 0090048 |
| . 22 | . 8327227 | 68.033484 | . 0146986 | . 72 | . 0498700 | 112.168 253 | . 0089152 |
| . 23 | . 8370657 | .717232 69.407852 | .OI4 5524 | . 73. | . 0542129 | 113.29555 .3 | $.0088265$ |
| . 24 | . 8414086 | 69.407852 | . 0144076 | . 74 | . 0585558 | 114.434 202 | .009 7386 |
|  | 1. 8457515 | 70. 105412 | 0.0142642 | 4.75 | 2.0628083 | 115.584285 | 0.co8 6517 |
| . 26 | . 8500945 | . 809983 | . 0141223 | . 76 | . 0672417 | 116.745926 | . 0085656 |
| . 27 | . 8544374 | 71.521636 | . 0139818 | . 77 | . 0715847 | 117.919242 | . 0084804 |
| . 28 | . 8587804 | 72.240440 | . 0138427 | . 78 | . 0759276 | 119.104 351 | . 0083960 |
| . 29 | . 8631233 | .966 468 | . 0137049 | . 79 | . 0802706 | 120.301 369 | . 0083125 |
| $4 \cdot 30$ | I. 8674663 | 73.699794 |  | 4.80 | 2.0846135 | 121.510418 | 0.0082297 |
| .31 .32 .33 | . 8718092 | 74.440489 | .OI3 4335 | .81 | . 0889565 | 122.731618 | . 0081479 |
| . 32 | . 8761522 | 75.188 628 | .oI3 2999 | . 82 | -. 0932994 | 123.965091 | . 008.0668 |
| . 33 | . 8804951 | .944287 76.707539 | . 13131675 | . 83 | . 0976423 | 125.210961 | . 0079865 |
| . 34 | . 884 8381 | 76.707539 | .013 0365 | . 84 | . 1019853 | 126.469352 | . 007907 I |
| 4.35 .36 | $\begin{array}{r}1.889 \\ \hline 80310 \\ \hline 8239\end{array}$ |  |  | 4.85 | 2. 1063282 | 127.740390 | 0.0078284 |
| . 36 | . 8935239 | 78.257134 | . 0127784 | . 86 | . 1106712 | 129.024203 | . 0077505 |
| -37 | . 8978609 | 79.043632 | .012 6512 | . 87 | . 1150141 | 130.320918 | . 0076734 |
| . 38 | . 9022098 | .838033 80.640419 | .0125254 .0124007 | . 88 | . 1193571 | 131.630665 | . 0075970 |
| -39 | . 9065528 | 80.640419 | . 0124007 | . 89 | .1237000 | 132.953575 | . 0075214 |
| 4.40 | I. 9108957 | 81.450869 | 0.0122773 | 4.90 | 2.128 0430 | 134.289780 | 0.0074466 |
| . 41 | . 9152387 | 82.269464 | .OI2 1552 | .91 | . 1323859 | 135.639415 | . 0073725 |
| . 42 | . 9195816 | 83.096285 | . 0120342 | . 92 | -1367289 | 137.002613 | . 0072991 |
| . 43 | . 9239246 | .931 417 | .oil 9145 | . 93 | . 1410718 | 138.379 513 | . 0072265 |
| . 44 | .928 2675 | 84.774942 | .oII 7959 | -94 | . 1454147 | 139.770250 | . 0071546 |
| 4.45 | 1.9326104 | 85.626944 | 0.011 6786 |  | 2. 1497577 | 141. 174964 | 0.0070834 |
| . 46 | . 9369534 | 86.487509 | .oII 5624 | . 96 | . 1541006 | 142.593796 | . 0070129 |
| . 47 | .941 2963 | 87.356723 | .oil 4473 | . 97 | . 1584436 | 144.026888 | . 006943 I |
| . 48 | -945 6393 | 88.234673 | .oil 3334 | . 98 | . 1627865 | 145.474382 | . 0068741 |
| . 49 | . 9499822 | 89.121 446 | .OII 2206 | .99 | . 1671295 | 146.936424 | . 0068057 |
| 4.50 | 1. 9543252 | 90.017 I3I | 0.0111090 | 5.00 | 2.171 4724 | 148.413159 | 0.0067379 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{4}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right.$ ) | $\mathrm{e}^{\text {a }}$ | $\mathrm{e}^{-\mathrm{a}}$ |

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $u$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{u}$ | $e^{-4}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.00 | 2.171 4724 | 148.413159 | 0.0067379 | $5 \cdot 50$ | 2.3886197 | 244.691 932 | 0.0040868 |
| . OI | . I75 8154 | 149.904736 | . 0066709 | . 51 | . 3929626 | 247.151 127 | . 004 0461 |
| . 02 | . 180 1583 | 151.411304 | . 0066045 | . 52 | . 3973055 | 249.635037 | . 0040058 |
| . 03 | . 1845012 | 152.933 OI3 | . 0065388 | . 53 | . 4016485 | 252.143 911 | . 0039660 |
| . 04 | . I88 8442 | I54.470 OI5 | . 0064737 | . 54 | . 4059914 | 254.677999 | . 0039265 |
| 5.05 | 2.1931871 | 156.022464 | 0.0064093 | $5 \cdot 55$ | 2.4103344 | 257.237556 | 0.0038875 |
| . 06 | . 1975301 | 157.590516 | . 0063456 | . 56 | .414 6773 | 259.822836 | . 0038488 |
| . 07 | . 2018730 | 159.174327 | . 0062824 | . 57 | . 4190203 | 262.434099 | . 003 8105 |
| . 08 | . 2062160 | 160.774056 | .0062199 | . 58 | .4233632 | 265.071606 | $.0037726$ |
| . 09 | . 2105589 | 162.389862 | . 0061580 | - 59 | . 4277062 | 267.735620 | . 0037350 |
| 5.10 | 2.2149019 | 164.021907 | 0.0060967 | 5.60 | 2.432 0491 | 270.426407 | 0.0036979 |
| . II | .2192448 | 165.670355 | . 0060361 | .6I | . 4363920 | 273.144 238 | . 0036611 |
| . 12 | .2235877 | 167.335369 | . 0059760 | . 62 | . 4407350 | 275.889383 | . 0036246 |
| . 13 | . 2279307 | 169.017118 | .0059166 | . 63 | . 4450779 | 278.662 II7 | . 0035886 |
| . 14 | . 2322736 | 170.715 768 | . 0058577 | . 64 | . 4494209 | 281.462 718 | . 0035529 |
| 5.15 | 2.2366166 | 172.431490 | 0.0057994 | 5.65 | 2.4537638 | 284.291 466 | 0.003 5175 |
| . 16 | . 2409595 | I74.164 455 | .0057417 | . 66 | . 4581068 | 287.148 642 | . 0034825 |
| . 17 | . 2453025 | 175.914837 | . 0056846 | .67 | . 4624497 | 290.034534 | . 0034479 |
| . 18 | . 2496454 | 177.6828 II | .0056280 | . 68 | . 4667927 | 292.949430 | . 0034136 |
| . 19 | . 2539884 | 179.468553 | . 0055720 | . 69 | . 47 I I356 | 295.893620 | . 0033796 |
| 5.20 | 2.2583313 | 181.272 242 | 0.0055166 | 5.70 | 2.4754785 | 298.867401 | 0.0033460 |
| . 21 | . 2626743 | 183.094058 | . 0054617 | . 71 | . 4798215 | 301.871068 | . 003 3127 |
| . 22 | . 267 OI72 | 184.934 I84 | .0054073 | . 72 | . 4841644 | 304.904923 | $.0032797$ |
| .23 | . 2713601 | 186.792804 | . 0053535 | . 73 | . 4885074 | 307.969268 | $.0032471$ |
| . 24 | . 275703 I | 188.670103 | . 0053003 | . 74 | . 4928503 | 3II.064 4II | . 0032148 |
| 5.25 | 2.2800460 | 190.566269 | 0.0052475 | 5.75 | 2.4971933 | 314.190 660 | 0.0031828 |
| . 26 | .2843890 | I92.48I 491 | . 0051953 | . 76 | . 5015362 | 317.348329 | . 0031511 |
| . 27 | . 2887319 | 194.415963 | . 0051436 | 77 | . 5058792 | 320.537733 | $.003 \text { I } 198$ |
| . 28 | . 2930749 | 196.369875 | . 0050924 | . 78 | . 5102221 | 323.759 I90 | $.0030887$ |
| .29 | . 297 4178 | 198.343426 | .0050418 | . 79 | . 5145651 | 327.013024 | . 0030580 |
| $5 \cdot 30$ | 2.3017608 | 200.336 810 | 0.0049916 | 5.80 | 2.5189080 | 330.299560 | 0.0030276 |
| . 3 I | . 3061037 | 202.350228 | . 0049419 | . 81 | . 5232509 | 333.619 I26 | . 0029974 |
| . 32 | -310 4466 | 204.383 882 | .0048928 | . 82 | . 5275939 | 336.972054 | $.0029676$ |
| - 33 | - 3147896 | 206.437974 | . 0048441 | . 83 | -531 9368 | 340.358679 | . 0029381 |
| . 34 | . 3191325 | 208.512710 | . 0047959 | . 84 | . 5362798 | 343.779341 | . 0029088 |
| $5 \cdot 35$. | 2.3234755 | 210.608 298 | 0.0047482 | 5.85 | 2.5406227 | 347.23438 I | 0.0028799 |
| . 36 | . 3278184 | 212.724946 | . 0047009 | . 86 | . 5449657 | 350.724144 | . 0028512 |
| . 37 | . 3321614 | 214.862868 | . 0046541 | . 87 | - 5493086 | 354.248980 | $.0028229$ |
| . 38 | . 3365043 | $217.022275$ | . 0046078 | . 88 | - 5536516 | 357.809242 | . 0027948 |
| - 39 | - 3408473 | 219.203386 | . 0045620 | . 89 | - 5579945 | 361.405284 | . 0027670 |
| 5.40 | 2.3451902 | 22I.406 416 | 0.0045166 | 5.90 | 2.5623374 | 365.037468 | 0.0027394 |
| . 41 | . 3495331 | 223.631588 | . 0044716 | . 91 | . 5666804 | 368.706 I56 | . 0027122 |
| . 42 | . 3538761 | 225.879122 | . 0044271 | . 92 | . 5710233 | 372.411714 | $.0026852$ |
| . 43 | . 3582190 | 228. 149245 | . 0043831 | . 93 | . 5753663 | 376.154 514 | . 0026585 |
| . 44 | . 3625620 | $230.442 \quad 183$ | . 0043395 | . 94 | . 5797092 | 379.934930 | . 0026320 |
| 5.45 | 2.3669049 | 232.758166 | 0.0042963 | 5.95 | 2.5840522 | 383.753339 | 0.0026058 |
| . 46 | . 3712479 | 235.097424 | . 0042536 | .96 | . 588 395I | 387.610124 | . 0025799 |
| . 47 | - 3755908 | 237.460193 | . 0042112 | . 97 | . 592 7381 | 391.505 671 | $.0025542$ |
| . 48 | - 3799338 | $239.846707$ | $.0041693$ | $\text { . } 98$ | $.5970810$ | $395.440 \quad 368$ | $.0025288$ |
| . 49 | . 3842767 | 242.257207 | . 0041278 | . 99 | . 6014239 | 399.414610 | . 0025037 |
| $5 \cdot 50$ | 2.3886197 | 244.691932 | 0.0040868 | 6.00 | 2.6057669 | 403.428793 | 0.0024788 |
| $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(e^{u}\right)$ | $e^{\text {u }}$ | $e^{-u}$ | $\log _{\mathrm{e}}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | $e^{\text {u }}$ | $\mathrm{e}^{-}$ |

The Exponential.

| $u$ | $\log _{10}\left(e^{u}\right)$ | $\mathrm{e}^{\mathbf{u}}$ |  |  | $e^{-u}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | . 43429 44819 | 2.71828 | 183 |  |  | 0.36787944 I |
| 2 | . 8585889638 | 7.38905 | 610 |  |  | 0.135 335283 |
| 3 | I. 3028834457 | 20.0855 | 369 |  | (I) | 497870684 |
| 4 | 1.7371779276 | 54.598 I | 500 |  | ( I) | 183156389 |
| 5 | 2.1714724095 | I48. 413 | I59 |  | (2) | 673794700 |
| 6 | 2.6057668914 | 403. 428 | 793 |  | (2) | 247875218 |
| 7 | 3.0400613733 | $109,6.63$ | 316 |  | (3) | 911 88ı 966 |
| 8 | 3.4743558552 | $298{ }^{\prime \prime} 0.95$ | 799 |  | (3) | 335462628 |
| 9 | 3.9086503371 | $810 \quad 3.08$ | 393 |  | (3) | 123409804 |
| 10 | 4.3429448190 | 22026.4 | 658 |  | (4) | 453999298 |
| II | 4.7772393009 | 598 74.I | 417 |  | (4) | 167017008 |
| 12 | 5.2115337828 | 162754. | 791 |  | (5) | 614421235 |
| 13 | 5.6458282647 | 442 413. | 392 |  | (5) | 226032941 |
| 14 | 6.0801227466 | 120260 | 4.28 |  | (6) | 831528719 |
| 15 | 6.5144 I 72285 | 326 90I | 7.37 |  | (6) | 30590232 I |
| 16 | 6.9487117105 | 888 6II | 0.52 |  | (6) | I12 535175 |
| 17 | 7.3830061924 | 241549 | 52.8 |  | (7) | 413993772 |
| 18 | 7.8173006743 | 656599 | 69.1 |  | (7) | 152299797 |
| 19 | 8.2515951562 | 178482 | 301. |  | (8) | 560279644 |
| 20 | 8.68588 9638I | $485 \quad 165$ | 195. |  | (8) | 206 II5 362 |
| 2 I | 9.1201841200 | I3I 88I | 573 | [ I] | (9) | 758256043 |
| 22 | 9.5544786019 | 358 491 | 285 | [ I$]$ | (9) | 278946809 |
| 23 | 9.9887730838 | 974480 | 345 | [I] | (9) | 102618796 |
| 24 | 10.4230675657 | 264891 | 22 I | [2] | ( IO) | 377513454 |
| 25 | 10.8573620475 | 720048 | 993 | [2] | ( IO) | 138879439 |
| 26 | 11.29165 65295 | 195729 | 609 | [3] | (II) | 510908903 |
| 27 | II. 7259510114 | 532048 | 241 | [3] | (II) | 187952882 |
| 28 | 12.16024 54933 | 144625 | 707 | [4] | (12) | 691440 OII |
| 29 | 12.59453 99752 | $393 \quad 133$ | 430 | [4] | (12) | 254366565 |
| 30 | I3.02883 44571 | 106864 | 746 | [5] | (I3) | 935762297 |
| 3 I | 13.46312 89390 | 290488 | 497 | [5] | (13) | 344247711 |
| 32 | 13.89742 34209 | 789629 | 602 | [5] | (13) | 126641656 |
| 33 | 14.33171 79028 | 214643 | 580 | [6] | (I4) | 465888 6I5 |
| 34 | 14.76601 23847 | 58346 I | 743 | [6] | (I4) | I7I 390843 |
| 35 | 15.2003068666 | 158 601 | 345 | [7] | (15) | 630511676 |
| 36 | 15.6346013485 | 43 I I23 | 155 | [7] | (15) | 231952283 |
| 37 | 16.0688958304 | 117191 | 424 | [8] | ( I6) | 853304763 |
| 38 | 16.5031903123 | 318559 | 318 | [8] | (16) | 3I3 913 279 |
| 39 | 16.93748 47942 | 865934 | 004 | [8] | (16) | 115482242 |
| 40 | 17.3717792761 | $235 \quad 385$ | 267 | [9] | (17) | 424835426 |
| 4 I | 17.8060737580 | 639843 | 493 | [9] | (17) | 156288219 |
| 42 | 18.2403682399 | 173927 | 494 | [10] | (18) | 574952227 |
| 43 | 18.6746627218 | 472783 | $9-47$ | [10] | (18) | 2 II 513104 |
| 44 | 19.10895 72037 | 128516 | 001 | [II] | (19) | 778 113 22.1 |
| 45 | 19.5432516856 | 349342 | 7 II | [II] | (19) | 286 251 858 |
| 46 | 19.9775461675 | 949 6II | 942 | [II] | (19) | 105306174 |
| 47 | 20.4118405495 | 258 I3I | 289 | [12] | (20) | 387399763 |
| 48 | 20.8461351314 | 701673 | 591 | [12] | (20) | 142516408 |
| 49 | 21.2804296133 | 190734 | 657 | [13] | (2I) | 524288566 |
| 50 | 21.71472 40952 | 518470 | 553 | [13] | (2I) | 192874985 |

The numbers in square brackets denote the numbers of figures between the last figure given and the decimal point; for example, the first nine figures of ${ }^{50}$ are 518470553 , and there are 13 additional figures before the decimal point is reached. The numbers in parentheses denote the numbers of ciphers between the decimal point and the first significant figure; for example, in $\mathrm{e}^{-50}$ there are 2I ciphers between the decimal point and the figures 192874985.

The Exponential.

| u | $\log _{10}\left(\mathrm{e}^{\mathrm{u}}\right)$ | eu | $\mathrm{e}-\mathrm{u}$ |
| :---: | :---: | :---: | :---: |
| 51 | 22.14901 85771 | 140934 908 [14] | (22) 709547416 |
| 52 | 22.5833130590 | 383 100 800 [14] | (22) 261027907 |
| 53 | 23.0170075409 | 10+ $137594[15]$ | (23) 960268005 |
| 54 | 23.4519020228 | 283075330 [15] | (23) 353262857 |
| 55 | 23.8861965047 | 769478527 [15] | (23) 129958143 |
| 56 | 24.3204909866 | 209165950 [16] | (24) 478089288 |
| 57 | 24.7547854685 | 568572000 [16] | (24) 175879220 |
| 58 | 25.18907 99504 | 154553894 [17] | (25) 647023493 |
| 59 60 | 25.6233744323 | 420121040 [17] | (25) 238026641 <br> (26) <br> 875 <br> 751076 |
| 60 | 26.0576689142 26.4919633961 | 114 200 739 <br> 310 429 794 <br> 18$]$   <br> 18$]$   | $\begin{array}{lllll}\text { (26) } & 875 & 651 & 076 \\ \text { (26) } & 322 & 134 & 029\end{array}$ |
| 62 | 26.9262578780 | 843835667 [18] | (26) 118506487 |
| 63 | 27.3605523599 | 229378316 [19] | (27) 435961000 |
| 64 | 27.79484 68418 | 623514908 [19] | (27) 160 381 089 |
| 65 | 28.2291413237 | 169488924 [20] | (28) 590009054 |
| 66 | 28.6634358056 | 460718663 [20] | (28) 217052201 |
| 67 | 29.0977302875 | 125236317 [21] | (29) 798490425 |
| 68 | 29.5320247694 | 340427605 [21] | (29) 293748211 |
| 69 | 29.9663192513 | 925378 172 [21] | (29) 108063928 |
| 70 | 30.4006137332 | 251543857 [22] | (30) 397544974 |
| 71 | 30.8349082151 | 683767123 [22] | (30) 146248623 |
| 72 | 31.2692026970 | 185867175 [23] | (31) 538018616 |
| 73 | 31.70349 71789 | 505239363 [23] | (31) 197925988 |
| 74 | 32.13779 16608 | 137338298 [24] | (32) 728129018 |
| 75 76 | 32.5720861427 | $\begin{array}{llll}373 & 324 & 200 \\ \text { IOI } & 480 & 030\end{array}$ | (32) 267853696 (33) 085415469 |
| 76 77 | 33.0063806246 33.44067 51066 |  | (33) <br> (33) <br> 965 <br> 362 <br> 51514 <br> 1509 |
| 77 | 33.4406751066 33.8749695885 | 275851 749841 746 700 | $\begin{array}{lllll}\text { (33) } & 362 & 514 & 092 \\ \text { (33) } & 133 & 361 & 482\end{array}$ |
| 79 | 34.3092640704 | 203828 107 [26] | (34) 490609473 |
| 80 | 34.7435585523 | 554062238 [26] | (34) 180485139 |
| 81 | 35.1778530342 | 150609 731 [27] | (35) 663967720 |
| 82 | 35.61214 .75161 | 409399696 [27] | (35) 244260074 |
| 83 | 36.04644 19980 | III 286 376 [28] | (36) 898582594 |
| 84 | 36.4807364799 | 302507732 [28] | (36) 330570063 |
| 85 | 36.9150309618 | 822301271 [28] | (36) 121 609930 |
| 86 | 37.3493254437 | 223524660 [29] | (37) 447377931 |
| 87 | 37.7836199256 | 607603023 [29] | (37) 164581143 |
| 88 | 38.2179144075 | 165163626 [30] | (38) 605460189 |
| 89 | 38.6522088894 | 448961282 [30] | (38) 222736356 |
| 90 | 39.0865033713 | 122040329 [31] | (39) 819401262 |
| 91 | 39.5207978532 | 331740 о10 [31] | (39) 301 440879 |
| 92 | 39.9550923351 | 901762841 [31] |  |
| 93 | 40.3893868170 | $\begin{array}{llll}245 & 124 & 554 & {[32]} \\ 666617 & 322\end{array}$ | (40) <br> (40) <br> 407 <br> 150 <br> 15058 <br> 078 <br> 156 |
| 94 | 40.8236812989 41.2579757808 | $\begin{array}{lllll}606 & 317 & 622 & {[32]} \\ 181 & 123 & 908 & {[33]}\end{array}$ | $\begin{array}{lllll}\text { (40) } & 150 & 078 & 576 \\ \text { (41) } & 552 & 108 & 228\end{array}$ |
| 96 | 41.6922702627 | 492345829 [33] | (4I) 203109266 |
| 97 | 42.1265647446 | 133833472 [34] | (42) 747197234 |
| 98 | 42.5608592265 | $363797095[34]$ | (42) 274878501 |
| 99 | 42.9951537084 | 988903032 [34] | (42) 101122149 |
| 100 | 43.42944 81903 | 268 811 714 [35] | (43) 372007598 |

The numbers in square brackets denote the numbers of figures between the last figure given and the decimal point; for example, the first nine figures of $\mathrm{e}^{\text {so }}$ are 518470553 , and there are 13 additional figures before the decimal point is reached. The numbers in parentheses denote the numbers of ciphers between the decimal point and the first significant figure; for example, in $\mathrm{e}^{-50}$ there are 2I. ciphers between the decimal point and the figures 192874985.
( $\mathrm{p}=\mathrm{n} \times 43429448 \mathrm{I} 9$. . .)

| $n$ | p | n | p | n | D | n | p | n | p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 000 | 0.050 | 2171 | 0.100 | 4343 | 0.150 | 6514 | 0.200 | 8686 |
| .001 | 043 | .05I | 2215 | . IOI | 4386 | . 151 | 6558 | . 201 | 8729 |
| . 002 | 087 | . 052 | 2258 | . 102 | 4430 | . 152 | 6601 | . 202 | 8773 |
| . 003 | 130 | . 053 | 2302 | . 103 | 4473 | . 153 | 6645 | . 203 | 8816 |
| . 004 | 174 | . 054 | 2345 | . 104 | 4517 | . 154 | 6688 | . 204 | 8860 |
| 0.005 | 217 | 0.055 | 2389 | 0.105 | 4560 | 0.155 | 6732 | 0.205 | 8903 |
| . 006 | 26 I | . 056 | 2432 | . 106 | 4604 | . 156 | 6775 | . 206 | 8946 |
| . 007 | 304 | . 057 | 2475 | . 107 | 4647 | . 157 | 6818 | . 207 | 8990 |
| . 008 | 347 | . 058 | 2519 | . 108 | 4690 | . 158 | 6862 | . 208 | 9033 |
| . 009 | 39 I | . 059 | 2562 | . 109 | 4734 | . 159 | 6905 | . 209 | 9077 |
| 0.010 | 434 | 0.060 | 2606 | 0.110 | 4777 | 0.160 | 6949 | 0.210 | 9120 |
| . 017 | 478 | .06I | 2649 | . III | 4821 | . I6I | 6992 | . 211 | 9164 |
| . 012 | 521 | . 062 | 2693 | . 112 | 4864 | . 162 | 7036 | . 212 | 9207 |
| . 013 | 565 | . 063 | 2736 | . II3 | 4908 | . 163 | 7079 | . 213 | 9250 |
| . 014 | 608 | . 064 | 2779 | . II4 | 495 I | . 164 | 7122 | . 214 | 9294 |
| 0.015 | 651 | 0.065 | 2823 | O.II5 | 4994 | 0.165 | 7166 | 0.215 | 9337 |
| . 016 | 695 | . 066 | 2866 | . 116 | 5038 | . 166 | 7209 | . 216 | 938I |
| . 017 | 738 | . 067 | 2910 | .117 | 508 I | . 167 | 7253 | . 217 | 9424 |
| . 018 | 782 | . 068 | 2953 | . 118 | 5125 | . 168 | 7296 | . 218 | 9468 |
| . 019 | 825 | . 069 | 2997 | . 119 | 5168 | . I69 | 7340 | . 219 | 9511 |
| 0.020 | 869 | 0.070 | 3040 | 0.120 | 5212 | 0.170 | 7383 | 0.220 | 9554 |
| . 021 | 912 | . 071 | 3083 | . 12 I | 5255 | . I7I | 7426 | . 22 I | 9598 |
| . 022 | 955 | . 072 | 3127 | . 122 | 5298 | . 172 | 7470 | . 222 | 9641 |
| . 023 | 999 | . 073 | 3170 | . I23 | 5342 | . 173 | 7513 | . 223 | 9685 |
| . 024 | 1042 | . 074 | 32 I 4 | . 124 | 5385 | . 174 | 7557 | . 224 | 9728 |
| 0.025 | 1086 | 0.075 | 3257 | 0.125 | 5429 | 0.175 | 7600 | 0.225 | 9772 |
| . 026 | 1129 | . 076 | 3301 | . 126 | 5472 | . 176 | 7644 | . 226 | 9815 |
| . 027 | 1173 | . 077 | 3344 | . 127 | 5516 | . 177 | 7687 | . 227 | 9858 |
| . 028 | 1216 | . 078 | 3387 | . 128 | 5559 | . 178 | 7730 | . 228 | 9902 |
| . 029 | 1259 | . 079 | 343 I | . 129 | 5602 | . 179 | 7774 | . 229 | 9945 |
| 0.030 | 1303 | 0.080 | 3474 | 0.130 | ${ }^{5} 546$ | 0.180 | 7817 | 0.230 | 9989 |
| . 031 | I346 | .08I | 3518 | . I3I | 5689 | . 18 I | 786I | . 23 I | 10032 |
| . 032 | I 390 | . 082 | 3561 | . I32 | 5733 | . 182 | 7904 | . 232 | 10076 |
| . 033 | I 433 | . 083 | 3605 | . I33 | 5776 | .183 | 7948 | . 233 | IOII9 |
| . 034 | 1477 | . 084 | 3648 | . 134 | 5820 | . 184 | 7991 | . 234 | 10162 |
| 0.035 | 1520 | 0.085 | 3692 | 0.135 | 5863 | 0.185 | 8034 | 0.235 | 10206 |
| . 036 | 1563 | . 086 | 3735 | . 136 | 5906 | . 186 | 8078 | . 236 | 10249 |
| . 037 | 1607 | . 087 | 3778 | . 137 | 5950 | . 187 | 812I | . 237 | 10293 |
| . 038 | 1650 | . 088 | 3822 | . 138 | 5993 | . 188 | 8165 | . 238 | 10336 |
| . 039 | I694 | . 089 | 3865 | . I39 | 6037 | . I89 | 8208 | . 239 | 10380 |
| 0.040 | 1737 | 0.090 | 3909 | 0.140 | 6080 | 0.190 | 8252 | 0.240 | 10423 |
| .041 | 1781 | .09I | 3952 | . I4I | 6124 | . 191 | 8295 | . 241 | 10466 |
| . 042 | 1824 | . 092 | 3996 | . I42 | 6167 | . 192 | 8338 | . 242 | 10510 |
| . 043 | 1867 | . 093 | 4039 | . I43 | 6210 | . 193 | 8382 | . 243 | 10553 |
| . 044 | I9II | . 094 | 4082 | . 144 | 6254 | . 194 | 8425 | . 244 | 10597 |
|  |  | 0.095 | 4126 | 0.145 | 6297 | 0.195 | 8469 |  |  |
| . 046 | 1998 | . 096 | 2169 | . 146 | 6341 | . 196 | 8512 | . 246 | 10684 |
| . 047 | 2041 | . 097 | 4213 | . 147 | 6384 | . 197 | 8556 | . 247 | 10727 |
| . 048 | 2085 | . 098 | 4256 | . 148 | 6428 | . 198 | 8599 | . 248 | 10771 |
| . 049 | 2128 | . 099 | 4300 | . 149 | 647 I | . 199 | 8642 | . 249 | 108I4 |
| 0.050 | 2171 | 0.100 | 4343 | 0.150 | 6514 | 0.200 | 8686 | 0.250 | 10857 |
| $n$ | p | n | D | n | D | n | p | n | D |

( $\mathrm{p}=\mathrm{n} \times 43429$ 44819 . . .)

| n | p | n | p | n | p | $n$ | D | n | p |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.250 | 10857 | 0.300 | I3029 | 0.350 | 15200 | 0.400 | 17372 | 0.450 | 19543 |
| .25I | 10901 | . 301 | 13072 | .35I | I5244 | . 401 | 17415 | .45I | 19587 |
| . 252 | 10944 | . 302 | 13116 | - 352 | 15287 | . 402 | 17459 | . 452 | 19630 |
| . 253 | 10988 | . 303 | 13159 | . 353 | 1533 I | . 403 | 17502 | . 453 | 19674 |
| . 254 | I IO3I | . 304 | 13203 | - 354 | 15374 | . 404 | I7545 | . 454 | 19717 |
| 0.255 | 11075 | 0.305 | 13246 | 0.355 | 15417 | 0.405 | I7589 | 0.455 | 19760 |
| . 256 | IIII8 | . 306 | I 3289 | . 356 | I5461 | . 406 | 17632 | . 456 | 19804 |
| . 257 | I I I6I | . 307 | 13333 | - 357 | I5504 | . 407 | 17676 | . 457 | 19847 |
| . 258 | I I 205 | . 308 | 13376 | - 358 | 15548 | . 408 | 17719 | . 458 | I9891 |
| . 259 | I I248 | . 309 | 13420 | . 359 | 15591 | . 409 | 17763 | -459 | 19934 |
| 0.260 | II292 | 0.310 | 13463 | 0.360 | 15635 | 0.410 | 17806 | 0.460 | 19978 |
| .26I | II335 | .3II | 13507 | . 361 | 15678 | .41I | 17850 | . 461 | 20021 |
| .262 | 11379 | -312 | 13550 | . 362 | 15721 | . 412 | 17893 | . 462 | 20064 |
| . 263 | 11422 | . 313 | 13593 | . 363 | I.5765 | . 413 | 17936 | . 463 | 20108 |
| . 264 | II465 | . 314 | 13637 | . 364 | 15808 | . 414 | 17980 | . 464 | 20151 |
| 0.265 | II509 | 0.315 | 13680 | 0.365 | 15852 | 0.415 | 18023 | 0.465 | $20195$ |
| . 266 | II 552 | . 316 | 13724 | . 366 | I 5895 | . 416 | 18067 | . 466 | $20238$ |
| . 267 | I 1596 | . 317 | 13767 | . 367 | 15939 | . 417 | 181 10 | . 467 | 20282 |
| . 268 | I I639 | . 318 | I38II | - 368 | 15982 | . 418 | I8I54 | . 468 | 20325 |
| . 269 | 11683 | . 319 | I 3854 | -369 | 16025 | . 419 | 18197 | . 469 | 20368 |
| 0.270 | 11726 | 0.320 | 13897 | 0.370 | 16069 | 0.420 | 18240 | 0.470 | 20412 |
| . 271 | 11769 | . 321 | I3941 | . 371 | 16II2 | . 42 I | 18284 | . 471 | 20455 |
| . 272 | I1813 | . 322 | 13984 | . 372 | 16156 | . 422 | 18327 | . 472 | 20499 |
| . 273 | II856 | . 323 | 14028 | . 373 | 16199 | .423 | 18371 | . 473 | 20542 |
| . 274 | 11900 | - 324 | 14071 | . 374 | 16243 | . 424 | 184I4 | . 474 | 20586 |
| 0.275 | 11943 | 0.325 | 14115 | 0.375 | 16286 | 0.425 | I84:58 | 0.475 | 20629 |
| . 276 | 11987 | . 326 | 14158 | . 376 | 16329 | . 426 | 18501 | . 476 | 20672 |
| . 277 | 12030 | . 327 | 14201 | . 377 | 16373 | . 427 | 18544 | . 477 | 20716 |
| .278 | 12073 | - 328 | I 4245 | - 378 | 16416 | . 428 | 18588 | . 478 | $20759$ |
| .279 | I2II7 | . 329 | I4288 | . 379 | 16460 | . 429 | 1863I | . 479 | 20803 |
| 0.280 | 12160 | 0.330 | 14332 | 0.380 | 16503 | 0.430 | I8675 | 0.480 | 20846 |
| .28I | 12204 | . 33 I | I 43375 | . 38 I | 16547 | .431 | 18718 | . 48 I | $20890$ |
| . 282 | 12247 | - 332 | 14419 | . 382 | 16590 | . 432 | 18762 | . 482 | 20933 |
| . 283 | 12291 | - 333 | 14462 | . 383 | 16633 | . 433 | 18805 | . 483 | $20976$ |
| . 284 | 12334 | . 334 | 14505 | -384 | 16677 | . 434 | 18848 | . 484 | 21020 |
| 0.285 | 12377 | 0.335 | 14549 | 0.385 | 16720 | 0.435 | 18892 | 0.485 | 21063 |
| . 286 | 12421 | . 336 | 14592 | . 386 | 16764 | . 436 | 18935 | . 486 | 21107 |
| . 287 | 12464 | . 337 | 14636 | . 387 | 16807 | . 437 | 18979 | .487 | 21150 |
| . 288 | 12508 | . 338 | 14679 | . 388 | 16851 | . 438 | 19022 | . 488 | 21194 |
| . 289 | 12551 | . 339 | I. 4723 | . 389 | 16894 | . 439 | 19066 | . 489 | 21237 |
| 0.290 | 12595 | 0.340 | 14766 | 0.390 | 16937 | 0.440 | 19109 | 0.490 | 21280 |
| . 291 | 12638 | . 341 | 14809 | . 391 | 16981 | . 44 I | 19152 | . 49 I | 21324 |
| . 292 | 1268 I | - 342 | 14853 | . 392 | 17024 | . 442 | 19196 | . 493 | 21367 |
| . 293 | 12725 | . 343 | I4896 | - 393 | I 7068 | . 443 | 19239 | . 493 | 214II |
| . 294 | 12768 | - 344 | I4940 | -394 | I7III | . 444 | 19283 | . 494 | 21454 |
| 0.295 | 12812 | 0.345 | 14983 | 0.395 | 17155 | 0.445 | 19326 | 0.495 | 21498 |
| . 296 | I2855 | . 346 | 15027 | . 396 | I7198 | . 446 | 19370 | . 496 | 21541 |
| . 297 | 12899 | -347 | 15070 | - 397 | 17241 | . 447 | 19413 | . 497 | 21584 |
| . 298 | 12942 | -348 | 15113 | - 398 | 17285 | . 448 | 19456 | . 498 | 21628 |
| . 299 | 12985 | - 349 | 15I'57 | -399 | 17328 | . 449 | 19500 | . 499 | 21671 |
| 0.300 | 13029 | 0.350 | 15200 | 0.400 | 17372 | 0.450 | 19543 | 0.500 | 21715 |
| n | p | n | D | $n$ | p | n | p | n | p |

## TABLE V

## NATURAL LOGARITHMS

Note. -In Table V, for $u$ greater than 158 , linear interpolation of $\log _{e} u$ suffices to give a value whose error is not greater than one unit in the last place.

Natural Logarithms.

| u | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega F_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega F_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega \mathbf{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | - - | $\infty$ | 50 | 3.91202 | 2000 | 100 | 4.60517 | 1000 | 150 | 5.01064 | 667 |
| 1 | 0.00000 | 100000 | 51 | 3.93183 | 1961 | 101 | 4.61512 | 990 | 151 | 5.01728 | 662 |
| 2 | 0.69315 | 50000 | 52 | 3.95124 | 1923 | IO2 | 4.62497 | 980 | 152 | 5.02388 | 658 |
| 3 | 1.09861 | 33333 | 53 | 3.97029 | 1887 | 103 | 4.63473 | 971 | 153 | 5.03044 | 654 |
| 4 | 1. 38629 | 25000 | 54 | 3.98898 | 1852 | 104 | 4.64439 | 962 | 154 | 5.03695 | 649 |
| $5$ | I. 60944 | 20000 | 55 | 4.00733 | 1818 | 105 | 4.65396 | 952 | 155 | 5.04343 | 645 |
| $6$ | 1.79176 | 16667 | 56 | 4.02535 | I786 | 106 | 4.66344 | 943 | I56 | 5.04986 | 641 |
| 7 | 1.94591 | 14286 | 57 | 4.04305 | I754 | 107 | 4.67283 | 935 | 157 | 5.05625 | 637 |
| 8 | 2.07944 | 12500 | 58 | 4.06044 | I724 | 108 | 4.68213 | 926 | I58 | 5.06260 | 633 |
| 9 | 2.19722 | IIIII | 59 | 4.07754 | 1695 | 109 | 4.69135 | 917 | 159 | 5.06890 | 629 |
| 10 | 2.30259 | 10000 | 60 | 4.09434 | 1667 | 110 | 4.70048 | 909 | 160 | 5.07517 | 625 |
| II | 2.39790 | 9091 | 61 | 4.11087 | 1639 | III | 4.70953 | 901 | 161 | 5.08 I 40 | 621 |
| 12 | 2.48491 | 8333 | 62 | 4.12713 | 1613 | II2 | 4.71850 | 893 | 162 | 5.08760 | 617 |
| 13 | 2.56495 | 7692 | 63 | 4.14313 | 1587 | 113 | 4.72739 | 885 | 163 | 5.09375 | 613 |
| 14 | 2.63906 | 7143 | 64 | 4. 15888 | 1562 | II4 | 4.73620 | 877 | 164 | 5.09987 | 610 |
| 15 | 2.70805 | 6667 | 65 | 4. 17439 | 1538 | 115 | 4.74493 | 870 | 165 | 5. 10595 | 606 |
| 16 | 2.77259 | 6250 | 66 | 4. 18965 | 1515 | 116 | 4.75359 | 862 | 166 | 5.11199 | 602 |
| 17 | 2.83321 | 5882 | 67 | 4.20469 | 1493 | 117 | 4.76217 | 855 | 167 | 5.11799 | 599 |
| 18 | 2.89037 | 5556 | 68 | 4.2195 I | 1471 | II8 | 4.77068 | 847 | 168 | 5.12396 | 595 |
| 19 | 2.94444 | 5263 | 69 | 4.234 II | 1449 | 119 | 4.77912 | 840 | 169 | 5.12990 | 592 |
| 20 | 2.99573 | 5000 | 70 | 4.24850 | 1429 | 120 | 4.78749 | 833 | I70 | 5.13580 | 588 |
| 21 | 3.04452 | 4762 | 71 | 4.26268 | 1408 | 12I | 4.79579 | 826 | 171 | 5.14166 | 585 |
| 22 | 3.09104 | 4545 | 72 | 4.27667 | I389 | 122 | 4.80402 | 820 | 172 | 5.14749 | 58 I |
| 23 | 3.13549 | 4348 | 73 | 4.29046 | 1370 | 123 | 4.8 I 218 | 813 | 173 | 5.15329 | 578 |
| 24 | 3.17805 | 4167 | 74 | $4 \cdot 30407$ | 1351 | 124 | 4.82028 | 806 | 174 | 5.15906 | 575 |
| 25 | 3.21888 | 4000 | 75 | $4 \cdot 31749$ | I333 | 125 | 4.82831 | 800 | 175 | 5.16479 | 571 |
| 26 | 3.25810 | 3846 | 76 | 4.33073 | 1316 | 126 | 4.83628 | 794 | 176 | 5.17048 | 568 |
| 27 | 3.29584 | 3704 | 77 | $4 \cdot 34381$ | 1299 | 127 | 4.84419 | 787 | 177 | 5.17615 | 565 |
| 28 | 3.33220 | 3571 | 78 | $4 \cdot 35671$ | 1282 | 128 | 4.85203 | 78 I | 178 | 5.18178 | 562 |
| 29 | $3 \cdot 36730$ | 3448 | 79 | $4 \cdot 36945$ | 1266 | 129 | 4.8598 I | 775 | I79 | 5.18739 | 559 |
| 30 | 3.40120 | 3333 | 80 | 4.38203 | 1250 | 130 | 4.86753 | 769 | 180 | 5.19296 | 556 |
| 31 | 3.43399 | 3226 | 81 | $4 \cdot 39445$ | 1235 | I31 | 4.87520 | 763 | 181 | 5.19850 | 552 |
| 32 | 3.46574 | 3125 | 82 | 4.40672 | 1220 | 132 | 4.88280 | 758 | 182 | 5.20401 | 549 |
| 33 | 3.49651 | 3030 | 83 | 4.41884 | 1205 | 133 | 4.89035 | 752 | 183 | 5.20949 | 546 |
| 34 | $3 \cdot 52636$ | 2941 | 84 | 4.43082 | 1190 | 134 | 4.89784 | 746 | 184 | 5.21494 | 543 |
| 35 | 3.55535 | 2857 | 85 | 4.44265 | 1176 | 135 | 4.90527 | 741 | 185 | 5.22036 | 54 I |
| 36 | 3.58352 | 2778 | 86 | 4.45435 | I 163 | 136 | 4.91265 | 735 | 186 | 5.22575 | 5.38 |
| 37 | 3.61092 | 2703 | 87 | 4.46591 | 1149 | 137 | 4.91998 | 730 | 187 | 5.23 III | 535 |
| 38 | 3.63759 | 2632 | 88 | 4.47734 | 1136 | 138 | 4.92725 | 725 | 188 | 5.23644 | 532 |
| 39 | 3.66356 | 2564 | 89 | 4.48864 | I124 | I39 | 4.93447 | 719 | 189 | 5.24175 | 529 |
| 40 | 3.68888 | 2500 | 90 | 4.49981 | IIII | 140 | 4.94164 | 714 | 190 | 5.24702 | 526 |
| 41 | 3.71357 | 2439 | 91 | 4.51086 | 1099 | 141 | 4.94876 | 709 | 191 | 5.25227 | 524 |
| 42 | 3.73767 | 238 I | 92 | 4.52179 | 1087 | 142 | 4.95583 | 704 | 192 | 5.25750 | 52 I |
| 43 | 3.76120 | 2326 | 93 | $4 \cdot 53260$ | 1075 | 143 | 4.96284 | 699 | 193 | 5.26269 | 518 |
| 44 | 3.78419 | 2273 | 94 | $4 \cdot 54329$ | 1064 | 144 | 4.9698I | 694 | 194 | 5.26786 | 515 |
| 45 | 3.80666 | 2222 | 95 | 4.55388 | 1053 | 145 | 4.97673 | 690 | 195 | 5.27300 | 513 |
| 46 | 3.82864 | 2174 | 96 | 4.56435 | 1042 | 146 | 4.98361 | 685 | 196 | 5.27811 | 510 |
| 47 | 3.85015 | 2128 | 97 | 4.57471 | 1031 | 147 | 4.99043 | 680 | 197 | 5.28320 | 508 |
| 48 | 3.87120 | 2083 | 98 | 4.58497 | 1020 | 148 | 4.9972 I | 676 | 198 | 5.28827 | 505 |
| 49 | 3.89182 | 2041 | 99 | 4.59512 | 1010 | 149 | 5.00395 | 67 I | 199 | 5.29330 | 503 |
| 50 | 3.91202 | 2000 | 100 | 4.60517 | 1000 | 150 | 5.01064 | 667 | 200 | 5.29832 | 500 |
| $e^{x}$ | x | $e^{-x}$ | $e^{x}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $e^{x}$ | x | $e^{-x}$ |

Smithsonian Tables

Natural Logarithms.

| u | $\log _{\mathrm{e}} \mathrm{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 200 | 5.29832 | 500 | 250 | 5.52146 | 400 | 300 | 5.70378 | 333 | 350 | 5.85793 | 286 |
| 201 | 5.30330 | 498 | 251 | 5.52545 | 398 | 301 | 5.70711 | 332 | 351 | 5.86079 | 285 |
| 202 | $5 \cdot 30827$ | 495 | 252 | 5.52943 | 397 | 302 | 5.71043 | 331 | 352 | 5.86363 | 284 |
| 203 | $5 \cdot 31321$ | 493 | 253 | 5.53339 | 395 | 303 | 5.71373 | 330 | 353 | 5.86647 | 283 |
| 204 | 5.31812 | 490 | 254 | $5 \cdot 53733$ | 394 | 304 | 5.71703 | 329 | 354 | 5.86930 | 282 |
| 205 | 5.32301 | 488 | 255 | 5.54126 | 392 | 305 | 5.72031 | 328 | 355 | 5.87212 | 282 |
| 206 | $5 \cdot 32788$ | 485 | 256 | 5.54518 | 391 | 306 | 5.72359 | 327 | 356 | 5.87493 | 28I |
| 207 | 5.33272 | 483 | 257 | 5.54908 | 389 | 307 | 5.72685 | 326 | 357 | 5.87774 | 280 |
| 208 | 5.33754 | 48 I | 258 | 5.55296 | 388 | 308 | 5.73010 | 325 | 358 | 5.88053 | 279 |
| 209 | $5 \cdot 34233$ | 478 | 259 | $5 \cdot 55683$ | 386 | 309 | 5.73334 | 324 | 359 | 5.88332 | 279 |
| 210 | 5.347I I | 476 | 260 | 5.56068 | 385 | 310 | 5.73657 | 323 | 360 | 5.88610 | 278 |
| 211 | 5.35186 | 474 | 261 | $5 \cdot 56452$ | 38.3 | 311 | 5.73979 | 322 | 36 I | 5.88888 | 277 |
| 212 | $5 \cdot 35659$ | 472 | 262 | 5.56834 | 382 | 312 | 5.74300 | 32 I | 362 | 5.89164 | 276 |
| 213 | 5.36129 | 469 | 263 | 5.57215 | 380 | 313 | 5.74620 | 319 | 363 | 5.89440 | 275 |
| 214 | $5 \cdot 36598$ | 467 | 264 | $5 \cdot 57595$ | 379 | 314 | 5.74939 | 318 | 364 | 5.897 I 5 | 275 |
| 215 | $5 \cdot 37064$ | 465 | 265 | $5 \cdot 57973$ | 377 | 315 | 5.75257 | 317 | 365 | 5.89990 | 274 |
| 216 | $5 \cdot 37528$ | 463 | 266 | 5.58350 | 376 | 316 | 5.75574 | 316 | 366 | 5.90253 | 273 |
| 217 | 5:37990 | 461 | 267 | 5.58725 | 375 | 317 | 5.75890 | 315 | 367 | 5.90536 | 272 |
| 218 | $5 \cdot 38450$ | 459 | 268 | 5.59099 | 373 | 318 | 5.76205 | 314 | 368 | 5.90808 | 272 |
| 219 | $5 \cdot 38907$ | 457 | 269 | 5.59471 | 372 | 319 | 5.76519 | 313 | 369 | 5.91080 | 271 |
| 220 | $5 \cdot 39363$ | 455 | 270 | 5.59842 | 370 | 320 | 5.76832 | 312 | 370 | 5.91350 | 270 |
| 221 | 5.39816 | 452 | 271 | 5.60212 | 369 | 321 | 5.77144 | 312 | 371 | 5.91620 | 270 |
| 222 | 5.40268 | 450 | 272 | 5.60580 | 368 | 322 | 5.77455 | 3 II | 372 | 5.91889 | 259 |
| 223 | 5.40717 | 448 | 273 | 5.60947 | 366 | 323 | 5.77765 | 310 | 373 | 5.92158 | 258 |
| 224 | 5.41165 | 446 | 274 | 5.61313 | 365 | 324 | 5.78074 | 309 | 374 | 5.92426 | 267 |
| 225 | 5.41610 | 444 | 275 | 5.61677 | 364 | 325 | 5.78383 | 308 | 375 | 5.92693 | 267 |
| 226 | 5.42053 | 442 | 276. | 5.62040 | 362 | 326 | 5.78690 | 307 | 376 | 5.92959 | 256 |
| 227 | 5.42495 | 441 | 277 | 5.62402 | 361 | 327 | 5.78996 | 306 | 377 | 5.93225 | 265 |
| 228 | 5.42935 | 439 | 278 | 5.62762 | 360 | 328 | 5.79301 | 305 | 378 | 5.93489 | 265 |
| 229 | 5.43372 | 437 | 279 | 5.63121 | 358 | 329 | 5.79606 | 304 | 379 | 5.93754 | 264 |
| 230 | 5.43808 | 435 | 280 | 5.63479 | 357 | 330 | 5.79909 | 303 | 380 | $5 \cdot 94017$ | 253 |
| 231 | 5.44242 | 433 | 281 | 5.63835 | 356 | 331 | 5.80212 | 302 | 381 | 5.94280 | 252 |
| 232 | 5.44674 | 43 I | 282 | 5.64191 | 355 | 332 | 5.80513 | 301 | 382 | 5.94542 | 262 |
| 233 | 5.45104 | 429 | 283 | 5.64545 | 353 | 333 | 5.808 I 4 | 300 | 383 | 5.94803 | 26 I |
| 234 | 5.45532 | 427 | 284 | 5.64897 | 352 | 334 | 5.8III4 | 299 | 384 | 5.95064 | 260 |
| 235 | 5.45959 | 426 | 285 | 5.65249 | 351 | 335 | 5.81413 | 299 | 385 | 5.95324 | 260 |
| 236 | 5.46383 | 424 | 286 | 5.65599 | 350 | 336 | 5.81711 | 298 | 386 | 5.95584 | 259 |
| 237 | 5.46806 | 422 | 287 | 5.65948 | 348 | 337 | 5.82008 | 297 | 387 | 5.958 .42 | 258 |
| 238 | 5.47227 | 420 | 288 | 5.66296 | 347 | 338 | 5.82305 | 296 | 388 | 5.96101 | 258 |
| 239 | 5.47646 | 418 | 289 | 5.66643 | 346 | 339 | 5.82600 | 295 | 389 | 5.96358 | 257 |
| 240 | 5.48064 | 417 | 290 | 5.66988 | 345 | 340 | 5.82895 | 294 | 390 | 5.96615 | 256 |
| 24 I | 5.48480 | 415 | 291 | 5.67332 | 344 | 341 | 5.83188 | 293 | 391 | 5.96871 | 256 |
| 242 | 5.48894 | 413 | 292 | 5.67675 | 342 | 342 | 5.8348 I | 292 | 392 | 5.97126 | 255 |
| 243 | 5.49306 | 412 | 293 | 5.68017 | 341 | 343 | 5.83773 | 292 | 393 | 5.97381 | 254 |
| 244 | 5.49717 | 410 | 294 | 5.68358 | 340 | 344 | 5.84064 | 291 | 394 | 5.97635 | 254 |
|  | 5.50126 | 408 | 295 | 5.68698 | 339 | 345 | 5.84354 | 290 | 395 | 5.97889 | 253 |
| 246 | $5 \cdot 50533$ | 407 | 296 | 5.69036 | 338 | 346 | 5.84644 | 289 | 396 | 5.98141 | 253 |
| 247 | $5 \cdot 50939$ | 405 | 297 | 5.69373 | 337 | 347 | 5.84932 | 288 | 397 | 5.98394 | 252 |
| 248 | 5.51343 | 403 | 298 | 5.69709 | 336 | 348 | 5.85220 | 287 | 398 | 5.98645 | 25 I |
| 249 | 5.51745 | 402 | 299 | $5 \cdot 70044$ | 334 | 349 | 5.85507 | 287 | 399 | 5.98896 | 25 I |
| 250 | 5.52146 | 400 | 300 | 5.70378 | 333 | 350 | 5.85793 | 286 | 400 | 5.99146 | 250 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ |

Natural Logarithms.

| u | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | 4 | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | ${ }_{\text {logeu }}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\text {e }} \mathbf{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 400 | 5.99146 | 250 | 450 | 6. 10925 | 222 | 500 | 6.2146 I | 200 | 550 | 6.30992 | 182 |
| 401 | 5.99396 | 249 | 451 | 6.11147 | 222 | 501 | 6.21661 | 200 | 551 | 6.31173 | 181 |
| 402 | 5.99645 | 249 | 452 | 6.11368 | 221 | 502 | 6.21860 | 199 | 552 | 6.31355 | 18 I |
| 403 | 5.99894 | 248 | 453 | 6.11589 | 221 | 503 | 6.22059 | 199 | 553 | 6.31536 | I8I |
| 404 | 6.00141 | 248 | 454 | 6.11810 | 220 | 504 | 6.22258 | 198 | 554 | 6.31716 | 181 |
| 405 | 6.00389 | 247 | 455 | 6.12030 | 220 | 505 | 6.22456 | 198 | 555 | 6.31897 | 180 |
| 406 | 6.00635 | 246 | 456 | 6.12249 | 219 | 506 | 6.22654 | 198 | 556 | 6.32077 | I80 |
| 407 | 6.0088 I | 246 | 457 | 6. 12468 | 219 | 507 | 6.22851 | 197 | 557 | 6.32257 | I80 |
| 408 | 6.01127 | 245 | 458 | 6. 12687 | 218 | 508 | 6.23048 | 197 | 558 | 6.32436 | I79 |
| 409 | 6.01372 | 244 | 459 | 6. 12905 | 218 | 509 | C. 23245 | 196 | 559 | 6.32615 | 179 |
| 410 | 6.01616 | 244 | 460 | 6. I3I23 | 217 | 510 | 6.23441 | 196 | 560 | 6.32794 | 179 |
| 4II | 6.01859 | 243 | 46 I | 6. 13340 | 217 | 511 | 6.23637 | 196 | 561 | 6.32972 | 178 |
| 412 | 6.02102 | 243 | 462 | 6.13556 | 216 | 512 | 6.23832 | 195 | 562 | 6.33150 | 178 |
| 413 | 6.02345 | 242 | 463 | 6. 13773 | 216 | 513 | 6.24028 | 195 | 563 | 6.33328 | 178 |
| 414 | 6.02587 | 242 | 464 | 6. 13988 | 216 | 514 | 6.24222 | 195 | 564 | 6.33505 | 177 |
| 415 | 6.02828 | 241 | 465 | 6. 14204 | 215 | 515 | 6.24417 | 194 | 565 | 6. 33683 | 177 |
| 416 | 6.03069 | 240 | 466 | 6.14419 | 215 | 516 | 6.246 I I | 194 | 566 | 6.33859 | 177 |
| 417 | 6.03309 | 240 | 467 | 6. I4633 | 214 | 517 | 6.24804 | 193 | 567 | 6.34036 | 176 |
| 418 | 6.03548 | 239 | 468 | 6.14847 | 214 | 518 | 6.24998 | 193 | 568 | 6.34212 | I76 |
| 419 | 6.03787 | 239 | 469 | 6.15060 | 213 | 519 | 6.25190 | 193 | 569 | 6.34388 | 176 |
| 420 | 6.04025 | 238 | 470 | 6.15273 | 213 | 520 | 6.25383 | 192 | 570 | 6.34564 | 175 |
| 421 | 6.04263 | 238 | 471 | 6. 15486 | 212 | 521 | 6.25575 | 192 | 571 | 6.34739 | 175 |
| 422 | 6.04501 | 237 | 472 | 6.15698 | 212 | 522 | 6.25767 | 192 | 572 | 6.34914 | 175 |
| 423 | 6.04737 | 236 | 473 | 6.15910 | 2 II | 523 | 6.25958 | 191 | 573 | 6.35089 | 175 |
| 424 | 6.04973 | 236 | 474 | 6.16121 | 2 II | 524 | 6.26149 | I9I | 574 | 6.35263 | I74 |
| 425 | 6.05209 | 235 | 475 | 6.16331 | 2 II | 525 | 6.26340 | 190 | 575 | 6.35437 | I74 |
| 426 | 6.05444 | 235 | 476 | 6.16542 | 210 | 526 | 6.26530 | 190 | 576 | 6.35611 | 174 |
| 427 | 6.05678 | 234 | 477 | 6.16752 | 210 | 527 | 6.26720 | 190 | 577 | 6.35784 | 173 |
| 428 | 6.05912 | 234 | 478 | 6.16961 | 209 | 528 | 6.26910 | 189 | 578 | 6.35957 | 173 |
| 429 | 6.06146 | 233 | 479 | 6.17170 | 209 | 529 | 6.27099 | 189 | 579 | 6.36130 | 173 |
| 430 | 6.06379 | 233 | 480 | 6.17379 | 208 | 530 | 6.27288 | 189 | 580 | 6.36303 | 172 |
| 43 I | 6.066 II | 232 | 48I | 6.17587 | 208 | 531 | 6.27476 | 188 | 581 | 6.36475 | 172 |
| 432 | 6.06843 | 231 | 482 | 6.17794 | 207 | 532 | 6.27664 | 188 | 582 | 6.36647 | 172 |
| 433 | 6.07074 | 231 | 483 | 6.18002 | 207 | 533 | 6.27852 | 188 | 583 | 6.36819 | 172 |
| 434 | 6.07304 | 230 | 484 | 6.18208 | 207 | 534 | 6.28040 | 187 | 584 | 6.36990 | 171 |
| 435 | 6.07535 | 230 | 485 | 6.18415 | 206 | 535 | 6.28227 | 187 | 585 | 6.37161 | I71 |
| 436 | 6.07764 | 229 | 486 | 6.18621 | 206 | 536 | 6.28413 | 187 | 586 | 6.37332 | 171 |
| 437 | 6.07993 | 229 | 487 | 6. 18826 | 205 | 537 | 6.28600 | 185 | 587 | 6.37502 | 170 |
| 438 | 6.08222 | 228 | 488 | 6.19032 | 205 | 538 | 6.28786 | 186 | 588 | 6.37673 | 170 |
| 439 | 6.08450 | 228 | 489 | 6.19236 | 204 | 539 | 6.28972 | 186 | 589 | 6.37843 | 170 |
| 440 | 6.08677 | 227 | 490 | 6. 1944 | 204 | 540 | 6.29157 | 185 | 590 | 6.38012 | 169 |
| 441 | 6.08904 | 227. | 491 | 6.19544 | 204 | 54 I | 6.29342 | 185 | 591 | 6.38182 | 169 |
| 442 | 6.09131 | 226 | 492 | 6.19848 | 203 | 542 | 6.29527 | 185 | 592 | 6.38351 | 169 |
| 443 | 6.09357 | 226 | 493 | 6.20051 | 203 | 543 | 6.29711 | 184 | 593 | 6.38519 | 169 |
| 444 | 6.09582 | 225 | 494 | 6.20254 | 202 | 544 | 6.29895 | I84 | 594 | 6. 38688 | 168 |
| 445 | 6.09807 | 225 | 495 | 6.20456 | 202 | 545 | 6.30079 | 183 | 595 | 6.38856 | 168 |
| 446 | 6.10032 | 224 | 496 | 6.20658 | 202 | 546 | 6.30262 | 183 | 596 | 6.39024 | 168 |
| 447 | 6.10256 | 224 | 497 | 6.20859 | 201 | 547 | 6.30445 | 183 | 597 | 6.39192 | 168 |
| 448 | 6. 10479 | 223 | 498 | 6.21060 | 201 | 548 | 6.30628 | 182 | 598 | 6.39359 | 167 |
| 449 | 6.10702 | 223 | 499 | 6.21261 | 200 | 549 | 6.30810 | 182 | 599 | 6.39526 | 167 |
| 450 | 6. 10925 | 222 | 500 | 6.21461 | 200 | 550 | 6.30992 | 182 | 600 | 6.39693 | 167 |
| $e^{x}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ |

Natural Logarithms.

| u | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega F_{0}{ }^{\prime}$ | $u$ | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathbf{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 600 | 6.39693 | 167 | 650 | 6.47697 | 154 | 700 | 6.55108 | 143 | 750 | 6.62007 | 133 |
| 601 | 6.39859 | 166 | 651 | 6.47851 | 154 | 701 | 6.5525 I | 143 | 751 | 6.62141 | I33 |
| 602 | 6.40026 | 166 | 652 | 6.48004 | I 53 | 702 | 6.55393 | 142 | 752 | 6.62274 | I33 |
| 603 | 6.40192 | 166 | 653 | 6.48 I 58 | 153 | 703 | 6.55536 | 142 | 753 | 6.62407 | I33 |
| 604 | 6.40357 | 166 | 654 | 6.4831 I | 153 | 704 | 6.55678 | 142 | 754 | 6.62539 | I33 |
| 605 | 6.40523 | 165 | 655 | 6.48464 | 153 | 705 | 6.55820 | 142 | 755 | 6.62672 | I32 |
| 606 | 6.40688 | 165 | 656 | 6.48616 | 152 | 706 | 6.55962 | 142 | 756 | 6.62804 | 132 |
| 607 | 6.40853 | 165 | 657 | 6.48768 | 152 | 707 | 6.56103 | 141 | 757 | 6.62936 | I32 |
| 608 | 6.41017 | 164 | 658 | 6.48920 | 152 | 708 | 6.56244 | 141 | 758 | 6.63068 | 132 |
| 609 | 6.41182 | 164 | 659 | 6.49072 | 152 | 709 | 6.56386 | 141 | 759 | 6.63200 | I32 |
| 610 | 6.41346 | 164 | 660 | 6.49224 | 152 | 710 | 6.56526 | 141 | 760 | 6.63332 | 132 |
| 6 II | 6.41510 | 164 | 661 | 6.49375 | 15 I | 711 | 6.56667 | 141 | 761 | 6.63463 | 131 |
| 612 | 6.41673 | 163 | 662 | 6.49527 | 15 I | 712 | 6.56808 | 140 | 762 | 6.63595 | I3I |
| 613 | 6.41836 | 163 | 663 | 6.49677 | 15 I | 713 | 6.56948 | 140 | 763 | 6.63726 | I3I |
| 614 | 6.41999 | 163 | 664 | 6.49828 | 151 | 714 | 6.57088 | 140 | 764 | 6.63857 | I3I |
| 615 | 6.42162 | 163 | 665 | 6.49979 | 150 | 715 | 6.57228 | 140 | 765 | 6.63988 | 13 I |
| 616 | 6.42325 | 162 | 666 | 6.50129 | 150 | 716 | 6.57368 | 140 | 766 | 6.64118 | 131 |
| 6 I 7 | 6.42487 | 162 | 667 | 6.50279 | 150 | 717 | 6.57508 | 139 | 767 | 6.64249 | 130 |
| 618 | 6.42649 | 162 | 668 | 6.50429 | 150 | 718 | 6.57647 | 139 | 768 | 6.64379 | I 30 |
| 619 | 6.428 II | 162 | 669 | 6.50578 | 149 | 719 | 6.57786 | I 39 | 769 | 6.64509 | I 30 |
| 620 | 6.42972 | 16I | 670 | 6.50728 | 149 | 720 | 6.57925 | 139 | 770 | 6.64639 | I 30 |
| 621 | 6.43133 | 16I | 671 | 6.50877 | I49 | 721 | 6.58064 | I39 | 771 | 6.64769 | 130 |
| 622 | 6.43294 | 161 | 672 | 6.51026 | 149 | 722 | 6.58203 | I39 | 772 | 6.64898 | I30 |
| 623 | 6.43455 | 161 | 673 | 6.51175 | 149 | 723 | 6.5834 I | 138 | 773 | 6.65028 | 129 |
| 624 | 6.43615 | 160 | 674 | 6.51323 | 148 | 724 | 6.58479 | I38 | 774 | 6.65157 | 129 |
| 625 | 6.43775 | 160 | 675 | 6.5147 I | 148 | 725 | 6.58617 | 138 | 775 | 6.65286 | 129 |
| 626 | 6.43935 | 160 | 676 | 6.51619 | 148 | 726 | 6.58755 | I38 | 776 | 6.65415 | 129 |
| 627 | 6.44095 | 159 | 677 | 6.51767 | 148 | 727 | 6.58893 | 138 | 777 | 6.65544 | 129 |
| 628 | 6.44254 | 159 | 678 | 6.51915 | 147 | 728 | 6.59030 | 137 | 778 | 6.65673 | 129 |
| 629 | 6.44413 | 159 | 679 | 6.52062 | 147 | 729 | 6.59167 | 137 | 779 | 6.65801 | 128 |
| 630 | 6.44572 | 159 | 680 | 6.52209 | 147 | 730 | 6.59304 | 137 | 780 | 6.65929 | 128 |
| 631 | 6.44731 | 158 | 681 | 6.52356 | 147 | 731 | 6.59441 | 137 | 78i | 6.66058 | 128 |
| 632 | 6.44889 | 158 | 682 | 6.52503 | 147 | 732 | 6.59578 | 137 | 782 | 6.66185 | 128 |
| 633 | 6.45047 | 158 | 683 | 6.52649 | 1.46 | 733 | 6.59715 | 136 | 783 | 6.66313 | 128 |
| 634 | 6.45205 | 158 | 684 | 6.52796 | 146 | 734 | 6.59851 | I36 | 784 | 6.66441 | 128 |
| 635 | 6.45362 | 157 | 685 | 6.52942 | 146 | 735 | 6.59987 | 136 | 785 | 6.66568 | 127 |
| 636 | 6.45520 | 157 | 686 | 6.53088 | 146 | 736 | 6.60123 | I36 | 786 | 6.66696 | 127 |
| 637 | 6.45677 | 157 | 687 | 6. 53233 | 146 | 737 | 6.60259 | I36 | 787 | 6.66823 | 127 |
| 638 | 6.45834 | 157 | 688 | 6. 53379 | 145 | 738 | 6.60394 | I36 | 788 | 6.66950 | 127 |
| 639 | 6.45990 | 156 | 689 | 6.53524 | 145 | 739 | 6.60530 | I 35 | 789 | 6.67077 | 127 |
| 640 | 6.46147 | 156 | 690 | $6.53{ }^{1} 669$ | 145 | 740 | 6.60665 | 135 | 790 | 6.67203 | 127 |
| 641 | 6.46303 | ${ }^{1} 56$ | 691 | 6.53814 | 145 | 741 | 6.60800 | 135 | 791 | 6.67330 | 126 |
| 642 | 6.46459 | 156 | 692 | 6.53959 | 145 | 742 | 6.60935 | 135 | 792 | 6.67456 | 126 |
| 643 | 6.46614 | 156 | 693 | 6.54103 | 144 | 743 | 6.61070 | I35 | 793 | 6.67582 | 126 |
| 644 | 6.46770 | 155 | 694 | 6.54247 | 144 | 744 | 6.61204 | I 34 | 794 | 6.67708 | 126 |
| 645 | 6.46925 | 155 | 695 | 6.54391 | 144 | 745 | 6.61338 | 134 | 795 | 6.67834 | 126 |
| 646 | 6.47080 | 155 | 696 | 6.54535 | 144 | 746 | 6.61473 | I 34 | 796 | 6.67960 | 126 |
| 647 | 6.47235 | 155 | 697 | 6.54679 | 143 | 747 | 6.61607 | 134 | 797 | 6.68085 | 125 |
| 648 | 6.47389 | 154 | 698 | 6.54822 | 143 | 748 | 6.61740 | 134 | 798 | 6.682 II | 125 |
| 649 | 6.47543 | 154 | 699 | 6.54965 | 143 | 749 | 6.61874 | I34 | 799 | 6.68336 | 125 |
| 650 | 6.47697 | 154 | 700 | 6.55108 | 143 | 750 | 6.62007 | 133 | 800 | 6.68461 | 125 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $e^{x}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ |

Natural Logarithms.

| u | $\log _{\mathrm{e}} \mathrm{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\log _{\mathrm{e}} \mathrm{L}$ | $\omega \mathrm{F}_{0}$ | u | $\log _{\text {e }} \mathrm{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\mathbf{l o g}_{\mathrm{e}} \mathrm{U}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 800 | 6.68461 | 125 | 850 | 6.74524 | 118 | 900 | 6.80239 | III | 950 | 6.85646 | 105 |
| 801 | 6.68586 | 125 | 851 | 6.74641 | 118 | 901 | 6.80351 | III | 951 | 6.85751 | 105 |
| 802 | 6.687 II | 125 | 852 | 6.74759 | 117 | 902 | 6.80461 | III | 952 | 6.85857 | 105 |
| 803 | 6.68835 | 125 | 853 | 6.74876 | 117 | 903 | 6.80572 | III | 953 | 6.85961 | 105 |
| 804 | 6.68960 | 124 | 854 | 6.74993 | II7 | 904 | 6.80683 | III | 954 | 6.86066 | $105{ }^{-}$ |
| 805 | 6.69084 | 124 | 855 | 6.75110 | II7 | 905 | 6.80793 | 110 | 955 | 6.86171 | 105 |
| 806 | 6.69208 | 124 | 856 | 6.75227 | 117 | 906 | 6.80904 | I 10 | 956 | 6.86276 | 105 |
| 807 | 6.69332 | 124 | 857 | 6.75344 | 117 | 907 | 6.81014 | I 10 | 957 | 6.86380 | 104 |
| 808 | 6.69456 | 124 | 858 | 6.75460 | 117 | 908 | 6.81124 | 110 | 958 | 6.86485 | 104 |
| 809 | 6.69580 | 124 | 859 | 6.75577 | 116 | 909 | 6.81235 | 110 | 959 | 6.86589 | 104 |
| 810 | 6.69703 | 123 | 860 | 6.75693 | 116 | 910 | 6.8I344 | IIO | 960 | 6.86693 | 104 |
| 8II | 6.69827 | 123 | 861 | 6.75809 | 116 | 911 | 6.81454 | 110 | 961 | 6.86797 | 104 |
| 812 | 6.69950 | 123 | 862 | 6.75926 | 116 | 912 | 6.81564 | 110 | 962 | 6.86901 | 104 |
| 813 | 6.70073 | 123 | 863 | 6.76041 | 116 | 913 | 6.81674 | 110 | 963 | 6.87005 | 104 |
| 8I4 | 6.70196 | 123 | 864 | 6.75157 | 116 | 914 | 6.81783 | 109 | 964 | 6.87109 | 104 |
| 8 I 5 | 6.70319 | 123 | 865 | 6.76273 | II6 | 915 | 6.81892 | 109 | 965 | 6.87213 | 104 |
| 816 | 6.70441 | 123 | 866 | 6.76388 | II5 | 916 | 6.82002 | 109 | 966 | 6.87316 | 104 |
| 817 | 6.70564 | 122 | 867 | 6.76504 | II5 | 917 | 6.821 I I | 109 | 967 | 6.87420 | 103 |
| 818 | 6.70686 | 122 | 868 | 6.76619 | II5 | 918 | 6.82220 | 109 | 968 | 6.87523 | 103 |
| 819 | 6.70808 | 122 | 869 | 6.76734 | II5 | 919 | 6.82329 | 109 | 969 | 6.87626 | 103 |
| 820 | 6.70930 | 122 | 870 | 6.76849 | II5 | 920 | 6.82437 | 109 | 970 | 6.87730 | 103 |
| 821 | 6.71052 | 122 | 871 | 6.76964 | II5 | 921 | 6.82546 | 109 | 971 | 6.87833 | 103 |
| 822 | 6.71174 | 122 | 872 | 6.77079 | 115 | 922 | 6.82655 | 108 | 972 | 6.87936 | 103 |
| 823 | 6.71296 | 122 | 873 | 6.77194 | 115 | 923 | 6.82763 | 108 | 973 | 6.88038 | 103 |
| 824 | 6.714 I 7 | 121 | 874 | 6.77308 | II4 | 924 | 6.82871 | 108 | 974 | 6.88 I 4 I | 103 |
| 825 | 6.71538 | I2I | 875 | 6.77422 | II4 | 925 | 6.82979 | 108 | 975 | 6.88244 | 103 |
| 826 | 6.71659 | 12 I | 876 | 6.77537 | II4 | 926 | 6.83087 | 108 | 976 | 6.88346 | 102 |
| 827 | 6.71780 | 121 | 877 | 6.77651 | II4 | 927 | 6.83195 | 108 | 977 | 6.88449 | 102 |
| 828 | 6.71901 | 121 | 878 | 6.77765 | II4 | 928 | 6.83303 | 108 | 978 | 6.8855 I | 102 |
| 829 | 6.72022 | I2I | 879 | 6.77878 | II4 | 929 | 6.834 II | 108 | 979 | 6.88653 | 102 |
| 830 | 6.72143 | 120 | 880 | 6.77992 | II4 | 930 | 6.83518 | 108 | 980 | 6.88755 | 102 |
| 831 | 6.72263 | 120 | 88I | 6.78106 | II4 | 931 | 6.83626 | 107 | 981 | 6.88857 | 102 |
| 832 | 6.72383 | 120 | 882 | 6.78219 | II3 | 932 | 6.83733 | 107 | 982 | 6.88959 | 102 |
| 833 | 6.72503 | 120 | 883 | 6.78333 | II3 | 933 | 6.83841 | 107 | 983 | 6.89061 | 102 |
| 834 | 6.72623 | 120 | 884 | 6.78446 | II3 | 934 | 6.83948 | 107 | 984 | 6.89163 | 102 |
| 835 | 6.72743 | 120 | 885 | 6.78559 | 113 | 935 | 6.84055 | 107 | 985 | 6.89264 | 102 |
| 835 | 6.72863 | 120 | 886 | 6.78572 | II3 | 936 | 6.84162 | 107 | 986 | 6.89366 | IOI |
| 837 | 6.72982 | 119 | 887 | 6.78784 | II3 | 937 | 6.84268 | 107 | 987 | 6.89467 | IOI |
| 838 | 6.73102 | 119 | 888 | 6.78897 | II3 | 938 | 6.84375 | 107 | 988 | 6.89568 | IOI |
| 839 | 6.73221 | 119 | 889 | 6.79010 | 112 | 939 | 6.84482 | 106 | 989 | 6.89669 | 101 |
| 840 | 6.73340 | II9 | 890 | 6.79122 | 112 | 940 | 6.84588 | 106 | 990 | 6.89770 | 101 |
| 841 | 6.73459 | 119 | 891 | 6.79234 | 112 | 94 I | 6.84694 | 106 | 991 | 6.89871 | IOI |
| 842 | 6.73578 | 119 | 892 | 6.79347 | 112 | 942 | 6.84801 | 106 | 992 | 6.89972 | 101 |
| 843 | 6.73697 | 119 | 893 | 6.79459 | 112 | 943 | 6.84907 | 106 | 993 | 6.90073 | IOI |
| 844 | 6.73815 | 118 | 894 | 6.79571 | 112 | 944 | 6.85013 | 106 | 994 | 6.90174 | IOI |
| 845 | 6.73934 | 118 | 895 | 6.79682 | 112 | 945 | 6.85118 | 106 | 995 | 6.90274 | IOI |
| 846 | 6.74052 | 118 | 896 | 6.79794 | 112 | 946 | 6.85224 | 106 | 996 | 6.90375 | 100 |
| 847 | 6.74170 | 118 | 897 | 6.79906 | III | 947 | 6.85330 | 106 | 997 | 6.90475 | 100 |
| 848 | 6.74288 | 118 | 898 | 6.80017 | III | 948 | 6.85435 | 105 | 998 | 6.90575 | 100 |
| 849 | 6.74406 | 118 | 899 | 6.80128 | III | 949 | 6.85541 | 105 | 999 | 6.90675 | 100 |
| 850 | 6.74524 | 118 | 900 | 6.80239 | III | 950 | 6.85646 | 105 | 1000 | 6.90776 | 100 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ | $e^{x}$ | X | $e^{-x}$ | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{-x}$ |

Natural Logarithms.

| u | Logeu | u | Logeu | u | $\log _{\mathrm{e}} \mathbf{u}$ | u | $\mathrm{Log}_{\mathrm{e}} \mathrm{u}$ | 4 | $L_{\text {oge }} \mathrm{U}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1000 | 6.90776 | 1361 | 7.21598 | 1721 | 7.45066 | 2III | 7.65492 | 2503 | 7.82525 |
| 1009 | 6.91672 | I367 | 7.22037 | 1723 | 7.45182 | 2113 | 7.65586 | 2521 | 7.83241 |
| '1013 | 6.92067 | 1373 | 7.22475 | 1733 | 7.45761 | 12.129 | 7.66341 | 2531 | 7.83637 |
| 1019 | 6.92658 | 1381 | 7.23056 | I74 I | 7.46221 | 21311 | 7.66435 | 2539 | 7.83953 |
| 102I | 6.92854 | I 399 | 7.2435 I | I747 | 7.46566 | 2137 | 7.66716 | 2543 | 7.84 II |
| IO3I | 6.93828 | 1409 | 7.25064 | 1753 | 7.46908 | 2141 | 7.66903 | 2549 | 7.84346 |
| 1033 | 6.94022 | 1423 | 7.26052 | 1759 | 7.47250 | 2143 | 7.66996 | 2551 | 7.84424 |
| 1039 | 6.94601 | 1427 | 7.25333 | 1777 | 7.48268 | 2153 | 7.67462 | 2557 | 7.84659 |
| 1049 | 6.95559 | 1429 | 7.26473 | 1783 | 7.48605 | 2161 | 7.67833 | 2579 | 7.85516 |
| 1051 | 6.95750 | 1433 | 7.26753 | 1787 | 7.48829 | 2179 | 7.68662 | 2591 | 7.85980 |
| 1061 | 6.96697 | I439 | 7.27170 | I'89 | 7.48941 | 2203 | 7.69758 | 2593 | 7.86057 |
| 1063 | 6.96885 | 1447 | 7.27725 | 180I | 7.49610 | 2207 | 7.69939 | 2609 | 7.86672 |
| 1069 | 6.97448 | I451 | 7.28001 | I8II | 7.50163 | 2213 | 7.70210 | 2617 | 7.86978 |
| 1087 | 6.99118 | 1453 | 7.28139 | 1823 | 7.50824 | 222I | 7.70571 | 2521 | 7.87131 |
| 1091 | 6.99485 | 1459 | 7.2855 I | 1831 | 7.51262 | 2237 | 7.71289 | 2633 | 7.87588 |
| 1093 | 6.99568 | 1471 | 7.29370 | 1847 | 7.52132 | 2239 | 7.71378 | 2647 | 7.88118 |
| 1097 | 7.00033 | I48I | 7.30047 | 1861 | 7.52887 | 2243 | 7.7155.7 | 2657 | 7.88495 |
| 1103 | 7.00579 | 1483 | 7.30182 | 1857 | 7.53209 | 2251 | 7.71913 | 2659 | 7.88571 |
| I 109 | 7.01121 | 1487 | $7 \cdot 30452$ | 1871 | 7.53423 | 2267 | 7.72621 | 2663 | 7.88721 |
| III7 | 7.01840 | 1489 | $7 \cdot 30586$ | 1873 | 7.53530 | 2269 | 7.72709 | 2671 | 7.89021 |
| 1123 | 7.02376 | 1493 | $7 \cdot 30854$ | 1877 | 7.537.43 | 2273 | 7.72886 | 2677 | 7.89245 |
| II 29 | 7.02909 | I499 | $7 \cdot 31255$ | 1879 | 7.53849 | 228I | 7.73237 | 2683 | 7.89469 |
| II5I | 7.04839 | I5II | $7 \cdot 32053$ | 1889 | 7.54380 | 2287 | 7.73500 | 2687 | 7.89518 |
| II53 | 7.05012 | 1523 | $7 \cdot 32844$ | 1901 | 7.55014 | 2293 | 7.73762 | 2689 | 7.80692 |
| 1163 | 7.05876 | 153 I | $7 \cdot 33368$ | 1907 | 7.55329 | 2297 | 7.73936 | 2693 | 7.89841 |
| 1171 | 7.06561 | 1543 | 7.34148 | 1913 | 7.55643 | 2309 | 7.74457 | 2699 | 7.90064 |
| II8I | 7.0741 .2 | I. 549 | 7.34536 | 1931 | 7.56579 | 2311 | 7.74544 | 2707 | 7.90360 |
| 1187 | 7.07918 | 1553 | 7.34794 | 1933 | 7.56683 | 2333 | 7.75491 | 27 II | 7.90507 |
| 1193 | 7.08423 | I559 | 7.35180 | 1949 | 7.57507 | 2339 | 7.75748 | 2713 | 7.90581 |
| I201 | 7.09091 | I 567 | $7 \cdot 35692$ | 1951 | 7.57610 | 2341 | 7.75833 | 2719 | 7.90802 |
| 1213 | 7. 10085 | 1571 | 7.35947 | 1973 | 7.58731 | 12347 | 7.76089 | 2729 | 7.911169 |
| 1217 | 7.10414 | 1579 | 7.36455 | 1979 | 7.59035 | 2351 | 7.76260 | 2731 | 7.91242 |
| 1223 | 7. 10906 | 1583 | 7.36708 | 1987 | 7.59438 | 2357 | 7.76514 | 27.41 | 7.91608 |
| 1229 | 7. 11396 | 1597 | 7.37588 | 1993 | 7.597.40 | 2371 | 7.77107 | 2749 | 7.91899 |
| 1231 | 7.11558 | 1601 | $7 \cdot 37838$ | 1997 | 7.59940 | 2377 | 7.77359 | 2753 | 7.92045 |
| 1237 | 7. 12044 | 1607 | 7.38212 | 1999 | 7.60040 | 2381 | 7.77528 | 2767 | 7.92552 |
| 1249 | 7.13010 | 1609 | 7.38337 | 2003 | 7.60240 | 2383 | 7.77612 | 12777 | 7.92913 |
| 1259 | 7. 13807 | 1613 | 7.38585 | 2011 | 7.60639 | 2389 | 7.77853 | 2789 | 7.93344 |
| 1277 | 7.15227 | 1619 | 7.38956 | 2017 | 7.60937 | 2393 | 7.78030 | 2791 | 7.93416 |
| 1279 | 7.15383 | 162I | $7 \cdot 39080$ | 2027 | 7.61431 | 2399 | 7.78281 | 2797 | 7.93630 |
| 1283 | 7.15696 | 1627 | 7.39449 | 2029 | 7.6II 530 | 24 II | 7.78780 | 2801 | 7.93773 |
| 1289 | 7.16162 | 1637 | 7.40062 | 2039 | 7.62021 | 2417 | 7.79028 | 2803 | 7.93845 |
| I291 | 7.16317 | 1657 | 7.41276 | 2053 | 7.62706 | 2423 | 7.79276 | 2819 | 7.94414 |
| 1297 | 7. 16781 | . 1663 | 7.41638 | 2063 | 7.63192 | 2437 | 7.79852 | 2833 | 7.94909 |
| 1301 | 7.17089 | 1667 | 7.41878 | 2069 | 7.63482 | 244 I | 7.80016 | 2837 | 7.95050 |
| 1303 | 7.17,242 | 1669 | 7.41998 | 2081 | 7.64060 | 2447 | 7.80262 | 2843 | 7.95262 |
| 1307 | 7.17549 | 1693 | 7.43426 | 2083 | 7.64156 | 2459 | 7.80751 | 285 I | 7.95543 |
| 1319 | $7 \cdot 18463$ | 1697 | 7.43662 | 2087 | 7.64348 | 2.467 | 7.81076 | 2857 | 7.95753 |
| 1321 | 7.18514 | 1699 | 7.43780 | $2089$ | $7.64444$ | $12473$ | 7.81319 | 2861 | $7.95893$ |
| 1327 | 7.19068 | 1709 | 7.44366 | 2099 | 7.64922 | 2477 | 7.81480 | 2879 | 7.96520 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x |

Natural Logarithms.

| u | $L^{\text {oge }}$ | u | $L^{\text {Logeu }}$ | u | $\log _{\mathrm{e}} \mathrm{U}$ | u | $\mathrm{Log}_{\mathrm{e}} \mathrm{U}$ | u | Logell |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2887 | 7.96797 | 3323 | 8. 10862 | 3709 | 8.21852 | 4129 | 8.32579 | 456I | 8.42530 |
| 2897 | 7.97143 | 3329 | 8.11043 | 3719 | 8.22 I 21 | 4 I 33 | 8.32676 | 4567 | 8.42661 |
| 2903 | 7.97350 | 333I | 8.11103 | 3727 | 8.22336 | 4139 | 8.32821 | 4583 | 8.4301 I |
| 2909 | 7.97556 | 3343 | 8.11462 | 3733 | 8.22497 | $4{ }^{15} 5$ | 8.33159 | 4591 | 8.43185 |
| 2917 | 7.9783 I | 3347 | 8. I 1582 | 3739 | 8.22657 | 4157 | 8.33255 | 4597 | 8.43316 |
| 2927 | 7.98173 | 3359 | 8. 11940 | 3761 | 8.23244 | 4 I 59 | 8.33303 | 4603 | 8.43446 |
| 2959 | 7.98582 | 3361 | 8.11999 | 3767 | 8.23403 | 4177 | 8.33735 | 4621 | 8.43837 |
| 2953 | 7.99058 | 3371 | 8.12296 | 3769 | 8.23456 | 4201 | 8.334308 | 4637 | 8.44 I 82 |
| 2957 | 7.99193 | 3373 | 8. I2356 | 3779 | 8.23721 | 42 II | 8.34546 | 4639 | 8.44225 |
| 2963 | 7.99396 | 3389 | 8.12829 | 3793 | 8.24091 | 4217 | 8.34688 | 4643 | 8.44312 |
| 2969 | 7.99598 | 3391 | 8. 12888 | 3797 | 8.24197 | 4219 | 8.34735 | 4649 | 8.4444 I |
| 2971 | 7.99665 | 3407 | 8. 13359 | 3803 | 8.24355 | 4229 | 8.34972 | 4651 | 8.44484 |
| 2999 | 8.00603 | 34I3 | 8. 13535 | 3821 | 8.24827 | 4231 | 8.35019 | 4657 | 8.44613 |
| 3001 | 8.00670 | 3433 | 8.14119 | 3823 | 8.24879 | 4241 | 8.35255 | 4663 | 8.44741 |
| 3011 | 8.01003 | 3449 | 8.14584 | 3833 | 8.251 I 40 | 4243 | 8.35303 | 4673 | 8.44956 |
| 3019 | 8.01268 | 3457 | 8. 148 I 6 | 3847 | 8.25505 | 4253 | 8.35538 | 4679 | 8.45084 |
| 3023 | 8.01400 | 3461 | 8.14931 | 3851 | 8.25609 | 4259 | 8.35679 | 4691 | 8.45340 |
| 3037 | 8.01853 | 3463 | 8. 14989 | 3853 | 8.25661 | 4261 | 8.35726 | 4703 | 8.45596 |
| 3041 | 8.01994 | 3467 | 8. 15104 | 3863 | 8.25920 | 4271 | 8.35960 | 4721 | 8.45978 |
| 3049 | 8.02257 | 3469 | 8.15162 | 3777 | 8.26282 | 4273 | 8.36007 | 4723 | 8.46020 |
| 3061 | 8.02650 | 3491 | 8. 15794 | 388 I | 8.26385 | 4283 | 8.36241 | 4729 | 8.46147 |
| 3067 | 8.02846 | 3499 | 8.16023 | 3889 | 8.26591 | 4289 | 8.36381 | 4733 | 8.46231 |
| 3079 | 8.03236 | 3511 | 8. 16366 | 3907 | 8.27053 | 4297 | 8.36567 | 4751 | 8.46611 |
| 3083 | 8.03366 | 3517 | 8.16536 | 39 II | 8.27155 | 4327 | 8.37263 | 4759 | 8.46779 |
| 3089 | 8.03560 | 3527 | '8. 16820 | 3917 | 8.27308 | 4337 | 8.37494 | 4783 | 8.47282 |
| 3109 | 8.04206 | 3529 | 8. 16877 | 3919 | 8.27359 | 4339 | 8.37540 | 4787 | 8.47366 |
| 3119 | 8.04527 | 3533 | 8. 16990 | 3923 | 8.27461 | 4349 | 8.37770 | 4789 | 8.47408 |
| 3121 | 8.04591 | 3539 | 8. 17160 | 3929 | 8.27614 | 4357 | 8.37954 | 4793 | 8.47491 |
| 3137 | 8.05102 | 354 I | 8.17216 | 393.1 | 8.27665 | 4363 | 8.38092 | 4799 | 8.47616 |
| 3163 | 8.05928 | 3547 | 8. 17386 | 3943 | 8.27970 | 4373 | 8.38320 | 480 I | 8.47653 |
| 3167 | 8.06054 | 3557 | 8.117667 | 3947 | 8.2807 1 | 4391 | 8.38731 | 4813 | 8.47908 |
| 3169 | 8.06117 | 3559 | 8. 17723 | 3967 | 8.28577 | 4397 | 8.38868 | 4817 | 8.47991 |
| 3181 | 8.06495 | 3571 | 8. 18060 | 3989 | 8.29130 | 4409 | 8.39140 | 4831 | 8.4828 I |
| 3187 | 8.06684 | 3581 | 8.18340 | 4001 | 8.294:30 | 4421 | 8.39412 | 486 I | 8.48900 |
| 3191 | 8.06809 | 3583 | 8. 18396 | 4003 | 8.29480 | 4423 | 8.39457 | 4871 | 8.49105 |
| 3203 | 8.07184 | 3593 | 8. 18674 | 4007 | 8.29580 | 4441 | 8.39863 | 4877 | 8.49229 |
| 3209 | 8.07371 | 3607 | 8. 19063 | 4013 | 8.29729 | 4447 | 8.39998 | 4889 | 8.49474 |
| 3217 | 8.07620 | 3613 | 8. 19229 | 4019 | 8.29879 | 4451 | 8.40088 | 4903 | 8.49760 |
| 3221 | 8.07745 | 3617 | 8. 19340 | 4021 | 8.29929 | 4457 | 8.40223 | 4909 | 8.49883 |
| 3229 | 8.07993 | 3623 | 8. 19506 | 4027 | 8.30078 | 4463 | 8.40358 | 4919 | 8.50086 |
| 3251 | 8.08672 | 3631 | 8. 19726 | 4049 | 8.30623 | 448I | 8.40760 | 493'I | 8.50330 |
| 3253 | 8.08733 | 3637 | 8. 19891 | 4051 | 8.30672 | 4483 | 8.40805 | 4933 | 8.50370 |
| 3257 | 8.08856 | 3643 | 8.20056 | 4057 | 8.30820 | 4493 | 8.41028 | 4937 | 8.50451 |
| 3259 | 8.08918 | 3659 | 8.20495 | 4073 | 8.312114 | 4507 | 8.41339 | 4943 | 8.50573 |
| 3271 | 8.09285 | 3671 | 8.20822 | 4079 | 8.31361 | 4513 | 8.41472 | 4951 | 8.50734 |
| 3299 | 8. 10137 | 3673 | 8.20876 | 4091 | 8.31654 | 4517 | 8.41560 | 4957 | 8.50856 |
| 3301 | 8.10198 | 3677 | 8.20985 | 4093 | 8.31703 | 4519 | 8.41605 | 4967 | 8.51057 |
| 3307 | 8.10380 | 3691 | 8.21365 | 4099 | 8.31850 | 4523 | 8.4 I 693 | 4969 | 8.51097 |
| 3313 | 8.10561 | 3697 | 8.21528 | 4111 | 8.32142 | 4547 | 8.42222 | 4973 | 8.51178 |
| 3319 | 8.10742 | 3701 | 8.21636 | 4127 | 8.3253! | 4549 | 8.42266 | 4987 | 8.514 .59 |
| $e^{x}$ | x | $e^{x}$ | x | $e^{x}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $e^{x}$ | x |

Natural Logarithms.

| $u$ | $\mathrm{Log}_{\mathrm{e}} \mathrm{U}$ | u | $\mathrm{LoO}_{\mathrm{e}} \mathrm{U}$ | $u$ | Logeu $^{\text {u }}$ | $u$ | $\mathrm{Log}_{\text {el }}$ | u | Logeu |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 4993 | 8.51579 | 5437 | 8.60098 | 5849 | 8.67403 | 6287 | 8.74624 | 6733 | 8.81478 |
| 4999 | 8.51699 | 5441 | 8.60172 | 5851 | 8.67437 | 6299 | 8.74815 | 6737 | 8.81537 |
| 5003 | 8.51779 | 5443 | 8.60209 | 5857 | 8.67539 | 6301 | 8.74846 | 6761 | 8.31893 |
| 5009 | 8.51899 | 5449 | 8.60319 | 5861 | 8.67608 | 631 I | 8.75005 | 6763 | 8.81922 |
| 5011 | 8.51939 | 5471 | 8.60722 | 5867 | 8.67710 | 6317 | 8.75100 | 6779 | 8.82158 |
| '5021 | 8.52138 | 5477 | 8.60831 | 5869 | 8.67744 | 6323 | 8.75195 | 6781 | 8.82188 |
| 5023 | 8.52178 | 5479 | 8.60868 | 15879 | 8.67914 | 6329 | 8.75290 | 6791 | 8.82335 |
| 5039 | 8.52496 | 5483 | 8.6094 I | 5881 | 8.67948 | 6337 | 8.75416 | 6793 | 8.82365 |
| 5051 | 8.52734 | 5501 | 8.61269 | 5897 | 8.68220 | 6343 | 8.755 II | 6803 | 8.82512 |
| 5059 | 8.52892 | 5503 | 8.61305 | 5903 | 8.68322 | 6353 | 8.75668 | 6823 | 8.82805 |
| 5077 | 8. 53248 | 5507 | 8.61378 | 5923 | 8.68660 | 6359 | 8.75763 | 6827 | 8.82864 |
| 5081 | 8. 53326 | 5519 | 8.61595 | 5927 | 8.68727 | 6361 | 8.75794 | 6829 | 8.82893 |
| 5087 | 8.53444 | 5521 | 8.61631 | 5939 | 8.68930 | 6367 | 8.75888 | 6833 | 8.82952 |
| 5099 | 8. 53680 | 5527 | 8.61740 | '5953 | 8.69165 | 6373 | 8.75983 | 684 I | 8.83069 |
| 5101 | 8.53719 | 5531 | 8.6 I 812 | 5981 | 8.69634 | 6379 | 8.76077 | 6857 | 8.83303 |
| 5107 | 8.53837 | 5557 | 8.62281 | 5987 | 8.69735 | 6389 | 8.76233 | 6863 | 8.83390 |
| 5113 | 8.53954 | 5563 | 8.62389 | 6007 | 8.70068 | 6397 | 8.76358 | 6869 | 8.83477 |
| 5119 | 8.54071 | 5569 | 8.62497 | 6011 | 8.70135 | 6421 | 8.76733 | 6871 | 8.83506 |
| 5147 | 8.54617 | 5573 | 8.62569 | 6029 | 8.70434 | 6427 | 8.76826 | 6883 | 8.8368 I |
| 5153 | 8.54733 | 5581 | 8.62712 | 6037 | 8.70566 | 6449 | 8.77168 | 6889 | 8.83768 |
| 5167 | 8.55005 | 5591 | 8.62891 | 6043 | 8.70666 | 6451 | 8.77199 | 6907 | 8.84029 |
| 5171 | 8. 55082 | 5623 | 8.63462 | 6047 | 8.70732 | 6469 | 8.77478 | 6911 | 8.84087 |
| 5179 | 8.55237 | 5639 | 8.63746 | 6053 | 8.70831 | 6473 | 8.77539 | 6917 | 8.84174 |
| 5189 | 8.55430 | 5641 | 8.63782 | 6067 | 8.71062 | 648 I | 8.77663 | 6947 | 8.84607 |
| 5197 | 8.55584 | 5647 | 8.63888 | 6073 | 8.71161 | 6491 | 8.77817 | 6949 | 8.84635 |
| 5209 | 8.55814 | 5651 | 8.63959 | 6079 | 8.71260 | 6521 | 8.78278 | 6959 | 8.84779 |
| 5227 | 8.56159 | 5653 | 8.63994 | 6089 | 8.71424 | 6529 | 8.78401 | 6961 | 8.84808 |
| 5231 | 8.56236 | 5657 | 8.64065 | 6091 | 8.71457 | 6547 | 8.78676 | 6967 | 8.84894 |
| 5233 | 8.56274 | 5659 | 8.64100 | 6101 | 8.71621 | 655 I | 8.78737 | 6971 | 8.8495 I |
| 5237 | 8.56350 | 5669 | 8.64277 | 6II3 | 8.71817 | 6553 | 8.78768 | 6977 | 8.85037 |
| 5261 | 8.56808 | 5683 | 8.64523 | 6121 | 8.71948 | 6563 | 8.78920 | 6983 | 8.85123 |
| 5273 | 8.57035 | 5689 | 8.64629 | 6 GI 31 | 8.72111 | 6569 | 8.79012 | 6991 | 8.85238 |
| 5279 | 8.57149 | 5693 | 8.64699 | 6133 | 8.72144 | 6571 | 8.79042 | 6997 | 8.85324 |
| 5281 | 8.57187 | 5701 | 8.64840 | 6143 | 8.72307 | 6577 | 8.79133 | 7001 | 8.85381 |
| 5297 | 8.57490 | 5711 | 8.65015 | 6151 | 8.72437 | 6581 | 8.79194 | 7013 | 8.85552 |
| 5303 | 8.57603 | 5717 | 8.65120 | 6163 | 8.72632 | 6599 | 8.79467 | 7019 | 8.85638 |
| 5309 | 8.57716 | 5737 | 8.65469 | 6173 | 8.72794 | 6607 | 8.79588 | 7027 | 8.85752 |
| 5323 | 8.57979 | 5741 | 8.65539 | 6197 | 8.73182 | 6619 | 8.79770 | 7039 | 8.85922 |
| 5333 | 8.58167 8.58429 | 5743 | 8.65574 | 6199 | 8.73214 | 6637 | 8.80042 | 7043 | 8.85979 |
| 5347 | 8.58429 | 5749 | 8.65678 | 6203 | 8.73279 | 6653 | 8.80282 | 7057 | 8.86178 |
| 5351 | 8.58504 | 5779 | 8.66199 | 6211 | 8.73408 | 6659 | 8.80372 | 7069 | 8.86347 |
| 5381 | 8.59063 | 5783 | 8.66268 | 6217 | 8.73504 | 6661 | 8.80402 | 7079 | 8.86489 |
| 5387 | 8.59174 | 5791 | 8.66406 | 6221 | 8.73569 | 6673 | 8.80582 | 7103 | 8.86827 |
| 5393 | 8.59286 | 5801 5807 | 8.66579 8.66682 |  | 8.73697 | 6679 | 8.80672 | 7109 | 8.86912 |
| 5399 | 8.59397 | 5807 | 8.66682 | 6247 | 8.73986 | 6689 | 8.80822 | 7121 | 8.87080 |
| 5407 | 8.59545 | 5813 | 8.66785 | 6257 | 8.74146 | 6691 | 8.80852 | 7127 | 8.87165 |
| 5413 | 8.59656 | 5821 | 8.66923 | 6263 | 8.74241 | 6701 | 8.81001 | 7129 | 8.87193 |
| 5417 | 8.59730 | 5827 | 8.67026 | 6269 | 8.74337 | 6703 | 8.81031 | 7151 | 8.87501 |
| 5419 | 8.59767 | 5839 | 8.67231 | 6271 | 8.74369 | 6709 | 8.81121 | 7159 | 8.87613 |
| 542 I | 8.59988 | 5843 | 8.67300 | 6277 | 8.74465 | 6719 | 8.81269 | 7177 | 8.87864 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ |  | $\mathrm{e}^{\mathrm{x}}$ | $\times$ | $\mathrm{e}^{\mathrm{x}}$ | x |

Natural Logarithms.

| $u$ | Logeu | u | $\mathrm{Log}_{\mathrm{e}} \mathrm{H}$ | 4 | $\log _{\text {e }} \mathbf{U}$ | u | Logeu | u | Logeu |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 7187 | 8.88003 | 7621 | 8.93866 | 8093 | 8.99875 | 8573 | 9.05637 | 9001 | 9. 10509 |
| 7193 | 8.88086 | 7639 | 8.94102 | 8101 | 8.99974 | 858I | 9.05731 | 9007 | 9.10576 |
| 7207 | 8.88281 | 7643 | 8.94155 | 8 III | 9.00098 | 8597 | 9.05917 | 9011 | 9.10620 |
| 7211 | 8.88336 | 7649 | 8.94233 | 8117 | 9.00172 | 8599 | 9.05940 | 9013 | 9. 10642 |
| 7213 | 8.88364 | 7669 | 8.94494 | 8123 | 9.00245 | 8609 | 9.06056 | 9029 | 9.10820 |
| 7219 | 8.88447 | 7673 | 8.94546 | 8147 | 9.0054I | 8623 | 9.06219 | 9041 | 9. 10953 |
| 7229 | 8.88586 | 7681 | 8.946511 | 8161 | 9.00712 | 8627 | 9.06265 | 9043 | 9. 10975 |
| 7237 | 8.88696 | 7687 | 8.94729 | 8167 | 9.00786 | 8629 | 9.06288 | 9049 | 9.11041 |
| 7243 | 8.88779 | 7691 | 8.94781 | 8171 | 9.00835 | 8641 | 9.06427 | 9059 | 9.11151 |
| 7247 | 8.88834 | 7699 | 8.94885 | 8179 | 9.00933 | 8647 | 9.06497 | 9067 | 9. 11240 |
| 7253 | 8.88917 | 7703 | 8.94937 | 8191 | 9.01079 | 8663 | 9.06682 | 9091 | 9. 11504 |
| 7283 | 8.89330 | 7717 | 8.95118 | 8209 | 9.01299 | 8669 | 9.06751I | 9103 | 9.11636 |
| 7297 | 8.89522 | 7723 | 8.95196 | 8219 | 9.01420 | 8677 | 9.06843 | 9109 | 9.11702 |
| 7307 | 8.89659 | 7727 | 8.95248 | 8221 | 9.01445 | 8681 | 9.06889 | 9127 | 9. 11899 |
| 7309 | 8.89686 | 7741 | 8.95429 | 8231 | 9.0r566 | 8689 | 9.06981 | 9133 | 9.11965 |
| 7321 | 8.89850 | 7753 | 8.95584 | 8233 | 9.01591 | 8693 | 9.07027 | 9137 | 9.12009 |
| 733: | 8.89987 | 7757 | 8.95635 | 8237 | 9.01639 | 8699 | 9.07096 | 9151 | 9.12162 |
| 7333 | 8.90014 | 7759 | 8.95661 | 8243 | 9.01712 | 8707 | 9.07188 | 9157 | 9.12227 |
| 7349 | 8.90232 | 7789 | 8.96047 | 8263 | 9.01954 | 8713 | 9.07257 | 9161 | 9.1227I |
| 7351 | 8.90259 | 7793 | 8.96098 | 8269 | 9.02027 | 8719 | 9.07326 | 9173 | 9.12402 |
| 7369 | 8.90504 | 7817 | 8.96406 | 8273 | 9.02075 | 8731 | 9.07464 | 918 I | 9.12489 |
| 7393 | 8.90829 | 7823 | 8.96482 | 8287 | 9.022 | 8737 | 9.07532 | 9187 | 9. 12554 |
| 7411 | 8.91072 | 7829 | 8.96559 | 8291 | 9.0229 | 8741 | 9.07578 | 9199 | 9. 12685 |
| 7417 | 8.91153 | 7841 | 8.96712 | 8293 | 9.02317 | 8747 | 9.07647 | 9203 | 9.12728 |
| 7433 | 8.91368 | 7853 | 8.96765 | 8297 | 9.02365 | 8753 | 9.07715 | 9209 | 9. 12794 |
| 7451 | 8.91610 | 7867 | 8.97043 | 8311 | 9.02534 | 8761 | 9.07807 | 922 I | . 12924 |
| 7457 | 8.91691 | 7873 | 8.97119 | 8317 | 9.02606 | 8779 | 9.08012 | 9227 | 9.12989 |
| 7459 | 8.91718 | 7877 | 8.97170 | 8329 | 9.02750 | 8783 | 9.08057 | 9239 | 9.13119 |
| 7477 | 8.91959 | 7879 | 8.97196 | 8353 | 9.03038 | 8803 | 9.08285 | 9241 | 9.13141 |
| 7481 | 8.92012 | 7883 | 8.97246 | 8363 | 9.03157 | 8807 | 9.08330 | 9257 | 9.13314 |
| 7487 | 8.92092 | 7901 | 8.97474 | 8369 | 9.03229 | 8819 | 9.08466 | 9277 | 9. 13529 |
| 7489 | 8.92119 | 7907 | 8.97550 | 8377 | 9.03325 | 8821 | 9.08489 | 928 I | 9. 13572 |
| 7499 | 8.92252 | 7919 | 8.97702 | 8387 | 9.03444 | 8831 | 9.08602 | 9283 | 9. 13594 |
| 7507 | 8.92359 | 7927 | 8.97803 | 8389 | 9.03468 | 8837 | 9.08670 | 9293 | 9.13702 |
| 7517 | 8.92492 | 7933 | 8.97879 | 8419 | 9.03825 | 8839 | 9.08693 | 93II | 9.13895 |
| 7523 | 8.92572 | 7937 | 8.97929 | 8423 | 9.03872 | 8849 | 9.08806 | 93.19 | 9. 13981 |
| 7529 | 8.92652 | 7949 | 8.98080 | 8429 | 9.03943 | 8861 | 9.08941 | 9323 | 9. 14024 |
| 7537 | 8.92758 | 795I | 8.98105 | 8431 | 9.03967 | 8863 | 9.08964 | 9337 | 9.14174 |
| 7541 | 8.928II | 7963 | 8.98256 | 8443 | 9.04109 | 8867 | 9.09009 | 9341 | 9.14217 |
| 7547 | 8.92891 | 7993 | 8.98632 | 8447 | 9.04157 | 8887 | 9.09234 | 9343 | 9.14238 |
| 7549 | 8.92917 | 8009 | 8.98832 | 8461 | 9.04322 | 8893 | 9.09302 | 9349 | 9. 14302 |
| 7559 | 8.93049 | 801 I | 8.98857 | 8467 | 9.04393 | 8923 | 9.09639 | 9371 | 9. 14538 |
| 7561 | 8.93076 | 8017 | 8.98932 | 8501 | 9.04794 | 8929 | 9.09706 | 9377 | 9. 14602 |
| 7573 | 8.93234 | 8039 | 8.99206 | 8513 | 9.04935 | 8933 | 9.09751 | 9391 | 9.1475I |
| 7577 | 8.93287 | 8053 | 8.99380 | 8521 | 9.05029 | 8941 | 9.09840 | 9397 | 9.14815 |
| 7583 | 8.93366 | 8059 | 8.99454 | 8527 | 9.05099 | 8951 | 9.09952 | 9403 | 9.14878 |
| 7589 | 8.93446 | 8069 | 8.99578 | 8537 | 9.05216 | 8963 | 9. 10086 | 94 I 3 | 9. 14985 |
| 7591 | 8.93472 | 808I | 8.99727 | 8539 | 9.05240 | 8969 | 9. 10153 | 9419 | 9. 15048 |
| 7603 | 8.93630 | 8087 | 8.99801 | 8543 | 9.05287 | 8971 | 9.10175 | 942 I | 9.15070 |
| 7607 | 8.93682 | 8089 | 8.99826 | 8563 | 9.05521 | 8999 | 9.10487 | 9431 | 9.15176 |
| $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | $\times$ | $\mathrm{e}^{\mathrm{x}}$ | $\times$ | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x |

Natural Logarithms.

| $u$ | Logeu | u | $\mathbf{L o g}_{\text {e }} \mathbf{U}$ | u | $\mathbf{L o g}_{\text {e }} \mathbf{U}$ | 4 | $\mathrm{Log}_{\mathrm{e}} \mathrm{U}$ | u | $\mathrm{Log}_{\mathrm{e}} \mathrm{u}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 9433 | 9.15197 | 9551 | 9.16440 | 9719 | 9.18184 | 9833 | 9.19350 | 9967 | 9.20703 |
| 9437 | 9.15239 | 9587 | 9.16816 | 9721 | 9.18204 | 9839 | 9.194II | 9973 | 9.20764 |
| 9439 | 9.1526I | 9601 | 9.16962 | 9733 | 9.18328 | 9851 | 9.19533 | 10000 | 9.21034 |
| 9461 | 9. 15493 | 9613 | 9.17087 | 9739 | 9.18389 | 9857 | 9.19594 | 100000 | II. 51293 |
| 9463 | 9.15514 | 9619 | 9.17150 | 9743 | 9.18430 | 9859 | 9.19614 |  |  |
| 9467 | 9.15557 | 9623 | 9.17191 | 9749 | 9.18492 | 9871 | 9. 19736 |  |  |
| 9473 | 9.15620 | 9629 | 9.17253 | 9767 | 9.18676 | 9883 | 9.19857 |  |  |
| 9479 | 9.15683 | 9631 | 9.17274 | 9769 | 9. 18697 | 9887 | 9.19898 |  |  |
| 9491 | 9.15810 | 9643 | 9.17399 | 9781 | 9.18820 | 9901 | 9.20039 |  |  |
| 9497 | 9.15873 | 9649 | 9.1746I | 9787 | 9.1888I | 9907 | 9.20100 |  |  |
| 9511 | 9.16020 | 966I | 9.17585 | 9791 | 9.18922 | 9923 | 9.20261 |  |  |
| 9521 | 9.16126 | 9677 | 9.17751 | 9803 | 9.19044 | 9929 | 9.20322 |  |  |
| 9533 | 9.16251 | 9679 | 9.17771 | 98 II | 9.19126 | 9931 | 9.20342 |  |  |
| 9539 | 9.16314 | 9689 | 9.17875 | 9817 | 9. 19187 | 994I | 9.20442 |  |  |
| 9547 | 9.16398 | 9697 | 9.17957 | 9829 | 9. 19309 | 9949 | 9.20523 |  |  |
| $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\text {x }}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x | $\mathrm{e}^{\mathrm{x}}$ | x |

Coefficients for Computing,

$$
\mathrm{F}_{ \pm_{\mathrm{n}}}=\mathrm{F}_{0} \pm \mathrm{n} \omega\left[\mathrm{~F}_{0}^{\prime} \pm \frac{\mathrm{n}}{2} \alpha_{0}+\frac{\mathrm{n}^{2}}{6} \beta_{0} \pm \frac{\mathrm{n}}{12}\left(\frac{n^{2}}{2}-\mathrm{I}\right) \gamma_{0}\right] .
$$

| n | $\frac{\mathrm{n}^{2}}{6}$ | Diff. | $\frac{n}{12}\left(\frac{n^{2}}{2}-1\right)$ | Diff. | n | $\frac{n^{2}}{6}$ | Diff. | $\frac{n}{12}\left(\frac{n^{2}}{2}-1\right)$ | Diff. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.00 | +0.0000 |  | -0.0000 |  | 0.25 | +0.0104 |  | $\bigcirc 0.0202$ |  |
| . 01 | . 0000 | 0 | . 0008 | 8 | . 26 | . 0113 | 9 | . 0209 | 7 |
| . 02 | . 00001 | I | - . 0017 .0025 | 8 | . 27 | . 0122 | 9 | . 0217 | 7 |
| . 03 | . 00002 | I | . 0025 | 8 | . 28 | .0131 | 9 | . 02224 | 8 |
|  |  | 1 |  | 9 |  |  | 10 |  | 7 |
| 0.05 | +0.0004 | 2 | -0.0042 | 8 | 0.30 | +0.0150 |  | -0.0239 |  |
| . 06 | . 0006 | 2 | . 0050 | 8 | . 31 | . 0160 | 10 | . 0246 | 7 |
| . 07 | . 0008 | 3 | . 0058 | 8 | . 32 | . 0171 | 11 | . 0253 | 7 |
| . 08 | . 0011 | 3 | . 0066 | 9 | . 33 | . 0182 | II | . 0260 | 7 |
| . 09 | . 0014 | 3 | . 0075 | 8 | -34 | . 0193 | II | . 0267 | 7 |
| -. 10 | +0.0017 |  | -0.0083 |  | 0.35 | +0.0204 |  | -0.0274 |  |
| . II | . 0020 | 4 | . 0091 | 8 | . 36 | . 0216 | 12 | .0281 | 6 |
| . 12 | . 0024 | 4 | . 0099 | 8 | - 37 | . 0228 | 12 | . 0287 |  |
| . 13 | . 0028 | 5 | . 0107 | 9 | . 38 | . 0241 | 13 | . 0294 | 6 |
| . 14 | . 0033 | 5 | .OII6 | 8 | -39 | . 0254 | 13 | . 0300 | 7 |
| 0.15 | +0.0038 |  | -0.0124 |  | 0.40 | +0.0267 |  | $\bigcirc 0.0307$ |  |
| . 16 | . 0043 |  | . 0132 | 8 | . 41 | . 0280 | 13 | .0313 | 6 |
| . 17 | . 0048 | 6 | . 0140 | 8 | . 42 | . 0294 | 14 | . 0319 | 6 |
| . 18 | . 0054 | 6 | . 0148 | 7 | . 43 | . 0308 | 14 | . 0325 | 6 |
| . 19 | . 0060 | 7 | . 0155 | 8 | . 44 | . 0323 | 15 | .0331 | 6 |
| 0.20 | +0.0067 |  | -0.0163 |  | 0.45 | +0.0338 |  | $-0.0337$ |  |
| . 21 | . 0074 | 7 | . 0171 | 8 | . 46 | . . 0353 |  | . 0343 |  |
| . 22 | . 0081 | 7 | .0179 | 8 | . 47 | . 0368 | 15 | . 0348 | 5 |
| . 23 | . 0088 | 8 | . 0187 | 7 | - 48 | . 0384 | 16 | . 0354 | 5 |
| . 24 | . 0096 | 8 | . 0194 | 8 | -49 | . 0400 | 17 | . 0359 | 6 |
| 0.25 | +0.0104 |  | $\bigcirc .0202$ |  | 0.50 | +0.0417 |  | $\bigcirc .0365$ |  |

## TABLE VI

## THE GUDERMANNIAN

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.000 | 0.0000000 | I 0000 | $0^{\circ} 0000.00 .00$ | 206.26 |  |  |  |  |  |
| . 0.00 | .001 0000 | 100000 | 0 0326.26 | 205.26 | 0.050 | 0.0499792 .0509779 |  | 95 |  |
| . 002 | . 0020000 | I 0000 | 0 0652.53 | 206.26 | . 052 | .051 9766 | 9986 | 25840.94 | 99 |
| . 003 | . 0030000 | I 0000 | - 10 18.79 | 206.26 | . 053 | . 0529752 | 9986 | 30206.92 | 205.98 |
| . 004 | . 0040000 | I 0000 | 0 I3 45.06 | 206.26 | . 054 | .0539738 | 9985 | 30532.89 | 205.96 |
| 0.005 | 0.0050000 | 0000 | 0 I7 II. 32 | 206.26 | 0.055 | 0.0549723 | 9985 | 30858.85 | 205.95 |
| . 006 | . 0060000 | 0000 | - 2037.58 | 206.26 | . 056 | . 0559708 | 9984 | $\begin{array}{llll}3 & 12 & 24.80\end{array}$ | 205.94 |
| . 007 | . 0069999 | I 0000 | - 2403.84 | 206.26 | . 057 | . 0569692 | 9984 | 31550.73 | 205.93 |
| . 008 | . 0079999 | I 0000 | - 2730.10 | 206.26 | . 058 | . 0579575 | 9983 | 31916.66 | 205.92 |
| . 009 | . 0089999 | I 0000 | - 3056.36 | 206.26 | . 059 | . 0589658 | 9983 | 32242.57 | 205.91 |
| 0.010 | 0.0099998 | 99 | o 3422.61 |  | 0.060 | 0.0599640 | 82 | 32608.47 | 205.89 |
| . 011 | . 0109998 | 9999 | o 3748.87 | 206.25 | .061 | . 0609622 | 9981 | $\begin{array}{llll}3 & 29 & 34 \cdot 36\end{array}$ | 205.88 |
| . 012 | . OII 9997 | 9999 | 0 4115.12 | 206.25 | . 062 | .061 9603 | 9981 | 33300.23 | 205.87 |
| . 013 | . 0129996 | 9999 | - 4441.37 | 206.25 | . 063 | . 0629584 | 9980 | 33626.10 | 205.86 |
| . 014 | . O13 9995 | 9999 | 04807.61 | 206.24 | . 064 | . 0639564 | 9980 | 33951.94 | 205.84 |
| 0.015 | 0.014 999 | 99 | - 5133.86 | 206.24 | 0.065 | 0.0649543 | 79 | 34317.78 | 205.83 |
| . 016 | . 0159993 | 9999 | - 55 00.10 | 206.24 | . 066 | . 065952 I | 9978 | 34643.60 | 205.82 |
| . 017 | . O16 9992 | 9999 | - 5826.33 | 206.23 | . 067 | . 0669499 | 9978 | 35009.41 | 205.80 |
| . 018 | . 0179990 | 9998 | I OI 52.57 | 206.23 | . 068 | . 0679477 | 9977 | 353 35.21 | 205.79 |
| . 019 | . 0189989 | 9998 | I 05.18 .80 | 206.23 | . 069 | . 0689453 | 9976 | 35700.99 | 205.77 |
| 0.020 | 0.0199987 | 9998 | I 0845.02 |  | 0.070 | 0.0699429 | 997 | 40026.76 | 205.76 |
| . 021 | . 0209985 | 9998 | 11211.24 | 206.22 | . 07 I | . 0709404 | 9975 | 40352.51 | 205.75 |
| . 022 | . 0219982 | 9998 | I 1537.46 | 205.21 | . 072 | . 0719379 | 9974 | 40718.25 | 205.73 |
| . 023 | . 0229980 | 9997 | 11903.67 | 206.2I | . 073 | . 0729352 | 9973 | 4 Io 43.98 | 205.72 |
| . 024 | .0239977 | 9997 | I 2229.88 | 206.21 | . 074 | . 0739326 | 9973 | 41409.68 | $205 \cdot 70$ |
| 0.025 | 0.0249974 | 997 | I 2556.08 | 206.20 | 0.075 | 0.0749298 | 972 | 4 I7 35.38 | 205.69 |
| . 026 | . 0259971 | 9997 | I 2922.28 | 206.20 | . 076 | . 0759269 | 9971 | 4 21 OI. 06 | 205.67 |
| . 027 | . 0269967 | 9996 | I 3248.47 | 206. 19 | . 077 | . 0769240 | 9970 | 42426.72 | 205.65 |
| . 028 | . 0279963 | 9996 | I 3614.66 | 206. 18 | . 078 | . 0779210 | 9970 | 42752.37 | 205.64 |
| . 029 | . 0289959 | 9996 | I 3940.84 | 206.18 | . 079 | . 0789180 | 9969 | 43118.00 | 205.62 |
| 0.030 | 0.0299955 | 9995 | I 4307.02 | 206.17 | 0.080 | 0.0799148 | 9968 | 434 43.6I | 205.61 |
| . 031 | . 0309950 | 9995 | I 4633.19 | 206. 17 | .08I | .080 9116 | 9967 | 43809.21 | 205.59 |
| . 032 | .031 9945 | 9995 | I 4959.35 | 206. 16 | . 082 | .081 9083 | 9966 | 44134.79 | 205.57 |
| . 033 | .0329940 | 9995 | I 5325.50 | 206. 15 | . 083 | . 0829049 | 9966 | 44500.36 | 205.56 |
| . 034 | .0339935 | 9994 | I 5651.65 | 206. 15 | . 084 | .0839014 | 9965 | 44825.90 | 205.54 |
| 0.035 | 0.0349929 | 星 | 20017.79 | 206. I4 | 0.085 | 0.0848978 | 9964 | 4 5I 5I. 44 | 205.52 |
| . 036 | . 0359922 | 9994 | 20343.93 | 206. I3 | . 086 | . 0858942 | 9963 | 455 16.95 | 205.50 |
| . 037 | . 0369916 | 9993 | 20710.06 | 206. I2 | . 087 | . 0868905 | 9962 | 45842.44 | 205.49 |
| . 038 | .0379909 | 9993 | 2 IO 36.18 | 206. 12 | . 088 | . 0878866 | 996 I | 50207.92 | 205.47 |
| . 039 | . 038 990I | 9992 | 21402.29 | 206. II | . 089 | . 0888827 | 996 I | 50533.38 | 205.45 |
| 0.040 | 0.0399893 | 992 | $\begin{array}{llll}2 & 17 & 28.39\end{array}$ | 206. 10 | 0.090 | 0.0898787 | 9960 | 50858.82 | 205.43 |
| . 041 | . 0409885 | 9992 | 22054.49 | 206.09 | . 091 | .090 8747 | 9959 | 51224.25 | 205.41 |
| . 042 | .041 9877 | 9991 | 22420.58 | 206.08 | . 092 | .091 8705 | 9958 | 51549.65 | 205.39 |
| . 043 | . 0429868 | 9991 | 22746.65 | 206.07 | . 093 | . 0928662 | 9957 | 51915.03 | 205.38 |
| . 044 | . 0439858 | 9990 | 23112.72 | 206.07 | . 094 | . 0938619 | 9956 | 52240.40 | 205.36 |
| 0.045 | 0.0449848 | 9990 | 23438.79 | 206.06 | 0.095 | 0.0948574 | 9955 | 52605.75 | 205.34 |
| . 046 | . 0459838 | 9989 | 23804.84 | 206.05 | . 096 | . 0958529 | 9954 | 529 31.08 | 205.32 |
| . 047 | . 0469827 | 9989 | 24130.88 | 206.04 | . 097 | . 0968482 | 9953 | 53256.38 | 205.30 |
| . 048 | . 0479816 | 9988 | 24456.91 | 206.03 | . 098 | . 0978435 | 9952 | 55621.67 | 205.28 |
| . 049 | . 0489804 | 9988 | 24822.93 | 206.02 | . 099 | .0988387 | 0051 | 53946.94 | 205.26 |
| 0.050 | 0.0499792 | 9988 | 25148.95 | 206.01 | 0.100 | 0.0998337 | 9950 | 543 12.19 | 205.24 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega \mathrm{s}$ ¢ $\mathrm{ch} u$ | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | w sechu | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-90^{\circ}$ | $\omega$ sech |

The Gudermannian.

| u | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | ○ ' " | " |  |  |  | $8^{\circ}{ }^{\prime \prime}{ }^{\prime \prime}$ | " |
| 0.100 | 0.0998337 | 9950 | 54312.19 | 205.24 | 0.150 | 0.149 4406 | 9889 | 83344.35 | 203.97 |
| . IOI | . 1008287 | 9949 | 54637.42 | 205.22 | . 151 | . I50 4294 | 9887 | 83708.30 | 203.94 |
| . 102 | . IO1 8236 | 9948 | 55002.62 | 205.20 | . 152 | . I5I 418I | 9886 | 84032.22 | 203.90 |
| . 103 | . 1028 I 84 | 9947 | 55327.81 | 205.18 | . 153 | . I52 4065 | 9884 | 843 56.1I | 203.87 |
| . 104 | . 1038130 | 9946 | 55652.97 | 205.15 | . 154 | . I53 3949 | 9883 | 847 19.96 | 203.84 |
| 0. 105 | 0.1048076 | 9945 | 60018.12 | 205.13 | 0.155 | 0.154383 I | 988 I | 85043.79 | 203.81 |
| . 106 | . 1058021 | 9944 | 60343.24 | 205. 11 | . 156 | . I55 37II | 9880 | 85407.59 | 203.78 |
| . 107 | . 1067964 | 9943 | 60708.34 | 205.09 | . 157 | . I56 3590 | 9878 | 85731.35 | 203.75 |
| . 108 | . 1077907 | 9942 | 6 10 33.42 | 205.07 | . I58 | . I573467 | 9876 | 90055.08 | 203.72 |
| . 109 | . 1087848 | 994 I | 6 I3 58.48 | 205.05 | . 159 | . I58 3343 | 9875 | 90418.78 | 203.68 |
| 0.110 | 0.1097788 | 9940 | 6 I7 23.51 | 205.02 | 0.160 | O.I59 3217 | 9873 | 90742.45 | 203.65 |
| . III | . IIO 7728 | 9939 | 62048.52 | 205.00 | . 161 | . 1603089 | 9872 | 9 II 06.09 | 203.62 |
| . I I2 | . II I 7656 | 9938 | 62413.51 | 204.98 | . 162 | . I6I 2960 | 9870 | 9 I4 29.69 | 203.59 |
| . II3 | . 1127603 | 9936 | 62738.48 | 204.95 | . 163 | . 1622830 | 9869 | 91753.26 | 203.55 |
| . II4 | . II3 7539 | 9935 | 63103.42 | 204.93 | . I64 | . 1632697 | 9867 | 92116.80 | 203.52 |
| O.II5 | O.II4 7474 | 9934 | 63428.34 | 204.91 | 0.165 | 0.164 2564 | 9865 | 92440.31 | 203.49 |
| . II6 | . II5 7407 | 9933 | 63753.24 | 204.88 | . 166 | . 1652428 | 9864 | 92803.78 | 203.46 |
| . 117 | . 1167340 | 9932 | 641 I8.II | 204.86 | . 167 | . 1662291 | 9862 | 93127.22 | 203.42 |
| . 118 | . 1177271 | 9931 | 64442.96 | 204.84 | . 168 | . 1672153 | 986 I | 93450.62 | 203.39 |
| . 119 | . 1187201 | 9930 | 64807.78 | 204.81 | . 169 | . 168.2012 | 9859 | 93813.99 | 203.35 |
| 0.120 | 0.119 7130 | 928 | 65132.59 | 204.79 | 0.170 | 0.1691870 | 9857 | 94137.33 | $203 \cdot 32$ |
| . 121 | . 1207058 | 9927 | $65457 \cdot 36$ | 204.76 | .171 | . 1701727 | 9856 | 94500.63 | 203.29 |
| . 122 | . I2I 6985 | 9926 | 65822.11 | 204.74 | . 172 | .171 I58I | 9854 | 94823.90 | 203.25 |
| . 123 | . 1226910 | 9925 | 7 OI 46.84 | 204.71 | . 173 | . I72 I434 | 9852 | 95147.14 | 203.22 |
| . 124 | . 1236834 | 9924 | 70511.54 | 204.69 | . 174 | . 173 I286 | c85I | 95510.33 | 203.18 |
| 0.125. | 0.1246757 | 9922 | 70836.22 | 204.66 | 0.175 | 0.174 1136 | 9849 | 9.5833 .50 | 203. 15 |
| . 126 | . I25 6679 | 992 I | 7 I2 00.87 | 204.64 | . 176 | . I75 0983 | 9847 | IO OI 56.63 | 203. I 1 |
| . 127 | . 1266600 | 9920 | 7 I5 25.49 | 204.61 | . 177 | . 1760830 | 9845 | 100519.72 | 203.08 |
| . 128 | . 1276519 | 9919 | 7 I8 50.09 | 204.59 | . 178 | . 1770674 | 9844 | 100842.78 | 203.04 |
| . 129 | . 1286437 | 9917 | 72214.67 | $204 \cdot 56$ | . 179 | . 1780517 | 9842 | 101205.80 | 203.00 |
| 0.130 | O.I29 6354 | 9916 | 72539.22 | 204.53 | 0.180 | 0.179 0358 | 9840 | IO $15 \quad 28.78$ | 202.97 |
| . I3I | . I30 6269 | 9915 | 72903.74 | 204.51 | . 181 | . 180 0197 | 9838 | 10 1851.73 | 202.93 |
| . 132 | . 13I 6i83 | 9913 | 73228.23 | 204.48 | . 182 | . I81 0035 | 9837 | 102214.65 | 202.90 |
| . I33 | . 1326096 | 9912 | 73552.70 | 204.45 | . 183 | . I8I 987I | 9835 | IO 2537.52 | 202.86 |
| . 134 | . 1336008 | 99 II | 73917.14 | 204.43 | . 184 | . 1829705 | 9833 | 102900.35 | 202.82 |
| 0. I35 | 0.134 5918 | 9910 | 742 41.55 | 204.40 | 0.185 | 0.1839537 | 983 I | IO 3223.17 | 202.78 |
| . 136 | . I35 5827 | 9908 | 74605.94 | $204 \cdot 37$ | . 186 | . 1849367 | 9829 | IO 3545.93 | 202.75 |
| . 137 | . I36 5734 | 9907 | 74930.29 | 204. 34 | . 187 | . 1859196 | 9828 | Io 3908.66 | 202.71 |
| . I38 | . 1375641 | 9906 | 75254.62 | 204. 32 | . 188 | . 1869022 | 9826 | 104231.35 | 202.67 |
| . 139 | . I38 5545 | 9904 | $7 \quad 56$ I8.93 | 204. 29 | . 189 | . 1878847 | 9824 | 10 4554.01 | 202.63 |
| 0. 140 | O. I39 5449 | 9903 | 75943.20 | 204.26 | 0.190 | 0. 1888670 | 9822 | 10 49 16.62 | 202.60 |
| . 141 | . 140535 I | 9901 | 80307.45 | 204.23 | . I9I | . 1898492 | 9820 | 105239.20 | 202.56 |
| . I42 | . I4I 5252 | 9900 | 80631.66 | 204.20 | . 192 | . 1908311 | 9818 | IO 56 O1. 74 | 202.52 |
| . I43 | . I42 5I5I | 9899 | 80955.85 | 204.17 | . 193 | . 1918129 | 9817 | IO 5924.24 | 202.48 |
| . 144 | . 1435049 | 9897 | 8 I3 20.01 | 204. 14 | . 194 | . 1927944 | 9815 | II 0246.71 | 202.44 |
| 0. I45 | 0.144 4946 | 9896 | 8 16 44.14 | 204. 12 | 0. 195 | 0.193 7758 | 9813 | II 0609.13 | 202.40 |
| . 146 | . 145484 I | 9894 | 82008.24 | 204.09 | . 196 | - 1947570 | 98II | II 0931.51 | 202.37 |
| . 147 | . I46 4734 | 9893 | $\begin{array}{llllllllllll}8 & 23 & 32.31\end{array}$ | 204.06 | . 197 | . 1957380 | 9809 | II 1253.86 | 202.33 |
| . 148 | . 1474626 | 9891 | 82656.35 | 204.03 | . 198 | . 1967188 | 9807 | II I6 16.17 | 202.29 |
| . 149 | . 1484517 | 9890 | 83020.36 | 204.00 | . 199 | . 1976994 | 9805 | I I I9 38.43 | 202.25 |
| 0.150 | 0. 1494406 | 9889 | $83344 \cdot 35$ | 203.97 | 0.200 | 0.1986798 | 9803 | II 2300.66 | 202.21 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathbf{F}_{0}{ }^{\text {n }}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.200 | 0. 1986798 | 9803 | II 2300.66 | 202.21 |  |  |  |  |  |
| . 201 | . 1996601 | 9801 | II 2622.85 | 202.17 |  |  |  |  |  |
| . 202 | . 2006401 | 9799 | II 2944.99 | 202.13 |  |  |  |  |  |
| . 203 | . 2016200 | 9797 | II 33 07.10 | 202.09 | . 253 | . 2503434 | 9688 | 2037.02 |  |
| . 204 | . 2025996 | 9795 | II 3629.17 | 202.05 | . 254 | . 251 I 3 I 2 I | 9686 | $14 \quad 23 \quad 56.83$ | 199.79 |
| 0.205 | 0.2035790 | 9794 | II 39 5I.I9 | 202.01 | 0.255 | 0.2522805 | 9683 | $14 \quad 2716.59$ |  |
| . 206 | . 2045583 | 9792 | II 43 I3.18 | 201.96 | . 256 | . 2532488 | 968 I | 143036.31 | 199.69 |
| . 207 | . 2055374 | 9790 | II 4635.12 | 201.92 | . 257 | . 2542167 | 9679 | 143355.97 | 199.64 |
| . 208 | . 2065162 | 9788 | II 4957.02 | 201.88 | . 258 | . 255 I845 | 9676 | $\begin{array}{lllllllllllllllllllll}14 & 37 & 15.58\end{array}$ | 199.59 |
| . 209 | . 2074949 | 9786 | II 5318.89 | 201.84 | . 259 | . 256 I520 | 9674 | 144035.14 | 199.53 |
| 0.210 | 0.2084733 | 978 | II 5640.71 | 201.80 | 0.260 | 0.257 II92 | 9671 | 144354.65 | 199.48 |
| . 211 | . 20945 I 5 | 978 I | 120002.48 | 201.76 | . 261 | . 2580862 | 9669 | I4 47 14.10 | 199.43 |
| . 2 | . 2104296 | 9779 | 1203124.22 | 201.71 | . 252 | . 2590530 | 9666 | 145033.51 | 199.38 |
| . 213 | . 2II 4074 | 9777 | 120645.91 | 201.67 | . 263 | . 260 0195 | 9664 | 145352.87 | 199.33 |
| . 214 | . 212385 I | 9775 | 121007.56 | 201.63 | . 264 | . 2609857 | 9661 | 145712.18 | 199.29 |
| 0.215 | 0.2133625 | 9773 | 121329.17 | 201. 59 | 0.265 | 0.261 9518 | 9659 | 150031.43 |  |
| . 216 | . 2143397 | 9771 | 12 I6 50.74 | 201. 54 | . 266 | .2629175 | 9656 | 150350.63 | 199.19 |
| . 217 | . 2153167 | 9769 | 122012.26 | 201. 50 | . 267 | . 2638830 | 9654 | 150709.78 | 199.13 |
| . 218 | . 2162935 | 9767 | $12 \begin{array}{llll}12 & 23 & 33.74\end{array}$ | 201. 46 | . 268 | . 2648483 | 9651 | 15 IO 28.88 | 199.08 |
| .219 | . 2172701 | 9765 | I2 2655.18 | 201.42 | . 269 | . 265 8I33 | 9649 | I5 13 47.93 | 199.03 |
| 0.220 | 0.2182465 | 976 | I2 30 | 201.37 | 0.270 | 0.266778 I | 9646 | 151706.92 |  |
| .22I | . 2192227 | 9761 | $12333 \begin{array}{lll}12 & 37.92\end{array}$ | 201. 33 | . 271 | . 2677425 | 9644 | I5 2025.86 | 198.93 |
| . 222 | . 2201986 | 9759 | 123659.23 | 201.28 | . 272 | . 2687068 | 9641 | I5 2344.75 | 198.87 |
| . 223 | . 221 I744 | 9756 | 124020.49 | 201.24 | . 273 | . 2696708 | 9639 | $15 \quad 2703.59$ | 198.82 |
| . 224 | . 222 I499 | 9754 | I2 43 4I.7I | 201.20 | . 274 | . 2706345 | 9636 | 153022.37 | 198.77 |
| 0.225 | 0.2231252 | 9752 | 124702.88 | 201. 15 | 0.275 | 0.2715980 | 9633 | 153341.10 | 198.71 |
| . 226 | . 2241003 | 9750 | 125024.01 | 201. II | . 276 | . 2725612 | 9631 | 153659.78 | 198.66 |
| .227 | . 2250752 | 9748 | I2 53345.10 | 201. 06 | . 277 | . 2735242 | 9628 | 1540 18.41 | 198.61 |
| . 228 | . 2260499 | 9746 | 125706.14 | 201. 02 | . 278 | . 2744868 | 9626 | 154336.98 | 198.55 |
| . 229 | . 2270243 | 9743 | I3 0027.13 | 200 | . 279 | .2754493 | 9623 | I5 4655.49 | 198.50 |
| 0.230 | 0.2279986 | 9741 | I3 0348.08 | 200.93 | 0.280 | 0.2764114 | 9620 | 155013.95 | 198.45 |
| . 231 | . 2289726 | 9739 | 130708.99 | 200.88 | . 28I | . 2773734 | 9618 | 155332.36 | 198.38 |
| . 232 | . 2299464 | 9737 | I3 10 29.85 | 200.84 | . 282 | .2783350 | 96 I 5 | I5 5650.72 | 198.33 |
| .233 | . 2309199 | 9735 | I3 13 50.66 | 200.79 | .283 | . 2792964 | 9612 | 160009.02 | 198.27 |
| . 234 | . 2318933 | 9732 | I3 17 II. 42 | 200.74 | . 284 | . 2802575 | 9610 | 160327.26 | 198.22 |
| 0.235 | 0.2328664 | 9730 | I3 2032.15 | 200.70 | 0.285 | 0.28I 2184 | 9607 | 160645.45 | 198.16 |
| . 236 | . 2338393 | 9728 | I3 23252.82 | 200.65 | . 286 | . 2821789 | 9604 | 16 10 03.58 | 198. 11 |
| . 237 | . 234 8120 | 9726 | 132713.45 | 200.60 | . 287 | . 283 I393 | 9602 | 16 I3 21.66 | 198.05 |
| . 238 | .2357844 | 9723 | $13 \quad 30 \quad 34.03$ | 200.56 | . 288 | . 2840993 | 9599 | 161639.69 | 198.00 |
| . 239 | .2367566 | 9721 | I3 $33 \begin{array}{lll} & 54.56\end{array}$ | 200.51 | . 289 | .2850591 | 9596 | I6 19 57.66 | 197.94 |
| 0.240 | 0.2377286 | 9719 | $\begin{array}{llll}13 & 37 & 15.05\end{array}$ | 200.46 | 0.290 | 0.2860186 | 594 | $16 \quad 23 \quad 15.57$ | 197.89 |
| . 241 | . 2387004 | 9716 | I3 $40 \begin{array}{lll}35.49\end{array}$ | 200.42 | . 291 | . 2869778 | 9591 | 162633.43 | 197.83 |
| . 242 | . 2396719 | 9714 | I3 4355.88 | 200.37 | .292 | . 2879368 | 9588 | 162951.23 | 197.77 |
| . 243 | . 2406432 | 9712 | I3 4716.23 | 200.32 | . 293 | . 2888955 | 9586 | I6 3308.97 | 197.72 |
| . 244 | . 24I 6I43 | 9710 | I3 5036.53 | 200.27 | .294 | . 2898539 | 9583 | I6 3626.66 | 197.66 |
| 0.245 | 0.242585 I | 9707 | 1315356.77 | 200.23 | 0.295 | 0.2908121 | 9580 | I6 3944.30 | 197.60 |
| . 246 | . 2435557 | 9705 | 135716.98 | 200. 18 | . 296 | . 2917699 | 9577 | 164301.87 | 197.55 |
| . 247 | . 244 526I | 9703 | 140037.13 | 200. 13 | . 297 | . 2927275 | 9575 | $1646 \quad 19.39$ | 197.49 |
| . 248 | . 2454962 | 9700 | 140357.23 | 200.08 | . 298 | . 2936849 | 9572 | I6 4936.85 | 197.43 |
| . 249 | . 2464661 | 9698 | 140717.29 | 200.03 | . 299 | .2946419 | 9569 | 165254.26 | 197.38 |
| 0.250 | 0.2474358 | 9695 | 14 IO $37 \cdot 30$ | 199.98 | 0.300 | 0.2955987 | 9566 | 1656 II .60 | $197 \cdot 32$ |
| u | $2 \tan ^{-1}\left(e^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech $u$ | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | $\omega$ sech u |

SMITHSONIAN TABLES

The Gudermannian.

| u | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 0566 | $16^{\circ} 56^{\prime}$ II " 60 | 197 |  |  |  | 19 $39^{\prime} 22.13$ | 19 ${ }^{\prime \prime}$ |
| 0.300 | 0.2955987 | 9566 | 165011.60 | 19 | 0.350 | 0.3430655 | 9417 | 193922.34 | 94.25 |
| . 301 | . 2965552 | 9563 | I6 5928.89 | 197.26 | .351 | . 344007 I | 9414 | 194236.55 | 194.18 |
| . 302 | . 297 5114 | 9561 | I7 0246.13 | 197.20 | - 352 | - 3449483 | 941 I | 194550.70 | 194. 11 |
| . 303 | . 2984673 | 9558 | 170603.30 | 197. 15 | . 353 | - 3458893 | 9408 | 194904.78 | 194.05 |
| . 304 | . 2994229 | 9555 | 170920.42 | 197.09 | - 354 | . 3468299 | 9405 | 195218.80 | 193.98 |
| 0.305 | 0.3003783 | 9552 | I7 I2 37.48 | 197.03 | 0.355 | 0.3477702 | 9401 | 195532.75 | 193.92 |
| . 306 | . 3013334 | 9549 | 17 I5 54.48 | 196.97 | . 356 | . 3487101 | 9398 | I9 5846.63 | 193.85 |
| . 307 | . 3022882 | 9547 | 1719 II. 42 | 196.91 | - 357 | . 3496498 | 9395 | 200200.45 | 193.78 |
| . 308 | . 3032427 | 9544 | $17 \quad 2228.30$ | 196.85 | -358 | . 3505891 | 9392 | 200514.20 | 193.72 |
| . 309 | .3041969 | 954 I | 172545.12 | 196.79 | . 359 | .351 528I | 9388 | $20 \quad 0827.88$ | 193.65 |
| 0.310 | 0.3051509 | 9538 | I7 29 O1. 89 | 196.74 | 0.360 | 0.3524668 | 9385 | 20 II 41.50 | 193.58 |
| . 311 | . 3061045 | 9535 | $17{ }_{17} 3218.60$ | 196.68 | . 36 I | . 3534052 | 9382 | 20 I4 55.05 | 193.52 |
| . 312 | . 3070579 | 9532 | I7 3535.24 | 196.62 | . 362 | . 3543432 | 9378 | 20.1808 .54 | 193.45 |
| -313 | . 308 0110 | 9529 | 173851.83 | 196.56 | . 363 | . 3552809 | 9375 | 202121.95 | 193.38 |
| . 314 | . 3089638 | 9526 | 174208.36 | 196.50 | . 364 | . 3562183 | 9372 | $202435 \cdot 30$ | 193.32 |
| 0.315 | 0.3099163 | 9524 | I7 $45 \quad 24.83$ | 196. 4 | 0.365 | 0.3571554 | 9369 | 202748.59 | 193.25 |
| . 316 | . 3108685 | 9521 | I7 4841.23 | 196.38 | . 366 | . 3580921 | 9366 | 203101.80 | 193.18 |
| . 317 | .3II 8204 | 9518 | I7 5157.58 | 196.32 | . 367 | . 3590285 | 9362 | $20 \quad 3414.95$ | 193.II |
| . 318 | .312 772I | 9515 | $17 \quad 5513.87$ | 196.26 | . 368 | . 3599646 | 9359 | 203728.03 | 193.05 |
| . 319 | . 3137234 | 9512 | I7 58 30.10 | 196.20 | . 369 | . 3609003 | 9356 | 204041.04 | 192.98 |
| 0.320 | 0.3146744 | 9509 | I8 oi 46.26 | 196.14 | 0.370 | 0.361 8358 | 9352 | 204353.98 | 192.91 |
| . 32 I | .315 62.52 | 9506 | 180502.37 | 196.08 | . 371 | . 3627708 | 9349 | 204706.86 | 192.84 |
| . 322 | . 3165757 | 9503 | $\begin{array}{llllll}18 & 08 & 18.42\end{array}$ | 196.01 | . 372 | . 3637056 | 9346 | 2050.19 .66 | 192.77 |
| . 323 | -3175258 | 9500 | I8 II 34.40 | 195.95 | - 373 | . 3646400 | 9343 | 205332.40 | 192.70 |
| . 324 | . 3184757 | 9497 | 181450.32 | 195.89 | -374 | . 3655741 | 9339 | 205645.07 | 192.63 |
| 0.325 | O.319 4252 | 9494 | 18 18 06. 19 | 195.83 | 0.375 | 0.3665078 | 9336 | $20 \quad 5957.67$ | 192.57 |
| . 326 | . 3203745 | 9491 | 182121.99 | 195.77 | - 376 | . 3674413 | 9332 | 210310.20 | 192.50 |
| . 327 | . 3213235 | 9488 | I8 2437.72 | 195.71 | . 377 | . 3683743 | 9329 | 21 0622.66 | 192.43 |
| . 328 | . 3222721 | 9485 | I8 $27 \quad 53.40$ | 195.65 | - 378 | . 3693071 | 9326 | 210935.05 | 192.36 |
| . 329 | . 3232205 | 9482 | I8 3I 09.02 | 195.58 | - 379 | - 3702395 | 9322 | 211247.38 | 192.29 |
| 0.330 | 0.3241686 | 9479 | I8 3424.57 | 195.52 | 0.380 | 0.371 1716 | 9319 | 21 I5 59.63 | 192.22 |
| . 331 | . 325 I163 | 9476 | I8 3740.06 | 195.46 | .381 | . 3721033 | 9316 | 21 I9 II. 82 | 192.15 |
| . 332 | . 3260638 | 9473 | I8 $40 \quad 55.49$ | 195.40 | . 382 | . 3730347 | 9312 | 212223.93 | 192.08 |
| . 333 | . 327 O1 10 | 9470 | I8 4410.85 | 195.33 | . 383 | - 3739658 | 9309 |  | 192.01 |
| . 334 | . 3279578 | 9467 | I8 47 26.16 | 195.27 | . 384 | - 3748965 | 9305 | 212847.95 | 191.94 |
| 0.335 | 0.3289044 | 946 | I8 504 I .40 | 195.21 | 0.385 | 0.3758268 | 9302 | 21 31 59.85 | 191.87 |
| . 336 | . 3298506 | 9461 | I8 5356.57 | 195. 15 | . 386 | . 3767569 | 9299 | 213511.68 | 191. 80 |
| - 337 | . 3307965 | 9458 | I8 57 II .69 | 195.08 | . 387 | . 3776866 | 9295 | 2138123.45 | 191. 73 |
| . 338 | . 3317422 | 9455 | $19 \quad 00 \quad 26.74$ | 195.02 | . 388 | . 378 6159 | 9292 | 2I 4135.14 | 191. 66 |
| . 339 | . 3326875 | 9452 | 190341.72 | 194.95 | . 389 | - 3795449 | 9288 | 2I 4446.76 | 191. 59 |
| 0.340 | 0.3336325 | 9449 | F9 0656.65 | 194.89 | 0.390 | 0.3804736 | 9285 | 21 4758.3 I | 191.51 |
| . 341 | - 3345772 | 9445 | I9 10 II.50 | 194.83 | .39I | -381 4019 | 928 I | 21 51 09.79 | 191. 44 |
| . 342 | . 3355216 | 9442 | 19 I3 26.30 | 194.76 | - 392 | . 3823299 | 9278 | 215421.20 | 191.37 |
| . 343 | . 3364657 | 9439 | 19 I6 41.03 | 194.70 | - 393 | . 3832575 | 9275 | 215732.53 | 191. 30 |
| - 344 | . 3374095 | 9436 | 19 I9 55.70 | 194.63 | - 394 | -384 I848 | 927 I | 220043.80 | 191.23 |
| 0.345 | 0.3383529 | 9433 | 192310.30 | 194.57 | 0.395 | 0.385 1117 | 9268 | 220354.99 | 191.16 |
| . 346 | . 339 296i | 9430 | 192624.84 | 194.51 | . 396 | . 3860383 | 9264 | 220706.11 | 191.09 |
| - 347 | . 3402389 | 9427 | 192939.31 | 194.44 | - 397 | - 3869645 | 9261 | 22 10 17.16 | 191.OI |
| . 348 | . 341 I8I4 | 9424 | 193253.72 | 194.38 | - 398 | . 3878904 | 9257 | 22 I3 28. I4 | 190.94 |
| . 349 | . 3421236 | 9420 | 193608.06 | 194.31 | . 399 | - 388 8159 | 9254 | 22 I6 39.04 | 190.87 |
| 0.350 | 0.3430655 | 9417 | I9 3922.34 | 194.25 | 0.400 | 0.389741 I | 9250 | 22 I9 49.88 | 190.80 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ |  | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega \mathrm{s}$ | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

## The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | $\mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.400 | 0.3897411 | 9250 | $22^{\circ} 19^{\prime} 449^{\prime \prime} .88$ | 190.80 | 0.450 | 0.4355388 | 9066 |  |  |
| . 401 | . 3906660 | 9247 | 222300.64 | 190.72 | .45I | . 4364453 | 9063 | 250023.3 I |  |
| . 402 | -3915904 | 9243 | 2226 II. 32 | 190.65 | . 452 | . 4373514 | 9059 | 250330.20 | 186.85 |
| .403 | - 3925146 | 9240 | 2229 2I.94 | 190.58 | . 453 | . 4382571 | 9055 | 250637.01 | 186.77 |
| . 404 | - 3934383 | 9236 | 223232.48 | 190.51 | . 454 | . 439 I624 | 9051 | 250943.74 | 186.69 |
| 0.405 | 0.3943618 | 9232 | 223542.95 | 190.43 | 0.455 | 0.4400673 | 9047 | 25.1250 .39 | I86.6I |
| . 406 | . 3952848 | 9229 | $22 \quad 38 \quad 53.35$ | 190.36 | . 456 | . 4409718 | 9043 | 25 I5 56.96 | I86.53 |
| . 407 | . 3962075 | 9225 | 224203.67 | 190.29 | . 457 | . 4418759 | 9040 | $25 \quad 1903.46$ | 186.45 |
| . 408 | . 3971299 | 9222 | $2245 \quad 13.92$ | 190.21 | . 458 | . 4427797 | 9036 | 252209.87 | I86.37 |
| . 409 | . 3980519 | 9218 | 224824.09 | 190. 14 | . 459 | . 4436831 | 9032 | $25 \quad 2516.20$ | I86.29 |
| 0.410 | 0.3989735 | 9215 | 225134.19 | 190.06 | 0.460 | 0.4445861 | 9028 | 252822.46 | I86.2I |
| . 41 II | . 3998948 | 9211 | 225444.22 | 189.99 | . 46 I | . 4454886 | 9024 | $25 \quad 3128.63$ | 186. 13 |
| . 412 | . 400 8157 | 9207 | 225754.18 | 189.92 | . 462 | . 4463909 | 9020 | 253434.72 | 186.05 |
| . 413 | . 4017363 | 9204 | 23 OI 04.06 | I89.84 | . 463 | . 4472927 | 9016 | 253740.74 | I85.97 |
| . 414 | .4026565 | 9200 | 230413.86 | 189.77 | . 464 | . 448 1941 | 9012 | 254046.67 | 185.89 |
| 0.415 | 0.4035763 | 9197 | $2307 \quad 23.59$ | 189.69 | 0.465 | 0.4490951 | 9008 | 254352.52 | I85.8I |
| . 416 | . 4044958 | 9193 | 23 10 33.25 | I89.62 | . 466 | . 4499958 | 9004 | 254658.29 | I85.73 |
| .417 | . 4054149 | 9189 | $\begin{array}{llll}23 & 13 & 42.83\end{array}$ | 189.54 | . 467 | . 4508960 | 9001 | 255003.98 | 185.65 |
| . 418 | . 4063337 | 9186 | 23 I6 52.34 | 189.47 | . 468 | . 4517959 | 8997 | $25 \quad 5309.59$ | I85.57 |
| . 419 | . 407252 I | 9182 | 232001.77 | 189.39 | . 469 | . 4526954 | 8993 | 2556 15.12 | 185.49 |
| 0.420 | 0.408 1701 | 917 | 2323 II. I3 | 189.32 | 0.470 | 0.4535944 | 8989 | $25 \quad 5920.57$ | I85.41 |
| . 42 I | . 4090878 | 9175 | 232620.41 | 189.24 | . 471 | . 454 493I | 8985 | 260225.93 | I85.33 |
| . 422 | .410 0051 | 9171 | 232929.62 | 189.17 | . 472 | . 4553914 | 8,81 | 260531.22 | I85.24 |
| . 423 | . 4109220 | 9168 | 233238.75 | 189.09 | . 473 | . 4562893 | 8977 | 260836.42 | 185.16 |
| . 424 | .411 8385 | 9164 | 233547.8 I | 189.02 | . 474 | . 4571858 | 8973 | 26 II 41.54 | 185.08 |
| 0.425 | 0.4127548 | 9160 | 233856.79 |  | 0.475 | 0.4580839 | 8069 | 261446.58 | 185.00 |
| . 426 | . 4136706 | 9157 | 234205.69 | 188.87 | . 476 | . 4589806 | 8965 | 261751.54 | 184.92 |
| . 427 | . 4145861 | 9153 | $\begin{array}{lllll}23 & 45 & 14.52\end{array}$ | 188.79 | .477 | . 4598769 | 8961 | 262056.42 | 184.84 |
| . 428 | .4155012 | 9149 |  | 188.71 | . 478 | . 4607728 | 8957 | 2624 OI. 21 | 184.75 |
| . 429 | . 4164159 | 9145 | 23 51 31.95 | 188.64 | . 479 | . 4616683 | 8953 | 262705.93 | 184.67 |
| 0.430 | 0.4173303 | 9142 | 235440.55 | 188.56 | 0.480 | 0.4625634 | 8949 | 263010.56 | 184.59 |
| . 43 I | . 4182443 | 9138 | 235749.07 | 188.49 | .481 | . 463458 I | 8945 | 2633 I5.10 | 184.5I |
| . 432 | . 4191579 | 9134 | 240057.52 | I88.41 | . 482 | . 4643524 | 8941 | $26 \quad 3619.57$ | 184.42 |
| . 433 | . 4200711 | 9131 | 240405.89 | 188.33 | . 483 | . 4652464 | 8937 | 263923.95 | 184.34 |
| . 434 | . 4209840 | 9127 | 2407 I4.18 | 188.26 | . 484 | . 466 I 399 | 8933 | 264228.25 | 184.26 |
| 0.435 | 0.421 8965 | 9123 | 241022.40 | 188.18 | 0.485 | 0.4670330 | 8929 | $2645 \quad 32.47$ | I84. 18 |
| . 436 | . 4228086 | 9119 | $\begin{array}{lllll}24 & 13 & 30.54\end{array}$ | 188. 10 | . 485 | . 4679257 | 8925 | 264836.60 | 184.09 |
| . 437 | . 4237204 | -9116 | 241638.60 | 188.02 | .487 | . 468 8180 | 8921 | 265140.65 | I84.01 |
| . 438 | . 4246318 | 91.12 | 241946.59 | 187.95 | . 488 | .4697099 | 8917 | 265444.62 | 183.93 |
| . 439 | . 4255428 | 9108 | 242254.50 | 187.87 | . 489 | . 4706014 | 8013 | 265748.50 | I83.84 |
| 0.440 | 0.4264534 | 9104 | $24 \quad 2602.33$ | 187.79 | 0.490 | 0.4714925 | 8909 | 270052.31 | 183.76 |
| . 441 | . 4273636 | 910I | 242910.08 | 187.71 | . 49 I | . 4723832 | 8905 | 270356.02 | 183.68 |
| . 442 | . 4282735 | 9097 | 2432 17.75 | 187.64 | . 492 | . 4732735 | 8901 | 270659.65 | I83.59 |
| . 443 | . 4291830 | 9093 | $24 \quad 35 \quad 25 \cdot 35$ | 187.56 | . 493 | . 4741633 | 8897 | 271003.21 | 183.5I |
| . 444 | . 430092 I | co89 | $2438 \quad 32.87$ | 187.48 | . 494 | . 4750528 | 8893 | 27 I3 06.68 | I83.42 |
| 0.445 | 0.4310009 | 9085 | 244140.31 | 187.40 | 0.495 | 0.4759419 | 8889 | 271610.06 | 183.34 |
| . 446 | . 4319092 | 9082 | 244447.67 | 187.32 | . 496 | . 4768305 | 8885 | $27 \quad 1913.36$ | 183.26 |
| . 447 | . 432 8I72 | 9078 | 244754.96 | 187.24 | . 497 | . 4777188 | 8880 | 272216.57 | 183.17 |
| . 448 | . 4337248 | 9074 | 245102.16 | 187.17 | . 498 | . 4786066 | 8876 | $\begin{array}{llll}27 & 25 & 19.70\end{array}$ | 183.09 |
| . 449 | . 4346320 | 9070 | 245409.29 | 187.09 | . 499 | . 479494 I | 8872 | $27 \quad 28 \quad 22.75$ | 183.00 |
| 0.450 | 0.4355388 | 9066 | $2457 \quad 16.34$ | 187.01 | 0.500 | 0.48038 II | 8868 | 273125.71 | 182.92 |
| $u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ |  | $2 \tan ^{-1}\left(e^{u}\right)-90^{2}$ | $w$ sech u | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

Smithsonian tables

## The Gudermannian.

| u | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 8868 | 27 31 25.71 | 182.92 |  |  | 8657 | 0203.92 |  |
| 0.500 | 0.4803811 | 8868 | 273125.71 |  | 0.550 | 0.5241996 | 8657 | $30 \quad 0203.92$ | 57 |
| . 501 | . 4812677 | 8864 | $\begin{array}{llll}27 & 34 & 28.59\end{array}$ | 182.83 | 551 | . 5250651 | 8653 | $\begin{array}{llll}30 & 05 & 02.45\end{array}$ | 178.48 |
| . 502 | . 4821539 | 8860 | 273731.38 | 182.75 | . 55.2 | . 5259302 | 8649 | 300800.88 | 178.39 |
| . 503 | . 4830397 | 8856 | 274034.09 | 182.67 | . 553 | . 5267948 | 8644 | 301059.23 | 178.30 |
| . 504 | . 483 925I | 8852 | 274336.71 | I82.58 | . 554 | . 5276590 | 8640 | 30 I3 57.48 | I78.2I |
| 0.505 | 0.4848100 | 8848 | 274639.25 | 182.50 | 0.555 | 0. 5285228 | 8636 | 30 16 55.65 | 178.12 |
| . 506 | . 4856946 | 8844 | 2749 41.7.0 | 182.41 | . 556 | . 529 386I | 8631 | 301953.72 | 178.03 |
| . 507 | .4865787 | 8839 | 275244.07 | 182.33 | - 557 | . 5302490 | 8627 | 302251.71 | 177.94 |
| . 508 | . 4874625 | 8835 | 275546.35 | 182.24 | . 558 | . 53 I III5 | 8622 | $30 \quad 2549.60$ | 177.85 |
| . 509 | . 4883458 | 883 I | 275848.55 | 182.15 | . 559 | -531 9735 | 8618 | 302847.41 | 177.76 |
| 0.510 | 0.4892287 | 8827 | 28 OI 50.66 | 182.07 | 0.560 | 0.5328351 | 8614 | 303145.12 | 177.67 |
| .511 | . 490 I I 12 | 8823 | 280452.69 | 181.98 | . 561 | . 5336962 | 8609 | 303442.75 | 177.58 |
| . 512 | . 4909933 | 8819 | 280754.63 | I8I.90 | . 562 | . 5345569 | 8605 | 303740.28 | I77.49 |
| . 513 | . 4918749 | 8814 | 28 10 56.48 | 18i.8I | . 563 | . 5354172 | 8601 | 304037.73 | 177.40 |
| . 514 | . 4927562 | 88ı0 | 28 I3 58.25 | 181. 73 | . 564 | . 5362771 | 8596 | 304335.08 | 177.3I |
| 0.515 | 0.4936370 | 880 | 28 I6 59.94 | 181. 64 | 0.565 | 0.5371365 | 8592 | $30 \quad 4632.35$ | I77.22 |
| . 516 | . 494 5174 | 8802 | 2820 OI. 53 | I8I. 55 | . 566 | . 5379954 | 8587 | 304929.52 | I77.13 |
| . 517 | . 4953974 | 8798 | $28 \quad 2303.04$ | 181.47 | . 567 | . 5388539 | 8583 | 305226.60 | 177.04 |
| . 518 | . 4962769 | 8794 | $28 \quad 2604.47$ | 181.38 | . 568 | . 5397120 | 8579 | $3055 \quad 23.59$ | 176.95 |
| . 519 | . 497 I56I | 8789 | $28 \quad 29$ 05.8I | I8I. 29 | . 569 | . 5405696 | 8574 | 305820.49 | 176.85 |
| 0.520 | 0.4980348 | 8785 | $28 \quad 3207.06$ | 18I.2I | 0.570 | 0.5414268 | 8570 | 31 OI 17.30 | 176.76 |
| . 521 | . 498 913I | 8781 | $28 \quad 3508.22$ | I8I. 12 | . 571 | . 5422836 | 8565 | 310414.02 | 176.67 |
| . 522 | . 4997910 | 8777 | $28 \quad 38 \quad 09.30$ | 181.04 | . 572 | . 5431399 | 8561 | 310710.65 | 176.58 |
| . 523 | . 5006685 | 8773 | 284 I 10.29 | 180.95 | . 573 | . 5439958 | 8556 | 311007.18 | I76.49 |
| . 524 | . 5015456 | 8768 | 2844 II. 20 | 180.86 | . 574 | . 5448512 | 8552 | 311303.63 | 176.40 |
| 0.525 | 0.5024222 | 8764 | 2847 12.01 | 180.77 | 0.575 | 0.5457062 | 8548 | 3 I I5 59.98 | 176.31 |
| . 526 | . 5032984 | 8760 | 285012.75 | 180.69 | . 576 | . 5465607 | 8543 | 311856.24 | 176.22 |
| . 527 | . 5041742 | 8756 | $28 \quad 5313.39$ | 180.60 | . 577 | . 5474148 | 8539 | 3 I 2 I 52.4 I | 176. 12 |
| . 528 | . 5050495 | 8752 | $28 \quad 56$ I 3.95 | 180.51 | . 578 | . 5482685 | 8534 | 312448.49 | 176.03 |
| . 529 | . 5059245 | 8747 | 2859 14.4I | 180.43 | . 579 | . 549 1217 | 8530 | 312744.47 | 175.94 |
| 0.530 | 0.5067990 | 8743 | 290214.80 | 180.34 | 0.580 | 0.5499744 | 8525 | 3 I 3040.37 | 175.85 |
| . 53 I | . 507673 I | 8739 | 290515.09 | 180.25 | . 581 | . 5508267 | 8521 | 313336.17 | 175.76 |
| . 532 | . 5085468 | 8735 | 290815.30 | 180.16 | . 582 | -551 6786 | 8516 | 3 I 3631.88 | 175.66 |
| . 533 | . 5094200 | 8730 | 29 II I5.42 | 180.07 | . 583 | . 552 5300 | 8512 | 3 I 3927.50 | 175.57 |
| . 534 | . 5102928 | 8726 | 29 I4 I5.45 | 179.99 | . 584 | . 553 3810 | 8508 | 3I 4223.03 | I75.48 |
| 0.53 | 0.5111652 | 8722 | 291715.39 | 179.90 | 0.585 | 0.5542315 | 8503 | 3 I 4518.46 | 175.39 |
| . 536 | . 5120372 | 8717 | 292015.24 | I79.8I | . 586 | . 5550816 | 8499 | 314813.80 | 175.30 |
| . 537 | . 5129087 | 8713 | 2923 I5.01 | 179.72 | . 587 | . 5559313 | 8494 | 315109.05 | 175.20 |
| . 538 | . 5137798 | 8709 | 2926 I4. 69 | 179.63 | . 588 | . 5567804 | 8490 | 3 I 5404.2 I | I75.1 I |
| . 539 | . 5146505 | 8705 | 2929 I4.28 | 179.55 | . 589 | . 5576292 | 8485 | 315659.27 | 175.02 |
| 0.540 | 0.5155207 | 8700 | 293213.78 | 179.46 | 0.590 | -. 5584775 | 848 I | 315954.25 | 174.93 |
| -541 | - 5163905 | 8696 | 293513.20 | 179.37 | -591 | - 5593253 | 8476 | 320249.13 | I74.83 |
| . 542 | . 5172599 | 8692 | 2938 I2.52 | 179.28 | . 592 | . 5601727 | 8472 | $320543 \cdot 91$ | 174.74 |
| . 543 | . 5181289 | 8687 | 2941 II. 76 | 179.19 | - 593 | . 5610196 | 8467 | 320838.61 | 174.65 |
| . 544 | . 5189974 | 8683 | 2944 10.91 | 179.10 | . 594 | . 561886 I | 8463 | 32. II 33.21 | 174.55 |
| 0.545 | 0.5198655 | 8679 | 294709.95 | 179.01 | 0.595 | 0.562 .7122 | 8458 | 32 I4 27.71 | 174.46 |
| . 546 | . 5207332 | 8675 | 295008.93 | 178.93 | . 596 | . 5635577 | 8454 | 3217122.13 | I74.37 |
| - 547 | . 5216004 | 8670 | 295307.81 | 178.84 | - 597 | . 5644029 | 8449 | 322016.45 | 174.27 |
| - 548 | . 5224673 | 8666 | 2956 | 178.75 | . 598 | . 5652476 | 8445 | 322310.68 | I74.18 |
| - 549 | . 5233336 | 8662 | 2959 05.3I | 178.66 | . 599 | . 5660918 | 8440 | $32 \quad 2604.81$ | 174.09 |
| 0.550 | 0.5241996 | 8657 | $30 \quad 02 \quad 03.92$ | 178.57 | 0.600 | 0.5669356 | 8436 | $32 \quad 28 \quad 58.85$ | 173.99 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | ech | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | gdu | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.600 | 0.5669356 | 8436 | $32^{\circ} 28^{\prime} 58.85$ | 173.99 | 0.650 | 0.6085398 | 8205 | $34^{\circ} 52^{\prime} 00.134$ | 169.24 |
| . 601 | . 5677789 | 8431 | 323152.80 | 173.90 | . 651 | . 6093600 | 8200 | $\begin{array}{llll}34 & 54 & 49.52\end{array}$ | 169.14 |
| . 602 | . 56862 I 8 | 8426 | $\begin{array}{llll}32 & 34 & 46.66\end{array}$ | I73.8I | . 652 | .6I0 1798 | 8195 | 345738.62 | 169.04 |
| . 603 | . 5694642 | 8422 | $\begin{array}{llll}32 & 37 & 40.42\end{array}$ | 173.71 | . 653 | . 6109991 | 8191 | 350027.61 | 168.95 |
| . 604 | . 570306 I | 8417 | 324034.09 | I'73.62 | . 654 | .6II 8ı79 | 8186 | 350316.51 | I68.85 |
| 0.605 | 0.5711476 | 8413 | 324327.66 | I73.53 | 0.655 | 0.6126363 | 8 I 8 I | $350605 \cdot 31$ | 168.75 |
| . 606 | . 5719887 | 8408 | 3246 21.14 | 173.43 | . 656 | . 6134542 | 8177 | 350854.01 | I68.66 |
| . 607 | . 5728293 | 8404 |  | 173.34 | . 657 | . 6142716 | 8172 | 35 II 42.62 | I68.56 |
| . 608 | . 5736694 | 8399 | 325207.82 | 173.24 | . 658 | . 6150886 | 8167 | 35 I4 3I. 13 | 168.46 |
| . 609 | . 574 509I | 8395 | 3255 OI .01 | 173.15 | . 659 | .6I5 905I | 8163 | 35 I7 I9.54 | 168.36 |
| 0.610 | 0.5753484 | 8390 | 3257 54.12 | 173.06 | 0.660 | 0.6167211 | 8I58 | $35 \quad 2007.86$ | 168.27 |
| . 611 | . 5761871 | 8385 | 330047.13 | 172.96 | .66I | . 6175366 | 8 I 53 | $35 \quad 2256.08$ | 168.17 |
| .612 | . 5770255 | 838 I | 330340.04 | 172.87 | . 662 | . 6183517 | 8148 | $\begin{array}{llllllllll}35 & 25 & 44.20\end{array}$ | 168.07 |
| .613 | . 5778633 | 8376 | 330632.86 | 172.77 | . 663 | . 6191663 | 8 I 44 |  | 167.97 |
| .6I4 | . 5787007 | 8372 | 330925.59 | I72.68 | . 664 | . 6199804 | 8I 39 | 35 3I 20.14 | 167.88 |
| 0.615 | 0.5795377 | 8367 | 331218.22 | I72.59 | 0.665 | 0.6207941 | 8 I 34 | $35 \quad 3407.97$ | 167.78 |
| . 616 | . 580374 I | 8363 | 331510.76 | I72.49 | . 666 | . 6216073 | 8 I 29 | 353655.70 | 167.68 |
| . 617 | . 581 2102 | 8358 | $\begin{array}{llllllllllll}33 & 18 & 03.20\end{array}$ | 172.40 | . 667 | . 6224200 | 8125 | $35 \quad 3943.34$ | 167.58 |
| . 618 | . 5820457 | 8353 | 332055.55 | I72.30 | . 668 | . 6232322 | 8 I 20 | 354230.87 | 167.49 |
| . 619 | . 5828809 | 8349 | 332347.81 | 172.21 | . 669 | . 6240440 | 8II5 | 3545 I 8.3 I | 167.39 |
| 0.620 | 0.5837155 | 8344 | $\begin{array}{llll}33 & 26 & 39.97\end{array}$ | I72.II | 0.670 | 0.6248553 | 8iro | $35 \quad 4805.65$ | 167.219 |
| . 62 I | . 5845497 | 8340 | 3312932.03 | 172.02 | . 671 | . 625666 I | 8106 | $35 \quad 5052.89$ | 167.19 |
| . 622 | . 5853834 | 8335 | $\begin{array}{llll}33 & 32 & 24.00\end{array}$ | 171.92 | . 672 | . 6264764 | 8 I 101 | 355340.03 | 167.09 |
| . 623 | . 5862167 | 8330 |  | 171.83 | . 673 | . 6272863 | 8096 | 355627.08 | 167.00 |
| . 624 | . 5870495 | 8326 | $33 \quad 38 \quad 07.65$ | 171.73 | . 674 | . 6280956 | 8091 | 355914.03 | 166.90 |
| 0.625 | 0.5878819 | 8321 | 334059.34 | I\%1. 64 | 0.675 | 0.6289046 | 8087 | $36 \quad 0200.88$ | 166.80 |
| . 626 | . 5887137 | 8317 | 334350.93 | I71. 54 | . 676 | . 6297130 | 8082 | 360447.63 | 166.70 |
| . 627 | . 5895452 | 8312 | 334642.42 | I71. 45 | . 677 | .6305209 | 8077 | 360734.28 | $166.6 \bigcirc$ |
| . 628 | . 5903761 | 8307 | 334933.82 | I71. 35 | . 678 | . 6313284 | 8072 | 36 10 20.84 | 166.51 |
| . 629 | . 5912066 | 8303 | 335225.12 | I71. 26 | . 679 | . 632 I354 | 8068 | $\begin{array}{llllllllllllll}36 & 13 & 07.29\end{array}$ | 166.41 |
| 0.630 | 0.5920367 | 8298 | 335516.33 | 171.16 | 0.680 | 0.6329420 | 8063 | 36 15 53.65 | 166.31 |
| .63I | . 5928662 | 8293 |  | 171.06 | .681 | . 6337480 | 8058 | 3618189.91 | 166.21 |
| . 632 | . 5936954 | 8289 | 340058.46 | I70.97 | . 682 | . 6345536 | 8053 | 362126.07 | 166.11 |
| . 633 | . 5945240 | 8284 | 340349.38 | 170.87 | . 683 | . 6353587 | 8049 |  | 166.01 |
| . 634 | . 5953522 | 8280 | 340640.20 | 170.78 | . 684 | . 6361633 | 8044 | 362658.10 | 165.92 |
| 0.635 | 0.5961799 | 8275 | 340930.93 | 170.68 | 0.685 | 0.6369675 | 8039 | $36 \quad 2943.97$ | 165.82 |
| . 636 | . 5970072 | 8270 | $\begin{array}{llll}34 & 12 & 21.56\end{array}$ | 170.59 | . 686 | . 637 7711 | 8034 | $\begin{array}{llll}36 & 32 & 29.74\end{array}$ | 165.72 |
| . 637 | . 5978339 | 8266 | 34 I5 12.10 | 170.49 | . 687 | . 6385743 | 8029 | 363515.41 | 165.62 |
| . 638 | . 5986603 | 8261 | $\begin{array}{lllll}34 & 18 & 02.54\end{array}$ | 170.39 | . 688 | . 6393770 | 8025 | 363800.98 | 165.52 |
| . 639 | . 599 4861 | 8256 | $34 \quad 20 \quad 52.89$ | 170.30 | . 689 | . 6401792 | 8020 | 364046.45 | 165.42 |
| 0.640 | 0.6003115 | 8252 | $\begin{array}{llll}34 & 23 & 43.14\end{array}$ | 170.20 | 0.690 | 0.6409810 | 8015 | 3643.31 .82 | 165.32 |
| . 641 | . 6011364 | 8247 | $\begin{array}{lllll}34 & 26 & 33.29\end{array}$ | I70.11 | . 691 | . 6417823 | 8010 | 364617.09 | 165.22 |
| . 642 | . 6019609 | 8242 | $\begin{array}{llll}34 & 29 & 23.35\end{array}$ | 170.01 | . 692 | .6425830 | 8006 | 364902.27 | 165.13 |
| . 643 | . 6027849 | 8238 | $\begin{array}{llll}34 & 32 & 13.31\end{array}$ | 169.91 | . 693 | . 6433834 | 8001 | 3651747.34 | 165.03 |
| . 644 | .6036084 | 8233 | 343503.17 | 169.82 | . 694 | . 644 I832 | 7996 | 365432.32 | 164.93 |
| 0.645 | 0.6044315 | 8228 | 343752.94 | 169.72 | 0.695 | 0.6449825 | 7991 | $36 \quad 5717.20$ | 164.83 |
| . 646 | . 605254 I | 8224 | 344042.6 I | 169.62 | . 696 | . 6457814 | 7986 | 370001.98 | 164.73 |
| . 647 | . 6060762 | 8219 | 344332.19 | 169.53 | . 697 | . 6465798 | 7981 | 370246.66 | 164.63 |
| . 648 | . 6068979 | 8214 | 344621.67 | 169.43 | . 608 | . 6473777 | 7977 | 3705121.24 | 164.53 |
| . 649 | . 6077190 | 8210 | 3449 II. 05 | 169.33 | . 699 | . 648 I75I | 7972 | $37 \quad 0815.72$ | 164.43 |
| 0.650 | 0.6085398 | 8205 | 345200.34 | 169.24 | 0.700 | 0.6489721 | 7967 | 37 II 00.10 | 164.33 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | - ' " |  |  |  |  | - " " |  |
| 0.700 | 0.6489721 | 7967 | 37 II 00.10 | 164.33 | 0.750 | 0.6882014 | 7724 | 3925 51.72 | 159.32 |
| . 701 | . 6497685 | 7962 | $371344 \cdot 38$ | 164.23 | . 751 | . 6889735 | 7719 | 392830.98 | 159.22 |
| . 702 | . 6505645 | 7957 | 37 I6 28.57 | 164.13 | . 752 | . 689 745I | 7714 | 39 31 IO.15 | I59.1 |
| : 703 | .651 3600 | 7953 | 371912.65 | 164.03 | . 753 | . 6905163 | 7709 | 3933 49.2I | I 59.01 |
| .704 | . 652 I550 | 7948 | 37 21 56.63 | 163.93 | . 754 | . 6912870 | 7704 | 393628.18 | I 58.91 |
| 0.705 | 0.6529496 | 7943 | 372440.52 | 163.84 | 0.755 | 0.6920572 | 7699 | 393907.04 | I 58.8 I |
| . 706 | .6537436 | 7938 | 372724.31 | 163.74 | . 756 | . 6928269 | 7694 | 39 41 45.80 | 158.71 |
| . 707 | . 6545372 | 7933 | $37 \quad 30 \quad 07.99$ | 163.64 | . 757 | . 693 5961 | 7690 | 394424.46 | I 58.6 I |
| . 708 | . 6553303 | 7928 | 373251.58 | 163.54 | . 758 | . 6943648 | 7685 | 3947 03.01 | I58.5I |
| . 709 | . 656 I229 | 7924 | 373535.06 | 163.44 | . 759 | . 695 I330 | 7680 | 3949 4I. 47 | I 58.40 |
| 0.710 | 0.6569150 | 7919 | 373818.45 | 163.34 | 0.760 | 0.6959007 | 7675 | 395219.82 | 158.30 |
| . 711 | . 6577067 | 7914 | 3741 OI. 74 | 163.24 | . 761 | . 6966679 | 7670 | 395458.07 | 158.20 |
| . 712 | . 6584978 | 7909 | 374344.92 | 163.14 | . 762 | . 6974347 | 7665 | 395736.23 | I58.10 |
| . 713 | .6592885 | 7904 | 374628.01 | 163.04 | . 763 | . 6982009 | 7660 | 400014.28 | 158.00 |
| . 714 | . 6600787 | 7899 | 3749 II.00 | 162.94 | . 764 | . 6989667 | 7655 | 400252.22 | 157.90 |
| 0.715 | 0.6608684 | 7895 | 375153.89 | 162.84 | 0.765 | 0.6997319 | 7650 | 400530.07 | 157.80 |
| . 716 | . 66i 6576 | 7890 | 375436.68 |  | . 766 | . 7004967 | 7645 | 400807.81 | 157.69 |
| . 717 | . 6624463 | 7885 | 375719.36 | 162.64 | . 767 | . 7012610 | 7640 | 40 10 45.46 | 157.59 |
| . 718 | . 6632346 | 7880 | 3800 O1. 95 | 162.54 | . 768 | . 7020248 | 7635 | 40 13.23.00 | 157.49 |
| . 719 | . 6640223 | 7875 | $38 \quad 0244.44$ | 162.44 | . 769 | .7027880 | 7630 | 401600.44 | I 57.39 |
| 0.720 | 0.6648 | 7870 | 3805026.83 |  | 0.770 | 0.7035508 | 7625 | 40 18 37.78 | 157.29 |
| . 721 | . 6655964 | 7865 | 380809.11 | 162.24 | . 771 | . 704 313I | 7620 | 402115.01 | 157.19 |
| . 722 | . 6663827 | 7861 | 38 10 51.30 | 162.14 | . 772 | . 7050750 | 7616 | 402352.1 | 157.08 |
| . 723 | . 6671685 | 7856 | 38 I3 33.39 | 162.04 | . 773 | . 7058363 | 7611 | $40 \quad 26 \quad 29.18$ | 156.98 |
| . 724 | . 6679539 | 785 I | $\begin{array}{llllllllllllll}38 & 16 & 15\end{array}$ | 161.94 | . 774 | . 706597 I | 6 | 4029 06.1I | 156.88 |
| 0.725 | 0.6687387 | 7846 | 38 I8 57.26 | 161. 84 | 0.775 | 0.7073574 | 7601 | 40 3I 42.94 | 156.78 |
| . 726 | . 669523 I | 7841 | 38 21 39.05 | 161. 74 | . 776 | . 7081173 | 7596 | 403419.67 | 156.68 |
| . 727 | . 6703069 | 7836 | $38 \quad 24 \quad 20.73$ | 161. 64 | . 777 | . 7088766 | 7591 | $40 \quad 36 \quad 56.29$ | 156.57 |
| . 728 | . 6710903 | 7831 | $38 \quad 27 \quad 02.32$ | 161. 54 | . 778 | . 7096354 | 7586 | 403932.82 | I 56.47 |
| . 729 | . 6718732 | 7827 | 382943.80 | 161. 43 | . 779 | . 7103938 | 7581 | $40 \quad 4209.24$ | I 56.37 |
| 0.730 | 0.6726556 | 7822 | $38 \quad 32$ 25.19 | 161. 33 | 0.780 | 0.711 1516 | 7576 | 404445.56 | I56.27 |
| . 731 | . 6734376 | 7817 |  | 161. 23 | .78I | .711 9090 | 7571 | 404721.77 | 156.17 |
| . 732 | . 6742190 | 7812 |  | 16I. 13 | . 782 | . 7126659 | 7566 | $40 \quad 4957.89$ | 156.06 |
| . 733 | . 6750000 | 7807 | 384028.74 | 161.03 | . 783 | . 7134223 | 7561 | 405233.90 | I 55.96 |
| . 734 | . 6757804 | 7802 | $\begin{array}{lllll}38 & 43 & 09.72\end{array}$ | 160.93 | . 784 | . 714 I78I | 7556 | 405509.8 I | I 55.86 |
| 0.735 | 0.6765604 | 7797 | $3845 \quad 50.60$ | 160.83 | 0.785 | 0.7149335 | 7551 | $40 \quad 5745.62$ | 155.76 |
| . 736 | . 6773399 | 7792 | 3848 31.38 | 160.73 | . 786 | . 7156884 | 7546 | 410021.33 | I 55.66 |
| . 737 | . 6781189 | 7788 | 3851512.06 | 160.63 | . 787 | . 7164428 | 7541 | 410256.94 | I55.55 |
| . 738 | . 6788974 | 7783 | 38535152.64 | 160.53 | . 788 | . 7171967 | 7537 | 410532.44 | I 55.45 |
| . 739 | . 6796754 | 7778 | $38 \quad 5633.12$ | 160.43 | .789 | . 7179501 | 7532 | 410807.84 | 155.35 |
| 0.740 | 0.6804530 | 7773 | 3859 13.50 | 160.33 | 0.790 | 0.7187030 | 7527 | 41 IO 43.14 | 155.25 |
| . 741 | .681 2300 | 7768 | 39 OI 53.77 | 160.23 | .791 | . 7194554 | 7522 | $41 \quad 1318.33$ | I55. 15 |
| . 742 | .6820065 | 7763 | 390433.95 | 160.13 | . 792 | . 7202073 | 7517 | 41 I5 53.43 | I55.04 |
| . 743 | . 6827826 | 7758 | 390714.02 | 160.02 | . 793 | . 7209588 | 7512 | 41 I8 28.42 | 154.94 |
| . 744 | .6835582 | 7753 | 390954.00 | 159.92 | . 794 | . 7217097 | 7507 | 4 I 2103.3 I | 154.84 |
| 0.745 | 0.6843333 | 7748 | 391233.87 | I 59.82 | 0.795 | 0.7224601 | 7502 | 412338.10 | 154.74 |
| . 746 | . 6851079 | 7744 | 391513.64 | 159.72 | . 796 | . 7232101 | 7497 | 412612.78 | I 54.63 |
| . 747 | . 6858820 | 7739 | 39 17 53.31 | I 59.62 | . 797 | . 7239595 | 7492 | $412847 \cdot 36$ | I 54.53 |
| . 748 | . 6866556 | 7734 | $\begin{array}{llll}39 & 20 & 32.88\end{array}$ | I 59.52 | . 798 | . 7247084 | 7487 | 413121.84 | I 54.43 |
| . 749 | .6874287 | 7729 | $\begin{array}{llll}39 & 23 & 12.35\end{array}$ | I 59.42 | . 799 | . 7254569 | 7482 | 41 3356.22 | 154.33 |
| 0.750 | 0.6882014 | 7724 | 392551.72 | 159.32 | 0.800 | 0.7262048 | 7477 | 413630.50 | 154.22 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | hu | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{a}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | h | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.800 | 0.7262048 | 747 | 413630.50 | 154.22 | 0.850 | 0.7629677 | 7228 | - $42{ }^{\prime} \quad 53.38$ | 90 |
| . 801 | 0.7269523 .72048 | 7472 | 413904.67 | 154.12 | - 8.85 | 0.7629677 .763692 | 7223 | $\begin{array}{llll}43 & 42 & 53 \cdot 38 \\ 43 & 45 & 22.41\end{array}$ | 88 |
| . 802 | . 7276992 | 7467 | $4 \mathrm{I} 4 \mathrm{I} \quad 38.74$ | 154.02 | . 852 | . 7644122 | 7218 | 434751.34 | I48.88 |
| . 803 | . 7284457 | 7462 | 414412.71 | 153.92 | . 853 | . 7651338 | 7213 | 435020.17 | I48.78 |
| . 804 | .7291916 | 7457 | 41 4646.57 | I53.8I | . 854 | .7658548 | 7208 | 435248.89 | 148.67 |
| 0.805 | 0.7299371 | 7452 | 414920.34 | 153.71 | 0.855 | 0.7665754 | 7203 | 4355 I7.52 | I48.57 |
| . 806 | . 7306821 | 7447 | 4 I 5 I 54.00 | I53.6I | . 856 | . 7672954 | 7198 | 435746.04 | 148.47 |
| . 807 | . 7314266 | 7442 | 41 5427.56 | I 53.5 I | . 857 | . 7680149 | 7193 | 4400 I 4.45 | I48.36 |
| . 808 | . 7321705 | 7437 | 4 I 57 OI.OI | 153.40 | . 858 | . 7687340 | 7188 | 440242.76 | I48.26 |
| . 809 | . 7329140 | 7432 | 415934.36 | 153.30 | . 859 | .7694525 | 7183 | 440510.97 | 148.16 |
| 0.810 | 0.7336570 | 7427 | 420207.62 | I53.20 | 0.860 | 0.7701706 | 7178 | 440739.08 | 148.05 |
| .8II | . 7343995 | 7422 | 420440.76 | 153.10 | .86I | . 770 888I | 7173 | 44 10 07.08 | 147.95 |
| .8I2 | . 735 I414 | 7417 | 420713.81 | 152.99 | . 862 | . 7716051 | 7168 | $44 \quad 1234.98$ | 147.85 |
| . 813 | . 7358829 | 7412 | 420946.75 | 152.89 | . 863 | . 7723217 | 7163 | 44 I5 02.78 | 147.75 |
| .814 | .7366239 | 7407 | 42 I2 19.59 | 152.79 | . 864 | .7730377 | 7158 | 441730.48 | 147.64 |
| 0.815 | 0.7373644 | 7402 | 42 14 52.33 | 152.69 | 0.865 | 0.7737533 | 7153 | 44 I9 58.07 | 147.54 |
| .816 | .7381044 | 7397 | 42 17 24.96 | I 52.58 | . 866 | . 7744683 | 7148 | 442225.56 | 147.44 |
| .817 | . 7388439 | 7392 | 421957.50 | 152.48 | . 867 | . 775 I829 | 7143 | 442452.94 | 147.33 |
| . 818 | . 7395829 | 7387 | 422229.93 | 152.38 | . 868 | . 7758959 | 7138 | 442720.22 | 147.23 |
| . 819 | . 7403214 | 7383 | 422502.25 | 152.28 | . 869 | . 7766104 | 7133 | 442947.40 | 147.13 |
| 0.820 | 0.7410594 | 7378 | $42 \quad 2734.48$ | 152.17 | 0.870 | 0.7773235 | 7128 | $4432 \quad 14.48$ | 147.02 |
| . 82 I | . 7417969 | 7373 | 423006.60 | 152.07 | . 871 | . 7780360 | 7123 | 4434 41.45 | 146.92 |
| . 822 | . 7425339 | 7368 | $\begin{array}{llll}42 & 32 & 38.62\end{array}$ | 151.97 | . 872 | . 778 7481 | 7118 | 443708.32 | 146.82 |
| . 823 | . 7432704 | 7363 | 423510.53 | 151.85 | . 873 | . 7794596 | 7113 | 443935.09 | 146.71 |
| . 824 | .7440064 | 7358 | 423742.34 | 151.76 | . 874 | .7801707 | 7108 | 4442 OI. 75 | I46.6I |
| 0.825 | 0.7447420 | 7353 | 424014.05 | 151.66 | 0.875 | 0.780 88I2 | 7103 | 444428.31 | 146.51 |
| . 826 | . 7454770 | 7348 | $42 \quad 4245.66$ | 151.56 | . 876 | .781 5912 | 7098 | $44 \quad 4654.77$ | 146.41 |
| . 827 | . 746 2115 | 7343 | 4245 I7. I7 | I51.45 | . 877 | . 7823008 | 7093 | 4449 21.12 | 146.30 |
| . 828 | . 7469455 | 7338 | 424748.57 | I51.35 | . 878 | .7830098 | 7088 | 44 51 47.37 | 146.20 |
| . 829 | . 7476790 | 7333 | 425019.87 | 151.25 | . 879 | .7837184 | 7083 | 445413.52 | 146.10 |
| 0.830 | 0.7484120 | 7328 | 425251.05 | 151.14 | 0.880 | 0.7844264 | 7078 | 445639.56 | 145.99 |
| . 831 | . 749 I446 | 7323 | 425522.16 | 151.04 | . 881 | . 7851340 | 7073 | 445905.50 | 145.89 |
| . 832 | . 7498766 | 7318 | 4257 53.15 | 150.94 | . 882 | . 7858410 | 7068 | 45 OI 31.34 | I 45.79 |
| . 833 | . 7506081 | 7313 | 430024.04 | 150.84 | . 883 | . 7865476 | 7063 | 450357.08 | I45.68 |
| . 834 | .751 3391 | 7308 | 430254.82 | 150.73 | . 884 | . 7872536 | 7058 | 450522.71 | 145.58 |
| 0.835 | 0.7520697 | 7303 | 430525.50 | 150.63 | 0.885 | 0.7879591 | 7053 | $\begin{array}{llll}45 & 08 & 48.24\end{array}$ | 145.48 |
| . 836 | . 7527997 | 7298 | 430756.08 | 150.53 | . 886 | . 7886642 | 7048 | 45 II I3.66 | 145.37 |
| . 837 | . 7535292 | 7293 | 43 Io 26.56 | 150.42 | . 887 | .7893687 | 7043 | $45 \quad 1338.59$ | I45.27 |
| . 838 | . 7542582 | 7288 | 43 I2 56.93 | I 50.32 | . 888 | . 7900728 | 7038 | 45 I6 04.21 | 145. 17 |
| . 839 | . 7549868 | 7283 | 43 I5 27.20 | 150.22 | . 889 | . 7907763 | 7033 | 45 I8 29.32 | 145.06 |
| 0.840 | 0.7557148 | 7278 |  | 150.12 | 0.890 | 0.7914794 | 7028 | $45 \quad 2054.34$ | I44.96 |
| . 841 | . 7564423 | 7273 | $43 \quad 20 \quad 27.43$ | 150.01 | . 891 | . 792 1819 | 7023 | $45 \quad 2319.25$ | 144.86 |
| . 842 | . 7571694 | 7268 | $43 \quad 22 \begin{array}{lll}43 & 39\end{array}$ | 149.91 | . 892 | . 7928839 | 7018 | 452544.05 | 144.76 |
| . 843 | . 7578959 | 7263 | $43125 \begin{array}{lll}43 & 27.25\end{array}$ | I 49.8I | . 893 | . 7935855 | 7013 |  | I 44.65 |
| . 844 | . 7586219 | 7258 | 432757.01 | 149.70 | . 894 | . 7942865 | 7008 | $45 \quad 3033 \cdot 36$ | 144.55 |
| 0.845 | 0.7593475 | 7253 | $43 \quad 3026.66$ | 149.60 | 0.895 | 0.794987 I | 7003 | $45 \quad 32 \begin{array}{lll}47.85\end{array}$ | I44.45 |
| . 846 | . 7600725 | 7248 | $43 \quad 3256.21$ | 149.50 | . 896 | . 795687 I | 6998 | $45 \quad 35 \quad 22.25$ | I 44.34 |
| . 847 | . 7607970 | 7243 | $\begin{array}{lllll}43 & 35 & 25.65\end{array}$ | 149.39 | . 897 | . 7963857 | 6993 | 453746.54 | I44.24 |
| . 848 | . 76 I 521I | 7238 | 433755.00 | 149.29 | . 898 | . 7970857 | 6988 | 454010.73 | I44. I4 |
| . 849 | . 7622446 | 7233 | $43 \quad 4024.24$ | 149. 19 | . 899 | . 7977843 | 6983 | 454234.8 I | 144.03 |
| 0.850 | 0.7629677 | 7228 | 434253.38 | 149.09 | 0.900 | 0.7984823 | 6978 | 454458.80 | 143.93 |
| $u$ | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

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| $u$ | od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ | od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | odu | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0.900 | 0.7984823 | 6978 | $45^{\circ} 4458.80$ | 143.93 | 0.950 | 0.8327479 | 6728 | $47^{\circ} 42^{\prime} 46.58$ | 138.78 |
| . 901 | . 7991798 | 6973 | 454722.67 | 143.83 | .951 | . 8334205 | 6723 | 474505.3 I | 138.68 |
| . 902 | . 7998769 | 6968 | 454946.45 | 143.72 | . 952 | . 8340926 | 6719 | 474723.94 | 138.58 |
| . 903 | . 8005734 | 6963 | 4552 10.12 | 143.62 | . 953 | . 8347642 | 6714 | 474942.47 | 138.48 |
| . 904 | . 8012695 | 6958 | 455433.69 | 143.52 | -954 | . 8354353 | 6709 | 475200.89 | 138.37 |
| 0.905 | 0.801 9650 | 6953 | 455657.16 | 143.42 | 0.955 | 0.8361059 | 6704 | 475419.22 | 138.27 |
| . 906 | . 8026601 | 6948 | 455920.52 | $143 \cdot 31$ | . 956 | . 8367760 | 6699 | 475637.44 | 138.17 |
| . 907 | . 8033546 | 6943 | 46 or 43.78 | 143.21 | . 957 | . 8374456 | 6694 | 475855.55 | 138.07 |
| . 908 | . 8040487 | 6938 | 460406.94 | I43. I I | . 958 | . 8381147 | 6689 | 48 OI I3.57 | 137.96 |
| . 909 | . 8047422 | 6933 | 460630.00 | 143.00 | . 959 | . 8387833 | 6684 | 4803 31.48 | 137.86 |
| 0.910 | 0.8054353 | 6928 | 460852.95 | 142.90 | 0.960 | 0.8394514 | 6679 | 480549.29 | 137.76 |
| . 911 | . 8061278 | 6923 | 46 II 15.79 | 142.80 | . 961 | . 840119 I | 6674 | 480807.00 | 137.66 |
| . 912 | . 806 8198 | 6918 | 46 I3 38.54 | I42.69 | . 962 | . 8407862 | 6669 | 48 10 24.60 | 137.55 |
| .913 | . 8075114 | 6913 | 46 I6 or. 18 | 142.59 | .963 | . 8414528 | 6664 | 48 I2 42.10 | 137.45 |
| . 914 | . 8082024 | 6908 | $46 \quad 18 \quad 23.72$ | 142.49 | . 964 | . 8421190 | 6659 | 48 I4 59.50 | 137.35 |
| 0.915 | 0.8088930 |  | 462046.16 | 142.38 | 0.965 | 0.8427846 | 6654 | 481716.80 | 137.25 |
| .916 | . 8095830 | 6898 | $46 \quad 2308.49$ | 142.28 | . 966 | . 8434497 | 6649 | 48 19 33.99 | 137. 14 |
| .917 | . 8102726 | 68 | $46 \quad 2530.72$ | 142.18 | . 967 | . 8441144 | 6644 | 48 21 51.09 | 137.04 |
| .918 | . 8109616 | 6888 | 462752.85 | 142.08 | .958 | . 8447785 | 6639 | 482408.08 | 136.94 |
| . 919 | . 8116502 | 6883 | 463014.87 | 141.97 | . 969 | . 8454422 | 6634 | $48 \quad 2624.96$ | I36.84 |
| 0.920 | 0.8123383 | 6878 | 463236.79 | 141.87 | 0.970 | 0.8461053 | 6629 | 482841.75 | 136.73 |
| . 921 | .813 0258 | 6873 | 463458.61 | 141.77 | . 971 | . 8467680 | 6624 | 483058.43 | 136.63 |
| . 922 | . 8137129 | 6858 | 463720.33 | 141.66 | . 972 | . 8474301 | 6619 | 4833 15.01 | I36.53 |
| . 923 | . 8143994 | 6863 | 463941.94 | 141. 56 | . 973 | . 8480918 | 6614 | 48353 I .49 | ${ }_{1} 136.43$ |
| . 924 | . 8150855 | 6858 | 464203.45 | 141.46 | -974 | . 8487530 | 6609 | 483747.87 | I 36.32 |
| 0.925 | 0.8157710 | 6853 | 464424.85 | 141.35 | 0.975 | 0.8494136 | 6604 | 484004.14 | 136.22 |
| . 926 | .816 4561 | 6848 | 464646.16 | 141.25 | . 976 | . 8500738 | 6599 | 484220.3 I | 136.12 |
| . 927 | . 8171406 | 6843 | $464907 \cdot 36$ | I41.15 | . 977 | . 8507335 | 6594 | 484436.38 | 136.02 |
| -928 | . 8178247 | 6838 | 465128.45 | 141.05 | -978 | . 8513927 | 6589 | 484652.34 | ${ }_{1} 135.92$ |
| . 929 | .8185083 | 6833 | 465349.45 | 140.94 | -979 | . 8520514 | 6584 | 484908.21 | 135.81 |
| 0.930 | 0.819 1913 | 6828 | 46 | 140.84 | 0.980 | 0.8527096 | 6579 |  |  |
| . 931 | .8198739 .820560 | 6823 6818 | 46 <br> 47 <br> 47 <br> 0 | 140.74 140.63 | . 988 | .8533673 <br> .854 <br> 245 | 6574 6570 | $\begin{array}{llll}48 & 53 & 39.63 \\ 48 & 55 & 55.19\end{array}$ | I35.61 I35.51 |
| . 932 | .8205560 .8212375 | 6818 6813 | $\begin{array}{llll}47 & 00 & 51.81 \\ 47 & \text { o3 } & 12.40\end{array}$ | 140.63 140.53 | . 988 | .8540245 <br> .8546812 | 6570 6565 | $\begin{array}{llll}48 & 55 & 55.19 \\ 48 & 58 \\ \text { 10.64 }\end{array}$ | I35.51 I 35.40 |
| . 934 | . 8219186 | 6808 | 470532.88 | 140.43 | . 984 | . 8553374 | 6560 | 490026.00 | 135.30 |
| 0.935 | 0.8225992 | 6803 | 470753.25 | 140.33 | 0.985 | 0.8559931 | 6555 | 49024 i .25 | 135.20 |
| . 936 | . 8232792 | 67 | 47 Io 13.53 | 140.22 | . 986 | . 8566483 | 6550 | 490456.40 | 135. 10 |
| -937 | . 8239588 | 679 | 471233.70 | 140.12 | . 987 | . 8573030 | 6545 | 4907 II. 44 | I 35.00 |
| -938 | . 8246379 | 678 | 471453.77 | 140.02 | .988 | . 8579573 | 6540 | 490926.39 | 134.89 |
| . 939 | . 8253164 | 6783 | $47 \begin{array}{llll}47 & 13.74\end{array}$ | 139.91 | . 989 | . 858 6ı10 | 6535 | 49 II 41.23 | 134.79 |
| 0.940 | 0.8259945 | 6778 | 471933.60 | 139.8I | 0.990 | 0.8592642 | 6530 | 491355.97 | 134.69 |
| .94I | . 8266721 | 6773 | 472153.36 | 139.71 | . 991 | . 8599170 | 6525 | 491610.61 | 134.59 |
| . 942 | . 8273492 | 6768 | $47 \quad 2413.02$ | 139.61 | . 992 | . 8605692 | 6520 | 491825.15 | I 34.49 |
| -943 | . 8280257 | 6763 | 472632.57 | 139.50 | . 993 | .861 2210 | 6515 | 492039.58 | 134.38 |
| . 944 | . 8287018 | 6758 | 472852.02 | 139.40 | . 994 | . 8518723 | 6510 | 492253.92 | 134.28 |
| 0.945 | 0.8293774 | 6753 | 473111.37 | 139.30 | 0.995 | 0.8625230 | 6505 |  | 134.18 |
| . 946 | . 8300525 | 6748 | 473330.62 | 139.20 | . 996 | . 8631733 | 6500 | 492722.28 | I35.08 |
| . 947 | . 8307271 | 6743 | 473549.76 | 139.09 | . 997 | . 8638231 | 6495 | 492936.30 | 133.98 |
| . 948 | . 8314012 | 6738 | $473808.80$ | 138.99 I 38.89 | . 998 | . 8644724 | 6490 | 493150.23 | 133.87 |
| -949 | . 8320748 | 6733 | 474027.74 | 138.89 | . 999 | . 8651112 | 6485 | 493404.05 | 133.77 |
| 0.950 | 0.8327479 | 6728 | 474246.58 | 138.78 | 1.000 | 0.8657695 | 648 I | 493617.77 | 133.67 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | ws |  | $2 \tan ^{-1}\left(e^{\mathrm{a}}\right)-\frac{\pi}{2}$ | hu | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech $u$ |

Smithsonian tables

The Gudermannian.

| u | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 000 | 0.8657695 | 648 I | $49^{\circ} 36^{\prime}$ I7." 77 | $\begin{gathered} \text { " } \\ 133.6 \end{gathered}$ | 1.050 | 5576 |  |  |  |
| .00I | . 8664173 | 6476 | 4938 31.39 | I 33.57 | .051 | . 89881809 |  |  |  |
| . 002 | . 8670646 | 6471 | 494044.91 | 133.47 | . 052 | . 8988037 | 6225 | 5 I 2951.57 | 128.41 |
| . 003 | . 867 7114 | 6466 | 494258.33 | 133.37 | . 053 | .8994260 | 6221 | 513159.92 | I28.3I |
| . 004 | .8583578 | 6461 | 4945 II. 64 | I 33.26 | . 054 | . 9000478 | 6216 | 5134 08.18 | 128.21 |
| 1.005 | 0.8690036 | 6456 | 494724.86 | 133.16 | 1.055 | 0.9006691 | 6211 | 515616.34 | I28. 11 |
| . 006 | . 8796489 | 6451 | 494937.97 | 133.06 | . 056 | . 9012900 | 6206 | 513824.40 | I28.01 |
| . 007 | . 8702938 | 6446 | 49 51 50.98 | 132.96 | . 057 | .901 9103 | 6201 | 514032.36 | 127.91 |
| . 008 | . 870 9381 | 6441 | 495403.89 | I 32.86 | . 058 | . 8025302 | 6196 | 51 4240.21 | 127.8I |
| . 009 | . 8715820 | 6436 | 4956 16.69 | 132.76 | . 059 | . 9031496 | 6191 | 514447.97 | 127.71 |
| 1.010 | 0.8722254 | 6431 | $4958 \quad 29.40$ | I32.65 | 1.060 | 0.9037685 | 6187 | 514655.63 | 127.6I |
| . OII | . 8728582 | 6426 | 500042.00 | 132.55 | .0SI | . 9043869 | 6182 | 5149 03.18 | 127.51 |
| . 012 | .8735106 | 6421 | 500254.50 | I 32.45 | . 052 | . 9050048 | 6177 | 515110.64 | 127.41 |
| . 013 | . 874 I525 | 6416 | 500506.90 | I 32.35 | . 063 | . 9056222 | 6172 | 515318.00 | 127.3I |
| . 014 | . 8747939 | 6412 | 500719.20 | I32.25 | . 064 | . 9062392 | 6167 | 51 $55 \quad 25.25$ | 127.21 |
| 1.015 | 0.8754348 | 6407 | 500931.40 | 132.15 | 1.055 | 0.9068557 | 6162 | 5 I 5732.41 | I27. II |
| . 016 | . 8760752 | 6402 | 50 II 43.49 | 132.04 | . 065 | . 9074716 | 6157 | 51 5939.46 | 127.01 |
| . 017 | . 8767152 | 6397 | 50 I3 55.49 | I3I. 94 | . 057 | . 9080871 | 6 6 53 | 52 OI 46.42 | 126.91 |
| . 018 | . 8773546 | 6392 | $50 \quad 16 \quad 07.38$ | 131.84 | . 058 | . 9087022 | 6148 | 520353.27 | 126.8I |
| . 019 | . 8779936 | 6387 | 5018 19.17 | I31.74 | . 069 | . 9093167 | 6143 | 520600.03 | 126.71 |
| 1.020 | 0.8786320 | 6382 | 502030.86 | 131.64 | 1.070 | 0.9099307 | 6138 | 520806.68 | 126.6I |
| .02I | . 8792700 | 6377 | 502242.45 | 131.54 | . 071 | . 9105443 | 6133 | 52 10 13.24 | 126.51 |
| . 022 | . 8799074 | 6372 | '50 2453.94 | 131.44 | . 072 | .911 1574 | 6128 | 52 I2 19.70 | 126.4I |
| . 023 | . 8805444 | 6367 | 502705.32 | 131.34 | . 073 | .911 7699 | 6123 | 52 I4 26.05 | 126.3I |
| . 024 | .881 1809 | 6362 | 5029 16.61 | 131.23 | . 074 | . 912382 I | 6118 | 52 16 32.31 | I26.21 |
| I. 025 | 0.881 8169 | 6357 | 503127.79 | 131.13 | 1.075 | 0.9129937 | 6II4 | $\begin{array}{llll}52 & 18 & 38.46\end{array}$ | 126.11 |
| . 026 | . 8824524 | 6353 | $\begin{array}{lllll}50 & 33 & 38.87\end{array}$ | 131.03 | . 076 | . 9136048 | 6109 | $52 \quad 2044.52$ | 126.01 |
| . 027 | .8830874 | 6348 | 503549.85 | I 30.93 | . 077 | . 9142155 | 6104 | 522250.48 | I25.9I |
| . 028 | .8837219 | 6343 | $5038 \quad 00.73$ | I 30.83 | . 078 | . 9148256 | 6099 | 522456.33 | I25.8I |
| . 029 | .8843560 | 6338 | 5040 II.5I | 130.73 | . 079 | . 9154353 | 6094 | 522702.09 | 125.71 |
| 1.030 | 0.8849895 | 6333 | 5042 22.19 | 130.63 | 1.080 | 0.9160445 | 6090 | 522907.75 | 125.6 I |
| . 031 | . 8856226 | 6328 | 504432.76 | 130.53 | .08I | . 9166532 | 6085 | 52 31 13.30 | 125.51 |
| . 032 | . 8862551 | 6323 | 504643.24 | 130.42 | . 082 | . 9172615 | 6080 |  | 125.41 |
| . 033 | . 8868872 | 6318 | 5048 53.6I | I30. 32 | . 083 | .917 8692 | 6075 | 5235124.12 | I25.3I |
| . 034 | . 8875188 | 6313 | 505103.89 | 130.22 | . 084 | .918 4765 | 6070 | 523729.38 | 125.21 |
| 1.035 | 0.8881499 | 6308 | 505314.06 | 130.12 | 1.085 | 0.9190833 | 6065 | 523934.54 | I25. II |
| . 036 | .8887805 | 6304 | 5055 24.13 | 130.02 | . 086 | . 9196896 | 6061 | 524139.60 | I25.01 |
| . 037 | . 889 4106 | 6299 | 505734.10 | 129.92 | . 087 | . 9202954 | 6056 | 524344.56 | 124.91 |
| . 038 | .8900402 | 6294 | 505943.97 | 129.82 | . 088 | . 9209008 | 6051 | 524549.42 | I24.8I |
| . 039 | .8906693 | 6289 | 5 I O1 53.74 | 129.72 | . 089 | .921 5056 | 6046 | 5247 54.18 | 124.71 |
| 1.040 | 0.8912980 | 628 | 5I 0403.41 | 129.62 | 1.090 | 0.9221100 | 6041 | 524958.85 | 124.6I |
| . 041 | . 8919262 | 6279 | 510612.98 | 129.52 | .09I | . 9227139 | 6037 | 525203.41 | 124.51 |
| . 042 | . 8925538 | 6274 | 51 0822.44 | 129.42 | . 092 | .9233173 | 6032 | 525407.87 | I24.4I |
| . 043 | . 893 I810 | 6269 | 5 I 10 31.81 | 129.32 | . 093 | .923 9203 | 6027 | 525612.24 | 124.32 |
| . 044 | .8938077 | 6264 | 511241.07 | 129.2I | . 094 | . 9245227 | 6022 | 5258 16.50 | 124.22 |
| 1.045 | 0.8944339 | 6260 | 5I I4 50.24 | I29. II | 1.095 | 0.9251247 | 6017 | $53 \quad 0020.67$ | 124.12 |
| . 046 | . 8950596 | 6255 | 511659.30 | 129.01 | . 096 | .9257262 | 6013 |  | 124.02 |
| . 047 | . 8956848 | 6250 | 511908.26 | 128.91 | . 097 | . 9263272 | 6008 | 530428.70 | 123.92 |
| . 048 | .8963096 | 6245 | 512117.12 | 128.81 | . 098 | . 9269278 | 6003 | $\begin{array}{lllll}53 & 06 & 32.57\end{array}$ | 123.82 |
| . 049 | .8969338 | 6240 | 512325.88 | 128.71 | . 099 | .9275278 | 5998 | $\begin{array}{lllll}53 & 08 & 36.34\end{array}$ | 123.72 |
| 1.050 | 0.8975576 | 6235 | 512534.55 | 128.6I | 1. 100 | 0.9281274 | 5993 | 53 10 40.01 | 123.62 |
| $u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | w sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | sech | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u |

Smithsonian tables

The Gudermannian.

| u | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\text {n }}$ | u | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
| I. 100 | 0.9281274 | 5993 | 53 10 40.01 | 123.6 | I. 150 | 0.9574980 | 5756 | 545138.15 | II8.72 |
| . 101 | . 9287265 | 5989 | $531243 \cdot 59$ | 123.52 | .15I | . 9580734 | 5751 | 545336.82 | I 18.62 |
| . 102 | . 929 325I | 5984 | 53 I4 47.06 | 123.42 | . I52 | . 9586482 | 5746 | $\begin{array}{lllllllllllll}54 & 55 & 39\end{array}$ | I 18.53 |
| . 103 | . 9299232 | 5979 | 531650.43 | 123.32 | . 153 | . 5592226 | 5742 | 545733.87 | 118.43 |
| . 134 | . 9305209 | 5974 | 53 I8 53.71 | 123.23 | - 154 | . 9597965 | 5737 | 545932.25 | I 18.33 |
| I. 105 | 0.931 II8I | 5959 | $53 \quad 2056.89$ | 123.13 | I. I55 | 0.9603 .700 | 5732 | 55 OI 30.53 | II8.23 |
| . 106 | .931 7148 | 5965 | 532259.96 | 123.03 | . 156 | . 9609430 | 5727 | 550328.72 | I18.14 |
| . 107 | . 932 3110 | 5960 | $\begin{array}{llllll}53 & 25 & 02.94\end{array}$ | 122.93 | . 157 | . 9615155 | 5723 | 550526.81 | I 18.04 |
| . 108 | . 9329067 | 5955 | 532705.82 | 122.83 | . 158 | . 9520875 | 5718 | 550724.80 | II7.94 |
| . 109 | . 9335020 | 5950 | $53 \quad 2908.60$ | 122.73 | - 159 | . 9626591 | 5713 | 550922.69 | II7.85 |
| I.IIO | 0.9340968 | 5945 | 53 3I II. 29 | 122.63 | 1. 160 | 0.9632302 | 5709 | 55 II 20.49 | II7.75 |
| . III | . 934 691I | 5941 | 533313.87 | 122.54 | . 161 | . 9638008 | 5704 | 55 I3 18.19 | 117.65 |
| . I | . 9352849 | 5936 | $\begin{array}{llllllllllllllllllll}53 & 35 & 16.36\end{array}$ | I22.44 | . 162 | . 9643710 | 5699 | 55 15 15.80 | 117.56 |
| . II3 | . 9358782 | 593 I | $\begin{array}{llllllllllll}53 & 37 & 18.75\end{array}$ | 122.34 | . 163 | . 9649407 | 5695 | 55 I7 13.31 | 117.46 |
| . II4 | . 93647 II | 5926 | 5339 21.03 | 122.24 | . 164 | . 9655099 | 5690 | 55 I9 10.72 | 117.36 |
| I.II5 | 0.9370635 | 5922 | 534123.22 | 122.14 | I. 165 | 0.9660787 | 5685 | 552108.04 | II7.27 |
| . 116 | . 9376554 | 5917 | $5343 \quad 25.32$ | 122.04 | . 166 | . 9666470 | 5681 | 552305.26 | 117.17 |
| . 117 | . 938.2469 | 5912 |  | 122.94 | . 167 | .9672148 | 5676 | $\begin{array}{llllllllllll}55 & 25 & 02.38\end{array}$ | 117.07 |
| . 118 | . 9388378 | 5907 | $\begin{array}{lllll}53 & 47 & 29.21\end{array}$ | 121.85 | . 168 | .9677822 | 5671 | 552659.41 | 116.98 |
| . 119 | . 9394283 | 5902 | 5349 31.00 | 121.75 | . 169 | . 968 349I | 5667 | $\begin{array}{lllllllllllll}55 & 28 & 56.34\end{array}$ | 116.88 |
| 1.120 | 0.940 0I83 | 5 | 53 51 32.70 |  | I. I70 | 0.9689155 | 5662 | $55 \quad 3053.17$ | 116.79 |
| . 12 I | . 9406079 | 5893 | $\begin{array}{lllll}53 & 53 & 34 \cdot 30\end{array}$ | I2I. 55 | . 171 | . 9694815 | 5657 | $\begin{array}{lllll}55 & 32 & 49.91\end{array}$ | 116.69 |
| . 1 | .94I 1969 | 5888 | $\begin{array}{llllllllll}53 & 55 & 350\end{array}$ | 121.45 | . 172 | . 9700470 | 5653 | 553446.55 | I16. 59 |
| . I23 | . 9417855 | 5883 |  | 121. 35 | . 173 | . 970 6I20 | 5648 | 55 | I 16.50 |
| . 124 | . 9423736 | 5879 | 535938.51 | 121.26 | . 174 | .971 1766 | 5643 | $\begin{array}{llll}55 & 38 & 39.54\end{array}$ | I 16.40 |
| I. 125 | 0.9429613 | 5874 | 54 OI 39.72 | 121.16 | I. 175 | 0.9717407 | 5639 | 554035.90 | 116.31 |
| . 126 | . 9435484 | 5869 | 540340.83 | 121.06 | . 1.76 | . 9723043 | 5634 | 5542 32.16 | 116.21 |
| . 1 | . 944 I35I | 5864 | 540541.84 | 120.9 | . 177 | . 9728675 | 5629 | 554428.32 | II6. II |
| . I | -944 72I3 | 5860 | 540742.76 | 120.86 | . 178 | . 9734301 | 5625 | $5546 \quad 24.38$ | 116.02 |
| . 129 | -945 3070 | 5855 | $540943 \cdot 57$ | 120.77 | . 179 | . 9739924 | 5620 | 554820.35 | I 15.92 |
| 1. I30 | 0.9458923 | 5850 | 54 II 44.29 | 120.67 | I. 180 | 0.9745542 | 5615 | $55 \quad 5016.22$ | 115.83 |
| .131 | . 9464771 | 5845 | 54 I3 44.91 | I20.57 | . 181 | . 9751155 | 5611 | $55 \quad 5212.00$ | II5.73 |
| . 132 | . 947 06I4 | 584 I | 54 I5 45.43 | 120.47 | . 182 | .9756763 | 5606 | 555407.68 | 115.63 |
| . I33 | - 9476452 | 5836 | 54 I7 45.86 | 120.38 | . 183 | . 9762367 | 5601 | $55 \quad 5603.27$ | II5.54 |
| . 134 | . 9482286 | 5831 | 54 I9 46.18 | 120.28 | . 184 | . 9767966 | 5597 | 555758.76 | II5.44 |
| I. 135 | 0.948 8II5 | 5826 | 54 21 46.41 | 120.18 | I. 185 | 0.9773560 | 5592 | 5559 54.15 | I15.35 |
| .136 | . 9493939 | 5822 | 542346.54 | 120.08 | . 186 | . 977 9150 | 5588 | 56 O1 49.45 | II5.25 |
| . 137 | - 9499758 | 5817 | $\begin{array}{llll}54 & 25 & 46.58\end{array}$ | I 19.98 | . 187 | . 9784735 | 5583 | 56 | II5.16 |
| . 138 | -950 5573 | 5812 | 542746.51 | 119.89 | . 188 | . 9790316 | 5578 | 560539.76 | II5.06 |
| . 139 | -951 I383 | 5807 | 542946.35 | 119.79 | . 189 | . 9795892 | 5574 | 560734.78 | 114.96 |
| 1. 140 | 0.9517188 | 5803 | 54 3I 46.09 | I 19.69 | I. 190 | 0.980 I463 | 5569 | $56 \quad 0929.69$ | II4.87 |
| . 141 | . 952 2588. | 5798 | 543345.74 | 119.59 | . I9I | . 9807030 | 5564 | 56 II 24.51 | 114.77 |
| . 142 | . 9528784 | 5793 | 543545.28 | 119.50 | . 192 | .98I 2592 | 5560 | 56 | I I 4.68 |
| . 143 | -953 4575 | 5789 | 543744.73 | 119.40 | - 193 | .98i 8i49 | 5555 | 561513.87 | I I 4.58 |
| . I44 | . 954 036I | 5784 | 543944.08 | I 19.30 | . 194 | .9823702 | 555 I | 56 I7 08.4I | I 14.49 |
| I. I45 | 0.9546143 | 5779 | 54 41 43.34 | I 19.21 | I. 195 | 0.9829251 | 5546 | 56 I9 02.85 | II4.39 |
| . 146 | . 9551920 | 5775 | 544342.49 | II9.1I | . 196 | . 9834794 | 5541 | 5620 57.19 | II 4.30 |
| . 147 | . 9557692 | 5770 | 54454 I .55 | 119.01 | . 197 | . 9840333 | 5537 | 562251.44 | I I4.20 |
| . I48 | . 9563460 | 5765 | 544740.51 | I 18.91 | . 198 | .984 5858 | 5532 | 562445.60 | II4. I I |
| . 149 | -956 9222 | 5760 | 544939.38 | II8.82 | . 199 | . 985 I397 | 5527 | 562639.66 | II4.0I |
| I. 150 | 0.9574980 | 5756 | 545138.15 | 118.72 | I. 200 | 0.9856922 | 5523 | $56 \quad 2833.62$ | 113.92 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $\mathrm{an}^{-1}\left(e^{\mathrm{x}}\right)-\frac{\pi}{2}$ | h | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| $u$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\text {f }}$ | u | gd u | $\omega \mathrm{F}^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| I. 200 | 0. |  | $56^{\circ} 28^{\prime} 33.162$ | I 13. |  | 1.012 7356 |  | $0^{\circ}{ }^{\prime}{ }^{\prime \prime}$ |  |
| . 201 | . 9862443 | 5518 | $56 \quad 3027.49$ | II3.82 | . 251 | .OI3 2649 | 5291 | 580320.89 |  |
| . 202 | . 9867959 | 5514 | 5632 21. 26 | 113.73 | . 252 | . 0137938 | 5286 | $\begin{array}{lllll}58 & 05 & 09.98\end{array}$ | 109.04 |
| . 203 | .9873470 | 5509 | 563.414 .94 | 113.63 | . 253 | . O14 3222 | 5282 | 580658.98 | 108.95 |
| . 204 | . 9878977 | 5504 | 563608.53 | II3.54 | . 254 | . 0148502 | 5277 | 580847.88 | 108.86 |
| I. 205 | 0.9884479 | 5500 | 563802.02 | 113.44 | I. 255 | I.OI5 3777 | 5273 | 58 10 36.69 | 108.76 |
| . 206 | . 9889977 | 5495 | 563955.42 | II3.35 | . 256 | . 0159048 | 5269 | 58 12 25.40 | 108.67 |
| . 207 | . 9895470 | 5491 | 564148.72 | II3.25 | . 257 | .016 4314 | 5264 | 581414.03 | 108.58 |
| . 208 | .9900958 | 5486 | 5643 41.92 | 113.16 | . 258 | .016 9576 | 5260 | $58 \quad 1602.56$ | 108.49 |
| . 209 | . 9906442 | 5482 | 564535.03 | II3.06 | . 259 | . 0174833 | 5255 | 58 I7 51.00 | 108.39 |
| 1. 210 | 0.991 1921 | 5477 | 564728.05 | 112.97 | 1.260 | 1.018 0086 | 5251 | 58 19 39.35 | 108.30 |
| . 211 | . 9917396 | 5472 | 564920.97 | I 12.88 | . 261 | . 0185335 | 5246 | 58 21 27.61 | 108.21 |
| . 212 | . 9922866 | 5468 | 565113.80 | I 12.78 | . 262 | . 0190578 | 5242 | $\begin{array}{lllllllllllllll}58 & 23 & 15.77\end{array}$ | 108.12 |
| . 213 | . 9928331 | 5463 | 565306.54 | I12.69 | . 263 | . 0195818 | 5237 |  | 108.03 |
| . 214 | .9933792 | 5459 | 5654 59.17 | I 12.59 | . 264 | . 0201053 | 5233 | 582651.82 | 107.93 |
| 1.215 | 0.9939249 | 5454 | 565651.72 | I 12.50 | I. 265 | I. 0206283 | 5228 | $58 \quad 2839.71$ | 107.84 |
| . 216 | . 9944700 | 5449 | 565844.17 | I 12.40 | . 266 | .021 1510 | 5224 | $58 \quad 3027.50$ | 107.75 |
| . 217 | . 9950148 | 5445 | 570036.53 | I I2.3I | . 267 | .021 673I | 5219 | 5832 I5.21 | 107.66 |
| . 218 | . 9955590 | 5440 | $\begin{array}{llll}57 & 02 & 28.79\end{array}$ | I 12.22 | . 268 | .0221948 | 5215 | $\begin{array}{lllllllllllll}58 & 34 & 02.82\end{array}$ | 107.57 |
| . 219 | . 9961028 | 5436 | 570420.96 | I12.12 | . 269 | .022716 I | 5210 | 583550.34 | 107.47 |
| 1.220 | 0.9966462 | 5431 | 570613.03 | 112.03 | 1.270 | 1.023 2369 | 5206 | $\begin{array}{llll}58 & 37 & 37.77\end{array}$ | 107.38 |
| . 22I | . 997 I891 | 5427 | 570805.01 | III. 93 | . 271 | .0237573 | 5202 | 583925.10 | 107.29 |
| . 222 | . 997 7315 | 5422 | 570956.90 | III. 84 | . 272 | .0242772 | 5197 | 58 41 I2.35 | 107.20 |
| . 223 | . 9982735 | 5418 | 57 II 48.69 | III. 74 | . 273 | . 0247967 | 5193 | 584259.50 | 107. 11 |
| . 224 | . 998 8150 | 5413 | 57.1340 .39 | III. 65 | . 274 | . 025 3I58 | 5188 | 584446.56 | 107.02 |
| 1.225 | 0.999356 I | 5408 | 57 I5 31.99 | III. 56 | 1.275 | I. 0258344 | 5184 | 584633.53 | 106.92 |
| . 226 | . 9998967 | 5404 | 57 I7 23.50 | II I . 46 | . 276 | . 0263526 | 5179 | 5848 20.41 | 106.83 |
| . 227 | I.000 4369 | 5399 | 57 I9 14.92 | III. 37 | . 277 | .0268703 | 5175 | $58 \quad 5007.20$ | 106.74 |
| . 228 | . 0009766 | 5395 | 57 21 06.24 | III. 28 | . 278 | .0273876 | 5171 | 585153.90 | 106.65 |
| . 229 | . OOI 5I58 | 5390 | 572257.47 | III. 18 | . 279 | .0279044 | 5166 | 585340.50 | 106.56 |
| 1.230 | 1.002 0546 | 5386 | 572448.60 | II I . 09 | I. 280 | I. 0284208 | 5162 | $5855 \quad 27.02$ | 106.47 |
| . 231 | . 0025930 | 538 I | 572639.64 | I 10.99 | . 281 | . 0289367 | 5157 | $\begin{array}{llllllll}58 & 57 & 13.44\end{array}$ | 106.38 |
| . 232 | . 0031309 | 5377 | $57 \quad 2830.59$ | 110.90 | . 282 | . 0294523 | 5153 |  | 106.29 |
| . 233 | . 0036683 | 5372 | 57302 I .45 | I 10.8I | .283 | .0299673 | 5148 | 590046.01 | 106. 19 |
| . 234 | . 0042053 | 5368 | 5732 12.2I | 110.71 | . 284 | .0304819 | 5144 | 590232.16 | 106. 10 |
| 1.235 | 1.0047418 | 5363 | $57 \quad 3402.88$ | 110.62 | 1. 285 | 1.0309961 | 5140 | 590418.22 | 106.01 |
| . 236 | . 0052779 | 5359 | $57 \quad 35 \quad 53.45$ | 110.53 | . 286 | .031 5099 | 5135 | 590604.19 | 105.92 |
| . 237 | . 005 8ı35 | 5354 | 573743.93 | 110.43 | . 287 | .0320232 | 5131 | 590750.06 | 105.83 |
| . 238 | . 0063487 | 5349 | $573934 \cdot 32$ | 110.34 | . 288 | .0325360 | 5126 | 590935.85 | 105.74 |
| . 239 | . 0068834 | 5345 | 574124.6 I | 110.25 | . 289 | .0330485 | 5122 | 59 II 2I. 54 | 105.65 |
| I. 240 | 1.0074177 | 5340 | 574314.82 | 110.15 | 1.290 | 1.0335605 | 5118 | 59 I3 07.15 | 105.56 |
| . 241 | . 0079515 | 5336 | $57 \quad 4504.92$ | 110.06 | . 291 | . 0340720 | 5113 | 591452.66 | $105.47$ |
| . 242 | . 0084840 | 5331 | 574654.94 | 109.97 | . 292 | .0345831 | 5109 | 59 16 38.08 | 105.38 |
| . 243 | . 009 0178 | 5327 | 574844.86 | 109.88 | . 293 | .0350938 | 5104 | 59 I8 23.4I | 105.29 |
| . 244 | . 0095503 | 5322 | 575034.69 | 109.78 | . 294 | .0356040 | 5100 | 592008.66 | 105.20 |
| 1.245 | I. 10100823 | 5318 | 575224.43 | 109.69 | I. 295 | 1.036 II38 | 5096 | 59 21 53.81 | 105. 11 |
| . 246 | . 0106139 | 5313 | 575414.07 | 109.60 | . 296 | . 036 623I | 5091 | $\begin{array}{lllll}59 & 23 & 38.87\end{array}$ | 105.02 |
| .247 | .OII 1450 | 5309 | 5756 | 109.50 | . 297 | . 0371320 | 5087 | $\begin{array}{llll}59 & 25 & 23.84\end{array}$ | 104.93 |
| . 248 | . OII 6756 | 5304 | 575753.08 | 109.41 | . 298 | . 0376405 | 5083 | $\begin{array}{llll}59 & 27 & 08.72 \\ 59 & 28 & 53.51\end{array}$ | 104.83 |
| . 249 | . 0122058 | 5300 | 575942.44 | 109.32 | . 299 | .0381485 | 5078 | 5928 53.5I | 104.74 |
| 1.250 | 1. OI 27356 | 5295 | 58 OI 31.72 | 109.23 | 1.300 | 1.0386561 | 5074 | 593038.21 | 104.65 |
| u | $2 \tan ^{-1}\left(e^{4}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

SMITHSONIAN TABLES

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | od u | ${ } \mathrm{F}_{0}{ }^{\prime}$ | a | du | $\omega \mathrm{F}_{0}{ }^{\prime}$ | ad $u$ | ${ }^{\prime}{ }_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.300 | 1.038 6561 |  | $5930 \quad 38.21$ | 104.65 | 1.350 | 1.0634837 | 4858 | $60^{\circ} 55 \quad 59.27$ | . 21 |
| 301 | . 0391633 | 506 | 593222.82 |  | . 35 | . 06 | 4854 | 605739.43 | 100.12 |
| . 302 | . 0396700 | 5065 | 593407.34 | 104.47 | . 352 | . 0644546 | 4850 | 6059 19.51 | 100.03 |
| . 303 | . 0401763 | 5061 | 5935 51.77 | 104.38 | . 353 | . 0649393 | 4846 | 610059.50 | 99.95 |
| -304 | . 0406822 | 5056 | 5937 36.10 | 104.29 | - 354 | . 0654237 | 4841 | 610239.41 | 99.86 |
| I. 305 | 1.041 1876 | 5052 | 593920.35 | 104.20 | I. 355 | 1. 0659076 | 4837 | 61 0419.22 | 99.77 |
| . 30 | .041 6926 | 5048 | 5941 04.51 | 104.II | . 356 | . 0663911 | 4833 | 61 0558.95 | 99.69 |
| . 3 | . 0421971 | 5043 | 594248.58 | 104.02 | . 357 | . 0668742 | 4829 | 61 0738.59 | 99.60 |
| . 308 | . 0427012 | 5039 | 594432.56 | 103.93 | . 358 | . 0673568 | 4824 | 610918.15 | 99. |
| . 309 | . 0432049 | 5035 | 594616.45 | 103.84 | - 359 | . 0678390 | 4820 | 61 10 57.61 | 99.42 |
| 1.310 | I. 043 7081 | 5030 | 594800.25 | 103.76 | 1. 360 | I. 0683209 | 4816 | 611236.99 | 99.34 |
| . 311 | . 0442109 | 5026 | 594943.96 | 103.67 | . 361 | . 0688022 | 4812 | 611416.29 | 99.25 |
| . 312 | . 0447133 | 5021 | 595127.58 | 103.58 | . 362 | . 0692832 | 4808 | 611555.49 | . 16 |
| .313 | . 0452152 | 5017 | 5953 II.11 | 103.49 | . 363 | . 0697637 | 4803 | 611734.61 | 99.08 |
| . 314 | . 0457167 | 5013 | 5954 54.55 | 103.40 | . 364 | . 0702439 | 4799 | 611913.64 | 98.99 |
| 1.315 | 1.0462178 | 5008 | 595637.91 | 103.31 | 1. 365 | 1. 0707236 | 4795 | 612052.59 |  |
| . 316 | . 0467184 | 5004 | 595821.17 | 103.22 | . 366 | . 0712028 | 4791 | 612231.45 | 82 |
| . 317 | . 0472186 | 5000 | 600004.34 | 103.1 | - 367 | . 071 6817 | 4786 | 612410.22 | 73 |
| . 318 | . 0477184 | 4995 | 60 or 47.43 | 103.04 | - 368 | . 0721601 | 4782 | $\begin{array}{llll}61 & 25 & 48.90\end{array}$ | 98.64 |
| . 319 | . 0482177 | 4991 | 600330.42 | 102.95 | . 369 | . 0726382 | 4778 | 612727.50 |  |
| 1.320 | 1.0487166 | 4987 | 600513.33 | 102.86 | 1. 370 | 1.0731158 | 4774 | 61 2906.01 | 8.47 |
| . 321 | . 0492151 | 4983 | 60 o6 56.14 | 102.77 | . 371 | . 0735929 | 4770 | 613044.44 | 98.38 |
| . 322 | . 049 7131 | 4978 | 600838.87 | 102.6 | . 372 | . 0740697 | 4766 | 613222.78 | 98.30 |
| . 323 | . 0502107 | 4974 | 601021.51 | 102.59 | -373 | . 0745460 | 4761 | 6134 or. 03 | 98.21 |
| . 324 | . 0507079 | 4970 | 601204.06 | 102.50 | - 374 | . 0750220 | 4757 | 613539.20 | 98.12 |
| I. 325 | 1.0512046 | 4965 | 60 I3 46.52 | 102 | I. 375 | 1. 0754975 | 4753 | 613717.28 | 98.04 |
| . 326 | . 0517009 | 4961 | $6015 \quad 28.89$ | 102. | . 376 | . 0759725 | 4749 | 613855.27 | 97.95 |
| . 327 | . 0521968 | 4957 | 601711.17 | 102.24 | . 37 | . 0764472 | 4745 | 614033.18 | 97.86 |
| . 3 | . 0526923 | 4952 | 601853.37 | 102.15 | . 378 | . 0769215 | 4740 | 6142 II .00 | 97.78 |
| . 329 | . 0531873 | 4948 | 602035.47 | 102.06 | -379 | . 0773953 | 4736 | 61 4348.73 |  |
| 1.330 | 1.0536819 | 4944 | 602217.49 | 101 | I. 380 | 1. 0778687 | 4732 | 61 4526.38 | 97.61 |
| . 33 I | . 0541760 | 4939 | 602359.4 I | 101.8 | . 381 | . 0783417 | 4728 | 614703.94 | 97.52 |
| - 3 | . 0546698 | 493 | 602541.25 | 101. 79 | . 382 | . 0788143 | 4724 | 614841.42 | 97.43 |
| -33 | .0551631 | 493 | 602723.00 | 101. 71 | -383 | . 0792865 | 4720 | 615018.81 | $97 \cdot 35$ |
| - 3 | . 055 | 4927 | $60 \quad 2904.67$ | 101. 62 | -384 | . 0797582 | 4715 | 615156.12 | 97 |
| 1.335 | 1.0561484 | 4922 | 603046.24 | IOI. 53 | I. 385 | 1.0802295 | 47 II | 61 5333.34 | 97.18 |
| . 33 | . 0566404 | 4918 | 603227.72 | 101. 4 | . 386 | . 0807005 | 4707 | 6155 10.47 | 97.09 |
| - 337 | . 0571320 | 4914 | 603409.12 | 101. 35 | -387 | .081 1710 | 4703 | 615647.52 | 97.01 |
| . 338 | . 0576231 | 4909 | 603550.43 | 101. 26 | -388 | .081 6411 | 469 | 615824.48 | 96.92 |
| . 339 | . 0581139 | 4905 | 603731.65 | IoI. 18 | -389 | . 0821107 | 4695 | 6200 or. 36 | 96.83 |
| 1.340 | 1.0586042 |  | 6039 12.78 | 101.09 | I. 390 | 1.082 5800 | 4691 | 62 or 38.15 | 96.75 |
| . 341 | . 0590940 | 4897 | 604053.83 | 101.00 | -391 | . 0830488 | 4686 | 620314.86 | 96.66 |
| . 342 | . 0595835 | 4892 | 604234.78 | 100.91 | . 392 | . 8835173 | 4682 | 620451.48 | 96.58 |
| - 343 | . 0600725 | 4888 | 604415.65 | 100 | - 393 | . 0839853 | 4678 | 620628.01 | 96.49 |
| - 344 | . 060 5611 | 48 | 6045 56.43 | 100. | - 394 | . 0844529 | 4674 | 620804.46 | 96.41 |
| I. 345 | 1.061 0493 | 4880 | 604737.12 | 100.65 | I. 395 | 1.0849201 | 4670 | 620940.83 | 96.32 |
| . 346 | .061 5370 | 4875 | 6049 17.73 | 100.56 | . 396 | . 0853868 | 4666 | 62 II 17.11 | 96.24 |
| . 347 | . 0620243 | 4871 | 605058.24 | 100.47 | . 397 | . 0858532 | 4662 | 621253.30 | 96.15 |
| . 348 | . 0625112 | 4867 | 605238.67 | 100.38 | . 398 | . 0863192 | 4657 | 621429.41 | 96.07 |
| - 349 | . 0629977 | 4863 | 6054 19.01 | 100.30 | -399 | . 0867847 | 4653 | 621605.44 | 95.98 |
| 1. 350 | 1.063 4837 | 4858 | 605559.27 | 100.21 | I. 400 | 1.0872498 | 4649 | 621741.37 | 95.90 |
| u | $2 \tan ^{-1}\left(e^{\mathrm{a}}\right)-\frac{\pi}{2}$ |  | $2 \tan ^{-1}\left(e^{40}\right)-90^{\circ}$ | w sech u |  | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | w sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | w sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
| 1. 400 | 1.087249 | 4 | 62 I7 41.37 | 95.90 | 1. 450 | I. 1099869 | 4447 | 6335 51.24 | 91.72 |
| . 401 | . 0877145 | 4645 | 62 I9 I7.23 | 95.8I | .45I | . IIO 4314 | 4443 | $63 \quad 3722.92$ | 91.64 |
| . 402 | . 088 I788 | 464 I | $62 \quad 2053.00$ | 95.73 | . 452 | . IIO 8755 | 4439 | 6338 54.52 | 91.56 |
| . 403 | . 0886427 | 4637 | $\begin{array}{llll}62 & 22 & 28.68\end{array}$ | 95.64 | . 453 | . III 3192 | 4435 | 634026.03 | 91.47 |
| . 404 | .0891062 | 4633 | 622404.28 | 95.56 | . 454 | . III 7624 | 4431 | 63 41 57.46 | 91.39 |
| I. 405 | I. 0895693 | 4629 | 622539.80 | 95.47 | I. 455 | I. II2 2053 | 4427 | $63 \quad 43 \quad 28.82$ | 91.3I |
| . 406 | . 0900320 | 4625 | $62 \quad 2715.23$ | 95.39 | . 456 | . II2 6478 | 4423 | 634500.08 | 91.23 |
| . 407 | . 0904942 | 4620 | 622850.58 | 95.30 | . 457 | . II3 0899 | 4419 | 6346 31.27 | 91. 15 |
| . 408 | . 0909561 | 4616 | 623025.84 | 95.22 | . 458 | .113 5316 | 4415 | 634802.38 | 91.07 |
| . 409 | . 0914175 | 4612 | 6232 O1. 02 | 95.14 | . 459 | . II3 9729 | 44 II | 634933.40 | 90.98 |
| 1.410 | I.091 8785 | 4608 | 6233 36.II | 95.05 | I. 460 | I.II4 4138 | 4407 | 63 51 04.35 | 0.90 |
| .41I | . 0923391 | 4604 | 6235 II. 12 | 94.97 | . 46 I | . II4 8543 | 4403 | 635235.2 I | 90.82 |
| . 412 | . 0927993 | 4600 | 623646.04 | 94.88 | . 462 | . II5 2944 | 4399 | 635405.99 | 90.74 |
| . 413 | . 0932591 | 4596 | 623820.88 | 94.80 | . 463 | . 1157341 | 4395 | 635536.68 | 90.66 |
| . 414 | . 0937185 | 4592 | 623955.64 | 94.71 | . 464 | . II6 I734 | 4391 | 635707.30 | 90.58 |
| 1.415 | 1.0941775 | 4588 | 624130.31 | 94.63 | I. 465 | I. 1166124 | 4387 | $63 \quad 58 \quad 37.83$ | 90.49 |
| .416 | . 0946361 | 4584 | 624304.90 | 94.55 | . 466 | . II7 0509 | 4383 | 640008.29 | 90.41 |
| . 417 | . 0950942 | 4580 | 624439.40 | $94 \cdot 46$ | . 467 | . II7 4890 | 4379 | 64 O1 38.66 | 90.33 |
| . 418 | . 0955520 | 4576 | 624613.82 | 94.38 | . 468 | . II7 9268 | 4375 | 640308.95 | 90.25 |
| .419 | . 0960094 | 4571 | 624748.16 | 94.29 | . 469 | . II8 364I | 4372 | 6404 39.16 | 90.17 |
| I. 420 | 1.096 4663 | 45 | 624922.41 | 94.21 | I. 470 | I. 118801 r | 4368 | 640609.29 | . 09 |
| . 42 I | . 0969228 | 4563 | 625056.58 | 94.13 | . 471 | . II9 2377 | 4364 | 640739.34 | OI |
| . 422 | . 0973790 | 4559 | 625230.66 | 94.04 | . 472 | . 1196738 | 4360 | 640909.31 | 89.93 |
| . 423 | . 0978347 | 4555 | 625404.66 | 93.96 | . 473 | . 1201096 | 4356 | 64 10 39.19 | 89.85 |
| . 424 | . 0982900 | 4551 | 625538.58 | 93.88 | . 474 | . 1205450 | 4352 | 64 12 09.00 | 89.76 |
| I. 425 | 1. 0987449 | 4547 | 625712.41 | 93.79 | I. 475 | I. 1209800 | 4348 | $64 \quad 13 \quad 38.72$ | 89.68 |
| . 426 | . 0991994 | 4543 | 625846.16 | 93.71 | .476 | . 1214146 | 4344 | 641508.37 | 89.60 |
| . 42 | . 0996536 | 4539 | 630019.83 | 93.62 | . 477 | . 1218488 | 4340 | 641637.93 | 89.52 |
| . 428 | . 1001073 | 4535 | 63 or 53.41 | 93.54 | . 478 | . 1222826 | 4336 | 6418 07.41 | 89.44 |
| . 429 | . 1005606 | 4531 | 6303 26.91 | 93.46 | . 479 | . 122 716I | 4332 | 64 I9 36.8I | 89.36 |
| I. 430 | I. IOI Or34 | 4527 | 630500.33 | 93.37 | I. 480 | I. 123 I491 | 4328 | 64 21 06. 13 | 89.28 |
| . 43 I | . IOI 4659 | 4523 | 630633.66 | 93.29 | . 48 I | . 1235818 | 4325 | $64 \quad 2235.37$ | 89.20 |
| . 432 | . IOI 9180 | 4519 | 630806.91 | 93.21 | . 482 | . 124 OI40 | 432 I | $64 \quad 2404.53$ | 89.12 |
| . 433 | . 1023697 | 4515 | 630940.08 | 93.13 | . 483 | . 1244459 | 4317 | 642533.61 | 89.04 |
| . 434 | . 1028210 | 45 II | 63 II I3.16 | 93.04 | . 484 | . 1248774 | 4313 | 6427 02.6I | 88.06 |
| I. 435 | 1. 1032719 | 4507 | 63 12 46.16 | 92.96 | I. 485 | I. 1253085 | 4309 | $64 \quad 2831.53$ | 8.88 |
| . 436 | . 1037223 | 4503 | 63 I4 19.08 | 92.88 | . 486 | . 1257392 | 4305 | 643000.37 | 88.80 |
| . 43 | . 1041724 | 4499 | 63 I5 51.91 | 92.79 | . 487 | . 1261695 | 4301 | 64 31 29.13 | 88.72 |
| . 438 | . 1046221 | 4495 | 63 I7 24.66 | 92.71 | . 488 | . 1265994 | 4297 | 643257.81 | 88.64 |
| . 439 | . 1050714 | 449 I | 63 I8 57.33 | 92.63 | . 489 | . 1270289 | 4293 | 643426.41 | 88.56 |
| 1.440 | I. 1055202 | 4487 | $63 \quad 20 \quad 29.92$ | 92.54 | I. 490 | I. 127458 I | 4290 | $6435 \quad 54.93$ | 88.48 |
| . 441 | . 1059687 | 4483 | $63 \quad 2202.42$ | 92.46 | . 491 | . 1278869 | 4286 | $6437 \quad 23.37$ | 88.40 |
| . 442 | . 1064168 | 4479 | $\begin{array}{lllll}63 & 23 & 34.84\end{array}$ | 92.38 | . 492 | . 1283152 | 4282 | 6438 51.72 | 88.32 |
| . 443 | . 1068644 | 4475 | 6325 07.18 | 92.30 | . 493 | . 1287432 | 4278 | 644020.00 | 88.24 |
| . 444 | . 107 3117 | 4471 | $63 \quad 2639.44$ | 92.21 | . 494 | . 1291708 | 4274 | 64 4I 48.20 | 88.16 |
| I. 445 | I. 1077586 | 4467 | 6328 II. 61 | 92.13 | I. 495 | I. 1295980 | 4270 | 644316.32 | 88.08 |
| . 446 | . 1082050 | 4463 | 632943.70 | 92.05 | . 496 | . I30 0249 | 4266 | 644444.36 | 88.00 |
| . 447 | . 10865 II | 4459 | 63 31 15.71 | 91.97 | -497 | . I30 45I3 | 4263 | $64 \quad 4612.32$ | 87.92 |
| . 448 | . 1090968 | 4455 | $63 \quad 3247.63$ | 91.88 | . 498 | . I30 8774 | 4259 | 644740.20 | 87.84 |
| . 449 | . 109542 I | 4451 | 633419.48 | 91.80 | . 499 | . I3I 303I | 4255 | 6449 08.01 | 87.76 |
| 1.450 | I. 1099869 | 4447 | 633551.24 | 91.72 | 1.500 | I.I3I 7283 | 4251 | $64 \quad 5035.73$ | 87.68 |
| $u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | hu | $2 \boldsymbol{\operatorname { t a n }}^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | $u$ | $\operatorname{an}^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | sech |

SMITHSONIAN TABLES

The Gudermannian.

| $u$ | gd u | $\omega \mathrm{F}$ | gd u | $\omega \mathbf{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
| I. 500 | I.I3I 7283 | 425 I | $64 \quad 50 \quad 35.73$ | 87.68 | I. 550 | I. 1525078 | 4062 | 660201.8 I | 83.78 |
| . 501 | .132 I532 | 4247 | $64 \quad 52 \quad 03.37$ | 87.60 | . 551 | . 1529139 | 4058 | $\begin{array}{llll}66 & 03 & 25 \cdot 55\end{array}$ | 83.71 |
| . 502 | . 132 5778 | 4243 | $6453 \quad 30.93$ | 87.52 | . 552 | . 153 3195 | 4055 | 660449.22 | 83.63 |
| . 503 | . 1330019 | 4239 | 645458.42 | 87.44 | . 553 | - 1537248 | 4051 | 6606 I2.8I | 83.55 |
| . 504 | . I33 4257 | 4236 | 645625.82 | 87.37 | - 554 | . 1541297 | 4047 | 660736.33 | 83.48 |
| I. 505 | I. I33 8490 | 4232 | 645753.15 | 87.29 | I. 555 | I. I54 5342 | 4043 | 660859.77 | 83.40 |
| . 506 | . I34 2720 | 4228 | 645920.40 | 87.21 | . 556 | . I54 9384 | 4040 | 66 Io 23.14 | 83.33 |
| . 507 | . I34 6946 | 4224 | $650047 \cdot 56$ | 87.13 | - 557 | . 155342 I | 4036 | 66 II 46.42 | 83.25 |
| . 508 | . 1351168 | 4220 | 6502 I4.65 | 87.05 | - 558 | . I55 7456 | 4032 | 66 I3 09.63 | 83.17 |
| . 509 | . 1355387 | 4216 | 650341.66 | 86.97 | - 559 | . 156 I486 | 4029 | 66 I4 32.77 | 83.10 |
| 1.510 | I. 1359601 | 4213 | $\begin{array}{llll}65 & 05 & 08.59\end{array}$ | 86.89 | I. 560 | I. 1565513 | 025 | 66 I5 55.83 | 83.02 |
| . 511 | . 13638 I 2 | 4209 | 650635.44 | 86.81 | . 56 I | . 1569536 | 4021 | 66 I7 18.81 | 82.95 |
| . 512 | . 1368019 | 4205 | 650802.22 | 86.73 | . 562 | . 1573556 | 4018 | 66 I8 41.72 | 82.87 |
| . 513 | . 137 2222 | 4201 | 650928.91 | 85.66 | . 563 | .157 7571 | 4014 | 662004.55 | 82.79 |
| . 514 | . 137642 I | 4197 | 65 10 55.53 | 86.58 | . 564 | . 1581583 | 4010 | 66 21 27.3 I | 82.72 |
| I.515 | I. 1380617 | 4 | 651222.07 | 86.50 | I. 565 | I. 1585592 | 007 | 662249.99 | 82.64 |
| . 516 | . 1384808 | 41 | 65 I3 48.52 | 86.42 | . 566 | . 1589597 | 4003 | $66 \quad 2412.59$ | 82.57 |
| . 517 | . 1388896 | 4186 | 65 I5 14.91 | 86.3 | . 567 | . 1593598 | 3999 | $66 \quad 25 \quad 35.12$ | 82.49 |
| . 518 | . 1393180 | 4182 | 651641.21 | 86. 26 | . 568 | . 1597595 | 3996 | $66 \quad 26 \quad 57 \cdot 57$ | 82.42 |
| . 519 | . I39 7360 | 4178 | 65 I8 07.43 | 86. 18 | . 569 | . 1601589 | 3992 | 662819.95 | 82.34 |
| I. 520 | I. I40 I537 | 4175 | 65 19 33.58 | 86. | 1.570 | I. 1605579 | 3988 | 662942.25 | 82.26 |
| . 521 | . 1405709 | 4171 | $65 \quad 20 \quad 59.64$ | 86.03 | . 571 | . 1609566 | 3985 | 663104.48 | 82.19 |
| . 522 | . 1409878 | 4167 | $\begin{array}{llll}65 & 22 & 25.63\end{array}$ | 85.95 | . 572 | . 1613548 | 398I | 663226.63 | 82.11 |
| . 523 | . I4I 4043 | 4163 | $65 \quad 2351.54$ | 85.87 | . 573 | .161 7527 | 3977 | 663348.71 | 82.04 |
| . 524 | .14I 8205 | 4159 | $65 \quad 2517.38$ | 85.79 | . 574 | .162 1503 | 3974 | 6635 10.71 | 81.96 |
| I. 5 | I. 142 | 415 | $65 \quad 2643.13$ | 85.72 | I. 575 | 1.162 5475 | 0 | 663632.63 | 81. 89 |
| . 526 | . 1426516 | 415 | $65 \quad 28$ 08.81 | 85.64 | . 576 | . 1629443 | 3966 | $6637 \quad 54.48$ | 81.8I |
| . 5 | . I43 0666 | 4148 | 652934.41 | 85.5 | . 577 | . 1633408 | 3963 | 663916.26 | 81.74 |
| . 528 | . I43 48I2 | 4144 | 653059.93 | 85.48 | . 578 | . 1637369 | 3959 | 664037.96 | 8ı. 66 |
| . 529 | . I438954 | 4141 | $65 \quad 32 \quad 25.37$ | 85.40 | - 579 | . I64 I326 | 3955 | 664159.58 | 8I. 59 |
| 1.530 | I. I44 | 4137 | $\begin{array}{llll}65 & 33 & 50.74\end{array}$ | 85.33 | 1.580 | I. 164 5279 | 3952 | 6643 2I.I3 | 8 I .5 I |
| . 531 | . I44 7228 | 4 I 33 | 653516.02 | 85.25 | . 581 | . 164 9230 | 3948 | 6644 42.6I | 8 I .44 |
| . 532 | . 145 I359 | 4129 | 653641.23 | 85.17 | . 582 | .1653176 | 3945 | 6646 04.01 | 8ı. 36 |
| . 533 | . 1455486 | 4125 | $\begin{array}{lllll}65 & 38 & 06.37\end{array}$ | 85.09 | . 583 | .1657119 | 3941 | $6647 \quad 25 \cdot 33$ | 8I. 29 |
| . 534 | . 1459610 | 4122 | 653931.42 | 85.02 | . 584 | . 1661058 | 3937 | 664846.58 | 8I. 21 |
| I. 535 | 1.146 3730 | 4118 | 654056.40 |  | I. 585 | I. 1664993 | 934 | 665007.76 | 8I. 14 |
| . 536 | . I46 7846 | 4 II 4 | 6542 21.30 | 84.86 | . 586 | . 1668925 | 3930 | 66 51 28.86 | 8ı.06 |
| . 537 | . 1471958 | 4110 | 654346.12 | 84.78 | . 587 | . 1672854 | 3926 | 665249.89 | 80.99 |
| . 538 | . 1476067 | 4107 | 654510.87 | 84.71 | . 588 | . 1676778 | 3923 | 665410.84 | 80.92 |
| . 539 | . 148 OI72 | 4103 | $654635 \cdot 54$ | 84.63 | . 589 | . 1680699 | 3919 | 665531.72 | 80.84 |
| I. 540 | I. I48 4273 | 4099 | 6548 00.13 | 84.55 | I. 590 | I. 1684617 | 3916 | $6656 \quad 52.52$ | 80.77 |
| . 54 I | . 1488370 | 4095 | 654924.64 | 84.48 | . 591 | . 168853 I | 3912 | $66 \quad 5813.25$ | 80.69 |
| . 542 | . I49 2464 | 4092 | $65 \quad 5049.08$ | 84.40 | . 592 | . 169 244I | 3908 | 665933.91 | 80.62 |
| . 543 | . I49 6554 | 4088 |  | 84.32 | - 593 | . 1696348 | 3905 | 670054.49 | 80.54 |
| . 544 | . I50 0640 | 4084 | 655337.72 | 84.25 | - 594 | . 1700251 | 3901 | 670215.00 | 80.47 |
| I. 545 | I.I50 4722 | 4081 | 65 '55 OI. 93 | 84.17 | I. 595 | I.I70 4150 | 3898 | $6703 \quad 35.43$ | 80.40 |
| . 546 | . 1508801 | 4077 | 655626.06 | 84.09 | . 596 | . 1708046 | 3894 | 670455.79 | 80.32 |
| . 547 | - I5I 2876 | 4073 | 6557 50.11 | 84.01 | - 597 | . 1711938 | 3891 | 670616.07 | 80.25 |
| . 548 | . I5I 6947 | 4069 | 6559 14.08 | 83.94 | . 598 | -I7I 5827 | 3887 | 670736.28 | 80.17 |
| . 549 | . 152 IOI5 | 4066 | 660037.98 | 83.86 | - 599 | . 1719712 | 3883 | 670856.42 | 80.10 |
| I .550 | I. 1525078 | 4062 | 6602 or. 8 I | 83.78 | 1.600 | I. I72 3594 | 3880 | 671016.48 | 80.03 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{a}}\right)-90^{\circ}$ | $\omega$ s | u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |


| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime \prime}$ | u | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1. 600 | I. I72 3594 | 3880 | $67^{\circ} 10^{\prime} 16.48$ | 80.03 | 1.650 | 1.191 3170 | 3704 | $68^{\circ} 15^{\prime} 26^{\prime \prime} 76$ | 76.41 |
| . 601 | .172 7472 | 3876 | 67 II 36.47 | 79.95 | . 651 | . 191 6872 | 3701 | 68 16 43.13 | 76.34 |
| . 602 | . 1731346 | 3873 | 67 I2 56.39 | 79.88 | . 652 | . 192057 I | 3697 | 68 I7 59.44 | 76.27 |
| . 603 | . 173 5217 | 3869 | 67 I4 16.23 | 79.81 | . 653 | . 1924267 | 3694 | 68 19 15.67 | 76.20 |
| . 604 | . 1739084 | 3865 | 67 I5 36.00 | 79.73 | . 654 | . 1927960 | 3691 | 682031.83 | 76.12 |
| 1.605 | I. 1742948 | 3862 | 67 16 55.69 | 79.66 | 1.655 | I. 1931648 | 3687 | 68 21 47.92 | 76.05 |
| . 606 | . 1746808 | 3858 | 67 18 15.31 | 79.58 | . 656 | . 1935334 | 3684 | $68 \quad 2303.93$ | 75.98 |
| . 607 | . 1750665 | 3855 | 67 19 34.86 | 79.51 | . 657 | . 1939016 | 3680 | $68 \quad 2419.88$ | 75.91 |
| . 608 | . 1754518 | 385 I | $67 \quad 2054 \cdot 34$ | 79.44 | . 658 | . 1942695 | 3677 | 682535.76 | 75.84 |
| . 609 | . I75 8367 | 3848 | 6722 I3.74 | 79.36 | . 659 | . 1946370 | 3674 | 6826 5I. 57 | 75.77 |
| 1.610 | I. 1762213 | 3844 | 672333.07 | 79.29 | 1. 660 | I. 1950042 | 3670 | $68 \quad 28 \quad 07.30$ | 75.70 |
| .6II | . 1766056 | 3841 | 672452.32 | 79.22 | . 661 | . 1953710 | 3667 | $68 \quad 2922.97$ | 75.63 |
| . 612 | . 1769895 | 3837 | 6726 I1.50 | 79.15 | . 662 | . 1957375 | 3663 | 683038.56 | 75.56 |
| .613 | . 1773730 | 3834 | 672730.61 | 79.07 | . 663 | . 1961037 | 3660 | 683154.09 | 75.49 |
| .6I4 | . 1777562 | 3830 | 672849.65 | 79.00 | . 664 | . 1964695 | 36.56 | 683309.54 | 75.43 |
| 1.6I5 | I. 1781390 | 3826 | 673008.61 | 78.93 | 1. 665 | I. 196 8349 | 3653 | $6834 \quad 24.93$ | 75.36 |
| . 616 | .178 5215 | 3823 | 673127.50 | 78.85 | . 666 | . 1972001 | 3650 | 683540.24 | 75.29 |
| . 617 | . 1789036 | 3819 | 673246.32 | 78.78 | . 667 | . 1975649 | 3646 | 683655.49 | 75.22 |
| . 618 | . 1792853 | 3816 | 673405.06 | 78.71 | . 668 | . 1979293 | 3643 | $68 \quad 3810.66$ | 75.15 |
| . 619 | . 1796667 | 3812 | $6735 \quad 23.73$ | 78.63 | . 669 | . 1982935 | 3639 | 683925.77 | 75.08 |
| 1.620 | I. 180 0478 | 3809 | 673642.33 | 78.56 | 1.670 | I. 198 6572 | 3636 | 684040.80 | 75.01 |
| . 621 | . 1804285 | 3805 | 673800.86 | 78.49 | . 671 | . 1990207 | 3633 | 684155.77 | 74.94 |
| . 622 | . 1808089 | 3802 | 6739 19.31 | 78.42 | . 672 | . 1993838 | 3629 | 684310.66 | 74.87 |
| . 623 | . 1811889 | 3798 | 674037.69 | 78.34 | . 673 | . 1997465 | 3626 | 684425.49 | 74.80 |
| . 624 | . 1815685 | 3795 | 67 4I 56.00 | 78.27 | . 674 | . 2001090 | 3623 | 684540.24 | 74.72 |
| 1. 625 | I. 181 9478 | 3791 | 674314.24 | 78.20 | 1.675 | I. 20047 II | 3619 | 684654.93 | 74.65 |
| . 626 | . 1823268 | 3788 | 674432.40 | 78.13 | . 676 | . 2008328 | 3616 | 684809.55 | 74.58 |
| . 627 | . 1827054 | 3784 | $6745 \quad 50.49$ | 78.06 | . 677 | . 2011942 | 3612 | 684924.09 | $74 \cdot 5 \mathrm{I}$ |
| . 628 | . 1830836 | 3781 | 674708.51 | 77.98 | . 678 | . 2015553 | 3609 | 685038.57 | 74.44 |
| . 629 | . 1834615 | 3777 | 674826.46 | 77.91 | . 679 | . 2019160 | 3606 | 68 5I 52.98 | $74 \cdot 37$ |
| 1.630 | I. 1838390 | 3774 | 674944.33 | 77.84 | 1.680 | I. 2022764 | 3602 | 685307.32 | $74 \cdot 30$ |
| . 631 | . 1842162 | 3770 | 675102.13 | 77.77 | .68I | . 2026365 | 3599 | 6854 21.58 | 74.23 |
| . 632 | . 184593 I | 3767 | 675219.85 | 77.69 | . 682 | . 2029962 | 3596 | 685535.78 | 74.17 |
| . 633 | . 1849696 | 3763 | 675337.52 | 77.62 | . 683 | . 2033556 | 3592 | 685649.92 | 74.10 |
| . 634 | . 1853457 | 3760 | 675455.11 | 77.55 | . 684 | . 2037147 | 3589 | 685803.98 | 74.03 |
| 1. 635 | I. 1857215 | 3756 | 675612.62 | 77.48 | 1. 685 | 1.2040734 | 3586 | 6859 I7.97 | 73.96 |
| . 636 | . 1860970 | 3753 | 675730.07 | 77.41 | . 686 | . 2044318 | 3582 | 690031.89 | 73.89 |
| . 637 | . 186472 I | 3749 | $67 \quad 58 \quad 47.44$ | 77.34 | . 687 | . 2047899 | 3579 | 69 OI 45.75 | 73.82 |
| . 638 | . 1868469 | 3746 | 680004.74 | 77.26 | . 688 | . 2051476 | 3576 | 690259.53 | 73.75 |
| . 639 | . 1872213 | 3742 | 68 OI 21.97 | 77.19 | . 689 | . 2055050 | 3572 | 690413.25 | 73.68 |
| 1. 640 | 1.187 5953 | 3739 | 680239.12 | 77.12 | 1.690 | 1. 2058620 | 3569 | 690526.90 | 73.61 |
| . 641 | . 1879691 | 3735 | 680356.21 | 77.05 | . 691 | . 2062187 | 3566 | 690640.48 | 73.54 |
| . 642 | . 1883424 | 3732 | 680513.22 | 76.98 | . 692 | . 206 5751 | 3562 | 690753.99 | 73.48 |
| . 643 | . 1887155 | 3729 | 680630.16 | 76.91 | . 693 | . 2069312 | 3559 | 690907.43 | 73.41 |
| . 644 | . 189088 I | 3725 | 680747.03 | 76.83 | . 694 | . 2072869 | 3556 | 69 IO 20.80 | 73.34 |
| 1.645 | I. 1894605 | 3722 | $\begin{array}{llll}68 & 09 & 03.83\end{array}$ | 76.76 | 1.695 | I. 2076423 | 3552 | 69 II 34.1I | 73.27 |
| . 646 | . 1898325 | 3718 | 68 10 20.56 | 76.69 | . 696 | . 2079974 | 3549 | 69 I2 47.34 | 73.20 |
| . 647 | . 1902041 | 3715 | 68 II 37.22 | 76.62 | . 697 | . 208352 I | 3546 | 691400.51 | 73.13 |
| . 648 | . 1905754 | 3711 | 68 I2 53.80 | 76.55 | . 698 | . 2087065 | 3542 | 69 15 13.61 | 73.07 |
| . 649 | . 1909463 | 3708 | 68 I4 10.32 | 76.48 | . 699 | . 2090605 | 3539 | 691626.64 | 73.00 |
| 1.650 | 1.191 3170 | 3704 | 681526.76 | 76.41 | 1.700 | I. 2094143 | 3536 | 691739.60 | 72.93 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 72. |  |  |  |  | " ${ }^{1}$ |
| 1.700 | 1.2094143 | 3536 | 69 I7 39.60 | 72.93 | 1.750 | 1.2266847 | 3374 | 70 I7 O1. 89 | 69.59 |
| . 701 | . 2097677 | 3532 | 69 I8 52.50 | 72.86 | .751 | . 2270219 | 3370 | 70 I8 II. 44 | 69.52 |
| . 702 | . 2101208 | 3529 | $6920 \quad 05.32$ | 72.79 | . 752 | . 2273588 | 3367 | 701920.93 | 69.45 |
| . 703 | . 2104735 | 3526 | 69 21 18.08 | 72.72 | . 753 | . 2276954 | 3364 | $70 \quad 2030.35$ | 69.39 |
| . 704 | . 2108259 | 3522 | 692230.77 | 72.66 | . 754 | . 2280316 | 2361 | 70 21 39.71 | 69.32 |
| 1.705 | 1.2111780 | 3519 | 692343.39 | 72.59 | 1.755 | I. 2283676 | 3358 | 702249.00 | 69.26 |
| . 706 | . 2115297 | 3516 | 692455.95 | 72.52 | . 756 | . 2287032 | 3355 | $70 \quad 23: 58.23$ | 69.19 |
| . 707 | .211 8812 | 3513 | 692608.43 | 72.45 | . 757 | . 2290385 | 3351 | $\begin{array}{lllll}70 & 25 & 07.39\end{array}$ | 69.13 |
| . 708 | . 2122.323 | 3509 | $6927 \quad 20.85$ | 72.38 | . 758 | . 2293735 | 3348 | $70 \quad 2616.48$ | 69.06 |
| . 709 | . 2125830 | 3506 | 692833.20 | 72.32 | . 759 | . 2297082 | 3345 | $70 \quad 2725.51$ | 69.00 |
| 1.710 | I.212 9335 | 3503 | 692945.49 | 72.25 | 1.760 | 1.2300425 | 3342 | $70 \quad 2834.48$ | 68.93 |
| . 711 | . 2132836 | 3499 | 693057.70 | 72.18 | . 761 | . 2303765 | 3339 | $70 \quad 2943 \cdot 38$ | 68.87 |
| . 712 | . 2136334 | 3496 | $6932 \quad 09.85$ | 72.11 | . 762 | . 2307103 | 3336 | $70 \quad 3052.22$ | 68.80 |
| . 713 | . 2139828 | 3493 | 6933 21.93 | 72.05 | . 763 | .231 0437 | 3333 | $70 \quad 3200.99$ | 68.74 |
| . 714 | .214 3319 | 3490 | 693433.94 | 71.98 | . 764 | . 2313768 | 3329 | $70 \quad 33 \quad 09.69$ | 68.67 |
| 1.715 | 1.2146807 | 3486 | 693545.89 | 71.91 | 1.765 | 1.231 7096 | 3326 | $\begin{array}{llll}70 & 34 & 18.33\end{array}$ | 68.61 |
| . 716 | . 2150292 | 3483 | 6936 57.76 | 71.84 | . 766 | . 2320420 | 3323 | $7035 \quad 26.91$ | 68.54 |
| . 717 | . 2153774 | 3480 | $6938 \quad 09.57$ | 71.78 | . 767 | .2323742 | 3320 | $70 \quad 3635.42$ | 68.48 |
| . 718 | . 2157252 | 3477 | 693921.32 | 71.71 | . 768 | .2327060 | 3317 | $\begin{array}{lllll}70 & 37 & 43.87\end{array}$ | 68.42 |
| . 719 | .2160727 | 3473 | 694032.99 | 71.64 | . 769 | .2330376 | 33 I 4 | 703852.25 | 68.35 |
| 1.720 | 1. 2164198 | 3470 | 69 4I 44.60 | 71.58 | 1.770 | I. 2333688 | 33II | 704000.57 | 68.29 |
| . 721 | . 2167667 | 3467 | 6942 56.14 | 71.51 | . 771 | . 2336997 | 3307 | 70 41 08.83 | 68.22 |
| . 722 | . 217 I132 | 3464 | 694407.62 | 71.44 | . 772 | . 2340303 | 3304 | $7042 \quad 17.02$ | 68.16 |
| . 723 | . 2174594 | 3460 | $6945 \quad 19.02$ | 71.37 | . 773 | . 2343606 | 3301 | $70 \quad 43$ 25.14 | 68.09 |
| . 724 | . 2178053 | 3457 | 694630.37 | 71.31 | . 774 | . 2346905 | 3298 | 704433.20 | 68.03 |
| 1.725 | I. 218 I508 | 3454 | 694741.64 | 71.23 | I. 775 | I. 2350202 | 3295 | 704541.20 | 67.96 |
| . 726 | . 2184960 | 3451 | 694852.85 | 71.16 | . 776 | . 2353495 | 3292 | 704649.13 | 67.90 |
| . 727 | . 2188409 | 3447 | 695003.99 | 71.10 | . 777 | .2356786 | 3289 | 704757.00 | 67.84 |
| . 728 | . 2191855 | 3444 | 695115.06 | 71.03 | . 778 | .2360073 | 3286 | $\begin{array}{llll}70 & 49 & 04.80\end{array}$ | 67.77 |
| . 729 | . 2195297 | 344 I | 695226.06 | 70.96 | . 779 | .2363357 | 3283 | $70 \quad 5012.54$ | 67.71 |
| 1.730 | I. 2198737 | 3438 | $6953 \quad 37.90$ | 70.90 | 1.780 | 1.236 6638 | 3279 | 70 51 20.22 | 67.64 |
| . 73 I | . 2202173 | 3434 | 695447.88 | 70.83 | .781 | . 2369916 | 3276 | $70 \quad 52 \quad 27.83$ | 67.58 |
| . 732 | . 2205605 | 3431 | 695558.68 | 70.76 | . 782 | . 237 3191 | 3273 | $7053 \quad 35.38$ | 67.52 |
| . 733 | . 2209035 | 3428 | 695709.42 | 70.70 | . 783 | . 2376463 | 3270 | 705442.87 | 67.45 |
| . 734 | . 2212461 | 3425 | 6958 20.10 | 70.63 | . 784 | . 237 973I | 3267 | 705550.29 | 67.39 |
| 1.735 | I.221 5885 | 3422 | 695930.71 | 70.56 | 1. 785 | I. 2382997 | 3264 | $70 \quad 5657.65$ | 67.33 |
| . 736 | . 2219304 | 3418 | 70004 I .25 | 70.50 | . 786 | .2386259 | 3261 | $70 \quad 58 \quad 04.94$ | 67.25 |
| . 737 | . 2222721 | 3415 | 70 OI 51.72 | 70.43 | . 787 | . 2389519 | 3258 | 705912.17 | 67.20 |
| . 738 | . 222 6135 | 3412 | 700302.13 | 70.37 | . 788 | . 2392775 | 3255 | 710019.34 | 67.13 |
| . 739 | . 2229545 | 3409 | 700412.47 | 70.30 | . 789 | . 2396028 | 3252 | 71 OI 26.44 | 67.07 |
| 1.740 | I. 2232952 | 3405 | 700522.75 | 70.23 | 1.790 | I. 2399279 | 3249 | 710233.48 | 67.01 |
| . 741 | . 2236356 | 3402 | 700632.96 | 70.18 | . 791 | . 2402526 | 3246 | 710340.46 | 66.94 |
| . 742 | . 2239757 | 3399 | 700743.10 | 70.11 | . 792 | . 2405770 | 3243 | 710447.37 | 66.88 |
| . 743 | . 2243154 | 3396 | 70 08 53.18 | 70.05 | . 793 | . 240 90II | 3239 | 710542.22 | 66.82 |
| . 744 | . 2246548 | 3393 | 70 10 03.19 | 69.98 | . 794 | . 2412249 | 3236 | 7107 OI .01 | 66.76 |
| 1.745 | I. 2249940 | 3390 | 70 II 13.14 | 69.91 | I. 795 | 1.2415483 | 3233 | 710807.73 | 66.69 |
| . 746 | . 2253328 | 3386 | 701223.02 | 69.85 | . 796 | . 2418715 | 3230 | 710914.39 | 66.63 |
| . 747 | .2256712 | 3383 | $\begin{array}{lllll}70 & 13 & 32.84\end{array}$ | 69.78 | . 797 | . 2421944 | 3227 | 711020.99 | 66.57 |
| . 748 | .2260094 | 3380 | 70 14 42.59 | 69.72 | . 798 | . 2425170 | 3224 | 71 II 27.52 | 66.50 |
| . 749 | . 2263472 | 3377 | 70 I5 52.27 | 69.65 | . 799 | .2428392 | 3221 | $71 \quad 1233.99$ | 66.44 |
| 1.750 | 1. 2266847 | 3374 | 7017 O1. 89 | 69.59 | 1.800 | 1.2431612 | 3218 | 711340.40 | 66.38 |
| u | $2 \tan ^{-1}\left(e^{\mathrm{u}}\right)-\frac{\pi}{2}$ | hu | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| $u$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.800 | I. 243' 1612 | 3218 | 711340.40 | 66.38 | I. 850 | I. 2588759 | 00 |  |  |
| . 80 | . 2434828 | 3215 | 711446.75 | 65.31 | . 851 | . 2191826 | 3066 | 720845.05 | 63.24 |
| . 802 | .2438042 | 3212 | 711553.03 | 66.25 | . 852 | . 2594890 | 3063 | 720948.26 | 63:18 |
| . 803 | . 2441252 | 320 | 711659.25 | 66.19 | . 853 | . 2597952 | 3060 | 72 10 51.41 | 63.12 |
| . 804 | .2444460 | 3206 | 7 I I8 05.4 I | 66.13 | . 854 | . 260 IOI I | 3057 | 72 II 54.50 | 63.06 |
| 1. 805 | 1. 2447664 | 03 | 71 I9 II. 50 |  | I. 855 | I. 2604066 | 3054 | 721257.53 | 63.00 |
| . 806 | . 2450865 | 3200 | 712017.53 | 66.0 | . 856 | . 260 7199 | 3051 | 72 14 00.50 | 62.94 |
| . 8 | . 2454064 | 3197 | 712123.50 | 65.9 | . 857 | .261 0169 | 30.48 | 72 15 03.41 |  |
| . 808 | .2457259 | 3194 | 712229.41 | 65.88 | . 858 | . 2613216 | 3046 | 72 16 06.26 | 62.82 |
| . 809 | . 246045 I | 3191 | 712335.26 | 65.8 I | . 859 | . 2616260 | 3043 | 72 I7 09.05 | 62.76 |
| 1.810 | I. 2463640 | 3 | 712441.04 | 65.75 | I. 86 | 1.261 9302 | .40 | 721811.78 | . 70 |
| .8II | . 2466827 | 3185 | 712546.76 | 65.69 | . 861 | . 2622340 | 3037 | 72 I9 14.45 | 62.64 |
| .812 | . 2470010 | 3182 | 712652.42 | 65.63 | . 862 | . 2625375 | 3034 | $72 \quad 2017.06$ | 62.58 |
| .8I3 | . 2473190 | 3179 | 712758.01 | 65.56 | . 863 | . 2628408 | 3031 | 72 21 19.61 | 62.52 |
| . 814 | . 2476367 | 3176 | 712903.54 | 65.50 | . 864 | .2631438 | 3028 | 7222 22.10 | 62.46 |
| 1.815 | 1.247 9541 | 3173 | 71.3009 .02 |  | 1.865 | 1.26344 | 3025 | $\begin{array}{lll}72 & 23 & 24.54\end{array}$ | 2.40 |
| .816 | . 2482712 | 3170 | 713114.42 | 65.38 | . 866 | . 2637488 | 3022 | 722426.91 | 62.34 |
| . 8 | .2485880 | 3167 | 713219.77 | 65.32 | . 867 | .2640509 | 3020 | $\begin{array}{lllll}72 & 25 & 29.22\end{array}$ | 28 |
| . 818 | .2489046 | 3164 | 713325.06 | 65.25 | . 868 | . 2643527 | 3017 | $\begin{array}{llllll}72 & 26 & 31.47\end{array}$ | 62.22 |
| . 819 | . 2422208 | 3161 | 713430.28 | 65.19 | . 869 | .2646543 | 3014 | 722733.67 | 62.16 |
| 1.820 | I. 249536 |  | 713535 |  | 1.870 | I. 264955 | 011 | $\begin{array}{llll}72 & 28 & 35.80\end{array}$ | 2. 11 |
| . 82 I | . 2498523 | 3155 | 713640.54 | 65.07 | . 871 | . 2652565 | 3008 | $\begin{array}{lllll}72 & 29 & 37.88\end{array}$ | 62.05 |
| . 822 | . 2501676 | 3 I 52 | 713745.58 | 65.01 | . 872 | . 2655571 | 3005 | $72 \quad 3039.90$ | 6I. 99 |
| . 823 | . 2504826 | 3149 | 713850.56 | 64.95 | . 873 | . 2658575 | 3002 | 72 31 41.85 | 61.93 |
| . 824 | .2507973 | 3146 | 71.3955 .47 | 64 | . 874 | .2661576 | 2999 | $72 \quad 3243.75$ | 61.87 |
| I. 825 | I.25I I | 3143 | 714100.32 | 64.82 | 1.875 | I. 266457 | 2997 | $723345 \cdot 59$ |  |
| . 82 | .251 4259 | 3140 | 714205.11 | 64.76 | . 876 | . 2667569 | 2994 | 723447.37 | 61.75 |
| . 82 | . 2517397 | 3137 | 714309.84 | 64.7 | . 87 | . 2670562 | 2991 | $\begin{array}{llll}72 & 35 & 49.09\end{array}$ | 61. 69 |
| . 82 | .2520532 | 3134 | 714414.51 | 64.64 | . 878 | . 2673551 | 2988 | $\begin{array}{lllll}72 & 36 & 50.75\end{array}$ |  |
| . 829 | .2523664 | 3I3I | 7145 I9.12 | 64.58 | . 879 | . 2676538 | 2985 | 723752.36 | 6 I .57 |
| 1.830 | I. 2526794 | 31 | 714623.67 |  | 1.880 | I. 267 9521 | 2982 | $\begin{array}{lllll}72 & 38 & 53.90\end{array}$ | 61.52 |
| .83I | . 2529920 | 3125 | 714728.15 | 64.45 | . 881 | . 2682502 | 2980 | $\begin{array}{lllllllllll}72 & 39 & 55\end{array}$ | 6 I .46 |
| . 832 | .2533043 | 31 | 714832.57 | 64.39 | . 882 | . 2685480 | 2977 | 7240 | 6 I .40 |
| . 833 | .2536164 | 3116 | 714936.94 | 64.33 | . 883 | . 2688456 | 2974 | 72 41 58.19 | 6 I .34 |
| . 834 | . 253 9281 | 3116 | 715041.24 | 64.27 | . 884 | . 269 I428 | 2971 | 724259.50 | 61.28 |
| 1.83 | I. 2542396 | 3 | 715145.48 |  | I. 885 | I. 2694398 | 2908 | 724400.75 | 22 |
|  | . 2545507 | 3110 | 715249.66 | 64.15 | . 886 | . 2697364 | 2965 | 724501.94 | 61.16 |
| . 8 | . 254 86I6 | 3107 | 715353.77 | 64.09 | . 887 | . 2700328 | 2962 | 724603.08 | 11 |
| . 838 | . 255 I72I | 3104 | 715457.83 | 64.03 | . 888 | .2703289 | 2960 | 724704.15 | 05 |
| . 839 | . 2554824 | 3101 | 715601.83 | 63.97 | . 889 | . 2706248 | 2957 | 724805.17 | 99 |
| 1. 840 | 1. 2557923 | 3098 | 715705.76 | 63.91 | I. 89 | I. 2709203 | 2954 | 724906.13 | 3 |
| . 841 | .2561020 | 3095 | 715809.64 | 63.84 | . 891 | . 2712156 | 2951 | 725007.03 |  |
| . 842 | . 2564114 | 3092 | 715913.45 | 63.78 | . 892 | . 2715106 | 2948 | 7251107.88 |  |
| . 843 | .2567205 | 3089 | 720017.21 | 63.72 | . 893 | . 2718053 | 29.46 | 725208.66 |  |
| . 844 | .2570293 | 3086 | 72 OI 20.90 | 63.66 | . 894 | .2720997 | 2943 | 725309.39 | 60.70 |
| 1.845 | 1.2573378 | 3084 | 72024.53 | 63.60 | I. 895 | 1. 2723938 | 2940 | 725410.06 |  |
| . 846 | . 2576460 | 3081 | 7203 28.10 | 63.54 | . 896 | . 2726877 | 2937 | 725510.67 | 58 |
| . 847 | . 2579539 | 3078 | 720431.61 | 63.48 | . 897 | . 272 9812 | 2934 | 7256 II. 23 |  |
| . 848 | . 2582615 | 3075 | 720535.06 | 63.42 | . 898 | . 2732745 | 2932 | 725711.72 | 60.47 |
| . 849 | .2585688 | 3072 | 720638.45 | $63 \cdot 36$ | . 899 | .2735675 | 2929 | 725812.16 | 60.41 |
| 1.850 | I. 2588759 | 3069 | 720741.78 | $63 \cdot 30$ | 1.900 | I. 2738603 | 2926 | 725912.54 | 60.35 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{0}\right)-90^{\circ}$ | $\omega$ sech | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ |  | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| $u$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\text { }}$ | od u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1.900 | I. 2738603 | 2926 | $72 \quad 59 \quad 12.54$ | 60.35 | 1.950 | 1.288 145I | 2789 | 734819.01 | 57.53 |
| . 901 | . 2741527 | 2923 | 730012.86 | 60.29 | .95I | . 2884239 | 2786 | 7349 16.51 | 57.47 |
| . 902 | . 2744449 | 2920 | 73 O1 13.13 | 60.24 | . 952 | . 2887024 | 2784 | 735013.95 | 57.42 |
| . 903 | . 2747368 | 2918 | 730213.33 | 60.18 | . 953 | . 2889806 | 2781 | 73 51 II. 34 | 57.36 |
| . 904 | . 2750284 | 2915 | 730313.48 | 60.12 | . 954 | . 2892586 | 2778 | 735208.68 | 57.3I |
| 1.905 | 1.2753197 | 2912 | 730413.58 | 60.06 | 1.955 | 1. 2895363 | 2776 | 735305.96 | 57.25 |
| . 906 | . 2756108 | 2909 | 730513.61 | 60.01 | . 956 | . 2898137 | 2773 | 735403.18 | 57.20 |
| . 907 | . 2759016 | 2906 | 730613.59 | 59.95 | -957 | . 2900909 | 2770 | 735500.35 | 57.14 |
| . 908 | . 2761921 | 2904 | 730713.51 | 59.89 | . 958 | . 2903678 | 2768 | 735557.46 | 57.09 |
| . 909 | . 2764823 | 2901 | 730813.37 | 59.83 | . 959 | . 2906444 | 2765 | 7356 54.52 | 57.03 |
| 1.910 | 1. 2767722 | 2898 | 730913.18 | 59.78 | 1.960 | 1. 2909208 | 2762 | 735751.53 | 56.98 |
| .91I | . 2770619 | 2895 | 731012.92 | 59.72 | . 961 | . 2911969 | 2760 | 735848.48 | 56.92 |
| . 912 | . 2773513 | 2893 | 73 I1 12.62 | 59.66 | . 962 | .291 4727 | 2757 | 735945.38 | 56.87 |
| .913 | . 2776404 | 2890 | 731212.25 | 59.61 | . 963 | .291 7483 | 2754 | 740042.22 | 56.8 I |
| . 914 | . 2779292 | 2887 | 731311.83 | 59.55 | . 964 | . 2920236 | 2752 | 74 OI 39.00 | 56.76 |
| 1.915 | 1.2782178 | 2884 | 731411.35 | 59.49 | 1.965 | 1. 2922987 | 2749 | 740235.73 | 56.70 |
| . 916 | . 2785061 | 2881 | 731510.81 | 59.43 | . 966 | . 2925734 | 2746 | 740332.41 | 56.65 |
| . 917 | . 2787941 | 2879 | 731610.22 | 59.38 | . 967 | . 2928480 | 2744 | 740429.03 | 56.60 |
| . 918 | . 2790818 | 2876 | 731709.56 | 59.32 | . 968 | . 2931222 | 2741 | 740525.60 | 56.54 |
| . 919 | . 2793693 | 2873 | 731808.86 | 59.26 | . 969 | . 2933962 | 2739 | 740622.12 | 56.49 |
| 1.920 | I. 2796565 | 2870 | 731908.09 | 59.21 | 1.970 | 1.2936699 | 2736 | 740718.58 | 56.43 |
| .921 | . 2799434 | 2868 | 732007.27 | 59.15 | .971 | . 2939434 | 2733 | 740814.98 | 56.38 |
| . 922 | . 2802300 | 2865 | 732106.39 | 59.09 | . 972 | . 2942166 | 2731 | 7409 I1.33 | 56.32 |
| . 923 | . 2805164 | 2862 | $\begin{array}{llll}73 & 22 & 05.46\end{array}$ | 59.04 | . 973 | . 2944895 | 2728 | 74 10 07.63 | 56.27 |
| . 924 | . 2808024 | 2859 | $\begin{array}{ll}73 & 2304.47\end{array}$ | 58.98 | . 974 | . 2947622 | 2725 | 74 II 03.87 | 56.22 |
| 1.925. | 1.281 0883 | 2857 | 732403.42 | 58.92 | 1.975 | 1. 2950346 | 2723 | 741200.06 | 56.16 |
| , 95 | .281 3738 | 2854 | 732502.32 | 58.87 | . 976 | . 2953068 | 2720 | 741256.20 | 56.11 |
| . 927 | . 2816590 | 2851 | 7326 от.16 | 58.8 I | . 977 | . 2955786 | 2718 | 741352.28 | 56.05 |
| . 928 | . 2819440 | 2849 | 732659.94 | 58.76 | . 978 | . 2958503 | 2715 | 741448.30 | 56.00 |
| . 929 | . 2822288 | 2846 | 732758.67 | 58.70 | . 979 | . 2961216 | 2712 | 741544.28 | 55.95 |
| 1.930 | I. 2825132 | 2843 | 732857.34 | 58.64 | 1.980 | 1. 2963927 | 2710 | 741640.20 | 55.89 |
| . 931 | . 2827974 | 2840 | 732955.95 | 58.59 | . 981 | . 2966636 | 2707 | 741736.06 |  |
| -9310 | . 2830813 | 2838 | 733054.51 | 58.53 | . 982 | . 2969342 | 2705 | 741831.87 | 55.78 |
| -933 | . 2833649 | 2835 | 733153.01 | 58.47 | . 983 | . 2972045 | 2702 | $74 \quad 1927.63$ | 55.73 |
| -934 | . 2836482 | 2832 | 733251.46 | 58.42 | .984 | . 2974745 | 2699 | 472023.34 | 55.68 |
| I. 935 | 1. 283 9313 | 2829 | 733349.85 | 58.36 | I. 985 | I. 2977443 | 2697 | 742118.99 | 55.62 |
| . 936 | . 2842141 | 2827 | 733448.18 | 58.31 | . 986 | . 2980139 | 2694 | 742214.58 | 55.57 |
| . 937 | . 2844967 | 2824 | 733546.46 | 58.25 | . 987 | . 2982832 | 2692 | 7423 10.13 | 55.52 |
| . 938 | . 2847789 | 2821 | 733644.68 | 58.19 | . 988 | . 2985522 | 2689 | 742405.62 | 55.46 |
| . 939 | . 2850609 | 2819 | 733742.85 | 58.14 | .989 | . 2988210 | 2686 | 7425 OI. 05 | 55.41 |
| 1.940 | 1. 2853427 | 2816 | 733840.96 | 58.08 | I. 990 | 1.2990895 | 2684 | 742556.44 | 55.36 |
| . 941 | . 2856241 | 2813 | 733939.01 | 58.03 | .991 | . 2993577 | 268 I | 742651.77 | 55.30 |
| . 942 | . 2859053 | 2811 | 734037.01 | 57.97 | . 992 | . 2996257 | 2679 | 742747.04 | 55.25 |
| . 943 | . 2861862 | 2808 | 734134.95 | 57.92 | . 993 | . 2998934 | 2676 | $74 \quad 2842.27$ | 55.20 |
| -944 | . 2864669 | 2805 | 734232.84 | 57.8 | -994 | -300 1609 | 2673 | 742937.44 | 55.14 |
| 1.945 | 1.2867473 | 2802 | 734330.68 | 57.80 | 1.995 | 1. 300428 I | 2671 | 743032.55 | 55.09 |
| . 946 | . 2870274 | 2800 | 734428.45 | 57.75 | . 996 | . 3006951 | 2668 | 743127.62 | 55.04 |
| . 947 | . 2873072 | 2797 | 734526.17 | 57.69 | . 997 | -300 9618 | 2666 | 743222.63 | 54.98 |
| -948 | .2875868 .287861 | 2794 | 734623.84 | 57.64 57.58 | -998 | -3012282 | 2663 | $\begin{array}{llllllllll}74 & 33 & 17.59\end{array}$ | 54.93 |
| . 949 | . 2878661 | 2792 | 734721.45 | 57.58 | . 999 | -301 4944 | 2661 | 743412.49 | 54.88 |
| 1.950 | 1.2881451 | 2789 | 734819.01 | 57.53 | 2.000 | 1.3017603 | 2658 | 743507.34 | 54.83 |
| 4 | $\left\|2 \tan ^{-1}\left(e^{\mathrm{a}}\right)-\frac{\pi}{2}\right\|$ | wsech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ |  |  | $2 \tan ^{-1}\left(e^{\mathrm{a}}\right)-\frac{\pi}{2}$ | chu | $2 \tan ^{-1}\left(\mathrm{ea}^{4}\right)-90^{\circ}$ | $\omega$ sech $u$ |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.000 |  |  |  |  |  |  |  |  | " |
| , | 1.301 |  | 743507.34 |  | 2.05 | 1.3147349 | 2533 | $75 \quad 1943.53$ | 52.24 |
| . 001 | . 3020260 | 2655 | 743602.14 | 54.77 | .05I | . 3149880 | 2530 | $75 \quad 2035.75$ | 52.19 |
| . 002 | . 3022914 | 2653 | 743656.89 | 54.72 | . 052 | -315 2409 | 2528 | 75. 21 27.91 | 52.14 |
| . 003 | . 3025566 | 2650 | 7437 51.58 | 54.67 | . 053 | -3I5 4936 | 2525 | 752220.03 | 52.09 |
| . 004 | . 3028215 | 2648 | 743846.22 | 54.61 | . 054 | . 3157460 | 2523 | $75 \quad 2312.09$ | 52.04 |
| 2.005 | I. 303086 I | 2645 | 743940.81 | 54.56 | 2.055 | I. 3159982 | 2520 | 7524 04.II | 51.99 |
| . 006 | . 3033505 | 2643 | $744035 \cdot 35$ | 54.5I | . 056 | . 3162501 | 2518 | 75.2456 .07 | 51.94 |
| . 007 | . 3036147 | 2640 | 744129.83 | 54.46 | . 057 | - 3165018 | 2516 | 752547.98 | 51.89 |
| . 008 | . 3038786 | 2638 | $74 \quad 4224.26$ | 54.40 | . 058 | . 3167532 | 2513 | $\begin{array}{lllllllllll}75 & 26 & 39.85\end{array}$ | 51.84 |
| . 009 | - 304 I422 | 2635 | 744318.64 | $54 \cdot 35$ | . 059 | -3I7 0044 | 25 II | 752731.66 | 51.79 |
| 2.010 | I. 3044056 | 2633 | $\begin{array}{llll}74 & 44 & 12.97\end{array}$ | $54 \cdot 30$ | 2.060 | I.3I7 2554 | 2508 | $\begin{array}{lll}75 & 28 & 23.42\end{array}$ | 51.74 |
| . 011 | . 3046687 | 2630 | $\begin{array}{lllllll}74 & 45 & 07.24\end{array}$ | 54.25 | .06I | . 317 5061 | 2506 | $75 \quad 29$ I5.14 | 51.69 |
| . 012 | . 3049316 | 2627 | 7446 O1. 46 | 54. 19 | . 062 | . 3177566 | 2503 | 753006.80 | 51.64 |
| . 013 | . 3051942 | 2625 | 744655.63 | 54.14 | . 063 | - 3180068 | 2501 | 753058.41 | 51.59 |
| . 014 | . 3054566 | 2622 | 744749.74 | 54.09 | . 064 | - 3182568 | 2499 | 75 31 49.98 | 51.54 |
| 2.015 | 1. 3057187 | 2620 | $74 \quad 4843.81$ | 54.04 | 2.065 | I. 3185065 | 2496 | 753241.49 | 51. 49 |
| . 016 | . 3059805 | 2617 | $74 \quad 4937.82$ | 53.99 | . 066 | . 3187560 | 2494 | 753332.95 | 51.44 |
| . OI7 | . 3062421 | 2615 | $74 \quad 5031.78$ | 53.93 | . 067 | . 3190053 | 2491 | $\begin{array}{llll}75 & 34 & 24.37\end{array}$ | 51.39 |
| . 018 | . 3065035 | 2612 | 745125.69 | 53.88 | . 068 | - 3192543 | 2489 | $75 \quad 3515.73$ | 51.34 |
| . 019 | . 3067646 | 2610 | 745219.54 | 53.83 | . 069 | . 319503 I | 2487 | $75 \quad 3607.04$ | 51.29 |
| 2.020 | I. 3070254 | 2607 | $\begin{array}{llll}74 & 53 & 13.35\end{array}$ | 53.78 | 2.070 | 1.319 7516 | 2484 | 753658.31 | 51.24 |
| .02I | . 3072860 | 2605 | $74 \quad 54$ 07.10 | 53.73 | . 071 | -319 9999 | 2482 | 75.37 49.52 | 51. 19 |
| . 022 | - 3075464 | 2602 | 745500.80 | 53.67 | . 072 | - 3202480 | 2479 | $75 \quad 3840.69$ | 51.14 |
| . 023 | . 3078065 | 2600 | 745554.45 | 53.62 | . 073 | . 3204958 | 2477 | 753931.80 | 51.09 |
| . 024 | . 3080663 | 2597 | 745648.05 | 53.57 | . 074 | . 3207433 | 2475 | 754022.87 | 51.04 |
| 2.025 | I. 3083259 | 2595 | 745741.59 | 53.52 | 2.075 | I. 3209907 | 2472 | 754113.89 | 50.99 |
| . 026 | . 3085853 | 2592 | $74 \quad 5835.08$ | 53.47 | . 076 | . 3212378 | 2470 | $75 \quad 4204.85$ | 50.94 |
| . 027 | . 3088443 | 2590 | $74 \quad 5928.52$ | 53.42 | . 077 | .321 4846 | 2467 | 754255.77 | 50.89 |
| . 028 | . 3091032 | 2587 | 750021.91 | 53.36 | . 078 | -321 7312 | 2465 | 754346.64 | 50.84 |
| . 029 | . 3093618 | 2585 | 75 OI 15.25 | 53.31 | . 079 | -3219776 | 2463 | 754437.46 | 50.79 |
| 2.030 | 1.3096201 | 2582 | 750208.54 | 53.26 | 2.080 | 1.3222238 | 2460 | 754528.23 | 50.75 |
| . 031 | . 3098782 | 2580 | 750301.78 | 53.21 | .081 | . 3224697 | 2458 | 754618.95 | 50.70 |
| . 032 | . 310 I361 | 2577 | 750354.96 | 53.16 | . 082 | . 3227153 | 2455 | 754709.62 | 50.65 |
| . 033 | . 3103936 | 2575 | 750448.09 | 53.11 | . 083 | . 3229608 | 2453 | 754800.24 | 50.60 |
| . 034 | . 3106510 | 2572 | 750541.17 | 53.06 | . 084 | . 3232059 | 2451 | 754850.82 | 50.55 |
| 2.035 | 1.310 908I | 2570 | 750634.20 | 53.00 | 2.085 | I. 3234509 | 2448 | 754941.34 | 50.50 |
| . 036 | .311 1649 | 2567 | 7507 27.18 | 52.95 | . 086 | . 3236956 | 2446 | 755031.82 | 50.45 |
| . 037 | . 3 II 4215 | 2565 | 7508 20.11 | 52.90 | . 087 | . 323 9401 | 2444 | 75 51 22.25 | 50.40 |
| . 038 | .311 6779 | 2562 | 750912.99 | 52.85 | . 088 | . 3241843 | 2441 | $75 \quad 5212.62$ | 50.35 |
| . 039 | -3II 9340 | 2560 | 751005.81 | 52.80 | . 089 | . 3244283 | 2439 | 755302.95 | 50.30 |
| 2.040 | 1.3121898 | 2557 | 75 10 58.59 | 52.75 | 2.090 | I. 3246721 | 2436 | 755353.23 | 50.26 |
| . 041 | -312 4455 | 2555 | 75 II 51.31 | 52.70 | .09I | . 324 9156 | 2434 | 755443.46 | 50.21 |
| . 042 | . 3127008 | 2552 | 751243.98 | 52.65 | . 092 | . 3251589 | 2432 | 755533.65 | 50.16 |
| . 043 | -3129559 | 2550 | 75 13 36.60 | 52.60 | . 093 | . 3254020 | 2429 | $75 \quad 5623.78$ | 50.11 |
| . 044 | -3I3 2108 | 2547 | 75 14 29.17 | 52.55 | . 094 | . 3256448 | 2427 | $75 \quad 5713.86$ | 50.06 |
| 2.045 | I. 3134654 | 2545 | 751521.69 | 52.49 | 2.095 | I. 3258874 | 2425 | $75 \quad 5803.90$ | 50.01 |
| . 046 | . 3137198 | 2543 | 751614.16 | 52.44 | . 096 | . 3261297 | 2422 | 755853.89 | 49.96 |
| . 047 | -3I3 9739 | 2540 | 7517006.58 | 52.39 | . 097 | - 3263718 | 2420 | 755943.83 | 49.92 |
| . 048 | - 3142278 | 2538 | $75 \quad 1788.95$ | 52.34 | . 098 | . 326 6I37 | 2418 | 760033.72 | 49.87 |
| . 049 | -3I4 48I5 | 2535 | 751851.27 | 52.29 | . 099 | . 3268554 | 2415 | 76 OI 23.56 | 49.82 |
| 2.050 | I.314 7349 | 2533 | $75 \quad 1943 \cdot 53$ | 52.24 | 2.100 | 1. 3270968 | 2413 | 760213.36 | 49.77 |
| $u$ | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | 49.77 |  |  |  |  | " |
| 2.100 | 1. 32700 | 2413 | 760213.36 | 49.77 | 2.150 | I. 3388732 | 2298 | 764242.42 | 47.41 |
| . 101 | . 3273380 | 2411 | 760303.11 | 49.72 | . 151 | . 339 I029 | 2296 | 7643 29.8I | $47 \cdot 36$ |
| . 102 | - 3275789 | 2408 | 760352.80 | 49.67 | . 152 | - 3393325 | 2294 | 7644 I7.15 | 47.32 |
| . 103 | . 327 8196 | 2406 | 760442.45 | 49.63 | . 153 | . 339 56I7 | 2292 | 764504.44 | 47.27 |
| . 104 | . 328 060I | 2404 | 760532.06 | 49.58 | . 154 | - 3397908 | 2290 | 764551.69 | 47.23 |
| 2.105 | I. 3283003 | 2401 | 760621.6 I | 49.53 | 2.155 | 1. 3400197 | 2287 | 764638.89 | 47.18 |
| . 106 | . 3285403 | 2399 | 7607 II.II | 49.48 | . 156 | - 3402483 | 2285 | 764726.05 | 47.13 |
| . 107 | . 3287801 | 2397 | 760800.57 | 49.43 | . 157 | . 3404767 | 2283 | 764813.16 | 47.09 |
| . 108 | . 3290197 | 2394 | $76 \quad 0849.98$ | 49.39 | . 158 | . 3407049 | 2281 | 764900.23 | 47.04 |
| . 109 | . 3292590 | 2392 | 760939.34 | 49.34 | . 159 | . 3409328 | 2278 | 764947.25 | 47.00 |
| 2. 110 | 1. 3294980 | 2390 | 76 10 28.66 | 49.29 | 2.160 | 1.341 1605 | 2276 | $76 \quad 5034.22$ | 46.95 |
| . III | . 3297369 | 2387 | 76 II 17.92 | 49.24 | . 161 | -341 388I | 2274 | 765121.15 | 46.90 |
| . II2 | . 3299755 | 2385 | 761207.14 | 49.19 | . 162 | . 341 6I53 | 2272 | $76 \quad 5208.03$ | 46.86 |
| . II3 | - 3302139 | 2383 | 761256.31 | 49.15 | . 163 | . 3418424 | 2270 | $76 \quad 5254.87$ | 46.8I |
| . II4 | . 3304520 | 2380 | 76 I3 45.43 | 49.10 | . 164 | . 3420693 | 2267 | 765341.66 | 46.77 |
| 2.115 | I. 3306900 | 237 | 76 I4 34.5I | 49.05 | 2.165 | I. 3422959 | 65 | $76 \quad 5428.40$ | 46.72 |
| . I16 | . 3309277 | 2376 | 76 I5 23.54 | 49.00 | . 166 | . 3425223 | 2263 | 765515.10 | 46.68 |
| . 117 | . 331165.1 | 2373 | 76 I6 12.52 | 48.96 | . 167 | . 3427485 | 2261 | 7656 O1.76 | 46.63 |
| . II8 | . 3314023 | 2371 | 7617701.45 | 48.91 | . 168 | . 3429744 | 2259 | 765648.36 | 46.59 |
| . I I9 | .33I 6393 | 2369 | 76 I7 50.33 | 48.86 | . 169 | -343 2002 | 2256 | 765734.93 | 46.54 |
| 2.120 | I.331 876I | 2367 | 76 I8 39.17 | 48.8I | 2.170 | I. 3434257 | 2254 | 765821.45 | 46.50 |
| . 121 | . 3321127 | 2364 | 761927.96 | 48.77 | . 171 | . 3436510 | 2252 | $76 \quad 5907.92$ | 46.45 |
| . 122 | . 3323490 | 2362 | $76 \quad 2016.70$ | 48.72 | . 172 | -343 876I | 2250 | $76 \quad 59 \quad 54 \cdot 35$ | 46.41 |
| . 123 | . 3325850 | 2360 | 762105.40 | 48.67 | . 173 | . 344 IoIo | 2248 | 770040.73 | 46.36 |
| . 124 | - 3328209 | 2357 | 762154.04 | 48.62 | . 174 | . 3443256 | 2245 | 77 O1 27.07 | 46.31 |
| 2.125 | I. 3330565 | 2355 | 762242.64 | 4858 | 2.175 | 1. 3445501 | 2243 | 770213.36 | 46.27 |
| . 125 | . 3332919 | 2353 | 7623131.20 | 48.53 | .176 | - 3447743 | 2241 | 770259.61 | 46.22 |
| . 127 | . 333527 I | 2350 | 762419.70 | 48.48 | . 177 | . 3449983 | 2239 | 770345.81 | 46.18 |
| . 128 | . 3337620 | 2348 | 762508.16 | 48.44 | . 178 | - 3452220 | 2237 | 770431.96 | 46.13 |
| . 129 | . 3339967 | 2346 | 762556.57 | 48.39 | . 179 | . 3454456 | 2234 | $77 \quad 0518.08$ | 46.09 |
| 2.I30 | I. 3342312 | 2344 | $76 \quad 2644.94$ | 48.34 | 2.180 | I. 3456689 | 2232 | $77 \quad 06104.14$ | 46.04 |
| .13I | . 3344654 | 2341 | $76 \quad 2733.26$ | 48.29 | . 18 I | - 345892 I | 2230 | 770650.17 | 46.00 |
| . 132 | . 3346995 | 2339 | 702821.53 | 48.25 | . 182 | . 346 I150 | 2228 | 77 07 36.14 | 45.95 |
| . I33 | - 3349333 | 2337 | $76 \quad 2909.75$ | 48.20 | . 183 | . 3463377 | 2226 | 770822.08 | 45.91 |
| . I34 | . 3351668 | 2335 | 762957.93 | 48.15 | . 184 | . 3465601 | 2224 | 770907.96 | 45.87 |
| 2.135 | I. 3354002 | 2332 | 763046.06 | 48.11 | 2.185 | 1. 3467824 | 222I | 770953.81 | 45.82 |
| . 136 | . 3356333 | 2330 | 763134.14 | 48.06 | . 186 | . 3470044 | 2219 | 77 10 39.60 | 45.78 |
| . 137 | . 3358662 | 2328 | 763222.18 | 48.01 | . 187 | . 3472262 | 2217 | 77 II 25.36 | 45.73 |
| . 138 | . 3360988 | 2325 | 753310.17 | 47.97 | . 188 | - 3474478 | 2215 | 771211.07 | 45.69 |
| . 139 | . 336 33I3 | 2323 | 7633 58.1I | 47.92 | . 189 | . 3476692 | 2213 | 771256.73 | 45.64 |
| 2.140 | I. 3365635 | 232I | 763446.01 | 47.87 | 2.190 | 1. 3478904 | 2 II | $\begin{array}{llll}77 & 13 & 42.35\end{array}$ | 45.60 |
| . 141 | . 3367955 | 2319 | 763533.86 | 47.83 | . 191 | . 348 III4 | 2208 | 77 14 27.93 | 45.55 |
| . 142 | . 3370272 | 2316 | .76 36121.66 | 47.78 | . 192 | - 3483321 | 2206 | 77 If 13.46 | 45.5 I |
| . I43 | . 3372588 | 2314 | 763709.42 | 47.73 | . 193 | - 3485526 | 2204 | 771558.95 | 45.46 |
| . I44 | - 3374901 | 2312 | $763757 \cdot 13$ | 47.69 | . 194 | . 3487729 | 2202 | $77 \quad 1644.39$ | 45.42 |
| 2.145 | 1.3377212 | 2310 | 763844.79 | 47.64 | 2. 195 | I. 3489930 | 2200 | $\begin{array}{llll}77 & 17 & 29.79\end{array}$ | 45.38 |
| . I46 | . 3379520 | 2307 | 763932.41 | 47.59 | . 196 | - 3492129 | 2198 | 77 I8 15.14 | 45.33 |
| . 147 | . 3381826 | 2305 | 764019.98 | 47.55 | -197 | - 3494326 | 2196 | 77 I9 00.45 | 45.29 |
| . 148 | - 3384131 | 2303 | 764107.51 | 47.50 | . 198 | - 3496520 | 2193 | 77 I9 45.72 | 45.24 |
| . I49 | . 3386432 | 2301 | 764154.99 | 47.46 | . 199 | - 3498713 | 2191 | $77 \quad 2030.94$ | 45.20 |
| 2.150 | 1.3388732 | 2298 | 764242.42 | 47.41 | 2.200 | I. 3500903 | 2189 | 77 21 16.11 | 45.16 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | hu | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | $\omega$ sech u |

Smithsonian Tables

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | ""16 |  |  |  | 20 ${ }^{\circ}{ }^{\prime \prime}$ | " |
| 2.200 | 1. 3500903 | 2189 | 772116.11 | 45.16 | 2.250 | 1. 3607733 | 2085 | 775759.64 | 43.00 |
| . 201 | . 3503091 | 2187 | 7722 O1. 25 | 45. I I | . 251 | - 360 9817 | 2083 | 775842.62 | 42.96 |
| . 202 | . 3505277 | 2185 | 772246.34 | 45.07 | . 252 | -361 1899 | 2081 | 775925.56 | 42.92 |
| . 203 | . 3507461 | 2183 | $77 \quad 2331.38$ | 45.02 | . 253 | -361 3978 | 2079 | 780008.46 | 42.88 |
| . 204 | . 3509643 | 2181 | 772416.38 | 44.98 | . 254 | . 3616056 | 2077 | 780051.32 | 42.83 |
| 2.205 | 1.351 1822 | 2179 | 7725 OI. 34 | 44.94 | 2.255 | 1.361 8I32 | 2075 | 78 or 34.13 | 42.79 |
| . 205 | . 3514000 | 2176 | 772546.25 | 44.89 | . 256 | -362 0205 | 2073 | 7802 16.90 | 42.75 |
| . 207 | .351 6175 | 2174 | 772631.12 | 44.85 | . 257 | - 3622277 | 2071 | 780259.63 | 42.71 |
| . 208 | . 3518348 | 2172 | 772715.95 | 44.80 | . 258 | . 3624347 | 2069 | $\begin{array}{lllll}78 & 03 & 42.32\end{array}$ | 42.67 |
| . 209 | -352 0519 | 2170 | 772800.73 | 44.76 | . 259 | . 3626414 | 2067 | 780424.97 | 42.63 |
| 2.210 | 1.3522688 | 2168 | $77 \quad 2845.47$ | 44.72 | 2.260 | 1. 3628480 | 2065 | $\begin{array}{llll}78 & 05 & 07.57\end{array}$ | 42.58 |
| . 211 | . 3524855 | 2166 | 772930.16 | 44.67 | . 261 | . 3630543 | 2063 | 780550.13 | 42.54 |
| . 212 | . 3527020 | 2164 | $77 \quad 3014.82$ | 44.63 | . 262 | . 3632605 | 2060 | $\begin{array}{llll}78 & 06 & 32.66\end{array}$ | 42.50 |
| . 213 | . 3529183 | 2162 | 773059.42 | 44.59 | .263 | - 3634664 | 2058 | $\begin{array}{cccc}78 & 07 & 15.14 \\ 78 & 07 & 57\end{array}$ | 42.46 |
| . 214 | . 353 I343 | 2159 | 77 31 43.99 | 44.54 | . 264 | . 3636722 | 2056 | $78 \quad 0757.57$ | 42.42 |
| 2.215 | 1.3533502 | 2157 | $\begin{array}{llll}77 & 32 & 28.51\end{array}$ | 44.50 | 2.265 | 1. 3638777 | 2054 | $\begin{array}{llll}78 & 08 & 39.97\end{array}$ | 42.38 |
| . 216 | . 3535658 | 2155 | $77 \quad 3312.99$ | 44.46 | . 266 | . 364083 I | 2052 | 780922.33 | 42.33 |
| . 217 | . 353 7812 | 2153 | $77 \quad 33157.42$ | 44.41 | . 267 | - 3642882 | 2050 | 78 10 04.64 | 42.29 |
| . 218 | . 3539964 | 2151 | 773441.81 | 44.37 | . 268 | . 3644931 | 2048 | 78 10 46.91 | 42.25 |
| . 219 | - 3542 II4 | 2149 | 773526.16 | 44.33 | . 269 | . 3646979 | 2046 | 78 II 29.14 | 42.21 |
| 2.220 | I. 3544262 | 2147 | 773610.46 | 44.28 | 2.270 | I. 3649024 | 2044 | 78 I2 II. 33 | 42.17 |
| . 221 | . 3546408 | 2145 | 773654.72 | 44.24 | . 271 | . 3651068 | 2042 | $\begin{array}{llllll}78 & 12 & 53.48\end{array}$ | 42.13 |
| . 222 | . 3548552 | 2143 | $77 \quad 3738.94$ | 44.20 | . 272 | - 3653109 | 2040 | 78 I3 35.59 | 42.09 |
| . 223 | . 3550693 | 2141 | $77 \quad 38$ 23.1I | 44.15 | . 273 | . 3655149 | 2038 | 78 I4 17.66 | 42.05 |
| . 224 | . 3552833 | 2138 | $77 \quad 39 \quad 07.24$ | 44. I I | . 274 | . 3657186 | 2036 | 78 I4 59.68 | 42.00 |
| 2.225 | 1. 3554970 | 2136 | 773951.33 | 44.07 | 2.275 | I. 3659221 | 2034 | 781541.66 | 41.96 |
| . 226 | - 3557106 | 2134 | 774035.38 | 44.02 | .276 | . 3661255 | 2032 | 78 16 16 23.61 | 41. 92 41.88 |
| . 227 | - 3559239 | 2132 | 774119.38 | 43.98 | . 277 | - 3663286 | 2030 | 78 I7 05.51 | 41. 88 |
| . 228 | . 356 I 370 | 2130 | $\begin{array}{lllll}77 & 42 & 03.34\end{array}$ | 43.94 | . 278 | . 365 5316 | 2028 | $\begin{array}{llll}78 & 17 & 47.37\end{array}$ | 4 I .84 |
| . 229 | - 3563499 | 2128 | 774247.25 | 43.89 | . 279 | . 3667343 | 2026 | 78 I8 29.19 | 41.80 |
| 2.230 | I. 3565626 | 2126 | 7743 31.13 | 43.85 | 2.280 | 1. 3669369 | 2024 | 78 19 10.97 | 41.76 |
| . 231 | . 3567751 | 2124 | 774414.96 | 43.81 | .281 | . 367 I392 | 2023 | 78 i9 52.71 | 41.72 |
| . 232 | - 3569874 | 2122 | 774458.74 | 43.77 | . 282 | -367. 3414 | 2021 | $78 \quad 2034.40$ | 41.68 |
| . 233 | . 3572095 | 2120 | 774542.49 | 43.72 | .283 | . 3675433 | 2019 | 782116.06 | 4 I .64 |
| . 234 | -357 4II4 | 2118 | $77 \quad 46$ 26.19 | 43.68 | . 284 | . 367 745I | 2017 | 78 21 57.68 | 41.60 |
| 2.235 | I. 3576230 | 2 I 16 | $\begin{array}{llll}77 & 47 & 09.85\end{array}$ | 43.64 | 2.285 | I. 3679466 | 2015 | $\begin{array}{lll}78 & 22 & 39.25\end{array}$ | 4I. 55 |
| . 236 | . 3578345 | 2114 | $77 \quad 4753.47$ | 43.60 | . 286 | . 3681480 | 2013 | $\begin{array}{lllll}78 & 23 & 20.78 \\ -8 & 24 & 02 .\end{array}$ | 4 I .5 I |
| . 237 | . 3580457 | 2 III | $77 \quad 4837.04$ | $43 \cdot 5.5$ | . 287 | . 3683492 | 2011 | $\begin{array}{llll}78 & 24 & 02.28 \\ 78 & 24 & 43.73\end{array}$ | 4 I .47 |
| . 238 | - 3582568 | 2109 | 774920.57 | 43.51 | . 288 | . 3685501 | 2009 | $\begin{array}{lllllllllllllllll}78 & 24 & 43.73\end{array}$ | 41.43 |
| . 239 | . 3584676 | 2107 | 775004.06 | 43.47 | . 289 | . 3687509 | 2007 | $78 \quad 25 \quad 25.14$ | 4 I .39 |
| 2.240 | I. 3586783 | 2105 | 775047.51 | 43.43 | 2.290 | . 3689515 | 2005 | $\begin{array}{lll}78 & 26 & 06.51 \\ 78 & 26 & 47.85\end{array}$ | $4 \mathrm{I} \cdot 35$ |
| . 241 | . 3588887 | 2103 | 775130.91 | 43.38 | . 291 | . 3691519 | 2003 | $\begin{array}{lll}78 & 26 & 47.85\end{array}$ | 4 I .3 I |
| . 242 | . 3590989 | 2101 | $77 \quad 5214.27$ | 43.34 | . 292 | - 369352 I | 2001 | $\begin{array}{llll}78 & 27 & 29.14 \\ 78 & 28 & 10.30\end{array}$ | 41.27 |
| . 243 | - 3593089 | 2099 | $775257 \cdot 59$ | $43 \cdot 30$ | . 293 | . 3695520 | 1999 | $\begin{array}{llll}78 & 28 & 10.39 \\ 78 & 28 & 51.60\end{array}$ | 4 I .23 |
| . 244 | - 3595187 | 2097 | 775340.87 | 43.26 | . 294 | . 3697518 | 1997 | 782851.60 | 41.19 |
| 2.245 | 1.359 7283 | 2095 | 775424.10 | 43.21 | 2.295 | 1. 3699514 | 1995 | $\begin{array}{lll}78 & 29 & 32.77\end{array}$ | 41.15 |
| . 246 | . 3599377 | 2093 | $77 \quad 5507.29$ | 43.17 | . 296 | . 3701508 | 1993 | $\begin{array}{lllllllllll}78 & 30 & 13.89\end{array}$ | 41.11 |
| . 247 | . 360 I469 | 2091 | 775550.44 | 43.13 | . 297 | - 3703500 | 1991 | $\begin{array}{llllllllll}78 & 30 & 54.98 \\ 78 & 31 & 36.03\end{array}$ | 4 I .07 |
| . 248 | . 3603559 | 2089 | 775633.55 | 43.09 | . 298 | -370 5490 | 1989 | $\begin{array}{lll}78 & 31 & 36.03 \\ 78 & 32 & 17.04\end{array}$ | 41.03 40.99 |
| . 249 | . 3605647 | 2087 | 775716.62 | 43.04 | . 299 | -370 7479 | 1987 | $78 \quad 32$ 17.04 | 40.99 |
| 2.250 | 1.360 7733 | 2085 | 775759.64 | 43.00 | 2.300 | 1.3709465 | 1985 | 783258.01 | 40.95 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.300 | I.370 9465 | 198 | $78^{\circ} 32^{\prime} 58.101$ | 40.95 | 2.350 | I. 380633 I | 1800 | 06' 16.03 | 38.99 |
| . 301 | . 371 I 449 | 1983 | 783338.94 | 40.91 | . 351 | . 3808221 | 1888 | 790655.00 | 38.95 |
| . 302 | . 3713431 | 1981 | $78 \quad 3419.82$ | 40.87 | . 352 | .381 0io8 | 1886 | 790733.93 | 38.91 |
| . 303 | -371 5412 | 1979 | 783500.67 | 40.83 | -353 | .381 1994 | 1885 | 790812.82 | 38.87 |
| . 304 | . 3717390 | 1977 | 783541.48 | 40.79 | - 354 | . 3813877 | 1883 | 790851.67 | 38.84 |
| 2.305 | I.371 9367 | 1975 | 783622.25 | 40.75 | 2.355 | I.38I 5759 | 188I | 790930.49 | 38.80 |
| . 306 | . 372 1341 | 1974 | 783702.98 | 40.71 | . 356 | .381 7639 | 1879 | 79 10 09.27 | 38.76 |
| . 307 | . 3723314 | 1972 | $\begin{array}{lllllllllll}78 & 37 & 43.66\end{array}$ | 40.66 | - 357 | -381 9517 | 1877 | 79 IO 48.01 | 38.72 |
| . 308 | . 3725284 | 1970 | $78 \quad 38 \quad 24.31$ | 40.63 | - 358 | . 3821394 | 1875 | 79 II 26.71 | 38.08 |
| . 309 | . 3727253 | 1968 | 783904.92 | 40.59 | -359 | . 3823268 | 1874 | 79 12 05.37 | 38.64 |
| 2.310 | I. 3729220 | 1966 | 783945.49 | 40.55 | 2.360 | I. 382514 I | 1872 | 79 I2 44.00 | 38.61 |
| .3II | . 373 I185 | 1964 | 784026.02 | 40.51 | .36I | . 3827012 | 1870 | 79 I3 22.59 | 38.57 |
| -312 | - 373 3148 | 1962 | 784106.51 | 40.47 | . 362 | . 382 888I | 1868 | 79 I4 OI.I4 | 38.53 |
| . 313 | . 3735109 | 1960 | 784146.96 | 40.43 | - 363 | . 3830748 | 1866 | 79 I4 39.65 | 38.49 |
| -314 | . 3737068 | 1958 | 784227.37 | 40.39 | . 364 | . 383 26I3 | 1864 | 79 I5 18.12 | 38.46 |
| 2.315 | I. 3739025 | 1956 | $78 \quad 4307.74$ | 40.35 | 2.365 | I. 3834476 | 1863 | 791556.56 | 38.42 |
| . 316 | - 3740980 | 1954 | 784348.07 | 40.31 | . 366 | .3836338 | 1861 | 79 16 34.96 | 38.38 |
| . 317 | . 3742934 | 1952 | 784428.36 | 40.27 | . 367 | . 383 8198 | 1859 | 79 I7 13.32 | 38.34 |
| . 318 | . 3744885 | 1950 | 784508.61 | 40.23 | . 368 | . 3840056 | 1857 | 79 17 51.64 | 38.30 |
| . 319 | -374 6835 | 1949 | 784548.82 | 40.19 | . 369 | - 384 I912 | 1855 | 79 I8 29.93 | 38.27 |
| 2.320 | 1.3748782 | 1947 | 784618.99 | 40.15 | 2.370 | 1.384 3766 | 1853 | 79 19 08.18 | 38.23 |
| . 321 | . 3750728 | 1945 | 784700.13 | 40.11 | -37I | . 3845619 | 1852 | 79 I9 46.39 | 38.19 |
| - 322 | . 3752672 | 1943 | 784749.22 | 40.07 | -372 | - 3847470 | 1850 | $79 \quad 2024.56$ | 38.15 |
| . 323 | . 3754614 | 1941 | 784829.28 | 40.04 | - 373 | . 3849318 | 1848 | 79 21 02.70 | 38.12 |
| - 324 | . 3756554 | 1939 | $78 \quad 4909.29$ | 40.00 | - 374 | . 385 II65 | 1846 | 792140.80 | 38.08 |
| 2.325 | I. 3758492 | 1937 | 784949.27 | 39.96 | 2.375 | I. 3853011 | 1844 | 792218.86 | 38.04 |
| . 326 | . 3760428 | 1935 | 785029.21 | 39.92 | . 376 | . 3854854 | 1843 | 79.2256 .88 | 38.00 |
| . 327 | - 3762362 | 1933 | 78 51 09.10 | 39.88 | - 377 | . 3856696 | 1841 | $\begin{array}{llllll}79 & 23 & 34.87\end{array}$ | 37.97 |
| . 328 | . 3764295 | 1931 | 78 51 48.96 | 39.84 | - 378 | . 3858536 | 1839 | 792412.81 | 37.93 |
| . 329 | . 3766225 | 1930 | 785228.78 | 39.80 | - 379 | . 3860374 | 1837 | 792450.73 | 37.89 |
| 2.330 | I. 3768154 | 1928 | $\begin{array}{llll}78 & 53 & 08.56\end{array}$ | 39.76 | 2.380 | I. 3862210 | 1835 | 792528.60 | 37.86 |
| . 331 | . 3770081 | 1926 | 785348.30 | 39.72 | .381 | . 3864044 | 1833 | $79 \quad 2606.44$ | 37.82 |
| . 332 | - 3772006 | 1924 | 785428.01 | 39.68 | . 382 | . 3865877 | 1832 | 792644.24 | 37.78 |
| - 333 | . 3773929 | 1922 | 785507.67 | 39.64 | -383 | . 3867708 | 1830 | 792722.00 | 37.74 |
| . 334 | . 3775850 | 1920 | 785547.29 | 39.61 | - 384 | . 3869537 | 1828 | 792759.73 | 37.71 |
| 2.335 | 1.377 7769 | 1918 | $\begin{array}{llll}78 & 56 & 26.88\end{array}$ | 39.57 | 2.385 | 1.3871364 | 1826 | $79 \quad 2837.41$ | 37.67 |
| . 336 | . 3779686 | 1916 | 785706.43 | 39.53 | . 386 | . 3873189 | 1824 | 792915.07 | 37.63 |
| - 337 | -378 1601 | 1914 | 785745.94 | 39.49 | . 387 | . 3875013 | 1823 | $79 \quad 2952.68$ | 37.60 |
| . 338 | -378 3515 | 1913 | $78 \quad 58 \quad 25.40$ | 39.45 | . 388 | . 3876834 | 182 I | 793030.26 | 37.56 |
| - 339 | - 3785427 | I9II | 785904.84 | 39.41 | . 389 | . 3878655 | 1819 | 793107.80 | 37.52 |
| 2.340 | I. 3787336 | 1909 | 785944.23 | 39.37 | 2.390 | I. 3880473 | 1817 | 79 31 45.30 | 37.49 |
| -341 | - 3789244 | 1907 | 790023.58 | 39.33 | . 391 | . 3882289 | 1816 | $\begin{array}{llll}79 & 32 & 22.77\end{array}$ | 37.45 |
| - 342 | - 3791150 | 1905 | 79 OI 02.89 | 39.30 | - 392 | . 3884104 | I8I4 | $\begin{array}{llll}79 & 33 & 00.20\end{array}$ | $37 \cdot 41$ |
| . 343 | . 3793054 | 1903 | 79 O1 42.17 | 39.26 | - 393 | . 3885917 | 1812 | $\begin{array}{lllllllll}79 & 33 & 59\end{array}$ | $37 \cdot 37$ |
| - 344 | - 3794957 | 1901 | 790221.41 | 39.22 | - 394 | . 3887728 | 1810 | 793414.95 | $37 \cdot 34$ |
| 2.345 | I. 3796857 | 1899 | 790300.61 | 39.18 | 2.395 | I. 3889537 | I808 | 793452.27 | $37 \cdot 30$ |
| - 346 | - 3798756 | 1898 | $\begin{array}{lllllllllllll}79 & 03 & 39.77\end{array}$ | 39. I4 | . 396 | - 389 I345 | 1807 | $\begin{array}{lllllllllllllllllll}79 & 35 & 29.55\end{array}$ | 37.26 |
| - 347 | -380 0652 | 1896 | 790418.89 | 39.10 | - 397 | - 3893150 | 1805 | 793606.80 | 37.23 |
| -348 | - 3802547 | 1894 | 790457.97 | 39.06 | - 398 | -389 4954 | 1803 | 793644.01 | 37.19 |
| - 349 | - 3804440 | 1892 | 790537.02 | 39.03 | - 399 | - 3896757 | 1801 | 7937 2I. 18 | 37.15 |
| 2.350 | I.380633I | 1890 | 790616.03 | 38.99 | 2.400 | I. 3898557 | 1800 | 793758.32 | 37.12 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega \mathrm{s}^{\text {ch }} \mathrm{u}$ | $2 \tan ^{-1}\left(\mathrm{e}^{4}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.400 | 1.3898557 | 1800 | $79^{\circ} 37{ }^{\prime \prime} 58.32$ | 37.12 | 2.4 |  |  |  | 4 |
| . 401 | . 3900356 | 1798 | $\begin{array}{llll}79 & 38 & 35.42\end{array}$ | 37.08 | 2.451 |  |  |  |  |
| . 402 | . 3902153 | 1796 | $\begin{array}{lllll}79 & 39 & \mathbf{1 2 . 4 8}\end{array}$ | 37.05 | . 452 | - 3989779 | 1710 | 800919.91 | $35 \cdot 30$ 35.27 |
| . 403 | - 3903948 | I794 | 793949.51 | 37.01 | . 453 | . 399 I488 | 1708 | 800955.16 | 35.23 |
| . 404 | - 390 574I | 1792 | 794026.50 | 36.97 | . 454 | . 3993195 | 1706 | 80 10 30.37 | 35.20 |
| 2.405 | I. 3907533 | 1791 | 79 41 03.45 | 36.94 | 2.455 | I. 399490 I | I705 | 80 II 05.55 | 35.16 |
| . 406 | . 3909323 | 1789 | 794140.37 | 36.90 | . 456 | . 3996605 | 1703 | 80 II 40.70 | 35.13 |
| . 407 | -391 IIII | 1787 | 794217.25 | 36.86 | . 457 | . 3998307 | 1701 | 8012 I 5.8 I | 35.09 |
| . 408 | . 3912897 | 1785 | 7942 54.10 | 36.83 | . 458 | . 4000007 | 1700 | 80 I2 50.88 | 35.06 |
| . 409 | . 391468 I | 1784 | 794330.91 | 36.79 | . 459 | . 4001706 | 1698 | 801325.92 | 35.02 |
| 2.410 | I.391 6464 | 1782 |  | 36.75 | 2.460 | I. 4003403 | I696 | 80 I4 00.93 | 34.99 |
| .41I | -391 8245 | 1780 | 794444.42 | 36.72 | . 461 | . 4005099 | 1695 | 80 I4 35.90 | 34.95 |
| . 412 | . 3920025 | 1778 | 7945 21.12 | 36.68 | . 462 | . 4006793 | 1693 | 801510.84 | 34.92 |
| .413 | . 3921802 | 1777 | $7945 \quad 57.78$ | 36.65 | . 463 | . 4008485 | 1691 | 80 15 45.74 | 34.89 |
| .414 | - 3923578 | I775 | 794634.41 | 36.61 | . 464 | . 4010175 | 1690 | 80 16 20.61 | 34.85 |
| 2.415 | 1. 3925352 | 1773 | 7947 II.00 | 36.57 | 2.465 | I. 4011864 | 1688 | 80 16 55.45 | 34.82 |
| . 416 | . 3927124 | 1771 | 794747.56 | 36.54 | . 466 | . 401 3551 | 1686 | 80 I7 30.25 | 34.78 |
| . 417 | . 3928895 | 1770 | 794824.08 | 36.50 | . 467 | . 4015237 | 1685 | 80 18 05.01 | 34.75 |
| . 418 | . 3930664 | 1768 | 794900.57 | 36.47 | . 468 | . 4016921 | 1683 | 80 I8 39.74 | 34.71 |
| . 419 | - 393 243I | 1766 | 794937.02 | 36.43 | . 469 | . 4018603 | 168I | 80 I9 14.44 | 34.68 |
| 2.420 | 1. 3934196 | 1764 | 79 50 13.43 | 36.39 | 2.470 | I. 4020283 | 1680 | 801949.10 | 34.65 |
| . 42 I | . 3935960 | 1763 | 795049.80 | 36.36 | . 47 I | . 4021962 | 1678 | $80 \quad 2023.73$ | 34.61 |
| . 422 | - 3937722 | 1761 | 79 51 26.15 | 36.32 | . 472 | . 4023639 | 1676 | $80 \quad 2058.33$ | 34.58 |
| . 423 | - 3939482 | 1759 | 795202.45 | 36.29 | . 473 | . 4025315 | 1675 | 80 21 32.89 | 34.54 |
| . 424 | . 3941240 | 1758 | $79 \quad 5238.72$ | 36.25 | -474 | . 4026989 | 1673 | 802207.41 | 34.51 |
| 2.425 | 1. 3942997 | 1756 | $\begin{array}{llll}79 & 53 & 14.96\end{array}$ | 36.22 | 2.475 | I. 402866 I | 1672 | 802241.91 | 34.48 |
| . 426 | . 3944752 | 1754 | 7953 51.15 | 36.18 | . 476 | . 4030332 | 1670 | 802316.36 | 34.44 |
| . 427 | . 3946505 | 1752 | 795427.32 | 36.14 | . 477 | . 4032001 | 1668 | $80 \quad 2350.79$ | 34.41 |
| . 428 | - 3948257 | 1751 | $\begin{array}{llllllll}79 & 55 & 03.44\end{array}$ | 36. II | . 478 | . 4033668 | 1666 | 802425.18 | $34 \cdot 37$ |
| . 429 | - 3950006 | 1749 | $79 \quad 5539.54$ | 36.07 | -479 | . 4035334 | 1665 | 802459.54 | $34 \cdot 34$ |
| 2.430 | 1.3951754 | 1747 | $79 \quad 5615.59$ | 36.04 | 2.480 | I. 4036998 | 1663 | 802533.86 | 34.3I |
| . 431 | . 3953501 | 1745 | 795651.61 | 36.00 | .48I | . 4038660 | 1662 | 8026 08.15 | 34.27 |
| . 432 | . 3955245 | 1744 | 795727.60 | 35.97 | . 482 | . 404 0321 | 1660 | 802642.40 | 34.24 |
| . 433 | . 3956988 | 1742 | $79 \quad 58 \quad 03.55$ | 35.93 | . 483 | . 4041980 | 1658 | 8027 I6.62 | 34.20 |
| . 434 | . 3958729 | 1740 | $79 \quad 5839.46$ | 35.90 | . 484 | . 4043637 | 1657 | 802750.81 | 34.17 |
| 2.435 | 1.3960469 | 1739 | 795915.34 | 35.86 | 2.485 | I. 4045293 | 1655 | $\begin{array}{llll}80 & 28 & 24.97\end{array}$ | 34.14 |
| . 436 | . 3962207 | 1737 | 7959 51.19 | 35.83 | . 486 | . 4046947 | 1653 | $80 \quad 2859.09$ | 34.10 |
| . 437 | - 3963943 | 1735 | $80 \quad 0026.99$ | 35.79 | . 487 | . 4048600 | 1652 | 80 | 34.07 |
| . 438 | - 3965677 | 1733 | 80 OI 02.77 | 35.76 | . 488 | . 405 025I | 1650 | 803007.23 | 34.04 |
| . 439 | - 3967410 | 1732 | 80 or 38.51 | 35.72 | . 489 | .4051900 | 1648 | 803041.25 | 34.00 |
| 2.440 | I. 396914 I | 1730 | 800214.2 I | 35.69 | 2.490 | I. 4053548 | 1647 | 803115.23 | 33.97 |
| . 441 | . 3970870 | 1728 | 800249.88 | 35.65 | . 491 | . 4055194 | 1645 | 803149.19 | 33.94 |
| . 442 | - 3972597 | 1727 | 800325.51 | 35.62 | . 492 | . 4056838 | 1644 | 803223.10 | 33.90 |
| . 443 | . 3974323 | 1725 | 8004 OI.II | 35.58 | . 493 | . 405848 I | 1642 | 80 | 33.87 |
| . 444 | - 3976047 | I723 | 800436.67 | 35.54 | . 494 | . 406 OI22 | 1640 | 803330.84 | 33.84 |
| 2.445 | 1. 3977770 | 1722 | 800512.20 | 35.51 | 2.495 | 1.405 1762 | 1639 | 803404.66 | 33.80 |
| . 446 | - 3979490 | 1720 | 80 | 35.48 | . 496 | . 4063400 | 1637 | 80 | 33.77 |
| . 447 | . 3981209 | 1718 | 8006123.15 | 35.44 | . 497 | . 4055036 | 1636 | 80 | 33.74 |
| .448 | - 3982927 | 1716 | 80 | 35.41 | . 498 | .406667 I | 1634 | 80 | 33.70 |
| . 449 | - 3984642 | 1715 | 800733.96 | 35.37 | . 499 | .4068304 | 1632 | 803619.60 | 33.67 |
| 2.450 | 1. 3986356 | 1713 | 800809.31 | $35 \cdot 34$ | 2.500 | I. 4069936 | 1631 | 803653.26 | 33.64 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(\mathrm{e}^{0}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech | $2 \tan ^{-1}(\mathrm{eu})-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.500 | I. 4069936 | 163I | $80^{\circ} 36^{\prime} 53.126$ | 33.64 | 2.550 | 22 |  | 04'14.22 | 22 |
| . 501 | . 407 I 566 | 1629 | 80 3726.88 | 33.60 | .551 | .415 1043 | 1551 | 81 0446.22 | 31.98 |
| . 502 | . 4073194 | 1627 | 803800.46 | 33.57 | - 552 | . 4152593 | 1549 | 81 0518.19 | 31.95 |
| . 503 | . 407482 I | 1626 | $\begin{array}{lllll}80 & 38 & 34.01\end{array}$ | 33.54 | . 553 | . 4154142 | I 548 | 81 05 50.13 | 31.92 |
| - 504 | . 4076446 | 1624 | 80 3907.54 | $33 \cdot 50$ | - 554 | .415 5688 | 1546 | 81 0622.03 | 31.89 |
| 2.505 | 1. 4078069 | 1623 | 803941.02 | $33 \cdot 47$ | 2.555 | 1.415 7234 | 1545 | 81 0653.9 I | 31.85 |
| . 506 | . 407969 I | 1621 | $80 \quad 4014.47$ | 33.44 | . 556 | . 4158778 | 1543 | 81 0725.75 | 31.83 |
| . 507 | . 408 I3II | 1619 | 80 4047.90 | 33.40 | . 557 | .416 0320 | I54I | 81 0757.56 | 31.80 |
| . 508 | . 4082930 | 1618 | 804121.28 | $33 \cdot 37$ | . 558 | .416 I860 | I 540 | 81 0829.34 | 31.76 |
| . 509 | . 4084547 | 1616 | 804154.64 | $33 \cdot 34$ | . 559 | . 4163400 | 1538 | 8I 0901.09 | 31.73 |
| 2.510 | 1. 4086163 | 15 | 804227.96 | 33.31 | 2.560 | 1.416 4937 | 1537 | 81 0932.80 | 31.70 |
| .511 | . 4087777 | 1613 | 8043 O1. 25 | 33.27 | . 561 | . 4166473 | 1535 | 8i Io 04.49 | 31.67 |
| . 512 | . 4089389 | 1612 | 804334.5 I | 33.24 | . 562 | . 4168008 | 1534 | 81 10 36.14 | 31.64 |
| . 513 | . 4091000 | 1610 | 804407.73 | 33.21 | . 563 | . 4169541 | 1532 | 81 II 07.77 | 31.61 |
| . 514 | . 4092609 | 1608 | 804440.92 | 33.17 | . 564 | . 4171073 | 1531 | 8I II 39.36 | 31.58 |
| 2.515 | I. 4094216 | 1 | $80 \quad 4514.08$ | 33.14 | 2.565 | 1.4172603 | 1529 | 81 1210.92 | 3I. 54 |
| . 516 | . 4095822 | 1605 | 804547.20 | 33.11 | . 566 | . 4174131 | 1528 | 81 1242.45 | 31.51 |
| . 517 | . 4097427 | 1504 | 804620.30 | 33.08 | . 567 | .4175659 | 1526 | 81 13 13.95 | 31.48 |
| . 518 | . 4099029 | 1602 | 804653.36 | 33.04 | . 568 | . 4177184 | 1525 | 81 13 45.4 I | 31.45 |
| . 519 | .410053 I | 1600 | $80 \quad 47 \quad 26.38$ | 33.01 | . 569 | .4178708 | 1523 | 81 14 16.85 | 31.42 |
| 2.520 | 1.410 2230 | 99 | 804759.38 | 32.98 | 2.570 | I. 418023 I | 1522 | 81 14 48.25 | 31. 39 |
| . 521 | . 4103828 | I 597 | 80 4832.34 | 32.95 | . 571 | . 4181752 | 1520 | 81 15 19.63 | 31.36 |
| . 522 | . 4105425 | 1595 | $80 \quad 4905.27$ | 32.91 | . 572 | . 4183271 | 1519 | 8i I5 50.97 | 3 I .33 |
| . 523 | .410 7020 | 1594 | 80 | 32.88 | . 573 | .4184789 | 1517 | 81 16 22.28 | 31.30 |
| . 524 | . 4108613 | 1593 | 80 50 II. 03 | 32.85 | . 574 | .4186306 | 1516 | 8ı 1653.56 | 3 I .27 |
| 2.525 | 1.4110205 | 1591 | 805043.86 | 32.82 | 2.575 | I.418 7821 | 1514 | 81 17 24.81 | 31.23 |
| . 526 | . 4111795 | 1589 | 805116.66 | 32.78 | . 576 | . 4189334 | 1513 | 81 17 56.03 | 31.20 |
| . 527 | - 4 II 3384 | 1588 | 8o 51 49.43 | 32.75 | . 577 | -419 0847 | 1511 | 81 181827.22 | 3 I .17 |
| . 528 | .4II 4971 | 1586 | 805222.17 | 32.72 | . 578 | . 4192357 | 1510 | 81 I8 58.38 | 3I.I4 |
| . 529 | .4II 6556 | 1585 | 805254.87 | 32.69 | . 579 | . 4193866 | 1508 | 81 19 29.50 | 3 I .1 I |
| 2.530 | I.4II 8140 | 1583 | $80 \quad 53 \quad 27.54$ | 32.65 | 2.580 | I.419 5374 | 1.507 | 81 2000.60 | 31.08 |
| . 53 I | .4II 9722 | 1582 | 805400.18 | 32.62 | . 58 I | . 4196880 | 1505 | 81 2031.67 | 3 I .05 |
| . 532 | .4121303 | 1580 | 80 | 32.59 | . 582 | . 4198384 | 1504 | 81 21 02.70 | 31.02 |
| . 533 | . 4122882 | 1578 | $80 \quad 5505.36$ | 32.56 | . 583 | . 4199888 | 1502 | 81 2133.70 | 30.99 |
| . 534 | . 4124460 | 1577 | 805537.90 | 32.53 | . 584 | . 420 1389 | 1501 | 81 2204.68 | 30.96 |
| 2.535 | 1.412 6036 | 1575 | 805610.41 | 32.49 | 2.585 | I. 4202889 | 1499 | 81 2235.62 | 30.93 |
| . 536 | . 4127611 | 1574 | 805642.89 | 32.46 | . 586 | . 4204388 | 1498 | 81 2306.53 | 30.90 |
| . 537 | . 4129184 | 1572 | 805715.33 | 32.43 | . 587 | . 4205885 | 1496 | 81 2337.4 I | 30.87 |
| . 538 | .413 0755 | 1571 | 805747.75 | 32.40 | . 588 | . 420738 I | 1495 | 81 2408.26 | 30.84 |
| . 539 | . 4132325 | 1569 | 805820.13 | 32.37 | . 589 | . 4208875 | 1493 | 81 2439.09 | 30.81 |
| 2.540 | 1.4133893 | 1568 | $\begin{array}{lllll}80 & 58 & 52.48\end{array}$ | 32.33 | 2.590 | 1.421 0368 | 1492 | 8I 2509.88 | 30.77 |
| . 54 I | . 4135460 | 1566 | 805924.80 | 32.30 | . 591 | . 4211859 | 1491 | 81 2540.63 | 30.74 |
| . 542 | . 4137025 | 1564 | 80 5957.08 | 32.27 | . 592 | . 4213349 | 1489 | 81 26 II. 36 | 30.71 |
| .543 | . 4138589 | 1563 | 81 0029.34 | 32.24 | . 593 | . 4214837 | 1488 | 81 2642.06 | 30.68 |
| . 544 | .414 OI5I | 1561 | 81 OI OI. 56 | 32.21 | . 594 | . 4216324 | 1486 | 81 2712.73 | 30.55 |
| 2.545 | 1.414 1712 | 1560 | 81 OI 33.75 | 32.17 | 2.595 | 1.421 7809 | 1485 | 81 $2743 \cdot 37$ | 30.52 |
| . 546 | . 4143271 | 1558 | 81 0205.91 | 32.14 | . 596 | . 4219293 | 1483 | 812813.98 | 30.59 |
| . 547 | . 4144829 | 1557 | 81 0238.03 | 32.11 | . 597 | . 4220776 | 1482 | 81 2844.55 | 30.56 |
| . 548 | . 4146385 | 1555 | 81 03 10.13 | 32.08 | . 598 | . 4222257 | 1480 | 81 29 I5.10 | 30.53 |
| . 549 | . 4147939 | 1554 | 81 0342.19 | 32.05 | . 599 | .4223736 | 1479 | 81 2945.62 | 30.50 |
| 2.550 | 1.414 9492 | 1552 | 81 0414.22 | 32.02 | 2.600 | 1.4225214 | 1477 | 81 30 16.11 | 30.47 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

Smithsonian tables

The Gudermannian.

| u | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.600 | 1.4225214 |  | 81 $30^{\circ}$ 16"II | 30.47 |  |  |  |  | 29.00 |
| . 601 | . 4226691 |  | 8r 3046.56 |  |  |  |  |  | . 00 |
| . 602 | . 422 8166 | 1474 | 813 |  | , |  |  | 81 5531.62 | 28.97 |
| . 603 | .4229640 | 1473 | 81 3147.39 | 30.38 | . 653 | . 430 I495 | 1402 | 56 |  |
| . 604 | . 423 III2 | 1471 | 81 32 I7.75 | 30.35 | . 654 | . 4302896 | 1400 | 8I 5658.41 | 28.89 |
| 2.605 | 1. 4232583 | 1470 | 81 3248.09 | 30.32 | 2.655 | I. 4304296 | I 399 | 81 5727.28 | 28.86 |
| . 606 | . 4234052 | 1469 | $\begin{array}{llll}81 & 33 & 18.40\end{array}$ | 30.29 | . 656 | . 4305694 | I 398 | 81 5756.12 | 28.83 |
| . 607 | . 4235520 | 1467 | 81 3348.67 | 30.26 | . 657 | . 430709 I | I396 | 81 $58 \quad 24.94$ | 28.80 |
| . 608 | . 4236986 | 1466 | 81 3418.92 | 30.23 | . 658 | . 4308487 | 1395 | 81 5853.72 | 28.77 |
| . 609 | . 4238451 | 1464 | 81 3449.15 | 30.20 | . 659 | . 430 988I | 1394 | 81 5922.48 | 28.74 |
| 2.610 | 1.4239915 | 1463 | 81 3519.32 | 30.17 | 2.660 | I.43I I274 | 1392 | 81 5951.21 | 28.72 |
| . 611 | . 4241377 | 1461 | 81 3549.48 | 30.14 | . 661 | . 4312665 | 1391 | 820019.91 | 28.69 |
| . 612 | . 4242837 | 1460 | 8i 3619.61 | 30.11 | . 662 | . 4314055 | 1389 | 820048.58 | 28.66 |
| .613 | . 4244297 | 1458 | 8I 3649.7 I | 30.08 | . 663 | . 4315444 | 1388 | 82 OI I7.23 | 28.63 |
| . 614 | . 4245754 | 1457 | 81 3719.77 | 30.05 | . 664 | -431 683I | I387 | 82 or 45.84 | 28.60 |
| 2.615 | 1.4247211 | 1456 | 8 I 3749.8 I | 30.02 | 2.665 | I.431 8217 | I385 | 820214.43 | 28.57 |
| . 616 | . 4248665 | 1454 | 81 3819.82 | 29.99 | . 666 | . 4319602 | 1384 | 820242.99 | 28.55 |
| . 617 | . 425 OII9 | 1453 | 81 3849.80 | 29.96 | . 667 | . 4320985 | I383 | 8203 II. 52 | 28.52 |
| .618 | . 4251571 | 1451 | 81 3919.75 | 29.93 | . 668 | . 4322367 | 1381 | 820340.02 | 28.49 |
| . 619 | . 425302 I | 1450 | 81 3949.67 | 29.90 | . 669 | . 4323747 | 1380 | 820408.50 | 28.46 |
| 2.620 | 1.4254470 | 8 | 81 4019.56 | 29.87 | 2.670 | I. 4325127 | 1378 | 820436.95 | 28.43 |
| . 621 | . 4255918 | 1447 | 81 4049.42 | 29.85 | . 671 | . 4326504 | 1377 | 820505.36 | 28.40 |
| . 622 | . 4257364 | 1446 | 81 4I 19.25 | 29.82 | . 672 | . 432 7881 | 1376 | 820533.75 | 28.38 |
| . 623 | . 4258809 | 1444 | 8I 4I 49.05 | 29.79 | . 673 | . 4329256 | 1374 | 820602.12 | 28.35 |
| . 624 | . 4260252 | 1443 | 81 4218.82 | 29.76 | . 674 | . 4330629 | I373 | 820630.45 | 28.32 |
| 2.625 | 1. 4261694 | 144I | 81 4248.56 | 29.73 | 2.675 | 1. 4332002 | 1372 | 820658.76 | 28.29 |
| . 626 | . 426 3135 | 1440 | 814318.28 | 29.70 | . 676 | . 4333373 | 1370 | 820727.03 | 28.26 |
| . 627 | . 4264574 | 1438 | 81 4347.96 | 29.67 | . 677 | . 4334742 | 1369 | 820755.28 | 28.24 |
| . 628 | . 4266012 | 1437 | 81 44 I7.6I | 29.64 | . 678 | . 433 6110 | I368 | 820823.51 | 28.21 |
| . 629 | . 4267448 | 1436 | 81 4447.24 | 29.61 | . 679 | . 4337477 | I366 | 820851.70 | 28.18 |
| 2.630 | I. 4268883 | 1434 | 81 45 16.83 | 29.58 | 2.680 | I. 4338843 | 1365 | 820919.86 | 28.15 |
| . 631 | . 427 03I6 | 1433 | 81 4546.40 | 29.55 | .68I | . 4340207 | 1363 | 820948.00 | 28.12 |
| . 632 | . 427 I748 | 1431 | 81 4615.94 | 29.52 | . 682 | . 434 I570 | 1362 | 82 10 16.11 | 28.10 |
| . 633 | . 4273179 | 1430 | 8 I 4645.44 | 29.49 | . 683 | . 434 293I | 1361 | 82 10 44.20 | 28.07 |
| . 634 | . 4274608 | 1428 | 81 47 I4.92 | 29.46 | . 684 | . 4344291 | 1359 | 82 II I2.25 | 28.04 |
| 2.635 | 1.4276036 |  | 81 4744.37 | 29.43 | 2.685 | 1. 4345650 | 1358 | 82 II 40.28 | 28.01 |
| . 636 | . 4277462 | 1426 | 81 48 I3.79 | 29.41 | . 685 | . 4347008 | I 357 | 82 12 08.28 | 27.99 |
| . 637 | . 4278887 | 1424 | 81 4843.18 | 29.38 | . 687 | . 4348364 | 1355 | 82 I2 36.25 | 27.96 |
| . 638 | . 4280310 | 1423 | 81 49 I2.55. | 29.35 | . 688 | . 4349719 | 1354 | 821304.19 | 27.93 |
| . 639 | . 428 I732 | 1421 | 81 49 41.88 | 29.32 | . 689 | . 4351072 | 1353 | 82 13 32.11 | 27.90 |
| 2.640 | 1.4283153 | 1420 | 81 50 II. 18 | 29.29 | 2.690 | 1.4352424 | 1351 | 82 I3 59.99 | 27.87 |
| . 641 | . 4284572 | 1419 | 81 5040.46 | 29.26 | . 691 | . 4353775 | I350 | 82 I 427.86 | 27.85 |
| . 642 | . 4285990 | 1417 | 81 5109.70 | 29.23 | . 692 | . 4355124 | 1349 | 821455.69 | 27.82 |
| . 643 | . 4287407 | 1416 | 81 5I 38.92 | 29.20 | . 693 | . 4356472 | 1347 | 8215123.49 | 27.79 |
| . 644 | . 4288822 | 1414 | 81 52 08.1I | 29.17 | . 694 | . 435 7819 | I346 | 82 I5 51.27 | 27.77 |
| 2.645 | 1. 4290236 | 1413 | 81 5237.27 | 29.14 | 2.695 | 1. 4359164 | I345 | 821619.02 | 27.74 |
| . 646 | . 4291648 | 1412 | 81 5306.40 | 29.12 | . 696 | . 4360508 | 1343 | 821646.75 | 27.71 |
| . 647 | . 4293059 | 1410 | 81 5335.50 | 29.09 | . 697 | . 436 I851 | 1342 | 821714.44 | 27.68 |
| . 648 | . 4294468 | 1409 | 81 54.04 .57 | 29.06 | . 698 | . 4363192 | I34I | $821742: 11$ | 27.65 |
| . 649 | . 4295876 | 1407 | 81 5433.62 | 29.03 | . 699 | . 4364532 | I339 | $82 \quad 1809.75$ | 27.63 |
| 2.650 | 1. 4297283 | 1406 | 81 $55 \quad 02.63$ | 29.00 | 2.700 | 1.4365871 | 1338 | $\begin{array}{lllll}82 & 18 & 37.36\end{array}$ | 27.60 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | h | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech | u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gdu | $\omega F_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.700 | 1.436 587 I | 1338 | $82^{\circ} 188^{\prime} 37.36$ | 27.60 | 2.750 | I. 443 II44 | 1273 | $82^{\circ} 4 \mathrm{I}^{\prime} 03.70$ | 26.26 |
| . 701 | .4367209 | 1337 | $82 \begin{array}{llll}8 & 19 & 4.95\end{array}$ | 27.57 | .75I | . 4432416 | 1272 | 824129.95 | 26.24 |
| . 702 | . 4368545 | 1335 | 82 19 32.51 | 27.54 | . 752 | . 4433688 | 127 I | 824156.18 | 26.21 |
| . 703 | . 4369879 | 1334 | 822000.04 | 27.52 | . 753 | . 4434958 | 1270 | 824222.38 | 26. 19 |
| . 704 | . 437 I213 | 1333 | $82 \quad 2027.54$ | 27.49 | . 754 | . 4436227 | 1268 | 824248.55 | 26.16 |
| 2.705 | I. 4372545 | 1331 | 822055.02 | 27.46 | 2.755 | I. 4437495 | 1267 | 824314.70 | 26.14 |
| . 706 | . 4373876 | 1330 | 82 21 22.47 | 27.44 | . 756 | . 4438761 | 1266 | 824340.82 | 26.11 |
| . 707 | . 4375205 | 1329 | 82 21 49.89 | 27.41 | . 757 | . 4440026 | 1265 | 824406.92 | 26.08 |
| . 708 | . 4376533 | 1327 | 822217.29 | 27.38 | . 758 | . 4441290 | 1263 | 824432.99 | 26.06 |
| . 709 | . 4377860 | 1326 | 822244.66 | 27.35 | . 759 | . 4442553 | 1262 | 824459.03 | 26.03 |
| 2.710 | I. 4379186 | 1325 | $82 \quad 2312.00$ | 27.33 | 2.760 | I. 44438 I 4 | I26I | 824525.05 | 26.01 |
| . 711 | . 4380510 | 1324 | 822339.31 | 27.30 | . 761 | . 4445074 | 1260 | 824551.04 | 25.98 |
| . 712 | . 438 I833 | 1322 | 822406.60 | 27.27 | . 762 | . 4446333 | 1258 | 824617.01 | 25.95 |
| . 713 | . 438 3154 | 1321 | 822433.85 | 27.25 | . 763 | . 444759 I | 1257 | 824642.95 | 25.93 |
| . 714 | . 4384475 | 1320 | 8225 OI. 09 | 27.22 | . 764 | . 4448847 | 1256 | 824708.87 | 25.90 |
| 2.715 | I. 4385794 | 1318 | 8225128.29 | 27.19 | 2.765 | 1 L .4450102 | 1255 | 824734.76 | 25.88 |
| . 716 | . 438 7III | 1317 | $82 \quad 25 \quad 55.47$ | 27.17 | . 766 | . 4451356 | 1253 | 824800.62 | 25.85 |
| . 717 | . 4388428 | 1316 | 822622.63 | 27.14 | . 767 | .4452609 | 1252 | 824826.46 | 25.83 |
| . 718 | . 4389743 | 1314 | 822649.75 | 27.11 | . 768 | . 4453860 | I25I | 824852.27 | 25.80 |
| . 719 | . 4391057 | 1313 | 822716.85 | 27.08 | . 769 | . 445 511I | 1250 | 82.49 18.06 | 25.77 |
| 2.720 | I. 4332369 | 1312 | 822743.92 | 27.06 | 2.770 | 1. 4456360 | 1248 | 824943.82 | 25.75 |
| . 72 I | . 4393680 | 1310 | 822810.96 | 27.03 | . 771 | . 4457607 | 1247 | 825009.56 | 25.72 |
| . 722 | . 4394990 | 1309 | $\begin{array}{lllll}82 & 28 & 37.98\end{array}$ | 27.00 | . 772 | . 4458854 | 1246 | 825035.27 | 25.70 |
| . 723 | . 4396299 | 1308 | $82 \begin{array}{llllllll}82 & 29 & 04.97\end{array}$ | 26.98 | . 773 | . 446 10099 | 1245 | 825100.95 | 25.67 |
| . 724 | . 4397606 | 1307 | 822931.94 | 26.95 | . 774 | . 446 I343 | 1243 | 825126.61 | 25.65 |
| 2.725 | 1. 43988912 | 1305 | $82 \quad 2958.87$ | 26.92 | 2.775 | I. 4462586 | 1242 | 825152.25 | 25.62 |
| . 726 | . 440 0216 | 1304 | 823025.79 | 26.90 | . 776 | . 4463827 | I24I | 825217.86 | 25.60 |
| . 727 | . 440 I 520 | 1303 | 823052.67 | 26.87 | . 777 | . 4465068 | 1240 | 825243.44 | 25.57 |
| . 728 | . 4402822 | 1301 | 823119.53 | 26.84 | . 778 | . 4466307 | 1238 | 825309.00 | 25.55 |
| . 729 | . 440 4123 | 1300 | 82 3I 46.36 | 26.82 | . 779 | . 4467545 | 1237 | 825334.53 | 25.52 |
| 2.730 | I. 4405422 | 1299 | 823213.16 | 26.79 | 2.780 | I. 4468781 | 1236 | 825400.04 | 25.49 |
| . 731 | . 4406720 | 1298 | 823239.94 | 26.76 | . 781 | .4470017 | 1235 | 82. 5425.52 | 25.47 |
| . 732 | . 440 8017 | 1296 | 823306.69 | 26.74 | . 782 | . 4471251 | 1234 | 825450.98 | 25.44 |
| . 733 | . 44093 I 3 | 1295 | 823333.42 | 26.71 | . 783 | . 4472484 | 1232 | 825516.41 | 25.42 |
| . 734 | .441 0607 | 1294 | 823400.11 | 26.68 | . 784 | .4473716 | 1231 | 825541.81 | 25.39 |
| 2.735 | I.44I 1900 | 1292 | 823425.78 | 26.66 | 2.785 | I. 4474946 | 1230 | 825607.19 | 25.37 |
| . 736 | . 441 3192 | 1291 | 823453.43 | 26.63 | . 786 | . 447 6I75 | 1229 | 825632.55 | 25.34 |
| . 737 | -441 4483 | 1290 | $\begin{array}{llll}82 & 35 & 20.05\end{array}$ | 26.61 | . 787 | . 4477403 | 1227 | 825657.88 | 25.32 |
| . 738 | . 4415772 | 1289 | 823546.64 | 26.58 | . 788 | . 4478630 | 1226 | 8257 23.19 | 25.29 |
| . 739 | .441 7060 | 1287 | 823613.21 | 26.55 | .789 | . 4479856 | 1225 | 825748.47 | 25.27 |
| 2.740 | I.441. 8347 | 1286 | 823639.75 | 26.53 | 2.790 | 1. 4481080 | 1224 | 825813.72 | 25.24 |
| . 741 | . 4419632 | 1285 | $\begin{array}{lllll}82 & 37 & 06.26\end{array}$ | 26.50 | .791 | . 4482303 | 1223 | 825838.95 | 25.22 |
| . 742 | . 4420916 | 1283 | 823732.75 | 26.47 | . 792 | . 4483525 | I22I | 825904.16 | 25.19 |
| .743 | . 4422199 | 1282 | $\begin{array}{lllll}82 & 37 & 59.21\end{array}$ | 26.45 | . 793 | . 4484746 | 1220 | 825929.34 | 25.17 |
| . 744 | . 442348 I | 1281 | $\begin{array}{lllll}82 & 38 & 25.64\end{array}$ | 26.42 | . 794 | . 4485966 | 1219 | 825954.49 | 25.14 |
| 2.745 | I. 442476 I | 1280 | $\begin{array}{llll}82 & 38 & 52.05\end{array}$ | 26.40 | 2.795 | I. 4487184 | 1218 | 830019.62 | 25.12 |
| .746 | - 4426040 | 1278 | $\begin{array}{llll}82 & 39 & 18.43\end{array}$ | 26.37 | . 796 | . 4488401 | 1217 | 830044.73 | 25.09 |
| . 747 | . 4427318 | 1277 | $\begin{array}{llll}82 & 39 & 44.79\end{array}$ | 26.34 | . 797 | -448 9617 | 1215 | 83 OI 09.81 | 25.07 |
| . 748 | . 4428594 | 1276 | 8240 II. I2 | 26.32 | . 798 | . 4490832 | 1214 | 83 OI 34.86 | 25.04 |
| . 749 | .4429870 | 1275 | 824037.42 | 26.29 | . 799 | . 4492045 | 1213 | 83 or 59.90 | 25.02 |
| 2.750 | I. 443 II44 | 1273 | 824103.70 | 26.26 | 2.800 | 1. 4493258 | 1212 | 830224.90 | 24.99 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech $u$ | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | $\mathrm{gd} u$ | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.800 | I. 4493258 | 1212 | $83^{\circ} 022^{\prime \prime} 24.90$ |  | 850 |  |  | - " |  |
| . 801 | . 4494469 | I2II | 830249.88 | 24.97 | .85'I | 4553517 | 1152 |  |  |
| . 802 | . 4495679 | 1209 | $\begin{array}{lllll}83 & 03 & 14.84\end{array}$ | 24.94 | . 852 | . 4554668 | II5I | 832331.58 |  |
| . 803 | . 4496888 | 1208 | 8303139.77 | 24.92 | . 853 | . 455 5819 | II50 | 832355.31 | 23.71 |
| . 804 | . 4498095 | 1207 | 830404.68 | 24.89 | . 854 | . 4556968 | II48 | $83 \quad 24$ I9.01 | 23.69 |
| 2.805 | I. 4499301 | 1206 | $\begin{array}{llll}83 & 04 & 29.56\end{array}$ | 24.87 | 2.855 | I. $4558 \mathrm{II5}$ | 1147 | 832442.69 | 23.67 |
| . 806 | . 4500507 | 1205 | 830454.42 | 24.85 | . 856 | . 4559262 | 1146 | $83 \quad 2506.34$ | 23.64 |
| . 807 | . 450 1710 | 1203 | 830519.25 | 24.82 | . 857 | . 4560408 | I 145 | 832529.97 | 23.62 |
| . 808 | . 4502913 | 1202 | 830544.06 | 24.80 | . 858 | . 4561552 | II44 | 832553.58 | 23.59 |
| . 809 | . 450 4II5 | I201 | 830608.84 | 24.77 | . 859 | . 4562696 | II43 | 8326 17.16 | 23.57 |
| 2.810 | I. 4505315 | 1200 | 830633.60 | 24.75 | 2.860 | I. 4563838 | 1142 | $\begin{array}{lll}83 & 2640.72\end{array}$ | 23.55 |
| .8II | . 4506514 | 1199 | 830658.33 | 24.72 | . 86 I | . 4564979 | 1140 | 832704.25 | 23.52 |
| . 812 | . 4507712 | I I98 | 830723.04 | 24.70 | . 862 | . 456 6II9 | 1139 | $8327 \quad 27.77$ | 23.50 |
| . 813 | . 4508909 | I:196 | 830747.73 | 24.67 | . 863 | . 4567258 | II38 | 832751.26 | 23.48 |
| . 814 | . 4510105 | 1195 | $\begin{array}{lllllll}83 & 08 & 12.39\end{array}$ | 24.65 | . 864 | . 4568395 | II37 | 8328 14.72 | 23.45 |
| 2.815 | 1.451 1299 | 1194 | 83 08 37.03 | 24.62 | 2.865 | I. 4569532 | 1136 | $83 \quad 2838.16$ | 23.43 |
| .816 | . 4512492 | 1193 | 830901.64 | 24.60 | . 866 | . 4570667 | II35 | 8329 0.1. 58 | 23.41 |
| . 817 | .451 3684 | 1191 | $\begin{array}{llllllllllll}83 & 09 & 26.23\end{array}$ | 24.58 | . 867 | . 457 1801 | II34 | 832924.98 | 23.38 |
| .818 | . 4514875 | 1190 | 830950.79 | 24.55 | . 868 | . 4572935 | 1133 | 832948.35 | 23.36 |
| . 819 | . 4516065 | I 189 | 83 IO 15.33 | 24.53 | . 869 | . 4574067 | II3I | 8330 II. 70 | 23.34 |
| 2.820 | I.451 7253 | 1188 | 83 10 39.84 | 24.50 | 2.870 | I. 4575198 | II30 | $83 \quad 30 \quad 35.03$ | 23.32 |
| . 821 | . 451844 I | 1187 | 83 II 04.33 | 24.48 | . 871 | . 4576327 | 1129 | 833058.33 | 23.29 |
| . 822 | -451 9627 | II86 | 83 II 28.80 | 24.45 | . 872 | . 4577456 | 1128 | 83 31 21.6I | 23.27 |
| . 823 | . 452 0812 | II84 | 83 II 53.24 | 24.43 | . 873 | . 4578584 | 1.127 | 83 31 44.87 | 23.25 |
| . 824 | . 4521995 | I 183 | 831217.66 | 24.41 | . 874 | . 4579710 | 1126 | 833208.11 | 23.22 |
| 2.825 | 1.452 3178 | 1182 | 831242.05 | 24.38 | 2.875 | 1. 4580835 | 1125 | 833231.32 | 23.20 |
| . 826 | . 4524359 | I I8I | 83 13 06.42 | 24.36 | . 876 | . 4581959 | 1124 | 833254.50 | 23.18 |
| . 827 | . 4525540 | 1180 | 83 13 30.76 | 24.33 | . 877 | . 4583083 | 1123 | 8333317.67 | 23.15 |
| . 828 | . 4526719 | 1178 | 83 I3 55.08 | 24.31 | . 878 | . 4584204 | II2I | 833340.81 | 23.13 |
| . 829 | . 4527897 | 1177 | 83 I4 19.38 | 24.28 | . 879 | . 4585325 | I 120 | 833403.93 | 23.11 |
| 2.830 | I. 4529073 | 1176 | 83 I4 43.65 | 24.26 | 2.880 | I. 4586445 | III9 | 833427.03 | 23.08 |
| . 83 I | . 4530249 | II75 | 83 I5 07.90 | 24.24 | . 881 | . 4587564 | 1118 | 833450.10 | 23.06 |
| . 832 | . 4531423 | II74 | 83 15 32.12 | 24.21 | . 882 | . 458 8681 | 1117 | 8335 I3.15 | 23.04 |
| . 833 | . 4532597 | II73 | 83 15 56.32 | 24.19 | . 883 | . 4589798 | 1116 | 833536.18 | 23.02 |
| . 834 | . 4533769 | II7I | $\begin{array}{llll}83 & 16 & 20.50\end{array}$ | 24. 16 | . 884 | . 459 09I3 | III5 | 8335 59.18 | 22.99 |
| 2.835 | I. 4534940 | II70 | $83 \quad 1644.65$ | 24.14 | 2.885 | I. 4592027 | III4 | 833622.16 | 22.97 |
| . 836 | . 453 6109 | 1169 | 83 I7 08.78 | 24.12 | . 886 | . 4593140 | ILI3 | 833645.12 | 22.95 |
| . 837 | . 4537278 | 1168 | 83 I7 32.88 | 24.09 | . 887 | . 4594252 | IIII | 833708.06 | 22.92 |
| . 838 | . 4538445 | 1167 | 83 I7 56.96 | 24.07 | . 888 | . 4595363 | IIIO | 833730.97 | 22.90 |
| . 839 | . 453 9612 | II66 | 83 I8 21.02 | 24.04 | . 889 | . 4596473 | 1109 | 833753.86 | 22.88 |
| 2.840 | I. 4540777 | I'165 | 83 I8 45.05 | 24.02 | 2.890 | I. 459758 I | 1108 | $83 \quad 3816.73$ | 22.86 |
| . 841 | . 454 194I | 1163 | 83 19 09.06 | 24.00 | . 891 | . 4598689 | 1107 | $\begin{array}{lllll}83 & 38 & 39.57\end{array}$ | 22.83 |
| .842 | . 4543104 | 1162 | 83 I9 33.04 | 23.97 | . 892 | . 4599795 | 1106 | 833902.40 | 22.81 |
| . 843 | - 4544265 | 1161 | 83 I9 57.01 | 23.95 | . 893 | . 4600901 | 1105 | 8339 25.19 | 22.79 |
| . 844 | . 4545426 | 1160 | $83 \quad 2020.94$ | 23.93 | . 894 | . 4602005 | 1104 | 833947.97 | 22.77 |
| 2.845 | I. 4546585 | I I59 | $83 \quad 2044.85$ | 23.90 | 2.895 | I. 4603108 | 1103 | $83 \quad 4010.73$ | 22.74 |
| . 846 | - 4547743 | 1158 | 83 21 08.74 | 23.88 | . 896 | . 4604210 | I IOI | 834033.46 | 22.72 |
| . 847 | . 4548900 | 1156 | 832132.61 | 23.85 | . 897 | . 46053 II | 1100 | 834056.17 | 22.70 |
| . 848 | . 4550056 | 1155 | 83 21 56.45 | 23.83 | . 898 | . 4606411 | 1099 | 834118.85 | 22.68 |
| . 849 | . 455 1211 | II54 | $83 \quad 2220.27$ | 23.8 I | . 899 | . 4607510 | 1098 | 834141.52 | 22.65 |
| 2.850 | I. 4552365 | I153 | $83 \quad 2244.07$ | 23.78 | 2.900 | I. 4608607 | 1097 | 834204.16 | 22.63 |
| u | $2 \tan ^{-1}\left(e^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | $\omega$ sech u | $u$ | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $u$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2.900 | 1. |  | $83^{\circ} 42^{\prime} 04.16$ | 22.63 |  |  |  | - $00^{\prime} 28.00$ |  |
| .90I | . 4609704 | 1096 | 834226.78 | 22.61 | .95I | . 4663167 | 1043 | 840049.53 | 51 |
| . 902 | . 4610800 | 1095 | 834249.37 | 22.59 | . 952 | .4664209 | 1042 | 84 OI II.03 | 21. 49 |
| . 903 | .46I 1894 | 1094 | 8343 II. 95 | 22.56 | . 953 | . 466525 I | IO4I | 84 or 32.51 | 21.47 |
| . 904 | . 4612987 | 1093 | 8343 34.50 | 22.54 | . 954 | . 466 6291 | 1040 | 84 OI 53.97 | 21.45 |
| 2.905 | I. 4614080 | 1092 | 834357.03 | 22.52 | 2.955 | 1.4667330 | 1039 | 840215.40 | 2 I .43 |
| . 906 | .461 5171 | 1091 | 834419.54 | 22.50 | . 956 | . 4668368 | 1038 | 840236.82 | 21.40 |
| . 907 | .461 626I | 1090 | 834442.02 | 22.47 | . 957 | . 4669406 | 1037 | 840258.21 | 21. 38 |
| . 908 | .461 7350 | 1088 | $83 \quad 4504.48$ | 22.45 | . 958 | . 4670442 | 1036 | 840319.58 | 21. 36 |
| . 909 | . 4618438 | 1087 | 834526.92 | 22.43 | . 959 | . 4671477 | 1035 | 840340.93 | 21.34 |
| 2.910 | 1.4619525 | 1086 | 834549.34 | 22.41 | 2.960 | I. 4672511 | 1034 | 840402.27 | 21.32 |
| .91I | . 4620610 | 1085 | 8346 II. 73 | 22.38 | .961 | . 4673544 | 1033 | 840423.57 | 21.30 |
| . 912 | . 462 I695 | 1084 | 8346 34. II | 22.36 | . 962 | .4674576 | 1032 | 840444.86 | 21.28 |
| . 913 | . 4622779 | 1083 | 834656.46 | 22.34 | . 963 | .4675607 | 1031 | 840506.13 | 21.26 |
| . 914 | . 462 386I | 1082 | 834718.79 | 22.32 | . 964 | . 4676637 | 1029 | $84 \quad 05 \quad 27.37$ | 21.23 |
| 2.915 | 1. 4624942 | 1081 | 834741.09 | 22.30 | 2.965 | 1. 4677666 | 1028 | 840548.60 | 21.21 |
| . 916 | .4626023 | 1080 | 834803.38 | 22.27 | . 966 | . 4678694 | 1027 | 840609.80 | 21.19 |
| .917 | .4627102 | 1079 | $\begin{array}{lllll}83 & 48 & 25.64 \\ 83 & 4 & 47.88\end{array}$ | 22.25 | . 967 | . 4679721 | 1026 | 840630.98 | 21.17 |
| .918 | . 4628180 | 1078 | 834847.88 | 22.23 | . 968 | . 4680747 | 1025 | 840652.14 | 21.15 |
| . 919 | . 4629257 | 1077 | 8349 IO. 10 | 22.21 | . 969 | .468 I772 | 1024 | 8407 I3.29 | 21.13 |
| 2.920 | 1.4630334 | 1076 | 834932.29 | 22.18 | 2.970 | 1. 4682796 | 1023 | 840734.40 | 21.11 |
| . 921 | .4631409 | 1074 | 834954.47 | 22.16 | . 971 | . 4683819 | 1022 | 840755.50 | 21.09 |
| . 922 | . 4632483 | 1073 | 835016.62 | 22.14 | . 972 | . 468 484I | 1021 | 840816.58 | 21.07 |
| .923 | . 4633555 | 1072 | 835038.75 | 22.12 | . 973 | . 468 586I | 1020 | 840837.64 | 21.05 |
| . 924 | . 4634627 | 1071 | 83 5I 00.86 | 22.10 | . 974 | . 468 6881 | 1019 | 840858.67 | 21.02 |
| 2.925 | 1. 4635698 | 1070 | 835122.94 | 22.07 | 2.975 | I. 4687900 | IOI8 | 8409 I9.69 | 21.00 |
| . 926 | . 4636768 | 1069 | 835145.00 | 22.05 | . 976 | . 4688918 | 1017 | 840940.68 | 20.98 |
| . 927 | .4637836 | 1068 | 835207.05 | 22.03 | . 977 | . 4689935 | 1016 | 84 10 01. 65 | 20.96 |
| . 928 | . 4638904 | 1067 | 835229.07 | 22.01 | . 978 | . 4690950 | 1015 | 841022.60 | 20.94 |
| . 929 | . 4639970 | 1066 | 835251.06 | 21. 99 | . 979 | . 469 1965 | 1014 | 84 10 43.53 | 20.92 |
| 2.930 | 1.4641036 | 1065 | 835313.04 | 21.97 | 2.980 | 1.4692979 | 1013 | 84 II 04.44 | 20.90 |
| .93I | . 4642100 | 1064 | 8353134.99 | 21.94 | .98I | . 4693992 | IOI2 | 84 II 25.33 | 20.88 |
| . 932 | . 4643163 | 1063 | 835356.93 | 21.92 | . 982 | . 4695003 | IOII | 841146.20 | 20.86 |
| . 933 | . 4644226 | 1062 | 835418.84 | 21.90 | . 983 | . 4696014 | 1010 | 841207.05 | 20.84 |
| . 934 | . 4645287 | 1061 | 835440.73 | 21.88 | . 984 | . 4697024 | 1009 | 841227.88 | 20.82 |
| 2.935 | 1.464 6347 | 1060 | 8355502.59 | 21.86 | 2.985 | I. 4698033 | 1008 | 841248.68 | 20.80 |
| . 936 | . 4647406 | 1059 | 8355124.44 | 21.83 | . 986 | . 4699040 | 1007 | 84 I3 09.47 | 20.78 |
| . 937 | . 4648464 | 1058 | 835546.26 | 21.8 I | . 987 | . 4700047 | 1006 | 84 I3 30.23 | 20.75 |
| . 938 | . 464952 I | 1056 | 835608.07 | 21.79 | . 988 | . 4701053 | 1005 | 841350.98 | 20.73 |
| . 939 | . 4650577 | 1055 | 835629.85 | 21.77 | .989 | . 4702057 | 1004 | 84 I4 II.70 | 20.71 |
| 2.940 | 1.465 1632 | 1054 | 835651.60 | 21.75 | 2.990 | 1.4703061 | 1003 | 841432.40 | 20.69 |
| . 941 | . 4652686 | 1053 | 835713.34 | 21.73 | .991 | . 4704064 | 1002 | 841453.09 | 20.67 |
| .942 | . 4653739 | 1052 | 835735.06 | 21.70 | . 992 | . 4705065 | 1001 | 84 I5 13.75 | 20.65 |
| -943 | . 4654790 | 1051 | $\begin{array}{lllll}83 & 57 & 56.75 \\ 83 & 58 & 18.4\end{array}$ | 21.68 | . 993 | . 4706066 | 1000 | 841534.39 | 20.63 |
| . 944 | . 465 5841 | 1050 | 835818.42 | 21. 66 | . 994 | . 4707066 | 999 | 841555.01 | 20.61 |
|  | 1.465 6891 | 1049 | 835840.07 | 21.64 | 2.995 | I. 4708065 | 998 | 841615.61 | 20.59 |
| . 946 | . 4657939 | 1048 | 835901.70 | 21.62 | . 996 | . 4709062 | 997 | 841636.19 | 20.57 |
| . 947 | . 4658087 | 1047 | $\begin{array}{llll}83 & 59 & 23.31 \\ 83 & 59 & 44.90\end{array}$ | 21.60 21.58 | . 997 | -471 0059 | 996 | 84 16 56.75 | 20.55 |
| . 948 | . 4660033 | 1046 | $\begin{array}{lll}83 & 59 & 44.90 \\ 84 & 00 & 06.46\end{array}$ | 21.58 | . 998 | . 4711055 | 995 | 841717.29 | 20.53 |
| . 949 | . 4661079 | 1045 | 840006.46 | 21.55 | . 999 | . 4712050 | 994 | 8417 37.8I | 20.51 |
| 2.950 | I. 4662123 | 1044 | 840028.00 | 21.53 | 3.000 | 1.4713043 | 993 | 841758.30 | 20.49 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{4}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | chu | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| u | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | $\mathrm{gd} u$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | $\mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gdu | $\omega \mathrm{F}_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 3.00 | 1.4713043 | 9933 | $84^{\circ} 17^{\prime} 58.30$ | 204.88 | 3.50 | I.510 4199 | 6034 | $86^{\circ} 32^{\prime} 26^{\prime \prime} .47$ |  |
| . OI | . 4722927 | 9835 | 842122.17 | 202.85 | . 51 | .511 0203 | 5974 | 863430.31 |  |
| . 02 | . 4732713 | 9737 | 842444.01 | 200.84 | . 52 | . 5116147 | 5915 | 863632.92 | 122.00 |
| . 03 | . 4742401 | 964 I | 842803.86 | 198.85 | . 53 | . 5122033 | 5856 | 863834.31 | 120.79 |
| . 04 | . 4751994 | 9545 | 84 31 2I. 72 | 196.88 | . 54 | .5127859 | 5798 | $864034 \cdot 50$ | 119.59 |
| 3.05 | 1.476 1492 | 9451 | 843437.63 | 194.93 | 3.55 | I. 5133628 | 5740 | 864233.49 | I 18.40 |
| . 06 | . 4770896 | 9357 | 843751.59 | 193.00 | . 56 | . 5139340 | 5683 | 864431.30 | 117.22 |
| . 07 | .4780206 | 9264 | 844103.64 | 191.09 | . 57 | . 5144995 | 5627 | $8546 \quad 27.94$ | 116.06 |
| . 08 | . 4789425 | 9173 | 844413.78 | 189.20 | . 58 | . 5150594 | 5571 | $86 \quad 4823.43$ | 114.91 |
| . 09 | . 479 855I | 9082 | 844722.04 | 187.32 | . 59 | .515 6I37 | 5516 | 865017.76 | 113.66 |
| 3.10 | I. 4807588 | 8992 | 845028.43 | 185.47 | 3.60 | I. 5161625 | 5461 | 8652 10.96 | 112.63 |
| . II | .481 6535 | 9903 | 845332.97 | 183.63 | . 65 | . 5167058 | 5406 | 865403.03 | III. 52 |
| . 12 | . 4825393 | 88 I 4 | 845635.69 | 181.81 | . 62 | . 5172438 | 5353 | 865553.99 | I 10.41 |
| . 13 | . 4834164 | 8727 | 845936.59 | 180.00 | . 63 | . 5177764 | 5300 | 865743.85 | 109.3I |
| . 14 | . 4842847 | 8640 | 850235.70 | 178.22 | . 64 | . 5183037 | 5247 | 865932.62 | 108.22 |
| 3.15 | 1.485 1445 | 8555 | 850533.04 | 176.45 | 3.65 | 1. 5188258 | 5195 | 87 O1 20.30 | 107. 15 |
| . 16 | . 4859957 | 8470 | 850828.61 | 174.70 | . 66 | . 5193427 | 5143 | 870306.92 | 106.08 |
| . 17 | . 4868385 | 8386 | 85 II 22.45 | 172.97 | . 67 | . 5198544 | 5092 | 870452.47 | 105.03 |
| . 18 | .4876729 | 8303 | 85 I4 14.56 | 171.26 | . 68 | . 52036 II | 5041 | 870636.98 | 103.99 |
| . 19 | .488 4991 | 822 I | 851704.97 | 169.56 | . 69 | . 5208627 | 4991 | 870820.45 | 102.95 |
| 3.20 | 1.489 3170 | 8139 | 85 19 53.69 | 167.88 | 3.70 | 1.521 3593 | 4942 | 871002.89 | 101.93 |
| . 21 | . 4901269 | 8058 | 85 | 166.21 | . 71 | . 5218511 | 4893 | 87 II 44.31 | 100.92 |
| . 22 | . 4909287 | 7978 | 85 | 164.56 | . 72 | . 5223379 | 4844 | 87 I3 24.73 | 99.91 |
| . 23 | . 4917226 | 7899 | $85 \quad 2809.86$ | 162.93 | . 73 | . 5228199 | 4796 | 87 I5 04.14 | 98.92 |
| . 24 | . 4925085 | 7821 | 853051.99 | 161.32 | . 74 | . 5232971 | 4748 | 871642.57 | 97.94 |
| 3.25 | I. 4932867 | 7743 | $\begin{array}{lllll}85 & 33 & 32.50\end{array}$ | 159.71 | 3.75 | 1.5237695 | 4701 | 871820.02 | 96.96 |
| . 26 | . 4940572 | 7667 | 8536 II. 42 | 158.13 | . 76 | . 5242373 | 4654 | 871956.50 | 96.00 |
| . 27 | . 4948200 | 7590 | $85 \quad 3848.77$ | 156.56 | . 77 | . 5247004 | 4608 | 872132.03 | 95.05 |
| . 28 | . 4955753 | 7515 | 854124.55 | I55.01 | . 78 | . 5251589 | 4562 | 872306.60 | 94.10 |
| . 29 | . 4963231 | 7441 | 854358.79 | 153.47 | . 79 | . 5256128 | 4517 | 872440.23 | 93.17 |
| $3 \cdot 30$ | 1.4970634 | 7367 | 854631.50 | 151.95 | 3.80 | 1.5260622 | 4472 | $\begin{array}{llll}87 & 2612.93\end{array}$ | 92.24 |
| . 31 | . 4977964 | 7294 | 854902.69 | 150.44 | . 8 I | . 5265072 | 4428 | 872744.71 | 91.32 |
| . 32 | . 4985221 | 7221 | 855132.38 | 148.95 | . 82 | . 5269478 | 4384 | 872915.58 | 90.42 |
| . 33 | . 4992407 | 7150 | 855400.59 | 147.47 | . 83 | . 5273839 | 4340 | 873045.55 | 89.52 |
| . 34 | . 499 952I | 7079 | $85 \quad 5627.32$ | 146.00 | . 84 | . 527 8157 | 4297 | 873214.62 | 88.63 |
| 3.35 | I. 5006564 | 7008 | 855852.60 | 144.56 | 3.85 | 1.5282433 | 4254 | 873342.80 | 87.75 |
| . 36 | . 5013537 | 6939 | 86 O1 16.44 | 143. 12 | . 86 | . 5286666 | 4212 | 873510.11 | 86.87 |
| - 37 | . 502 0441 | 6870 | $\begin{array}{lllll}86 & 03 & 38.84\end{array}$ | 141.70 | . 87 | . 5290856 | 4170 | 873636.55 | 86.01 |
| . 38 | . 5027277 | 6802 | $86 \quad 0559.84$ | 140.29 | . 88 | . 5295005 | 4128 | 873802.13 | 85.15 |
| . 39 | . 5034045 | 6734 | $86 \quad 0819.44$ | 138.90 | . 89 | . 529 9113 | 4087 | 873926.86 | 84.31 |
| 3.40 | I. 5040746 | 6667 | 86 10 37.65 | 137.52 | 3.90 | 1.5303180 | 4047 | 874050.75 | 83.47 |
| . 41 | . 5047380 | 6601 | 86 12 54.48 | 136.16 | . 91 | . 5307207 | 4007 | 8742 13.81 | 82.64 |
| .42 | . 5053948 | 6536 | 86 I5 09.96 | 134.80 | . 92 | . 5311193 | 3967 | 874336.03 | 8 I .82 |
| . 43 | . 5060451 | 6471 | 86 I7 24.10 | 133.47 | . 93 | . 5315140 | 3927 | 874457.45 | 8 I .00 |
| . 44 | . 5066889 | 6406 | 86 I9 36.90 | 132.14 | . 94 | . 5319048 | 3888 | 874618.05 | 80.20 |
| 3.45 | I. 5073264 | 6343 | 86 21 48.38 | 130.83 | 3.95 | 1.5322917 | 3850 | $874737.85$ | 79.40 |
| . 46 | . 5079575 | 6280 | $85 \quad 23 \quad 58.56$ | 129.53 | . 96 | . 5326747 | 38II | 874856.85 | 78.61 |
| . 47 | . 5085823 | 6217 | $\begin{array}{llll}85 & 26 & 07.44\end{array}$ | 128.24 | . 97 | . 5330539 | 3773 | 875015.07 | 77.83 |
| . 48 | . 5092010 | 6156 | 8628 I5.05 | 126.97 | . 98 | . 5334294 | 3736 | 875132.52 | 77.06 |
| . 49 | . 509 8135 | 6095 | 863021.39 | 125.71 | . 99 | . 533 80II | 3699 | 875249.19 | 76.29 |
| $3 \cdot 50$ | 1.510 4199 | 6034 | $86 \quad 32 \quad 26.47$ | 124.46 | 4.00 | 1.5341691 | 3662 | 875405.10 | 75.53 |
| u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech u | u | $2 \tan ^{-1}\left(e^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

Smithsonian tables

| $u$ | gdu | $\omega F_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ | $u$ | $\mathrm{gd} \mathbf{u}$ | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |
| 4.00 | 1. 5341691 | 3662 | 875405.10 | 75.53 | 4.50 | 1.5485792 | 2222 | $8843 \quad 37.40$ | 45.82 |
| . 01 | . 5345335 | 3626 | 875520.26 | 74.78 | . 51 | . 5488003 | 2199 | 884422.99 | 45.37 |
| . 02 | . 5348943 | 3590 | 875634.67 | 74.04 | . 52 | - 549 O191 | 2178 | 884508.13 | 44.92 |
| . 03 | . 5352514 | 3554 | 875748.33 | 73.30 | . 53 | . 5492358 | 2I56 | $88 \quad 45 \quad 52.82$ | 44.47 |
| . 04 | . 5356050 | 3518 | 8759 O1. 27 | 72.57 | . 54 | . 5494503 | 2134 | 884637.07 | 44.03 |
| 4.05 | I. 535955 I | 3483 | 880013.48 | 71.85 | $4 \cdot 55$ | 1. 5496627 | 2 II3 | 884720.88 | $43 \cdot 59$ |
| . 06 | . 5363017 | 3449 | 88 OI 24.97 | 71.14 | . 56 | . 5498730 | 2092 | 884804.25 | 43.15 |
| . 07 | . 5366449 | 3415 | 88 02 35.76 | 70.43 | . 57 | . 550 08II | 2071 | 884847.19 | 42.73 |
| . 08 | . 5369846 | 3381 | $\begin{array}{llllllllll}88 & 03 & 45.83\end{array}$ | 69.73 | . 58 | . 5502873 | 205I | 884929.70 | 42.30 |
| . 09 | . 5373210 | 3347 | 880455.22 | 69.03 | . 59 | . 5504913 | 2030 | 8850 II. 79 | 41.88 |
| 4.10 | I. 5376540 | 3314 | 880603.91 | 68.35 | 4.60 | 1. 5506933 | 2010 | 885053.46 | 41.46 |
| . II | . 5379837 | 328 I | 8807 II.91 | 67.67 | . 61 | . 5508933 | 1990 | 885134.72 | 4 I .05 |
| . 12 | . 5383102 | 3248 | 880819.25 | 67.00 | . 62 | .551 0914 | 1970 | 885215.56 | 40.64 |
| . I3 | . 5386333 | 3216 | 880925.91 | 65.33 | . 63 | . 5512874 | 1951 | 885256.00 | 40.24 |
| . 14 | . 5389533 | 3184 | 88 10 31.91 | 65.67 | . 64 | -55I 48I5 | 193I | 885336.04 | 39.84 |
| 4.15 | I. 5392701 | 3152 | 88 II 37.25 | 65.02 | 4.65 | I.551 6737 | 1912 | 885415.68 | 39.44 |
| . 16 | . 5395837 | 312 I | 881241.94 | 64.37 | . 66 | -5518640 | 1893 | $88 \quad 5454.92$ | 39.05 |
| . 17 | . 5398943 | 3090 | 88 I3 45.99 | 63.73 | . 67 | . 5520523 | 1874 | $88 \quad 5533.77$ | 38.66 |
| . 18 | . 5402017 | 3059 | 88 I4 49.40 | 63.10 | . 68 | . 5522388 | 1856 |  | 38.28 |
| . 19 | . 540 506I | 3029 | 88 I5 52.19 | 62.47 | . 69 | . 5524235 | 1837 | 885650.33 | 37.89 |
| 4.20 | I. 5408074 | 2998 | 88 16 54.34 | 6 x .85 | $4 \cdot 70$ | 1.552 6063 | 19 | $88 \quad 5728.03$ | $37 \cdot 52$ |
| . 2 I | . 5411058 | 2969 | 88 I7 55.88 | 61.23 | . 71 | . 5527873 | 1801 | $88 \quad 58 \quad 05.36$ | 37.14 |
| . 22 | . 5414012 | 2939 | 88 18 56.81 | 60.62 | . 72 | . 5529664 | 1783 | 885842.32 | 36.77 |
| . 23 | . 5416936 | 2910 | 881957.13 | 60.02 | . 73 | - 5531438 | 1765 | 8859 18.91 | 36.41 |
| . 24 | . 54 I 983 I | 288I | $88 \quad 2056.85$ | 59.42 | -74 | . 5533195 | 1748 | 8859 55.14 | 36.05 |
| 4.25 | 1. 5422698 | 2852 | 88 21 55.98 | ${ }^{58} 8.83$ | 4.75 | I. 5534934 | 1730 | 890031.01 | 35.69 |
| . 26 | . 5425536 | 2824 | 8812254.52 | 58.25 | . 76 | . 5536655 | 1713 | 89 O1 06.52 | 35.33 |
| . 27 | . 5428346 | 2796 | 882352.48 | 57.67 | -77 | . 5538360 | 1696 | 89 о1 41. 68 | 34.98 |
| . 28 | . 5431128 | 2768 | 882449.86 | 57.09 | . 78 | . 5540047 | 1679 | 890216.48 | 34.63 |
| . 29 | . 5433882 | 2741 | 882546.67 | 56.53 | . 79 | . 5541718 | 1662 | 890250.94 | 34.29 |
| $4 \cdot 30$ | 1. 5436609 | 2713 | $88 \quad 26.42 .91$ | 55.96 | 4.80 | 1.554 3372 | 1646 | 890325.06 | 33.95 |
| . 31 | . 5439308 | 2686 | 8812738.60 | 55.41 | .8I | . 5545010 | 1630 | 890358.84 | 33.61 |
| . 32 | . 544 198i | 2660 | 80 | 54.86 | . 82 | . 5546631 | 1613 | 890432.28 | 33.28 |
| . 33 | . 5444628 | 2633 | 882928.31 | 54.3 I | . 83 | . 5548236 | 1597 | 890505.39 | 32.94 |
| - 34 | . 5447247 | 2607 | $88 \quad 3022.35$ | 53.77 | . 84 | - 5549825 | 1581 | 890538.17 | 32.62 |
| 4.35 | I. 544984 I | 2581 | 883115.85 | 53.24 | 4.85 | I.555 I399 | 1566 | 890610.63 | 32.29 |
| . 36 | . 5452409 | 2555 | $88 \quad 3208.82$ | 52.71 | . 86 | . 5552957 | 1550 | 890642.76 | 31.97 |
| . 37 | . 545 49521 | 2530 | 8833101.27 | 52.18 | . 87 | . 5554499 | 1535 | 890714.57 | 31.65 |
| . 38 | . 5457469 | 2505 | 88 | 51.66 | . 88 | . 5556026 | 1519 | 890746.07 | 31.34 |
| . 39 | . 545996 I | 2480 | $883444 \cdot 59$ | 51.15 | . 89 | . 5557538 | 1504 | 890817.25 | 31.03 |
| 4.40 | 1.5462429 | 2455 | $\begin{array}{llll}88 & 35 & 35.49 \\ 88 & 36 & \end{array}$ | 50.64 | 4.90 | 1.5559034 | 1489 | 890848.12 | 30.72 |
| . 41 | . 5464872 | 243 I | $\begin{array}{lllll}88 & 36 & 25.88 \\ 88 & 37 & \end{array}$ | 50.14 | . 91 | . 5560516 | 1474 | 890918.69 | 30.41 |
| . 42 | . 5467290 | 2407 | 88 37 1.5 .76 <br> 88 38  | 49.64 | - 92 | . 5561983 | 1460 | 890948.95 | 30.11 |
| . 43 | . 5469585 | 2383 | $\begin{array}{llllllllllllll}88 & 38 & 05.15\end{array}$ | 49.14 | . 93 | . 5563436 | 1445 | 89 10 18.91 | 29.81 |
| . 44 | . 5472055 | 2359 | 8838 54.05 | 48.65 | . 94 | . 5564874 | 1431 | 891048.57 | 29.51 |
| 4.45 | 1.5474403 | 2335 | $\begin{array}{llll}88 & 39 & 42.46\end{array}$ | 48.17 | 4.95 | 1. 5566297 | 1417 | 89 II 17.93 | 29.22 |
| . 46 | . 5476726 | 2312 | 884030.40 | 47.69 | . 96 | . 5567707 | 1403 | 89 II 47.01 | 28.93 |
| . 47 | . $547 \mathrm{CO27}$ | 2289 | 884117.85 | 47.22 | . 97 | . 5569103 | 1389 | 89 12 15.79 | 28.64 |
| . 48 | -548 1305 | 2266 | 884204.83 | 46.75 | . 98 | . 5570484 | 1375 | 89 I2 44.29 | 28.36 |
| . 49 | . 5483560 | 2244 | $88 \quad 42$ 51. 35 | 46.28 | . 99 | . 5571852 | 1361 | 891312.51 | 28.07 |
| 4.50 | 1.5485792 | 2222 | $88 \quad 43 \quad 37.40$ | 45.82 | 5.00 | 1.5573206 | 1348 | 891340.44 | 27.79 |
| u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | $\omega$ sech $u$ | u | $2 \tan ^{-1}\left(\mathrm{e}^{u}\right)-\frac{\pi}{2}$ | $\omega$ sech u | $2 \tan ^{-1}\left(e^{u}\right)-90^{\circ}$ | $\omega$ sech u |

The Gudermannian.

| $u$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | u | gd u | $\omega \mathrm{F}_{0}{ }^{\prime}$ | gd u | $\omega F_{0}{ }^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 5.00 | I. 5573206 | 1348 | $89^{\circ} 133^{\prime} 40.14$ | 27.79 | 5.50 | 1. 5626228 | 817 | 893154.10 |  |
| . 11 | - 5574547. | 1334 | 891408.10 | 27.52 | . 51 | . $56270+2$ | 809 | 893210.87 | 16.69 |
| . 02 | . $5575875^{\circ}$ | 1321 | 891435.48 | 27.24 | . 52 | . 5627847 | 801 | 893227.48 | 16.53 |
| . 03 | -5577189 | 1308 | 891502.58 | 26.97 | . 53 | . 5628644 | 793 | 893243.92 | 16.36 |
| . 04 | . 5578490 | 1295 | 891529.42 | 26.71 | . 54 | . 5629433 | 785 | 893300.20 | 16.20 |
| 5.05 | 1. 5579778 | 1282 | 891556.00 | 26.44 | 5.55 | 1.5630215 | 777 | 893316.32 | 16.04 |
| . 06 | . 5581054 | 1269 | 891622.30 | 26.18 | . 56 | . 5630988 | 770 | 893332.27 | 15.88 |
| . 07 | . 5582317 | 1256 | 891648.35 | 25.92 | . 57 | . 5631754 | 762 | 893348.07 | 15.72 |
| . 08 | . 5583567 | 1244 | 891714.14 | 25.66 | . 58 | . 5632512 | 755 | 893403.71 | 15.56 |
| . 09 | . 5584804 | 1232 | 891739.67 | 25.40 | . 59 | . 5633263 | 747 | 893419.20 | 15.41 |
| 5.10 | 1. 5586030 | 1219 | 891804.94 | 25.15 | 5.60 | 1. 5634006 | 740 | $893434 \cdot 53$ | 15.25 |
| . 11 | -558 7243 | 1207 | 891829.97 | 24.90 | . 61 | . 5634742 | 732 | 893449.7 I | 15.10 |
| . 12 | . 5588444 | 1195 | 89 18 54.74 | 24.65 | . 62 | . 563547 I | 725 | 893504.73 | 14.95 |
| . 13 | . 5589633 | 1183 | 891919.27 | 24.41 | . 63 | . 5636192 | 718 | 893519.61 | 14.80 |
| . 14 | . 559 08II | 1172 | 891943.56 | 24.16 | . 64 | . 5636906 | 711 | 893534.34 | 14.66 |
| 5.15 | 1.559 1976 | 1160 | 892007.60 | 23.92 | 5.65 | 1.5637613 | 703 | 893548.93 | 14.51 |
| . 16 | - 559 313I | 1148 | 892031.40 | 23.69 | . 66 | . 5638313 | 697 | 893603.36 | 14.37 |
| -17 | - 5594273 | 1137 | 892054.97 | 23.45 | . 67 | . 5639006 | 690 | 893617.66 | 14.22 |
| . 18 | . 5595404 | 1126 | 892118.31 | 23.22 | . 68 | . 5639692 | 683 | 893631.81 | 14.08 |
| . 19 | . 5596524 | 1114 | 89 2I 41.41 | 22.99 | . 69 | . 5640372 | 676 | 893645.82 | 13.94 |
| 5.20 | 1.5597633 | 1103 | 892204.28 | 22.76 | 5.70 | 1.5641044 | 669 | 893659.70 | 13.80 |
| . 2 | . 559873 I | 1092 | 892226.92 | 22.53 | . 71 | . 5641710 | 663 | 893713.43 | 13.67 |
| . 22 | . 5599818 | 1081 | 892249.34 | 22.31 | . 72 | . 5642369 | 656 | 893727.03 | I3.53 |
| . 23 | . 5600894 | 1071 | 8923 II. 53 | 22.08 | . 73 | . 5643022 | 649 | 893740.49 | 13.40 |
| . 24 | . 5601959 | 1060 | 8923 33.51I | 21.86 | . 74 | . 5643668 | 643 | 893753.82 | 13.26 |
| 5.25 | 1.5603014 | 1049 | 892355.26 | 21.65 | 5.75 | 1. 5644308 | 637 | 893807.01 | 13.13 |
| . 26 | . 5604058 | 1039 | 892416.80 | 21.43 | . 76 | . 564494 I | 630 | 893820.08 | 13.00 |
| . 27 | . 5605092 | 1029 | 8924 38.13 | 2 I . | . 77 | . 5645568 | 624 | 893833.01 | 12.87 |
| . 28 | . 5606116 | 1018 | 892459.24 | 21.01 | . 78 | . 5646189 | 618 | 893845.82 | 12.74 |
| . 29 | . 5607129 | 1008 | 8925 20.14 | 20.80 | . 79 | . 5646804 | 612 | 893858.50 | 12.61 |
| $5 \cdot 30$ | 1.5608132 | 998 | 892540.84 | 20.59 | 5.80 | 1.5647412 | 606 | 893911.05 | 12.49 |
| -3.1 | . 5609126 | 988 | 8926 O1. 33 | 20.39 | . 8 I | . 5648015 | 599 | 893923.48 | 12.37 |
| . 32 | . 5610109 | 979 | 8926 21.61 | 20.18 | . 82 | . 564861 I | 504 | 893935.78 | 12.24 |
| - 33 | . 5611083 | 969 | 892641.69 | 19.98 | . 83 | . 5649202 | 588 | 893947.96 | 12.12 |
| . 34 | . 5612047 | 959 | 8927 OI. 58 | 19.78 | . 84 | . 5649787 | 582 | 894000.02 | 12.00 |
| $5 \cdot 35$ | 1.5613001 | 950 | 892721.26 | 19.59 | 5.85 | 1. 5650365 | 576 | 8940 II. 96 | 11.88 |
| . 36 | . 5613946 | 940 | 892740.75 | 19.39 | . 86 | . 5650939 | 570 | $8940 \quad 23.78$ | I 1.76 |
| . 37 | .56I 488 I | 931 | 892800.05 | 19.20 | . 87 | . 5651506 | 565 | 894035.48 | 11.65 |
| . 38 | .561 5807 | 922 | 892819.15 | 19.01 | . 88 | . 5652068 | 559 | 894047.07 | 11.53 |
| . 39 | .561 6724 | 912 | 892838.06 | 18.82 | . 89 | . 5652624 | 553 | 894058.54 | H. 41 |
| 5.40 | 1.561 7632 | 903 | 892856.79 | 18.63 | 5.90 | 1. 5653175 | 548 | 894109.90 | 11.30 |
| .41 | . 561853 I | 894 | 892915.33 | 18.45 | .91 | . 5653720 | 542 | 894121.15 | 11. 19 |
| . 42 | . 5619421 | 885 | 892933.68 | 18.26 | . 92 | . 5654259 | 537 | 894132.28 | 11.08 |
| . 43 | . 5620302 | 877 | 8929 5II. 85 | 18.08 | . 93 | . 5654794 | 532 | 894143.30 | 10.97 |
| . 44 | . 5621174 | 868 | 893009.85 | 17.90 | . 94 | . 5655323 | 526 | 894 II 54.2 I | 10.86 |
| 5.45 | 1.5622038 | 859 | 893027.66 | 17.72 | 5.95 |  | 521 |  |  |
| . 46 | . 5622893 | 85 I | 893045.29 | 17.55 | . 96 | . 5656365 | 516 | 894215.71 | 10.64 |
| . 47 | .5623739 | 842 | 893102.75 | 17.37 | . 97 | . 5656879 | 511 | 894226.30 | 10.54 |
| . 48 | .5624577 | 834 | 893120.04 | 17.20 | . 98 | . 5657387 | 506 | 894236.79 | 10.43 |
| . 49 | . 5625407 | 826 | 893137.15 | 17.03 | . 99 | . 5657890 | 501 | 894247.17 | 10.33 |
| 5.50 | 1.5626228 | 817 | 893154.10 | 16.86 | 6.00 | 1.5658388 | 496 | 894257.44 | 10.23 |
| $u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | sech u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | ${ }_{\text {wech u }}$ | u | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-\frac{\pi}{2}$ | ${ }^{\omega} \operatorname{sech} u$ | $2 \tan ^{-1}\left(\mathrm{e}^{\mathrm{u}}\right)-90^{\circ}$ | w sech u |

Smithsonian tables

## TABLE VII

## THE ANTI=GUDERMANNIAN

m expressed in minutes in terms of the Gudermannian, gd $u$ expressed in degrees and minutes. I minute $=0.00029088821$ radians,
$0.0002908882 \mathrm{Im}=\log _{\mathrm{e}} \tan \left(\frac{\mathrm{I}}{4} \pi+\frac{\mathrm{I}}{2} \operatorname{gdu}\right)=\mathrm{u}$ radians.
In this table the second decimal place is sometimes erroneous by a unit.

The Anti-Gudermannian.

| gd u | $0^{\circ}$ | $\mathrm{I}^{\circ}$ | $2^{\circ}$ | $3^{\circ}$ | $4^{\circ}$ | $5^{\circ}$ | $6^{\circ}$ | $7^{\circ}$ | $8^{\circ}$ | $9^{\circ}$ | $10^{\circ}$ | gdu |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}^{\prime}$ | 0'.00 | 60.00 | 120.02 | $\overline{180.08}$ | 240.19 | $\overline{300.38}$ | 360.66 | 421.05 | 48 I .57 | 542.23 | 603.07 | $\mathrm{o}^{\prime}$ |
| 1 | 1.00 | 61.00 | 121.02 | 181.08 | 241.20 | 301.38 | 361.66 | 422.06 | 482.58 | 543.25 | 604.08 | 1 |
| 2 | 2.00 | 62.00 | 122.03 | 182.08 | 242.20 | 302.39 | 362.67 | 423.06 | 483.59 | 544.26 | 605.10 | 2 |
| 3 | 3.00 | 63.00 | 123.03 | 183.09 | 243.20 | 303.39 | 363.67 | 424.07 | 484.60 | 545.27 | 606.12 |  |
| 4 | 4.00 | 64.00 | 124.03 | 184.09 | 244.20 | 304.40 | 364.68 | 425.08 | 485.61 | 546.28 | 607.13 | 4 |
| 5 | 5.00 | 65.00 | 125.03 | 185.09 | 245.21 | 3105.40 | 365.69 | 426.09 | 486.62 | 547.30 | 608.15 | 5 |
| 6 | 6.00 | 66.00 | 126.03 | 186.09 | 246.21 | 306.40 | 366.69 | 427.09 | 487.63 | 548.31 | 609.16 | 6 |
| 7 | 7.00 | 67.00 | 127.03 | 187.09 | 247.21 | 307.41 | 367.70 | 428.10 | 488.64 | 549.32 | 6ro. 18 | 7 |
| 8 | 8.00 | 68.00 | 128.03 | 188.09 | 248.21 | 308.41 | 368.70 | 429.11 | 489.65 | 550.34 | 6ir.19 | 8 |
| 9 | 9.00 | 69.0 | 129.03 | 189.09 | 249. | 309.42 | 369.71 | 430.12 | 490.66 | 551.35 | 612.21 | 9 |
| 10 | 10.00 | 70 | 130.03 | 190.10 | 250. | 310.42 | 370.72 | 431.13 | 491.67 | 552.36 | 613.23 | 10 |
| II | 11.00 | 71.0 | 131.03 | I91. 10 | 251.22 | 311.42 | 371.72 | 432.13 | 492.68 | 553.37 |  | II |
| 12 | 12. | 72.00 | 132.03 | 192. 10 | 252.23 | 312.43 | 372.73 | 433. 14 | 493.69 | 554.39 |  | 12 |
| ${ }^{1} 3$ | 13.00 | 73.00 | 133.03 | 193.10 | 253.23 | 313.43 | 373.74 | 434. 5 | 494.70 | 555.40 | 616.27 | I3 |
| 14 | 14.00 | 74.01 | 134.031 | 194. 10 | 254.23 | 314.44 | 374.74 | 435. 16 | 495.71 | 556.41 | 617.29 | I4 |
| 15 | 15.00 | 75.01 | 135.03 | 195.10 | 255.23 | 315.44 | 375.75 | 436.17 | 496.72 | 557.43 | 618.31 | 15 |
| 16 | 16.00 | 76.01 | 136.03 | 196. 11 | 256.24 | 316.45 | B76.75 | 437.17 | 497.73 | 558.44 | 619.32 | 16 |
| 17 | 17.00 | 77.01 | 137.04 | 197.11 | 257.24 | 317.45 | 377.76 | 438.18 | 498.74 | 559.45 | 620.34 | 17 |
| 18. | 18.0 | 78.01 | 138.04 | 198. II | 258.24 | 318.45 | 378.76 | 439.19 | 499.75 | 560.47 | 621.36 | 18 |
| 19 | 19.00 | 79.01 | 139.04 | 199. II | 259.25 | 319.46 | 379.77 | 440.20 | 500.76 | 561.48 | 622.37 | 19 |
| 20 | 20.00 | 80.01 | 140.04 | 200.11 | 260.25 | 320.46 | 380.78 | 441 | 501.77 | 562.49 | 623.39 | 20 |
| 21 | 21.00 | 8 Br .01 | 141.04 | 201. II | 261.25 | 321.47 | 381.78 | 442.21 | 502.78 | 563.51 | 624.40 | 2 I |
| 22 | 22.00 | 82.01 | 142.04 | 202.12 | 262.25 | 322.47 | 382.79 | 4 | 503.79 | 564.52 | 625.42 | 22 |
| 23 | 23.00 | 83.01 | 143.04 | 203.12 | 263.26 | 323.48 | 383.79 | 444.23 | 504.80 | 505.53 | 626.44 | 23 |
| 24 | 24.00 | 84.01 | 144.04 | 204. 12 | 264.26 | 324.48 | 384.80 | 445.24 | 505.81 | 566.55 | 627.45 | 24 |
| 25 | 25.00 | 85.01 | 145.04 | 205.12 | 265.26 | 325.48 | 385.81 | 446.25 | 506.83 | 567.56 | 628.47 | 25 |
| 26 | 26.00 | 86.0I | 146.04 | 206. 12 | 266.27 | 326.49 | 386.8I | 447.26 |  | 568.57 | 629.49 | 26 |
| 28 | 27.00 | 87.01 | 147.04 | 207.13 | 267.27 | 327.49 | 387.82 | 448.26 | 508.85 | 569.59 | 630.50 | 27 |
| 28 | 28.00 | 88.01 | 148.05 | 208.13 | 268.27 | 328.50 | 388.83 | 449.27 | 509.86 | 570.60 | 631.52 | 28 |
| 29 | 29.00 | 89.01 | 149.05 | 209.13 | 269.27 | 329.50 | 389.83 | 450.28 | 5110.87 | 571.62 | 6312.54 | 29 |
| 30 | 30.00 | 90.01 | 150.05 | 210.13 | 270. | 330.51 | 390.84 | 451.29 | 511.88 | 572.63 | 633.56 | 30 |
| 31 | 31 | 9 I .01 | 151.05 | 211.131 | 271.28 | 331.517 | 391.85 | 452.30 | 512.89 | 573.64 | 634.57 | 31 |
| 32 | 32 | 92.01 | 152.05 | 212.13 | 272.28 | 332.52 | 392.85 | 453.31 | 513.90 | 574.66 | 635.59 | 32 |
| 33 | 33.00 | 93.01 | 153.05 | 213.14 | 273.29 | 333.52 | 393.86 | 454.32 | 514.91 | 575.67 | 636.61 | 33 |
| 134 | 34.00 | 94.01 | 154.05 | 2I4. 14 | 274.29 | 334.53 | 354.86 | 455.33 | 515.93 | 576.69 | 637.62 | 34 |
| 35 | 35.00 | 95.01 | 155.05 | 215.14 | 275.29 | 335.53 | 395.87 | 456.33 | 516.94 | 577.70 | 638.64 | 35 |
| 36 | 36.00 | 96.01 | 156.05 | 216.14 | 276.30 | 336.54 | 395.88 | 457.34 | 517.95 | 578.71 | 639.66 | 36 |
| 37 | 37.00 | 97.01 | 157.05 | 217.14 | 277.30 | 337.54 | 397.88 | 458.35 | 518.96 | 579.73 | 640.68 | 37 |
| 38 | 38.00 | 98.01 | 158.06 | 218.15 | 278.30 | 338.55 | 398.89 | 459.36 | 519.97 | 580.74 | 641.69 | 38 |
| 39 | 39.00 | 99.01 | I59.06 | 219.15 | 279.31 | 339.55 | 399.90 | 460.37 | 520.98 | 581.76 | 642.71 | 39 |
| 40 | 40.00 | 10 | 160.06 | 220.15 | 280.31 | 340.56 | 400.91 | 461.38 | 521.99 | 582.77 | 643.73 | 40 |
| 4 I | 41.00 | IOI. OI | 161.06 | 221.15 | 281.31 | 341.56 | 401.9I | 462.39 | 523.01 | 583.79 | 644.75 | 4 I |
| 42 | 42.00 | 102.01 | 162.06 | 222.15 | 282.32 | 342.57 | 402.92 | 463.40 | 524.02 | 58.80 | 645.76 | 42 |
| 43 | 43.00 | 103.02 | 163.06 | 223.16 | 283.32 | 343.57 | 403.93 | 464.4 I | 525.03 | 585.81 | 646.78 | 43 |
| 44 | 44.00 | 104.02 | I64.06 | 224.16 | 284.32 | 344.58 | 404.93 | 465.41 | 526.04 | 586.83 |  | 44 |
| 45 | 45. | 105.02 | 165.06 | 225.16 | 285.33 | 345.58 | 405.94 | 466.42 | 527.05 | 587.84 | 648.821 | 45 |
| 46 | 46.00 | 106.02 | 166.06 | 226.16 | 286.33 | 346.59 | 406.95 | 467.43 | 528.06 | 588.86 | 649.84 | 46 |
| 47 | 47.00 | 107.02 | 167.07 | 227.16 | 287.33 | 347.59 | 407.95 | 468.44 | 529.08 | 589.87 | 650.85 | 47 |
| 48 | 48.00 | 108.02 | 168.07 | 228. 17 | 288.34 | 348.60 | 408.96 | 469.45 | 530.09 | 590.89 | 651.87 | 48 |
| 49 | 49.00 | 109.02 | 169.07 | 229.17 | 1289.34 | 349.60 | 409.97 | 470.46 | 531.10 | 591.90 | 652.89 | 49 |
| 50 | 50.00 | 110.02 | 170.07 | 230.17 | 290.34 | 350.61 | 410.97 | 47 I .47 | 532:1 | 592.92 | 653.91 | 50 |
| 51 | 51.00 | ITI. 02 | 171.07 | 231.17 | 291.35 | 351.6 I | 411.98 | 472.48 | 533.12 | 593.93 | 654.93 | 51 |
| 52 | 52.00 | 112.02 | 172.07 | 232.18 | 292.35 | 352.62 | 412.99 | 473.49 | 534.14 | 594.95 | 655.94 | 52 |
| 53 | 53.00 | 113.02 | 173.07 | 233.18 | 293.35 | 353.62 | 414.00 | 474.50 | 535.15 | 595.96 | 656.96 | 53 |
| 54 | 54.00 | 114.02 | 174.07 | 234.18 | 294.36 | 354.63 | 415.00 | 475.51 | 536.16 | 596.98 | 657.98 | 54 |
| 55 | 55.00 | 115.02 | 175.07 | 235. | 295.36 | 355.63 | 416.01 | 476.52 | 537.17 | 597.99 | 659.00 | 55 |
| 56 | 56.00 | 116.02 | 176.08 | 236.18 | 296.37 | 356.64 | 417.02 | 477.53 | 538.18 | 599.01 | 660.02 | 56 |
| 57 | 57.00 | 117.02 | 177.08 | 237.19 | 297.37 | 357.64 | 418.03 | 478.54 | 539.20 | 600.02 | 661.04 | 57 |
| 58 | 58.00 | 118.02 | 178.08 | 238.19 | 298.37 | 358.65 | 419.03 | 479.55 480.56 | 540.21 | 601.04 602.05 | 662.05 663.07 | 58 |
| 59 60 | 59.00 60.00 | 119.02 120.02 | 179.08 180.08 | 239.19 240.19 | 299.38 300.38 | 359.65 360.66 | 420.04 | 480.56 | 541.22 542.23 | 602.05 603.07 | 663.07 664.09 | 59 |

The Anti-Gudermannian.

| gd u | $1 \mathrm{I}^{\circ}$ | $12^{\circ}$ | $13^{\circ}$ | $14^{\circ}$ | $15^{\circ}$ | 16 | $17^{\circ}$ | $18{ }^{\circ}$ | - | $20^{\circ}$ | du |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{\prime}$ | $664 \prime .09$ | 725.32 | 786.78 | 848.49 | 910.46 | 972.73 | $1035 \cdot 30$ | 1098.22 | 1161.49 | 1225.14 | $0^{\prime}$ |
| I | 665 | 726.34 | 787.81 |  | 9II. 50 |  | 1036.35 | 1099.27 | I 162.54 | 1226.20 |  |
| 2 | 666.13 | 727.37 | 788.83 | 850.55 | 912.53 | 974.8 I | 1037.40 | 1100.32 | 1163.60 | 1227.27 | 2 |
| 3 | 667.15 | 728.39 | 789.86 |  | 913.57 | 975.85 | 1038.44 | IIOI. 37 | II64.66 | I228.33 | 3 |
| 4 | 668.17 | 729.41 | 790.89 | 852.61 | 914.60 | 976.89 | 1039.49 | 1102.42 | I 165.72 | 1229.40 | 4 |
| 5 | 669.19 | 730.43 | 791.91 | 853.64 | 915.64 | 977.93 | 1040.53 | I'IO3.47 | I 166.78 | 1230.46 | 5 |
| 6 |  | 73 | 792 | 85 | 916.67 | 978.97 | 1041.58 | 1104.53 | 1167.83 | 123I. 53 | 6 |
| 7 |  | 732.48 | 793.97 |  | 917.71 | 980.01 | 1042.63 | r105.58 | 1168.89 | 1232.59 | 7 |
| 8 | 672. | 733.5 | 794.99 | 856.73 | 918.75 | 981.05 | 1043.67 |  | I 169.95 | 1233.66 | 8 |
| 9 | 673.2 | 734 | 796.02 |  | gl9. | 982.09 | 1044.72 | I 107.68 | 1171.01 | 1234.72 | 9 |
| IO | 674. | 735 | 797.04 |  | 920.82 | 983.13 | 1045.77 | I 108.74 | 1172.07 | 1235.79 | 10 |
| II |  |  |  |  |  |  | 1046.8 I | 1109.79 | I173.13 | 1236.85 | II |
| 12 | 676.3 | 737.59 | 799.10 | 860.8 | 922.89 | 985.22 | 1047.86 | IIIIO. 84 | II74.19 | 1237.92 | 12 |
| 13 |  | 738.62 | 800.13 | 861.89 | 923.93 | 986. 26 | 1048 | IIII. 89 | I175.24 | 1238.98 | I3 |
| 14 | 678.3 | 739.64 | 80 I .15 | 852.92 | 924.96 |  | 1049.95 | III 12.95 | 1176.30 | 1240.05 | 14 |
| I'5 | 679.38 | 740 | 802. 18 |  | 926.00 | 988.34 | 1051.00 | 1114.00 | II77.36 | I24I. II | I5 |
| 16 | 68 | 74 |  |  | 927.03 |  | 1052.05 | III5.05 | 1178.42 | 1242. 18 | 16 |
| 17 | 681.4 | 7422.71 | 804.24 | 856.02 | 928.07 | 990.42 | IO53.09 | III6. I' | I I79.48 | 1243.25 | 17 |
| I8 | 682.44 | 743.73 | 805.26 | 857.05 | 929.11 | 991 | IO54. I4 | I I'I7 | II80.54 | 1244.31 | 18 |
| 19 | 683.46 | 744.76 | 806.29 | 868.08 | 93 | 992.5 I | 1055 | III8.21 | 1181.60 | 1245.38 | 19 |
| 20 | 684.48 | 745.78 | 807.32 | 869.11 | 93 I .1 | 993.55 | 1056.24 | I I I 19.27 | 1182.66 | 1246.44 | 20 |
| 21 | 685 | 746.8 I | 808.35 | 870.14 | 932.22 |  | 1057.28 | I 120.32 | 1183.72 |  | 2 I |
| 22 | 686.5 | 747.83 | 809.37 | 871.18 | 933.26 |  |  | 112 | 1184.78 |  | 22 |
| 23 | 687.5 | 748.85 | 8 IO .40 | 872.21 | 934.29 | 996 | 1059 | I 122.4 |  | 1249.64 | 23 |
| 24 | 688.56 | 749.8 | 811.43 | 873.24 | 935.33 | 997.72 |  | II 213.48 | I I86.90 | 1250.71 | 24 |
| 25 | 689.58 | 750 | 812.46 | 874.27 | 936.37 | 998.76 | 106I. 48 | I 124.53 | 1187.96 | 1251.78 | 25 |
| 26 |  | 75 |  |  |  |  |  |  | 1189.02 |  | 26 |
| 27 | 691.62 | 752.9 | 814 | 876.3 | 938.44 | 1000.8 |  | II | 1190.08 | 1253.91 | 27 |
| 28 | 692.64 | 753.97 | 8 I 5.54 | 877.37 | 939.48 | IOOI .8 | 1064.62 | II2 | 119 | 1254.98 | 28 |
| 29 |  | 755 | 816.57 | 878.40 | 940.52 | 100 |  | I 128.75 | 1192.20 | 1256.05 | 29 |
| 30 |  |  |  | 879.4 | 94.56 | 1003.97 | 1066.72 | 1129.81 | 1193.26 | 1257.12 | 30 |
| 3 I |  | 757.05 |  | 880.4 | 942.59 | I005.02 |  | I'I30.86 |  | 1258.18 | 3 I |
| 32 |  |  | 819.66 | 881. 50 | 943.63 | 1005 | 1068.8 I | II3I.92 | I195.39 | I259.25 | 32 |
| 33 |  | 759.09 | 820.69 | 882.5 | 944.67 | 1007.10 | 1069.86 | 1132.97 | I 196.45 | 1260.32 | 33 |
| 34 | 698.76 | 760.12 | 821.71 | 883.57 | 945.71 | 1008. I5 | 1070.91 | I 34.0 | I197.51 | 1261.39 | 34 |
| 35 | 699.78 | 761.14 | 822.74 | 884.60 | 946.74 | I009. I9 | 1071.96 | I I 35.08 | 1198.57 | 1262.45 | 35 |
| 36 | 700.80 | 762.17 |  | 885.64 | 947.78 | IOTO. 23 | 1073.01 | II36.14 | II99.63 | 1263.52 | 36 |
| 37 | 701.82 | 763.19 | 824.80 | 886.67 | 948.82 | IOII. 28 | 1074.06 | 1137.19 | 1200.69 | 1264.59 | 37 |
| 38 | 702.85 | 764.22 |  | 887.70 | 949.86 | IOI2. 32 | 1075 | 1138.25 | 1201.75 |  | 38 |
| 39 | 703.87 | 765.24 | 826.85 | 888.74 | 950.9 | 1013.36 | 1076. 16 | 1139.30 | 1202.82 | 1266.73 | 39 |
| 40 | 704.89 | 766.27 | 827.89 | 889.77 | 951.94 | IOI4.4T | 1077.21 | 1140.36 | 1203.88 | 1267.80 | 40 |
| 4 |  |  | 828.92 | 890.80 | 952.98 | IOI 5.45 | 1078.26 | II4I.4I | 1204.94 | 1268.87 | 4 I |
| 42 | 706.93 | 768.32 | 829.95 | 891.84 | 954.01 | IOI6. 50 | 1079.31 | II 42.47 | 1206.00 | 1269.93 | 42 |
| 43 | 707.95 | 769.34 | 830.98 | 892.87 | 955.05 | IOI7. 5 | 1080.36 | I 143.52 | 1207.06 | 1271.00 | 43 |
| 44 | 708.97 | 770.37 | 832.00 | 893.91 | 956.09 | IOI8. 58 | 108I. 41 | I I 44.58 | 1208. I3 | 1272.07 | 44 |
| 45 | 709 | 771.39 | 833.03 | 894.9 | 957.13 | 1019.63 | 1082.46 | I 145.64 | 1209. 19 | 1273.14 | 45 |
| 46 | 711.02 |  |  | 895.97 | 958.17 | 1020.67 | 1083.51 | II 46.69 | I210. 25 | 1274.21 | 46 |
| 47 | 712.04 | 773.44 | 835.09 | 897.01 | 959.21 | 1021.72 | 1084.56 | I I 47.75 | 1211.3I | 1275.28 | 47 |
| 48 | 713.06 | 774.47 | 836.12 | 898.04 | 960.25 | 1022.76 | 1085.61 | II48.80 | 1212.38 | 1276.35 | 48 |
| 49 | 714.08 |  | 837.15 | 899.0 | 961.29 | 1023.81 | 1086.66 | I I 49.86 | 1213.44 | 1277.42 | 49 |
| 50 | 715 | 776.52 | 838.18 | 900. II | 962.33 | 1024.85 | 1087.71 | 1150.92 | 1214.50 | 1278.49 | 50 |
| 51 | 716.12 | 777.54 | 839.21 |  | 963.37 | 1025.90 |  | 1151.97 | 1215.57 | 1279.56 | 51 |
| '52 | 717. I'5 | 778.57 | 840.24 | 902.18 | 964.41 | 1026.94 | 1089.81 | 1153.03 | 1216.63 | 1280.63 | 52 |
| 53 | 718.17 | 779.59 | 841.27 | 903.22 | 955.45 | 1027.99 | 1090.86 | I 154.09 | 1217.69 | 1281.70 | 53 |
| $54^{\prime}$ | 719.19 | 780.62 | 842.30 | 904.25 | 966.49 | 1029.03 | 109'I . 91 | II55.14 | 1218.76 | 1282.77 | 54 |
| 55 | 720.21 | 781.65 | 843.33 | 905.28 | 957.53 | 1030.08 | I092.96 | 1156.20 | 1219.82 | 1283.84 | 55 |
| 56 | 721.23 | 782.67 | 844.36 | 906.32 | 968.57 | 1031. 12 | IO94.01 | II 57.26 | 1220.88 | 1284.91 | 56 |
| 57 | 722.26 | 783.70 | 845.39 | 907.35 | 969.6 I | 1032.17 | 1095.06 | I I'58.32 | 1221.95 | 1285.98 | 57 |
| 58 | 723.28 | 784.73 | 846.42 | 908.39 | 970.65 | 1033.21 | 1096. 11 | 1159.37 | 1223.01 | 1287.05 | 58 |
| 59 | 724.30 | 785.75 | 847.45 | 909.43 | 971.69 | 1034.26 | 1097.16 | 1160.43 | 1224.07 | I288. I3 | 59 |
| 60 | $725 \cdot 32$ | 786.78 | 848.49 | 910.46 | 972.73 | IO35. | 1098.22 | I 161 | 1225.14 | 1289.20 | 60 |

SMITHSONIAN TABLES

The Anti-Gudermannian.

| gd u | $2 \mathrm{I}^{\circ}$ | $22^{\circ}$ | $23^{\circ}$ | 24 | $25^{\circ}$ | 26 | 27 | $28^{\circ}$ | 29 | $30^{\circ}$ | gd u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{O}^{\prime}$ | 1289'. 20 | I353.69 | 1418.63 | 1484.06 | I549.99 | 1616.47 | 1683.52 | $\underline{1751.16}$ | 1819.44 | 1888.38 | O' |
| 1 | 1290 | I354 | I4I9.72 |  | 1551. 10 | 16 I 7.58 | 1684.64 | 1752.29 |  | 1889.53 |  |
| 2 | 1.291. 34 | I 355.84 | 1420.80 | 1486.25 | 1'552.20 | 1618.70 | 1685.76 | 1753.43 | 1821.72 | 1890.69 | 2 |
| 3 | 1292.41 | 1356.92 | I421.89 |  | 1553 | 凹619.8I |  | 1754.56 | I822.87 | 1891.84 | 3 |
| 4 | 1293.48 | I358. | 1422.98 | 1488.44 | I 554.4 I | I620.92 | 1688.01 | 1755.69 | 1824.01 | 1893.00 | 4 |
| 5 | I294. 55 | I359.08 | 1424.06 |  | I'5155.5.1 | 1622.04 | 1689.13 | 1756.83 | 1825.16 | 1894. 15 | 5 |
| 6 | 1295.63 | 1360. 16 | I4425. 15 | I490.63 | I556.62 | 1623.15 |  | 1757.96 | 1826.30 |  | 6 |
| 7 | 1296.70 | 1361.24 | 1426.24 | I491. 72 | 1553.72 | 1624.26 | 1691.38 | 1759.09 |  |  | 7 |
| 8 | 1297.77 | 1362.32 | $1427 \cdot 32$ | 1492.82 | 1558.83 |  |  | 1760.23 | 1828.59 | 1897.62 | 8 |
| 9 |  |  |  | I493. |  |  |  |  |  |  | 9 |
| 10 | 1299.91 | 1364.48 | I429.50 | I495.01 | 1561.04 | 1627.61 |  | I762.50 | 1830.88 |  | 10 |
| II | I3 | 1365.56 | 1430.59 | 149 | 1562 | 1628.72 | 1695.87 | 1763.63 | 1832.02 | 1901.09 | I I |
| 12 | 1302 | 1366.64 | 1431.68 |  | I.563.215 | 1629.84 |  | 1764.77 | 1833.17 | 1902.25 | 12 |
| I3 | I'303. I3 | 1367.72 | 1432.76 | 1498.30 | I'564.35 | 1630.95 | 1698. 12 | 1765.90 | 1834.32 | 1903.40 | I3 |
| 14 | 1304.20 | I 368.80 | 1433.85 | 1499.40 |  | 1632.06 | 1699.25 | 1767.04 | 1835.46 | 1904. 56 | I4 |
| 15 | 1305.28 | İ369.88 | I'434.94 | I 500.49 | I.566.56 | 1633.18 | I700.37 | I768.17 | I836.6I | 1905.72 | I 5 |
| I6 | I306.35 | I370 | 1436.03 | I'50 |  | 1634.29 | I701.50 | 1769.31 |  | 1906.88 | 16 |
| I | I 307.42 | I372.04 | I437. 12 | 1502.69 |  | 1635.4 I | 1702.62 | 1770.44 | 1838.90 | 1908.03 | 17 |
| 18 | ${ }^{1}$ I 308.50 | 1373.12 | I 4388.21 | 1503.78 | 1569.88 | 1636.52 | 1703.75 | 1771.58 | I840.05 | 1909. 19 | 18 |
| 19 | I309.57 | 1374.20 | 1439.29 | 1504.88 | 1570.99 | 1637.64 | 1704.87 | 1772.71 | 1841.19 | 1910. 35 | 19 |
| 20 | I3I0.6 | T375.28 | I440.38 | I'505.98 | I572.09 |  | I706.00 | 1773.85 | 1842.34 | 1911.5I | 20 |
| 21 | 131 | I376. | I44I | 1507.08 | 1573.20 | 1639.87 | 1707.12 | 1774.98 | I843.49 | 1912.67 | 2 I |
| 22 | I312 | I 377.44 | 1442.56 | I508. 17 | I574.31 | 1640.99 | I'708.25 | I'776. 12 | I844.64 | 1913.83 | 22 |
| 23 | I313 | I 378.52 | 1443.65 | I509.27 | I575.4I | I642. 10 | I709.'37 | 1777.26 |  | 1914.98 | 23 |
| 24 | I3I4. | 1379.61 | I444.74 | 1510.37 | I.576.52 | 1643.22 | 1710.50 | I778.39 | I846.93 | 1916. I4 | 24 |
| 25 | I316.01 | 1380.69 | I445.83 | I5II.47 | 1577.63 | $1644 \cdot 34$ | 1711.63 | I779.53 | 1848.08 | 1917.30 | 25 |
| 26 | I317.08 | I381.77 | 1446.92 | 15 I 2.57 | 1578.73 | I 645.45 | I712.75 | I780.67 | I849.23 | 1918.46 | 26 |
| 27 | I3I8.16 | I'382.85 | I448.01 | 1513.67 | 1579.84 | 1646.57 | I713.88 | I'78i. 8 I | 1850.37 | 1919.62 | 27 |
| 28 | 1319.23 | 1383.93 | I449. 10 | 1514.76 | 1580.95 | 1647.69 | 1715.01 | 1782.94 | 1851.52 | 1920.78 | 28 |
| 29 | I320.3I | 1385.02 | 1450.19 | I515.86 | 1582.06 | 1648.80 | I716. I4 | 1784.08 | 1852.67 | 1921.94 | 29 |
| 30 | I32I. 38 | I386. 10 | 1451.28 | 1516.96 | 1583. 17 | I649.92 | I7I7.26 | I785.22 | 1853.82 | 1923.10 | 30 |
| 3 I | 1322.45 | 1387.18 | 1452.37 | I5I8.06 | 1584.27 | 1651.04 | I'718.39 | 1786.36 |  | 1924.26 | 3 I |
| 32 | I3223.53 | I'388.26 | I 453.46 | I519. 16 | I 585.38 | 1652.16 | 1719.52 | I787.50 | 1856.121 | 1925.43' | 32 |
| 33 | I324.60 | 1389.35 | I454. 55 | I520.26 | I 586.49 | 1653.27 | I'720.65 | I788.63 | 1857.27 | I926.59 | 33 |
| 34 | I1325.68 | I 390.43 | 1455.64 | 1521.36 | 1587.60 | $1654 \cdot 39$ | .1721.77 | 1789.77 | 1858.42 | I927.75 | 34 |
| 35 | I326.75 | I391.5I | 1456.73 | 1522.46 | I 588.71 | 1655.5 I | 1722.90 | I790.91 | 1859.57 | 1928.91 | 35 |
| 36 | 1327.83 | I 392.59 | 1457.83 | I523.56 | I 589.82 | I656.63 | 1724.03 | I'792.05 | 1860.72 | 1930.07 | 36 |
| 37 | I 328.90 | I393.68 | I458.92 | I'524.66 | I590.92 | 1657.75 | 1725.16 | I'793. I9 | 1861.87 | 1931.23 | 37 |
| 38 | I'329.98 | I 394.76 | 1460.01 | I 525.76 | I592.03 | 1658.87 | I726.29 | 1794.33 | 1863.02 | 19332.40 | 38 |
| 39 | 1331.06 | 1395.84 | 1461. 10 | I 526.86 | I:593. I4 |  | 1727.42 | I795.47 | 1864.17 | 1933.56 | 39 |
| 40 | I332.13 | I306.93 | 1462 . 19 | 1527.96 | I 594.25 | I66I. IO | I728.54 | 1796.6I | 1865.32 | 1934.72 | 40 |
| 4 I | Il333.2I | I 398.01 | 1463.28 | 15129.06 |  | 1662.22 | I729.67 |  | I866.47 | 1935.88 | 4 I |
| 42 | 1334.29 | I 399 . IO | $1464 \cdot 38$ | 15330.16 | I 596.47 | 1663 | 1730.80 | 1798.89 | 1867.62 | 1937.05 | 42 |
| 43 | I 3335.37 | 1400. 18 | 1465.47 | 1531.26 |  | 1664.46 | 1731.93 | 1800.03 | 1868.77 | 1938.21 | 43 |
| 44 | I 336.44 | I401. 25 | 1466.56 | I532.36 | I598.69 | 1665.58 | 1733.06 | I801. I7 | 1869.92 | 1939.37 | 44 |
| 45 | I 337.52 | 1402.35 | 1467.65 | 1533.46 | I 599.80 | 1666.70 | 【734.19 | I802.3I | 1871.08 | 1940.54 | 45 |
| 4 | 13138.60 |  | 1468.75 | 1534.56 | 1600.9I | 1667.82 | 1735.32 | 1803.45 |  | 1941.70 | 46 |
| 47 | I 339.67 | 1404.512 | 1469.84 | I535.66 | 1602.02 | 1668.94 | 1736.45 | I804. 59 | 1873.38 | 1942.85 | 47 |
| 48 | I340.75 | 1405.60 | 1470.93 | 1536.77 | 1603.13 | 1670.06 | 1737.58 | I805.73 | 1874.53 | 1944.03 | 48 |
| 49 | I341.83 | 1406.69 | 1472.02 | 1537.87 | 1604.24 | 167i. 18 | 1738.71 | I806.87 | 1875.69 | 1945.19 | 49 |
| 50 | I342.91 | 1407.77 | 1473 . 12 | I538.97 | 1605.35 | 1672.30 | 1739.84 | 1808.01 | 1876.84 | 1946.36 | 50 |
| 5 I | I343.98 | 1408.86 | I474.2I | I'540.07 | 1606.46 | 1673.42 | 1740.98 | 1809.15 | 1877.99 | 1947.52 | 5 I |
| 52 | I 345.06 | I409.94 | 1475.30 | I541. I7 | 1607.58 | 1674.54 | I742.11 | I8IO. 30 | 1879.14 | 1948.69 | 52 |
| 53 | I 346.14 | I4II.03 | I476.40 | 1542.27 | 1608.69 | 1675.66 | 1743.24 | I8II.44' | 1880.30 | 1949.85 | 53 |
| 54 | I347.22 | 1412.11 | 1477.49 | $1543 \cdot 38$ | 1609.80 | 1676.79 | I744.37 | I812.58 | 1881.45 | 1951.02 | 54 |
| 55 | I348.29 | 1413.20 | 1478.59 | I544.48 | 1610.91 | 1677.91 | 1745.50 | I8I'3.72 | 1882.60 | 1952.18 | 55 |
| 56 | 1349.37 | I4I4.28 | 1479.68 | I545. 58 | 16I2.02 | 1679.03 | 1746.63 | 1814.86 | 1883.76 | 1953.35 | 56 |
| 57 | 1350.45 | I4I5.37 | 1480.77 | I546.69 | 16I3.13 | 1680. 15 | 1747.76 | 1816.01 | 1884.91 | 1954.51 | 57 |
| 58 | 1351.53 | I416.46 | 1481.87 | 1547.79 | 1614.25 | 1681.27 | 1748.90 | 1817.15 | 1886.07 | 1955.68 | 58 |
| 59 | 1352.6I | 1417.54 | 1482.96 | I548.89 | 16I5.36 | 1682.39 | 1750.03 | 1818.29 | 1887.221 | 1956.85 | 59 |
| 60 | I 353.69 | 1418.63 | 1484.06 | I 549.99 | 1616.47 | 1683.52 | 1751.16 | 1819.44 | 1888.38 | 1958.01 | 6 |


| od u | $31^{\circ}$ | 32 | $33^{\circ}$ | $34^{\circ}$ | $35^{\circ}$ | $36^{\circ}$ | $37^{\circ}$ | 8 | $39^{\circ}$ | $40^{\circ}$ | ad |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| o' | 1958'. | 2028.38 | 2099.53 | 2171.48 | 2244.29 | 2317.99 | 2392.63 | 2468.26 | 2544.93 | 2622. | o' |
|  |  |  | 2100.72 |  |  |  |  |  |  |  |  |
| 2 | 1960 | 2030.74 | 2101. | 2173.89 |  | 2320.46 | 2395.14 |  |  |  |  |
| 3 | 1961. | 2031 | 2 IO 3 | 2175 | 2247.95 | 2321.70 | 2396.39 | 2472.07 |  |  | 3 |
| 4 | 1962.68 | 2033.10 | 2104 | 2176.31 | 2249.17 | 2322.93 | 2397.64 | 2473.34 |  |  |  |
| 5 | 1963.85 | 2034.28 | 210 | 2177.51 | 2250.39 | 2324.17 |  | 2474.61 | 2551.37 |  |  |
| 6 |  |  | 2106 |  |  |  |  |  | 2552.66 |  | 6 |
| 7 | 1966.1 | 2036.64 | 2107.88 | 2179.93 | 2252.84 | 2326.65 | 2401.40 | 2477.15 | 2553.95 |  |  |
| 8 | 1967.35 | 2037.82 | 2109.07 | 2181.14 | 2254.06 | 2327.89 |  |  | 2555.23 |  |  |
| 9 |  | 2039 | 2110.27 |  |  | 2329.1 | 2403.91 |  | 2556.52 |  |  |
| Io | 1969 | 2040 | 2111.46 | 2183.55 |  | 2330 | 2405. | 2480.97 |  |  | 10 |
| II | 19 |  | 2112.66 | 1184.76 | 2257.73 | 2331 | 2406 | 2482.24 | 2559. 10 |  | II |
|  |  |  | 2113 |  |  | 23 | 2407 | 2483.51 |  |  | 12 |
| 13 | 197 |  | 2115 | 2187.18 |  | 23 | 2408 | 2484.78 |  |  | 13 |
| 14 | 1974 | 2044.91 | 2116 | 12188.39 | 2261.40 | 2335.32 | 2410 | 12486.06 |  | 2641 . 00 | 14 |
| r'5 | 1975 | 2046 | 2117 | 2189.60 | 2262.63 | 2336.56 | 2411 | 2487.33 | 2564.27 | 2642.31 | 15 |
| 16 |  |  | 21 |  |  |  | 2412 |  |  |  | 16 |
| 17 | 1977. | 2048.46 | 2119.83 | 2192.02 |  | 2339 | 2413.9 | 2489.88 |  |  | 7 |
| 18 | 1979 | 2049.64 | 2121.03 | 2193.2 | 226 | 2340. | 2415.21 | 2491.15 | 2568. 14 |  | 8 |
| 19 | 1980 | 2050. |  | 21 | 226 | 2341. | 2415.47 | 2492.43 | 2569.43 |  | 19 |
| 20 | 1981.3 |  | 21 | 2195 |  | 2342. | 2417.73 | 2493.70 | 2570.73 |  | 0 |
| 21 | 1982.5 |  | 2124.62 | 2196.86 | 2269.98 | 23 | 2418.99 |  | 2572.02 |  | 21 |
| 22 | 1983 | 205 | 2125.81 | 2198 |  | 23 |  |  |  |  | 22 |
| 23 | 1984 | 20 |  | 2199 |  |  |  |  | 25 |  | 23 |
| 24 | 1986.07 | 2056 | 21 | 2200.50 |  |  |  |  | 257 |  | 24 |
| 25 | 1987.24 | 205 | 2129.41 | 2201.7 | 227 | 2348 | 2424.02 |  | 2577. | 43 | 25 |
| 26 | 1988. | 205 | 2130.61 | 2202.92 | 2276.11 | 2350.21 | 2425 | 2501.35 | 2578.49 | 2656.74 | 26 |
| 27 | 1989.59 | 2060 | 2131.80 | 2204.14 | 2277 - 34 | 2351. 46 | 2426.54 | 2502.63 | 2579.78 | 2658.05 | 27 |
| 28 | 1990.7 | 12061 | 2133.0 | 2205.35 |  | 2352.70 | 2427.80 | 2503.91 | 2581.08 |  | 28 |
| 29 | 1991.93 |  | 2134.20 |  |  | 2353.95 | 2429.06 |  | 25 |  | 29 |
| 30 | 1993 |  | 2135.40 | 2207 |  | 2355. | 2430.32 | 2506.46 |  |  | 30 |
| 3 |  |  | 2136.60 | 12208.99 | 2282.25 |  |  | 2507.74 |  |  | 31 |
| 32 | 199 | 2066 | 2137 | 10 | 2283. |  |  |  | 2586.26 |  | 32 |
| 33 | 199 | 2067 |  | 22II. 4 | 228 | 235 |  | 2510.30 |  | 266 | 33 |
| 34 | 199 | 2068 | 2140.20 |  |  | 236 |  |  |  |  |  |
| 35 | 199 | 2069 | 2141 | 2213 | 2287.17 | 236 |  |  | 5 | 2668.58 | 36 |
| 36 | 2000 | 2070 | 2142. | 221 |  | 2362.66 | 2437. | 2514 | 2591.45 | 2669.89 | 36 |
| 37 | 2001 | 2072.16 | 2143.8 | 2216.27 | 228 | 2363. | 2439.15 | 2515 | 2592.75 | 2671.21 | 37 |
| 5 | 2002 | 2073.35 | 2145 | 2217. | 22 | 236 | 2440 | 2516.69 | 2594.05 |  | 38 |
| 39 | 2003 | 2074.54 | 2146.20 |  | 1229 | 23 | 244 | 2517.97 | 2595.35 |  | 39 |
| 40 | 20 | 207 | 2147.4 | 2219.92 | 2293.32 | 2367.6 | 24 | 2519.25 | 2596.65 | 2675.16 | 40 |
| 4 I | 20 | 2076 | 2148.6 |  |  | 2368.89 |  | 25 | 2597.95 |  | 4 I |
| 4 |  | 2078 | 2149.8I |  |  |  |  | 1252 | 2599.24 |  | 42 |
| 43 | 2008 |  | 2151.0 | 22 | 2297 |  |  | 252 |  |  | 43 |
|  | 2009 | 2080 | 2 I 52.21 L | 2224.79 | 2298.24 |  | 2447 | 252 | 2601.84 | 2688.44 | 44 |
| 45 | 2OIO | 2081. 67 | 2153.41 |  | 2299.48 |  | 2449 | 251 | 2603.14 | 2681.76 | 45 |
| 46 | 2011 | 2082.86 | 215 |  | 2300 | 2375 | 2450.52 | 2526.95 |  |  | 46 |
| 47 | 2013.07 | 2084.04 | 2155 | 222 | 2301 | 2377.3 | 2451.79 | 2528.23 | 2605.75 | 2684.40 | 47 |
| 48 | 2014 | 208 |  | 222 | 2303 |  | 2453.05 | 12529.51 | 2607 | 2685.72 | 48 |
| 49 | 201 | 2086.42 | 2158.2 | 2230.87 | 230 |  | 245 | 25 | 2608.35 | 66 | 49 |
| '50 | 2016.60 | 2087.61 | 2159.4 | 2232.09 | 230 | 2380.1 | $2455 \cdot 5$ | 2532.08 | 2609.65 | 668 | 50 |
| 5 | :2017.78 | 2088.80 | 2160.63 |  | 2306.88 |  | 2456.85 | 2533.36 | 2610.95 | 2689.69 | 51 |
| 52 | 2018.96 | 2089.99 | 2161.84 | 2234.53 | 2308.11 | 2382.62 | 2458.12 | 2534.65 | 2612.26 | 2691.01 | 5 |
| 53 | 2020.13 | 2091.19 | 2163.04 | 223 | 2309 | 2383.87 | 2459.39 | 2535.93 | 2613.56 | 2692.33 | 53 |
| 5 | 2021.3I | 2092 . 38 | 2164.25 | 12236.97 | 2315 | 2385.12 | 2466.65 | 2537.22 | 2614.86 | 2693 | 5 |
| 55 | 2022.4 | $2093 \cdot 57$ | 2165.45 | 2238.19 | 23 | 2386.37 | 2461.92 | 2538.50 | 2616.17 | 2694 | 55 |
| 56 | 2023 | 2094.76 | 2166.66 |  | 1231 |  | 2463.19 | 2539 |  | 2696.30 | 56 |
|  | 2024.85 | 2095.95 | 2167 | 2240.63 | 2314. | 2388.8 | 24 | 2541. | 2618 | 26.3 | 57 |
|  | 2026.03 | 2097 | 2 | 2241.85 | 12315 | 239 |  | 25 |  | 2698.95 | 58 |
|  | 2022 | 2098.3 | 2170 | 2243.07 | 2316.75 | 2391 |  | 2543. |  | 2700.27 | 59 |
| 60 | 20 | 2099 | 217 | 224 | 2317 | 239 |  |  |  | 2701 |  |

The Anti-Gudermannian.

| gd u | $4 \mathrm{I}^{\circ}$ | $42^{\circ}$ | $43^{\circ}$ | $44^{\circ}$ | $45^{\circ}$ | 46 | $47^{\circ}$ | $48^{\circ}$ | $49^{\circ}$ | $50^{\circ}$ | du |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{\prime}$ | $2701{ }^{\prime} .60$ | 2781.71 | 2863 . 10 | 2945.8 I | 3029.94 | 3II5.55 | 3202.71 | 3291.53 | $\overline{3382.08}$ | 3474.47 | o' |
| 1 | 270 | 2783.06 | 2864.46 | 2947.2I | 303I. 35 | 3 II 6.99 | 3204.18 | 3293.02 | 3383.61 | 3476.03 | I |
| 2 | 2704.25 | 2784.40 | 2865.83 | 2948.60 | 3032.77 | 3118.43 | 3205.65 | 3294.52 | 3385.13 | 3477.59 | 2 |
| 3 | 2705.57 | 2785.75 | 2567.20 | 2949.99 | 3034. I8 | 3 II 19.87 | 3207.12 | 3296.01 | 3386.66 | 3479.14 | 3 |
| 4 | 2706.90 | 2787.09 | 2868.57 | 2951.38 | 3035.60 | 3 I 2 I .3 I | 3208.58 | 3297.51 | 3388.18 | 3480.70 | 4 |
| 5 | 2708.23 | 2788.44 | 2869.94 | 2952.77 | 3037.02 | 3122.75 | 3210.05 | 3299.01 | 3389.71 | 3482.26 | 5 |
| 6 | 2709 | 2789.79 | 2871.31 | 2954.16 | 3038.43 | 3124. I9 | 32II. 52 | 3300.5 I | 3391.24 | 3483.82 | 6 |
| 7 | 2710.88 | 2791. I4 | 2872.68 | 2955.56 | 3039.85 | 3125.63 | 3212.99 | 3302.00 | 3392.77 |  |  |
| 8 | 2712 | 2792.49 | 2874.05 | 2956.95 | 3041.27 | 3127.08 | 3214.46 | 33303.50 | 3394.29 | 3486.94 | 8 |
| 9 | 2713 | 2793.84 | 2875.42 | 2958.34 | 3042.68 |  | 3215.93 | 3305.00 | 3395.82 | 3488.50 | 9 |
| 10 | 2714.86 | 2795.19 | 2876.79 | 2959.74 | 3044. IO | 3129.96 | 3217.40 | 3306.50 | 3397 . 35 | 3490.06 | 10 |
| II | 2716.1 | 2796.54 | 2878. 16 | 296I. I3 | 3045.52 | 3I3I.4I | 3218.87 | 3308.00 | 3398.88 | 3491.62 | II |
| 12 | 2717.52 | 2797.89 | 2879.53 | 2962.53 | 3046.94 | 3'132.85 | 3220.34 | 3309.50 | 3400.41 | 3493.18 | 12 |
| 13 | 2718.85 | 2799.24 | 2880.90 | 2963.92 | 3048.36 | 3 I 34.30 | 3221.82 | 3311.00 | 3401.94 | 3494.74 | 13 |
| 14 | 2720.18 | 2800.59 | 2882.28 | 2965.32 | 3049.78 | 3 I 35.75 | 3223.29 | 3312.50 | 3403.47 | 3496.3I | I4 |
| 15. | 2721.5I | 2801.94 | 2883.65 | 2966.71 | 3051.20 | 3137.19 | 3224.76 | 3314.00 | 3405.00 | 3497.87 | I5 |
| 16 | 2722.8 | 2803.29 | 2885.02 | 296 | 3052.62 | 3138.64 | 3226.23 | 3315.50 | 3406.54 | 3499.43 | 16 |
| 17 | 2724.17 | 2804.64 | 2886.39 | 296 | 3054.04 | 3 I 40.08 | 3227.71 | 33177.00 | 3408.07 | 3501.00 | 17 |
| I8 | 2725.50 | 2805.99 | 2887.77 | 2970.90 | 3055.46 | 3 I 41.5 | 3229. 18 | 3318.51 | 3409.60 | 3502.56 | I8 |
| 19 | 2726.83 | 2807.34 | 2889.14 | 2972.30 | 3056.88 | 3142.98 | 3230.66 | 3320.01 | 3411.14 | 3504.13 | 19 |
| 20 | 2728.17 | 2808.70 | 2890.52 | 2973.70 | 3058.3 I | 3144.42 | 3232 . I3 | 3321. 52 | 3412.67 | 3505.70 | 20 |
| 21 | 2729.50 | 2810.05 | 2891.89 | 2975.09 | 3059.73 | 3145.87 | 3233.6 I | 3323.02 | 3414.20 | 3507.26 | 2 I |
| 22 | 2730.83 | 281 I .40 | 2893.27 | 2976.49 | 306I. I5 | 3147.32 | 3235.08 | 3324.53 | 3415.74 | 3508.83 | 22 |
| 23 | 2732.16 | 2812.76 | 2894.64 | 2977.89 | 3062 . 58 | 3148.77 | 3236.56 | 3326.03 | 3417.28 | 3510.40 | 23 |
| 24 | 2733.50 | 28I4. 11 | 2896.02 | 2979.29 | 3064.00 | 3150.22 | 3238.04 | 3327.54 | 3418.8I | 3511.97 | 24 |
| 25 |  | 2815.46 | 2897.40 | 2980.69 | 3065.42 | 3151.67 | 3239.52 | 3329.04 | 3420.35 | 3513.54 | 25 |
| 26 | 2736.16 | 2816.82 | 2898.77 | 2982.09 | 3066.85 | 3153.12 | 3240.99 | 3330.55 | 342 I. 89 | 3515.11 | 26 |
| 27 | 2737.50 | 2818.17 | 2900. 15 | 2983.49 | 3068.27 | 3154.57 | 3242.47 | 3332.06 | 3423.43 | 3516.68 | 27 |
| 28 | 2738.83 |  | 2901.53 | 2984.89 | 3069.70 | 3156.03 | 3243.95 | 3333.56 | 3424.96 | 3518.25 | 28 |
| 29 | 2740.17 | 12820.88 | 2902.91 | 2986.29 | 307 I. 13 | 3157.48 | 3245.43 | 3335.07 | 3426.50 | 3519.82 | 29 |
| 30 | 2741.50 | 2822.24 | 2904. 28 | 2987.70 | 3072.55 |  |  | 3336.58 | 3428.04 | 352I. 39 | 30 |
| 31 | 2742.84 | 2823.60 | 2905.66 | 2989 . 10 | 3073.98 | 3160.38 | 3248.39 | 3338.09 | 3429.58 | 3522.96 | 3 I |
| 32 | 2744. 17 | 2824.95 | 2907.04 | 2990.50 | 3075.41 | 3161.84 | 3249.87 | 3339.60 | 3431.12 | 3524.54 | 32 |
| 33 | $2745 \cdot 5 \mathrm{I}$ | 2826.3 I | 2908.42 | 2991.90 | 3076.84 | 3163.29 | 325 . 35 | 3341. II | 3432.66 | 3526. II | 33 |
| 34 |  | 2827.67 | 2909.80 | 2993.31 | 3078.26 | 3164.74 | 3252.84 | 3342.62 | 3434.20 | $3527.68$ | 34 |
| 35 |  | 2829.03 | 2911. 18 | 2994.71 | 3079.69 |  | $3254 \cdot 32$ | 3344. 14 | 3435.75 | 3529.26 | 35 |
| 36 |  | 2830.39 | 2912.56 | 2996. 12 | 3081. 12 | 3167.65 | 3255.80 | 3345.65 | 3437.29 | 3530.83 | 36 |
| 37 | 2750.85 | 2831.74 | 2913.94 | 2997.52 | 3082.55 | 3169.11 | 3257.28 | 3347. 16 | 3438.83 | $3532.4 \mathrm{I}$ | 37 |
| 38 | 2752.19 | 2833.10 | 2915.32 | 2998.93 | 3083.98 | 3170.57 | 3258.77 | 3348.67 | 3440.38 | 3533.99 | 38 |
| 39 | $2753 \cdot 53$ | 2834.46 | 2916.71 | 3000.33 | 3085.41 | 3172.02 | 3260.25 | 3350. 19 | 344 I .92 | 3535.56 | 39 |
| 40 | 2754.87 | 2835.82 | 2918.09 | 3001.74 | 3086.84 | 3173.48 | 3261.74 | 3351.70 | 3443.47 | 3537.14 | 40 |
| 4 I | 2756.2 I | 2837.18 | 2919.47 | 3003. I4 | 3088.27 | 3174.94 | 3263.22 | 3353.21 | 3445.01 | 3538.72 | 41 |
| 42 | 2757.55 | 2838.54 | 2920.85 | 3004.55 | 3089.70 | 3176.40 | 3264.71 | 3354.73 | 3446.56 | 3540.30 | 42 |
| 43 | 2758.89 | 2839.90 | 2922.24 | 3005.96 | 3091. I4 | 3177.85 | 3266.19 | 3356.24 | 3448. Io | 3541.88 | 43 |
| 44 | 2760.23 | 2841.27 | 2923.62 | 3007.36 | 3092.57 | 3179.3I | 3267.68 | 3357.76 | 3449.65 | 3543.45 | 44 |
| 45 | 2761.57 | 2842.63 | 2925.01 | 3008.77 | 3094.00 | 3180.77 | 3269.17 | 3359.28 | 345I. 20 | 3545.04 | 45 |
| 46 | 2762.91 | 2843.99 | 2926.39 | 3010.18 | 3095.43 | 3182.23 | 3270.65 | 3360.79 | 3452.75 | 3546.62 | 46 |
| 47 | 2764.25 | 2845.35 | 2927.78 | 3011.59 | 3096.87 | 3183.69 | 3272.14 |  | 3454.29 | 3548.20 | 47 |
| 48 |  |  | 2929.16 | 3013.00 | 3098.30 | 3185. 15 | 3273.63 | 3363.83 | 3455.84 | 3549.78 | 48 |
| 49 | 2766.93 | 2848.08 | 2930.55 | 3014.41 | 3099.74 | 3186.61 | 3275.12 | 3365.35 | 3457.39 | 355 I . 36 | 49 |
| 5 | 2768.27 | 2849.44 | 2931.93 | 3015.82 | 3101.17 | 3188.07 | 3276.61 | 3366.87 | 3458.94 | 3552.94 | 50 |
| 51 | 2769.62 | 2850.8 I | $2933 \cdot 32$ | 3017.23 | 31102.60 | 3189.54 | 3278. 10 | 3368.39 | 3460.49 | $3554 \cdot 53$ | 51 |
| 52 | 2770.96 | 2852.17 | 2934.71 | 3018.64 | 3104.04 | 3191.00 | 3279.59 | 3369.91 | 3462.04 | 3556. II | 52 |
| 53 | 2772.30 | $2853 \cdot 53$ | 2936.09 | 3020.05 | 3105.48 | 3 I 92.46 | 3281.08 | 3371.43 | 3463.60 | 3557.70 | 53 |
| 54 | 2773.64 | 2854.90 | 2937.48 | 3021.46 | 3106.92 | 3193.92 | 3282.57 | 3372.95 | 3465.15 | 3559.28 | 54 |
| 55 | 2774.99 | 2856.26 | 2938.87 | 3022.87 | 3108.35 | 3195.39 | 3284.06 | 3374.47 | 3466.70 | 3560.87 | 55 |
| 56 | 2776.33 | 2857.63 | 2940.26 | 3024.29 | 3109.79 | 3196.85 | 3285.56 | 3375.99 | 3468.26 | 3562.45 | 56 |
| 57 | 2777.68 | 2858.99 | 2941.65 | 3025.70 | 3 III .23 | 3198.32 | 3287.05 | $3377 \cdot 51$ | 3469 . 81 | 3564.04 | 57 |
| 58 | 2779.02 | 2860.36 | 2943.04 | 3027. II | 3 IT 2.67 | 3199.78 | 3288.54 | 3379.04 | 3471.36 | 3565.63 | 58 |
| 59 | 2780.37 | 2861. 73 | 2944.42 | 3028.52 | 3114.11 | 3201. 25 | 3290.04 | 3380.56 | 3472.92 | 3567.22 | 59 |
| 60 | 2781.71 | 2863.10 | 2945.8I | 3029.94 | 3115.55 | 3202.71 | 3291. 53 | 3382.08 | 3474.47 | 3568.8 I | 60 |


| gd u | 5 |  | $53^{\circ}$ |  |  | 56 | 57 | $58^{\circ}$ |  | $60^{\circ}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| o' | 3568'.8 | 3665 | 3763.76 | 3864.64 | 3967.97 | 407 | 4182.62 | 4294.30 | 440 | 4527.37 |  |
|  |  | 3666.82 | 3765.42 |  | 3969.7 I |  | 4184.46 | 4296. 19 |  |  |  |
| 2 | 位 | 3668. | 3767.09 | 3868.04 | 3971.46 | 4077. |  |  | 4413.03 |  |  |
| 3 | 357 | 3670.07 | 3768.75 | 3869.74 | 3973.20 | 4079.27 | 4188. I3 | 4299.96 |  |  |  |
| 4 | 3575. 17 | 3671.70 | 3770.4 I | 3871.45 | 3974.95 | 408 I .06 | 4189.97 | 4301.85 |  |  |  |
| 5 | 3576.76 | $3673 \cdot 32$ |  | 3873.15 | 3976.69 |  | 4191.8 I | 4303.74 |  |  |  |
| 6 | 357 |  |  |  |  |  | 4193.65 | 4305.64 | 4420.8 I |  |  |
| 7 | 3579.94 |  | 3775.41 |  | 398 |  | 4195.49 | 4307.53 | 4422.76 | 4541.39 |  |
| 8 | 358 |  |  |  |  |  | 4197. | 4309.42 | 4424.70 | 4543.40 |  |
| 9 |  |  |  |  |  |  |  | 4311.32 |  | 4545.4 I |  |
| 10 | 358 |  |  |  |  |  |  | 43 |  |  | o |
|  | 3586 | 3683 | 3782.08 | 3883.39 | 3987 | 4093 | 4202.87 | 4315.11 | . 5 |  | II |
| 12 | 3587 | 368 | 3783.75 | 3885.10 | 3988. | 4095. | 4204.71 | 4317.01 |  | 455 | 12 |
| 13 | 3589 | 3686 | 3785.42 | 3886.8 | 3990. | 4097 | 4206. |  | 4434.46 | 455 | I3 |
| 14 | 3591. II | 3687.99 | 3787.09 | 3888.52 | 399 | 409 | 4208.41 | 4320.80 | 4436.42 |  | 14 |
| 15 | 3592 | 368 |  | 3890.23 | 399 | 41 | 4210. | 4322.70 | 7 |  | 15 |
| 16 |  |  | 3790.43 |  |  |  |  |  | 4440.33 |  | 16 |
| 17 | 3595.9 | 3692.90 | 3792.10 |  | 3997. | 41 | 421 | 4326.51 | 4442.29 |  | 17 |
| 18 | 3597.5 | 3694.53 | 379 | 38 | 3999. |  |  | 4328.4 I | 4444.24 |  | 18 |
| 9 | 3599 |  | 379 |  | 400 | 41 |  | 4330.3I |  | 4565.55 | 19 |
| 20 |  |  | 379 |  |  |  | 421 | 4332.22 |  |  | 20 |
| 21 |  |  | 379 | 39 |  | 4 |  |  | 4450.12 |  | 1 |
|  |  |  | 380 | 390 |  |  |  |  | 44512.09 | 4571.61 | 22 |
| 23 | 360 |  | 380 |  |  |  |  | 4337 |  | 4573.64 | 23 |
| 24 | 360 |  |  |  |  | 41 |  | 433 | 445 |  | 24 |
| 25 |  |  |  |  |  |  |  |  |  |  | 25 |
| 26 | 3610 | 3707.63 | 380 | 390 |  | 4120 | 4230.64 | 4343.66 | 4459.94 |  | 25 |
| 27 | 3611.92 | 3709.27 |  | 3910 | 4015.3 | 4122 | 4232 | 4345.57 | 446 r .91 |  | 8 |
| 28 | 3613.52 | 3710.91 | 3810.5 | 3912 | 4017.07 | 4124 | 423 | 4347.48 | 446 |  | 28 |
| 29 | 3615.13 | 3712.56 | 3815 |  | 401 | 412 |  | 4349.40 |  |  | 29 |
| 30 | 3616.74 | 3714.20 | 3813 | 39 |  |  |  | 4351.3I | 446 | 4587.83 | 30 |
| 31 |  |  |  | 391 |  |  |  | 4 |  | 4589.86 | 3 I |
| 32 |  | 3717 |  | 3919 |  |  |  | 435 | 447 |  | 32 |
| 33 |  |  |  |  |  | 1 |  |  | 4473 | 459 | 33 |
|  |  |  |  | 39 |  | 413 |  |  |  |  | 35 |
| 35 |  |  | 382 |  |  |  |  |  |  |  | 35 |
| 36 | 3626 |  | 3824 |  | 4031.2I |  | 4249.26 | 4362.8I | 4479.66 | 4600.03 | 36 |
| 37 | 3628.0 | 3725 | 3825.69 | 3928.0 | 4032 | 4140 | 4251.13 |  | 448 r .63 | 4602.07 | 37 |
| 38 | 362 | $3727 \cdot 36$ | 3827.3 | 3929.79 | 403 | 4142 | 4252 | 4366.65 | 4483.61 |  | 38 |
| 39 | 363 I .22 | 3729.01 | 3829.0 | 3931.51 | 4036 |  | 4254.86 | 4368.57 | 4485.59 |  | 39 |
| 40 | 3632.83 |  | 3830.75 |  | 4038. |  | 4256.73 | 4370.50 | 4487.57 | 9 | 40 |
| 41 |  |  | 3832 |  | 404 |  | 4258. | 4372.42 | 4489.55 |  | 4 I |
| 42 |  |  | 38 |  | 40 |  | 4260 |  | 449 | 4612 | 42 |
| 43 |  | 37 | 3835 | 3938 |  |  | 4262 |  | 44 |  | 3 |
| 44 | 36 |  | 3837.50 | 394 | 40 | 415 | 42 |  |  |  | 44 |
| 45 | 3640 | 373 | 3839.19 | 394 | 404 |  | 42 | 4380. | 44 | 1 | 45 |
| 46 | 3642 | 3740.56 | 3840.88 | 3943.63 | 4048.94 | 4157.00 |  |  | 4499.47 |  | 46 |
| 47 | 3644.13 | 3742.21 | 3842.58 | 3945.36 | 4050.72 | 4158. | 4269. | 4383.98 | 4501.45 | 4622.50 | 47 |
| 48 | 3645.75 | 3743.87 | 38 | 3947 | 4052 | 4160. | 4271. | 4385. | 4503.44 |  | 48 |
| 49 | 364 | 3745.52 | 38 | 3948.83 | 405 | 416 | 4273 |  | 4505.43 | 46 | 49 |
| 50 | 3648.98 | 3747.18 | 3847.66 | 3950 | 4056.0 | 4 I 6 |  | 4389.77 | 4507 | 46 | 50 |
| 51 |  | 3748.83 | 3849.35 | 3952.3 I | 4057.8 | 4166.13 |  | 4391.70 | 4509.4 I | 4630.71 | 51 |
| 52 | 365 | 375 | 3051.05 |  | 4059. | 4167.96 |  | 4393.6 | 45 II .40 | 4632. | 52 |
| 53 | 3653 |  | 3852.75 | 3955.78 | 4061. 41 | 4169.79 | 4281. | 4395.57 | 4513.39 |  | 53 |
| 54 |  | 3755. | 3854.44 | 3957.52 | 4063. 19 | 4171.62 | 4282. | 4397.5 I | 4515.39 | 4636.87 | 54 |
| 55 | 3657.08 | 375 | 3856.14 | 3959.2 | 4064.9 | 4173.45 | 4284 | 4399. | 4517.38 | 4638.93 | 55 |
| 56 | 3658.70 | 375 |  | 3961 | 4066.76 | 4175.28 | 428 | 440 I .38 | 4519.38 | 4640.98 | 56 |
|  | 3660.32 | 3758 | 3859.54 | 396 | 4068.54 | 4177.12 | 4288.6 | 4403. | 4521.37 | 4643.04 | 57 |
| 58 | 3661.95 |  | 3861. 24 | 39 | 4070.33 | 41 | 4290. | 4405. | 4523.37 | 4645. I0 | 58 |
|  | 366 | 37 | 3862.94 | 3966.22 | 4072.12 | 4180.78 | 4292 | 4407. | 4525 |  | 59 |
|  | 3665 |  |  | 3967.97 |  |  | 429 | 440 | 4527 | 4649.23 |  |

The Anti-Gudermannian.

| od u | $61^{\circ}$ | $62^{\circ}$ | $63^{\circ}$ | $64^{\circ}$ | $65^{\circ}$ | $66^{\circ}$ | $67^{\circ}$ | $68^{\circ}$ | $69^{\circ}$ | $70^{\circ}$ | gd u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathrm{o}^{\prime}$ | 4649'.23 | 4774.98 | 4904.94 | 5039.42 | 5178.8I | 5323.51 | 5474.01 | 5630.82 | 5794.56 | 5965.92 | o |
| I | 4651.29 | 4777.11 | 4907.14 |  | 5181.18 |  | 5476.57 | 5633.49 | 5797.35 | 5968.84 | 1 |
| 2 | 4653.35 | 4779.25 | 4909.35 | 5043.99 | 5183.54 | 5328.43 | 5479.13 | 5636.16 | 5800.14 | 5971.77 | 2 |
| 3 | 4655.42 | 4781.38 | 491I. 55 | 5046.27 | 5185.91 | 5330.90 | 5481. 69 | 5638.84 | 5802.94 | 5974.70 | 3 |
| 4 | 4657.49 | 4783.51 | 4913.76 | 5048.56 | 5188.29 | 5333.36 | 5484.26 | 5641.51 | 5805.74 | 5977.63 | 4 |
| 5 | 4659.55 | 4785.65 | 4915.97 | 5050.85 | 5190.66 | 5335.83 | 5486.83 | 5644.19 | 5808.54 | 5980.57 | 5 |
| 6 | 4661.62 | 4787.79 | 4918.18 | 5053.14 | 5193.03 | 5338.30 | 5489.40 | 5646.87 | 5811.34 | 5983.50 | 6 |
| 7 | 4663.69 | 4789.92 | 4920.39 | 5055.43 | 5195.4 I | 5340.77 | 5491.97 | 5649.56 | 5814.15 | 5986.44 | 7 |
| 8 | 4665.76 | 4792.06 | 4922.60 | 5057.72 | 5197.79 | 5343.24 | $5494 \cdot 5$ | 5652.24 | 5816.95 | 5989.38 | 8 |
| 9 | 4667.83 | 4794.20 | 4924.81 | 5060.01 | 5200. 17 | 5345.7 | 5497. II | 5654.93 | 5819.76 | 5992.33 | 9 |
| Iо | 4669.91 | 4795.34 | 4927.03 | 5062.30 | 5202.55 | 5348. 18 | 5499. | 5657.61 | 5822.57 | 5995.27 | 0 |
| II | 467 I .98 | 4798.49 | 4929.24 | 5064.60 | 5204.93 | 5350.66 | 5502.27 | 5660.30 | 5825.39 | 5998.22 | 11 |
| 12 | 4674.06 | 4800.63 | 493 I. 46 | 5066.90 | 5207 -31 | 5353.14 | 5504.85 | 5663.00 | 5828.20 | 6001.17 | I2 |
| 13 | 4676.13 | 4802.77 | 4933.68 | 5069. 19 | 5209.70 | 5355.6I | 5507.43 | 5665.69 | 5831.02 | $6004 \cdot 13$ | 13 |
| 14 | 4678.2 I | 4804.92 | 4935.90 | 5071.49 | 5212.08 | 5358.09 | 5510.01 | 5668.38 | 5833.84 | 6007.08 | 14 |
| 15 | 4680.29 | 4807.07 | 4938.12 | 5073.80 | 5214.47 | 5360.58 | 5512.60 | 567.1.08 | 5836.66 | 6010.04 | 15 |
| 16 | 4682.37 | 4809.21 | 4940.34 | 5076.10 | 5216.85 | 5363.06 | 5515.18 | 5673.78 | 5839.48 | 6013.00 | 16 |
| 17 | 4684.45 | 4811.36 | 4942.57 | 5078.40 | 5219.25 | 5365.55 | 5517.77 | 5676.48 | 5842.31 | 6015.96 | 17 |
| 18 | 4686.53 | 4813.51 | 4944.79 | 5080.71 | 5221.64 | 5368.03 | 5520.36 | 5679.19 | 5845.13 | 6018.93 | 18 |
| 19 | 4688.6 I | 4815.67 | 4947.02 | 5083.0I | 5224.04 | 5370.52 | 5522.95 | 5681.89 | 5847.96 | 6021.90 | 19 |
| 20 | 4690.70 | 4817.82 | 4949.24 | 5085.32 | 5226.43 | 5373 | 5525. | 5684.60 | 5850.79 | 6024.87 | 20 |
| 2 I | 4692.78 | 4819.97 | 4951.47 | 5087.63 | 5228.83 | 5375.50 | 5528. 14 | 5687.31 | 5853.63 | 6027.84 | 21 |
| 22 | 4694.87 | 4822.13 | 4953.70 | 5089.94 | 5231.23 | 5378.00 | 5530.74 | 5690.02 | 5856.47 | 6030.8 I | 22 |
| 23 | 4696.96 | 4824.29 | 4955.94 | 5092.25 | 5233.63 | 5380.49 | 5533.34 | 5692.73 | 5859.31 | 6033.79 | 23 |
| 24 | 4699.05 | 4826.44 | 4958.17 | 5094.57 | 5236.03 | 5382.99 | 5535.94 | 5695.45 | 5862.15 | 6036.77 | 24 |
| 25 | 4701. 14 | 4828.60 | 4960.40 | 5096.88 | 5238.43 | 5385.49 | 5538.55 | 5698.17 | 5864.99 | 6039.75 | 25 |
| 26 | 4703.23 | 4830.76 | 4962.64 | 5099.20 | 5240.84 | 5387.99 | 5541.15 | 5700.89 | 5867.84 | 6042.74 | 26 |
| 27 | 4705.32 | 4832.93 | 4964.87 | 5101.52 | 5243.24 | 5390.49 | 5543.76 | 5703.61 | 5870.69 | 6045.73 | 27 |
| 28 | 4707.4 I | 4835.09 | 4967.11 | 5103.84 | 5245.65 | 5392.99 | 5546.37 | 5706.33 | 5873.54 | 6048.72 | 28 |
| 29 | 4709.51 | 4837.25 | 4969.35 | 5106. 16 | 5248.06 | 5395.50 | 5548.98 | 5709.06 | 5877.39 | 6051.71 | 29 |
| 30 |  | 4839.42 | 4971. 59 | 5108.48 | 5250.47 |  | 5551.5 | 574 I. | 5879.24 | 6054.70 | 30 |
| 31 | 4 | 484 I .58 | 4973.83 | 5110.80 | 5252.88 | 5400.52 | 5554.20 | 5714.51 | 5882.10 | 6057.70 | 31 |
| 32 | 4715.7 | 4843.75 | 4976.08 | 5113.13 | 5255.30 | 5403.03 | 5556.82 | 5717.25 | 5884.96 | 6060.70 | 32 |
| 33 | 4717.89 | 4845.92 | 4978.32 | 5115.45 | 5257.71 | 5405.54 | 5559.44 | 5719.98 | 5887.82 5800.68 | 6063.7 I | 33 |
| 34 | 4719.99 | 4848.09 | 4980.57 | ${ }_{\text {5117. }}^{5117}$ | 5260.13 5262.55 | 5408.05 | 5562.06 5564.68 | 5722.71 5725.45 | 5890.68 5893.55 | 6066.71 6069.71 | 34 35 |
| 35 | 4722.09 | 4850.26 | 4982.82 18. | 5120.11 | 5262.55 | 5410.57 |  | 5725.45 5728.19 | 5893.55 5806.41 | 6069.71 6072.72 | 35 |
| 36 | 4724. 19 | 4852.43 | 4985.06 | 5122.44 | $5264.97$ | 5413.08 | $\begin{aligned} & 5567.30 \\ & 5569.93 \end{aligned}$ | 5728.19 5730.93 | 5896.41 5899.28 |  | 36 |
| 37 | 4726.30 | 4854.61 | 4987.3 l 4989.56 | 5124.77 5127.II | $\left\|\begin{array}{l} 5267.39 \\ 5260.8 \mathrm{I} \end{array}\right\|$ | 5415.60 5418.12 | 5569.93 5572.55 | 5730.93 5733.68 | 5899.28 5902.15 | 6075.73 6078.75 | 37 38 |
| 39 | 4730.51 | 4858.96 | 4991.82 | 5129.44 | 5272.23 | 5420.64 | 5575.18 | 5736.42 | 5905.03 | 608 I .76 | 39 |
| 40 |  | 4861.13 | 4994.07 | 9131.78 | 5274.66 | 5423.17 | 5577.81 | 5739.17 | 5907.90 | 6084.78 | 40 |
| 41 |  | 4863.31 | 4996.32 | 5134.11 | 5277.09 | 5425.69 | 5580.44 | 5741.92 | 5910.78 | 6087.81 | 41 |
| 42 | 4736.83 | 4865.49 | 4998.58 | 5136.45 | 5279.52 | 5428.22 | 5583.08 | 5744.67 | 5913.67 | 6090.83 | 42 |
| 43 | 4738.94 | 4867.67 | 5000.84 | 51138.79 | 5281.95 | 5430.75 | 5585.71 | 5747.43 | 5916.55 5919 |  | 43 |
| 44 | 4741.05 | 4869.86 | 5003.10 | 5141.14 | 5284.38 | 5433.28 | 5588.35 5590.99 | 5750.18 5752.94 | $\begin{array}{\|l\|} 5919.44 \\ 5922.32 \end{array}$ | 6096.89 6099.92 | 44 |
| 45 | 4743.16 | 4872.04 | $5005 \cdot 36$ | 5143.48 | 5286.82 | 5435.8I | 5590.99 | 5752.94 | 5922.32 5025.22 | 6099.92 6102.95 | 45 |
| 46 | 4745.28 <br> 4747 | 4874.22 4876.41 | 5007.62 5009.88 | $\begin{aligned} & 5145.83 \\ & 5148.17 \end{aligned}$ | 5289.25 5291.69 | 5438.35 5440.88 | 5503.64 5596.28 |  | 5925.22 5928.11 | 6102.95 6105.99 | 46 |
| 47 48 | 4747.39 4749.51 | 4876.41 l | 5009.88 5012.15 | 5148.17 5150.52 | 5291.69 5294.13 | 5440.88 5443.42 | 5590.28 5598.93 | 5758.46 576 I .23 | 5928.11 | 6105.99 6109.03 | 48 |
| 49 | 4751.63 | 4880.79 | 5014.4 I | 5152.87 | 5296.57 | 5445.96 | 5601.57 | 5763.99 | 5933.90 | 6112.07 | 49 |
| 50 | 4753.74 | 4882.98 | 5016.68 | 5155.22 | 5299.01 | 5448.50 | 5604.22 | 5766.76 | 5936.80 | 6115.12 | 50 |
| 51 | 4755.86 | 4885.17 | 5018.94 | 5157.57 | 5301.45 | 5451.05 | 5606.87 | 5769.53 | 5939.70 | 6118.16 | 51 |
| 52 | 4757.98 | 4887.36 | 5021.21 | 5159.93 | 5303.90 | 5453.59 | 5609.53 | 5772.31 | 5942.61 | 6121.21 | 52 |
| 53 | 4760 . IO | 4889.55 | 5023.48 | 5162.28 | 5306.34 | 5456. I4 | 5612.18 | 5775.08 | 5945.51 | 6124.26 | 53 |
| 54 | 4762.23 | 4891.75 | 5025.76 | 5164.64 | 5308.79 | 5458.68 | 5614.84 | 5777 | 5948.42 | $6127 \cdot 32$ 6130.38 | 54 |
| 55 | 4764.35 | 4893.94 | 5028.03 | 5167.00 | 53II. 24 | 5461 I .23 | 5617.50 | 5783.4 | 5951 | 6130.38 | 55 |
| 56 | 4766.47 | 4896.14 | 5030.30 | 5169.36 | 5313.69 | 5463.78 | 5620.16 | 5783.42 | 5954.24 5957 59 | 6133.44 6136.50 | 56 |
| 57 | 4768.60 | 4898.34 | 5032.58 | 5171.72 | 5316.15 5318.60 | 5466.34 | 5622.82 5625.49 | 5786.20 5788.08 | $\left\|\begin{array}{l} 5957.16 \\ 5050.08 \end{array}\right\|$ | 6136.50 6139.56 | 57 |
|  | 4770.73 4772.86 | 4900.54 4902.74 | 5034.86 5037.14 | (174.08 | 5318.60 532 I .06 | 5468.89 5471.45 | 5625.49 5628.15 | 5788.98 5791.77 | $\begin{aligned} & 5950.08 \\ & 5963.00 \end{aligned}$ | 6139.56 6142.63 615 | 59 |
| 60 | 4774.98 | 4904.94 | 5039.42 | 5178.81 | 5323.51 | 5474.0I | 5630.82 | 5794.56 | 5965.92 | 6145.7 | 60 |

The Anti-Gudermannian.

| gd u |  |  |  |  | $75^{\circ}$ | \% | 77 | 78 | 79 | 80 | ad |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| o' | 6145'.70 | 6334 | $\overline{6534 \cdot 42}$ | 6745.74 | $\overline{6970.34}$ | 721 | 7467.21 | 7744.57 | 8045.71 | 8375.20 | O' |
| 1 | 6148 | 6338.08 | 6537.85 |  |  |  | 7471.66 | 7749.38 | 8050.95 |  |  |
| 2 | 6151 | 6341.32 | 6541.27 |  |  | 7218.35 | 7476. II | 7754.20 | 8056.20 | 8386.73 | 2 |
| 3 |  |  |  |  |  | 7222.49 | 7480.57 | 7759.02 |  | 8392.52 | 3 |
| 4 |  |  |  |  |  |  |  | 7763.86 |  | 8398.31 |  |
| 5 |  |  | 655 I .57 |  | 6989.71 | 723 |  |  |  | 8404.11 |  |
| 6 | 6164.18 | 635 | 6555.0I | 6767.58 | 6993.60 |  |  | 7773.55 |  |  | 6 |
| 7 | 6167.27 | 6357 | 6558.45 | 6771.23 | 6997.49 |  |  | 7778.40 |  |  | 7 |
| 8 | 6170.36 | 6360.8 | 6561. 89 | 6774.89 | 7001 | 724 |  | 7783.26 | 8087.88 |  |  |
| 9 | 6173.45 | 6364.08 | 6565.34 |  | 7005.28 | 7247 | 7507 | 7788.12 | 8093 . 19 |  | 9 |
| 10 | 6176 | 6367.35 | 6568.79 |  | 7009.19 | 7251 | 751 | 7793.00 |  |  | ıo |
| II |  | 6370 | 6572.25 | 6785.88 |  | 7255.83 | 751 |  | 8103.83 |  |  |
| 12 | 6182.75 | 6373 | 6575.70 | 6789.55 | 7017.01 | 7260.02 | 7520. |  | 8109.17 |  | 12 |
| 13 |  | 63 | 6579.16 | 6793.22 |  | 7264.2 | 7525.47 |  | 8IIT4.5I |  | 13 |
| 14 | 6188.96 |  | 658 | 6796 |  | ,7268. |  |  | 8i19.86 |  | 14 |
| 15 | 6192.07 | 63 |  |  |  |  |  |  | 8125.22 |  | 15 |
| 16 | 6195.18 | 6386.99 | 6589.57 | 6804.27 |  | 7276.83 |  | 7822.38 | 8130.58 | 8468.58 | 16 |
| 17 | 6198.30 | 6390.28 | 6593.05 | 6807.96 | 7036 | 7281 |  | 7827.30 | 8135.95 | 8474.50 | 17 |
| 18 | 6201.42 | 6393.57 | 6596.52 | 681ı. 65 | 7040 | 7285 | 754 | 7832.23 | 8141.33 |  | 18 |
| 19 | 6204.5 | 6396.86 | 6600.01 | 6815.35 | 7044.52 | 7289 | 75.52. | 7837.16 | 8146.72 | 8486.37 | 19 |
| 20 | 6207.66 | 6400.15 | 6603.49 | 6819.05 | 7048.47 | 7293 | 7557 | 7842.10 | 8152.12 | 8492.32 |  |
| 21 | 6210. | 6403 | 6606.98 |  | 705 | 729 | 7561 |  |  |  | 21 |
| 22 | 6213.91 | 6406 | 6610.47 |  | 7056.37 | 7302. | 7566.39 |  |  | 8504.25 | 22 |
| 23 | 6217 | 6410.05 | 6613.96 | 68 | 7060.33 | 7306. | 7570.96 | 7 | 81 | 8510.23 | 23 |
| 24 | 6220 | 6413 | 6617 | 68 |  | 7310. | 7575. | 7861. 94 | 8173.80 | 8516.22 | 24 |
| 25 | 62 |  | 6620.97 |  |  | 7314. | 7580.13 | 7866.91 | 8i7 | 8522.22 | 25 |
| 26 | 6226. | 64 | 6624.47 | 6841.34 |  | 7319.21 | 7584 | 7871.90 | 8184.69 | 8528.23 | 26 |
| 27 | 6229 | 6423.29 | 6627.98 | 6845.07 |  | 732 | 7589 | 7876.89 | 8190.15 | 8534.26 | 27 |
| 28 | 6232.74 | 6426.6I | 6631.49 | 6848.80 | 7080 | 732 | 7593 | 7881. 89 | 8195.61 | 8540.29 | 28 |
| 29 | 6235.89 | 6429.93 | 6635.01 | 6852.53 | 7084.19 | 733 | 7598.5 | 7886.89 | 8201.09 |  | 29 |
| 30 | 6239.04 | 6433.25 | 6638.53 | 6856.27 | 7088.18 | 733 | 7603. | 7891.91 | 8206.57 | 8552.38 | 30 |
| 3 I | 6242 | 6436.58 | 66 | 6860 | 709 | 734 | 7607.78 | 7896.93 | 8212.06 |  | 31 |
| 32 | 6245 | 6439.91 | 6645.58 | 6863.77 | 7096 | 7344.8 | 7612.41 | 7901.95 | 8217.56 |  | 32 |
| 33 |  | 6443 |  | 6867.52 | 7100 | 7349.18 | 7617. | 7906.98 | 8223.07 |  | 33 |
| 34 |  |  |  | 6871.27 | 7104 | 7353.48 |  | 7912.03 | 8228.59 |  |  |
| 35 | 62 |  |  | 6875.03 |  | 7357.79 | 7626.33 | 7017 | 8234 |  | 35 |
| 36 | 6258.0 | 6453.26 | 6659.72 | 6878.80 | 7112.23 |  |  | 7922.13 | 8239.66 |  | 36 |
|  | 6261 | 6456.61 | 6663.26 | 6882.56 | 71 | 7366 | 7635 | 7927.19 | 8245.20 | 8595.06 |  |
| 38 | 6264 | 6459.95 | 6666.8I | 6886.34 | 7120 | 7370 | 7640.3 | 7932.26 | 8250.75 | 8601. 20 | 38 |
| 39 | 6267.5I | 6463.3 I | 6670.36 | 6890. 11 | 7124.31 | 7375 | 764 | 7937.34 |  |  | 39 |
| 40 | 6270.69 | 6466.66 | 6673.91 | 6893.89 | 7128.35 | 7379 | 7649 | 7942.43 | 826 | 86I3.51 | 40 |
| 41 | 6273.87 |  |  | 6897.68 | 7132.39 |  | 7654.35 |  | 8267.46 |  | 4 |
| 42 | 6277.05 | 6473.38 | 668 | 6901.4 | 7136.43 | 7388.08 | 7659.04 | 7952. |  |  | 42 |
| 43 | 628 |  | 6684.59 | 6905.25 | 7140.48 | 7392.43 | 7663.74 | 7957 |  |  | 43 |
| 44 | 628 | 6480. II | 6688.16 | 6909 |  | 7396.79 | 7668. | 仡 | 8284 |  | 44 |
| 45 |  | 6483. | 6691. 73 | 6912.85 | 71 | 74 | 7673.15 |  | 8289 | 8644.47 | 45 |
| 46 | 6289.82 | 6486.86 | 6695.31 | 6916.65 | 7152.67 |  | 7677.87 |  | 8295.49 |  | 46 |
| 47 | 6293.01 | 6490.23 | 6698.89 | 6920.46 | 7156.74 | 7409.8 | 7682.59 | 7978.23 | 8301.12 | 8656.94 | 47 |
| 48 | 6296.21 | 6493.6I | 6702.47 | 6924.27 | 7160.81 | 7414.26 | 7687.32 | 7983.37 | 8306.77 | 8663.19 | 48 |
| 49 | 6299.42 | 6497.00 | 6706.06 | 6928.09 | 7164.89 | 7418.64 | 7692.05 | 7988.52 | 8312.42 | 8669.45 | 49 |
| 50 | 6302 | 6500.38 | 6709.65 | 693 | 716 | 7423.03 | 7696.79 | 7993.6 | 831 | 8675.72 | 50 |
| 51 | 6305.83 | 6503 | 6713.24 | 6935.7 | 7173.06 | 7427 | 770 | 7998.85 | 8323.75 |  | 51 |
| 52 | 6309 | 6507.17 | 6716.84 | 6939.56 | 7177. | 7431.8 | 7706 | 8004.03 | 8329. |  | 52 |
| 53 | 6312.26 | 6510.56 | 6720.44 | 6943.40 | 7181. | 7436 | 771 | 8009.21 | 8335.12 |  | 5 |
| 54 | 6315.48 | 6513.96 | 6724.04 | 6947.23 | 7185.35 |  |  | 8014.4 | 8340.82 |  | 54 |
| 55 | 6318.70 | 6517.36 | 6727.65 | 6951.07 | 7189 |  |  | 8019.60 | 8346.52 | 8707.25 | 55 |
| 56 | 6321.92 | 6520.77 |  | 6954.92 | 7193.57 | 7449.4 | 7725.38 | 8024.8I | 8352.24 | 8713.59 | 56 |
|  | 6325.14 | 6524. 18 | 6734.88 | 6958 | 7197.69 | 7453.8 | 7730.17 | 8030.02 | 8357.96 | 8719.94 | 57 |
|  | 632 | 6527.59 | 6738.50 | 6962.62 | 7201.8 I | 7458.33 | 7734.96 | 8035.24 | 8363.70 | 8726.30 | 88 |
|  | 633 | 6531. | 6742.12 | 6966.48 | 7205.9 | 7462.76 | 7739.76 | 8040.47 | 8369.44 | 8732.68 | 59 |
| 60 | 6 | 6534.42 | 6745 | 69 | 7210.07 | 767 |  | 8045.71 | 8375.20 | 8739. |  |

The Anti-Gudermannian.

| gd u | $81^{\circ}$ | $82^{\circ}$ | $83^{\circ}$ | $84^{\circ}$ | $85^{\circ}$ | $86^{\circ}$ | $87^{\circ}$ | $88^{\circ}$ | $89^{\circ}$ | gd u |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O | 8739.06 | 9145.46 | 9605.82 | TOI36.89 | 10764.62 | 11532.52 | I2522.11 | I3916.43 | I6299.56 | $\mathrm{O}^{\prime}$ |
| 1 | 8745.46 | 9152.65 | 9614.03 | 10146.46 | 10776. 11 | 11546.88 | 12541.27 | 13945.20 | 16357.34 |  |
| 2 | 8751.87 | 9159.86 | 9622.27 | 10156.07 | 10787.65 | I1561.3I | 12560. 54 | I 3974.22 | 16416.11 | 2 |
| 3 | 8758.29 | 9167.08 | 9630.52 | 10165.70 | 10799. 22 | 11575.80 | 12579.91 | 14003.48 | 16475.90 | 3 |
| 4 | 8764.73 | 9174.32 | 9638.80 | IOI75.37 | 10810.82 | II 590.34 | I2599.40 | I4033.00 | 16536.76 | 4 |
| 5 | 8771.17 | 9181.57 | 9647.09 | IOI85.05 | 10822.47 | 11604.95 | 12619.00 | I4062.77 | 16598.69 | 5 |
| 6 | 8777.63 | 9188.84 | 9655.40 | 10194.77 | 10834.16 | 11619.62 | I2638.70 | I4092.80 | 16661.78 | 6 |
| 7 | 8784.10 | 9196. 13 | 9663.74 | 10204.51 | 10845.89 | 11634.36 | 12658.53 | I4123.09 | I6726.04 | 7 |
| 8 | 8790.58 | 9203.42 | 9672.09 | 10214.28 | 10857.65 | 11649. 16 | 12678.46 | 14153.66 | 16791. 53 | 8 |
| 10 | 8797.08 | 9210.74 | 9680.47 | 10224.08 | 10869.46 | 11664.02 | I2698. 52 | 14184.49 | 16858.29 | 9 |
| 10 | 8803.58 | 9218.07 | 9688.86 | 10233.90 | 1088ı.3I | 11678.94 | 12718.69 | I4215.61 | 16926.36 | Io |
| II | 8810.10 | 9225.41 | 9697.28 | 10243.75 | 10893.20 | 11693.93 | I2738.98 | I4247.01 | I6995.81 | II |
| 12 | 8816.63 | 9232.77 | 9705.71 | 10253.64 | 10905. 13 | I1708.99 | 12759.39 | 14278.70 | 17066.70 | 12 |
| 13 | 8823.17 | 9240.15 | 9714.17 | 10263.54 | 10917.10 | II724.11 | 12779.92 | 14310.68 | 17139.09 | I3 |
| 14 | 8829.73 | 9247.54 | 9722.64 | 10273.48 | 10929 | 11739 | 12800.58 | 14342.97 | 17213.03 | 14 |
| 15 | 8836.30 | 9254.95 | 9731.14 | I0283.45 | 10941. 17 | 11754.56 | 12821. 36 | 14375.56 | I7288.57 | 15 |
| 16 | 8842.88 | 9262.37 | 9739.66 | 10293.45 | 10953.26 | 11769.88 | 12842.26 | 14408.46 | 17365.83 | 16 |
| 17 | 8849.47 | 9269.81 | 9748.20 | 10303.47 | 10965.40 | 11785.27 | 12863.30 | I4441.68 | 17444.87 | 17 |
| 18 | 8856.07 | 9277.27 | 9756.76 | 10313.53 | 10977.59 | 11800.73 | I2884.46 | 14475.23 | I7525.77 | 18 |
| 19 | 8862.69 | 9284.74 | 9765.34 | 10323.61 | 10989.81 | 11816.26 | 12905.75 | 14509. 10 | 17608.63 | 19 |
| 20 | 8869.32 | 9292.23 | 9773.94 | 10333.72 | 11002.08 | 11831.87 | 12927.18 | 14543.31 | I7693.49 | 20 |
| 2 I | 8875 | 9299.73 | 9782.57 | 10343.85 |  | 11847.54 | 12948.74 | 14577.87 | 17780.53 | 21 |
| 22 | 8882.62 | 9307.25 | 9791.21 | 10354.03 | 11026.75 | 11863.28 | 12970.44 | 14612.78 | 17869.83 | 22 |
| 23 | 8889.29 | 9314.79 | 9799.88 | 10364.24 | 11039.15 | 11879. 10 | 12992.27 | I4648.04 | 17961.5I | 23 |
| 24 | 8895.97 | 9322.34 | 9808.57 | 10374.47 | 11051.60 | 11894.99 | 13014.25 | 14683.67 | I8055.70 | 24 |
| 25 | 8902.66 | 9329.91 | 9817.28 | 10384.73 | I 1064.09 | 11910.95 | I3036.36 | 14719.67 | 18152.55 | 25 |
| 26 | 8009.37 | 9337 | 9826.02 | 10395.03 | 1 1076.63 | 11926.99 | I3058.62 | 14756.05 | I8252.20 | 26 |
| 27 | 8916.09 | 9345 | 9834.77 | 10405.35 | 11089.21 | 11943.10 | I3081. 02 | 14792.83 | 18354.83 | 27 |
| 28 | 8922.82 | 9352.72 | 9843.55 | 10415.71 | IIIII. 84 | 11959.29 | I3103. 58 | I4830.00 | I8460.62 | 28 |
| 29 | 8929.57 | 9360.35 | 9852.35 | 10426.09 | IIII4.52 | 11975.55 | I3126.27 | 14867.57 | 18569.76 | 29 |
| 30 | 8936.33 | 93 | 9861. 17 | 10436.51* | III27.24 | 11991.89 | I3149.12 | I4905.56 | 18682.49 | 30 |
| 3 I | 8943.10 | 9375.67 | 9870.02 | 10446.96 | III40.01 | 12008.3 I | 13172.13 | I4943.98 | 18799.03 | 31 |
| 32 | 8949.88 | 9383.36 | 9878.88 | $10457 \cdot 44$ | 11152.82 | 12024.81 | 13195.28 | 14982.83 | I8919.67 | 32 |
| 33 | 8956.68 | 9391.06 | 9887.77 | 10467.95 | I 1165.69 | 12041.39 | I 3218.60 | 15022.12 | 19044.69 | 33 |
| 34 | 8963.49 | 9398.79 | 9896.69 | 10478.50 | 11178.60 | 12058.05 | I3242.07 | 15061.87 | 19174.44 | 34 |
| 35 | 8970.32 | 9406.53 | 99 | 10 | III91. 56 | 12074.79 | I3265.70 | 151 | 19309.27 | 35 |
| 36 | 8977.16 | 9414.28 | 9914.59 | 10499.69 | II204.57 | 12091.60 | I3289.50 | 15142.77 | I9449.6I | 36 |
| 37 | 8884.01 | 9422.05 | 9923.57 | 10510.33 | 11217.63 | 12108.51 | 13313.47 | 15183.94 | 19595.92 | 37 |
|  | 8990.87 | 9429.84 | 9932.57 | 10521.01 | 11230.74 | 12125.49 | 13337.60 | 15225.62 | 19748.73 | 38 |
| 39 | 8997.75 | 9437.65 | 9941.60 | 10531.71 | 11243.90 | 12142.57 | 13361.90 | 15267.80 | 19908.66 | 39 |
| 40 | 9004 | 9445.48 |  | 10542.45 | I 1257. II | 12159.72 | I3386.37 | 15310.51 | 20076. | 40 |
| 4 I | 9011.55 | 9453.32 | 9959.73 | 10553.23 | 11270.37 | 12176.96 | I3411. 02 | 15353.76 | 20252.72 | 4 |
| 42 | 9018.47 | 9461.18 | 9968.83 | 10564.04 | 11283.68 | 12194.29 | I3435.85 | 15397.56 | 20438.59 | 42 |
| 43 | 9025.41 | 9469.06 | 9977.96 | 10574.88 | II 297.04 | 12211.71 | I 3460.85 | 15441.92 | 20635.09 | 43 |
| 44 | 9032.36 | 9476.96 | 9987. II | 10585.76 | I1310.46 | 12229.21 | 13485.05 | 15486.86 | 20843.50 | 44 |
| 45 | 9039.32 | 9484.87 | 9996.28 | 10596.67 | II 323.93 | 12246.8I | I3511.43 | 15532.40 | $21065 \cdot 37$ | 45 |
| 46 | 9046.29 | 9492.8 i | 10005.48 | 10607.62 | 11337.45 | 12264.49 | 13537.00 | 15578.55 | 21302.55 | 46 |
| 47 | 9053.28 | 9500.76 | 10014.70 | 10618.60 | 11351.02 | I2282.26 | 13562.75 | 15625.32 | $21557 \cdot 31$ | 47 |
| 48 | 9060.29 | 9508.73 | 10023.95 | 10629.61 | II 364.65 | 12300.13 | 13588.71 | 15672.75 | 21832.48 | 48 |
| 49 | 9067.31 | 9516.71 | 10033.22 | 10640.67 | 11378.33 | 12318.09 | I3614.85 | 15720.83 | 22131.60 | 49 |
| 50 | $9074 \cdot 34$ | 9524.72 | 10042.52 | 10651.75 | I 1392.06 | 12336.15 | I3641.20 | 15769.59 | 22459.26 | 50 |
| 51 | 908 I .39 | 9532.74 | 10051. 84 | 10662.87 | I 1405.85 | 12354.30 | 13667.75 | 15819.06 | 22821.46 | 51 |
| 52 | 9088.45 | 9540.79 | 10061.19 | 10674.03 | II419.70 | 12372.54 | 13694.52 | 15869.25 | $23226.39-$ | 52 |
| 53 | 9095.52 | 9548.85 | 10070. 56 | 10685.22 | II433.60 | 12390.89 | I3721.48 | I5920. 19 | 23685.42 | 53 |
| 54 | 9102.61 | 9556.93 | 10079.96 | 10696.46 | II 447.56 | 12409.33 | 13748.67 | 15971.89 | $24215 \cdot 35$ | 54 |
| 55 | 9109.72 | 9565.03 | 10089. 38 | 10707.72 | II461.58 | 12427.87 | 13776.07 | 16024.38 | 24842.12 | 55 |
| 56 | 9116.84 | 9573.15 | Io098.83 | 10719.03 | II 1475.65 | 12446.51 | I3803.68 | I6077.68 | 25609.23 | 56 |
| 57 | 9123.97 | 958i. 29 | 10108.30 | 10730.37 | II489.78 | 12465.26 | 13831.53 | 16131.82 | 26598.21 | 57 |
| 58 | 9131.12 | 9589.45 | IOII7.81 | 10741.75 | I 1503.97 | 12484.10 | 13859.60 | 16186.83 | 27992. IO | 58 |
| 59 | 9138.28 | 9597.62 | IoI27.33 | 10753.17 | 11518.21 | 12503.05 | 13887.90 | 16212.74 | 30374.96 | 59 |
| 60 | 9145.46 | 9605.82 | IOI36.89 | I0764.62 | I 1532.52 | 12522.11 | I3916 | I6299. |  | 60 |

## TABLE VIII

## CONVERSION OF RADIANS INTO ANGULAR MEASURE AND VICE VERSA

Conversion of Angular Measure into Radians.

| $n$ | Radians for n degrees | Radians for n minutes | Radians for $\boldsymbol{n}$ seconds | n | Radians for n degrees |
| :---: | :---: | :---: | :---: | :---: | :---: |
| I | 0.01745329252 | 0.0002908882 I | 0.000004848 I 4 | 6I | 1.06465084372 |
| 2 | . 03490658504 | . 00058177642 | . 00000969627 | 62 | .08210 41362 4 |
| 3 | .05235987756 | .00087266463 | .00001 45444 I | 63 | .09955742876 |
| 4 | .0698I 3I700 8 | .00116 355283 | .00001 939255 | 64 | .II7OI 07212 8 |
| 5 | 0.08726646260 | 0.00145444104 | 0.00002424068 | 65 | I. 13446401380 |
| 6 | . 10471 97551 2 | .00174 532925 | .00002908882 | 66 | .15191 730632 |
| 7 | .12217 304764 | . 00203621746 | .00003393696 | 67 | .16937059884 |
| 8 | . 13962634016 | .00232710567 | .00003878509 | 68 | . 18682389136 |
| 9 | . 15707963268 | .00261 799388 | . 00004363323 | 69 | . 20427718388 |
| 10 | 0.17453292520 | 0.00290888209 | 0.00004848137 | 70 | 1.22173047640 |
| 11 | . 19198 62177 2 | .00319 977030 | . 00005332950 | 71 | . 23918376892 |
| 12 | . 20943951024 | . 00349065850 | . 00005 8I776 | 72 | . 25663 706I4 4 |
| 13 | .22689280276 | .0037815467 I | . 00006302578 | 73 | .27409035396 |
| 14 | . 24434609528 | . 00407243492 | . 00006787392 | 74 | . 29154364648 |
| 15 | 0.26179938780 | 0.00436332313 | 0.00007272205 | 75 | I. 3089969390 o |
| 16 | . 27925268032 | . 0046542 II 34 | .00007757019 | 76 | . 32645 023I5 2 |
| 17 | . 29670597284 | . 00494509955 | . 00008241833 | 77 | . 34390352404 |
| 18 | .3I4I5 926536 | . 00523598776 | . 00008726646 | 78 | .36135 68165 6 |
| 19 | -33161 255788 | . 00552687596 | . 00009211460 | 79 | .3788I Oiogo 8 |
| 20 | 0.34906585040 | 0.00581776417 | 0.00009696274 | 80 | 1. 39626340160 |
| 21 | .36651 91429 2 | .00610 865238 | .00010 181087 | 8 I | .4I37I 6694I 2 |
| 22 | . 38397243544 | .00639954059 | .000I0 66590 I | 82 | .43116 998664 |
| 23 | .40142572796 | . 00669042880 | .00011 I5071 5 | 83 | . 44862327916 |
| 24 | .41887902048 | . 00698 I3I70 I | .000II 635528 | 84 | . 46607657168 |
| 25 | 0.43633231300 | 0.00727220522 | 0.000121203 | 85 | I. 48352986420 |
| 26 | . 45378560552 | .00756309343 | .00012 605156 | 86 | . 50098 31567 2 |
| 27 | . 47123889804 | .00785 39816 3 | .00013 089969 | 87 | .51843 64492 4 |
| 28 | .48869219056 | .008I4 486984 | .00013 574783 | 88 | . 53588974176 |
| 29 | . 50614548308 | . 00843575805 | .00014 059597 | 89 | . 55334303427 |
| 30 | 0.52359877560 | 0.00872664626 | 0.0001454441 | 90 | I. 57079632679 |
| 3 I | . 54105 2068I 2 | .00901 753447 | .00015 02922 | 9 I | .5882496193 I |
| 32 | . 55850536064 | . 00930842268 | . 00015514038 | 92 | . 60570 29II8 3 |
| 33 | . 57595865316 | . 00959931089 | . 0001599885 I | 93 | .62315620435 |
| 34 | .5934I 19456 8 | .00989 01990 9 | .00016 48366 5 | 94 | .64060946687 |
| 35 | 0.61086523820 | 0.0101810873 .0 | 0.00016968479 | , | 1.65806278939 |
| 36 | . 62831853072 | . 0104719755 I | .00017 453293 | 96 | .67551 60819 I |
| 37 | . 64577182324 | . 01076286372 | .00017 93810 | 97 | . 69296937443 |
| 38 | .66322511576 | . 01105375193 | . 00018422920 | 98 | . 71042266695 |
| 39 | .68067840828 | .OII34 46401 4 | .00018 907734 | 99 | . 72787595947 |
| 40 | 0.69813 I7008 0 | O.OII63 552835 | 0.00019392547 | 100 | 1.7453292519 9 |
| 4 I | . 71558499332 | .OI192 641656 | .0001987736 I | 110 | .91986 21771 9 |
| 42 | . 73303828584 | .0122I 730476 | .00020362175 | 120 | 2.09439510239 |
| 43 | .75049 I5783 6 | . OI250 8ig29 7 | . 00020846988 | 130 | . 26892802759 |
| 44 | . 76794487088 | . 01279 908ıI 8 | .00021 33I80 2 | 140 | . 44346095279 |
| 45 | 0.78539 81634 0 | 0.01308996939 | 0.00021816616 | 150 | 2.61799387799 |
| 46 | . 80285145592 | . O1338 085760 | . 00022301429 | 160 | . 79252680319 |
| 47 | . 82030474844 | . OI367 I7458 I | . 00022786243 | 170 | . 96705972839 |
| 48 | .83775804096 | . O1396 263402 | .00023 271057 | 180 | 3.14159 265359 |
| 49 | . 8552 I I 33348 | . OI425 35222 | .00023755870 | 190 | -31612 557879 |
| 50 | 0.87266462000 | 0.01454441043 | 0.00024240684 | 200 | $3 \cdot 49065850399$ |
| 5 I | .89011 791852 | .OI483 529864 | .00024725498 | 210 | . 66519 I4291 9 |
| 52 | .90757 I2IIO 4 | . 01512618685 | . 0002521031 I | 220 | .83972435439 |
| 53 | .92502450356 | .OI541 707506 | . 00025695125 | 230 | 4.01425727959 |
| 5 | . 94247779608 | . 01570796327 | . 00026 17993 9 | 240 | . 18879020479 |
| 55 | 0.95993 I0886 0 | 0.01599885148 | 0.00026664752 | 250 | 4.36332312999 |
| 56 | . 97738438112 | . 01628973969 | .00027149566 | 260 | . 53785605519 |
| 57 | .99483767364 | .01658062789 | .0002763438 o | 270 | . 71238898038 |
| 58 | I. 01229096616 | . 01687 I5161 0 | . 00028 II919 4 | 300 | $5 \cdot 23598775598$ |
| 59 | .02974425868 | .01716 24043 I | .00028604007 | 330 | . 75958653158 |
| 60 | 1.04719 75512 0 | 0.01745329252 | 0.0002908882 | 360 | 6.28318530718 |

Conversion of Radians into Angular Measure.

| Padians |  | Angle | Radians | Angle |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | - |  |  | - | " |
| O.I | 0543 | 46.4806247 | 0.006 | O 20 | 37.5888375 |
| 0.2 | II 27 | 32.9612494 | . 007 | 24 | 03.8536437 |
| 0.3 | 17 II | 19.4418741 | . 008 | 27 | 30. II84500 |
| 0.4 | 2255 | 05.9224988 | . 009 | 30 | 56.3832562 |
| 0.5 | $28 \quad 38$ | 52.4031235 | 0.0100 | O 34 | 22.6480625 |
| 0.6 | $34 \quad 22$ | 38.8837483 | . 0001 | 00 | 20.6264806 |
| 0.7 | $40 \quad 06$ | 25.3643730 | . 0002 | 00 | 41.2529612 |
| 0.8 | 4550 | II. 8449977 | . 0003 | OI | OI. 87944 I9 |
| 0.9 | 5133 | 58.3256224 | . 0004 | OI | 22.5059225 |
| 1.00 | 57 I7 | 44.8062471 | 0.0005 | O OI | 43.1324031 |
| 0.01 | 0034 | 22.6480625 | . 0006 | 02 | 03.7588837 |
| 0.02 | OI 08 | 45.2961249 | . 0007 | 02 | 24.3853644 |
| 0.03 | OI 43 | 07.9441874 | . 0008 | 02 | 45.0118450 |
| 0.04 | 02 I7 | 30.5922499 | . 0009 | 03 | 05.6383256 |
| 0.05 | 0251 | 53.2403124 | 0.00100 | $0 \quad 03$ | 26.26480625 |
| 0.06 | 0326 | I5.88837 48 | .0000I | 00 | 02.05264806 |
| 0.07 | 0400 | 38.5364373 | . 00002 | 00 | 04.125 .29612 |
| 0.08 | 0435 | OI. I8449 58 | . 00003 | 00 | 06.18794419 |
| 0.09 | 0509 | 23.8325622 | . 00004 | 00 | 08.25059225 |
| 0.100 | 0543 | 46.4806247 | 0.00005 | - 00 | 10.31324031 |
| 0.001 | 0003 | 26.2648062 | . 00006 | 00 | 12.37588837 |
| 0.002 | 0006 | 52.52961 25 | . 00007 | 00 | 14.43853644 |
| 0.003 | 00 IO | 18.79441 87 | . 00008 | 00 | 16.50118 450 |
| 0.004 | 00 I3 | 45.0592250 | . 00009 | 00 | 18.56383256 |
| 0.005 | 0017 | II.32403 I2 | 0.00010 | $0 \quad 00$ | 20.62548052 |

SMITHSONIAN TABLES

Numerical Constants.
$\log _{10} 2=0.301029995663981$
$\log _{e} 2=0.693147180559945$
$\log _{\mathrm{e}} \mathrm{IO}=2.302585092994046$
$e=2.71828 \times 828459045$
$\log _{10} \mathrm{e}=0.43429448 \mathrm{I} 903252$
$\log _{10} \log _{10} \mathrm{e}=9.637784311300537$
$\pi=3.141592653589793$
$\log _{10} \pi=0.497149872694134$
$\log _{\mathrm{e}} \pi=\mathrm{I} .144729885849400$
$\frac{I}{\pi}=0.31830$ 98861 83791
$\pi^{2}=9.869604401089359$
$\frac{\mathrm{I}}{\pi^{2}}=0$. IOI 32 II836 42338
$\sqrt{\boldsymbol{\pi}}=1.772453850905516$
$\frac{\mathrm{I}}{\sqrt{\pi}}=0.564189583547756$
$\log _{10} \frac{\mathrm{I}}{\sqrt{\pi}}=9.751425063652933$
$\sqrt{\frac{\pi}{2}}=$ I.2533I 4I373 15500
$\sqrt{\frac{2}{\pi}}=0.797884560802865$
$\log _{10} \sqrt{\frac{2}{\pi}}=9.901940061484924$
I radian $=206264.8062470964$ seconds
$=3437.7467707849$ minutes
$=57.29577$ 95I3I degrees
$\log _{10} 206264.80625=5.3144251332$

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[^0]:    ${ }^{1}$ More compendious and convenient, but less usual, is the notation employed by B. de Saint-Venant, $\operatorname{sih} u$, $\operatorname{coh} u$, tah $u$.
    ${ }^{2}$ Comptes Rendus. Paris, vol. 83, 1876, p. 594.

[^1]:    ${ }^{1}$ H. P. Manning's Non-Euclidean Geometry, p. 60.

[^2]:    ${ }^{1}$ Taken with additions from Prof. B. O. Peirce s Short Table of Integrals, and Prof. McMahon's Hyperbolic Functions.

[^3]:    ${ }^{1}$ See Bull. Geol. Soc. Am., vol. 2, 1891, p. 49, and Am. Jour. Sci., vol. 46, 1893, p. 337 .

[^4]:    ${ }^{1}$ The isocyclic diameter used in this illustration of hyperbolic functions lies in the circular section of a shear ellipsoid, or an ellipsoid in which the mean axis is mean proportional between the greatest and least axes. The position of the circular section of the general ellipsoid is also readily expressed in terms of hyperbolic functions. Let the equation of the ellipsoid be

    $$
    \frac{x^{2}}{a^{2}}+\frac{y^{2}}{b^{2}}+\frac{z^{2}}{c^{2}}=\mathrm{I} ; a>b>c
    $$

    If $\frac{b}{c}=\cosh u_{1}$, and $\frac{a}{b}=\cosh u_{2}$,
    the angle $\nu$ which the circular section makes with the greatest axis is given by

    $$
    \tan \nu=\frac{\mathrm{I}}{i} \tanh i \nu=\frac{b-{ }^{2}-a-^{2}}{c^{-2}-b-2}=\frac{\tanh u_{1}}{\sinh u_{2}}
    $$

    If $u_{1}=u_{2}$ and $\frac{a}{b}=a$ this expression reduces to $\tan \nu=a^{-1}$, or to the case of the shear ellipsoid.

[^5]:    ${ }^{1}$ The notation and general outline of treatment here presented closely follow Mr. Herbert L. Rice's treatise, Theory and Practice of Interpolation, I899. The Nichols Press, Lynn, Massachusetts.

[^6]:    ${ }^{1}$ Rice's Theory and Practice of Interpolation, section 83 .
    ${ }^{2}$ Prof. James McMahon : "On the General Term in the Reversion of Series." Bull. Am. Math. Soc., April, 1894.

[^7]:    ${ }^{1}$ See, also, " Inverse Interpolation by Means of a Reversed Series," Phil. Mag., May, 1908.

[^8]:    ${ }^{1}$ James McMahon, Hyperbolic Functions, p. 71.
    ${ }^{2}$ Crelle's Journal, vols. $6,7,8$, and 9 . These memoirs were afterwards reprinted in a separate volume. xlviii

[^9]:    ${ }^{1}$ Phil. Mag., vol. 24, p. 19.
    ${ }^{2}$ Thus spelled in Cayley's paper.
    ${ }^{3}$ Exercises de Cal. Int., vol. 2, I8ı6.
    ${ }^{4}$ Neueste Schriften der Naturforscher-Gesellschaft in Danzig, vol. 6, 1862.

[^10]:    ${ }^{1}$ Cambridge Phil. Soc., Trans., vol. I3, IS83.

[^11]:    Washington, D. C., January, rgo8.

[^12]:    Smithsonian Tables

[^13]:    Smithsonian Tables

